

RadonPy tutorial

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Python library for automated polymer MD



Automated pipeline of MD calculation for polymer properties seamless integrated with RDKit

Pre-process

Polymer chain generator

- Homopolymer
- Alternating copolymer
- Random copolymer
- Block copolymer

Unit cell generator

- Amorphous
 - Single component
 - Mixture
- Oriented (Nematic-like)
 - Single component
 - Mixture
- Crystalline

Force field assignment

- GAFF
- GAFF2

Atomic charge calculation

- Gasteiger
- RESP (using QM solver)
- ESP (using QM solver)

Input file generator

- NVE, NVT, NPT
- Annealing
- Thermal conduction
- Uni-axial extension

Post-process

Property calculation

- Density
- Cp, Cv
- Bulk modulus
- Thermal expansion
- Linear expansion
- Static dielectric const.
- Thermal conductivity
- Order parameter
- Young's modulus, etc

Data science

SMILES transformation

Cyclic polymer

Simulation

MD solver

QM solver

Psi4

LAMMPS

Linear polymer

Descriptor calculation

- Force field descriptor
 - Summary statistics
 - Kernel mean

Recommended system requirement

- Python 3.7, 3.8, 3.9
- RDKit >= 2020.03
- Psi4 >= 1.5
- resp
- dftd3
- mdtraj >= 1.9
- matplotlib
- scipy
- pandas
- LAMMPS >= 3Mar20

Installation

- 1. Download of miniforge https://github.com/conda-forge/miniforge
- 2. Installation of miniforge on Linux system bash ./Miniforge3-Linux-x86 64.sh
- 3. Create conda environment (Python 3.9)

conda create -*n* radonpy python=3.9 conda activate radonpy

4. Installation of requirement packages by conda

conda install -c psi4 -c conda-forge rdkit psi4 resp scipy mdtraj matplotlib pandas

5. Installation of LAMMPS by conda

conda install -c conda-forge lammps

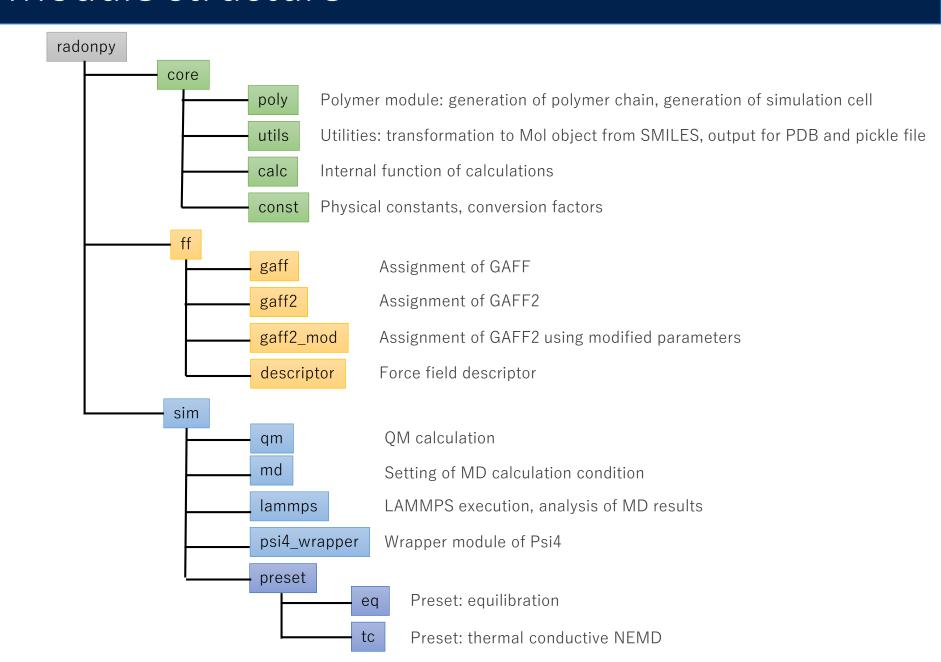
or manually build from source of LAMMPS official site. In this case, the environment variable must be set:

export LAMMPS_EXEC=<path-to-LAMMPS-binary>

6. Installation of RadonPy

git clone -b main https://github.com/RadonPy/RadonPy.git export PYTHONPATH=<Path-to-RadonPy>:\$PYTHONPATH

Module structure



Example of workflow

Input: SMILES, polymerization degree, temperature, etc.

