

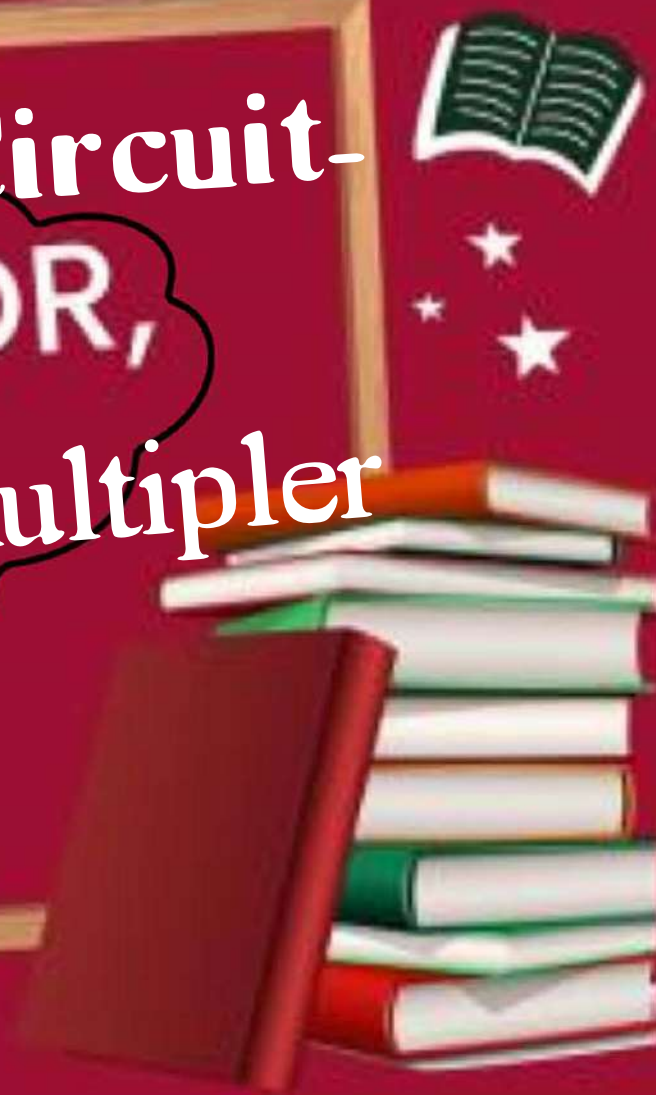
EC/EE/CS & IT/IN

Digital Electronics

**Combinational Circuit-
COMPARATOR,
HA,FA,Multiplexer**

LECTURE NO. 5

Chandan Jha Sir (CJ Sir)



मंजिल यूँ ही नहीं
मिलती राही को,
जूनून सा दिल में
जगाना पड़ता है,
पूछा चिड़िया से
कि घोसला कैसे बनता है
वो बोली कि तिनका-तिनका
उठाना पड़ता है.

ABOUT ME



- **Cleared Gate Multiple times with double Digit Rank (AIR 23, AIR 26)**
- **Qualified ISRO Exam**
- **Mentored More then 1 Lakhs+ Students (Offline & Online)**
- **More then 250+ Motivational Seminar in various Engineering College including NITs & Some of IITs**



Chandan Jha

Logic GATE

└→ INVERTER

$$f = \frac{1}{2N \times \tau_{pd}}$$

AND
OR

$$Y = A \cdot B$$

$$Y = A + B$$

$$\underline{\underline{PPL}} \rightarrow 1$$

$$ECL \rightarrow 0$$

Sunday

Monday

NAND

$$Y = \overline{A \cdot B}$$

NOR

?

