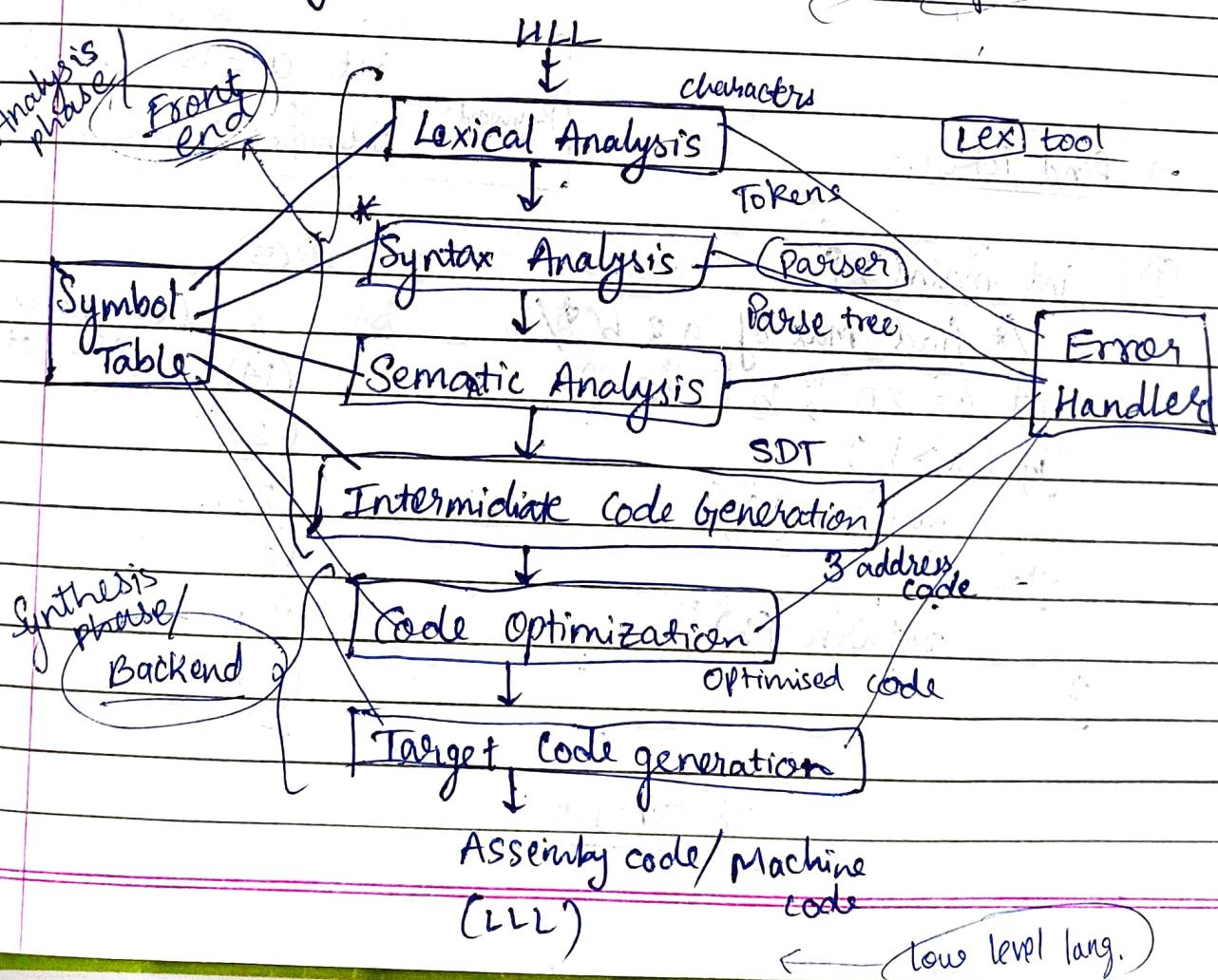


## Compiler Design:

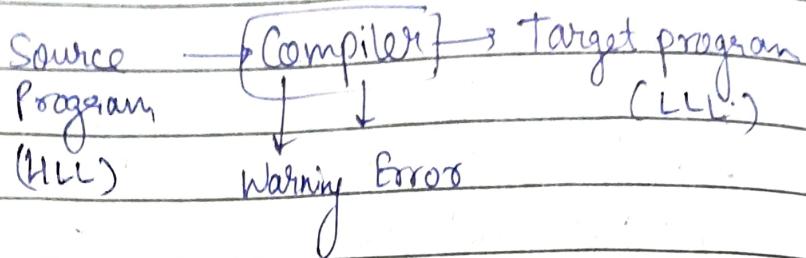
- 1) Lexical Analysis
- 2) Parser (Syntax Analyzer) \*\*\*
- 3) Semantic Analysis (easy)
- 4) Intermediate code generator \*\*
- 5) Code optimization (easy)

V2

### Phases of Compiler:



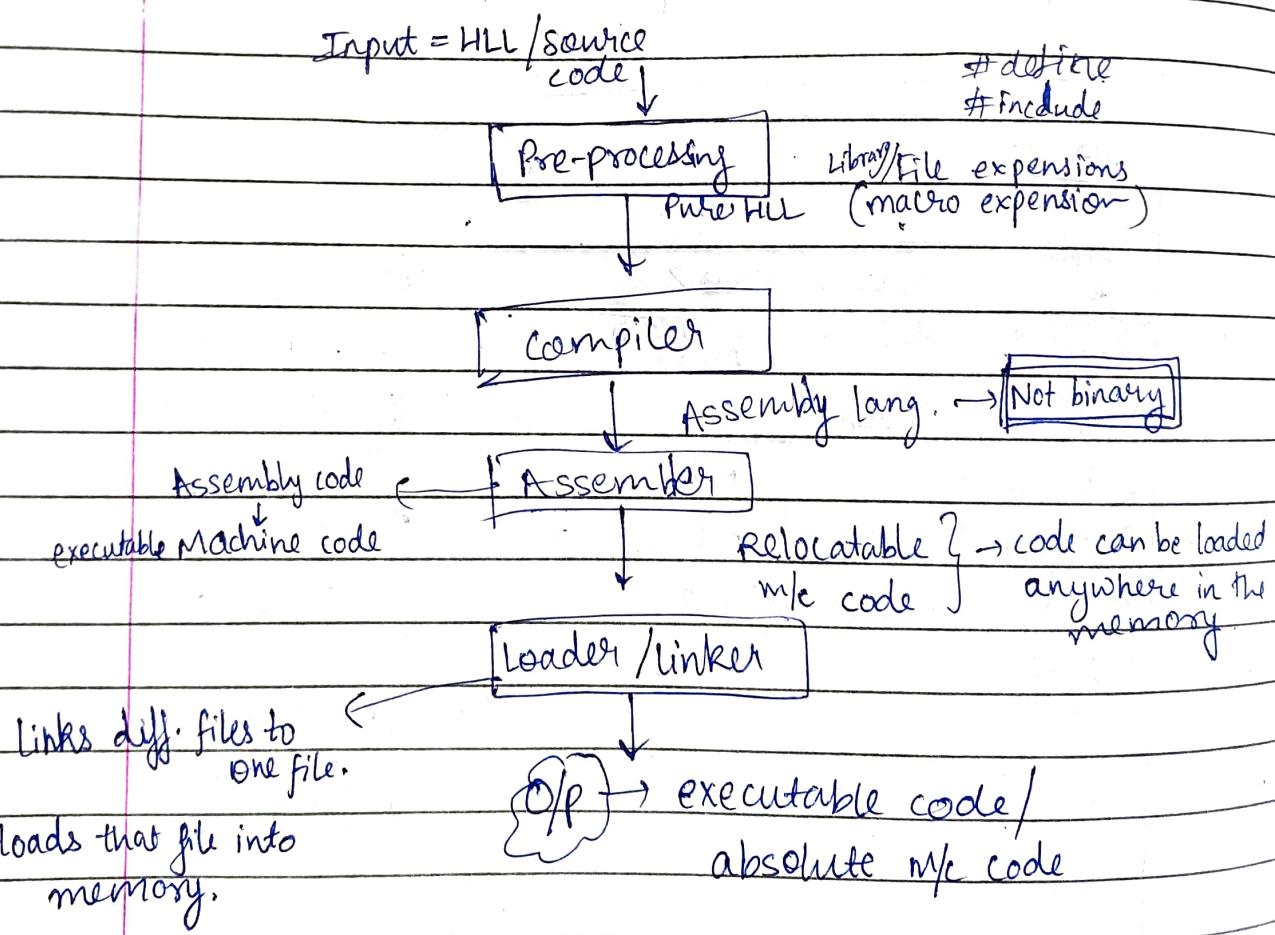
①



- Types of compiler:
- Single pass comp. (process takes 1 hr)
  - MultiPass comp. " multiple

②

## Language Processing System:



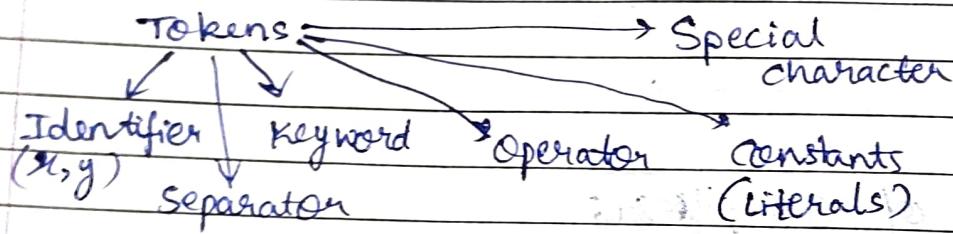
L-3

## ⑤ Lexical Analysis - { Lexen, Tokenizer, Scanner }

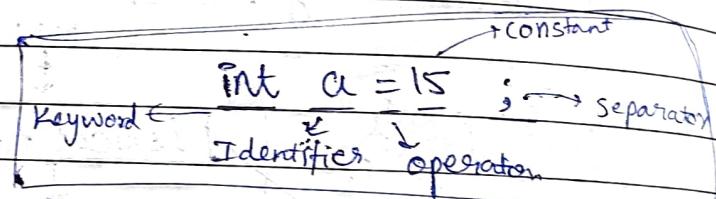
### 1) Tokenization

- 2) Give Error messages
- Exceeding length
  - Unmatched String
  - Illegal character

