EC 425/525, Set 2

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Prologue

Schedule

Last time

Research basics, our class, and R

Today

Admin: Canvas exists. Updated class website.

Material: The Rubin causal model (not mine), Chapter 2 MHE. R basics.

Assignment₁ Install R and RStudio on your computer.

Assignment₂ Take 15 minutes to quietly think about your interests.

Future

Lab: Matrix work, regression, functions, simulation

Long run: Deepen understandings/intuitions for causality and inference.

Review

Research fundamentals

Review

Research fundamentals

Angrist and Pischke provide four **fundamental questions for research**:

- 1. What is the **causal relationship of interest**?
- 2. How would an **ideal experiment** capture this causal effect of interest?
- 3. What is your **identification strategy**?
- 4. What is your **mode of inference**?

Seemingly straightforward questions can be fundamentally unanswerable.

Review

General research recommendations

More unsolicited advice:

- Be curious.
- Ask questions.
- Attend seminars.
- Meet faculty (UO + visitors).
- Focus on learning—especially intuition.[†]
- Be kind and constructive.

[†] Learning is not always the same as getting good grades.

What's so great about experiments?

Science widely regards **experiments** as the gold standard for research.

But why? The costs can be substantial.

Costs

- slow and expensive
- heavily regulated by review boards
- can abstract away from the actual question/setting

Benefits

So the benefits need to be pretty large, right?

Example: Hospitals and health

Imagine we want to know the causal effect of hospitals on health.

Research question

Within the population of poor, elderly individuals, does visiting the emergency room for primary care improve health?

Empirical exercise

- 1. Collect data on health status and hospital visits.
- 2. Summarize health status by hospital-visit group.

Example: Hospitals and health

Our empirical exercise from the 2005 National Health Inteview Survey:

Group	Sample Size	Mean Health Status	Std. Error
Hospital	7,774	3.21	0.014
No hospital	90,049	3.93	0.003

We get a t statistic of 58.9 when testing a difference in groups' means (0.72).

Conclusion? Hospitals make folks worse. Hospitals make sick people sicker.

Alternative conclusion: Perhaps we're making a mistake in our analysis... maybe sick people go to hospitals?

Potential outcomes framework

Let's develop a framework to better discuss the problem here.

- ullet Binary treatment variable (e.g., hospitalized): $\mathbf{D}_i = 0, 1$
- Outcome for individual i (e.g., health): \mathbf{Y}_i

This framework has a few names...

- Neyman potential outcomes framework
- Rubin causal model
- Neyman-Rubin "potential outcome" | "causal" "framework" | "model"

Potential outcomes framework

Research question: Does D_i affect Y_i ?

For each individual i, there are two **potential outcomes** (w/ binary D_i)

- 1. \mathbf{Y}_{1i} if $\mathbf{D}_i=1$ i's health outcome if she went to the hospital
- 1. \mathbf{Y}_{0i} if $\mathbf{D}_i = \mathbf{0}$ i's health outcome if she did not go to the hospital

The difference between these two outcomes gives us the **causal effect of hospital treatment**, *i.e.*,

$$\tau_i = \mathbf{Y}_{1i} - \mathbf{Y}_{0i}$$

#problems

This simple equation

$$\tau_i = \mathbf{Y}_{1i} - \mathbf{Y}_{0i}$$

leads us to the fundamental problem of causal inference.

We can never simultaneously observe Y_{1i} and Y_{0i} .

Most of applied econometrics focuses on addressing this simple problem.

Accordingly, our methods try to address the related question

For each Y_{1i} , what is a (reasonably) good counterfactual?

Solutions?

Problem We cannot directly calculate $\tau_i = \mathbf{Y}_{1i} - \mathbf{Y}_{0i}$.