$$Y = \overline{A + B}$$

POS

SOP

→ AND-OR

NAND-NAND

AOI

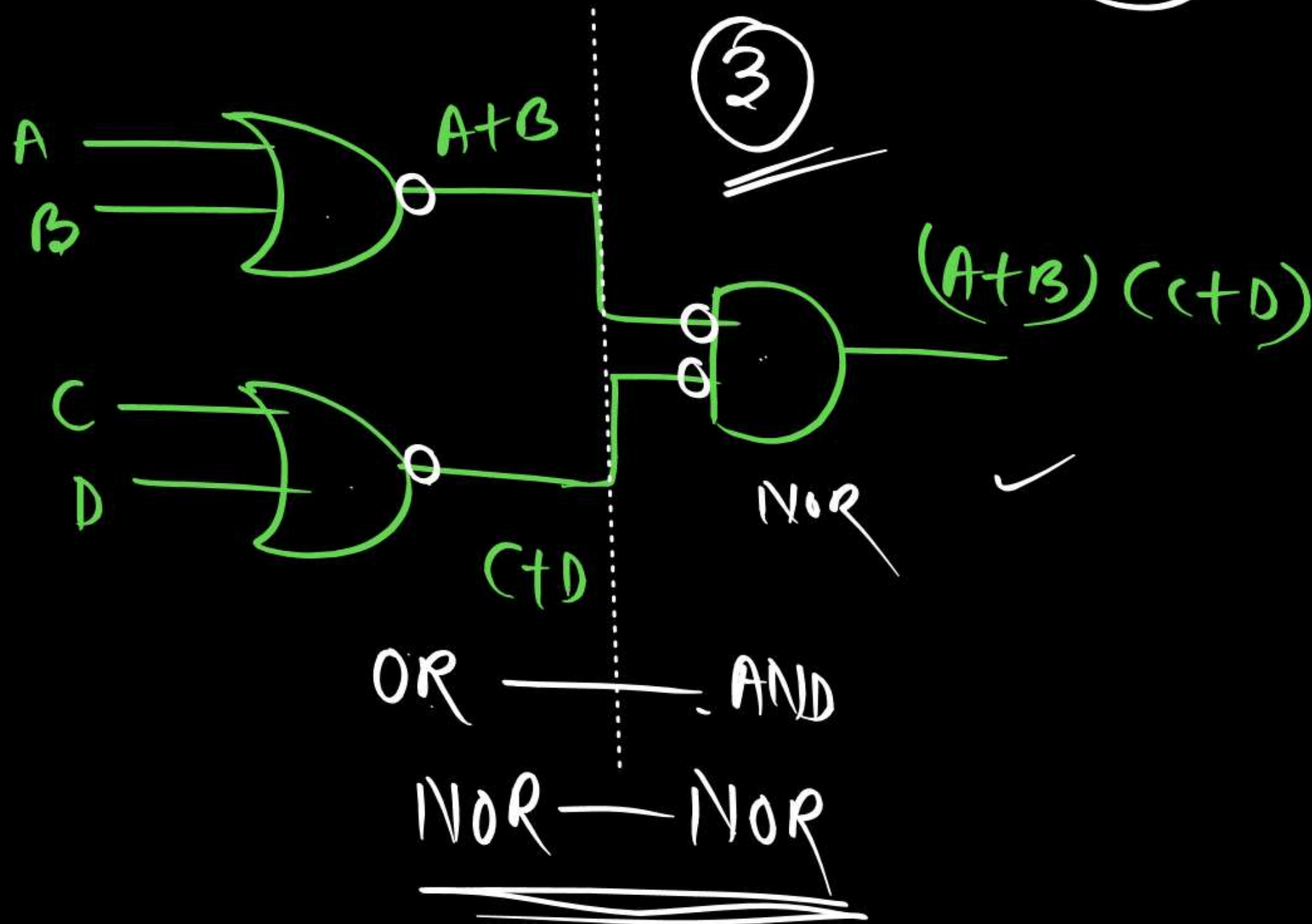
→ OR-AND

NOR-NOR

$(AB + CD) \rightarrow (3)$

$$f = (A+B)(C+D) \longrightarrow \text{POS}$$

NOR=?