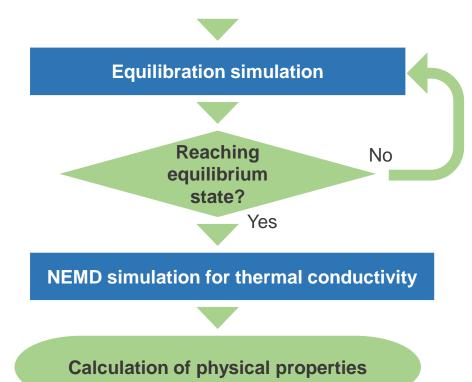
Conformation search of a repeating unit

Calculation of electronic properties of a repeating unit

Generation of a polymer chain

Assignment of force field parameters

Generation of a simulation cell



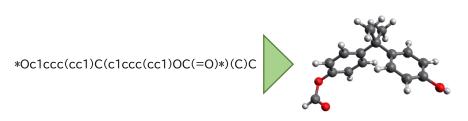
Repeating unit generation from SMILES

radonpy.core.utils.mol_from_smiles

SMILES

Monomer

from radonpy.core import utils
smiles = '*CC(*)c1ccccc1'
mol = utils.mol_from_smiles(smiles)



- For a given SMILES string of a polymer repeating unit, 3D atomic were generated using the ETKDG method.
- The input SMILES string has two asterisk symbols for representing two attachment points of the repeating unit.
- The two attachment points were capped with tritium atoms.
- For unidentified cis/trans isomer, The trans isomer is generated in default.
- For unidentified R/S chiral isomer, The S isomer is generated in default.

$$\begin{array}{c|c} H & H & H \\ \hline H & H & H \\ \hline H & H & H \\ \hline \end{array}$$

Example of a repeating unit of polystyrene

RDKit Mol object

RDKit Mol object contains information of atoms, bonds, atomic coordinates, etc. RadonPy extends the RDKit Mol object for polymer modeling and MD calculation.

Atom object

Mol.GetAtoms() atom = Mol.GetAtomWithIdx(idx)

atom.GetIdx()
atom.GetAtomicNum()
atom.GetSymbol()
atom.GetMass()

Returns a sequence containing all of the molecule's Atoms. Returns a particular Atom.

Returns the atom's index Returns the atomic number. Returns the atomic symbol Returns the atomic mass.

Bond object

Mol.GetBonds() bond = Mol.GetBondWithIdx(idx)

bond.Getldx()
bond.GetBondTypeAsDouble()
bond.IsInRing()
bond.GetBeginAtom()
bond.GetEndAtom()

Returns a sequence containing all of the molecule's Bonds. Returns a particular Bond.

Returns the bond's index

Returns the type of the bond as a double (i.e. 1.0 for SINGLE, 1.5 for AROMATIC, 2.0 for DOUBLE) Returns whether or not the bond is in a ring of any size.

Returns the bond's first atom.

Returns the bond's second atom.

Reference sites https://www.rdkit.org/docs/

(Japanese)
https://www.rdkit.org/docs_jp/
https://future-chem.com/rdkit-mol/

Conformation search

Input: SMILES, polymerization degree, temperature, etc.

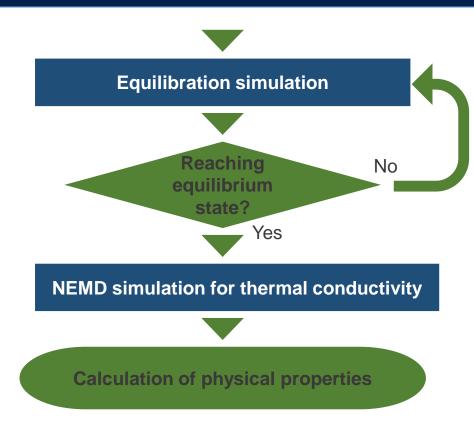
Conformation search of a repeating unit

Calculation of electronic properties of a repeating unit

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Conformation search

```
from radonpy.core import utils
from radonpy.sim import qm
from radonpy.ff.gaff2_mod import GAFF2_mod

ff = GAFF2_mod() # Instance of GAFF2_mod force field
mol = utils.mol_from_smiles(smiles) # Generation of mol object
mol, energy = qm.conformation_search(mol, ff=ff, work_dir=work_dir, psi4omp=omp_psi4, mpi=mpi, omp=omp, gpu=gpu, log_name='monomer1')
```

qm.conformation_search automatically executes following procedure for a given Mol object of a polymer repeating unit

- 1. [Conformation generation] 3D atomic coordinates of up to 1,000 different conformations were generated using the ETKDG version 2 method implemented in RDKit.
- **2.** [MM optimization] The potential energy of each conformation of a repeating unit was evaluated using the molecular mechanics calculation with GAFF2_mod after the geometry optimization.
- **3.** [Clustering] The optimized conformers were clustered by performing the Butina clustering based on the torsion fingerprint deviation.
- **4.** [**DFT optimization**] The most stable $\underline{\mathbf{4}}$ conformations were further optimized by performing DFT calculations with the ω B97M-D3BJ/6-31G(d,p).
- **5.** [Most stable conformation] Conformation IDs in the returned Mol object are sorted by the DFT energy. The most stable conformation is set to 0 of conformation ID.

radonpy.sim.qm.conformation_search

mol: Input of RDKit Mol object

Options

ff: Force field object for MM optimization

nconf: Maximum number of generated conformations by ETKDG [int]

dft_nconf: Maximum number of conformations to be geometry optimized by DFT calculations [int]

etkdg_ver: Version of ETKDG method [int]

rmsthresh: Threshold of RMS for clustering in conformation generation with ETKDG [float]

tfdthresh: Threshold of torsion fingerprint deviation in conformation clustering [float]

opt_method: Calculation method of the DFT optimization [str]

opt_basis: Basis set of the DFT optimization [str]

geom_iter: Maximum number of iteration in the DFT optimization [int]

geom_conv: Conversion criterion in the DFT optimization [str]

geom_algorithm: Algorithm in the DFT optimization [str]

log_name: Prefix of the file name of Psi4 log in the DFT optimization [str]

work_dir: Working directory [str]

psi4_omp: Parallel number of OpenMP in DFT optimization by Psi4 [int]