- 3) Eliminate comments, white spaces (Tab, blank space, new line)



### ⇒ find Tokens:



① int main() {  
 /\* find max of a & b \*/  
int a = 20 b = 30 ;  
if (a > b)  
    return (a);  
else  
    return (b);

⑤

x (comments are not taken)

⑯

⑰

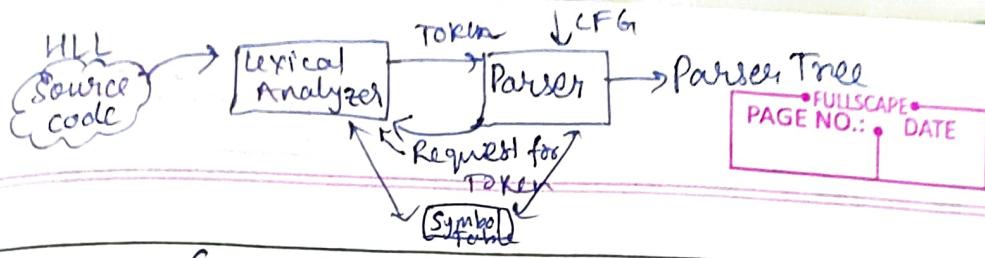
⑱

⑲

⑳

㉑

32 tokens.



② printf (" i=%d, &i=%x ", i, &i); (10)

10 tokens

⇒ Finite Automata (DFA, NFA) is used for tokenisation.  
i.e. (Application of FA.) Machine.

③ int main()

      
    n = y + z ;  
    int n, y, z;  
    printf (" sum=%d\n", n);  
    {

4

26

token

④ main() {

a = b++ + - - - ( + + + = );

printf ("%d\n", a, b);

?

4

15

25

tokens

⑤ main() {

int a=10;

char b="abc";

int c = 30;

char d = "xyz";

int /\*comment\*/ t = 40.5;

4

9

14

20

26

32

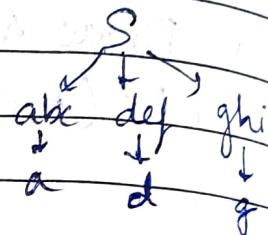
(33) tokens

V-5

⇒ Finding First() and Follow()

First(A) contains all terminals present in first place of every string derived by A.

- (1)  $S \rightarrow abc \mid def \mid ghi$
- (2) First(terminal) → terminal
- (3) First( $\epsilon$ ) →  $\epsilon$



- Q2)  $S \rightarrow ABC \mid ghi \mid jkl$   
 $A \rightarrow a \mid b \mid c$   
 $B \rightarrow b$   
 $D \rightarrow d$

$$\text{First}(D) = d$$

$$\text{First}(A) = (a, b, c)$$

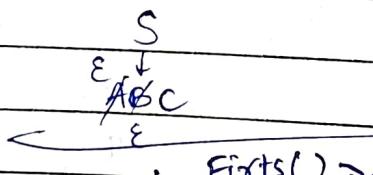
$$\text{First}(S) = (a, b, c, g, j)$$



- Q3)  $S \rightarrow ABC$   
 $B \rightarrow cd \mid \epsilon$   
 $A \rightarrow a \mid b \mid \epsilon$   
 $C \rightarrow ef \mid \epsilon$

$$\text{First}(C) = (e, f, \epsilon)$$

$$\text{First}(S) = (a, b, c, d, e, f, \epsilon)$$



- Q4)  $E \rightarrow TE'$   
 $E' \rightarrow *TE' \mid \epsilon$   
 $T \rightarrow FT'$   
 $T' \rightarrow \epsilon \mid +FT'$   
 $F \rightarrow id \mid (E$

Firsts() ↗

id, C

\* ,  $\epsilon$

id, (

+ ,  $\epsilon$

id, (

1/b Follow(1)

Follow(A) contains set of all terminals present immediate in right of 'A'

Rules:

1) Follow of start symbol is \$

$$F(A) = \{\$\}$$

\*Follow never contains \$\\$

Q) 2)  $S \rightarrow ACD$   
 $C \rightarrow a1b$ .

$$F(A) = \text{First}(C) = \{a, b\}$$

$$F(D) = \text{Follow}(S) = \{\$\}$$

3)  $S \rightarrow aSbS \mid bSaS \mid \epsilon$

$$F(S) = \{\$, b, a\}$$

4)  $S \rightarrow AaAb \mid BbBa$

$$A \rightarrow \epsilon$$

$$B \rightarrow \epsilon$$

$$F(A) = \{a, b\}$$

$$F(B) = \{b, a\}$$

5)  $S \rightarrow AB \mid C$

$$A \rightarrow DEF$$

$$B \rightarrow \epsilon$$

$$C \rightarrow \epsilon$$

$$D \rightarrow \epsilon$$

$$E \rightarrow \epsilon$$

$$F \rightarrow \epsilon$$

$$F(A) = \text{First}(B)$$

$$\epsilon \Rightarrow \text{First}(C)$$

$$\epsilon \Rightarrow F(S) = \{\$\}$$

Parsing: It is a process of deriving string from a given Grammar.

FULLSCALE  
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a given Grammar

Kit

Parsees:

Top Down Parser

Recursive Descent

LL(1)  
(Predictive)  
Parser

Bottom Up Parser

LR(k)  
Operator Precedence

LR(0)

LR(1)

LR(0)

SLR(1)

LALR(1), CLR(1)

LL  
left to right  
left most derivation

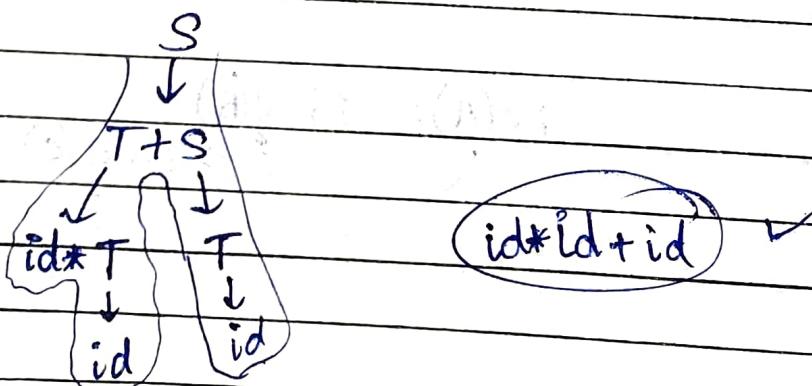
\* CFG is used

$$Q) S \rightarrow T + S \mid T$$

$$T \rightarrow id * \text{ or } T \mid id \mid (S)$$

$w = id * id + id$  → string.

ans:



## L-8 Check LL(1) Grammar: (Parsing Table)

$$S \rightarrow (L) \mid a^2$$

$$L \rightarrow {}^3 SL'$$

$$L' \rightarrow {}^4 \varepsilon \mid {}^5 SL'$$

$$S \rightarrow aSbS \mid bSaS \mid \varepsilon$$

Ans:

First()

$$F(S) = \{ \varepsilon, a \}$$

$$F(L) = \{ c, a \}$$

$$F(L') = \{ \varepsilon, \mid \}$$

Follow()

$$F_0(S) = \{ \$, \}, ?$$

$$F_0(L) = \{ \mid \}$$

$$F_0(L') = \{ \mid \}$$

Parse Table

	(	)	a	,	\$
S	$\overset{1}{S} \rightarrow (L)$		$\overset{2}{S} \rightarrow a$		
L	$\overset{3}{L} \rightarrow SL'$		$\overset{3}{L} \rightarrow SL'$		
L'		$\overset{4}{L}' \rightarrow \varepsilon$		$\overset{5}{L}' \rightarrow SL'$	

$$S \rightarrow (L)$$

$$S \rightarrow a$$

$$L \rightarrow SL'$$

$$L' \rightarrow \varepsilon$$

= first =  $\therefore L'$  follow

$$L' \rightarrow (SL')$$

$\therefore \mid$

(ii)

$$S \rightarrow aSbS \mid {}^2 bSaS \mid {}^3 \varepsilon$$

$$F(S) = \{ a, b, \varepsilon \}$$

$$F_0(S) = \{ \$, b, a \}$$

	a	b	\$
S	$\overset{1}{S} \rightarrow abS$	$\overset{2}{S} \rightarrow bSaS$	3
	$\overset{3}{S} \rightarrow \varepsilon$	$\overset{3}{S} \rightarrow \varepsilon$	$S \rightarrow \varepsilon$

$$S \rightarrow \varepsilon$$

$$\therefore \text{follow}(S) = \{ b, a, \$ \}$$

$\therefore$  This is not LL(1) Grammar.

~~Starts from main() to find if it is correct or not~~

## Compiler

- 1) Takes entire program at once as input
- 2) High speed
- 3) Memory required ↑
- 4) Errors - displayed together
- 5) Error detection hard
- 6) compiler are larger in size
- 7) eg: C, C++ uses compl.

## Interpreter

- 1) It takes single line of code at a time

- 2) Speed - low

- 3) Memory required ↓

- 4) Errors - If one line has error it will not execute further program.



