

Assignment-1

EE224BTECH11044 - Muthyala koushik*

1.Section-B : JEE Main/AIEEE

- 4) If $f : \mathbb{R} \rightarrow \mathbb{R}$ satisfies $f(x+y) = f(x) + f(y)$ for all $x, y \in \mathbb{R}$ and $f(1) = 7$, then $\sum_{r=1}^n f(r)$ is [2003]

a) $\frac{7n(n+1)}{2}$

b) $\frac{7n}{2}$

c) $\frac{7(n+1)}{2}$

d) $7n + (n+1)$

- 5) The function f from the set of natural numbers to integers is defined by

$$f(n) = \begin{cases} \frac{n-1}{2} & \text{when } n \text{ is odd,} \\ -\frac{n}{2} & \text{when } n \text{ is even.} \end{cases}$$

is

- a) neither one-one nor onto
b) one-one but not onto
c) onto but not one-one
d) one-one and onto both.

- 6) The range of the function $f(x) = 7 - x \cdot P \cdot x - 3$ is [2004]

- a) $\{1, 2, 3, 4, 5\}$
b) $\{1, 2, 3, 4, 5, 6\}$
c) $\{1, 2, 3, 4\}$
d) $\{1, 2, 3\}$

- 7) If $f : R \rightarrow S$, defined by $f(x) = \sin x - \sqrt{3} \cos x + 1$, is onto, then the interval of S is [2004]

- a) $[-1, 3]$
b) $[-1, 1]$
c) $[0, 1]$
d) $[0, 3]$

- 8) The graph of the function $y=f(x)$ is symmetrical about the line $x=2$, then [2004]

- a) $f(x) = -f(-x)$
b) $f(2+x) = f(2-x)$
c) $f(x) = f(-x)$
d) $f(x+2) = f(x-2)$

- 9) The domain of the function $f(x) = \frac{\sin^{-1}(x-3)}{\sqrt{9-x^2}}$ is [2004]

- a) $[1, 3]$
b) $[2, 3]$
c) $[1, 2]$
d) $[2, 3]$

- 10) Let $f : (-1, 1) \rightarrow B$, be a function defined by $f(x) = \tan^{-1} \frac{2x}{1-x^2}$, then f is both one-one and onto when B is the interval [2005]

a) $(0, \frac{\pi}{2})$

b) $[0, \frac{\pi}{2})$

c) $[-\frac{\pi}{2}, \frac{\pi}{2}]$

d) $(-\frac{\pi}{2}, \frac{\pi}{2})$

- 11) A function is matched below against an interval where it is supposed to be increasing. Which of the following pairs is incorrectly matched? [2005]

Interval	Function
a) $(-\infty, \infty)$	$x^3 - 3x^2 + 3x + 3$
b) $[2, \infty)$	$2x^3 - 3x^2 + 3x + 3$
c) $(-\infty, \frac{1}{3}]$	$3x^2 - 2x + 1$
d) $(-\infty, -4)$	$x^3 + 6x^2 + 6$

- 12) A real valued function $f(x)$ satisfies the functional equation

$$f(x-y) = f(x)f(y) - f(a-x)f(a+y)$$

where a is a given constant and $f(0)=1, f(2a-x)$ is equal to [2005]

- a) $-f(x)$
b) $f(x)$
c) $f(a) + f(a-x)$
d) $f(-x)$

- 13) The Largest interval lying in $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$ for which the function, $f(x) = 4^{-x^2} + \cos^{-1}\left(\frac{x}{2} - 1\right) + \log(\cos x)$, is defined, is [2007]
- $\left[-\frac{\pi}{4}, \frac{\pi}{2}\right)$
 - $\left[0, \frac{\pi}{2}\right)$
 - $[0, \pi]$
 - $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$
- 14) Let $f : N \rightarrow Y$ be a function defined as $f(x) = 4x + 3$ where $Y = \{y \in \mathbb{N} : y = 4x + 3 \text{ for some } x \in \mathbb{N}\}$. Show that f is invertible and its inverse is [2008]
- $g(y) = \frac{3y+4}{3}$
 - $g(y) = 4 + \frac{y+3}{4}$
 - $g(y) = \frac{y+3}{4}$
 - $g(y) = \frac{y-3}{4}$
- 15) Let $f(x) = (x+1)^2 - 1, x \leq -1$
Statement-1: The set $\{x : f(x) = f^{-1}(x)\} = \{0, -1\}$
Statement-2: f is a bijection. [2009]
- Statement-1 is true, Statement-2 is true. Statement-2 is not a correct explanation for Statement-1.
 - Statement-1 is true, Statement-2 is false.
 - Statement-1 is false, Statement-2 is true.
 - Statement-1 is true, Statement-2 is true. Statement-2 is not a correct explanation for Statement-1.
- 16) For real x , let $f(x) = x^3 + 5x + 1$, then [2009]
- f is onto \mathbb{R} but not one-one
 - f is one-one and onto \mathbb{R}
 - f is neither one-one nor onto \mathbb{R}
 - f is one-one but not onto \mathbb{R}
- 17) The domain of the function $f(x) = \frac{1}{\sqrt{|x|-x}}$ is [2011]
- $(0, \infty)$
 - $(-\infty, 0)$
 - $(-\infty, \infty) - \{0\}$
 - $(-\infty, \infty)$
- 18) $x \in \mathbb{R} - \{0, 1\}$, let $f_1(x) = \frac{1}{x}, f_2(x) = 1 - x$ and $f_3(x) = \frac{1}{1-x}$ be the three given functions. If a function, $J(X)$ satisfies $(f_2 \circ J \circ f_1)(x) = f_3(x)$ then $J(x)$ is equal to: [JEE M 2019-9 Jan(M)]
- $f_3(x)$
 - $f_3(x)$
 - $f_2(x)$
 - $f_1(x)$