Proposed solution

Compare outcomes for people who visited the hospital $(Y_{1i} \mid D_i = 1)$ to outcomes for people who did not visit the hospital $(Y_{0j} \mid D_j = 0)$.

$$E[\mathbf{Y}_i \mid \mathbf{D}_i = 1] - E[\mathbf{Y}_i \mid \mathbf{D}_i = 0]$$

which gives us the observed difference in health outcomes.

Q This comparison will return *an* answer, but is it *the* answer we want?

Selection

Q What does $E[Y_i \mid D_i = 1] - E[Y_i \mid D_i = 0]$ actually tell us?

A First notice that we can write i's outcome Y_i as

$$\mathbf{Y}_i = \mathbf{Y}_{0i} + \mathbf{D}_i \underbrace{\left(\mathbf{Y}_{1i} - \mathbf{Y}_{0i}\right)}_{\mathbf{T}_i}$$

Now write out our expectation, apply this definition, do creative math.

$$\begin{split} E[\mathbf{Y}_i \mid \mathbf{D}_i &= \mathbf{1}] - E[\mathbf{Y}_i \mid \mathbf{D}_i = 0] \\ &= E[\mathbf{Y}_{1i} \mid \mathbf{D}_i = 1] - E[\mathbf{Y}_{0i} \mid \mathbf{D}_i = 0] \\ &= E[\mathbf{Y}_{1i} \mid \mathbf{D}_i = 1] - E[\mathbf{Y}_{0i} \mid \mathbf{D}_i = 1] + E[\mathbf{Y}_{0i} \mid \mathbf{D}_i = 1] - E[\mathbf{Y}_{0i} \mid \mathbf{D}_i = 0] \end{split}$$

Selection

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Selection

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Selection

The **first term** is *good variation*—essentially the answer that we want.

$$egin{aligned} E[\mathbf{Y}_{1i} \mid \mathbf{D}_i = 1] - E[\mathbf{Y}_{0i} \mid \mathbf{D}_i = 1] \ &= E[\mathbf{Y}_{1i} - \mathbf{Y}_{0i} \mid \mathbf{D}_i = 1] \ &= E[au_i \mid \mathbf{D}_i = 1] \end{aligned}$$

The average causal effect of hospitalization for hospitalized individuals.

The **second term** is bad variation—preventing us from knowing the answer.

$$E[Y_{0i} \mid D_i = 1] - E[Y_{0i} \mid D_i = 0]$$

The difference in the average untreated outcome between the treatment and control groups.

Selection bias The extent to which the "control group" provides a bad counterfactual for the treated individuals.

Selection

Angrist and Pischke (MHE, p. 15),

The goal of most empirical economic research is to overcome selection bias, and therefore to say something about the causal effect of a variable like \mathbf{D}_i .

Q So how do experiments—the gold standard of empirical economic (and scientific) research—accomplish this goal and overcome selection bias?

Back to experiments

Q How do experiments overcome selection bias?

A Experiments break the link between potential outcomes and treatment.

In other words: Randomly assigning D_i makes D_i independent of which outcome we observe (meaning Y_{1i} or Y_{0i}).

Difference in means with random assignment of D_i

$$\begin{split} E[\mathbf{Y}_i \mid \mathbf{D}_i &= 1] - E[\mathbf{Y}_i \mid \mathbf{D}_i = 0] \\ &= E[\mathbf{Y}_{1i} \mid \mathbf{D}_i = 1] - E[\mathbf{Y}_{0i} \mid \mathbf{D}_i = 0] \\ &= E[\mathbf{Y}_{1i} \mid \mathbf{D}_i = 1] - E[\mathbf{Y}_{0i} \mid \mathbf{D}_i = 1] \quad \text{from random assignment of } \mathbf{D}_i \\ &= E[\mathbf{Y}_{1i} - \mathbf{Y}_{0i} \mid \mathbf{D}_i = 1] \\ &= E[\tau_i \mid \mathbf{D}_i = 1] \\ &= E[\tau_i] \quad \text{Random assignment of } \mathbf{D}_i \text{ breaks selection bias.} \end{split}$$

Example: Training programs

Governments subsidize training programs to assist disadvantaged workers.