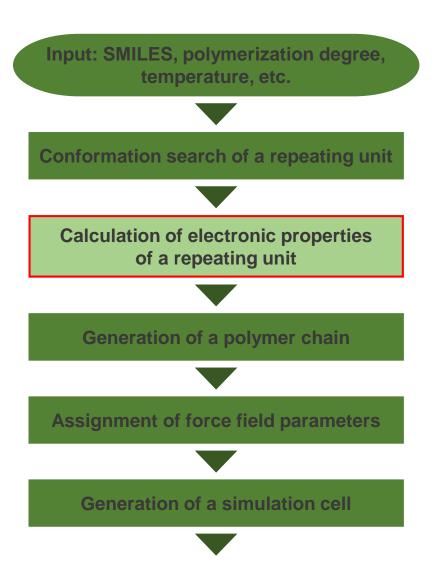
omp: Parallel number of OpenMP in MM calculation by LAMMPS [int]

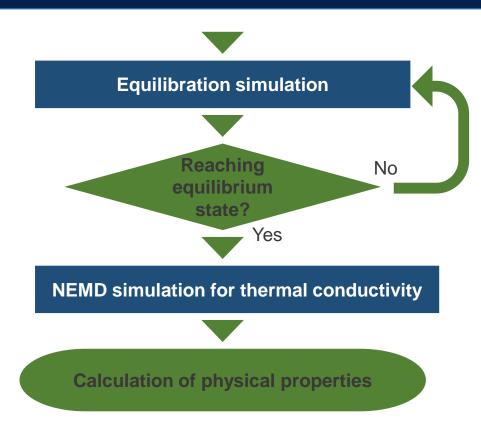
mpi: Process number of MPI in MM calculation by LAMMPS [int]

Returns

mol: RDKit Mol object, energy: Energy values of DFT and MM

Electronic property calculation





Electronic property calculation

from radonpy.sim import qm

qm.assign_charges(mol, charge='RESP', work_dir=work_dir, tmp_dir=tmp_dir, opt=False, omp=omp_psi4, memory=mem_psi4) qm_data = qm.sp_prop(mol, opt=False, work_dir=work_dir, tmp_dir=tmp_dir, omp=omp_psi4, memory=mem_psi4) polar_data = qm.polarizability(mol, opt=False, work_dir=work_dir, tmp_dir=tmp_dir, omp=conf_psi4_omp, memory=mem_psi4)

radonpy.sim.qm

assign_charges: Calculation and assignment atomic charge of the input Mol object

sp_prop: Calculation of total energy, HOMO, LUMO, dipole moment of the input Mol Object

polarizability: Calculation of polarizability tensor of the input Mol object

Notice: The electronic property calculation should perform for a repeating unit not for polymer chain because this process is very time consuming.

radonpy.sim.qm.assign_charges

Calculation and assignment of atomic charge

mol: Input of RDKit Mol object

Options

charge: Charge model (RESP, ESP, gasteiger, Mulliken, Lowdin) [str]

confld: Conformation ID of the RDKit mol object [int]

(confld=0 is the most stable conformation after conformation_search)

opt: With (True) / Without (False) geometry optimization by DFT calculation before the charge calculation [boolean]

work_dir: Working directory [str]

omp: Parallel number of OpenMP in Psi4 [int]

memory: Amount of memory usage (MB) in Psi4 [int]

log_name: Prefix of the file name of Psi4 log [str]

opt_method: Calculation method of the geometry optimization [str]

opt basis: Basis set of the geometry optimization [str]

geom iter: Maximum number of iteration in the geometry optimization [int]

geom_conv: Conversion criterion in the geometry optimization [str]

geom algorithm: Algorithm in the geometry optimization [str]

charge_method: Calculation method of the charge calculation [str]

(The default method is HF because of the GAFF recommendation)

charge basis: Basis set of the charge calculation [str]

charge_basis_gen: Basis set of the charge calculation for each element [dict]

Returns

Boolean: Success (True) / Fail (False)

radonpy.sim.qm.sp_prop

Calculation of total energy, HOMO level, LUMO level, and dipole moment

mol: Input of RDKit Mol object

Options

confld: Conformation ID of the RDKit mol object [int] With (True) / Without (False) geometry optimization by DFT calculation [boolean] opt: Working directory [str] work dir: Parallel number of OpenMP in Psi4 [int] omp: Amount of memory usage (MB) in Psi4 [int] memory: Prefix of the file name of Psi4 log [str] log name: opt method: Calculation method of the geometry optimization [str] Basis set of the geometry optimization [str] opt basis: opt basis gen: Basis set of the geometry optimization (for each element) [str] geom iter: Maximum number of iteration in the geometry optimization [int] geom conv: Conversion criterion in the geometry optimization [str] geom_algorithm: Algorithm in the geometry optimization [str] sp method: Calculation method of the single-point calculation [str] Basis set of the single-point calculation [str] sp basis:

Returns

```
dict type
qm_total_energy: Total enelgy (float, kJ/mol)
qm_homo: HOMO (float, eV)
qm_lumo: LUMO (float, eV)
qm_dipole_x, qm_dipole_y, qm_dipole_z Dipole moment (float, Debye)
```

sp basis gen: Basis set of the geometry optimization (for each element) [dict]

radonpy.sim.qm.polarizability

Calculation of polarizability tensor

mol: Input of RDKit Mol object

Options

confld: Conformation ID of the RDKit mol object [int]

opt: With (True) / Without (False) geometry optimization by DFT calculation) [boolean]

work_dir: Working directory [str]

omp: Parallel number of OpenMP in Psi4 [int] memory: Amount of memory usage (MB) in Psi4 [int]

log_name: Prefix of the file name of Psi4 log [str]

opt_method: Calculation method of the geometry optimization [str]

opt_basis: Basis set of the geometry optimization [str]

opt_basis_gen: Basis set of the geometry optimization (for each element) [str] geom iter: Maximum number of iteration in the geometry optimization [int]

geom_conv: Conversion criterion in the geometry optimization [str]

geom_algorithm: Algorithm in the geometry optimization [str]

polar_method: Calculation method of the polarizability calculation [str]

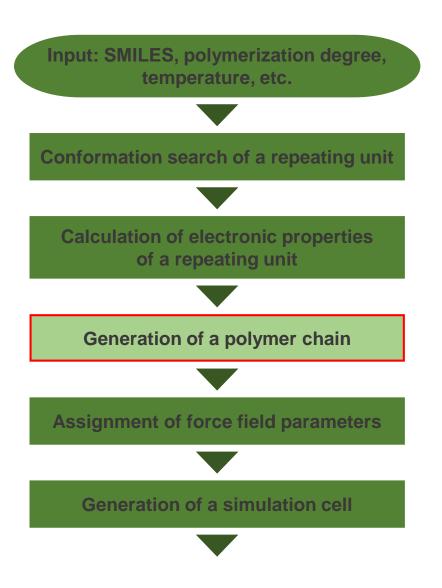
polar_basis: Basis set of the polarizability calculation [str]

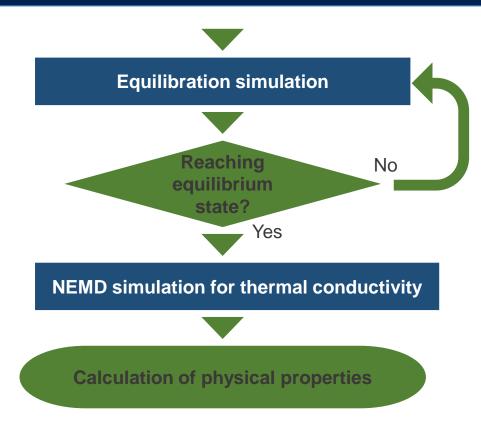
polar_basis_gen: Basis set of the polarizability calculation (for each element) [dict]

Returns

```
dict type qm_polarizability (float, ų) qm_polarizability_xx, qm_polarizability_yy, qm_polarizability_zz, qm_polarizability_xy, qm_polarizability_xz (float, ų)
```

Generation of a polymer chain generation





Polymer chain generation: homopolymer

```
from radonpy.core import poly, utils

smiles = '*CC(*)c1ccccc1'
mol = utils.mol_from_smiles(smiles)
ter = utils.mol_from_smiles('*C')

n = poly.calc_n_from_num_atoms(mol, 1000, terminal1=ter)
homopoly = poly.polymerize_rw(mol, n)
homopoly = poly.terminate_rw(homopoly, ter)
```

poly.calc_n_from_num_atoms(mol, natom, terminal1)

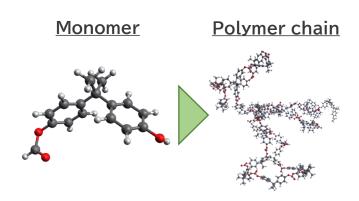
Calculate the degree of polymerization to achieve the specified number of atoms (*natom*)

poly.polymerize_rw(mol, n)

Generation of a polymer chain with self-avoiding random walk

poly.terminate rw(mol, ter)

Termination of a polymer chain



radonpy.core.poly.polymerize_rw

Generation of a homopolymer chain by self-avoiding random walk

mol: RDKit Mol object of repeating unit n: Degree of polymerization [int]

Options

headhead: Connection type of repeating units, head-to-head (True) / head-to-tail (False) [boolean]

confld: Conformation ID of the RDKit mol object [int]

tacticity: Select tacticity (atactic, isotactic, or syndiotactic) [str]

atac_ratio: R/S ratio of atactic polymer [float]

tac_array: Specify the array of R/S isomer [list of boolean]

retry: Maximum number of retry for this function when generating unsuitable structure [int]

retry_step: Maximum number of retry for a random-walk step when generating unsuitable structure [int]

dist_min: Threshold of minimum atom-atom distance (angstrom) [float]

opt: Optimization method in polymer chain growing [str]