XOR

$$A \oplus A = 0$$

$$A \oplus 0 = A$$

$$A \oplus \bar{A} = 1$$

$$A \oplus 1 = \bar{A}$$

$$A \oplus B \oplus C = \underline{\sum m(1, 2, 4, 7)}$$

X-NOR

$$A \odot A = 1$$

$$A \odot 1 = A$$

$$A \odot \bar{A} = 0$$

$$A \odot 0 = \bar{A}$$

1947

BJT


$$(A \oplus B) \oplus C = A \oplus B \oplus C$$

Associative

Boolean algebra. //

$$\Rightarrow A + BC = (A + B) \cdot (A + C)$$

$$\Rightarrow AB + \bar{A}C + BC = AB + \bar{A}C$$

$$\Rightarrow (A + B)(\bar{A} + C) = AC + \bar{A}B$$

$$\Rightarrow \overline{ABC} = \bar{A} + \bar{B} + \bar{C}$$

$$\overline{A + B + C} = \bar{A} \cdot \bar{B} \cdot \bar{C}$$

SOP

POS

K-MAP.

└→ Gray code.

└→ cyclic

Reflecting code

unity hamming distance code.

CT BABA RULE

SOP, dont

POS

I, PI, EPI

| A \ BC | | | | |
|--------|----|----|----|----|
| | 00 | 01 | 11 | 10 |
| 0 | 1 | 1 | 1 | |
| 1 | | | 1 | 1 |

| A \ BC | | | | |
|--------|----|----|----|----|
| | 00 | 01 | 11 | 10 |
| 0 | 1 | 1 | 1 | |
| 1 | | | 1 | 1 |

$$\{\bar{A}\bar{B}, AB, \bar{A}C, BC\}$$

$$\begin{aligned} \text{EPI} \\ &= \bar{A}\bar{B} + AB + \bar{A}C \end{aligned}$$