Q Do these programs have the desired effects (*i.e.*, increase wages)?

A Observational studies—comparing wage data from participants and non-participants—often find that people who complete these programs actually make lower wages.

Challenges Participants self select. **+** Programs target lower-wage workers.

Example: Training programs

How do we formalize these concerns in our framework?

Observational program evaluations

$$E[\mathrm{Wage}_i \mid \mathrm{Program}_i = 1] - E[\mathrm{Wage}_i \mid \mathrm{Program}_i = 0] =$$
 $E[\mathrm{Wage}_{1i} \mid \mathrm{Program}_i = 1] - E[\mathrm{Wage}_{0i} \mid \mathrm{Program}_i = 1] +$
Average causal effect of training program on wages for participants, *i.e.*, $\bar{ au}_1$
 $E[\mathrm{Wage}_{0i} \mid \mathrm{Program}_i = 1] - E[\mathrm{Wage}_{0i} \mid \mathrm{Program}_i = 0]$
Selection bias

If the program attracts/selects individuals who, on average, have lower wages without the program (sort of the point of the program), then we have negative selection bias.

Example: Training programs

```
egin{aligned} E[\mathrm{Wage}_i \mid \mathrm{Program}_i = 1] - E[\mathrm{Wage}_i \mid \mathrm{Program}_i = 0] = \ & E[\mathrm{Wage}_{1i} \mid \mathrm{Program}_i = 1] - E[\mathrm{Wage}_{0i} \mid \mathrm{Program}_i = 1] + \ & E[\mathrm{Wage}_{0i} \mid \mathrm{Program}_i = 1] - E[\mathrm{Wage}_{0i} \mid \mathrm{Program}_i = 0] \end{aligned}
```

So even if the program, on average, has an positive wage effect (in the participant group), i.e., $\overline{\tau}_1 > 0$, we will detect a lower effect due to the negative selection bias.

If the bias is sufficiently large (relative to the treatment effect), our estimate will even get the sign of the effect wrong.

Related While observational studies typically found negative program effects, several experiments found positive program effects.

Example: The STAR experiment

The Tennessee STAR experiment is a famous/popular example of an experiment that allows us to answer an important social/policy question.

Research question Do classroom resources affect student performance?

- Statewide(-ish) in Tennessee for the 1985–1986 kindergarten cohort
- Ran for 4 years with ~11,600 children. Cost ~\$12 million.

Treatments

- 1. Small classes (13–17 students)
- 2. Regular classes (22–35 students) plus part-time teacher's aide
- 3. Regular classes (22–35 students) plus full-time teacher's aide

Example: The STAR experiment

First question Did the randomization balance participants' characteristics across the treatment groups?

Ideally, we would have pre-experiment data on outcome variable.

Unfortunately, we only have a few demographic attributes.

Table 2.2.1, MHE

	Tı			
Variable	Small	Regular	Regular + Aide	P-value
Free lunch	0.47	0.48	0.50	0.09
White/Asian	0.68	0.67	0.66	0.26
Age in 1985	5.44	5.43	5.42	0.32
Attrition rate	0.49	0.52	0.53	0.02
K. class size	15.10	22.40	22.80	0.00
K. test percentile	54.70	48.90	50.00	0.00

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Demographics appear balanced across the three treatment groups.

Table 2.2.1, MHE

	Treatment: Class Size			
Variable	Small	Regular	Regular + Aide	P-value
Free lunch	0.47	0.48	0.50	0.09
White/Asian	0.68	0.67	0.66	0.26
Age in 1985	5.44	5.43	5.42	0.32
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K. class size	15.10	22.40	22.80	0.00
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The three groups differ significantly on attrition rate.

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Variable	Small	Regular	Regular + Aide	P-value
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The randomization generated variation in the treatment.

