

Introduction to Digital Systems

Part II (4 lectures)

2024/2025

Combinational Logic Blocks

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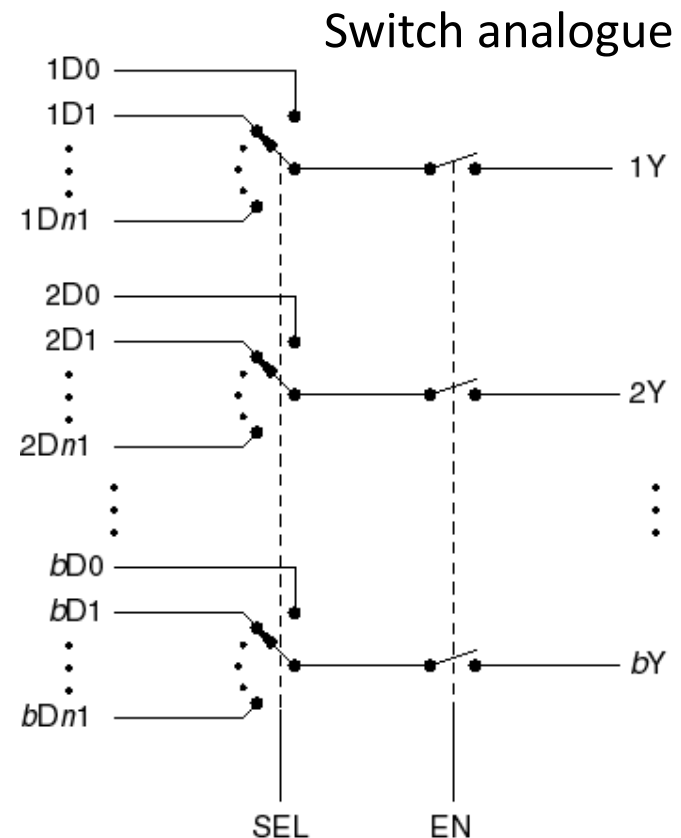
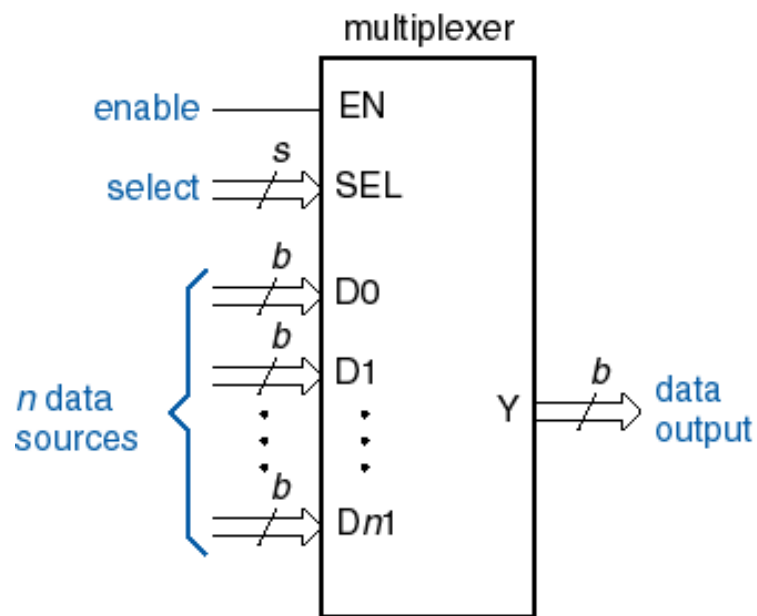
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Lecture 6 contents

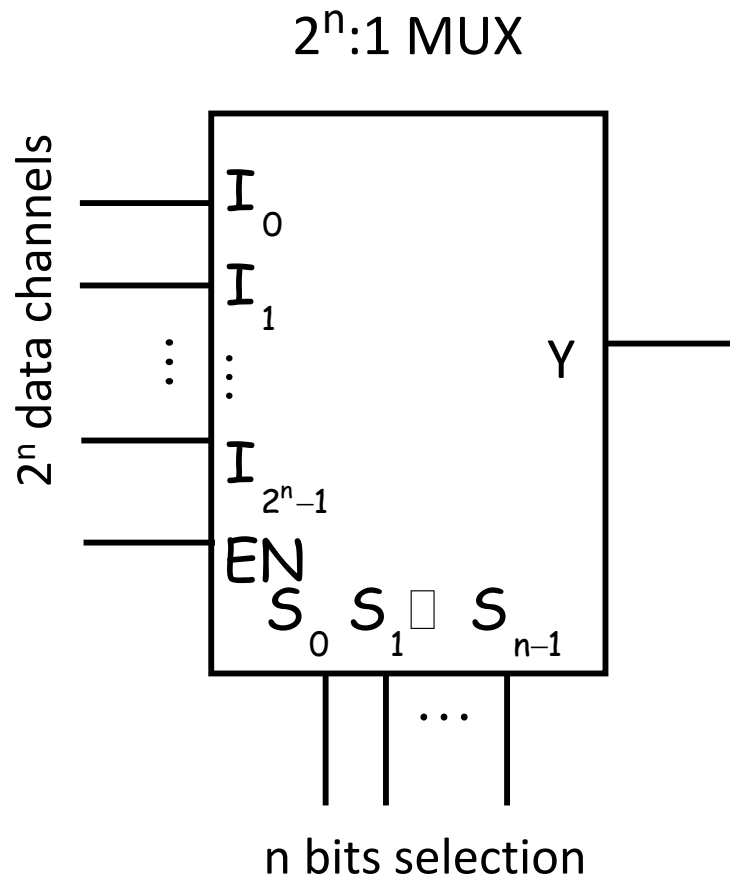
- Block oriented combinational logic design
- Multiplexers
- Demultiplexers

Multiplexers

- A multiplexer is a digital switch: one out of n data sources is passed to a single output
 - Information selector