SPI

$$I = 5$$

$$PI = 4$$

$$EPI = 2$$

SPI

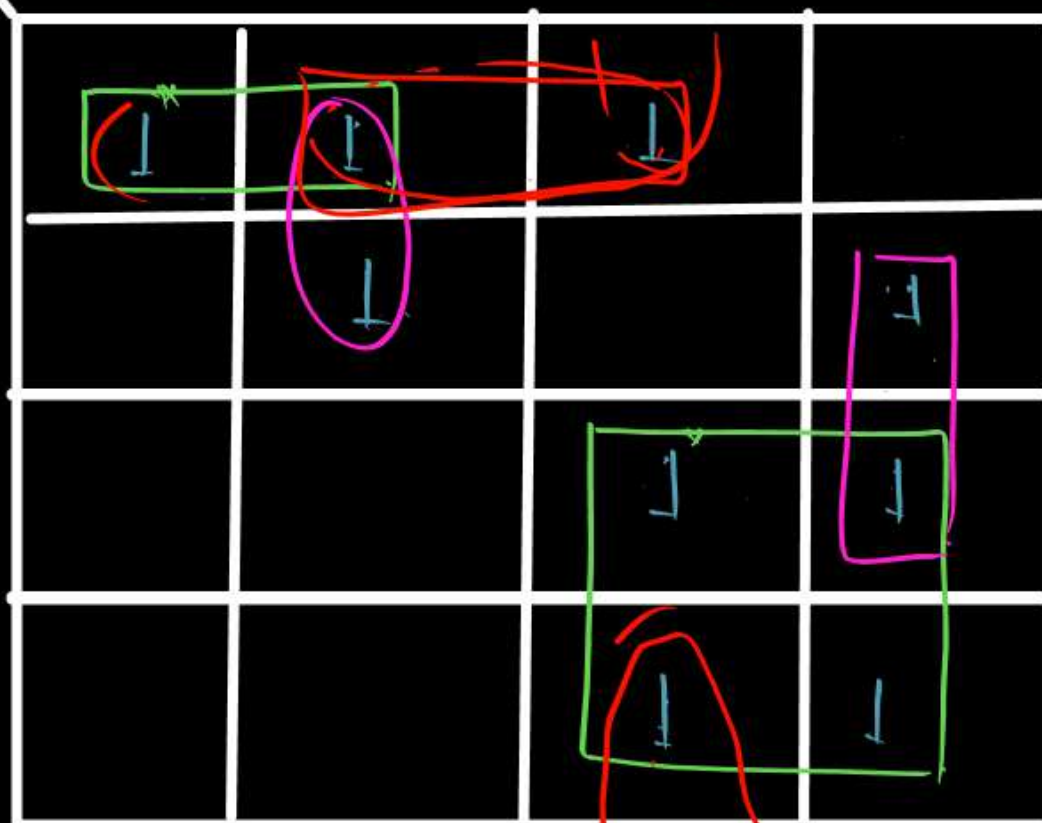
RPI

$$= \bar{A}\bar{B} + AB + BC$$

RPI

SPI \rightarrow Selective prime Implicant

RPI \rightarrow Reduced prime Implicant



$$PI = 6$$

$$I = 9$$

$$EPI = 4$$

$$SPI = 1$$

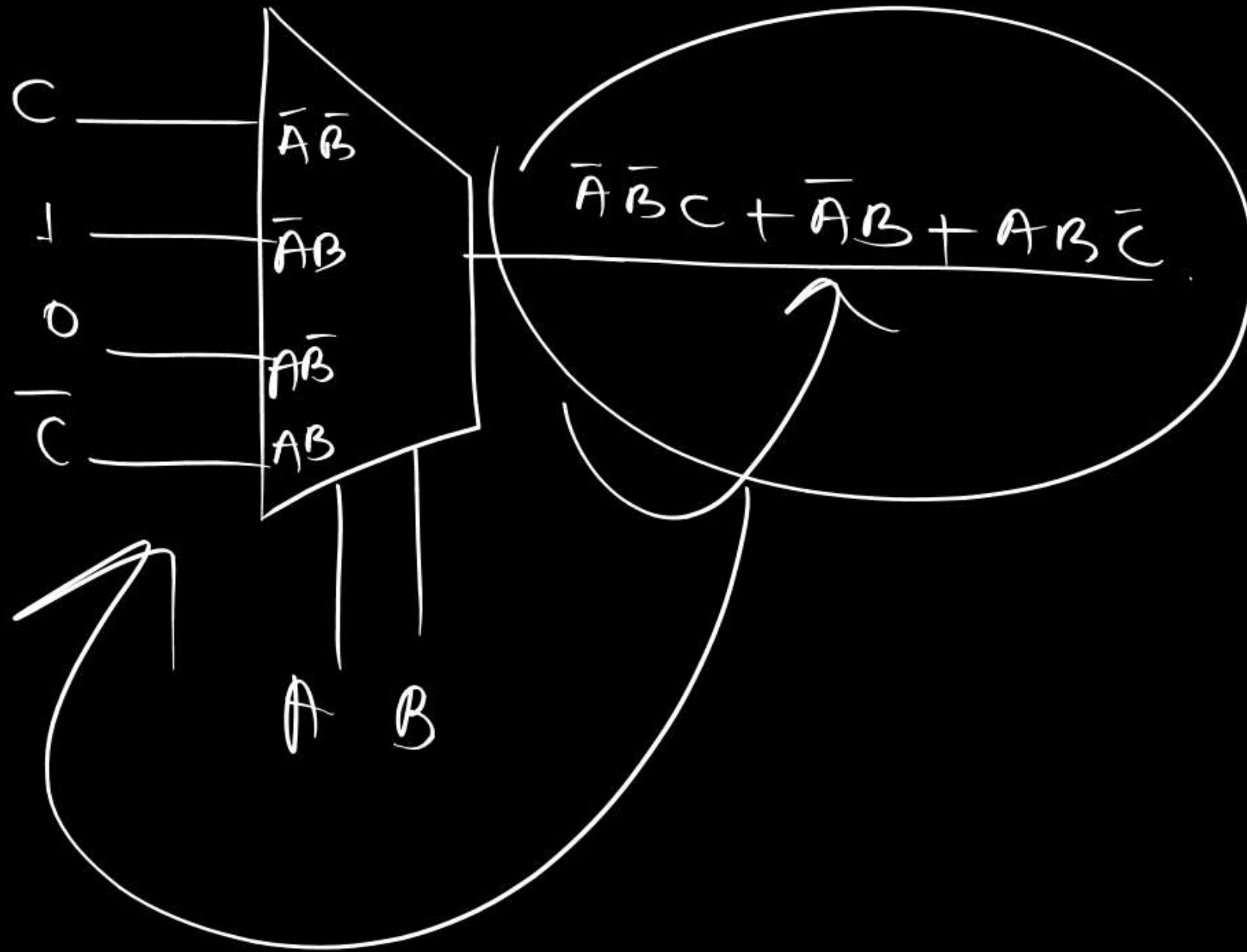
$$RPI = 1$$

Combinational circuit

