Bachelor Thesis

Benchmark of RISC-V in BTOR2

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Abstract

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1 Introduction

RISC-V, an open-source instruction set architecture, has gained significant attention due to its flexibility and extensibility and was even mentioned by the European Union for broader adoption [1]. Ensuring the correctness of RISC-V implementations is therefore of great importance, particularly in safety-critical applications.

Model checking has emerged as a powerful method for formally verifying hardware and software systems. Among the available model checking formats, BTOR2 has become a widely adopted standard for word-level hardware verification. As RISC-V is a processor architecture, it is a fitting choice. This thesis investigates the feasibility and effectiveness of applying model checking to RISC-V using the BTOR2 format.

The primary objective of this work is to develop tools that translate RISC-V processor states into BTOR2 models, enabling systematic verification, and to evaluate the performance of the model. This is extended by a set of tools to check if the model functions correctly. By implementing a suite of test cases and analyzing the results across different model checkers, this thesis aims to provide insights into the suitability of BTOR2-based model checking for RISC-V and to identify potential limitations and advantages of this approach.

The following chapters present the theoretical foundations, the methodology for transforming RISC-V states to BTOR2, the benchmarking process, and a discussion of the results.

2 RISC-V

As the first foundation for my benchmarks and, consequently, this thesis, I will discuss RISC-V and its operational principles.

2.1 Overview

RISC-V is an open-source instruction set architecture (ISA) first published in May 2011 by A. Waterman et al. [2]. As indicated by its name, it is based on the RISC design philosophy. RISC stands for Reduced Instruction Set Computer and its concept is to only include a small set of elemental and easy to execute instructions. With this, the decoding and execution of instructions can be faster compared to CISC (Complex Instruction Set Computer) design philosophy.

Since 2015, the development of RISC-V has been coordinated by the RISC-V International Association, a non-profit corporation based in Switzerland since 2020 [3]. Its objectives include providing an *open* ISA that is freely available to all, a *real* ISA suitable for native hardware implementation, and an ISA divided into a *small* base integer ISA usable independently, for example in educational contexts, with optional standard extensions to support general-purpose software development [4, Chapter 1].

Currently, RISC-V comprises four base ISAs: RV32I, RV64I, RV32E, and RV64E, which can be extended with one or more of the 47 ratified extension ISAs [4, Preface].

For the purposes of this work, I focus on a subset of the RV64I ISA.

2.2 The RV64I ISA

RV64I is not overly complex, but its structure is essential for understanding the subsequent work presented in this thesis. Therefore, I will explain all elements relevant to my work.

RV64I features 32 64-bit registers, labeled x0-x31, where x0 is hardwired to zero across all bits. Registers x1-x31 are general-purpose and may be interpreted by various instructions as collections of booleans, two's complement signed binary integers, or unsigned integers. Additionally, there is a non-accessible register called pc, which serves as the program counter and holds the address of the current instruction [4, Chapters 4.1, 2.1].

In RV64I, memory addresses are 64 bits in size. As the memory model is defined to be single-byte addressable, the address space of RV64I encompasses 2⁶⁴ bytes [4, Chapter 1.4]. The format of the memory is little endian, so the lower bits of a number are placed at lower addresses.

Like nearly all standard ISAs of RISC-V, RV64I employs a standard instruction encoding length of 32 bits, or one word. Only the compressed extension named C introduces instructions with a length of 16 bits [4, Chapter 1.5], but this special case is not considered here. All RV64I instructions are encoded in one of the six formats illustrated in Figure 1. These formats may consist of

• The opcode:

The opcode is used to differentiate between groups of instructions. It also defines the format type of the instruction.

• rd:

This is the destination register.

| 31 | 25 24 | 20 19 | | 15 14 | 12 11 | | 7 6 | | 0 |
|----------------|--------|----------|-----|---------|--------|----------|-----|--------|--------|
| funct7 | | rs2 | rs1 | fun | ct3 | rd | | opcode | R-Type |
| 31 | | 20 19 | | 15 14 | 12 11 | | 7 6 | | 0 |
| imm | [11:0] | | rs1 | fun | ct3 | rd | | opcode | I-Type |
| 31 | 25 24 | 20 19 | | 15 14 | 12 11 | | 7 6 | | 0 |
| imm[11:5] | | rs2 | rs1 | fun | ct3 i | imm[4:0] | | opcode | S-Type |
| 31 30 | 25 24 | 20 19 | | 15 14 | 12 11 | 8 | 7 6 | | 0 |
| [12] imm[10:5] | | rs2 | rs1 | fun | ct3 in | nm[4:1] | 111 | opcode | B-Type |
| 31 | | | | | 12 11 | | 7 6 | | 0 |
| | imr | n[31:12] | | | | rd | | opcode | U-Type |
| 31 30 | | 21 20 19 | | | 12 11 | | 7 6 | | 0 |
| [20] imm | [10:1] | 111 | imm | [19:12] | | rd | | opcode | J-Type |

Figure 1: RV64I encoding formats, used in [4, Chapter 2.3]

• funct3:

This is used to differentiate between instructions with the same opcode.

• rs1 & rs2:

These are the source registers.

• funct7:

This is used for further distinctions between instructions if there are more than eight instructions in an opcode group and funct3 does not suffice.

• *imm*:

This is an immediate value. In square brackets after *imm* is designated a subfield of the immediate which is represented by these bits. From these subfields, non-defined lower bits are filled with zeros whereas the highest defined bit is sign-extended to fill all non-defined higher bits.

The design of these formats results in the following features:

• Due to RISC-V's little-endian nature, the *opcode*, which encodes the general instruction, is always read first. Further specification of the instruction via funct3 and funct7 is consistently located at the same positions.

- If utilized by the instruction, rd, rs1, and rs2 are also always found in the same locations, simplifying decoding.
- The highest bit of *imm* is always bit 31, making it straightforward to sign-extend the immediate value.

The instructions relevant to my work are listed in Table 1 I have divided the instructions in Table 1 into nine groups based on their operations.

LUI and AUIPC move a high immediate into rd. In the case of AUIPC, the pc is added to this value. JAL and JALR instructions are unconditional jumps, where for JAL imm is added to pc and for JALR imm is added to rs1 and set as pc. Both link to the next instruction (current pc + 4) in rd.

branch instructions are conditional jumps. rs1 is compared to rs2 and if the comparison holds, imm is added to pc. The comparisons are = for BEQ, \neq for BNE, < for BLT, and \geq for BGE. In these instructions, the values in rs1 and rs2 are handled as two's complement integers. The suffix *U in an instruction generally designates an unsigned operation. In this case, the values in rs1 and rs2 are handled as unsigned integers. Apart from this, they work as their counterpart without the suffix.

load instructions load values from memory at address (rs1 + imm) into rd, either at Byte, Halfword, Word, or Doubleword length. By default, the value is sign-extended, and the suffix *U designates the loading of a non-sign-extended value. Conversely, store instructions write values from rs2 at the address (rs1 + imm) to memory. Here also the distinction between the different lengths is made, and the lowest byte, halfword, word, or the whole doubleword is stored at the address.

All further instructions can be seen as generic operations, differentiated by their suffixes. To simplify the explanation process, all operations without any suffix and their behavior are listed in Table 2. This is almost exactly the group with opcode op, except the SLTU instruction, which is not suffix-free. However, as with all other

| Instr | opcode | Type | Instr | opcode | Type | Instr | opcode | Type |
|-------|--------|------|-------|-----------|------|-------|--------|------|
| LUI | lui | U | SB | store | S | ADD | | |
| AUIPC | auipc | U | SH | | | SUB | | |
| JAL | jal | J | SW | | | SLT | | |
| JALR | jalr | I | SD | | | SLTU | | |
| BEQ | | | ADDI | | | XOR | op | R |
| BNE | | | SLTI | | | OR | | |
| BLT | branch | В | SLTIU | | I | AND | | |
| BGE | отансн | Б | XORI | op-imm | 1 | SLL | | |
| BLTU | | | ORI | | | SRL | | |
| BGEU | | | ANDI | | | SRA | | |
| LB | | | SLLI | | | ADDW | | |
| LH | | | SRLI | | I* | SUBW | | |
| LW | | | SRAI | | | SLLW | op-32 | R |
| LD | load | I | ADDIW | | I | SRLW | | |
| LBU | | | SLLIW | op-imm-32 | | SRAW | | |
| LHU | | | SRLIW | vp-vmm-3z | I** | | | |
| LWU | | | SRAIW | | | | | |

Table 1: Subset of RV64I instructions

instructions with the unsigned suffix, it behaves as its signed counterpart except for handling both rs1 and rs2 as unsigned integers.

These operations can be extended by the *I suffix, which is designated by the opcode op-imm. This replaces rs2 with imm in the behavior. Again, SLTI can be extended to an unsigned version SLTIU, which behaves as expected. A SUBI instruction does not exist as it is redundant; its behavior can be achieved by using ADDI with a negative immediate.

Additionally, the operations ADD, SUB, SLL, SRL, and SRA can be extended with the *W suffix. This forms the group with the opcode op-32. In contrast to the base instructions, these new ones behave as if the registers are only 32 bits. The result is placed in the low 32 bits of rd and sign-extended to the full 64 bits. Overflows are ignored.