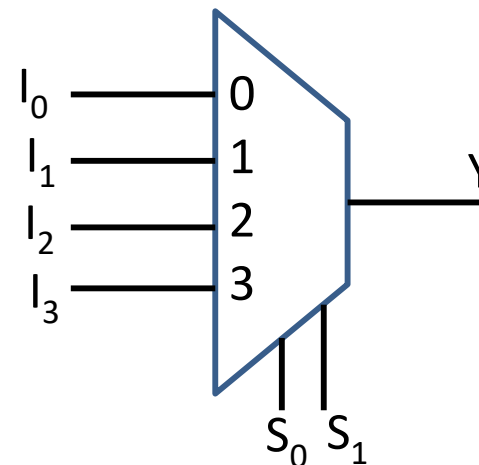
2ⁿ:1 Mux models



4:1 Mux Truth Table

EN	S ₁	S ₀	Y
0	x	x	0
1	0	0	I ₀
1	0	1	I ₁
1	1	0	I ₂
1	1	1	I ₃

Alternate Symbol



Functional description

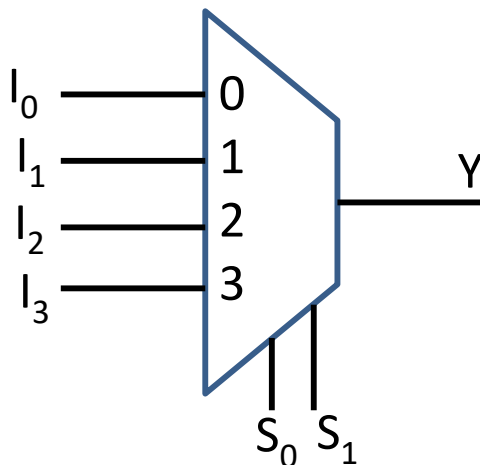
4:1 Mux Truth Table

EN	S_1	S_0	Y
0	x	x	0
1	0	0	I_0
1	0	1	I_1
1	1	0	I_2
1	1	1	I_3

$$Y = \text{EN} \cdot \left[\sum_{k=0}^{2^n-1} m(S)_k I_k \right]$$

$m(S)_k$ is the k^{th} minterm on the selection variables $S_0 \dots S_{n-1}$

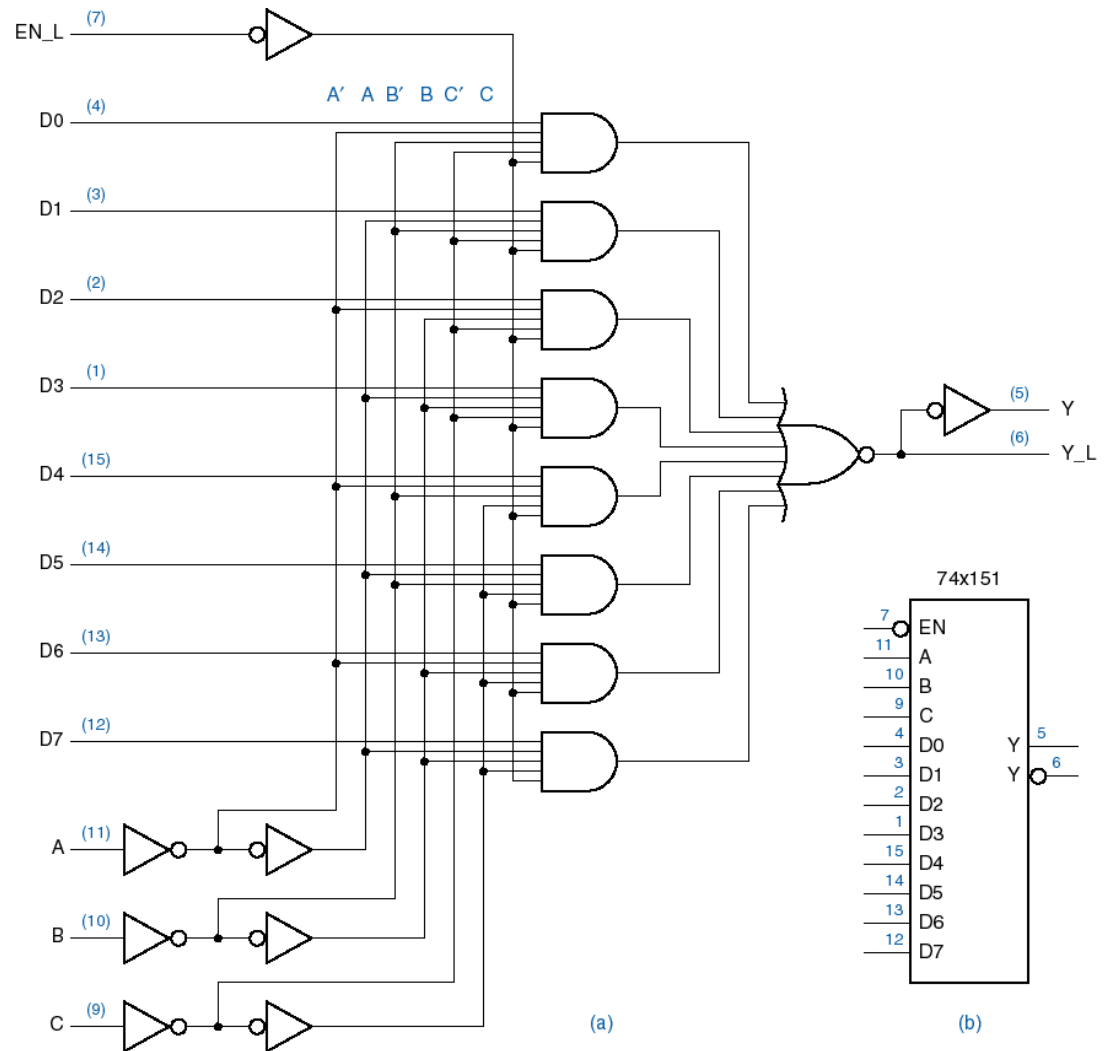
Alternate Symbol



Exercise: Draw the 4:1 Mux internal logic circuit

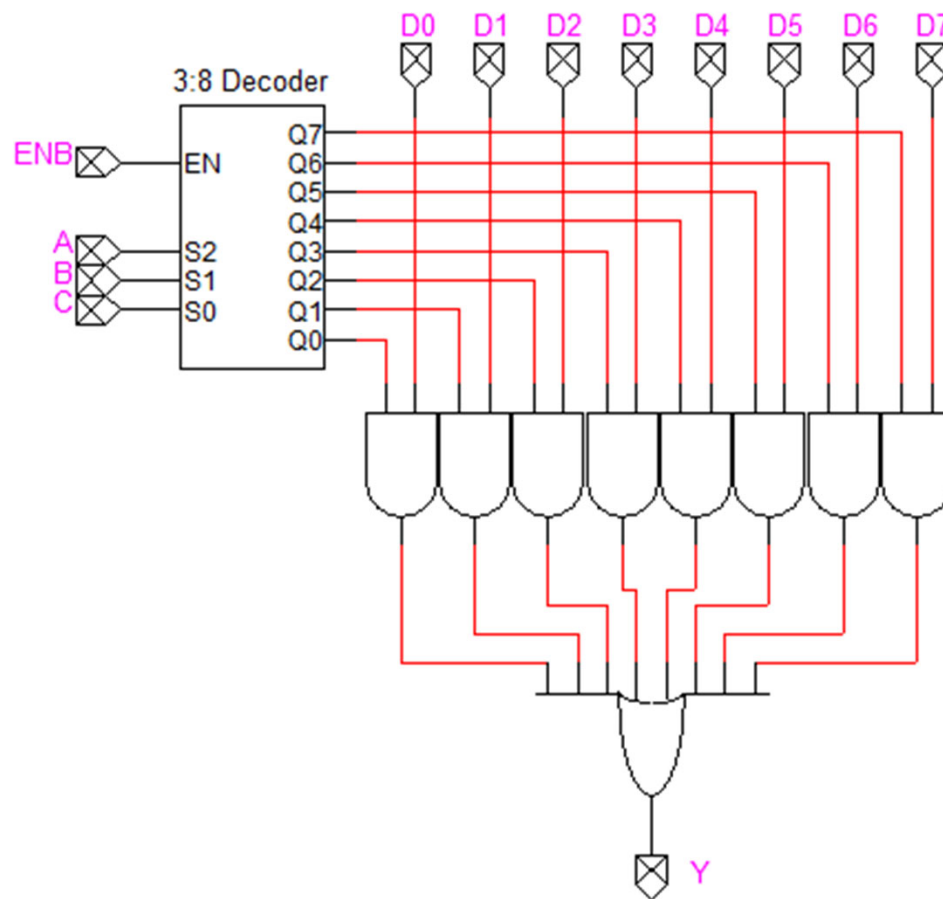
The 74151 model

- 8:1 mux
- Obtain the truth table
- Write the output equations



Mux and decoders

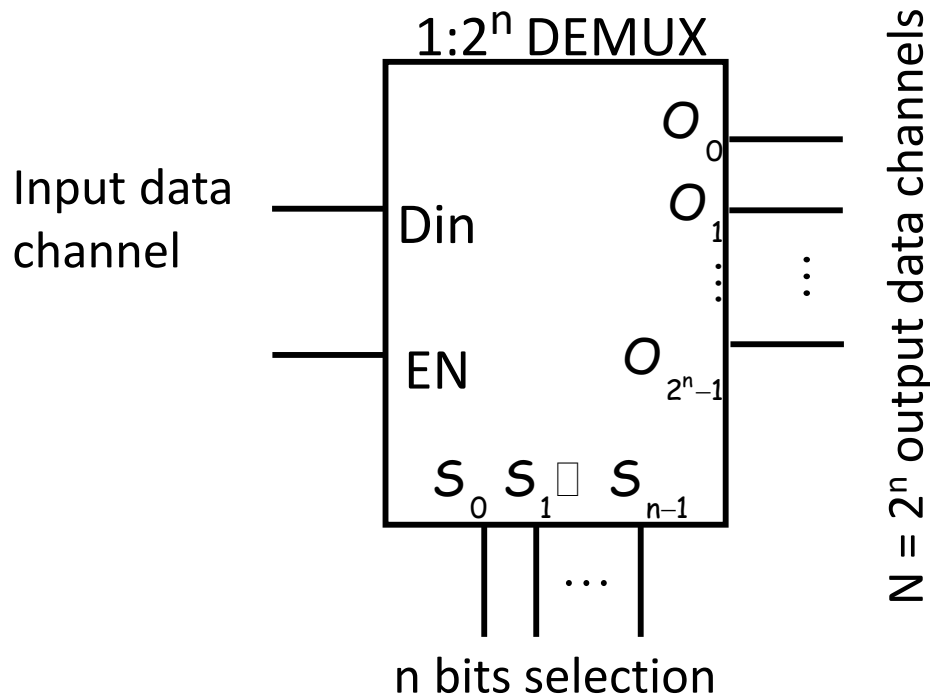
- Verify that the logic circuit is a 8:1 Mux



Demultiplexers

- Functional inverse of a multiplexer
 - An inverse digital switch: a single input is “routed” to one out of N outputs

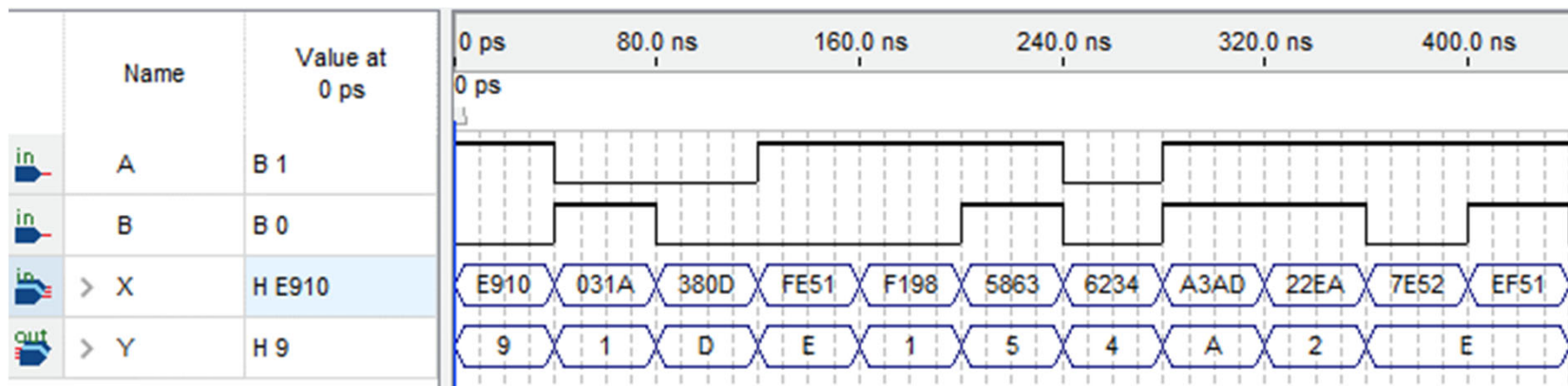
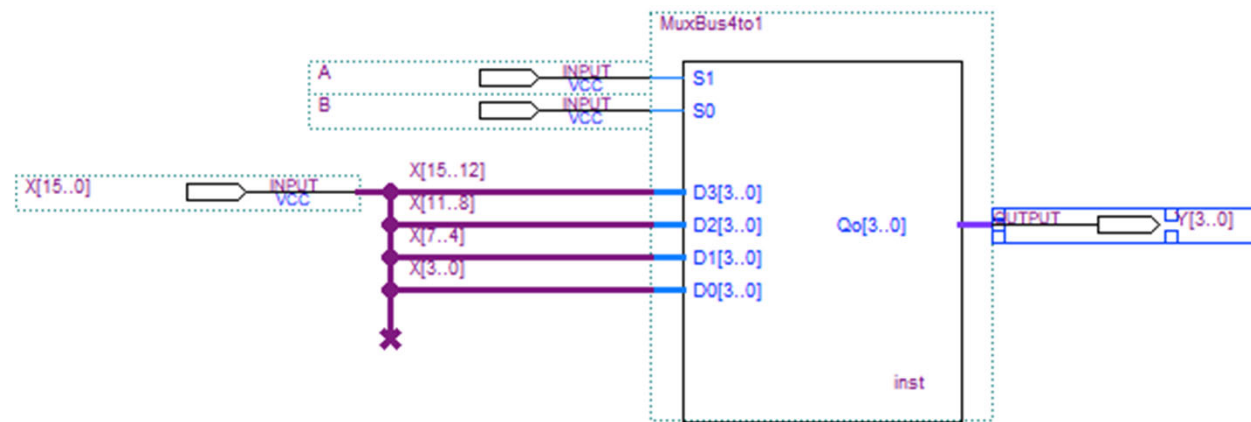
$$O_k = EN \cdot D_{in} m_k(S), \quad k = 0, \dots, 2^n - 1$$



Question: How can we use a demux as a decoder?