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The small-class treatment significantly increased test scores.

The STAR experiment

The previous table estimated/compared the treatment effects using simple differences in means.

We can make the same comparisons using regressions.

Specifically, we regress our outcome (test percentile) on dummy variables (binary indicator variables) for each treatment group.

Example of our three treatment dummies.

i	y_i	Trt_{1i}	Trt_{2i}	Trt_{3i}
1	y_1	1	0	0
2	y_2	1	0	0
•	•	•	•	•
ℓ	y_ℓ	1	0	0
$\ell+1$	$y_{\ell-1}$	0	1	0
•	•	•	•	•
p	y_p	0	1	0
p+1	y_{p+1}	0	0	1
•	• •	• •	• •	•
N	y_N	0	0	1

Regression analysis

Assume for the moment that the treatment effect is constant[†], i.e.,

$$\mathbf{Y}_{1i} - \mathbf{Y}_{0i} = \boldsymbol{\rho} \quad \forall i$$

then we can rewrite

$$\mathbf{Y}_i = \mathbf{Y}_{0i} + \mathbf{D}_i \left(\mathbf{Y}_{1i} - \mathbf{Y}_{0i} \right)$$

as

$$\mathbf{Y}_i = \underbrace{lpha}_{=E[\mathbf{Y}_{0i}]} + \mathbf{D}_i \underbrace{oldsymbol{
ho}}_{\mathbf{Y}_{1i}-\mathbf{Y}_{0i}} + \underbrace{\eta_i}_{\mathbf{Y}_{0i}-E[\mathbf{Y}_{0i}]}$$

Regression analysis

$$Y_i = \alpha + D_i \rho + \eta_i$$

Now write out the conditional expectation of Y_i for both levels of D_i

$$E[Y_i \mid \mathbf{D}_i = 1] = E[\alpha + \frac{\rho}{\rho} + \eta_i \mid \mathbf{D}_i = 1] = \alpha + \frac{\rho}{\rho} + E[\eta_i \mid \mathbf{D}_i = 1]$$

$$E[\mathrm{Y}_i \mid \mathrm{D}_i = 0] = E[lpha + \eta_i \mid \mathrm{D}_i = 0] = lpha + E[\eta_i \mid \mathrm{D}_i = 0]$$

Take the difference...

$$E[\mathbf{Y}_i \mid \mathbf{D}_i = 1] - E[\mathbf{Y}_i \mid \mathbf{D}_i = 0]$$

$$= \rho + \underbrace{E[\eta_i | \mathbf{D}_i = 1] - E[\eta_i \mid \mathbf{D}_i = 0]}_{\text{Selection bias}}$$

Regression analysis

$$E[Y_i \mid \mathbf{D}_i = \mathbf{1}] - E[Y_i \mid \mathbf{D}_i = 0] = E[\eta_i \mid \mathbf{D}_i = \mathbf{1}] - E[\eta_i \mid \mathbf{D}_i = 0]$$

Again, our estimate of the **treatment effect** (ρ) is only going to be as good as our ability to shut down the **selection bias**.

Selection bias in regression model:
$$E[\eta_i | \mathbf{D}_i = \mathbf{1}] - E[\eta_i \mid \mathbf{D}_i = 0]$$

Selection bias here should remind you a lot of omitted-variable bias.

There is something in our disturbance η_i that is affecting Y_i and is also correlated with D_i .

In other metrics-y words: Our treatment \mathbf{D}_i is endogenous.

Solutions and covariates

Selection bias in regression model: $E[\eta_i | \mathbf{D}_i = 1] - E[\eta_i | \mathbf{D}_i = 0]$

As before, if we randomly assign D_i , then selection bias disappears.

Another potential route to identification is to condition on covariates in the hopes that they "take care of" the relationship between D_i and whatever is in our disturbance η_i .

Without very clear reasons explaining how you know you've controlled for the "bad variation", clean and convincing identification on this path is going to be challenging.