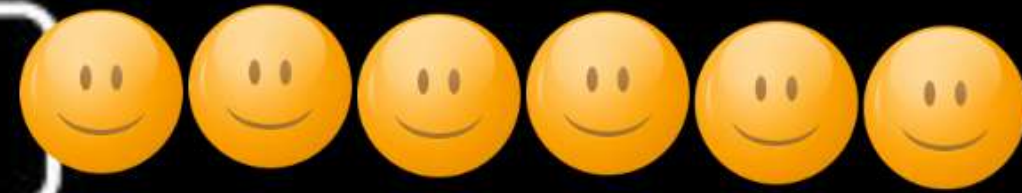
MUX \rightarrow universal logic

2x1 ✓
4x1 ✓
8x1

AND-OR

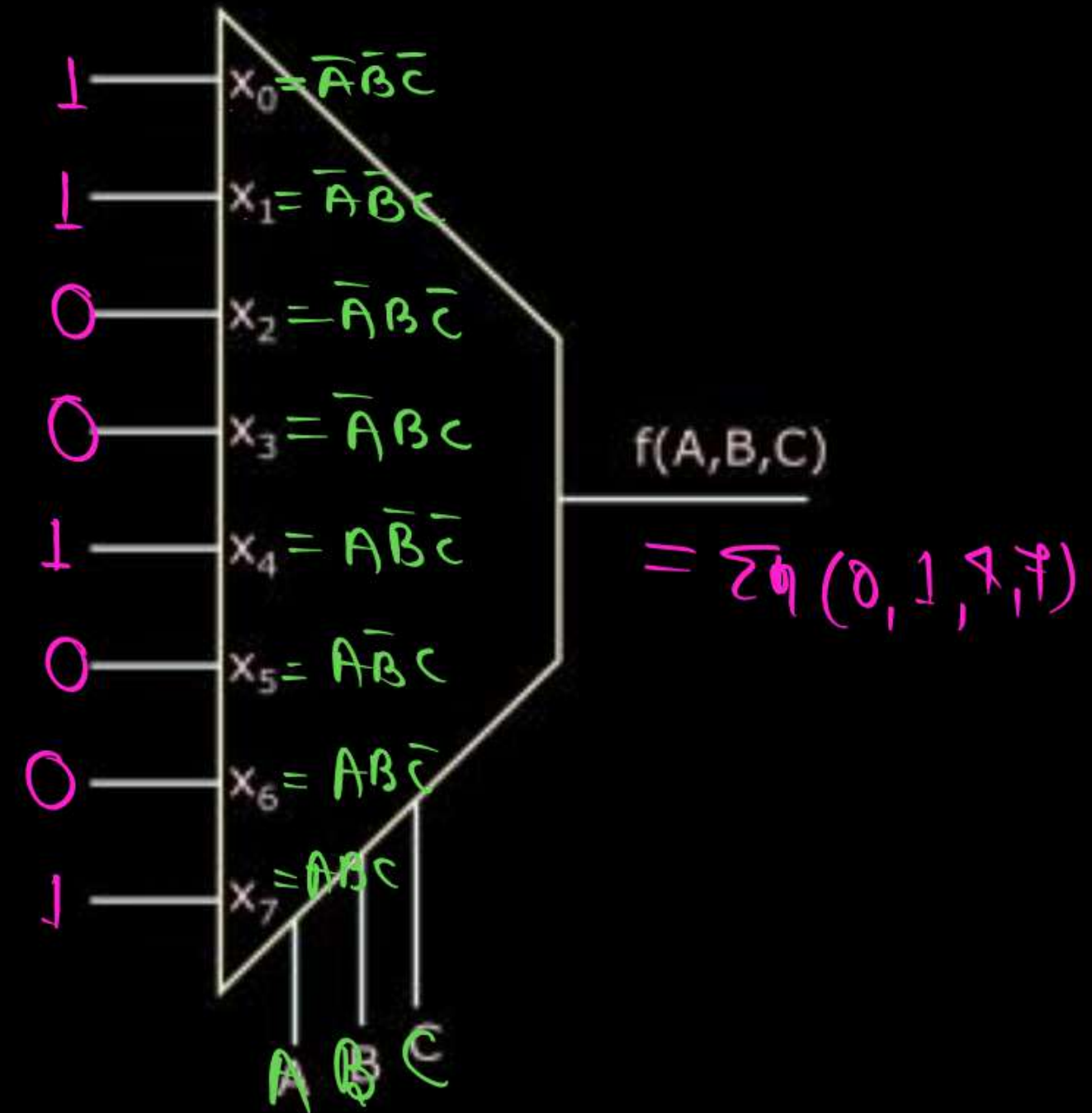


Type -5. Implementation of function



Ex. Implement the function given below by using 8x1 Mux

$$f(A, B, C) = \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + A\bar{B}\bar{C} + ABC$$
