1.
$$\sin \alpha = \frac{a}{c}$$
; $\cos \alpha = \frac{b}{c}$; $\operatorname{tg} \alpha = \frac{a}{b}$; $\operatorname{ctg} \alpha = \frac{b}{a}$; $(a, b - \operatorname{catetele}, c - \operatorname{ipotenuza} \operatorname{triunghiului} \operatorname{dreptunghic}, \alpha - \operatorname{unghiul}, \operatorname{opus} \operatorname{catetel} a)$.

2.
$$\operatorname{tg} \alpha = \frac{\sin \alpha}{\cos \alpha}$$
; $\operatorname{ctg} \alpha = \frac{\cos \alpha}{\sin \alpha}$.

3.
$$tg \alpha ctg \alpha = 1$$
.

4.
$$\sin\left(\frac{\pi}{2} \pm \alpha\right) = \cos \alpha$$
; $\sin(\pi \pm \alpha) = \mp \sin \alpha$.

5.
$$\cos\left(\frac{\pi}{2} \pm \alpha\right) = \mp \sin \alpha; \quad \cos(\pi \pm \alpha) = -\cos \alpha.$$

6.
$$\operatorname{tg}\left(\frac{\pi}{2} \pm \alpha\right) = \mp \operatorname{ctg}\alpha; \quad \operatorname{ctg}\left(\frac{\pi}{2} \pm \alpha\right) = \mp \operatorname{tg}\alpha.$$

7.
$$\sec\left(\frac{\pi}{2} \pm \alpha\right) = \mp \csc \alpha$$
; $\csc\left(\frac{\pi}{2} \pm \alpha\right) = \sec \alpha$.

8.
$$\sin^2 \alpha + \cos^2 \alpha = 1$$
.

9.
$$1 + \operatorname{tg}^2 \alpha = \sec^2 \alpha$$
.

10.
$$1 + \operatorname{ctg}^2 \alpha = \operatorname{cosec}^2 \alpha$$
.

11.
$$\sin(\alpha \pm \beta) = \sin \alpha \cos \beta \pm \sin \beta \cos \alpha$$
.

12.
$$\cos(\alpha \pm \beta) = \cos \alpha \cos \beta \mp \sin \alpha \sin \beta$$
.

13.
$$\operatorname{tg}(\alpha \pm \beta) = \frac{\operatorname{tg} \alpha \pm \operatorname{tg} \beta}{1 \mp \operatorname{tg} \alpha \operatorname{tg} \beta}$$

14.
$$\operatorname{ctg}(\alpha \pm \beta) = \frac{\operatorname{ctg} \alpha \operatorname{ctg} \beta \mp 1}{\operatorname{ctg} \beta \pm \operatorname{ctg} \alpha}$$
.

15.
$$\sin 2\alpha = 2\sin \alpha \cos \alpha$$
.

16.
$$\cos 2\alpha = \cos^2 \alpha - \sin^2 \alpha$$
.

17.
$$\operatorname{tg} 2\alpha = \frac{2\operatorname{tg} \alpha}{1 - \operatorname{tg}^2 \alpha}$$
.

18.
$$\operatorname{ctg} 2\alpha = \frac{\operatorname{ctg}^2 \alpha - 1}{2 \operatorname{ctg} \alpha}$$
.

19.
$$\sin 3\alpha = 3\sin \alpha - 4\sin^3 \alpha$$
.

$$20. \cos 3\alpha = 4\cos^3 \alpha - 3\cos \alpha.$$

$$21. \ \left| \sin \frac{\alpha}{2} \right| = \sqrt{\frac{1 - \cos \alpha}{2}}.$$

$$22. \left| \cos \frac{\alpha}{2} \right| = \sqrt{\frac{1 + \cos \alpha}{2}}.$$

23.
$$\left| \operatorname{tg} \frac{\alpha}{2} \right| = \sqrt{\frac{1 - \cos \alpha}{1 + \cos \alpha}}.$$

24.
$$\operatorname{tg} \frac{\alpha}{2} = \frac{\sin \alpha}{1 + \cos \alpha} = \frac{1 - \cos \alpha}{\sin \alpha}.$$

25.
$$\left| \operatorname{ctg} \frac{\alpha}{2} \right| = \sqrt{\frac{1 + \cos \alpha}{1 - \cos \alpha}}.$$

26.
$$\operatorname{ctg} \frac{\alpha}{2} = \frac{\sin \alpha}{1 - \cos \alpha} = \frac{1 + \cos \alpha}{\sin \alpha}$$
.

$$27. \ 1 + \cos \alpha = 2\cos^2 \frac{\alpha}{2}.$$

$$28. \ 1 - \cos \alpha = 2\sin^2 \frac{\alpha}{2}.$$

29.
$$\sin \alpha \pm \sin \beta = 2 \sin \frac{\alpha \pm \beta}{2} \cos \frac{\alpha \mp \beta}{2}$$
.