The last group is the combination of both suffixes *IW with the opcode op-imm-32. The behavior differs from the base instructions, as expected, by a replacement of rs2

| Instr | Behavior |
|-------|---|
| ADD | rd := rs1 + rs2 |
| SUB | rd := rs1 - rs2 |
| SLT | rd := 1 if $rs1 < rs2$ else $rd := 0$ |
| XOR | $rd := rs1 \oplus rs2$, bitwise |
| OR | $rd := rs1 \vee rs2$, bitwise |
| AND | $rd := rs1 \wedge rs2$, bitwise |
| SLL | rd := rs1 shifted left by $rs2$, new bits are zeros |
| SRL | rd := rs1 shifted right by $rs2$, new bits are zeros |
| SRA | rd := rs1 shifted right by $rs2$, sign extend |
| | |

Table 2: All suffix free operations in RV64I and their behavior. All values are handled either bitwise or as signed twos complement integers

with *imm* and only operating on 32 bits. Again, a SUBIW instruction is redundant as a negative immediate with ADDIW achieves the same result.

Compared to the full RV64I ISA, I have omitted the FENCE, ECALL, and EBREAK instructions, as without I/O interaction or an environment such as an OS or a debugger, these are not required.

For each of the instructions in Table 2, I also included the format in which each instruction is encoded. Most should be not surprising as they fit the description of the instructions. Only SLLI, SRLI, SRAI with I* and SLLIW, SRLIW, SRAIW with I** should need clarification. Both are essentially the I format but with extra constraints. For I* the highest realistic shift amount for 64 bit registers is also 64. So the bits [11,9:6] of *imm* have to be 0. The bit [10] gets a special role as it is used to differentiate between the two types of right shift. With I**, with the word suffix, the maximum shift amount is only 32, so the bit [5] of *imm* must also be 0.

2.3 Simulation of RISC-V

To run RISC-V code, the obvious way would be to run it on a RISC-V processor. As this is not practical in my case because I do not have one, I have to simulate the execution of RISC-V. For this, I will use a RISC-V-simulator of this described subset of RV64I in C that I have written for my bachelors project [5]. It will be used to test the BTOR2 model I will present in Chapter 4. Alternatively qemu [6] or QtRVSim [7] could be used, but QtRVSim has more detail than needed and qemu can not be fed with an inital state but only a full program. So I used my own, which takes the state of a RISC-V processor as an input as described in Section 2.3.3.

First, I explain the structure to represent a simple RISC-V processor I implemented.

2.3.1 Representing the State of a RISC-V Processor

The state requires a representation for all registers. pc is defined as a 64-bit integer, and the other 32 registers are implemented as an array, allowing each register to be referenced by its number. Additionally, I implemented an array of flags, one for each register, to differentiate between initialized and non-initialized registers. The memory is built from single memory cells, each holding an address and its byte of content. These are accumulated in a hash table called "memorytable", hashing on the address. If adding a new cell causes a collision, it is appended to the cells already in the bucket, forming a linked list. These structures are shown in Figure 2.

2.3.2 Running an Instruction

After fetching the current instruction from the hash table, it must be decoded. The easiest way to find the current instruction is a decision tree. First, I mask out the opcode and match it over all implemented opcodes. From there, either this is an endpoint and the instruction is identified, or funct3 must be masked and matched. A final differentiation over funct7 might be needed, but after this every leaf in the tree coincides with an instruction. Also, with knowing the opcode of the current instruction, I know the instruction format (Figure 1). This means that I can now also extract relevant register numbers and, if it exists, the immediate. The best

```
typedef struct memory_cell
{
    uint64_t address;
    uint8_t content;
    struct memory_cell *next_cell;
} memory_cell *next_cell;
} memory_cell;

typedef struct state
{
    uint64_t pc;
    uint64_t regs_values[32];
    bool regs_init[32];
    memory_table *memory;
} state;
```

Figure 2: State representation of a RISC-V processor in the simulation [5]

way to get these values is to apply a mask and shift this result to its correct place. For the immediate, as it possibly is divided into multiple fields, it might be needed to add multiple partial immediates together. At this point all information in the instruction is decoded and the current state can be modified according to the operation corresponding to the leaf reached after going through the tree. (TODO: Graph of the decision tree?)

2.3.3 Saving the State of a RISC-V Processor

To preserve the current state of a RISC-V processor, both the registers and memory must be stored. For this purpose, I have devised the format shown in Figure 3. The RISC-V simulation uses this format as input and output. The minimal file consists only of the two designators "REGISTERS:" and "MEMORY:" and one empty line between them. Under "REGISTERS:", all registers can be listed with their corresponding value. Of course, x0 cannot be different from 0. I included the option to reference it nonetheless to have the complete state included. Under "MEMORY:", after giving an address, the memory can be filled with 1-, 2-, 4-, or 8-byte sized memory content. The given address is the starting address of the content, with every

```
\langle 64bitHex \rangle
                                          up to 16 digits of [0-9a-fA-F]
                                ::=
\langle 32bitHex \rangle
                                           up to 8 digits of [0-9a-fA-F]
                                ::=
\langle 16bitHex \rangle
                                           up to 4 digits of [0-9a-fA-F]
                                ::=
\langle 8bitHex \rangle
                                           up to 2 digits of [0-9a-fA-F]
                                ::=
\langle memContent \rangle
                                           \langle 8bitHex \rangle
                                ::=
                                           \mid \langle 16bitHex \rangle
                                           \mid \langle 32bitHex \rangle
                                           \mid \langle 64bitHex \rangle
                                           \langle 64bitHex \rangle : \langle memContent \rangle
\langle cell \rangle
                                ::=
                                           |\langle cell \rangle \langle cell \rangle
\langle regNum \rangle
                                          0 |...| 31
                                ::=
\langle reg \rangle
                                          PC:\langle 64bitHex \rangle \setminus n
                                ::=
                                           \mid \mathbf{x}\langle regNum \rangle : \langle 64bitHex \rangle \setminus \mathbf{n}
                                           |\langle reg \rangle \langle reg \rangle|
\langle memory \rangle
                                          MEMORY: \n\langle cell \rangle
\langle registers \rangle
                                          REGISTERS: \n\langle reg \rangle
                                ::=
\langle state \rangle
                                           \langle registers \rangle \ (memory) \ n
                                ::=
```

Figure 3: Construction of .state files

byte after the first filling the next higher address.

3 BTOR2

The second foundation of my benchmarks is BTOR2, a word-level model checking format published by A. Niemetz et al. [8]. Before explaining the format, an overview of bounded model checking is necessary.

3.1 Bounded Model Checking

Bounded model checking (BMC) is a formal verification technique employed to detect errors in hardware or software systems by systematically exploring the state space of a finite-state model up to a specified bound, typically defined by the number of iterations or steps. As described by A. Biere in the "Handbook of Satisfiability", BMC is primarily utilized for falsification and testing, with a focus on identifying violations of temporal properties [9]. Nevertheless, BMC can also be extended to prove properties within the given bound.

In practice, BMC translates the verification problem into a satisfiability problem, determining whether a property violation can occur within the specified bound. The model comprises a finite state machine and a set of properties to be verified. The model checker systematically explores all possible state transitions up to the bound and evaluates whether the property holds. If a violation is detected, the tool generates a witness, which is a trace demonstrating how the property is violated. If no violation is found within the bound, the system is considered safe up to that bound, although this does not guarantee correctness for all possible executions.

For word-level hardware model checking, the BTOR2 format has become a de facto standard for describing models and is currently used in the "Hardware Model Checking Competition" [10]. Another format is AIGER [11], from which BTOR2 is derived [8], and which is used in the bit-level track of the HWMCC [10]. In software model checking, the "Competition on Software Verification" utilizes the C and Java programming languages as input formats [12]. Additionally, a translator from BTOR2 models to C programs has been presented to bridge the gap between hardware and software verification [13]. As this work focuses on BTOR2, the following section provides a detailed overview of the format.

3.2 The BTOR2 Language

In BTOR2, each line represents either a sort or a node, with the line number typically serving as an identifier. A sort functions similarly to a type, defining either the length of a bitvector or the size of an array of bitvectors. Nodes represent values of a defined sort and can be constants, operations, constraints, or properties. These values can be referenced by their node identifier, i.e., the line number. The syntax of BTOR2 is detailed in [8, Figure 1], and the available operators are listed in [8, Table 1].

Key features of BTOR2 include its support for sequential operations, which facilitates the implementation of a RISC-V structure. The primary feature is the state operator, which defines a node that is updated sequentially. An init node assigns an initial value to this state, while a next node specifies its subsequent value. bad nodes can be used to define endpoints for a model, indicating either the occurrence of an unintended event or, as in this work, the discovery of the intended information. In both cases, the resulting model produces a witness. Additionally, an input node allows an input to the model, with assignments to this node handled by the model checker. These inputs can be constrained by constraint nodes, which describe invariants for the inputs of the model. An example model with these sequential nodes is shown in Figure 4. This

| | ВТО | R2 model | | | Comments |
|----|------------|----------|------|------|--------------------------------|
| 1 | sort | bitvec | 1 | | bit "type" |
| 2 | sort | bitvec | 8 | | byte "type" |
| 3 | constd | 2 | 99 | | comparison constant |
| 4 | zero | 2 | | | |
| 5 | input | 2 | | i1 | input i1 |
| 6 | input | 2 | | i2 | input i2 |
| 7 | eq | 1 | 6 5 | | |
| 8 | constraint | -6 | | | $i1 \neq i2 must hold$ |
| 9 | state | 2 | | accu | sequential node accu |
| 10 | init | 2 | 9 4 | | initialization accu |
| 11 | add | 2 | 6 5 | | i1 + i2 |
| 12 | next | 2 | 9 11 | | $next\ accu\ is\ i1\ +\ i2$ |
| 13 | eq | 1 | 3 9 | | accu = constant |
| 14 | bad | 13 | | | property: $accu \neq constant$ |

Figure 4: An example BTOR2 model finding two numbers that are not equal and added together equal 99

model can now be checked by a model checker, which should produce a witness with an assignment of the two inputs i1 and i2 such that s1 = i1 + i2 = constant. Let us examine this witness in more detail.