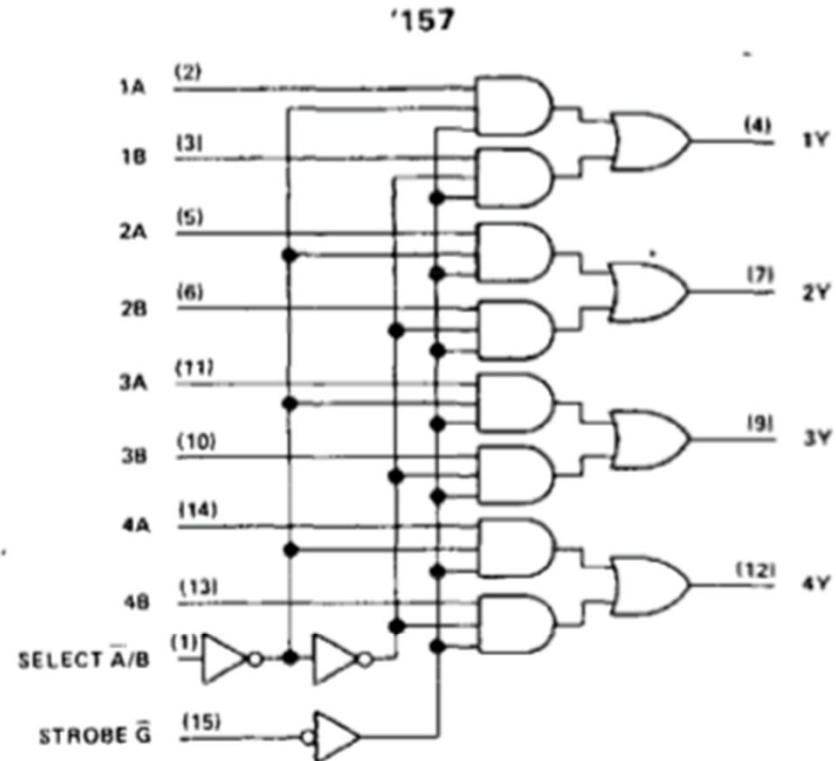
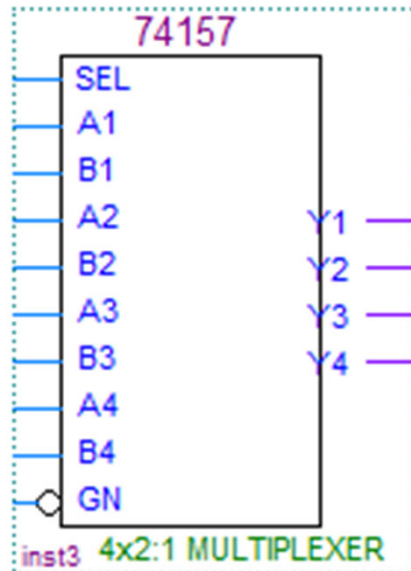
Multiplexing multibit data channels

- Mux 4:1, 4 bit input data channels
- Explain the timing diagram



The 74157 model

- 74157: 4x2:1



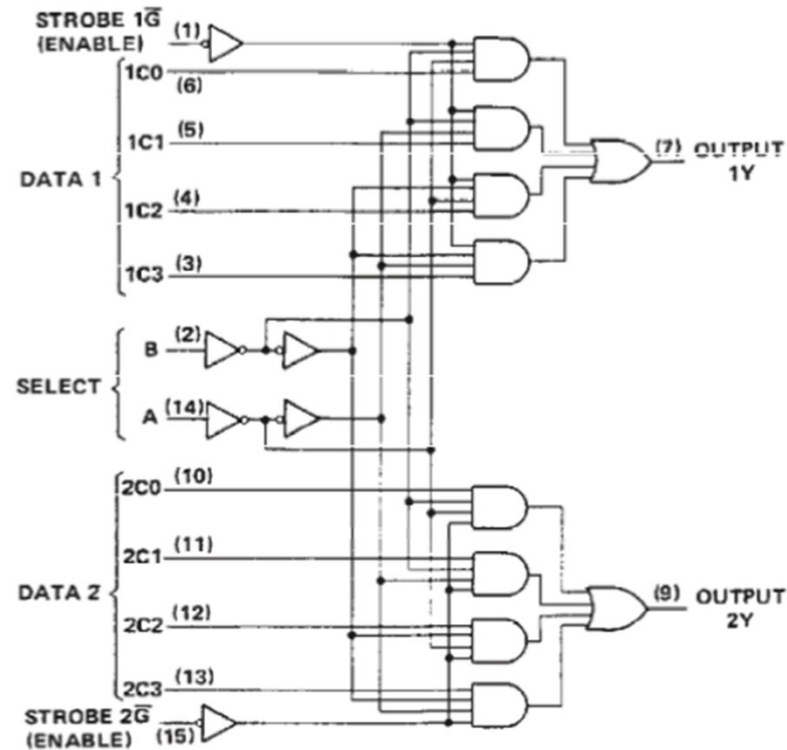
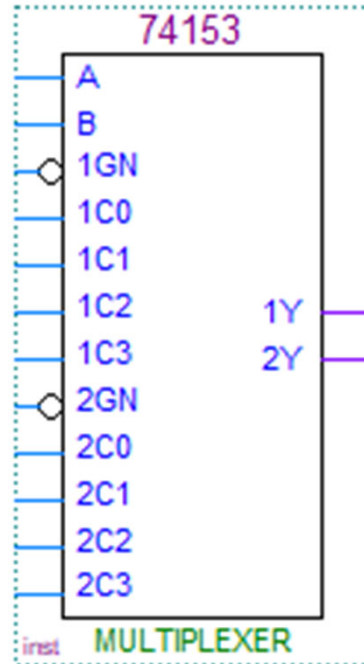
FUNCTION TABLE

INPUTS				OUTPUT Y	
STROBE \bar{G}	SELECT $\bar{A/B}$	A	B	'157, 'LS157, 'S157	'LS158 'S158
H	X	X	X	L	H
L	L	L	X	L	H
L	L	H	X	H	L
L	H	X	L	L	H
L	H	X	H	H	L

H = high level, L = low level, X = irrelevant

The 74153 model

- 74153: 2x4:1



FUNCTION TABLE

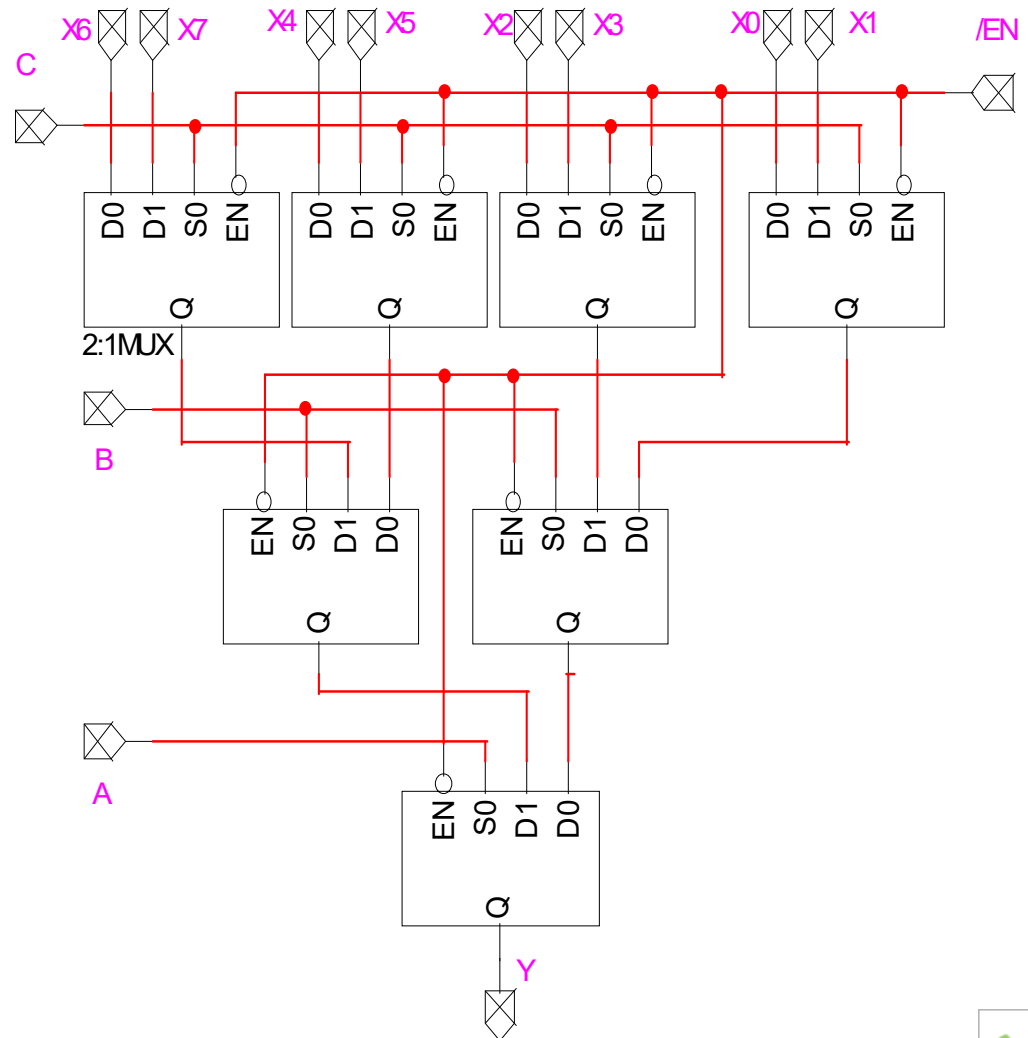
SELECT INPUTS		DATA INPUTS				STROBE	OUTPUT
B	A	C0	C1	C2	C3	\bar{G}	Y
X	X	X	X	X	X	H	L
L	L	L	X	X	X	L	L
L	L	H	X	X	X	L	H
L	H	X	L	X	X	L	L
L	H	X	H	X	X	L	H
H	L	X	X	L	X	L	L
H	L	X	X	H	X	L	H
H	H	X	X	X	L	L	L
H	H	X	X	X	H	L	H