30.
$$\cos \alpha + \cos \beta = 2 \cos \frac{\alpha + \beta}{2} \cos \frac{\alpha - \beta}{2}$$
.

31.
$$\cos \alpha - \cos \beta = -2\sin \frac{\alpha + \beta}{2}\sin \frac{\alpha - \beta}{2}$$
.

32.
$$\operatorname{tg} \alpha \pm \operatorname{tg} \beta = \frac{\sin(\alpha \pm \beta)}{\cos \alpha \cos \beta}$$

33.
$$\operatorname{ctg} \alpha \pm \operatorname{ctg} \beta = \frac{\sin(\beta \pm \alpha)}{\sin \alpha \sin \beta}$$
.

34.
$$\sin \alpha \sin \beta = \frac{1}{2} [\cos(\alpha - \beta) - \cos(\alpha + \beta)].$$

35.
$$\sin \alpha \cos \beta = \frac{1}{2} [\sin(\alpha + \beta) + \sin(\alpha - \beta)].$$

36.
$$\cos \alpha \cos \beta = \frac{1}{2} [\cos(\alpha + \beta) + \cos(\alpha - \beta)].$$

37. Ecuatii trigonometrice elementare:

$$\sin x = a, |a| \le 1; x = (-1)^n \arcsin a + \pi n;
\cos x = a, |a| \le 1; x = \pm \arccos a + 2\pi n;
\operatorname{tg} x = a, x = \operatorname{arctg} a + \pi n;
\operatorname{ctg} x = a, x = \operatorname{arcctg} a + \pi n$$

$$n \in \mathbb{Z}.$$

38.
$$\arcsin x + \arccos x = \frac{\pi}{2}, \quad |x| \le 1.$$

39.
$$\operatorname{arctg} x + \operatorname{arcctg} x = \frac{\pi}{2}$$
.

40.
$$\operatorname{arcsec} x + \operatorname{arccosec} x = \frac{\pi}{2}, \quad |x| \ge 1.$$

41.
$$\sin(\arcsin x) = x$$
, $x \in [-1; +1]$.

42.
$$\arcsin(\sin x) = x$$
, $x \in \left[-\frac{\pi}{2}; \frac{\pi}{2}\right]$.

43.
$$\cos(\arccos x) = x, \quad x \in [-1; +1].$$

44.
$$\arccos(\cos x) = x$$
, $x \in [0; \pi]$.

45.
$$\operatorname{tg}(\operatorname{arctg} x) = x, \quad x \in \mathbb{R}.$$

46.
$$\operatorname{arctg}(\operatorname{tg} x) = x, \quad x \in \left(-\frac{\pi}{2}; \frac{\pi}{2}\right).$$

47.
$$\operatorname{ctg}(\operatorname{arcctg} x) = x, \quad x \in \mathbb{R}.$$

48.
$$\operatorname{arcctg}(\operatorname{ctg} x) = x, \quad x \in (0; \pi).$$

49.
$$\arcsin x = \arccos \sqrt{1 - x^2} = \arctan \frac{x}{\sqrt{1 - x^2}} = \operatorname{arcctg} \frac{\sqrt{1 - x^2}}{x}, \quad 0 < x < 1.$$

50.
$$\arccos x = \arcsin \sqrt{1 - x^2} = \arctan \frac{\sqrt{1 - x^2}}{x} = \arctan \frac{x}{\sqrt{1 - x^2}}, \quad 0 < x < 1.$$

51.
$$\arctan x = \arcsin \frac{x}{\sqrt{1+x^2}} = \arccos \frac{1}{\sqrt{1+x^2}} = \arctan \frac{1}{x}, \quad 0 < x < +\infty.$$

52.
$$\arctan x = \arcsin \frac{1}{\sqrt{1+x^2}} = \arccos \frac{x}{\sqrt{1+x^2}} = \arctan \frac{1}{x}, \quad 0 < x < +\infty.$$