- 5) Error detection easy

- 6) smaller in size

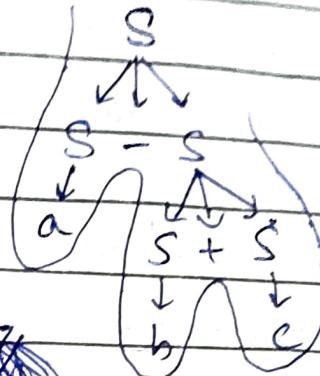
- 7) Python, perl, Ruby uses interpreter

## ① Left most Derivative:

eg:  $S \rightarrow S+S \mid S-S \mid a \mid b \mid c$

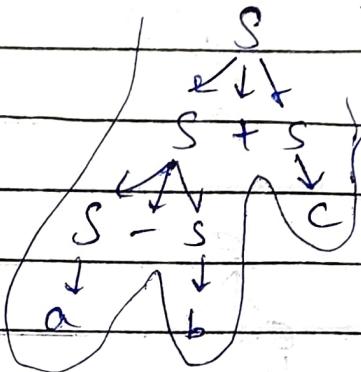
input:  $a-b+c$

$$\begin{aligned} LMD &= S-S \\ &= a-S \\ &= a-a-S+S \\ &= a-b+c \end{aligned}$$



## ② Right most Derivative:

$$\begin{aligned} RMD &= S+S \\ &= S+C \\ &= S-S+C \\ &= S-b+c \\ &= a-b+c \end{aligned}$$



## ③ Parse Tree:

It is a graphical representation of symbol that can be terminals or non-terminals.

### Properties:

- ① Root is always the start symbol
- ② All leaf nodes are terminals
- ③ All interior nodes are Non-Ter.

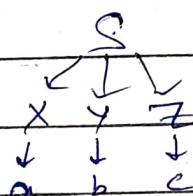
eg:

$$S \rightarrow XYZ$$

$$X \rightarrow a$$

$$Y \rightarrow b$$

$$Z \rightarrow c/d$$



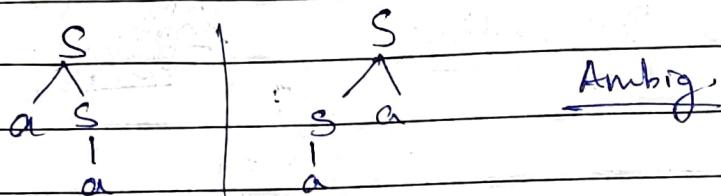
$$L = \{abc, abd\}$$

## Q) Ambiguous Grammar:

→ If we have more than 1 parse tree possible.  
 ∴ Grammar is ambiguous.

Q2)  $S \rightarrow aS \mid Sa \mid a$

input - aa

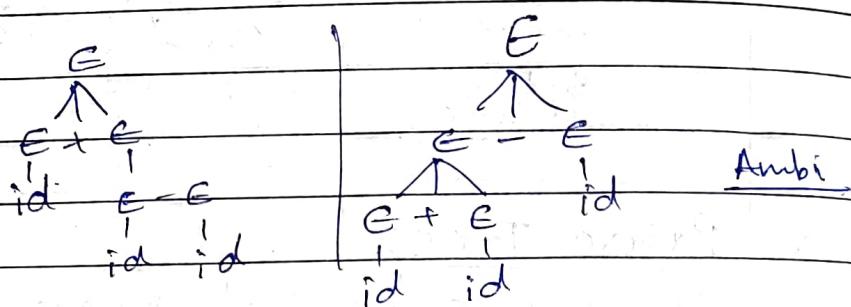


Q3)  $E \rightarrow E+E$

$$E \rightarrow E-E$$

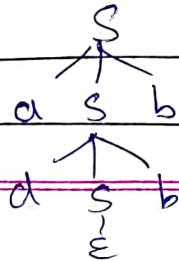
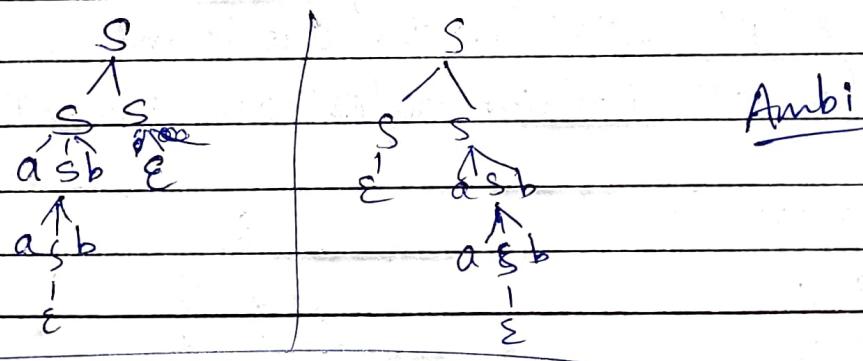
$$E \rightarrow id$$

input = id+id-id



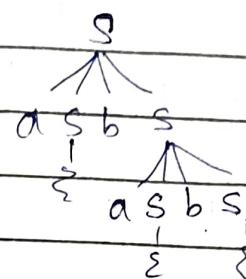
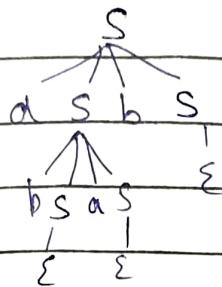
Q4)  $S \rightarrow aSb \mid SS \mid \epsilon$

("aabbaabb" input)



(a)  $S \rightarrow aSbS \mid bSaS \mid \epsilon$

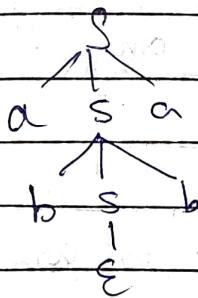
input = abab



Ambi:

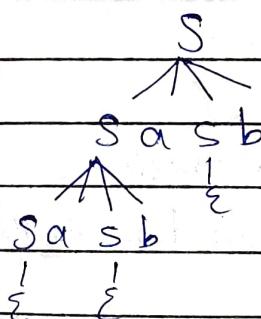
(b)  $S \rightarrow aSa \mid bSb \mid \epsilon$

~~No-Ambi~~ Un-Ambi

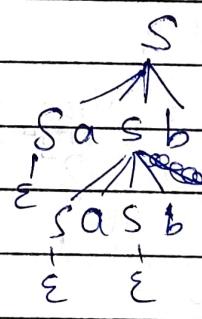


(c)  $S \rightarrow SaSb \mid \epsilon$

input = abab



abab



aabb

Unambi

①  $\Rightarrow$  For Associative Problem, make Left Recursive  
 $\rightarrow$  make left associative or right associative.

FULLSCAPE  
PAGE NO.: DATE

$E \rightarrow E + id$

② Ambiguous  $\rightarrow$  Un-ambiguous

③  $\Rightarrow$  For precedence Problem:

$\Rightarrow$  Introduce several different symbols like:

eg:  $E \rightarrow E + E \mid E * E \mid id$

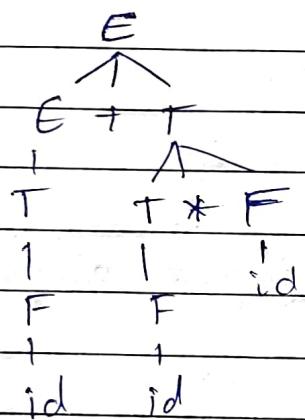
"+" < "\*" : precedence

$E \rightarrow E + T \mid T$

$T \rightarrow T * F \mid F$

$F \rightarrow id$

} Once we have reached T, we cannot generate any +



} So, we are taking care of precedence by defining diff. level.

(2↑3↑2)

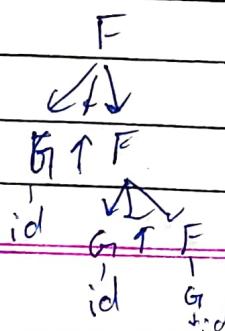
$2^{3^2}$

Right associative

(Grow towards right)

and:  $F \rightarrow G_1 \uparrow F \mid G$

$G_1 \rightarrow id$



(Q)  $B \rightarrow B \text{ or } B \mid B \text{ and } B \mid \text{not } B \mid t \mid f$

$B \rightarrow \cancel{B \text{ and } B} \ B \text{ or } F \mid F$

$F \rightarrow F \text{ and } G_1 \mid G$

$G_1 \rightarrow \text{not } G_1 \mid t \mid f$

or < and < not  
precedence.

or } left  
and } associative

(Q)  $A \rightarrow A \$ B \mid B$

$B \rightarrow B \# C \mid C$

$C \rightarrow C @ D \mid D$

$D \rightarrow d$

Tell associativity & precedence

ans: \$ # @ precedence  
A, B, C left associative

(Q)  $E \rightarrow E + E \mid E * E \mid \cancel{F}$

$F \rightarrow \text{id} - \text{id}$

+ and \* have the same precedence

- has high precedence than + & \*

(Q) How to remove left Recursion?

$A \rightarrow A\alpha \mid B$

① Direct  $B \rightarrow B\alpha$

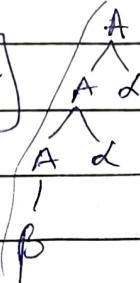
② Indirect  $\begin{array}{|l} A \rightarrow S^m \\ S \rightarrow A^k \end{array}$

## Recursion

$$A \rightarrow A\alpha | B$$

left Rec.

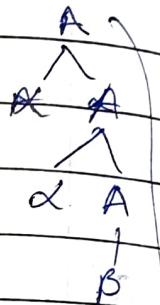
$$\text{Lang.} = B\alpha^*$$



$$A \rightarrow \alpha A | B$$

Right Rec.

$$\text{Lang.} = \alpha^* B$$



$$A() \{$$

A();

$\alpha$ ;

}

Infinite loop

$$A() \{$$

$\alpha$ ;

A();

}

Not going  
Infinite loop as  
 $\alpha$  checks condition

⊗

∴ L.R. convert R.R.