Returns

RDKit Mol object

Polymer chain generation: copolymer

Random copolymer

```
n = poly.calc_n_from_num_atoms([mol, mol2], 1000, ratio=[0.5, 0.5], terminal1=ter)
rcopoly = poly.random copolymerize rw([mol, mol2], n, ratio=[0.5, 0.5])
rcopoly = poly.terminate_rw(rcopoly, ter)
```

poly.random_copolymerize_rw(mols, n, ratio)

List of RDKit Mol object of repeating unit mols:

Degree of polymerization [int] n:

Options

ratio: Component ratio [list of float]

Alternating copolymer

```
acopoly = poly.copolymerize_rw([mol, mol2], 20)
acopoly = poly.terminate_rw(acopoly, ter)
```

poly.copolymerize_rw(mols, n)

List of RDKit Mol object of repeating unit mols:

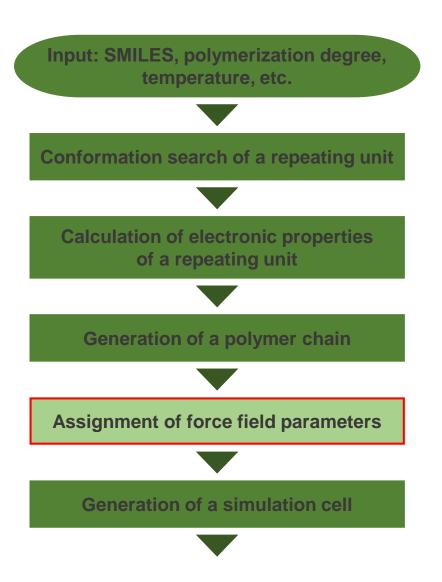
Degree of polymerization [int] n:

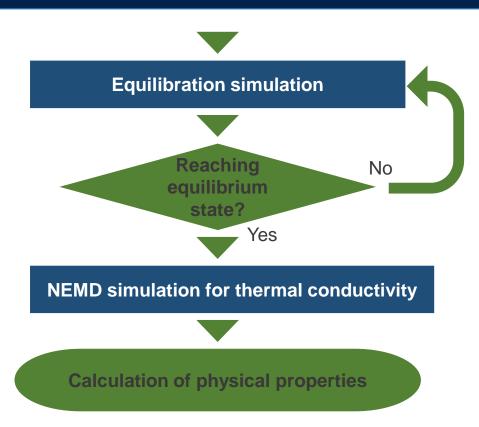
Block copolymer

n:

```
bcopoly = poly.block_copolymerize_rw([mol, mol2], [20, 20])
 bcopoly = poly.terminate rw(bcopoly, ter)
poly.block_copolymerize_rw(mols, n)
mols:
              List of RDKit Mol object of repeating unit
              List of degree of polymerization [list of int]
```

Assignment of force field parameters





Force field assignment

GAFF2 assignment

```
from radonpy.ff.gaff2 import GAFF2

ff = GAFF2()
result = ff.ff_assign(homopoly)
```

- Available elements: H, C, N, O, F, P, S, Cl, Br, I
- Original parameter set of GAFF2
- Return value: True (assignment success) / False (assignment fail)

Modified GAFF2 assignment

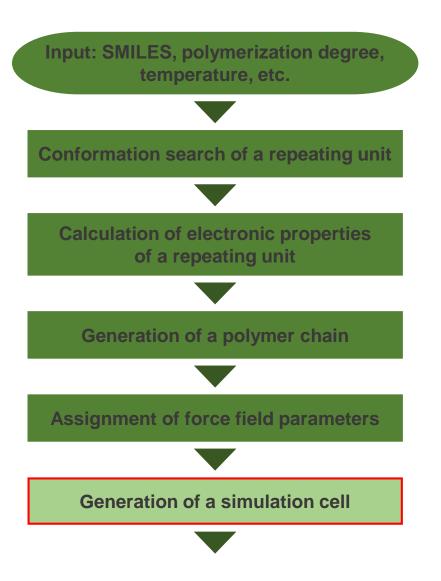
```
from radonpy.ff.gaff2 import GAFF2_mod

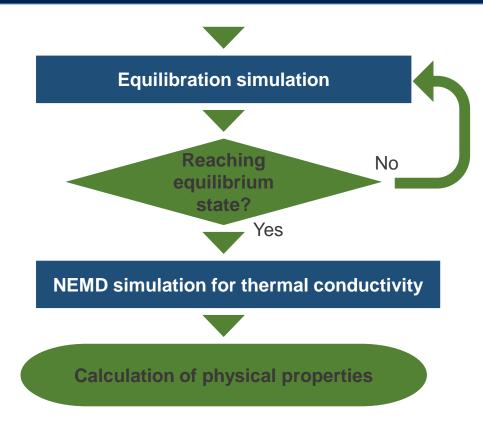
ff = GAFF2_mod()
result = ff.ff_assign(homopoly)
```

- Available elements: H, C, N, O, F, P, S, Cl, Br, I
- Modified parameters are used for fluorocarbon.
 - □ J. Trag, D, Zahn, J. Mol. Model. (2019) 25, 39
- Improving density evaluation of fluorocarbon polymers

Notice: The force field assignment should perform for a polymer chain not for simulation cell because this process is time consuming.