Select inputs A and B are common to both sections.
H = high level, L = low level, X = irrelevant

Mux hierarchies

- 8:1 with 7x(2:1)

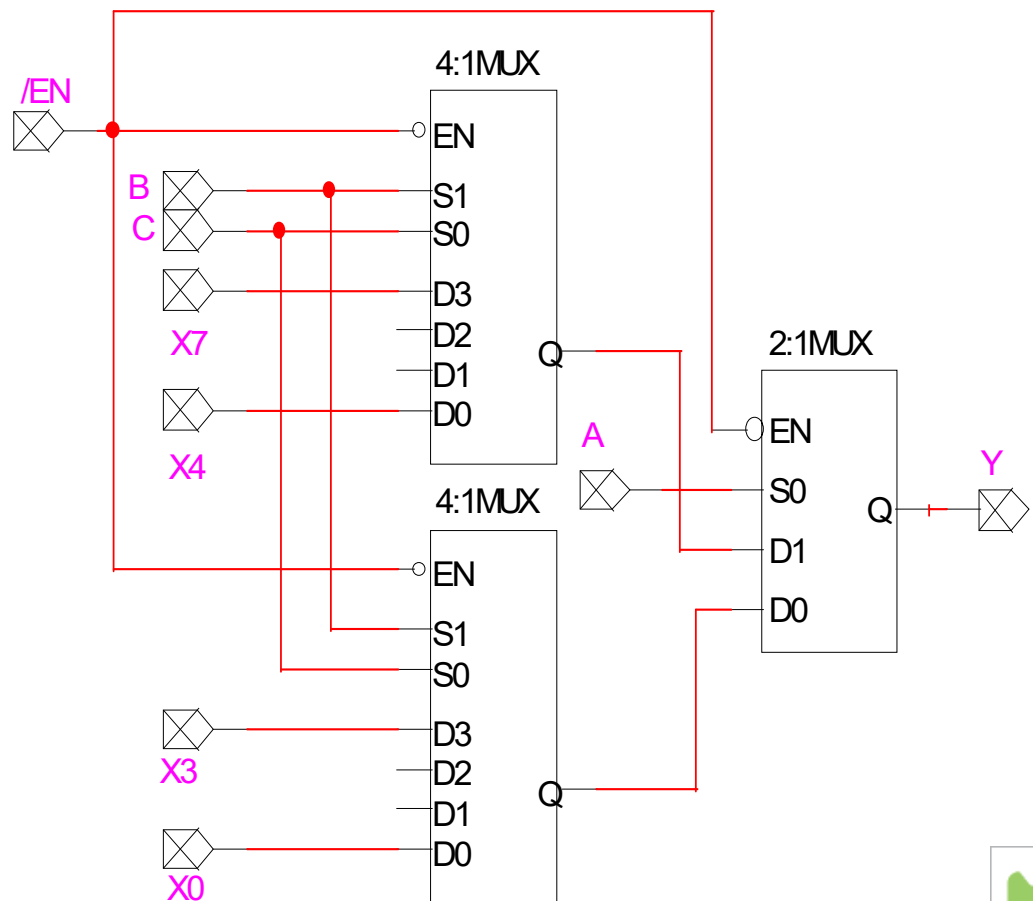
- Always check the design by obtaining the truth table.
- Note that IN THIS case A is the most significant selection variable



Mux hierarchies

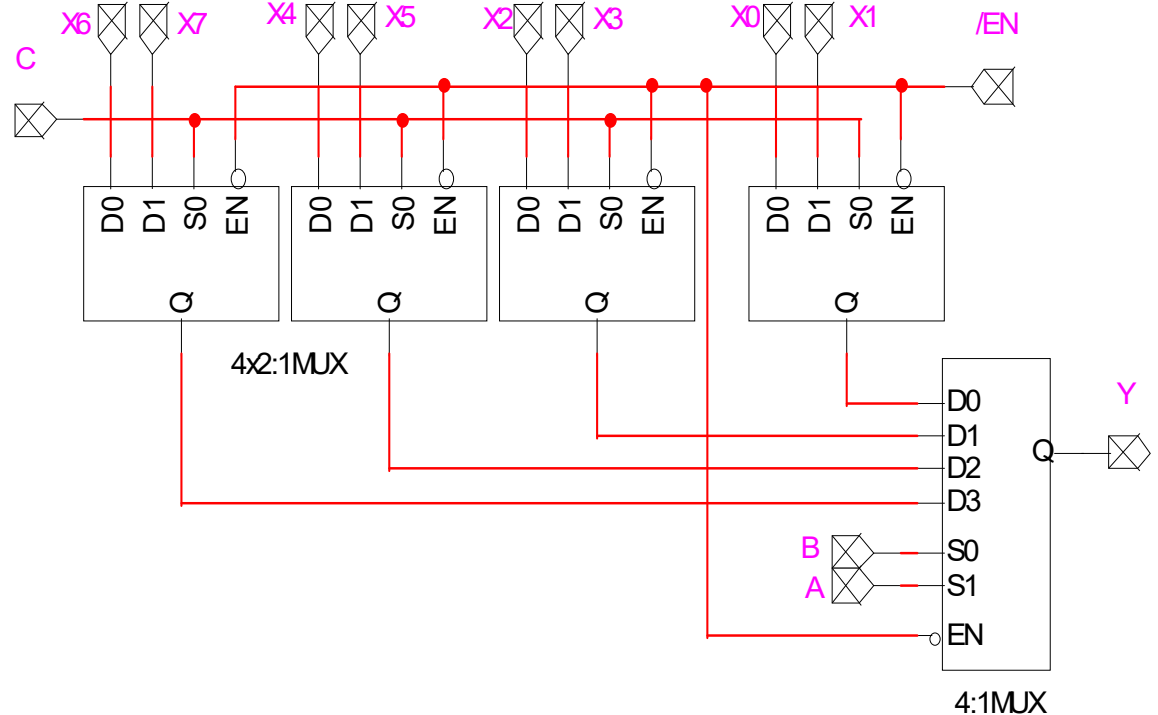
- 8:1 with 2x(4:1 MUX) + 1x(2:1 MUX)

- Always check the design by obtaining the truth table.
- Note that IN THIS case A is the most significant selection variable



Mux hierarchies

- 8:1 with 4x(2:1 MUX) + 1x(4:1 MUX)

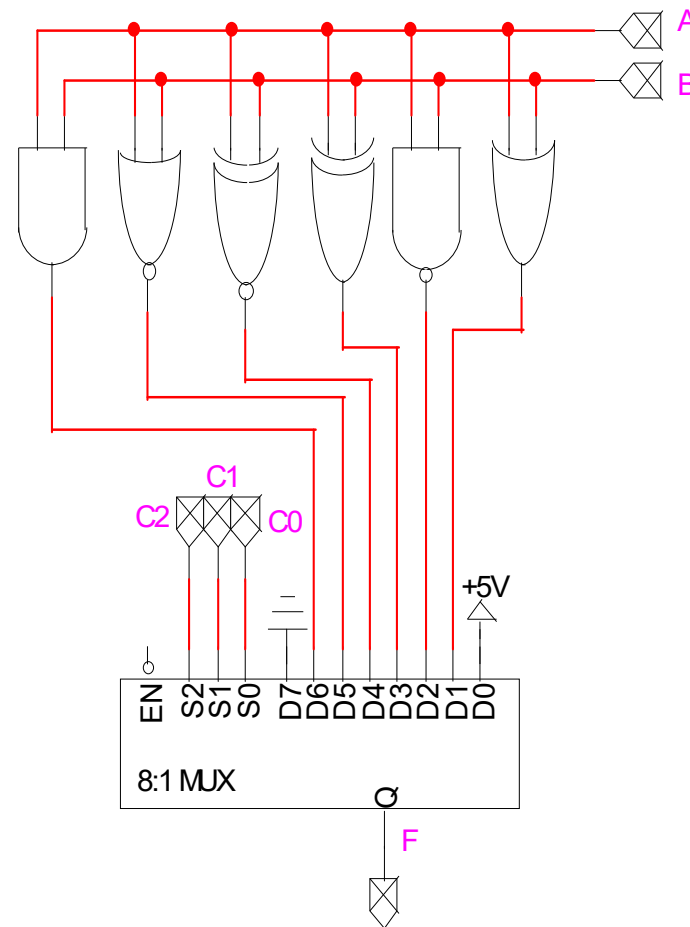


- Always check the design by obtaining the truth table.
- Note that IN THIS case A is the most significant selection variable