3.3 The BTOR2 Witness

Running the model in Figure 21 through BtorMC [8] with the option -trace-gen-full produces the complete witness shown in Figure 5. The syntax of BTOR2 witnesses is described in [8, Figure 2], but I will explain the example witness in Figure 5 line by line for clarity.

The witness begins with sat, indicating that a property in the model is satisfiable. The second line specifies the property that was violated. In this case, only one bad node exists in the model, and the witness shows that b0, meaning the first occurring bad node, was violated.

```
sat
b0
#0
0 00000000 accu#0
@0
0 11101000 i1@0
1 01111011 i2@0
#1
0 01100011 accu0#1
@1
0 00000100 i1@1
1 00000000 i2@1
```

Figure 5: The complete witness of the model in Figure 4

Subsequent lines list the iterations of the counterexample for the property. For each sequential iteration, the witness first presents—marked with #x, where x is the iteration number—a representation of all states in the current iteration with their respective values in binary. Second, marked with @x, all inputs for the iteration are listed, similar to the states. Note that the nodes of the inputs and the state in Figure 4 include a symbol, which is used in the witness to name the states and inputs. Examining the witness, it is evident that the counterexample requires two iterations to reach the violated property. In the first iteration, the state accu is initialized with 0, and i1 and i2 are assigned values that add up to 99 (01100011b). In the next iteration, this sum is set as the new value for accu, which violates the property.

4 Transforming RISC-V to BTOR2

This chapter addresses the central problem of this thesis: transforming a RISC-V state into the BTOR2 format for benchmarking purposes. F. Schrögendorfer conducted similar work in his master's thesis "Bounded Model Checking in Lockless Programs" [14], where he describes, among other topics, an encoding concept for a minimal machine in a multiprocessor context [14, Chapter 2]. In [14, Chapter 8], he outlines a method to encode programs for his machine model into a BTOR2 model. This approach cannot be directly replicated here, as his model assumes the entire program is known at encoding time, whereas I aim to preserve the RISC-V property that allows for self-modifying programs during execution. If this property were to be disregarded, it would be possible to analyze the complete behavior of a program by parsing the memory, but this is beyond the scope of this work. Even so, I let myself inspire by his structuring of the model.

4.1 The Concept

To successfully execute a RISC-V instruction, three fundamental steps must occur in sequence:

- Fetch the current instruction from memory
- Identify the instruction
- Execute the instruction

Due to the fixed instruction length of RISC-V, as mentioned in Section 2.2, fetching the current instruction is straightforward. Ultimately, a node is required that retrieves a word from memory at the location specified by pc.

For basic identification, the opcode must be extracted and checked. Depending on the opcode, further distinctions between instructions require extracting and checking funct3 and, if necessary, funct7. Ultimately, a node for each instruction is needed, holding a boolean value indicating whether this instruction was fetched.

To execute the instruction, the values of the immediate imm and, if used, the registers rs1 and rs2 must be extracted. All instructions only modify rd, pc, or memory. Therefore, the next-state logic can be generalized for these three cases.

Memory is only modified when a store instruction is identified. As all store instructions share the same type, computing the memory address is consistent across them. The final step is overwriting the memory at this address.

For the pc, except for jump commands, it always increments to point to the next instruction. The two unconditional jumps, JAL and JALR, must be handled separately. For branch instructions, after determining whether the relevant condition for the instruction holds, a general approach can be applied, as all branch instructions execute the same operation from this point onward.

With rd, generalization across instructions is not feasible. However, it is possible to generalize across all possible registers by adding a check in each register's update function to determine whether the register in question is rd.

4.2 Encoding

For improved visualization in the BTOR2 code, all sort-IDs are marked in gray, all node-IDs in red, and all non-ID numbers in blue. As described in the BTOR2 syntax [8, Figure 1], each line can have an accompanying symbol. Unfortunately, these

cannot be used as aliases for the line numbers, but for clarity, in the following figures I use them as such aliases. This allows each new figure to start with the relative line number n, making it feasible to describe repetitive addition to the model with algorithms. From these, another color, green, is included. This corresponds to an algorithm variable. In contrast to the other colors, green parts of symbols must be replaced with the variables value. As a small example, if i=2 and n=7,

n constd W i iConst

shall result in

7 constd 5 2 2Const

being added to the model.

It is implied that **n** is sufficiently incremented after adding new nodes to the model so that IDs do not overlap. With this, the following sections describe how a BTOR2 model is constructed from a RISC-V state file.

4.2.1 Constants

First in the model are the sorts needed. These are comparable to types and are used to define the bit width of a node. After them follow a first set of constants I called "non-progressive", which includes bitmasks, shift distances and also the values of all implemented opcodes. This is shown in Figure 6.

Of note is the representation of memory as an array of addressable memory cells, each 1 byte. The chosen address space of 16 bits is significantly smaller than the expected 64-bit address space, but representing a 64-bit addressable memory with 2^{64} bytes (\approx 18 exabytes) is not feasible. Therefore, I selected a 16-bit address space as a practical minimum, providing approximately 65kB and supporting programs with potentially over 10,000 instructions, which I consider sufficient for most use cases. The encoding is implemented so that the address space can be modified as needed.

Following this first set of constants are the "progressive" constants. To be able to e.g.

compute which registers are encoded in the instruction or which registers to change, I need a constant for each register number. This is excellent as a minimal example for an algorithm, which is shown in Algorithm 1.

(TODO: Change code to make address space modifiable by an option?)

Algorithm 1: progressive constants for encoding RISC-V in BTOR2

4.2.2 State Representation

The next logical step is defining a representation of a RISC-V state. This is straightforward, as shown in Figure 7. I also introduced a flag for each register in my code to track whether the register was written to, enabling the transformation of a witness to a state file containing only the relevant registers. As these flags do not affect the operation of the BTOR2 model and are only included for an aesthetic choice, they are not included in my description and will not be discussed further.

4.2.3 Initialization

To initialize a state in BTOR2 from a RISC-V state file, the values in the registers must be loaded as constants, and for each memory address mentioned in the state file, the value and address must be loaded as constants. Due to the inability to represent a full 64-bit address space, I must manage the reduction of the address space from the state file to the BTOR2 model. I chose to initialize only the addresses up to the BTOR2 model's address space maximum and omit all others from the state file, as this provides the most predictable behavior. All addresses not mentioned in the state file are zero-initialized. Finally, these constants are used to initialize the state.

| 1 | sort | bitvec | 1 | | Bool |
|----|--------|-------------------------|--------|---|-----------------------|
| 2 | sort | bitvec | 16 | | AS |
| 3 | sort | bitvec | 8 | | В |
| 4 | sort | bitvec | 16 | | Н |
| 5 | sort | bitvec | 32 | | W |
| 6 | sort | bitvec | 64 | | D |
| 7 | sort | array | 2 | 3 | Mem |
| | | | | | |
| 8 | one | Bool | | | true |
| 9 | zero | Bool | | | false |
| 10 | one | AS | | | addressInc |
| 11 | constd | AS | 4 | | pcInc |
| 12 | zero | В | | | emptyCell |
| 13 | one | $\overline{\mathbb{W}}$ | | | bitPicker |
| 14 | zero | D | | | emptyReg |
| | | | | | |
| 15 | consth | \mathbb{W} | 01F | | 5Bitmask |
| 16 | consth | $\overline{\mathbb{W}}$ | 03F | | 6Bitmask |
| 17 | consth | \mathbb{W} | 07F | | 7Bitmask |
| 18 | consth | \mathbb{W} | OFFF | | 12Bitmask |
| 19 | consth | $\overline{\mathbb{W}}$ | OFFFFF | | 20Bitmask |
| | | | | | |
| 20 | constd | \mathbb{W} | 7 | | ${	t shift ToRd}$ |
| 21 | constd | \mathbb{W} | 15 | | ${	t shift ToRs 1}$ |
| 22 | constd | $\overline{\mathbb{W}}$ | 20 | | ${\it shiftToRs2}$ |
| 23 | constd | \mathbb{W} | 12 | | ${\it shiftToFunct3}$ |
| 24 | constd | \mathbb{W} | 25 | | ${\it shiftToFunct7}$ |
| 25 | constd | \mathbb{W} | 5 | | shiftBy5 |
| 26 | constd | $\overline{\mathbb{W}}$ | 11 | | shiftBy11 |
| | | | | | |
| 27 | constd | \overline{W} | 3 | | load |
| 28 | constd | \overline{W} | 19 | | opImm |
| 29 | constd | \overline{W} | 23 | | auipc |
| 30 | constd | \overline{W} | 27 | | opImm32 |
| 31 | constd | $\overline{\mathbb{W}}$ | 35 | | store |
| 32 | constd | $\overline{\mathbb{W}}$ | 51 | | op |
| 33 | constd | W | 55 | | lui |
| 34 | constd | \overline{W} | 59 | | op32 |
| 35 | constd | \overline{W} | 99 | | branch |
| 36 | constd | \overline{W} | 103 | | jalr |
| 37 | constd | \overline{W} | 111 | | jal |
| | | | | | |