⊗

$$A \rightarrow A\alpha | B$$

→

$$\begin{array}{l} A \rightarrow BA' \\ A' \rightarrow \alpha A' | \epsilon \end{array}$$

\*\*

①

$$E \rightarrow E + T | T$$

. A:  $\overline{A} \overline{\alpha} \overline{B}$

anti  $\alpha$

$$E \rightarrow TE'$$

$$E' \rightarrow +TE' | \epsilon$$

Remove L.R.

$$\textcircled{1} \quad S \rightarrow \underline{S} \underline{O} \underline{S} \underline{I} \underline{S}, \underline{O} \underline{I} \underline{I}$$

$$A \rightarrow BA' \quad \boxed{A' \rightarrow \alpha A' | \epsilon} \quad S \rightarrow OIS^I$$

$$S^I \rightarrow OSISS^I | \epsilon$$

$$\textcircled{2} \quad S \rightarrow (L) | \alpha$$

$$L \rightarrow \underline{L}, \underline{S} | \underline{S}$$

$$\text{and: } L \rightarrow SL'$$

$$L' \rightarrow , SL' | \epsilon$$

$$S \rightarrow (L) | \alpha$$

$$\boxed{A \rightarrow BA'}$$

$$\boxed{A' \rightarrow \alpha A' | \epsilon}$$

$$\textcircled{3} \quad A \rightarrow A\alpha, | A\alpha_1 | A\alpha_2 | A\alpha_3 | \dots$$

$$\beta_1 | \beta_2 | \beta_3 | \dots$$

$$A \rightarrow A\alpha | \beta$$

and:

$$A \rightarrow \beta_1 A' | \beta_2 A' | \beta_3 A'$$

$$A' \rightarrow \alpha_1 A' | \alpha_2 A' | \alpha_3 A' \dots$$

$$\boxed{A \rightarrow BA'}$$

$$\boxed{A' \rightarrow \alpha A' | \epsilon}$$

① Grammar

Ambiguous (✗)      Unambiguous (✓)  
 (2 parse tree)

→ No parse work for it

② Grammar

LR      RR  
 ✗      ✓

→ Top down parse doesn't accept it.

→ convert L.R. to R.R.

$\xleftarrow{G_1} \xrightarrow{G_2}$   
 Deterministic      Non-D.  
 x

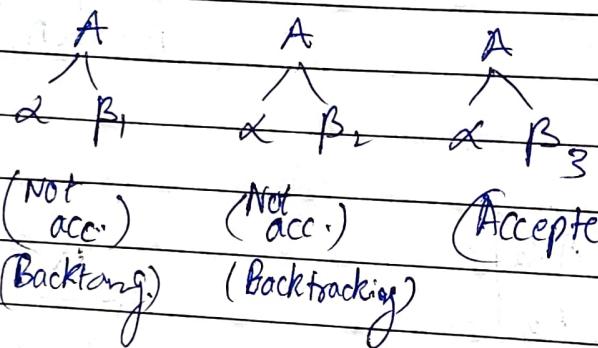
$A \rightarrow A\alpha | \beta$

(Q)  $S \rightarrow Aa$   
 $\quad \quad \quad A \rightarrow Sb | c$

$$\begin{array}{c} A \rightarrow \beta A' \\ A' \rightarrow \alpha A' | \epsilon \end{array}$$

$\Rightarrow S \rightarrow Aa$   
 $\underline{A \rightarrow Aab | c} \Rightarrow A \rightarrow CA'$   
 $\quad \quad \quad A' \rightarrow abA' | \epsilon$

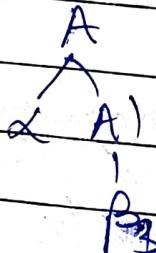
\*  $\Rightarrow A \rightarrow \alpha\beta_1 | \alpha\beta_2 | \alpha\beta_3$  we want  $\alpha\beta_3$



$\Rightarrow$  Left Factoring (Non-Deterministic  $\xrightarrow{*}$  Deterministic)

$A \rightarrow \alpha\beta_1 | \alpha\beta_2 | \alpha\beta_3$   
 to

$A \rightarrow \alpha A'$   
 $A' \rightarrow \beta_1 | \beta_2 | \beta_3$



Q)  $S \rightarrow bSSaas$   
     |  $bSSash$   
     |  $\underline{bSb}$   
     |  $a$

and!  $S \rightarrow bSS' | a$   
 $S' \rightarrow Saas | Sasb | b \rightarrow S' \rightarrow SaS'' | b$   
 $S'' \rightarrow aS | sb$

④ LL(1) Parser - (Top-Down Parser)  
     - left to Right scan,  
     - Left Most Derivative

⇒ First():  $S \rightarrow AB \quad A \rightarrow a$   
 $\text{First}(S) = \text{First}(A) = a$

$S \rightarrow A\overbrace{B}^{\text{First}(A)} \quad A \rightarrow a | \epsilon \quad B \rightarrow b$   
 $\text{First}(S) = \text{First}(A) = \{a, \text{First}(B)\} = \{a, b\}$

⇒ Follow():

- Follow of start symbol is always \$
- for  $A \rightarrow \alpha B$ ,  $\text{follow}(B) = \text{follow}(A)$
- for  $S \rightarrow aABC$ ,  $\text{follow}(A) = \text{first}(BC) = \text{first}(B)$   
 $B \rightarrow b$

		First()	Follow()
(1)	$S \rightarrow ABCD$	$\{b\}$	$\{\$\}$
	$A \rightarrow b$	$\{b\}$	$\{c\}$
	$B \rightarrow c$	$\{c\}$	$\{d\}$
	$C \rightarrow d$	$\{d\}$	$\{e\}$
	$D \rightarrow e$	$\{e\}$	$\{\$\}$

$\text{follow}(A) = \text{first}(BCD)$

$= \text{first}(B)$

$\text{follow}(D) = \text{follow}(S)$

		First()	Follow()
(1)	$S \rightarrow A B C D E$	$\{a, b, c\}$	$\{\$\}$
	$A \rightarrow a   \epsilon$	$\{a, \epsilon\}$	$\{b, c\}$
	$B \rightarrow b   \epsilon$	$\{b, \epsilon\}$	$\{c\}$
	$C \rightarrow c$	$\{c\}$	$\{d, e, \$\}$
	$D \rightarrow d   \epsilon$	$\{d, \epsilon\}$	$\{e, \$\}$
	$E \rightarrow e   \epsilon$	$\{e, \epsilon\}$	$\{\$\}$

		First()	Follow()
(2)	$S \rightarrow Bb   Cd$	$\{a, b, e, d\}$	$\{\$\}$
	$B \rightarrow aB   \epsilon$	$\{a, \epsilon\}$	$\{b\}$
	$C \rightarrow eC   \epsilon$	$\{e, \epsilon\}$	$\{d\}$

$E \rightarrow TE'$	$\{id, C\}$	$\{\$, )\}$
$E' \rightarrow +TE'   \epsilon$	$+ , \epsilon$	$\{\$, )\}$
$T \rightarrow FT'$	$\{id, C\}$	$\{+, \$, )\}$
$T' \rightarrow *FT'   \epsilon$	$* , \epsilon$	$\{\$, ), *\}$
$F \rightarrow id   (E)$	$\{id, ($	$\{\$, ), +, *\}$

		Fi	Fo
(1)	$S \rightarrow A(CB) \mid CB(Ba)$	a, b, d, g, h, ε	\$
	$A \rightarrow da \mid Bc$	d, g, h, ε	h, \$, g, \$
	$B \rightarrow g \mid \epsilon$	g, ε	\$, a, h, g
	$C \rightarrow h \mid \epsilon$	h, ε	g, \$, b, h

(2) Construct LL(1) Parsing Table.

$\Rightarrow S \rightarrow AaAb \mid BbBa$

$A \rightarrow \epsilon$

$B \rightarrow \epsilon$

} First remove  
- left recursion.  
- left factoring.

	First	Follow		a	b	\$
$S \rightarrow AaAb \mid BbBa$	a, b	\$	S	$S \rightarrow AaAb$	$S \rightarrow BbBa$	
$A \rightarrow \epsilon$	ε	a, b	A	$A \rightarrow \epsilon$		
$B \rightarrow \epsilon$	ε	b, a	B	$B \rightarrow \epsilon$	$B \rightarrow \epsilon$	

(3)  $\Rightarrow$  The Gate NVR:

Y-10

$$E \rightarrow TE'$$

$$E' \rightarrow \epsilon \mid TE'$$

First( $\epsilon$ )

{ id, ( }

{ +, }

Follow( $\epsilon$ )

{ +, \$, ) }

FULL SCRAP PAGE NO.: DATE

- Grammer

$$T \rightarrow FT'$$

{ id, ( } { +, \$, ) }

- first

$$T' \rightarrow \epsilon \mid *FT'$$

{ \*, } { +, \$, ) }

- Follow

$$F \rightarrow id \mid (E)$$

{ id, ( } { \*, +, \$, ) }

eg:

	id	+	*	(	)	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
$E'$		$E' \rightarrow TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$			$T \rightarrow PT'$		
$T'$		$T' \rightarrow \epsilon$	$T' \rightarrow FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow id$			$F \rightarrow (E)$		

stack

input

Production

Reversed  
(stack)

\$ E

id + id \$

$E \rightarrow TE'$

\$ E' I

id + id \$

$T \rightarrow FT'$

\$ E' T' F

id + id \$

$F \rightarrow id$

\$ E' T' id

id + id \$

Pop();

\$ E' T'

+ id \$

$T' \rightarrow \epsilon$

\$ E'

+ id \$

$E' \rightarrow TE'$

\$ E' T +

+ id \$

Pop();

\$ E' T I

id \$

$T \rightarrow FT$

\$ E' T F

id \$

$F \rightarrow id$

\$ E' T' id

id \$

Pop();

\$ E' T'

\$

$T' \rightarrow \epsilon$

\$ E'

\$

$E' \rightarrow \epsilon$

\$

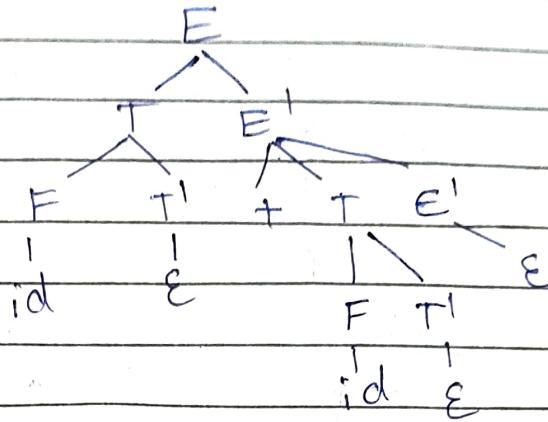
\$

Accepted.