$$= \sum m(0, 1, 4, 7)$$



Type -5. Implementation of function

Ex. Implement the function given below

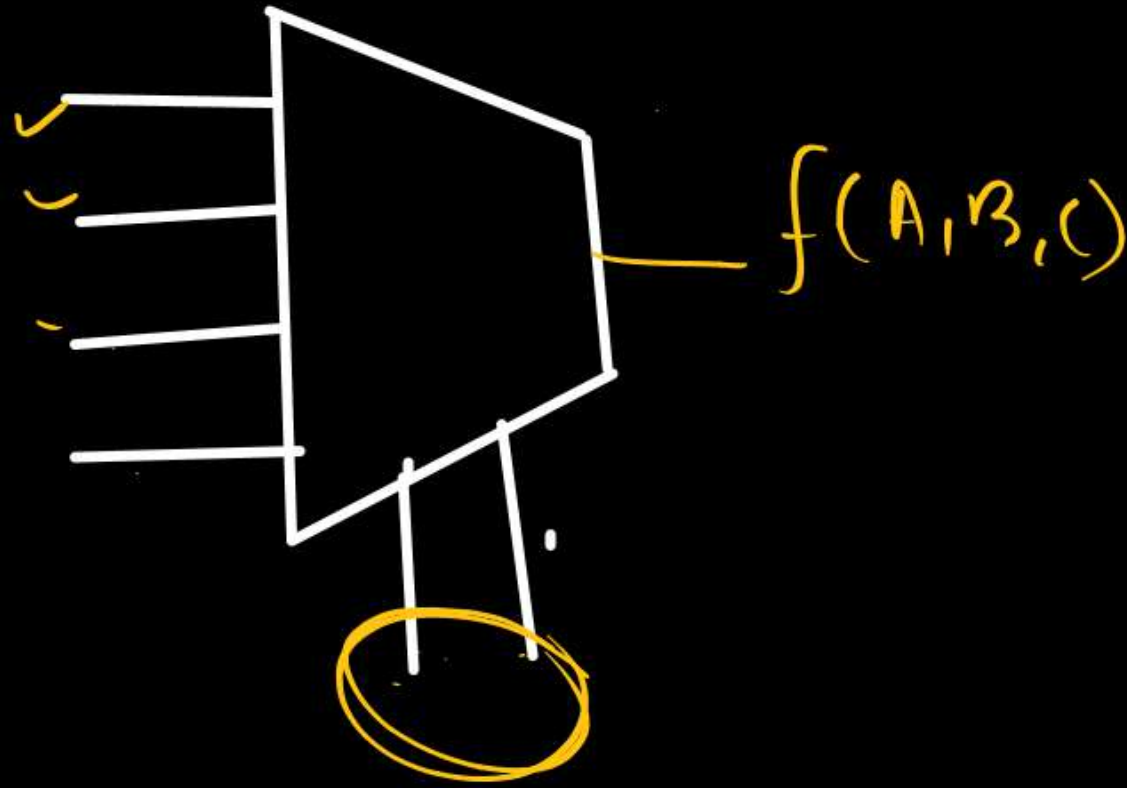
by using **4x1 Mux**

$$f(A, B, C) = \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + A\bar{B}\bar{C} + ABC$$

$$= \sum m(0, 1, 4, 7)$$

no. of select line = 2.