Figure 6: Sorts and non-progressive Constants for encoding RISC-V in BTOR2

| (n + 0) | state | D | х0 | (n + 17) | state | D | <i>x</i> 1 |
|----------|-------|---|-----|----------|-------|-----|------------|
| (n + 1) | state | D | x1 | (n + 18) | state | D | x1 |
| (n + 2) | state | D | x2 | (n + 19) | state | D | x1 |
| (n + 3) | state | D | хЗ | (n + 20) | state | D | x^2 |
| (n + 4) | state | D | x4 | (n + 21) | state | D | x2 |
| (n + 5) | state | D | x5 | (n + 22) | state | D | x^2 |
| (n + 6) | state | D | x6 | (n + 23) | state | D | x^2 |
| (n + 7) | state | D | x7 | (n + 24) | state | D | x2 |
| (n + 8) | state | D | х8 | (n + 25) | state | D | x2 |
| (n + 9) | state | D | х9 | (n + 26) | state | D | x2 |
| (n + 10) | state | D | x10 | (n + 27) | state | D | x2 |
| (n + 11) | state | D | x11 | (n + 28) | state | D | x2 |
| (n + 12) | state | D | x12 | (n + 29) | state | D | x2 |
| (n + 13) | state | D | x13 | (n + 30) | state | D | хЗ |
| (n + 14) | state | D | x14 | (n + 31) | state | D | хЗ |
| (n + 15) | state | D | x15 | (n + 32) | state | AS | pc |
| (n + 16) | state | D | x16 | (n + 33) | state | Mem | me |

Figure 7: State representation for encoding

For the registers, this is straightforward; for memory, all memory addresses are first written into a placeholder array, which is then used to initialize the actual memory. Due to BTOR2 constraints, these constants must be defined **before** the states, but initialization with the values must occur after the states. Thus, this initialization process **wraps around** the state representation. The generation of constants is shown in Algorithm 2 and comes **before** Figure 7, while the actual initialization is shown in Algorithm 3 and comes **after** Figure 7.

4.2.4 Fetching the Current Instruction

To fetch the current instruction, I read the four bytes of the instruction and concatenate them, as shown in Figure 8.

```
truePc \leftarrow value of pc in state file
maxPc \leftarrow number of addresses in BTOR2 model
pcValue \leftarrow truePc modulo maxPc
add to model:
 n constd
                    pcValue
              AS
                               pcConst
for every register x_i do
   if register is initialised in state file then
       registerValue \leftarrow value of x_i
       if registerValue \neq 0 then
           add to model:
                constd
                              register Value
                                                x_i Const
            n
       end
   end
end
add to model:
                                                    memPH
 (n + 0)
            state
                     Mem
 (n + 1)
            init
                     Mem
                            (n + 0) emptyCell
\overline{lastPH \leftarrow memPH}
initialCells \leftarrow initialised memory cells in state file with address under maxPc
for every cell c in cutInitialCells do
   address \leftarrow address of c
   value \leftarrow value of c
   add to model:
                                 address
     (n + 0)
                          AS
                constd
     (n + 1)
                constd
                          В
                                 value
     (n + 2)
                          Mem
                                 lastPH (n + 0) (n + 1)
                                                                PHAfterC
                write
   \overline{lastPH \leftarrow PHAfterc}
end
keep lastPH for initialisation
```

Algorithm 2: Generating initialisation constants from state file in BTOR2

```
add to model:
           AS
                pc pcConst
    init
for every register x_i do
   if x_iConst was defined then
      add to model:
                     x_i
           init
                         x_iConst
   end
end
With lastPH from Algorithm 2
add to model:
    init
           Mem
                 memory lastPh
```

Algorithm 3: Initialising states in the BTOR2 model

```
(n + 0)
                   AS
                        addressInc
          add
(n + 1)
                        address Inc\\
                                     (n + 0)
          add
                   AS
(n + 2)
          add
                   AS
                        address Inc\\
                                     (n + 1)
(n + 3)
          read
                   В
                        memory
                                    pc
(n + 4)
          read
                   В
                        memory
                                     (n + 0)
(n + 5)
                                     (n + 1)
          read
                   В
                        memory
(n + 6)
          read
                   В
                        memory
                                     (n + 2)
(n + 7)
          concat
                   Η
                        (n + 4)
                                     (n + 3)
(n + 8)
          concat
                   Η
                        (n + 6)
                                     (n + 5)
                        (n + 8)
                                     (n + 7)
(n + 9)
          concat
                                               instr
```

Figure 8: Fetching the current instruction from memory

4.2.5 Deconstruction of the Instruction

With the instruction available, it can be deconstructed to extract the opcode, rd, rs1, rs2, funct3, funct7, and imm. For everything except imm, this can be accomplished by shifting and masking, as shown in Figure 9.

The immediate, however, must first be constructed from its subfields, which are referenced in Figure 1. In the BTOR2 model, this is shown in Figure 10. This is the same method I used to get the immediate in the RISC-V simulation Section 2.3.2 Three points are noteworthy:

First, some immediate subfields overlap exactly. This is utilized in lines (n + 1) with the overlap of imm[11:5] for I- and S-type, and (n + 21) with J- and B-types imm[10:5] overlap. Second, as described in Section 2.2, the immediate is always sign-extended. This is achieved using arithmetic right shifts, which perform sign extension and correctly position the highest immediate bit. Third, at line (n + 8), sign extension requires a right shift by 19. As this matches the opcode for arithmetic instructions with immediate, I reused this constant.

Now, iTypeImm, sTypeImm, bTypeImm, uTypeImm, and jTypeImm are available. However, it is preferable to have a single node imm referencing the immediate value regardless of instruction. This is accomplished in Figure 11, where booleans are defined to check all opcodes that are neither R-type nor I-type. Then, if-then-else nodes are chained to select instructions of J-type, U-type, B-type, or S-type. If the instruction is none of these, I default to I-type, as R-type does not use an immediate value. Finally, imm is extended to the 64-bit width required by RV64I.

At this stage, the values of the designated rs1 and rs2 registers can also be extracted. This is shown for rs1 in Figure 4; the process is identical for rs2, with only the names changed. The starting equality comparisons can be omitted for rs2, as they are already defined for rs1 and can be referenced.

```
(n + 0)
                  W
                      instr
                                 7Bitmask
                                                   opcode
           and
(n + 1)
                      instr
                                 shiftToRd
           srl
(n + 2)
           and
                  W
                      (n + 1)
                                 5Bitmask
                                                   rd
(n + 3)
                      instr
                                 shiftToRs1
           srl
(n + 4)
                 \overline{W}
                      (n + 3)
                                 5Bitmask
                                                   rs1
           and
(n + 5)
                 W
                      instr
                                 shiftToRs2
           srl
(n + 6)
                      (n + 5)
           and
                  W
                                 5Bitmask
                                                   rs2
(n + 7)
           srl
                 \overline{W}
                      instr
                                 shiftToFunct3
(n + 8)
                                                   funct3
           and
                      (n + 7)
                                 shiftRd
(n + 9)
           srl
                  W
                      instr
                                 shiftToFunct7
                                                   funct7
```

Figure 9: Extraction of values from the instruction without imm

```
for i from 1 to 31 do
   add to model:
                         iConst
                                    isRs1Xi
                    rs1
end
add to model:
    ite
              isRs1X1
                        x1
                             x0
                                  checkX1
for i from 2 to 30 do
   add to model:
                 isRs1Xi
                                               checkXi
                                checkX(i-1)
        ite
end
add to model:
              isRs1X31
                          x31
                                check X30
                                           rs1val
```

Algorithm 4: Extracting the value of the register designated by rs1

| (n + 0) | sra | W | instr | shiftToRs2 | iTypeImm |
|----------|-----|--------------|-----------|------------------|----------|
| (n + 1) | and | W | iTypeImm | -5Bitmask | s[11:5] |
| (n + 2) | add | W | s[11:5] | rd | sTypeImm |
| (n + 3) | and | W | rd | -bitPicker | b[4:0] |
| (n + 4) | and | \mathbb{W} | funct7 | 6Bitmask | |
| (n + 5) | sll | \mathbb{W} | (n + 4) | shiftBy5 | b[10:5] |
| (n + 6) | and | \mathbb{W} | bitPicker | rd | |
| (n + 7) | sll | \mathbb{W} | (n + 6) | shiftBy11 | b[11] |
| (n + 8) | sra | \mathbb{W} | instr | mathI | |
| (n + 9) | and | \mathbb{W} | (n + 8) | 12Bitmask | b[31:12] |
| (n + 10) | add | \mathbb{W} | b[10:5] | b[4:0] | |
| (n + 11) | add | \mathbb{W} | b[11] | (n + 10) | |
| (n + 12) | add | W | b[31:12] | (n + 11) | bTypeImm |
| (n + 13) | and | \mathbb{W} | instr | -12Bitmask | uTypeImm |
| (n + 14) | and | W | rs2 | -bitPicker | j[4:0] |
| (n + 15) | and | \mathbb{W} | rs2 | bitPicker | |
| (n + 16) | sll | \mathbb{W} | (n + 15) | shiftBy11 | j[11] |
| (n + 17) | sll | \mathbb{W} | funct3 | shift To Funct 3 | j[14:12] |
| (n + 18) | sll | \mathbb{W} | rs1 | shift ToRs1 | j[19:15] |
| (n + 19) | sra | \mathbb{W} | instr | shiftBy11 | |
| (n + 20) | and | \mathbb{W} | (n + 19) | -20 Bitmask | j[31:20] |
| (n + 21) | add | \mathbb{W} | b[10:5] | j[4:0] | |
| (n + 22) | add | \mathbb{W} | j[11] | (n + 21) | |
| (n + 23) | add | \mathbb{W} | j[14:12] | (n + 22) | |
| (n + 24) | add | \mathbb{W} | j[19:15] | (n + 23) | |
| (n + 25) | add | \mathbb{W} | j[31:20] | (n + 24) | jTypeImm |