# (LL(1) Parsing) or (Predictive parser)

(TOP-DOWN PARSER)

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V.R.

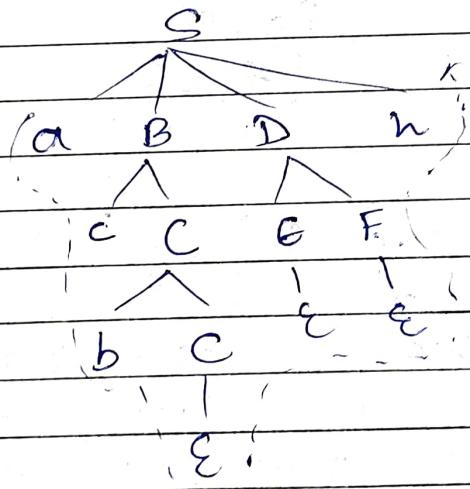
	First()	Follow()
$S \rightarrow aBDh$	{a}	{\$}
$B \rightarrow cC$	{c}	{g, f, h}
$C \rightarrow bC \mid \epsilon$	{b, ε}	{g, f, h}
$D \rightarrow EF$	{g, f, ε}	{h}
$E \rightarrow g \mid \epsilon$	{g, ε}	{f, h}
$F \rightarrow f \mid \epsilon$	{f, ε}	{h}

M	a	b	c	f	g	h	\$
S	$S \rightarrow aBDh$						
B			$B \rightarrow cC$		<del>g</del> <del>ε</del>	<del>g</del> <del>ε</del>	
C			$C \rightarrow bC$		$C \rightarrow \epsilon$	$C \rightarrow \epsilon$	$C \rightarrow \epsilon$
D				$D \rightarrow EF$	$D \rightarrow EF$	$D \rightarrow EF$	
E				$E \rightarrow \epsilon$	$E \rightarrow g$	$E \rightarrow \epsilon$	
F				$F \rightarrow f$		$F \rightarrow \epsilon$	

LL(1) parsing table ↗

	stack	input	production
Q)	\$ S	a cbh \$	$S \rightarrow aBDh$
ans:	\$ hDBa	acb h \$	POP();
	\$ hDB	cbh \$	$B \rightarrow cC$
	\$ hDCc	c bh \$	POP();
	\$ hDC	bh \$	$C \rightarrow bC$
	\$ hDCb	bh \$	POP();
	\$ hDC	h \$	$C \rightarrow \epsilon$
	\$ hD	h \$	$D \rightarrow EF$
	\$ hFE	h \$	$E \rightarrow \epsilon$
	\$ hF	h \$	$F \rightarrow \epsilon$
	\$ h	h \$	POP();
	\$	\$	<u>Accept</u>

Last Node  
Free



acb

## Bottom Up Parser

LR parser (Unambiguous)

LR(0) SLR(1) CLR(1) LALR(1)

Operator Parser (Ambiguous)

RMD in Reverse

(right most derivative)

✓  
LR(1)

LR(0)

## → Closure (I)

1. Add LR(0) item I to closure (I)

2. If  $A \rightarrow \alpha \cdot B\beta$  is LR(0) item I and  $B \rightarrow \gamma$  is in G, then Add  $B \rightarrow \gamma$  to closure (I) also.

3. Repeat above two steps from every newly added LR(0) item.

## → Goto (I, X)

1. Add LR(0) item I by moving dot after x.

2. Apply closure to the result obtained in step 1.

eg:  $S \rightarrow AA$   
 $A \rightarrow aA \mid b$

closure ( $S \rightarrow \cdot AA$ )

$$\Rightarrow S \rightarrow \cdot AA$$

$$A \rightarrow \cdot aA$$

$$A \rightarrow \cdot b$$

} closure  $\Rightarrow$  same

closure ( $S \rightarrow A \cdot A$ )

$$\Rightarrow S \rightarrow A \cdot A$$

$$A \rightarrow \cdot aA$$

$$A \rightarrow \cdot b$$

} closure  $\Rightarrow$  same

Goto ( $S \rightarrow \cdot AA$ , A)

④  $\Downarrow$

( $S \rightarrow A \cdot A$ )  $\Rightarrow$  closure

$S \rightarrow A \cdot A$

$A \rightarrow \cdot aBA$

$A \rightarrow \cdot b$

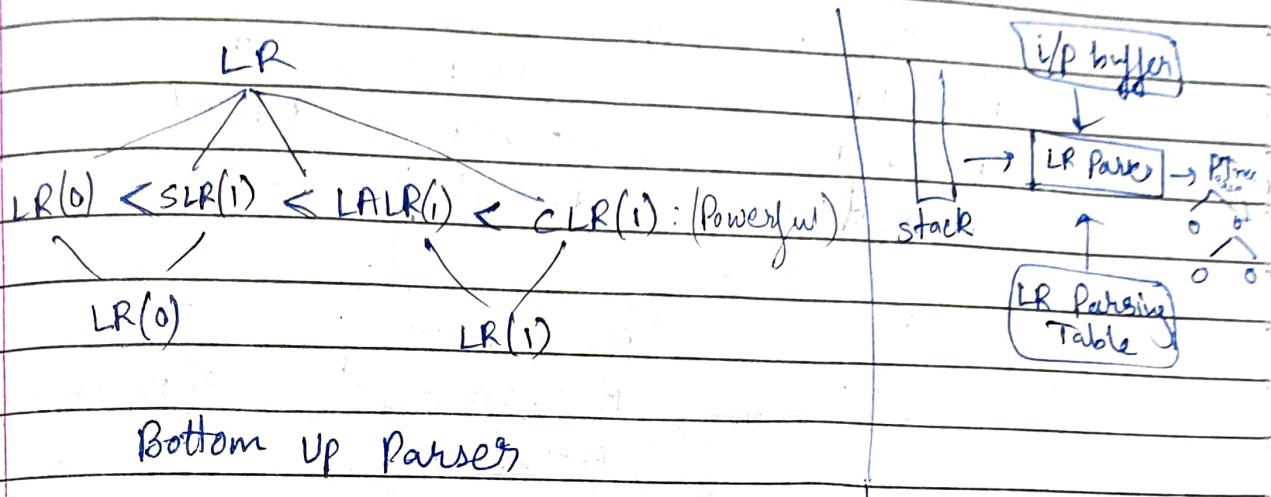
Goto ( $S \rightarrow A \cdot A$ , A)

$\Downarrow$

closure ( $S \rightarrow AA \cdot$ )

$\Downarrow$

$S \rightarrow AA \cdot$

LR ParsersBottom Up Parser① LR(0):

step- (i) Augment Grammar

(ii) Draw Canonical Collections of LR(0) item / DFD

(iii) Number the Productions

(iv) Create the parsing table

(v) Stack implementation

(vi) Draw parsing tree

eg:

$$E \rightarrow BB$$

$$B \rightarrow cB \mid d$$

ccdd \$

ans: ∵ (i)

$$E' \rightarrow E$$

$$E \rightarrow BB$$

$$B \rightarrow cB \mid d$$

(ii)

$$E' \rightarrow .E$$

(LR(0) items.)

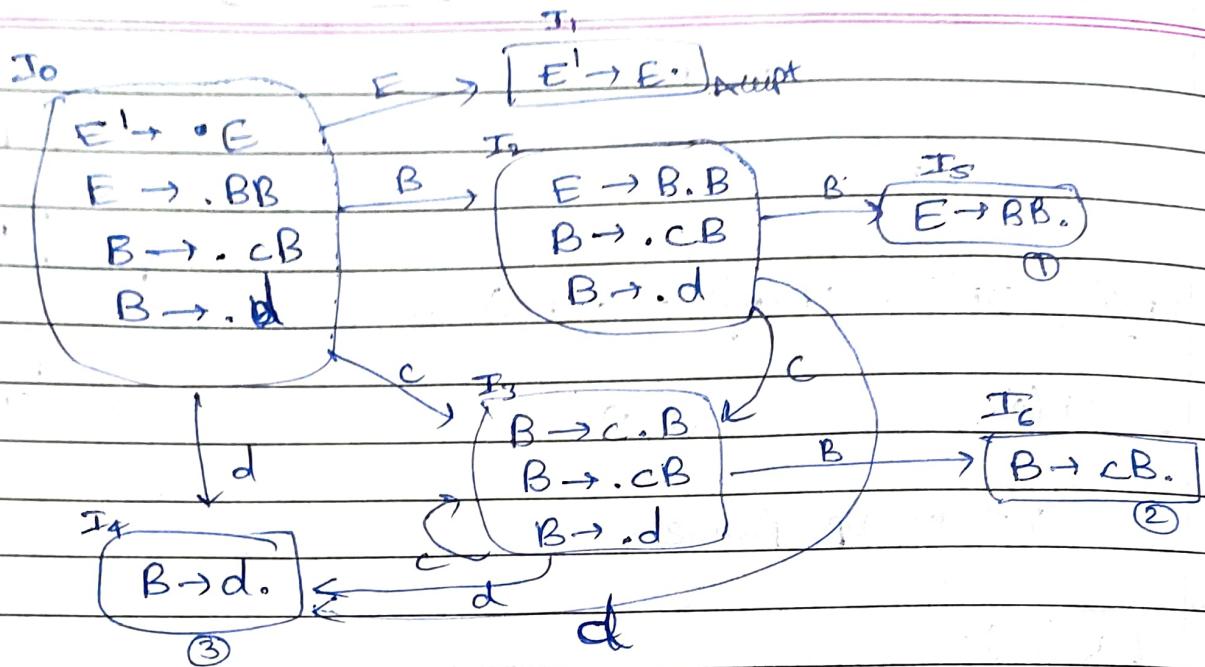
$$E \rightarrow .BB$$

$$B \rightarrow -cB$$

$$B \rightarrow .d$$

$$\begin{aligned} E' &\rightarrow E \\ E &\rightarrow BB \\ B &\rightarrow c \text{ or } d \end{aligned}$$