Logic Function Unit (LFU)

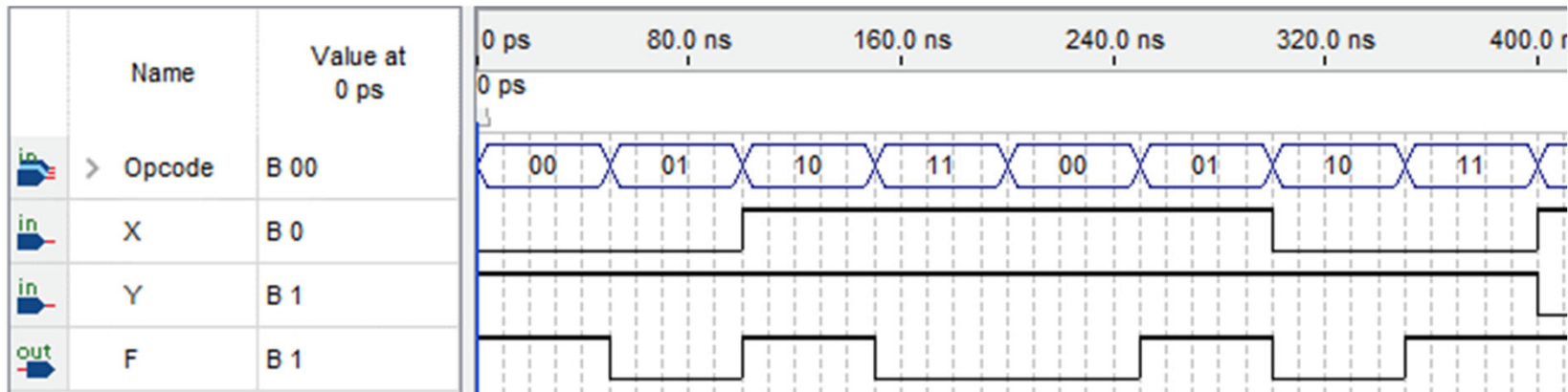
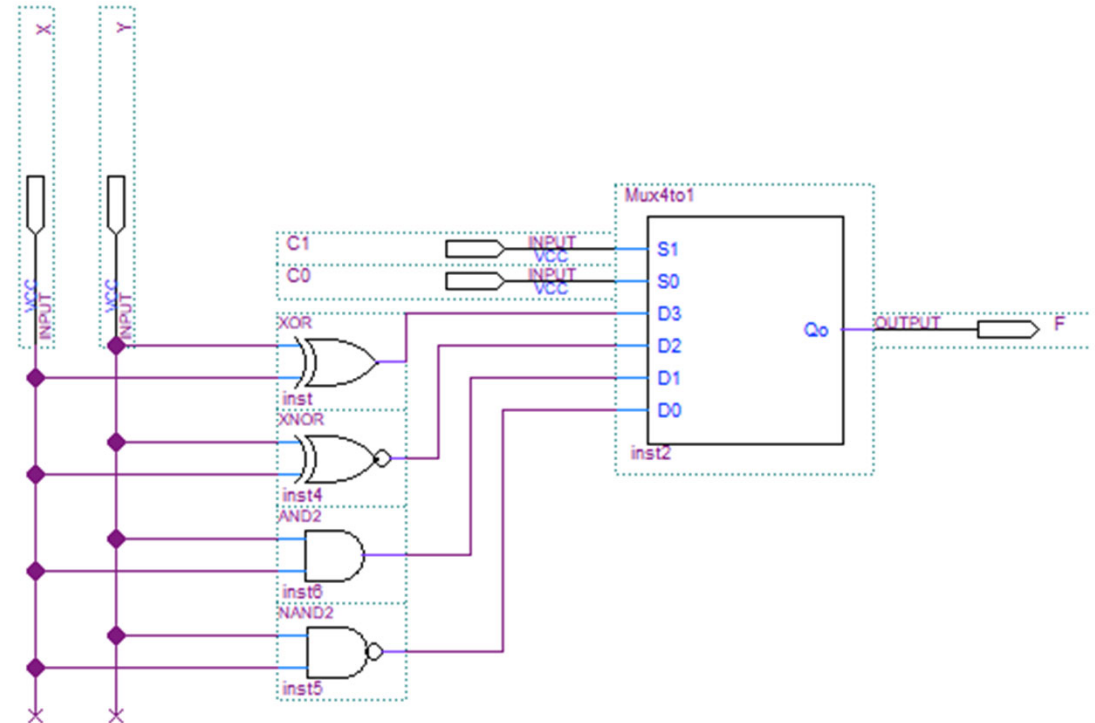
- Use $C_2C_1C_0$ as function code (Opcode)

C_2	C_1	C_0	F
0	0	0	1
0	0	1	$A+B$
0	1	0	$(A.B)'$
0	1	1	$A \oplus B$
1	0	0	$(A \oplus B)'$
1	0	1	$(A+B)'$
1	1	0	$A.B$
1	1	1	0



Exercise

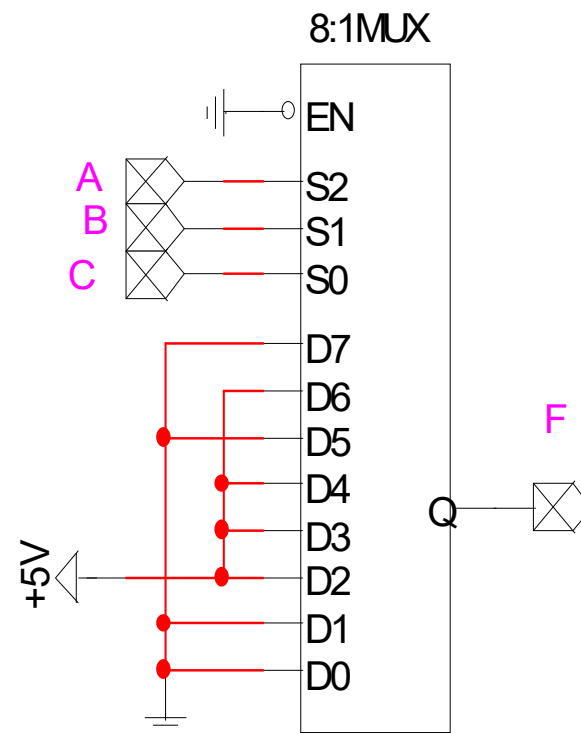
- Explain the LFU timing diagram



Boolean Functions with Multiplexers

- Simplest approach:
 - Direct mapping of the Truth Table
 - Selection = input variables
 - $D_k = F_k$

A	B	C	F
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	0



Boolean Functions with Multiplexers

- The general case:
 - Selection = a subset of input variables
 - $D_k = g_k$ where each g_k is a simpler Boolean function of the remaining input variables
- Example

n-1 input variables used for selection

I1 I2 ..			In	F			
...	0	0	0	1	1
...	1	0	1	0	1
				0	In	\bar{I}_n	1

Possible output values as a function of I_n

Example

- Implement the Boolean function $F(A,B,C,D)$ using a 8:1 Mux

$$F(A,B,C,D) = \sum m(1,3,6,7,8,11,12,14)$$

AB \ CD		A			
		00	01	11	10
C	00	0	0	1	1
	01	1	0	0	0
	11	1	1	0	1
	10	0	1	1	0

B

D

1. Use the Karnaugh map JUST to layout the truth table

2. Choose the subset of inputs to be assigned to the mux selection inputs

Eg. A,B,C

3. Find the logic values of the mux data inputs as functions of the remaining inputs

D in this case

Regions of the truth sharing the same value of the selection inputs. (A,B,C) in this case. DO NOT MISINTERPRET as prime implicants



Example

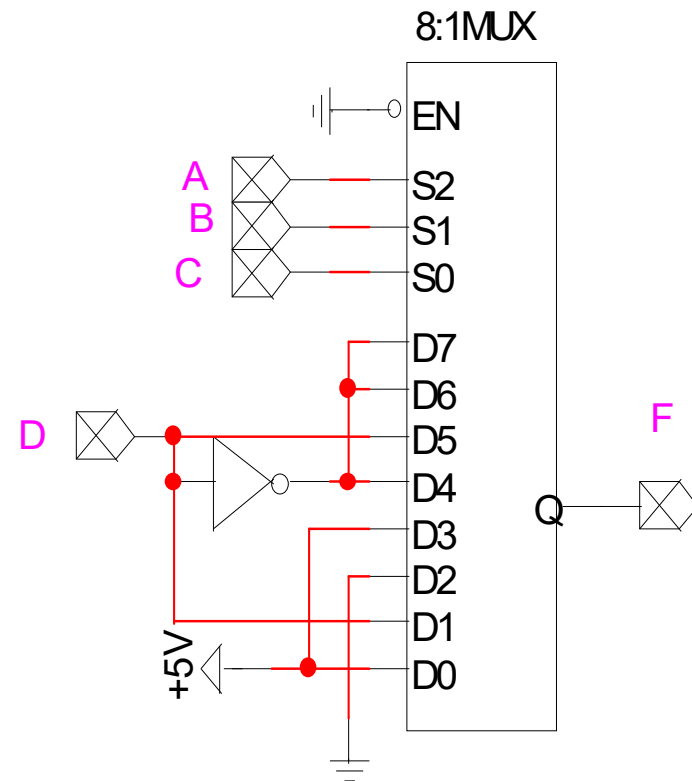
- Find the error in the logic circuit

$$F(A,B,C,D) = \sum m(1,3,6,7,8,11,12,14)$$

AB \ CD		A			
		00	01	11	10
C	00	0	0	1	1
	01	1	0	0	0
	11	1	1	0	1
	10	0	1	1	0

B

D



Exercise

- Implement the Boolean function F using a a MUX 4:1 and additional elementary logic

$$F(A,B,C,D) = \sum m(1,3,6,7,8,11,12,14)$$

- Several choices of input variables are possible to be assigned to the mux selection inputs. Try for example (A,B) and (C,D)