Figure 10: Extraction of all imm types from the instruction

| (n + 0) | eq | Bool | opcode | store | | isSType |
|----------|------|----------------|----------|----------|----------|----------|
| (n + 1) | eq | Bool | opcode | branch | | is BType |
| (n + 2) | eq | Bool | opcode | auipc | | |
| (n + 3) | eq | Bool | opcode | lui | | |
| (n + 4) | or | Bool | (n + 2) | (n + 3) | | is UType |
| (n + 5) | eq | Bool | opcode | jal | | is JType |
| | | | | | | |
| (n + 6) | ite | \overline{W} | is SType | sTypeImm | iTypeImm | checkS |
| (n + 7) | ite | \overline{W} | isBType | bTypeImm | checkS | checkB |
| (n + 8) | ite | \overline{W} | is UType | uTypeImm | checkB | checkU |
| (n + 9) | ite | \overline{W} | is JType | jTypeImm | check U | imm32 |
| | | | | | | |
| (n + 10) | sext | D | imm32 | 32 | | imm |

Figure 11: Finding the correct immediate by opcode

| (isJALR | (isJALR already exists) | | | | | | | | |
|---------|-------------------------|------|--------------|--------------|---------|--|--|--|--|
| n | and | Bool | isLoad | is 5 Funct 3 | is LHU | | | | |
| (n + 0) | consth | W | 20 | | | | | | |
| (n + 1) | eq | Bool | funct7 | (n + 0) | | | | | |
| (n + 2) | and | Bool | is 0 Funct 3 | (n + 1) | | | | | |
| (n + 3) | and | Bool | isLoad | (n + 2) | is SUBW | | | | |

Figure 12: Instruction detection of JALR, LHU and SUBW as described in Algorithm 5

4.2.6 Instruction Detection

For the next-state logic, it is essential to determine the current command. Therefore, I defined a check *isInstruction* for each instruction. As this is repetitive, Algorithm 5 describes a generalized approach to obtain these booleans. An example for each instruction subgroup in Algorithm 5 is provided in Figure 12. The funct7 checks from the *needsf7* subgroup can be reused if multiple instructions share the same funct7.

4.2.7 Next-State Logic

The next-state logic is the core of the model. Almost everything else supports this point. The goal is to create the changes each instruction would make and then apply

```
add to model:
  (n + 0)
                         opcode
                                   load
                                                  isLoad
                  Bool
             eq
  (n + 1)
                         opcode
                                   opImm
                                                  isOpImm
             eq
                  Bool
  (n + 2)
                                                  isAUIPC
                  Bool
                         opcode
                                   auipc
             eq
  (n + 3)
                         opcode
                                   opImm32
                                                  isOpImm32
                  Bool
  (n + 4)
                                                  isStore
                  Bool
                         opcode
                                   store
  (n + 5)
                         opcode
                                                  isOp
                  Bool
             eq
                                   op
                                                  isLUI
  (n + 6)
             eq
                  Bool
                         opcode
                                   lui
  (n + 7)
                         opcode
                                   op32
                                                  isOp32
             eq
                  Bool
  (n + 8)
                                                  isBranch
                  Bool
                         opcode
                                   branch
             eq
  (n + 9)
                                                  is JALR
                         opcode
                                   jalr
             eq
                  Bool
                                                  isJAL
 (n + 10)
                         opcode
                  Bool
                                   jal
             eq
for i from 0 to 7 do
   add to model:
                     funct3
                             iConst
                                         isiFunct3
             Bool
        eq
end
onlyOp \leftarrow [LUI, AUIPC, JAL, JALR]
needsf7 \leftarrow [SRL, SRA, SRLI, SRAI, SRLW, SRAW, SRLWI, SRAWI, ADD,
SUB, ADDW, SUBW]
rest \leftarrow [ all other instructions ]
for all instructions I in onlyOp do
|isI| is already defined
end
for all instructions I in rest do
   opname \leftarrow opcode name of I
   f3val \leftarrow expected funct3 of I as digit
   add to model:
                                  isf3valFunct3
        and
                      isopname
                                                    isI
end
for all instructions I in needs f7 do
   opname \leftarrow opcode name of I
   f3val \leftarrow expected funct3 of I as digit
   f7hex \leftarrow expected funct 7 of I as hexadecimal number
   add to model:
                                 f7hex
     (n + 0)
                         W
                consth
                                 funct7
     (n + 1)
                         Bool
                                                 (n + 0)
               eq
     (n + 2)
                         Bool
                                 isf3valFunct3
                                                 (n + 1)
               and
     (n + 3)
                                 isopname
                                                 (n + 2)
                and
                         Bool
                                                              isI
end
```

Algorithm 5: Generalised approach to instruction detection

only the changes specific to the instruction in the state. Each state node in the model must have an accompanying next node to function correctly. First, the changed values are computed.

Computing new Values for each Instruction

It is unnecessary to detail all instructions, as this simply follows the RV64I ISA. Instead, I provide examples for each group of instructions as divided in Table 1. These examples are found in Figure 13, specifically for

- AUIPC in Figure 13.1,
- JALR in Figure 13.2,
- BEQ in Figure 13.3,
- LHU in Figure 13.4,
- SD in Figure 13.7,
- ANDI in Figure 13.5,
- SLLIW in Figure 13.8,
- SLT in Figure 13.6, and
- SUBW in Figure 13.9.

These examples contain some overlaps that can be utilized, such as for load and store instructions or the cut-to-32bit values needed for word instructions. The SD example demonstrates that all other store instructions are interim results of preparing SD. Load instructions are similar, but each requires sign extension to 64 bits. Also, between SLLIW and SUBW, only one node rs1val32 suffices. In the generated model, this is taken into account but here I avoided it, so the examples are independent from each other. With this, we have everything necessary to define the next state.

| | n add | D imm | pc | rdAUIPC | |
|-----------------|--------|----------|-----------|-----------|----------------------------|
| | | 13.1: | AUIPC | | _ |
| (n + 0) | add | AS pc | pe | cInc | nextPc |
| (n + 1) | add | D imn | n rs | 1val | |
| (n + 2) | and | D -10 | onst (1 | n + 1) | |
| (n + 3) | slice | AS (n | + 2) 18 | õ | pcJALR |
| (n + 4) | uext | D nex | tPc = 48 | 3 | rdJALR |
| | | 13.2: | JALR | | |
| ${(n + 0)}$ add | AS | pc | pcInc | ; | nextPc |
| (n + 1) sli | ce AS | imm | 15 | 0 | ImmAS |
| (n + 2) add | AS | pc | Imm_{s} | AS | pcBranch |
| (n + 3) eq | Bool | rs1val | rs2va | 1 | |
| (n + 4) ite | AS | (n + 3) | pcBr | anch nex | tPc pcBEQ |
| | | 13.3: | BEQ | | |
| (n + 0) | add | D rs1v | al in | nm | |
| (n + 1) | slice | AS (n | | | 0 |
| (n + 2) | add | AS (n | | ldressInc | |
| (n + 3) | read | | | + 1) | |
| (n + 4) | read | | nory (n | | |
| (n + 5) | concat | | | + 4) | |
| (n + 6) | uext | D (n - | - 5) 48 | <u> </u> | 0 rdLHU |
| | | 13.4: | LHU | | |
| = | n and | D rs1val | imm | rdAND | $\overline{\overline{DI}}$ |
| _ | | 13.5: | ANDI | | |
| (n + 0 |)) slt | Bool r | s1val | rs2val | |
| (n + 1 | uext | D (| n + 0) | 63 | rdSLT |
| | | 13.6 | SLT | | |

Figure 13: Instruction execution for chosen instructions

```
(n + 0)
           add
                   D
                         rs1val
                                       imm
 (n + 1)
                         (n + 0)
                                                   0
           slice
                   AS
                                       15
 (n + 2)
           add
                   AS
                         (n + 1)
                                       addressInc
 (n + 3)
                         (n + 2)
                                       addressInc
           add
                   AS
 (n + 4)
           add
                   AS
                         (n + 3)
                                       addressInc
 (n + 5)
                                       addressInc
                   AS
                         (n + 4)
           add
 (n + 6)
                   AS
                         (n + 5)
                                       addressInc
           add
 (n + 7)
                         (n + 6)
                                       addressInc
           add
                   AS
 (n + 8)
                                       addressInc
           add
                   AS
                         (n + 7)
 (n + 9)
                                       7
                                                   0
           slice
                   В
                         rs2val
(n + 10)
                   В
                         rs2val
                                       15
                                                    8
           slice
(n + 11)
           slice
                   В
                         rs2val
                                       23
                                                    16
(n + 12)
                                       31
                                                    24
           slice
                   В
                         rs2val
(n + 13)
           slice
                   В
                         rs2val
                                       39
                                                    32
(n + 14)
                                       47
                                                    40
           slice
                   В
                         rs2val
(n + 15)
                                                    48
                   В
                                       55
           slice
                         rs2val
(n + 16)
           slice
                   В
                         rs2val
                                       63
                                                    56
(n + 17)
                                       (n + 1)
                                                    (n + 9)
                                                               memorySB
           write
                   Mem
                         memory
(n + 18)
           write
                   Mem
                         memorySB
                                       (n + 2)
                                                    (n + 10)
                                                               memorySH
(n + 19)
                         memorySH
                                       (n + 3)
                                                    (n + 11)
           write
                   Mem
(n + 20)
                                       (n + 4)
                                                    (n + 12)
                                                               memorySW
           write
                   Mem
                         (n + 19)
(n + 21)
                         memorySW
                                       (n + 5)
                                                    (n + 13)
           write
                   Mem
(n + 22)
                                       (n + 6)
                                                    (n + 14)
           write
                   Mem
                         (n + 21)
(n + 23)
           write
                   Mem
                         (n + 22)
                                       (n + 7)
                                                    (n + 15)
(n + 24)
           write
                   Mem
                         (n + 23)
                                       (n + 8)
                                                    (n + 16)
                                                               memorySD
```