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(iii)  $E' \rightarrow E$

- ①  $E \rightarrow BB$
- ②  $B \rightarrow CB$
- ③  $B \rightarrow d$

(iv) Parsing Table:

state	Action				Goto	
	c	d	\$	E	B	
I <sub>0</sub>	S <sub>3</sub>	S <sub>4</sub>		1	2	
I <sub>1</sub>			Accept			
I <sub>2</sub>	S <sub>3</sub>	S <sub>4</sub>			5	
I <sub>3</sub>	S <sub>3</sub>	S <sub>4</sub>			6	
I <sub>4</sub>	x <sub>3</sub>	x <sub>3</sub>	x <sub>3</sub>	0		
I <sub>5</sub>	x <sub>1</sub>	x <sub>1</sub>	x <sub>1</sub>			
I <sub>6</sub>	x <sub>2</sub>	x <sub>2</sub>	x <sub>2</sub>			

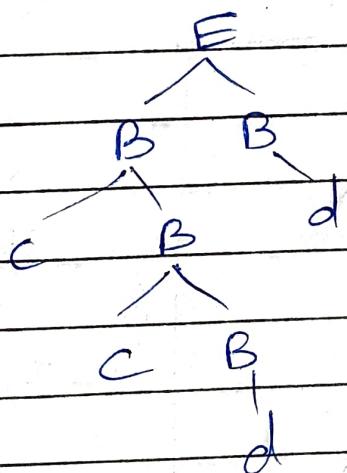
\* If a column has 's' and '0' together then it is not LR(0)

## (v) Stack implementation

stack	Input	Action
\$ 0	ccdd \$	shift c to stack & goto $S_3$
\$ 0 c 3	c dd \$	shift c and $S_3$
\$ 0 c 3 c 3	dd \$	shift d and $S_4$
\$ 0 c 3 c 3 d 4	d \$	reduce $\tau_3$ , $B \rightarrow d$
\$ 0 c 3 c 3 B 6	d \$	reduce $\tau_2$ , $B \rightarrow cB$
\$ 0 c 3 B 6	d \$	reduce $\tau_2$ , $B \rightarrow cB$
\$ 0 B 2	d \$	shift d, $S_4$
\$ 0 B 2 d 4	\$	reduce $\tau_3$ , $B \rightarrow d$
\$ 0 B 2 B S	\$	reduce $\tau_1$ , $E \rightarrow BB$
\$ 0 E I	\$	Accept
	✓	

Draw Parse tree:

(vi)



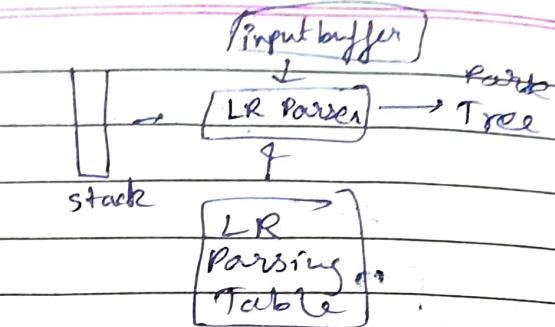
(A)

SLR(1):

→ Steps same as LR(0)



Parsing Table:



~~Reduce only in follow()~~

State	Action	Follow
$I_0$	$s_3 \ s_4$	$E \ B$
$I_1$		Accept
$I_2$	$s_3 \ s_4$	$S$
$I_3$	$s_3 \ s_4$	$G$
$I_4$	$r_3 \ r_3 \ r_3$	
$I_5$		$r_1$
$I_6$	$r_2 \ r_2 \ r_2$	

Conflict:

① Reduce-Reduce Conflict (RR)

LR(0) nota hai ✓

SLR(1) me nahi ✗

$I_4 \Rightarrow B \rightarrow d$ .

follow of  $B = \{c, d, \$\}$

$I_5 \Rightarrow E \rightarrow BB$ .

follow of  $E = \{ \$ \}$

$I_6 \Rightarrow r_2 \rightarrow B \rightarrow CB$

② Shift-Reduce Conflict (SR)

LR(0) ✓

SLR(1) ✗

LR(0) or SLR(1) or not?

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$$E \rightarrow T+E/T$$

$$T \rightarrow i$$

follow()

E { \$ }

T { +, \$ }

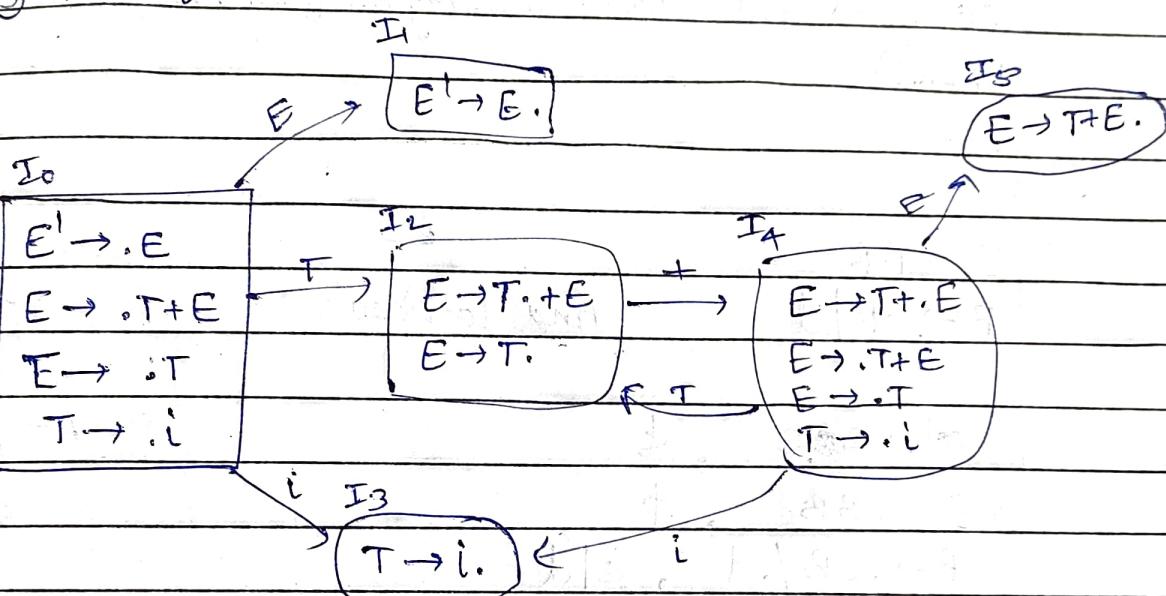
ans:

$$E' \rightarrow E$$

$$\textcircled{1} E \rightarrow T+E$$

$$\textcircled{2} E \rightarrow T$$

$$\textcircled{3} T \rightarrow i$$



State	Action			Goto	
	+	i	\$	E	T
$I_0$	$S_3$			1	2
$I_1$					
$I_2$	$S_1$ <del>(X)</del>	<del>(X)</del>		$\sigma_2$	
$I_3$	$r_3$	<del>(X)</del>		$r_3$	
$I_4$	$S_3$			5	2
$I_5$	<del>(X)</del>	<del>(X)</del>		$r_1$	

\* SLR  
me  
nikal  
jaayega

∴ LR(0) X (SR-conflict)

∴ SLR(1) ✓

CLR(1) :

LR(1) item = LR(0) item + look ahead

$LR(0) \Rightarrow$  Put reduce in full row

SLR(1)  $\Rightarrow$  Put reduce in follow of P

$CLR(1) \Rightarrow$  put reduce in only on Look Ahead.

## LALR(1)

$$Q) E \rightarrow B\bar{B}$$

$$B \rightarrow cB/d$$

find lookahead.

$\beta \rightarrow \alpha$

First

ans:  $E^I \rightarrow \text{BB.E}$ , \$

①  $E \rightarrow BB$ , \$

B → cB / .d, c | d

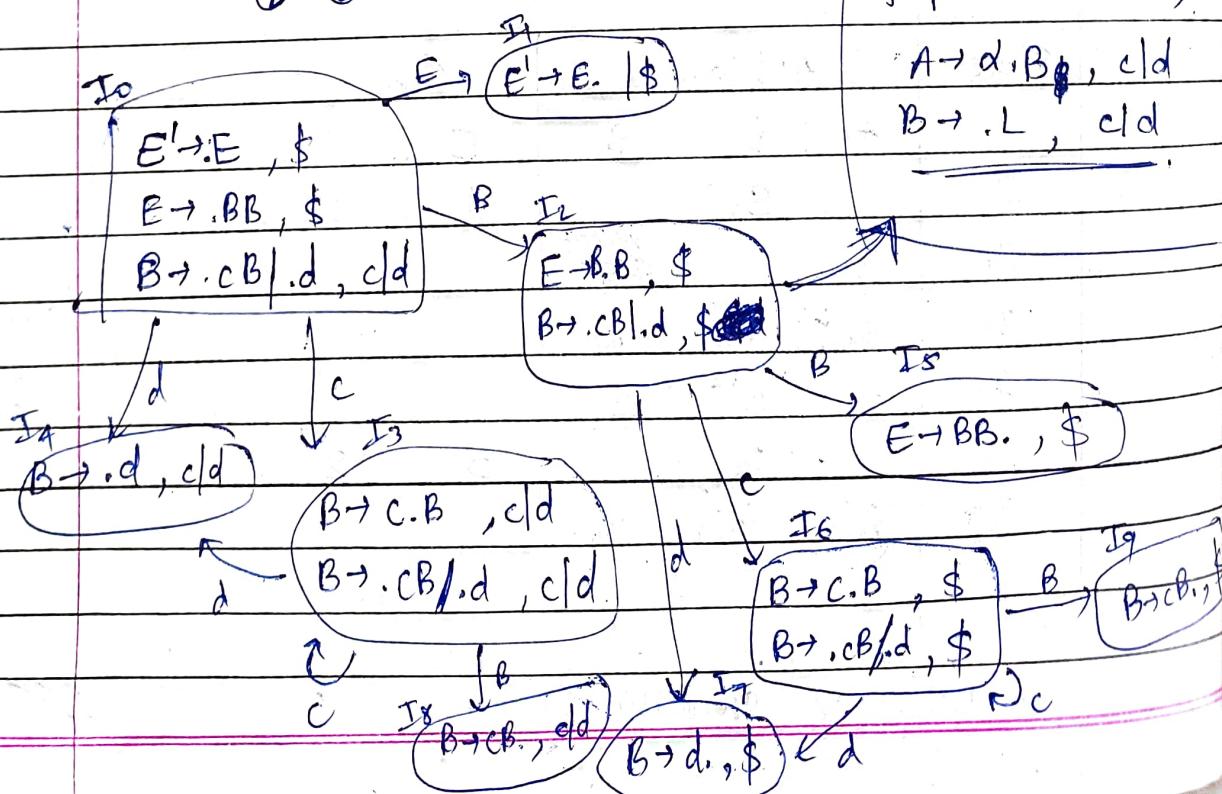
e.g.:  $A \rightarrow \alpha \cdot B$ ,  $(\beta, c)$