The experimental ideal

Covariates

That said, covariates can help with two things:

- 1. Even experiments may need **conditioning/controls**: The STAR experiment was random within school—not across schools.
- 2. Covariates can soak up unexplained variation—increasing precision.

Now that we've seen regression can analyze experiments, let's estimate the STAR example...

Table 2.2.2, MHE

Explanatory variable	1	2	3
Small class	4.82	5.37	5.36
	(2.19)	(1.26)	(1.21)
Regular + aide	0.12	0.29	0.53
	(2.23)	(1.13)	(1.09)
White/Asian			8.35
			(1.35)
Female			4.48
			(0.63)
Free lunch			-13.15
			(0.77)
School F.E.	F	Т	Т

The omitted level is Regular (with part-time aide).

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School F.E.	F	Т	T

Results without other controls are very similar to the difference in means.

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School FEs enforce the experiment's design and increase precision.

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Additional controls slightly increase precision.

R

Object types/classes

As we discussed last class, R revolves around objects, e.g., test \leftarrow 123.

Objects have types/classes.

- 1, 2/3, and are numeric.
- "Hello" and 'cruel world' are both character.
- TRUE, T, FALSE, and F are logical (as is the result of 3 > 2).

The class(x) function tells you the class of object x.

Structure

In addition to having types/classes, objects have some type of structure.

- 1:3, c(1, 2), and seq(2, 8, 2) each produce a numeric-class vector.
- c("Alright", "already") produces a vector of character class.
- c(1, 3, T, "Hello") produces a vector of character class.
- matrix(data = 1:15, ncol = 5) creates a matrix with class from data.
- data.frame(x = 1:2, y = c("a", "b"), z = T) produces a data.frame
 with three columns and two rows. The first column (x) is numeric; the
 second column (y) is character, and the third column (z) is logical.

Our matrix

```
matrix(data = 1:15, ncol = 5)

#> [,1] [,2] [,3] [,4] [,5]
#> x y z
#> [1,] 1 4 7 10 13 #> 1 1 a TRUE
#> [2,] 2 5 8 11 14 #> 2 2 b TRUE
#> [3,] 3 6 9 12 15
```

Our first data.frame!

Notice how R helps 'fill' out the columns when lengths don't match.

Packages

Straight out of the box, R has a ton of useful features, but it really gets its power from the additional packages (libraries) that users create.

- Open-source greatness Users find needs and create amazing solutions.
- *Caveat utilitor* There are a lot of packages, each with a lot of functions. Mistakes can happen.
- **Open-source greatness₂** Again, R is open source: Check the code! (Maybe. Sometimes it's very hard.)

Examples ggplot2 (plotting), dplyr (data work that can link with SQL), sf and raster (geospatial work), lfe (high-dimensional fixed-effect regression), data.table (fast and efficient data work)

Installing packages

Once you find a function/package that you need to install, you'll typically install it via install.packages("newAmazingPackage"). ††

We'll use the package dplyr throughout the course. Let's install it.

```
# Install 'dplyr' package
install.packages("dplyr")
```

Aside Notice the comment above the actual code (R uses # for comments). While not necessary for R to work, comments are necessary for research.

Using packages

Once you install a package, it is on your machine.

You don't need to install it again—though you probably should update them from time to time.

To **load a package**, use the library(package) function[†], e.g., to load dplyr

```
# Load 'dplyr'
library(dplyr)
```

Now all functions contained in dplyr are available (until you close R).

Package management

All of this installing, loading, updating, checking-for-existance-and-then-loading can get old.

```
As can typing library(pacakge1), library(package2), ...
```

[Enter] The pacman package... for package management, of course.

After installing (install.packages("pacman")), you can

- Install and load packages via p load(package1, ..., packageN)
- Update packages via p_update()

The p_load paradigm is especially helpful for collaboarations or projects across multiple machines.

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