Generation of a simulation cell



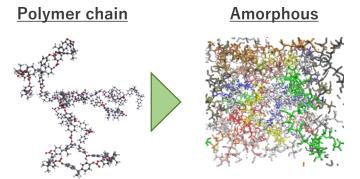


Amorphous cell generation

Generation of simulation cell of amorphous polymers (single component)

ac = poly.amorphous_cell(homopoly, 10, *density*=0.05)

The cell was constructed by randomly arranging and rotating 10 polymer chains such that they did not overlap with each other.



def amorphous_cell(mol, n, cell=None, density=0.03, retry=10, retry_step=100, threshold=2.0, dec_rate=0.8)

mol: RDKit Mol object of repeating unit

n: Number of replication of Mol object [int]

Options

cell: Adding to existing cell [Mol object] density: Density of generating cell [float]

retry: Maximum number of retry for this function when generating unsuitable structure [int]

retry_step: Maximum number of retry for a randomly arranging step when generating unsuitable structure [int]

threshold: Threshold of minimum atom-atom distance (angstrom) [float]

Returns

RDKit Mol object

Amorphous cell generation (mixture)

Generation of simulation cell of amorphous polymers (multi component)

ac = poly.amorphous_mixture_cell([poly1, poly2], [5, 5], density=0.1)

The cell was constructed by randomly arranging and rotating five poly1 and five poly2 such that they did not overlap with each other.

def amorphous_mixture_cell(mols, n, cell=None, density=0.03, retry=10, retry_step=100, threshold=2.0, dec_rate=0.8)

mols: List of RDKit Mol object of repeating unit

n: List of number of replication of Mol object [list of int]

Options

cell: Adding to existing cell [Mol object] density: Density of generating cell [float]

retry: Maximum number of retry for this function when generating unsuitable structure [int]

retry_step: Maximum number of retry for a randomly arranging step when generating unsuitable structure [int]

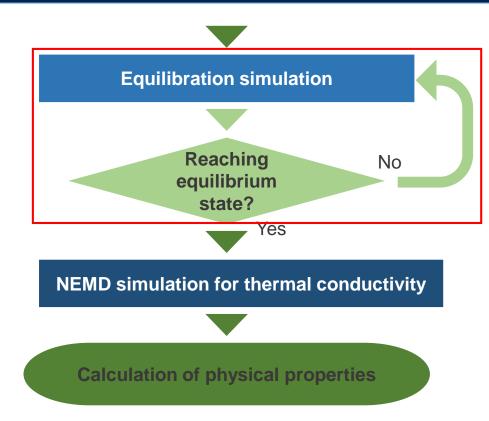
threshold: Threshold of minimum atom-atom distance (angstrom) [float]

Returns

RDKit Mol object

Equilibration simulation

Input: SMILES, polymerization degree, temperature, etc. **Conformation search of a repeating unit Calculation of electronic properties** of a repeating unit Generation of a polymer chain **Assignment of force field parameters** Generation of a simulation cell



radonpy.sim.preset.eq.EQ21step

Preset of equilibration using the 21-steps compression/decompression protocol

```
from radonpy.sim.preset import eq

eqmd = eq.EQ21step(ac, work_dir=work_dir)
ac = eqmd.exec(temp=300, press=1.0, mpi=mpi, omp=omp, gpu=gpu)
```

eq.EQ21step.exec performs following 3 steps:

1. Packing simulation

Increase the density of the amorphous polymers to an appropriate value for subsequent calculations

2. The 21-steps compression/decompression protocol

[G. S. Larsen, P. Lin, K. E. Hart, and C. M. Colina, *Macromolecules* **44**, 6944–6951 (2011).] A temperature rise to 600 K and a drop to 300 K were repeated for approximately 1.5 ns while the system was compressed to 50,000 atm and then decompressed to 1 atm by combining the NVT and NpT simulations

3. NPT equilibration

Run for 5 ns at 300 K and 1 atm

Physical property calculations from EMD

```
from radonpy.sim.preset import eq

eqmd = eq.EQ21step(ac, work_dir=work_dir)
ac = eqmd.exec(temp=300, press=1.0, mpi=mpi, omp=omp, gpu=gpu)

analy = eqmd.analyze()
prop_data = analy.get_all_prop(temp=300, press=1.0, save=True)
result = analy.check_eq()
```

eqmd.analyze()

Return analysis object

analy.get_all_prop(temp=temp, press=press, save=True)

Calculation of physical property from equilibration MD

Return

dict type (containing calculated physical properties)

analy.check_eq()

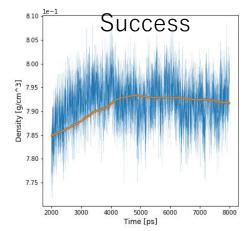
Determines the completion of the relaxation of the equilibration calculation based on

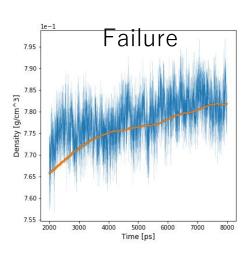
the convergence status for energies, density, and Rg.