$B \rightarrow Q.L$ ,  $B_q$   $\uparrow$  First(8)

if  $\beta$  was not there,

$A \rightarrow d, B \not\models, c \vdash d$

B → L, cl d



state	Action			Goto
	c	d	\$	E · B
I <sub>0</sub>	S <sub>3</sub>	S <sub>4</sub>		1 2
I <sub>1</sub>			Accept	
I <sub>2</sub>	S <sub>6</sub>	S <sub>7</sub>		5
I <sub>3</sub>	S <sub>3</sub>	S <sub>4</sub>		8
I <sub>4</sub>	r <sub>3</sub>	r <sub>3</sub>		
I <sub>5</sub>			r <sub>1,2</sub>	
I <sub>6</sub>	S <sub>6</sub>	S <sub>7</sub>		9
I <sub>7</sub>			r <sub>3</sub>	
I <sub>8</sub>	r <sub>2</sub>	r <sub>2</sub>		
I <sub>9</sub>			r <sub>2</sub>	

CLR(1) ↗

Convert to LALR(1) →

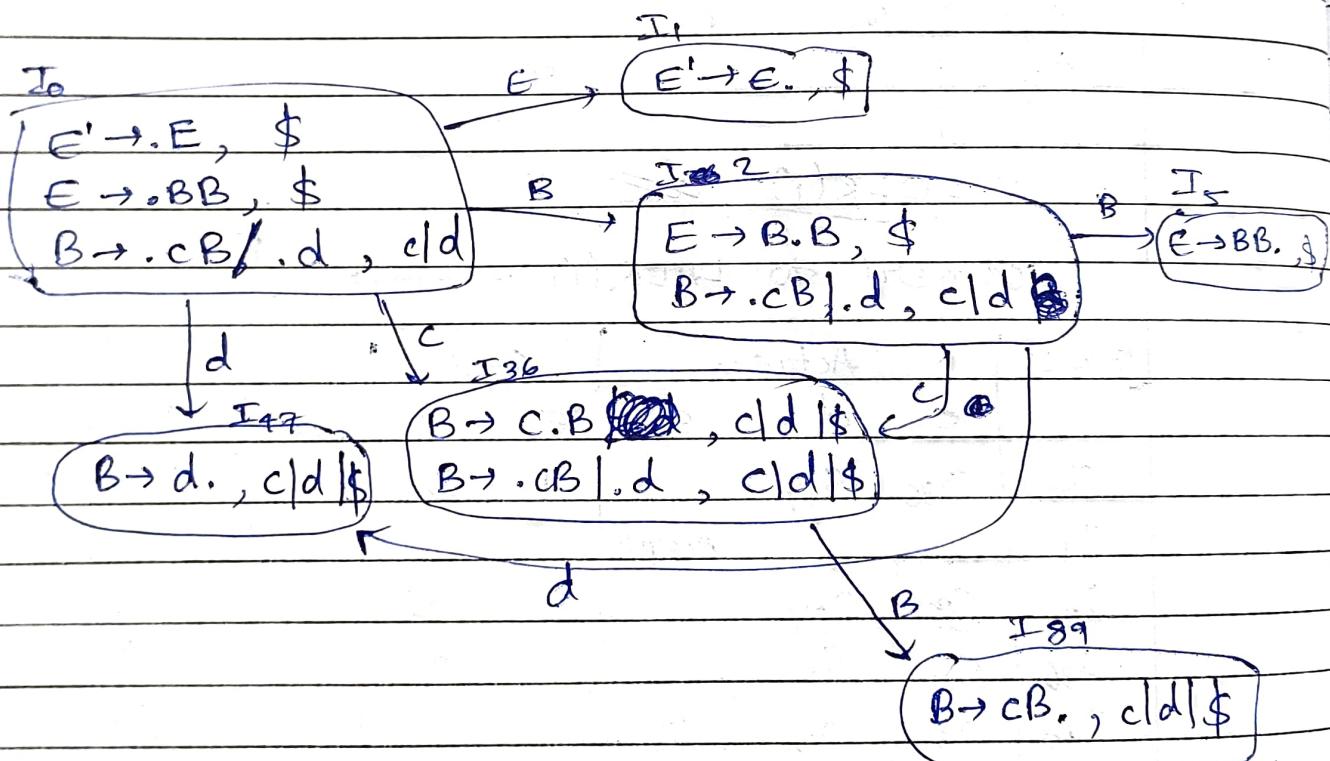
Find  
Production same  
& LookAhead diff.

state	Action			Goto
	c	d	\$	E · B
I <sub>0</sub>	S <sub>36</sub>	S <sub>47</sub>		1 2
I <sub>1</sub>			Accept	
I <sub>2</sub>	S <sub>6</sub>	S <sub>7</sub>		5
I <sub>36</sub>	S <sub>36</sub>	S <sub>17</sub>		89
I <sub>47</sub>	r <sub>3</sub>	r <sub>3</sub>	r <sub>3</sub>	
I <sub>5</sub>			r <sub>1</sub>	
I <sub>36</sub>	S <sub>36</sub>	S <sub>47</sub>		89
I <sub>47</sub>			r <sub>3</sub>	
I <sub>89</sub>	r <sub>2</sub>	r <sub>2</sub>	r <sub>2</sub>	
I <sub>9</sub>			r <sub>2</sub>	

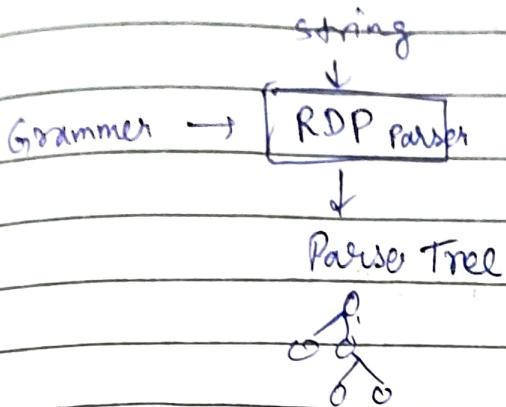
↓ convert into  
I<sub>36</sub>, I<sub>47</sub>, I<sub>89</sub>

Rewrite →

state	Action			Goto
	c	d	\$	$E \rightarrow B$
I <sub>0</sub>	s <sub>36</sub>	s <sub>17</sub>		1 2
I <sub>1</sub>				Accept
I <sub>2</sub>	s <sub>36</sub>	s <sub>17</sub>		5
I <sub>36</sub>	s <sub>36</sub>	s <sub>17</sub>		89
I <sub>47</sub>	r <sub>3</sub>	r <sub>3</sub>	r <sub>3</sub>	
I <sub>5</sub>			r <sub>1</sub>	
I <sub>89</sub>	r <sub>2</sub>	r <sub>2</sub>	r <sub>2</sub>	



## Recursive Descent Parser:



- Top-Down Parsing.
- Backtracking

### (a) Example Backtracking

$$S \rightarrow cAd$$

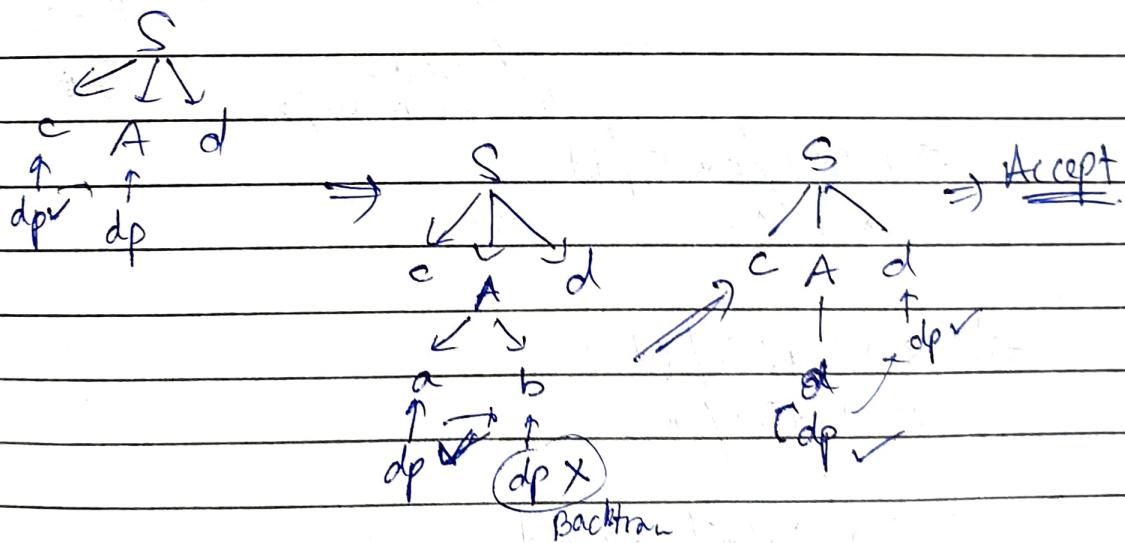
$$A \rightarrow ab \mid a$$

and input string  $w = cad$

↑ ↑ ↑  
i/p i/p i/p

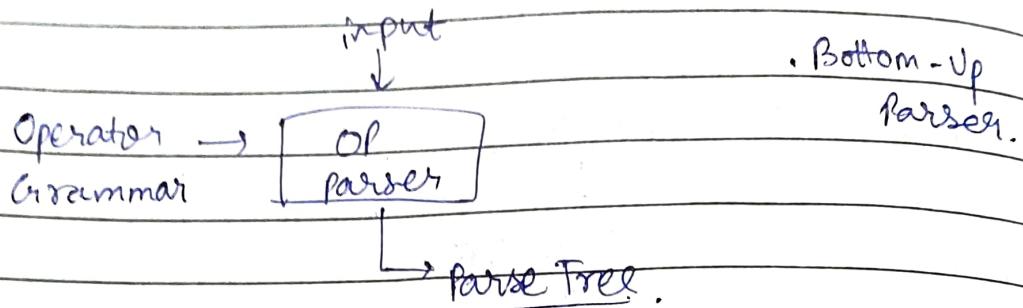
i/p = input

dp = descent  
pointer



(\*)

## Operator - Precedence: Parser



Bottom-Up  
Parser.

