

Домашнє завдання №17

Скласти програму (C/C++), яка дозволяє знаходити мінімальне кістякове дерево(англ. *minimum spanning tree*) для заданого графу за допомогою алгоритму Крускала.

Вибір варіанту

$$(N_{\text{ж}} + N_{\text{г}} + 1) \% 2 + 1$$

де: $N_{\text{ж}}$ – порядковий номер студента в групі, а $N_{\text{г}}$ – номер групи(1,2,3,4,5,6,7,8 або 9)

Варіанти завдань

Варіант	Кількість вершин графу
1	4
2	5

Приклад коду

Програма відображає заданий граф та мінімальне кістякове дерево(отримане після виконання алгоритму Крускала) у вигляді матриць суміжності(англ. *adjacency matrix*), в яких замість чисел 0 і 1(відсутність або присутність ребра), містяться ваги ребер(на відсутність ребра вказує значення NE – not exist).

Кількість вершин графу у прикладі	7
Макровизначення	<code>#define VERTEX_COUNT 7</code>

Лістинг

```
#include <stdio.h>
#include <stdlib.h>
#include <string.h>

#define VERTEX_COUNT 7
#define MAX_VERTEX_COUNT 8

#define UNDIRECT_BEHAVIOR

#define NE (~0) // NOT EXIST
#define NA NE // NOT AVAILABLE

#define EDGE_VALUES {\
/*****V0**V1**V2**V3**V4**V5**V6**V7*/\
/*V0*/{NA, 7, NE, 5, NE, NE, NE, NE},\
/*V1*/{NA, NA, 8, 9, 7, NE, NE, NE},\
/*V2*/{NA, NA, NA, NE, 5, NE, NE, NE},\
/*V3*/{NA, NA, NA, NA, 15, 6, NE, NE},\
/*V4*/{NA, NA, NA, NA, NA, 8, 9, NE},\
/*V5*/{NA, NA, NA, NA, NA, NA, 11, NE},\
/*V6*/{NA, NA, NA, NA, NA, NA, NA, NE},\
/*V7*/{NA, NA, NA, NA, NA, NA, NA, NA}\
}
```

```

typedef struct EdgeStruct {
    unsigned int sourceVertexIndex;
    unsigned int destinationVertexIndex;
    int weight;
} Edge;

typedef struct EdgesStruct {
    unsigned int vertexCount;
    unsigned int edgeCount;
    unsigned int reservedEdgeCount;
    Edge* items;
} Edges;

Edges* createEdges(int edgeValues[MAX_VERTEX_COUNT][MAX_VERTEX_COUNT], int vertexCount) {
    int edgeIndex, iIndex, jIndex;

    Edges* edges = (Edges*)malloc(sizeof(Edges));
    edges->vertexCount = vertexCount;

    edges->edgeCount = 0;
    for (iIndex = 0; iIndex < vertexCount; ++iIndex) {
#ifdef UNDIRECT_BEHAVIOR
        jIndex = iIndex + 1;
#else
        jIndex = 0;
#endif
        for (jIndex = 0; jIndex < vertexCount; ++jIndex) {
            if (edgeValues[iIndex][jIndex] != NE) {
                ++edges->edgeCount;
            }
        }
    }
    edges->reservedEdgeCount = edges->edgeCount;

    edges->items = (Edge*)malloc(edges->edgeCount * sizeof(Edge));

    edgeIndex = 0;
    for (iIndex = 0; iIndex < vertexCount; ++iIndex) {
#ifdef UNDIRECT_BEHAVIOR
        jIndex = iIndex + 1;
#else
        jIndex = 0;
#endif
        for (; jIndex < vertexCount; ++jIndex) {
            if (edgeValues[iIndex][jIndex] != NE) {
                edges->items[edgeIndex].sourceVertexIndex = iIndex;
                edges->items[edgeIndex].destinationVertexIndex = jIndex;
                edges->items[edgeIndex].weight = edgeValues[iIndex][jIndex];
                ++edgeIndex;
            }
        }
    }

    return edges;
}

void destroyEdges(Edges* edges) {
    if (edges) {
        free(edges->items);
        free(edges);
    }
}

typedef struct SubsetStruct {

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    unsigned int parent;
    unsigned int rank;
} Subset;

unsigned int find(Subset * subsets, unsigned int index) {
    if (subsets[index].parent != index) {
        subsets[index].parent = find(subsets, subsets[index].parent);
    }

    return subsets[index].parent;
}

void mergeSubsets(Subset * subsets, unsigned int first, unsigned int second) {
    unsigned int firstRoot = find(subsets, first);
    unsigned int secondRoot = find(subsets, second);

    if (subsets[firstRoot].rank < subsets[secondRoot].rank) {
        subsets[firstRoot].parent = secondRoot;
    }
    else if (subsets[firstRoot].rank > subsets[secondRoot].rank) {
        subsets[secondRoot].parent = firstRoot;