1. AB as a select line
2. BC as a select line
3. AC as a select line



Type -5. Implementation of function

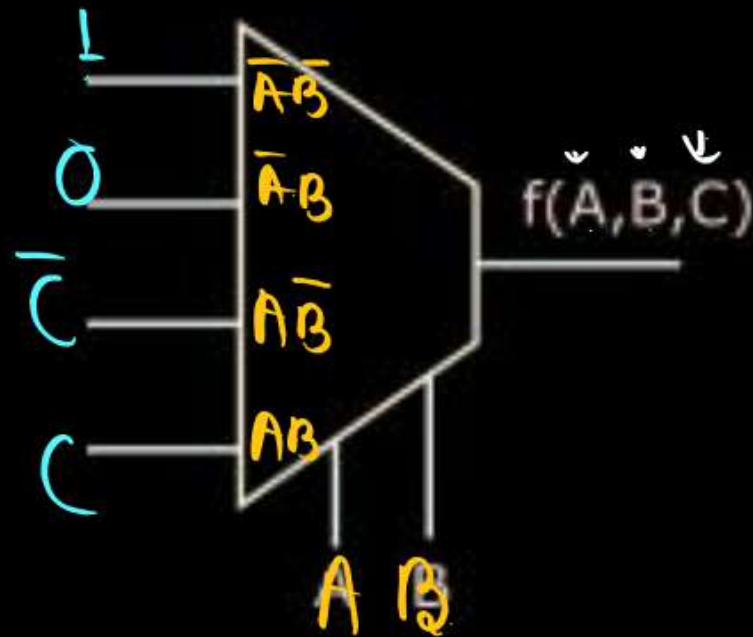
Ex. Implement the function given below

by using 4x1 Mux

$$f(A, B, C) = \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + A\bar{B}\bar{C} + ABC$$

$$= \sum m(0, 1, 4, 7)$$

1. AB as a select line



| | $\bar{A}\bar{B}$ | $\bar{A}B$ | $A\bar{B}$ | AB |
|-----------|------------------------------|------------------------|------------------------|------------------|
| \bar{C} | $\bar{A}\bar{B}\bar{C}$ 0 | $\bar{A}B\bar{C}$ 2 | $A\bar{B}\bar{C}$ 4 | $AB\bar{C}$ 6 |
| C | $\bar{A}B C$ 1 | $A\bar{B} C$ 3 | $A B \bar{C}$ 5 | $A B C$ 7 |
| | 1 | 0 | \bar{C} | C |