13.7: SD

| (n + 0) | and | W | imm32 | 5Bitmask | | | | |
|-------------------|-------------|----------------|---------|----------|---|---------|--|--|
| (n + 1) | slice | \mathbb{W} | rs1val | 31 | 0 | | | |
| (n + 2) | sll | \mathbb{W} | (n + 1) | (n + 0) | | | | |
| (n + 3) | sext | D | (n + 2) | 32 | | rdSLLIW | | |
| | 13.8: SLLIW | | | | | | | |
| | | | | | | | | |
| (n + 0) | slice | W | rs1val | 31 | 0 | | | |
| (n + 1) | slice | \overline{W} | rs2val | 31 | 0 | | | |
| (n + 2) | sub | \mathbb{W} | (n + 0) | (n + 1) | | | | |
| (n + 3) | sext | D | (n + 2) | 32 | | rdSUBW | | |
| 13.9: SUBW | | | | | | | | |

Figure 13: Continuation of Instruction execution for chosen instructions

| (n + 0) | ite | Mem | isSB | memorySB | memory |
|---------|------|-----|--------|----------|---------|
| (n + 1) | ite | Mem | isSH | memorySH | (n + 0) |
| (n + 2) | ite | Mem | isSW | memorySW | (n + 1) |
| (n + 3) | ite | Mem | isSD | memorySD | (n + 2) |
| (n + 4) | next | Mem | memory | (n + 3) | |

Figure 14: Next-State logic for the memory array

| (n + 0) | ite | AS | isBGEU | pcBGEU | nextPc |
|---------|------|----|---------|---------|---------|
| (n + 1) | ite | AS | isBLTU | pcBLTU | (n + 0) |
| (n + 2) | ite | AS | isBGE | pcBGE | (n + 1) |
| (n + 3) | ite | AS | isBLT | pcBLT | (n + 2) |
| (n + 4) | ite | AS | isBNE | pcBNE | (n + 3) |
| (n + 5) | ite | AS | isBEQ | pcBEQ | (n + 4) |
| (n + 6) | ite | AS | is JALR | pcJALR | (n + 5) |
| (n + 7) | ite | AS | is JAL | pcJAL | (n + 6) |
| (n + 8) | next | AS | pc | (n + 7) | |

Figure 15: Next-State logic for the pc register

The Next Memory

Defining the next memory array is straightforward. All store instructions are cascaded through if-then-else nodes, with the final 'else' set as the current memory array; if no 'if' matches, the array remains unchanged. This is shown in Figure 14.

The Next pc

For the next pc, the approach is similar, as shown in Figure 15. The only difference is that if no 'if' matches, pc must point to the next instruction to execute. The nextPc value was already computed for the JAL and JALR instructions and is reused here. The unconditional jumps also modify the value in rd, which is handled in the next section.

The Next rd

At last, the remaining registers must be updated. The procedure is defined in Figure 6. With the exception of x0, this is the same for all registers. The process is similar to defining the next memory or pc, but instead of a handful of instructions, all 39 relevant instructions must be considered, as only branch and store instructions do not modify rd. For brevity, the cascade for all relevant instructions is not shown in full in Algorithm 6, but only indicated.

```
add to model:
    next
                x0
for i from 1 to 31 do
   add to model:
                                isLUI
                                            rdLUI
       (n + 0)
                  ite
                         D
                                                        хi
       (n + 1)
                                is AUIPC
                                            rdAUIPC
                                                        (n + 0)
                  ite
                         D
                  ite
                         D
      (n + 47)
                                                        (n + 46)
                  ite
                         D
                                isSRAW
                                            rdSRAW
                                            iConst
      (n + 48)
                  eq
                         Bool
                                rd
      (n + 49)
                 ite
                         D
                                (n + 48)
                                            (n + 47)
                                                       xi
      (n + 50)
                         D
                                            (n + 49)
                 next
end
```

Algorithm 6: Next-state logic for all x registers

4.2.8 Properties

The final step is to define properties to terminate the model checker. The primary constraint is reaching a set number of iterations, as shown in Figure 16.

Additional properties are defined to check for invalid instructions. The first checks if the opcode is valid for the model. The second constraint detects if the instruction cannot be identified even when the opcode is valid, as shown in Figure 17. The constraint in Figure 18 handles instruction-address-misaligned exceptions for jump instructions.

```
(n + 0)
          one
                    D
(n + 1)
          constd
                    D
                           nIterations
(n + 2)
          state
                    D
                                                       counter
(n + 3)
          init
                    D
                           (n + 2)
                                        emptyReg
(n + 4)
                           (n + 2)
                    D
                                        (n + 0)
          add
(n + 5)
          next
                    D
                           (n + 2)
                                         (n + 4)
(n + 6)
                           (n + 2)
                                         (n + 1)
                    Bool
          eq
(n + 7)
                           (n + 6)
          bad
```

Figure 16: Terminating the model by iteration count

Other properties can be defined, such as terminating on a specific pc value or when a register reaches a specified value. An example for this can be the addition of Figure 19 to the model. The easiest way to exclude the iteration counter when adding this

4.3 Testing for Correctness

To test my model, I compared its results to those of my RISC-V simulator (Section 2.3).

Given a state, both the simulation and the BTOR2 model are run with the iteration maximum set to 1. The resulting BTOR2 witness cannot be directly compared to the resulting state of the simulation. Therefore, I implemented a simple converter from witness to state [15, src/restate_witness.c]. These two states can then be compared. A shell script for this purpose is provided at [15, sh_utils/compare_iterations.sh].

To generate RISC-V states, I implemented a fuzzer [15, $src/state_fuzzer.c]$ that generates randomized states with one valid instruction at the address of pc. The fuzzer first selects an instruction to test and fills all variable parts of the instruction, such as rd or imm. All registers relevant to the instruction are then assigned random 64-bit values. A pc value is generated to ensure the instruction fits within the limited address space of the BTOR2 model. If a jump instruction is chosen, possible address misalignment is corrected and address overflow is prevented. This simplifies later

```
(n + 0)
                        isLoad
                                      isOpImm
           or
                 Bool
 (n + 1)
                        is AUIPC
                 Bool
                                      (n + 0)
           or
 (n + 2)
           or
                        isOpImm32
                                      (n + 1)
                 Bool
 (n + 3)
                 Bool
                        isStore
                                      (n + 2)
           or
 (n + 4)
                 Bool
                        isOp
                                      (n + 3)
           or
 (n + 5)
                        isLUI
                                      (n + 4)
                 Bool
           or
 (n + 6)
                        isOp32
                                      (n + 5)
           or
                 Bool
 (n + 7)
                        isBranch
                                      (n + 6)
                 Bool
           or
 (n + 8)
                 Bool
                        isJALR
                                      (n + 7)
           or
                                      (n + 8)
 (n + 9)
                 Bool
                        isJAL
           or
(n + 10)
                        -(n + 9)
           bad
(n + 11)
                        is LUI
                                      is AUIPC
                 Bool
           or
(n + 12)
           or
                 Bool
                        isJAL
                                      (n + 11)
           or
                 Bool
(n + 58)
                        isSRAW
                                      (n + 57)
           or
                 Bool
(n + 59)
                 Bool
                        -(n + 9)
                                      (n + 58)
           and
(n + 60)
                        (n + 59)
           bad
```

Figure 17: Terminating the model on unknown instructions

```
(n + 0)
           zero
                    AS
 (n + 1)
           constd
                    AS
                           3
 (n + 2)
                           (n + 1)
                                      pcJAL
           and
                    AS
 (n + 3)
           and
                    AS
                           (n + 1)
                                      pcJALR
 (n + 4)
           and
                    AS
                           (n + 1)
                                      pcBEQ
                    AS
                           (n + 1)
           and
 (n + 9)
                           (n + 1)
                                      pcBGEU
           and
                    AS
(n + 10)
           neq
                    Bool
                           (n + 0)
                                       (n + 2)
(n + 11)
                    Bool
                           (n + 0)
                                       (n + 3)
           neq
(n + 12)
                           (n + 0)
                                       (n + 4)
                    Bool
           neq
                           (n + 0)
           neq
                    Bool
(n + 17)
                           (n + 0)
           neq
                    Bool
                                       (n + 9)
(n + 18)
           or
                    Bool
                           (n + 18)
                                       (n + 17)
(n + 19)
                    Bool
                           (n + 19)
                                       (n + 18)
           or
                    Bool
           or
(n + 24)
                    Bool
                           (n + 23)
                                       (n + 22)
           or
(n + 25)
           bad
                           (n + 24)
```

Figure 18: Terminating the model on misaligned addresses

| (n + 0) | constd | D | forbiddenValue | badValRegNum |
|---------|--------|------|---------------------|----------------------|
| (n + 1) | eq | Bool | $\mathbf{x}RegNum$ | is X Reg Num Bad Val |
| (n + 2) | bad | | is XReg Num Bad Val | |

Figure 19: Terminating the model on a specific register value

comparison of the resulting states, as correct execution of the instruction always results in the same state, despite differences between the simulation and the BTOR2 model.