    }
    else {
        subsets[secondRoot].parent = firstRoot;
        ++subsets[firstRoot].rank;
    }
}

int edgeCompare(const void* a, const void* b){
    return ((Edge*)a)->weight > ((Edge*)b)->weight;
}

Edges* KruskalMST(Edges* edges) {
    unsigned int resultEdgeIndex;
    unsigned int edgeIndex;
    unsigned int first;
    unsigned int second;
    unsigned int vertexIndex;
    Subset* subsets;
    Edge next_edge;
    Edges* result;

    if (!edges) {
        return NULL;
    }

    result = (Edges*)malloc(sizeof(Edges));
    if (!result) {
        return NULL;
    }
    result->vertexCount = edges->vertexCount;
    result->reservedEdgeCount = edges->vertexCount;
    result->items = (Edge*)malloc(edges->vertexCount * sizeof(Edge));

    qsort(edges->items, edges->edgeCount, sizeof(Edge), edgeCompare);

    subsets = (Subset*)malloc(edges->vertexCount * sizeof(Subset));

    for (vertexIndex = 0; vertexIndex < edges->vertexCount; ++vertexIndex){
        subsets[vertexIndex].parent = vertexIndex;
        subsets[vertexIndex].rank = 0;
    }

    for (resultEdgeIndex = 0, edgeIndex = 0; resultEdgeIndex + 1 < edges->vertexCount
    && edgeIndex < edges->edgeCount;) {

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        next_edge = edges->items[edgeIndex++];

        first = find(subsets, next_edge.sourceVertexIndex);
        second = find(subsets, next_edge.destinationVertexIndex);

        if (first != second){
            result->items[resultEdgeIndex++] = next_edge;
            mergeSubsets(subsets, first, second);
        }
    }

    result->edgeCount = resultEdgeIndex;

    free(subsets);

    return result;
}

void printGraphEdge(const char* title, Edges* edges) {
    int printEdgeValues[MAX_VERTEX_COUNT][MAX_VERTEX_COUNT] = { 0 };

    unsigned int edgeIndex, iIndex, jIndex;

    if (!edges || !edges->items) {
        return;
    }

    for (iIndex = 0; iIndex < edges->vertexCount; ++iIndex) {
        for (jIndex = 0; jIndex < edges->vertexCount; ++jIndex) {
            printEdgeValues[iIndex][jIndex] = NE;
        }
    }

    for (edgeIndex = 0; edgeIndex < edges->edgeCount; ++edgeIndex) {
        printEdgeValues[edges->items[edgeIndex].sourceVertexIndex %
MAX_VERTEX_COUNT][edges->items[edgeIndex].destinationVertexIndex % MAX_VERTEX_COUNT] =
edges->items[edgeIndex].weight;
    }

    printf("%s\r\n", title);
    for (jIndex = 0; jIndex < edges->vertexCount; ++jIndex) {
        printf(" V%-2d", jIndex);
    }
    printf("\r\n");
    for (iIndex = 0; iIndex < edges->vertexCount; ++iIndex) {
        printf("V%-2d", iIndex);
        for (jIndex = 0; jIndex < edges->vertexCount; ++jIndex) {
            if (jIndex) {
                printf(",");
            }
            printf(" ");
#ifdef UNDIRECT_BEHAVIOR
            if (iIndex < jIndex) {
                if (printEdgeValues[iIndex][jIndex] != NE) {
                    printf("%-2d", printEdgeValues[iIndex][jIndex]);
                }
                else {
                    printf("NE");
                }
            }
#ifdef UNDIRECT_BEHAVIOR
        }
        else {
            printf("NA");
        }
    }
}

```

```
#endif
        }
        printf("\r\n");
    }
    printf("\r\n");
}

int main() {
    int edgeValues[MAX_VERTEX_COUNT][MAX_VERTEX_COUNT] = EDGE_VALUES;
    Edges* edges = createEdges(edgeValues, VERTEX_COUNT), *spanningTreeEdges;
    if (!edges) {
        return 1;
    }

    spanningTreeEdges = KruskalMST(edges);
    if (!spanningTreeEdges) {
        destroyEdges(edges);
        return 1;
    }

    printGraphEdge("Graph:", edges);

    printGraphEdge("Spanning tree:", spanningTreeEdges);

    destroyEdges(edges);
    destroyEdges(spanningTreeEdges);

#ifdef __linux__
    (void)getchar();
#elif defined(_WIN32)
    system("pause");
#else
#endif

    return 0;
}
```