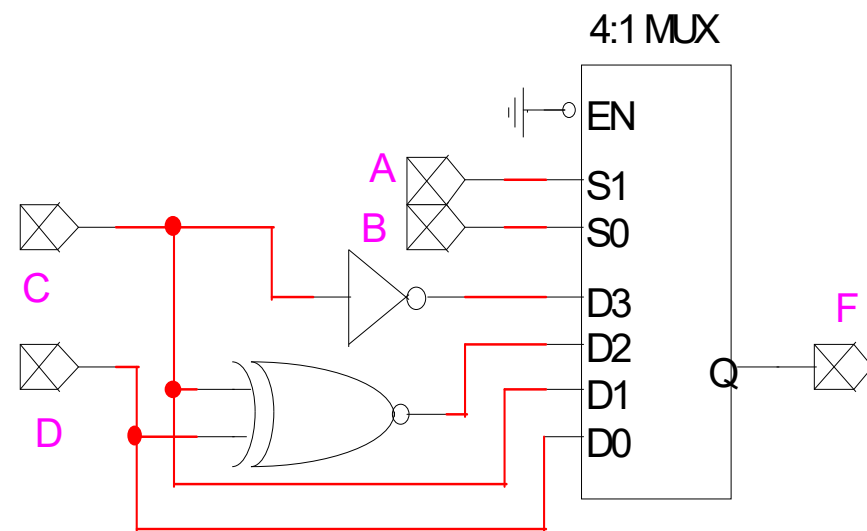
Exercise

- Using A,B for selection

$$F(A, B, C, D) = \sum m(1,3,6,7,8,11,12,13)$$

AB \ CD		A			
		00	01	11	10
C	00	0	0	1	1
	01	1	0	1	0
	11	1	1	0	1
	10	0	1	0	0
		B			

D



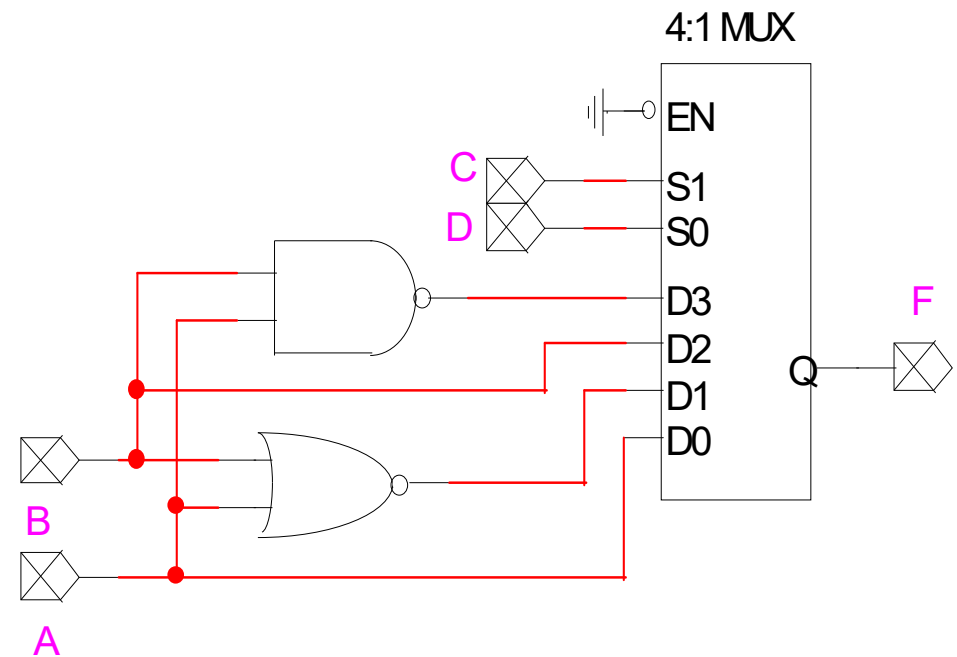
Exercise

- Using C,D for selection

$$F(A,B,C,D) = \sum m(1,3,6,7,8,11,12,14)$$

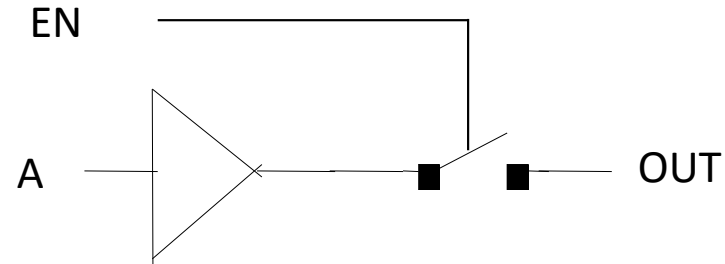
AB \ CD		A			
		00	01	11	10
C	00	0	0	1	1
	01	1	0	0	0
	11	1	1	0	1
	10	0	1	1	0
		B			

D



High-Impedance (High – Z)

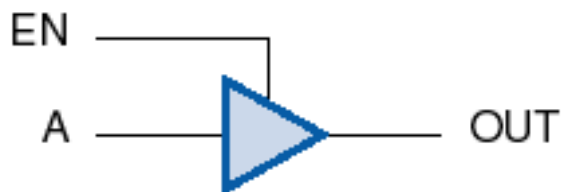
- A switch model



- When the switch is open there is an almost infinite resistance (Impedance) to the signal flow through the “wire” OUT.
- The output signal is left “floating” with neither HIGH or LOW logic levels assigned.
- The output is assigned a High-Z state and the device exhibits a 3 State behavior

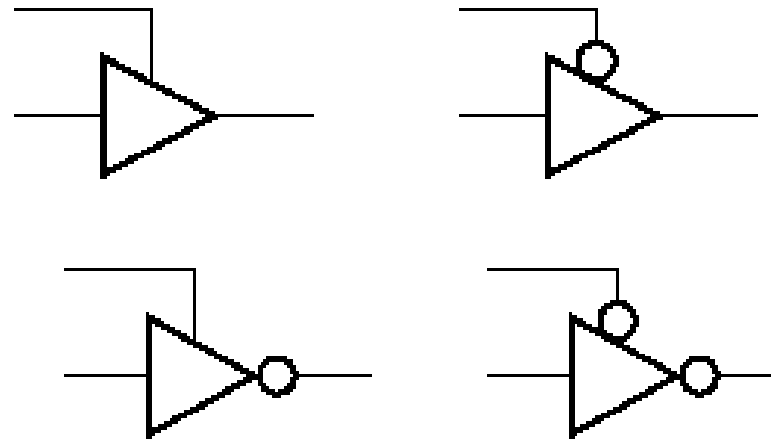
3 State Buffers

- Possible outputs: HIGH, LOW, High-Z



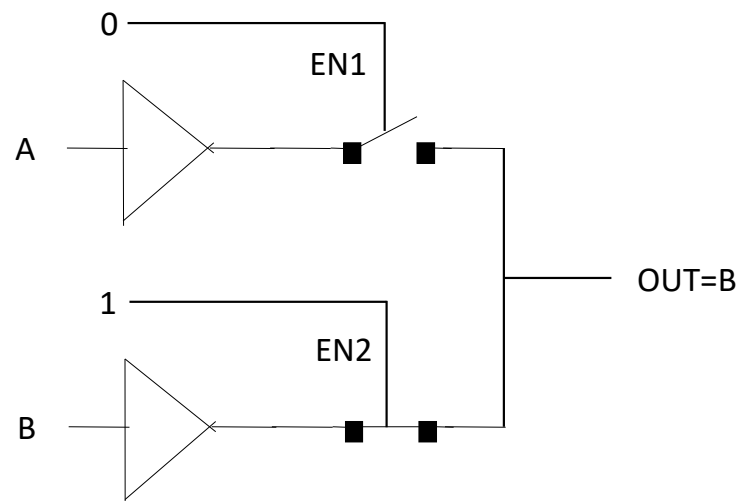
EN	A	OUT
L	L	Hi-Z
L	H	Hi-Z
H	L	L
H	H	H

Alternatives



Wire sharing

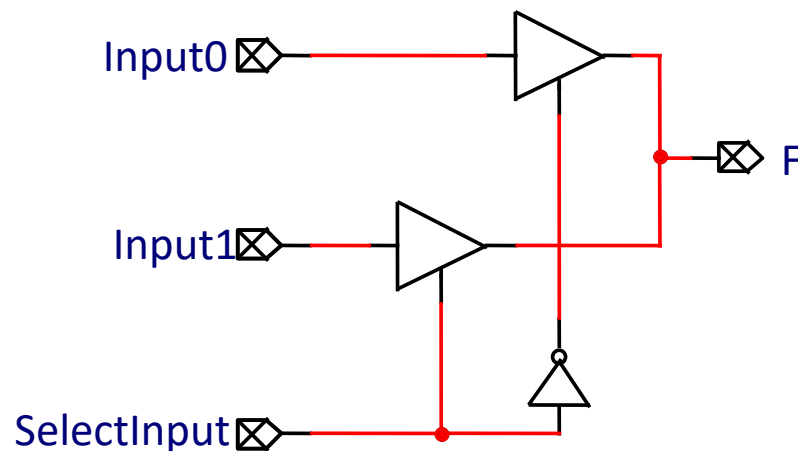
- High-Z outputs may be physically connected