With this setup, a series of tests can be conducted. For this, I implemented a shell script [15, sh_utils/test_btor2_model.sh]. As the number of tests increases, it becomes more challenging to track failed tests. To address this, I wrote a script to aggregate all failed tests into one file and add additional information such as instruction name or immediate value [15, sh_utils/diff_logger.sh].

I have executed approximately 5,000,000 tests on this model without a single failure, which leads me to conclude that my implementation is correct.

5 Benchmarks

With the model implemented, I was able to evaluate its performance. All benchmarks were executed on an Intel Core i5-6200U using the btormc model checker, which is distributed with the BTOR2 format [8]. Each test was run five times, and the resulting times were averaged. I also attempted to run the tests with the model checkers AVR [16] and Pono [17]. The challenges encountered with these tools are discussed in Section 5.2.

5.1 Tests

I devised two basic tests, each composed of four RISC-V instructions as illustrated in Figure 20. One test includes a memory operation, while the other does not, allowing for measurement of the impact of memory operations on the model's performance. The programs for these tests are intentionally similar: both feature three instructions forming a loop and one instruction serving as a "workhorse". The test names, add and write_mem, are derived from this key instruction. The program is embedded into a state, as exemplified in Figure 21, where the add program is configured for 256 loops. In this setup, x1 acts as a loop limiter, x2 as a loop counter, and x3 as an accumulator. The instructions are placed in the initial bytes of memory. In contrast, the memory operation test uses x2 as an address to store the first byte of a register, with x3 serving as this register. Both tests were also implemented with increasing loop counts up to 2048 to provide a reference for processing more iterations.

```
bge x2 x1 0x10 jump\ out\ of\ program\ if\ x1=x2 add x3 x3 x2 | either (add counter onto x3) | sb x3 0x14(x2) or (store the first byte of x3 at counter + 0x14) addi x2 x2 0x1 increment counter in x2 jump\ back\ to\ address\ 0
```

Figure 20: Base test cases for the benchmarks

```
REGISTERS:
PC:0
x1:100
x2:0

MEMORY:
0:001158E3 # BGE x2 x1 0x10
4:002181B3 # ADD x3 x3 x2
8:00110113 # ADDI x2 x2 1
c:00000067 # JALR x0 x0 0
```

Figure 21: Example state for benchmark add 0256

Additionally, I evaluated the impact of initialized memory on runtime. For this, I introduced tests with the prefix fullmem, where memory addresses 0x18 to 0xfff were filled with the bit pattern '0101'. The first four words of memory were filled with the test program. The fifth word could also be filled, but I opted to leave it zero-initialized to ensure the test terminates by jumping to this address and not finding a valid instruction. This guarantees termination.

I also investigated the impact of address space size by generating models from add_0256, add_1024, write_mem_0256, and write_mem_1024 with extended address space. These tests use the prefix "extaddr_x", where x denotes the maximum address length in bits.

Furthermore, I implemented the base add tests in a manner similar to the BTOR2 model described by F. Schrögendorfer in his master thesis [14, Chapter 8]. These tests use the prefix "nopc", as the program counter is abstracted to activation flags for each instruction. The model generation is demonstrated using nopc_add_0256 as

an example. First, the necessary sorts and constants for RISC-V are defined:

```
1
             bitvec
                       1
                             bool
    sort
2
    sort
             bitvec
                       8
                            memcell
3
                       16
    sort
             bitvec
                             addressspace
             bitvec
                       64
                            register
    sort
                       3 2
5
                             Memory
             array
    sort
                             false
    zero
                             true
    one
             2
8
                            emptymem
    zero
9
             4
    zero
                             emptyreg
10
             3
                            pcinit
    zero
             3
                            pcinc
11
    consth
                       10
12
    consth
                            instr1 pcmod
                       100
13
             4
                            nloops
    consth
```

With this now the registers and memory can be defined:

```
99
                                                             state
     state
                 pc
                           110
                                 state
                                             x10
                                                       121
                                                                        x21
                                                                        x22
                                         4
                                                                     4
100
     state
             4
                 x0
                           111
                                 state
                                             x11
                                                       122
                                                             state
             4
                                         4
                                                       123
                                                                     4
                                                                         x23
101
                           112
                                             x12
     state
                 x1
                                 state
                                                             state
102
     state
             4
                 x2
                           113
                                 state
                                             x13
                                                       124
                                                             state
103
                                         4
                                                       125
             4
                 x3
                           114
     state
                                 state
                                             x14
                                                             state
                                                       126
104
             4
                           115
                                         4
                                             x15
                 x4
     state
                                 state
                                                             state
105
     state
                 x5
                           116
                                 state
                                             x16
                                                       127
                                                             state
                                         4
             4
                                                       128
                                                                     4
106
     state
                 х6
                           117
                                 state
                                             x17
                                                             state
                                                                         x28
107
                           118
                                         4
                                                       129
     state
             4
                 x7
                                 state
                                             x18
                                                             state
                                                                         x29
             4
                 x8
                                         4
108
     state
                           119
                                 state
                                             x19
                                                       130
                                                             state
                                                                        x30
109
     state
             4
                 x09
                           120
                                         4
                                 state
                                             x20
                                                       131
                                                             state
                                                                        x31
```

Note that node IDs 14-98 are skipped. As BTOR2 requires unique but not continuous node IDs, I assigned each register node ID to equal the register number plus 100 for clarity when writing models manually.

Next, the initial memory is defined:

```
144
                                       169
                                                          166 167 168
     state
                                            write
145
               5
                  14 8
                                       170
                                                      3
     init
                                            consth
                                                         8
               3
                                                      2
146
     consth
                  0
                                       171
                                            consth
                                                         13
               2
                                                      5
                                                          169 170 171
147
                  e3
                                       172
     consth
                                            write
               5
                                                      3
148
                  144 146 147
                                       173
     write
                                            consth
                                                      25
               3
                                       174
                                                         01
149
                  1
     consth
                                            consth
150
               2
                                       175
                                                          172 173 174
     consth
                  58
                                            write
                                                      3
               5
                  148 149 150
151
                                       176
                                            consth
     write
               3
                  2
                                                      2
152
     consth
                                       177
                                                         11
                                            consth
153
     consth
               2
                  11
                                       178
                                            write
                                                      5
                                                          175 176 177
                                                      3
               5
                  151 152 153
154
     write
                                       179
                                            consth
                                                         b
                                                      2
155
     consth
               3
                  3
                                       180
                                                         00
                                            consth
156
                  00
                                       181
                                                          178 179 180
     consth
                                            write
               5
                                                      3
157
                  154 155 156
                                       182
     write
                                            consth
               3
                                                      2
158
                  4
                                       183
                                            consth
                                                         67
     consth
                                                      5
               2
                                                          181 182 183
159
     consth
                  b3
                                       184
                                            write
                                                      3
160
               5
                  157 158 159
                                       185
                                                         d
     write
                                            consth
161
               3
                  5
                                       186
                                                      2
                                                          00
     consth
                                            consth
                                                      5
162
               2
                  81
                                                          184 185 186
     consth
                                       187
                                            write
163
               5
                  16 161 162
                                       188
                                                      3
     write
                                            consth
                                                      2
164
     consth
               3
                  6
                                       189
                                            consth
                                                          00
                                                      5
                  21
                                       190
                                                         187 188 189
165
     consth
                                            write
               5
                     164 165
                                                      3
166
     write
                  16
                                       191
                                            consth
                                                         f
                                                      2
167
      consth
               3
                  7
                                       192
                                            consth
                                                         00
                                                      5
168
     consth
                  00
                                       193
                                            write
                                                         190 191 192
```

Due to BTOR2 constraints, initial memory must be defined before the intended memory state node. Node 144 serves only for memory initialization, as previously described in Section 4.2.3.

The actual memory state and instruction flags are then defined. I renamed the flags from stmt (Schrögendorfer) to instr for clarity. An exit code is unnecessary, as differentiation between model terminations is not required; only the termination time is of interest.

```
199
      state
              5
                  memory
200
      state
               1
                  instr0
201
               1
                  instr1
      state
202
               1
                   instr2
      state
203
               1
                   instr3
      state
              1
204
                   endflag
      state
```

Next up would be the inputs and constraints for these. Both are not needed for the RISC-V model because neither are threads needed as I do not model parallel processing, nor is flushing as I use a naive memory model. And without inputs, the constraints are also nonexistent. So really, next up is initialization and transitions of the states. First is pc:

```
300
      init
             3
                99
                      10
                                  pc is zero initialized
             3
                                  normal pc operation
301
     add
                99
                      11
302
             3
                99
                      12
                                  instr1 jump
      add
                      102
                                  instr1 branch condition
303
             1
                101
      eq
                                  IF condition THEN jump ELSE increment
304
             3
                303
                      302
                            301
      ite
                                  IF instr1 THEN check ELSE leave pc
305
             3
                200
                      304
                            99
      ite
306
                201
                       202
      or
             3
                                  IF instr2-3 THEN increment ELSE instr1
                            305
307
      ite
                306
                      301
308
             3
                203
                      10
                            307
                                  IF instr4 THEN jump0 ELSE try instr2-3
      ite
309
             3
                      308
     next
                99
```