53.
$$\arcsin x + \arcsin y = \begin{bmatrix} \arcsin(x\sqrt{1-y^2} + y\sqrt{1-x^2}), & \text{daca } xy \le 0 \text{ sau } x^2 + y^2 \le 1; \\ \pi - \arcsin(x\sqrt{1-y^2} + y\sqrt{1-x^2}), & \text{daca } x > 0, \ y > 0 \text{ si } x^2 + y^2 > 1; \\ -\pi - \arcsin(x\sqrt{1-y^2} + y\sqrt{1-x^2}), & \text{daca } x < 0, y < 0 \text{ si } x^2 + y^2 > 1. \end{bmatrix}$$

$$54. \arcsin x - \arcsin y = \begin{bmatrix} \arcsin(x\sqrt{1 - y^2} - y\sqrt{1 - x^2}), & \text{daca } xy \ge 0 \text{ sau } x^2 + y^2 \le 1; \\ \pi - \arcsin(x\sqrt{1 - y^2} - y\sqrt{1 - x^2}), & \text{daca } x > 0, y < 0 \text{ si } x^2 + y^2 > 1; \\ -\pi - \arcsin(x\sqrt{1 - y^2} - y\sqrt{1 - x^2}), & \text{daca } x < 0, y > 0 \text{ si } x^2 + y^2 > 1. \end{bmatrix}$$

55.
$$\arccos x + \arccos y = \begin{bmatrix} \arccos(xy - \sqrt{(1-x^2)(1-y^2)}), & \operatorname{daca} x + y \ge 0; \\ 2\pi - \arccos(xy - \sqrt{(1-x^2)(1-y^2)}), & \operatorname{daca} x + y < 0. \end{bmatrix}$$

56.
$$\arccos x - \arccos y = \begin{bmatrix} -\arccos(xy + \sqrt{(1-x^2)(1-y^2)}), & \text{daca } x \ge y; \\ \arccos(xy + \sqrt{(1-x^2)(1-y^2)}), & \text{daca } x < y. \end{bmatrix}$$

57.
$$\operatorname{arctg} x + \operatorname{arctg} y = \begin{bmatrix} \operatorname{arctg} \frac{x+y}{1-xy}, & \operatorname{daca} xy < 1; \\ \pi + \operatorname{arctg} \frac{x+y}{1-xy}, & \operatorname{daca} x > 0 \text{ si } xy > 1; \\ -\pi + \operatorname{arctg} \frac{x+y}{1-xy}, & \operatorname{daca} x < 0 \text{ si } xy > 1. \end{bmatrix}$$

$$58. \ \operatorname{arctg} x - \operatorname{arctg} y = \begin{bmatrix} \operatorname{arctg} \frac{x-y}{1+xy}, & \operatorname{daca} xy > -1; \\ \pi + \operatorname{arctg} \frac{x-y}{1+xy}, & \operatorname{daca} x > 0 \text{ si } xy < -1; \\ -\pi + \operatorname{arctg} \frac{x-y}{1+xy}, & \operatorname{daca} x < 0 \text{ si } xy < -1. \end{bmatrix}$$

$$59. \ 2\arcsin x = \begin{bmatrix} \arcsin(2x\sqrt{1-x^2}), & \operatorname{daca} |x| \le \frac{\sqrt{2}}{2}; \\ \pi - \arcsin(2x\sqrt{1-x^2}), & \operatorname{daca} \frac{\sqrt{2}}{2} < x \le 1; \\ -\pi - \arcsin(2x\sqrt{1-x^2}), & \operatorname{daca} - 1 \le x < -\frac{\sqrt{2}}{2}. \end{bmatrix}$$

60.
$$2\arccos x = \begin{bmatrix} \arccos(2x^2 - 1) & \text{cand } 0 \le x \le 1; \\ 2\pi - \arccos(2x^2 - 1) & \text{cand } -1 \le x < 0. \end{bmatrix}$$

$$61. \ 2 \operatorname{arctg} x = \begin{bmatrix} \operatorname{arctg} \frac{2x}{1 - x^2}, & \operatorname{daca} |x| < 1; \\ \pi + \operatorname{arctg} \frac{2x}{1 - x^2}, & \operatorname{daca} x > 1; \\ -\pi + \operatorname{arctg} \frac{2x}{1 - x^2}, & \operatorname{daca} x < -1. \end{bmatrix}$$

62.
$$\frac{1}{2}\arcsin x = \begin{bmatrix} \arcsin\sqrt{\frac{1-\sqrt{1-x^2}}{2}}, & \text{daca } 0 \le x \le 1; \\ -\arcsin\sqrt{\frac{1-\sqrt{1-x^2}}{2}}, & \text{daca } -1 \le x < 0. \end{bmatrix}$$

63.
$$\frac{1}{2}\arccos x = \arccos\sqrt{\frac{1+x}{2}}$$
, daca $-1 \le x \le 1$.

64.
$$\frac{1}{2} \operatorname{arctg} x = \begin{bmatrix} \operatorname{arctg} \frac{\sqrt{1+x^2}-1}{x}, & \operatorname{daca} x \neq 0; \\ 0, & \operatorname{daca} x = 0. \end{bmatrix}$$