- Of course $EN1 = EN2 = 1$ should never occur.
- Tight control of enabling inputs is required

A special kind of Mux

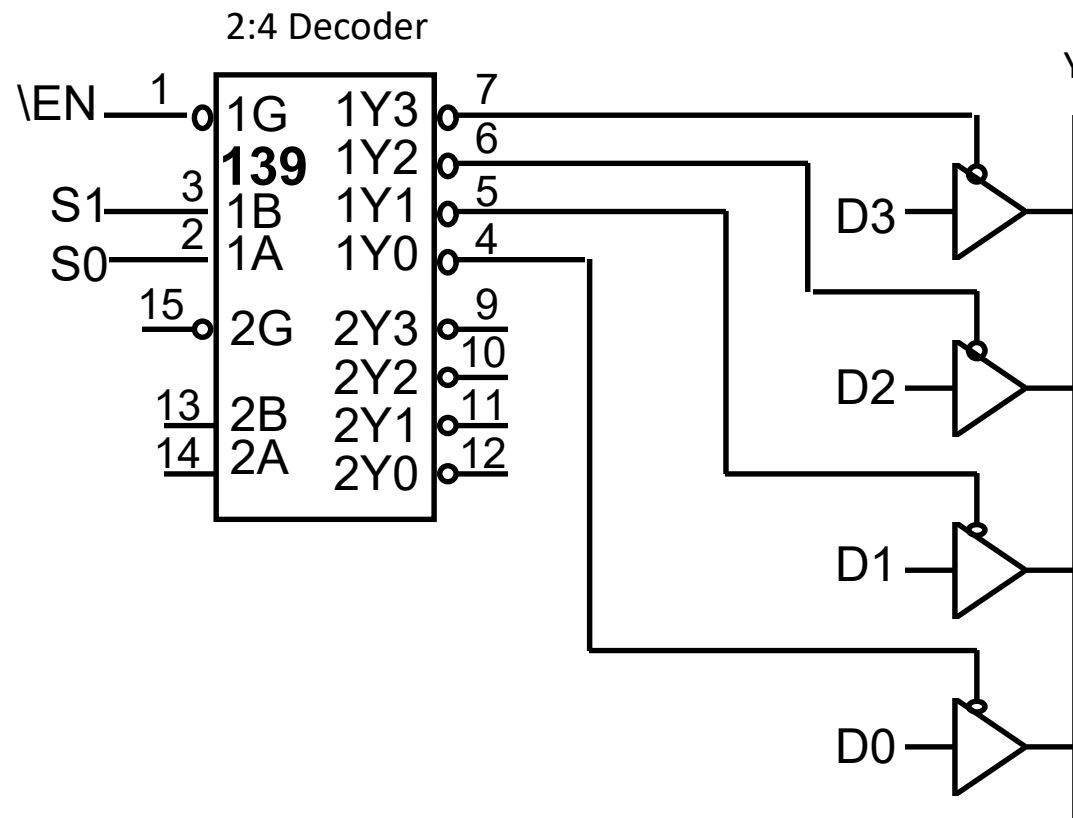
- Efficient multiplexing strategy
- Mux 2:1