Operator Grammar: (1) No Epsilon in right side  
(2) No adjacent variable

Example:

$$\Rightarrow E \rightarrow E+E / E-E / id$$

$$\Rightarrow E \rightarrow EA E / id$$

} Not operator grammar

$$A \rightarrow +/*$$

} grammar

converting  
by  $A \rightarrow +/*$

$$E \rightarrow B+E / E * E / id$$

$$A \rightarrow +/*$$

✓

Example:

$$AB \quad X$$

$$A+B \quad \checkmark$$

$$A*B \quad \checkmark$$

$$A/C \quad \checkmark$$

$$A-B \quad \checkmark$$

$$B+A \quad \checkmark$$

$$\Rightarrow S \rightarrow S \alpha S / id$$

$$A \rightarrow \alpha S \alpha / \alpha$$

$$\therefore S \rightarrow S \alpha S \alpha / S \alpha S / id$$

$$A \rightarrow \alpha S \alpha / \alpha$$

- ① Check OPG or Not
- ② Operator Precedence Relation Table
- ③ Parse the given string
- ④ Generate Parse Tree.

eg:  $T \rightarrow T+T / T.*T / id$

Basics

$id, a, b, c \Rightarrow High$

$\$ \Rightarrow Low$

$+ > +$  (left side)

$* > *$

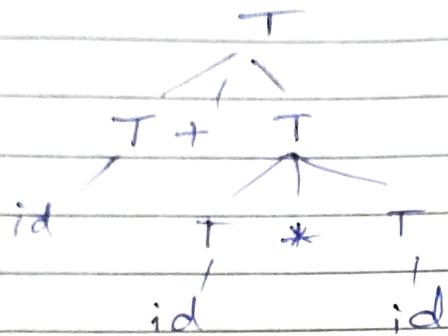
$id \neq id$

$\$ A \$$

	+	*	id	\$
+	>	<	<	>
*	>	>	<	>
id	>	>	$\neq$	>
\$	<	<	$\neq$	A

Stack	Relation	Input	Comment
\$	<	<u>id+id*id \$</u>	shift id
\$id	>	<u>+id*id \$</u>	reduce $T \rightarrow id$
\$T	<	<u>+id*id \$</u>	shift +
\$T+	<	<u>id*id \$</u>	shift id
\$T+id	>	<u>* id \$</u>	reduce $T \rightarrow id$
\$T+T	<	<u>* id \$</u>	shift <del>TOP*</del> *
\$T+T*	<	<u>id \$</u>	shift id
\$T+T*id	>	<u>\$</u>	reduce $T \rightarrow id$
\$T+T*T	>	<u>\$</u>	reduce $T \rightarrow T*T$
\$T+T	>	<u>\$</u>	reduce $T \rightarrow T+T$
\$T	A	<u>\$</u>	Accept

## Generate Parse Tree:



	a	b	c	d	e
f	>	<	<	<	<
g	>	<	<	<	<
a	>	>			
b	>	>			
c	>	>	-	-	>
d	>	>	-	-	>
\$	<	<	<	<	< A

$$\begin{aligned} \textcircled{2}: \quad E &\rightarrow E + T / T \\ T &\rightarrow T * V / V \\ V &\rightarrow a / b / c / d \end{aligned}$$

·	+	*	id	\$	
+	>	<	<	>	X
*	>	>	<	>	
id	>	>	-	>	
\$	<	<	<	A	

"a+b\*c\*d"

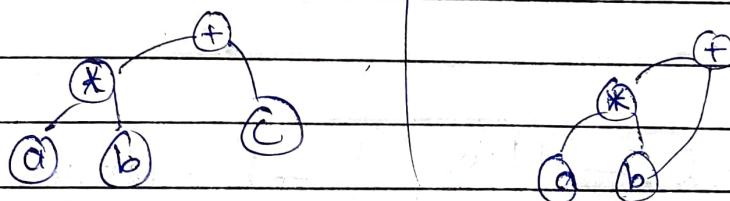
Stack	Rel.	String Input	Comment
\$	<	<u>a+b*c*d\$</u>	shift a
\$a	>	+b*c*d \$	reduce V → a
\$v	<	+b*c*d \$	shift +
\$v+	<	b*c*d \$	shift b
\$v+b	>	*c*d \$	reduce V → b
\$v+v	<	*c*d \$	shift *
\$v+v*	<	c*d \$	shift c
\$v+v*c	>	* d \$	reduce V → c
\$v+v+v	>	* d \$	reduce T → V
\$v+v*T	>	* d \$	reduce E → T
\$v+v*E	>	* d \$	??

$\therefore$  NO Production found for reduction operation

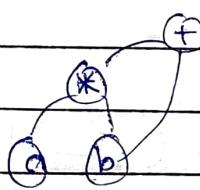
Since, parsing process failed to complete, the given input cannot be parsed by the given grammar using OPP method.

### DAG (Direct Acyclic Graph)

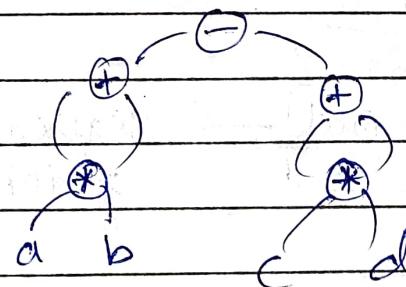
eg:  $a * b + c$



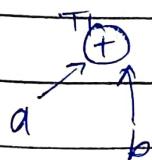
$a * b + b$



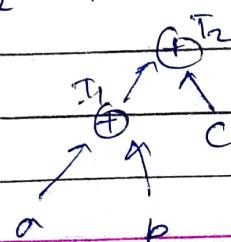
eg:  $((a * b) + (a * b)) - ((c * d) + (c * d))$



(Q)  $T_1 = a + b$



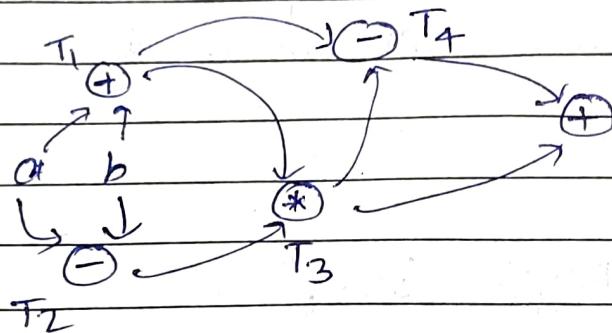
$T_2 = T_1 + c$



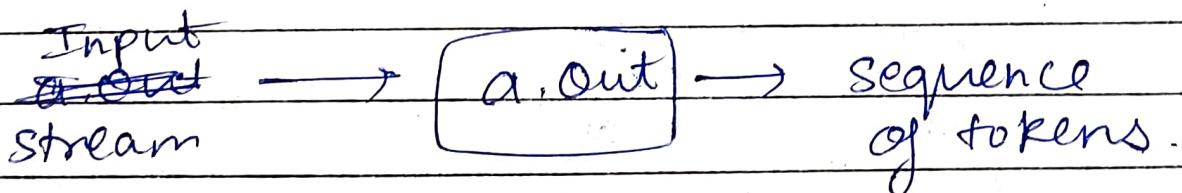
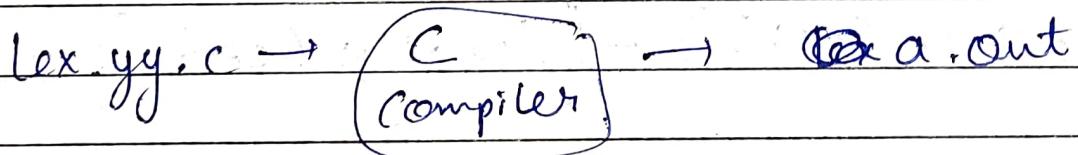
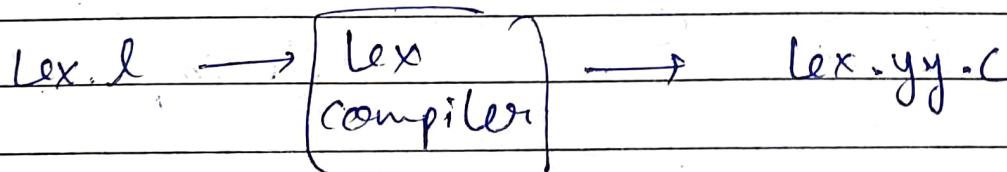
$$\begin{array}{l} \textcircled{1} \\ = \\ T_1 = a + b \\ T_2 = a - b \end{array}$$

$$\begin{array}{l} T_3 = T_1 * T_2 \\ T_4 = T_1 - T_3 \end{array}$$

$$T_5 = T_4 + T_3$$



Lex :





YACC :

Generates LALR Parser.

(Yacc)

parser.y



Yacc  
compiler

→ parser.tab.c

parser.tab.c



C  
compiler

→ a.out

~~Input~~  
Stream

a.out

→ (sequence of tokens)  
output

Definition  
of %

Rules

%

Supplementary code