As the transition for pc are quite possibly the most complex I added some explanation. x0 and x1 are skipped for now, so next registers x2 and x3:

```
314
                 102
                                         319
                                                           103
                                                                 9
      init
                                                init
                                                                  103
315
      one
             4
                                         320
                                                add
                                                       4
                                                           102
             4
                                                       4
                                                                        103
316
      add
                 102
                        315
                                         321
                                                ite
                                                           201
                                                                  320
             4
317
      ite
                 202
                        316
                              102
                                         322
                                               next
                                                       4
                                                           103
                                                                 321
318
             4
                 102
                       317
      next
```

x2 increments by one each time the third instruction is run and x3 adds x2 every time the second instruction is run. All other registers and the memory do not change during execution, so I show them in one big block:

```
init 4 100 9
310
                           340
                                 next 4 112 112
                                                       361
                                                             init 4
                                                                     123 9
           4
              100 100
311
     next
                           341
                                 init 4
                                         113 9
                                                       362
                                                             next
                                                                  4
                                                                     123
                                                                          123
312
      init
           4
              101
                  13
                           342
                                 next
                                       4
                                         113
                                              113
                                                       363
                                                                  4
                                                                     124
                                                                         9
                                                             init
           4
313
     next
              101
                  101
                           343
                                 init
                                      4
                                         114 9
                                                       364
                                                            next 4
                                                                     124 124
              104
323
     init
           4
                  9
                           344
                                 next 4
                                         114 114
                                                       365
                                                                  4
                                                                     125 9
                                                             init
           4
                  104
                           345
                                 init 4
324
     next
              104
                                         115 9
                                                                     125
                                                       366
                                                            \mathtt{next} 4
                                                                         125
325
           4
              105
                  9
                           346
                                 next 4
                                         115
                                              115
     init
                                                             init 4
                                                       367
                                                                     126
326
     next
           4
              105
                  105
                           347
                                 init
                                       4
                                         116
                                              9
                                                                  4
                                                                         126
                                                       368
                                                             next
                                                                     126
327
                  9
                           348
                                         116
           4
              106
                                       4
                                              116
     init
                                 next
                                                       369
                                                             \mathtt{init}\ 4
                                                                     127
328
           4
                           349
                                         117
     next
              106
                  106
                                 init 4
                                                       370
                                                            next 4
                                                                     127
                                                                         127
329
      init
           4
              107
                  9
                           350
                                 next
                                      4
                                         117 117
                                                       371
                                                             \mathtt{init}\ 4
                                                                     128
                                                                         9
330
           4
                           351
              107
                  107
                                 init 4
                                         118 9
     next
                                                       372
                                                             next 4
                                                                     128
                                                                          128
331
           4
              108
                  9
                           352
                                 next 4
                                         118
                                              118
      init
                                                       373
                                                             init
                                                                  4
                                                                     129
332
           4
              108
                  108
                           353
                                 init 4
                                         119
                                              9
     next
                                                                     129
                                                       374
                                                                  4
                                                                         129
                                                            next
333
     init
           4
              109
                  9
                           354
                                 next 4
                                         119 119
                                                       375
                                                             init 4
                                                                     130 9
334
     next
           4
              109 109
                           355
                                 init 4
                                         120 9
                                                       376
                                                             next 4
                                                                     130 130
335
     \mathtt{init}\ 4
              110 9
                           356
                                 next 4
                                         120 120
                                                       377
                                                             init 4
                                                                     131
                                                                          9
336
     next
           4
              110
                  110
                           357
                                 init
                                       4
                                         121
                                              9
                                                       378
                                                                  4
                                                                     131
                                                                          131
                                                            next
337
      init
           4
              111
                  9
                           358
                                 next
                                       4
                                         121
                                              121
                                                             init 5
                                                       379
                                                                     199 193
                                 \mathtt{init}\ 4
338
           4
                           359
                                         122
                                              9
     next
              111 111
                                                       380
                                                            next 5 199 199
339
     init 4 112 9
                           360
                                 next 4 122 122
```

Now only the instruction flags and with them the only property are left to handle:

```
200 7
381
      init
                                instr0 executes initally
382
                   200 203
                                instr0 only after instr3
     next
                   201 6
      init
384
                   200 -303
                                instr0 and no branch
      and
                   201 384
                                instr1 only after non-branching instr0
385
      next
386
                   202 6
      init
                                instr2 only after instr2
387
                    202 201
      next
                   203 6
388
      init
389
                   203 202
                                instr3 only after instr3
     next
390
                   204 6
                   200 303
391
      and
392
                   204 391
                                endflag if instr0 branches
      next
400
      bad
             204
                                endflag terminates
```

And with this, the model is can be run. The whole suite of add tests can be derived from this model by changing the constant value of node 13 to the appropriate loop count.

5.2 Results

To start I placed all iterations based benchmarks with btormc into Table 3 and the benchmarks of extended address space into Table 4. Also to get an overview of the times, I plotted the times of Table 3 in Figure 22. From Table 4 one can assume that the extension of address space does not impact the runtime of the model checker in a meaningful way. As seen in Table 5, with rising loop counts, memory operations need increasingly more time in comparison to their respective non-memory operation benchmarks. Also with rising loop counts the impact of large amounts of memory initialised is reduced, which was to be expected.

The nopc benchmark is significantly faster than my model. This was to be expected, as Schrögendorfer models one RISC-V program specifically whereas I model the processor and feed it different programs by initialization. In this perspective, it is not surprising that a specialised model is faster than a generalised one.

I also attempted to benchmark with the AVR and Pono model checkers, as they ranked first and second in the 2024 hardware model checking competition. Unfortunately, AVR did not terminate within 15 minutes when checking the add_0256 benchmark.

| loona | 1 | base | ful | $_{ m llmem}$ | nopc |
|-------|--------|----------|--------|---------------|-------|
| loops | add | writemem | add | writemem | add |
| 0256 | 2.635 | 2.877 | 9.759 | 13.344 | 0.136 |
| 0512 | 6.195 | 7.306 | 16.402 | 24.209 | 0.268 |
| 0768 | 10.802 | 13.283 | 24.093 | 36.388 | 0.414 |
| 1024 | 16.306 | 21.004 | 32.732 | 50.376 | 0.569 |
| 1280 | 23.032 | 30.200 | 42.410 | 65.746 | 0.728 |
| 1536 | 30.669 | 41.262 | 52.961 | 83.036 | 0.898 |
| 1792 | 39.463 | 53.940 | 64.598 | 101.475 | 1.075 |
| 2048 | 48.944 | 68.521 | 77.084 | 122.189 | 1.276 |

Table 3: Times of iterations based benchmarks

| pc width | add_0256 | add_1024 | writemem_0256 | writemem_1024 |
|----------|----------|----------|---------------|---------------|
| 16 | 2.635 | 16.306 | 2.877 | 21.004 |
| 17 | 2.632 | 16.464 | 2.88 | 21.131 |
| 18 | 2.626 | 16.511 | 2.890 | 21.215 |
| 19 | 2.626 | 16.452 | 2.889 | 21.181 |
| 20 | 2.624 | 16.460 | 2.890 | 21.163 |

Table 4: Times of extended address space benchmarks

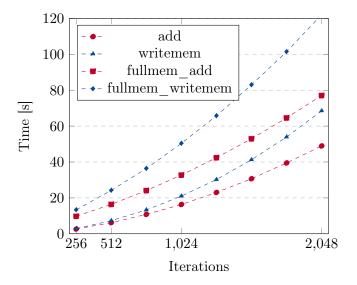


Figure 22: Table 3 plotted

| loops | $rac{add}{writemem}$ | $rac{fullmem_add}{fullmem_writemem}$ | $rac{add}{fullmem_add}$ | $rac{writemem}{fullmem_writemem}$ | $rac{add}{nopc_add}$ |
|-------|-----------------------|---|---------------------------|-------------------------------------|------------------------|
| 0256 | 0.92 | 0.73 | 0.27 | 0.22 | 19.38 |
| 0512 | 0.85 | 0.68 | 0.38 | 0.3 | 23.12 |
| 0768 | 0.81 | 0.66 | 0.45 | 0.37 | 26.09 |
| 1024 | 0.78 | 0.65 | 0.5 | 0.42 | 28.66 |
| 1280 | 0.76 | 0.65 | 0.54 | 0.46 | 31.64 |
| 1536 | 0.74 | 0.64 | 0.58 | 0.5 | 34.15 |
| 1792 | 0.73 | 0.64 | 0.61 | 0.53 | 36.71 |
| 2048 | 0.71 | 0.63 | 0.63 | 0.56 | 38.36 |

Table 5: Relative runtime of benchmarks

Pono determined that this benchmark is satisfiable, but required nearly six minutes using the <code>-smt-solver cvc5</code> option. With <code>-smt-solver bzla</code>, Pono was slower but functional; other solvers reported inability to handle arrays. These results suggest that model checkers considered superior in general are not necessarily optimal for my model, whereas btorme, despite being unmaintained since August 2024, performed best. I suspect that newer model checkers are optimized for handling inputs, as most competition benchmarks involve at least one input beyond a clock signal, while my model operates solely with known constants and its execution time is dependent on rapid state iteration.

Another issue with AVR and Pono is their inability to generate a "complete" witness, as produced by the btormc option -trace-gen-full, which provides the values of all states in the final frame. Without this feature, it is not possible to reconstruct a state from their output after execution.

6 Conclusion

I developed tools to transition from a state to a model and from a witness of this model back to a state. Additionally, I implemented a fuzzer for the states to verify the correct functioning of the model, as well as a set of basic tests to benchmark its performance. Finally, I presented and discussed the results of these benchmarks, concluding that model checkers which appear superior in general are worse at this specific task of mainly running iterations.

ToDo Counters

To Dos: 3; 1, 2, 3

Parts to extend: 0;

Draft parts: 0;

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(TODO: Add repo versions)