- Write the Truth Table

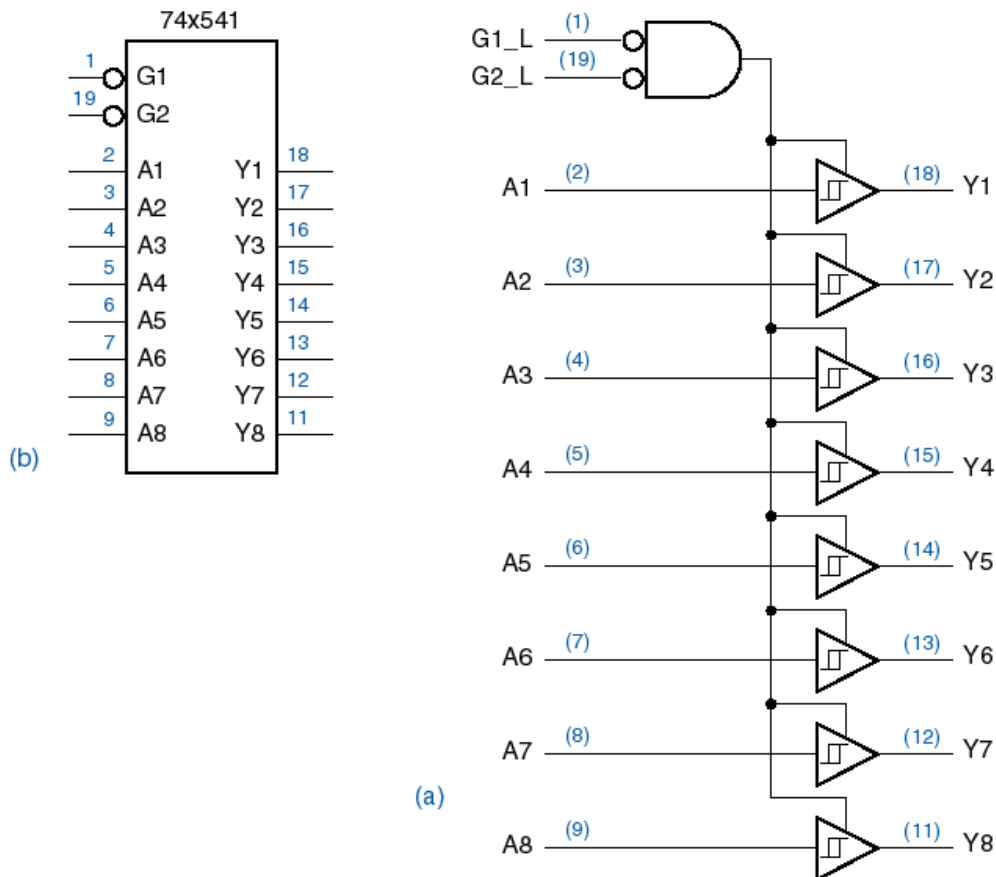
Exercise

- Write the truth table of the circuit and verify that's a 4:1 mux

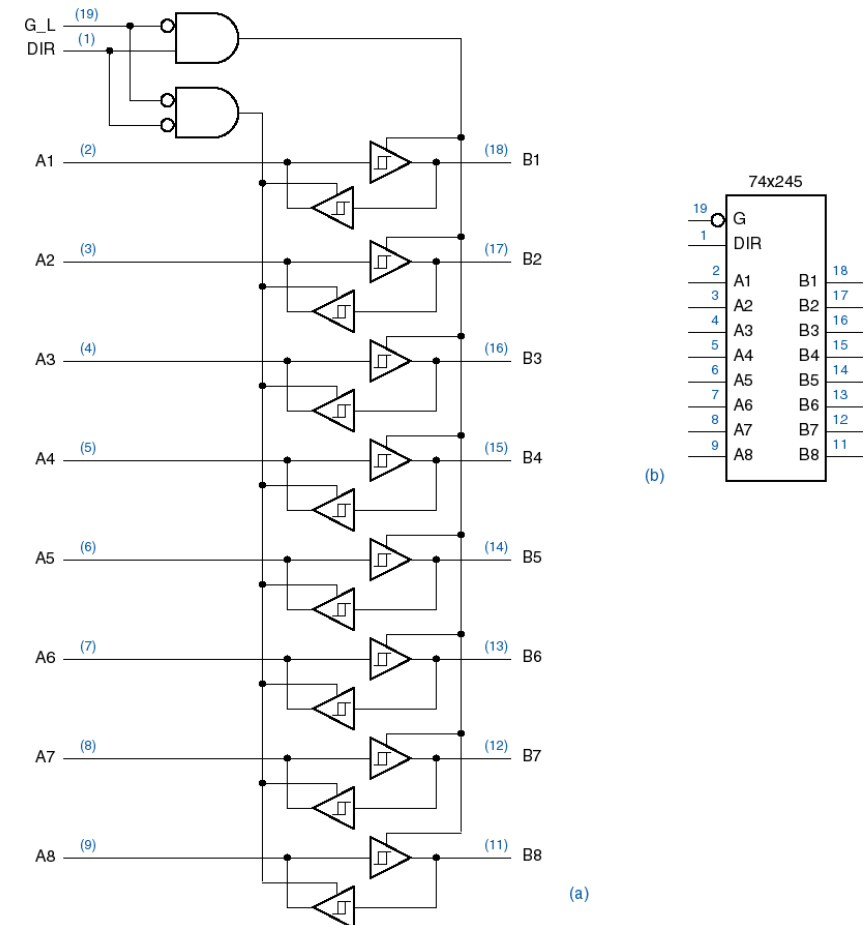


Aggregate 3 State Buffer Models

“BUS” Driver



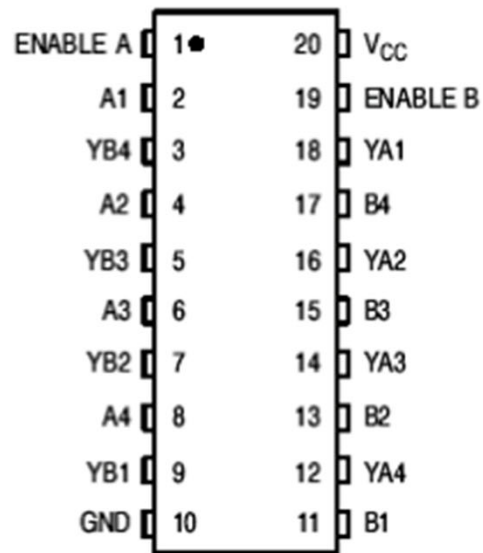
Transceiver



Aggregate 3 State Buffer Models

74HC244

PIN ASSIGNMENT

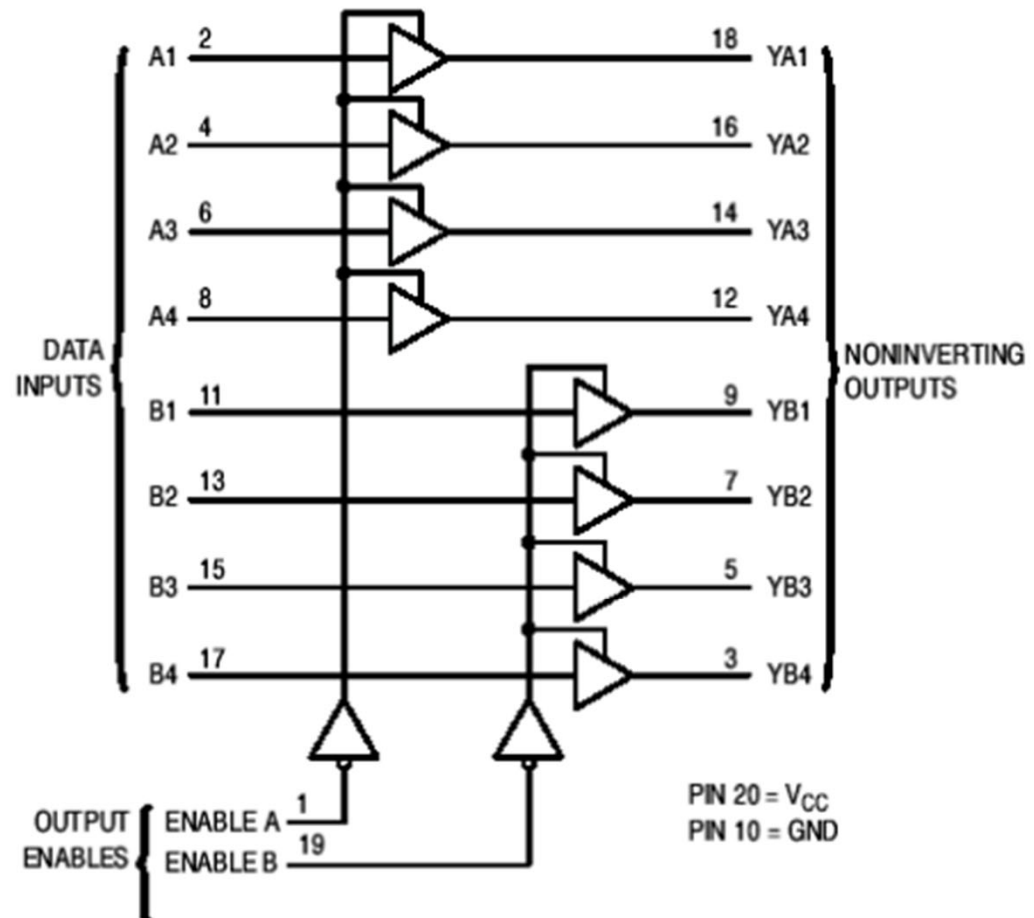


FUNCTION TABLE

Inputs		Outputs
Enable A, Enable B	A, B	YA, YB
L	L	L
L	H	H
H	X	Z

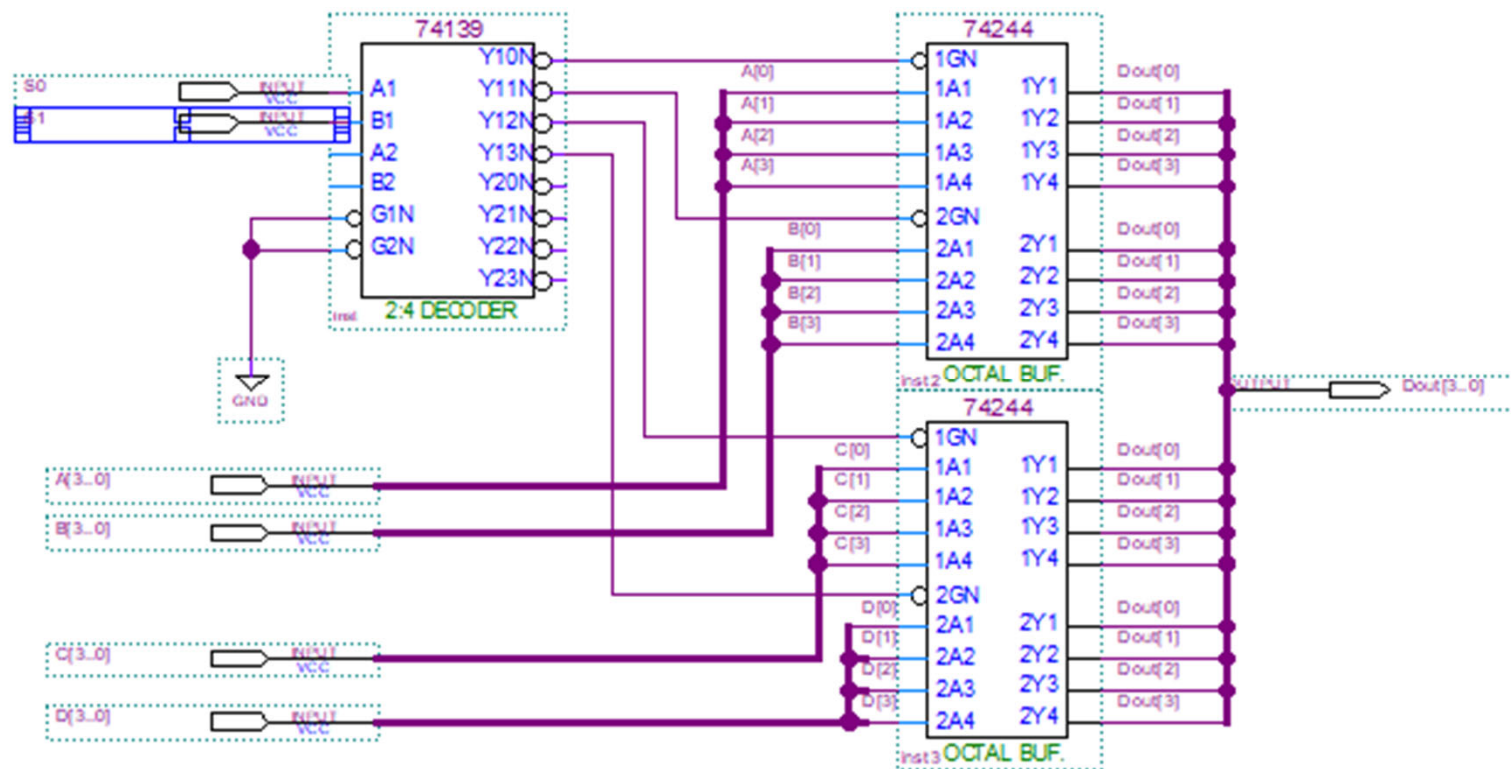
Z = high impedance

LOGIC DIAGRAM



Word Multiplexing

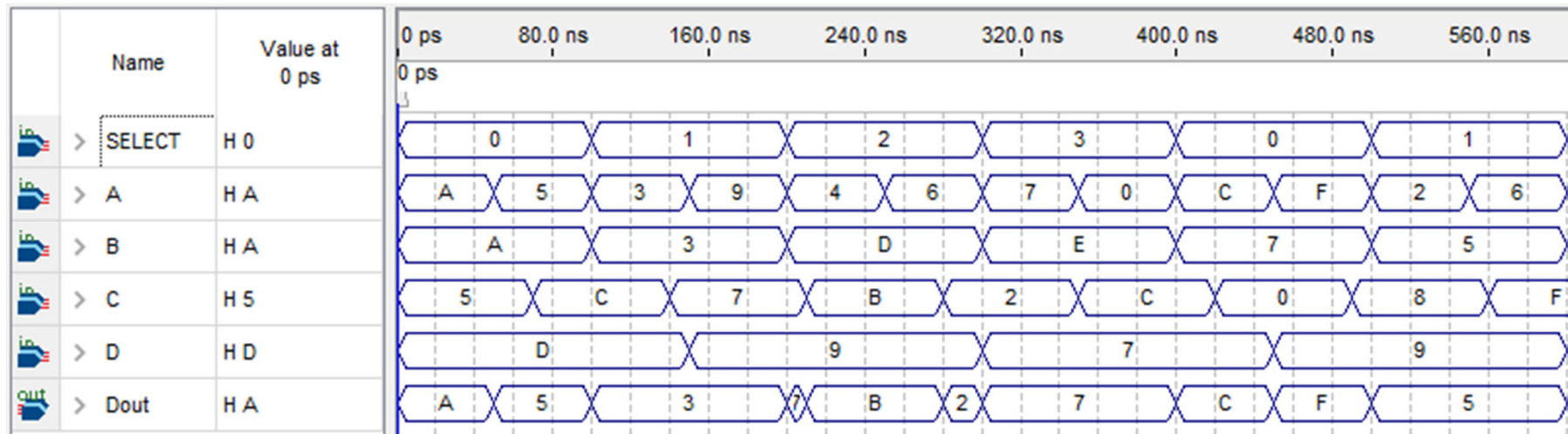
- Main idea:
 - Decode the 3 State buffers enabling inputs
 - Share the output data bus



Exercise

- Explain the timing diagram of the previous circuit

- SELECT = (S1,S0)



Final Remarks

- Always recall
 - The block symbol
 - The types of inputs and outputs
 - Data
 - Control
 - The truth table
 - The output equations
- Design with encapsulated logic requires mastering all the functional details of each block