This function must be executed after get_all_prop.

Return

Boolean: True (reached equilibrium state)
False (did not reach equilibrium state)





Additional EMD

Preset of additional equilibration

```
from radonpy.sim.preset import eq

eqmd = eq.Additional(ac, work_dir=work_dir)
ac = eqmd.exec(temp=300, press=1.0, mpi=mpi, omp=omp, gpu=gpu)

analy = eqmd.analyze()
prop_data = analy.get_all_prop(temp=300, press=1.0, save=True)
result = analy.check_eq()
```

eq.Additional.exec

NpT simulations were run for 5 ns at 300 K and 1 atm. Interface is the same as EQ21step.

Sample code of EMD

```
from radonpy.sim.preset import eq

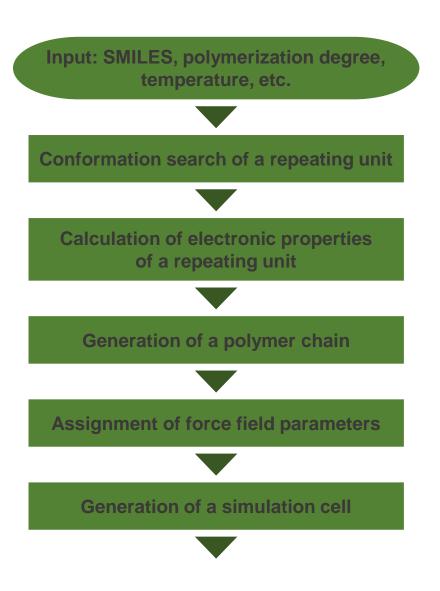
# Equilibration MD
eqmd = eq.EQ21step(ac, work_dir=work_dir)
ac = eqmd.exec(temp=temp, press=press, mpi=mpi, omp=omp, gpu=gpu)

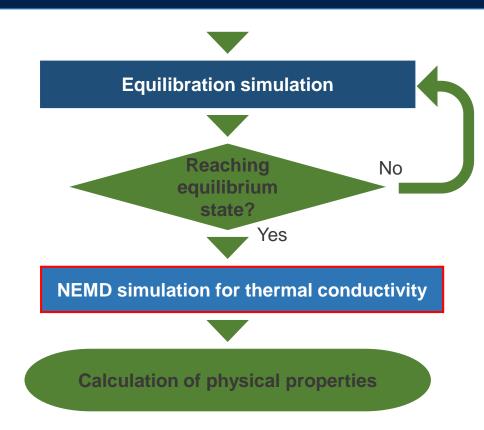
analy = eqmd.analyze()
prop_data = analy.get_all_prop(temp=temp, press=press, save=True)
result = analy.check_eq()

# Additional equilibration MD
for i in range(4):
    if result: break
    eqmd = eq.Additional(ac, work_dir=work_dir)
    ac = eqmd.exec(temp=temp, press=press, mpi=mpi, omp=omp, gpu=gpu)
    analy = eqmd.analyze()
    prop_data = analy.get_all_prop(temp=temp, press=press, save=True)
    result = analy.check_eq()
```

- Packing simulation and the 21-steps equilibration are performed.
- After the 21-steps equilibration, NpT simulations were run for more than 5 ns at 300 K and 1 atm until equilibrium was achieved.
- The achievement of the equilibrium was checked each 5 ns after the 21-steps equilibration.

NEMD simulation for thermal conductivity





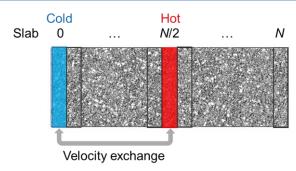
NEMD simulation of thermal conductivity

Preset of thermal conductive NEMD

```
from radonpy.sim.preset import to

nemd = tc.NEMD_MP(mol, work_dir=work_dir, axis='x')
mol = nemd.exec(decomp=True, temp=300, mpi=mpi, omp=omp, gpu=gpu)

nemd_analy = nemd.analyze()
TC = nemd_analy.calc_tc(decomp=True, save=True)
TCdecomp = nemd_analy.TCdecomp_data
```



The heat flux is generated in the system with temperature gradients induced by exchanging the velocity between the coldest atom in slab N/2 and the hottest atom in slab 0.

tc.NEMD_MP(mol, work_dir=work_dir, axis='x')

Setup of thermal conductive NEMD with Müller-Plathe method. axis: specifies the axis of heat flux direction

nemd.exec(decomp=True, temp=temp, mpi=10, omp=1, gpu=0)

Execute thermal conductive NEMD decomp: With (True) / Without (False) decomposition analysis of thermal conductivity

nemd.analyze()

Return analysis object

nemd_analy.calc_tc(decomp=True, save=True)

Calculation of thermal conductivity.

Return

Thermal conductivity (W/mK) [float]

After nemd_analy.calc_tc:

nemd_analy.TCdecomp_data : Results of decomposition analysis [dict]

nemd_analy.Tgrad_data['Tgrad_check']: Result of checking the linearity of temperature gradient [boolean]

nemd_analy.prop_df : Results of thermal conductivity and decomposition analysis [pandas.DataFrame]

Sample code

```
from radonpy.core import utils, poly
from radonpy.ff.gaff2_mod import GAFF2_mod
from radonpy.sim import qm
from radonpy.sim.preset import eq, to
smiles = '*C(C*)c1ccccc1'
ter smiles = '*C'
temp = 300
press = 1.0
omp_psi4 = 10
mpi = 10
omp = 1
apu = 0
mem = 10000
work_dir = './work_dir'
ff = GAFF2_mod()
mol = utils.mol from smiles(smiles)
mol, energy = gm.conformation search(mol, ff=ff, work dir=work dir,
                                     psi4_omp=omp_psi4, mpi=mpi, omp=omp, memory=mem, log_name='monomer1')
# Electronic propety calculation
qm.assign_charges(mol, charge='RESP', opt=False, work_dir=work_dir, omp=omp_psi4, memory=mem, log_name='monomer1')
qm_data = qm.sp_prop(mol, opt=False, work_dir=work_dir, omp=omp_psi4, memory=mem, log_name='monomer1')
polar_data = qm.polarizability(mol, opt=False, work_dir=work_dir, omp=omp_psi4, memory=mem, log_name='monomer1')
# RESP charge calculation of a termination unit
ter = utils.mol from smiles(ter smiles)
qm.assign_charges(ter, charge='RESP', opt=True, work_dir=work_dir, omp=omp_psi4, memory=mem, log_name='ter1')
# Generate polymer chain
dp = poly.calc_n_from_num_atoms(mol, 1000, terminal1=ter)
homopoly = poly.polymerize_rw(mol, dp, tacticity='atactic')
homopoly = poly.terminate_rw(homopoly, ter)
```

Sample code (continued)

```
# Force field assignment
result = ff.ff assign(homopoly)
if not result:
  print('[ERROR: Can not assign force field parameters.]')
# Generate simulation cell
ac = poly.amorphous cell(homopoly, 10, density=0.05)
# Equilibration MD
egmd = eq.EQ21step(ac, work dir=work dir)
ac = eqmd.exec(temp=temp, press=1.0, mpi=mpi, omp=omp, qpu=qpu)
analy = eqmd.analyze()
prop data = analy.get all prop(temp=temp, press=1.0, save=True)
result = analy.check_eq()
# Additional equilibration MD
for i in range(4):
  if result: break
  egmd = eq.Additional(ac, work dir=work dir)
  ac = eqmd.exec(temp=temp, press=press, mpi=mpi, omp=omp, gpu=gpu)
  analy = eqmd.analyze()
  prop data = analy.get all prop(temp=temp, press=press, save=True)
  result = analy.check_eq()
if not result:
  print('[ERROR: Did not reach an equilibrium state.]')
# Non-equilibrium MD for thermal condultivity
  nemd = tc.NEMD MP(ac, work dir=work dir)
  ac = nemd.exec(decomp=True, temp=temp, mpi=mpi, omp=omp, qpu=qpu)
  nemd analy = nemd.analyze()
  TC = nemd analy.calc tc(decomp=True, save=True)
  if not nemd analy.Tgrad data['Tgrad check']:
    print('[ERROR: Low linearity of temperature gradient.]')
  print('Thermal conductivity: %f' % TC)
```

Calculation results of physical properties

Appendix

Calculations of physical properties

Specific heat capacity

$$Cp = \frac{\langle \delta H^2 \rangle}{mk_B T^2}$$

Static dielectric constant

$$\varepsilon = 1 + \frac{\langle \boldsymbol{\mu}^2 \rangle - \langle \boldsymbol{\mu} \rangle^2}{3\varepsilon_0 V k_B T^2}$$

Compressibility

$$\beta_T = \frac{\langle \delta V^2 \rangle}{V k_B T}$$

Bulk modulus

$$K_T = \frac{1}{\beta_T}$$

Thermal expansion $\alpha_P = \frac{\langle \delta H \cdot \delta V \rangle}{V k_B T^2}$ coefficient

$$\alpha_P = \frac{\langle \delta H \cdot \delta V \rangle}{V k_B T^2}$$

Linear expansion coefficient

$$\alpha_{lx} = \frac{\alpha_P}{3}$$
 (isotropic)

$$\alpha_{lx} = \frac{\langle \delta H \cdot \delta L_x \rangle}{L_x k_B T^2}$$
 (anisotropic)

Self-diffusion coefficient

$$D = \frac{\langle |\mathbf{x}(t+t_0) - \mathbf{x}(t_0)|^2 \rangle}{6t}$$

Refractive index

$$\frac{n^2 - 1}{n^2 + 2} = \frac{4\pi}{3} \frac{\rho}{M} \alpha_{polar}$$

Unit of physical property in RadonPy

Physical property	Unit
Density	g/cm ³
Radius of gyration	Å
Cp, Cv	J/kg K
Compressibility	Pa ⁻¹
Bulk modulus	Pa
Volume expansion coeff., Linear expansion coeff.	K ⁻¹
Self-diffusion coeff.	m^2/s
Thermal conductivity	W/m K
Thermal diffusivity	m^2/s