Type -5. Implementation of function

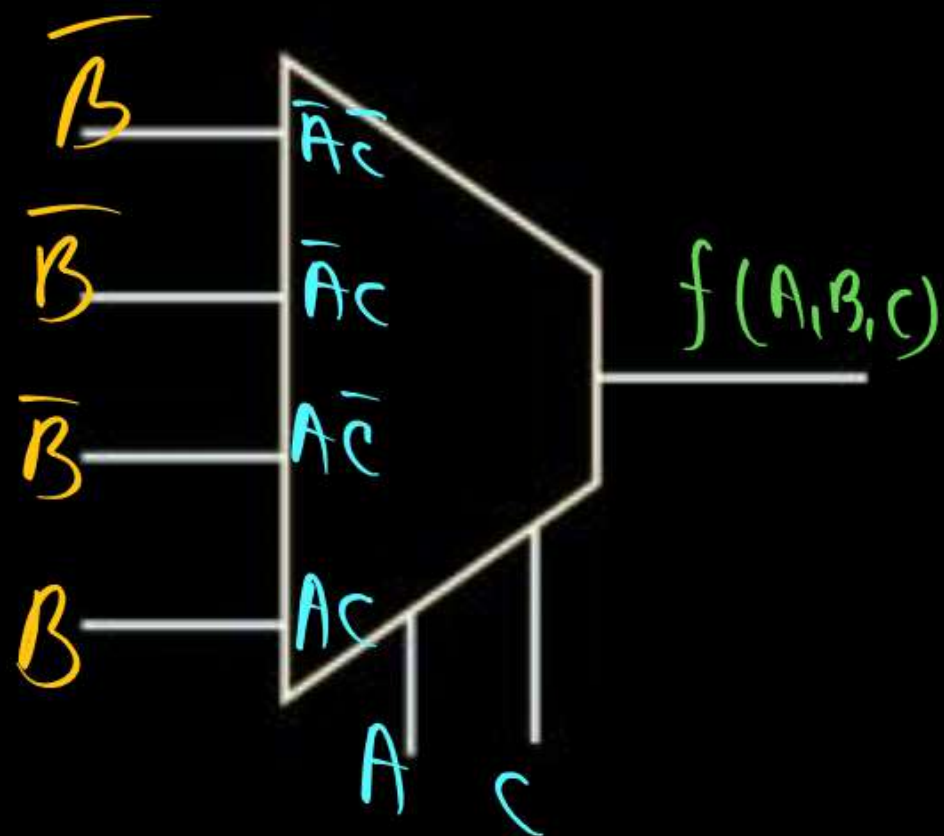
Ex. Implement the function given below

by using 4x1 Mux

$$f(A, B, C) = \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + A\bar{B}\bar{C} + ABC$$

$$= \sum m(0, 1, 4, 7)$$

2. AC as a select line



| | $\bar{A}\bar{C}$ | $\bar{A}C$ | $A\bar{C}$ | AC |
|-----------|---------------------------|---------------------|---------------------|---------------|
| \bar{B} | $\bar{A}\bar{B}\bar{C}$ 0 | $\bar{A}\bar{B}C$ 1 | $A\bar{B}\bar{C}$ 4 | $A\bar{B}C$ 5 |
| B | $\bar{A}B\bar{C}$ 2 | $\bar{A}BC$ 3 | $AB\bar{C}$ 6 | ABC 7 |
| | \bar{B} | \bar{B} | \bar{B} | B |

HW

$$f(A, B, C) = \sum m(0, 1, 4, 7)$$

Q Bc as a select line.

→ Comment Box

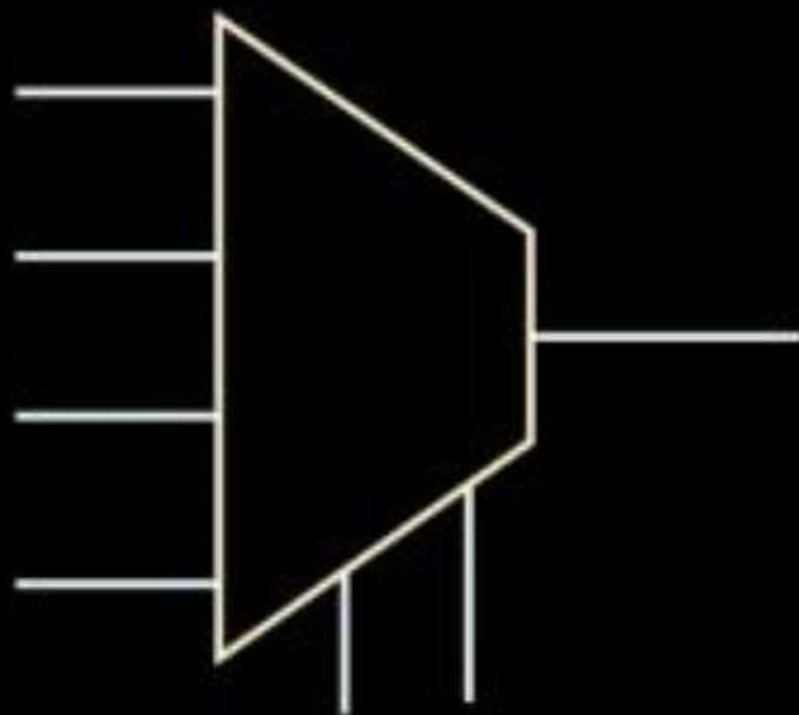
Type -5. Implementation of function

Ex. Implement the function given below

by using 4x1 Mux

$$f(A, B, C) = \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + A\bar{B}\bar{C} + ABC$$

2. BC as a select line



Type -5. Implementation of function

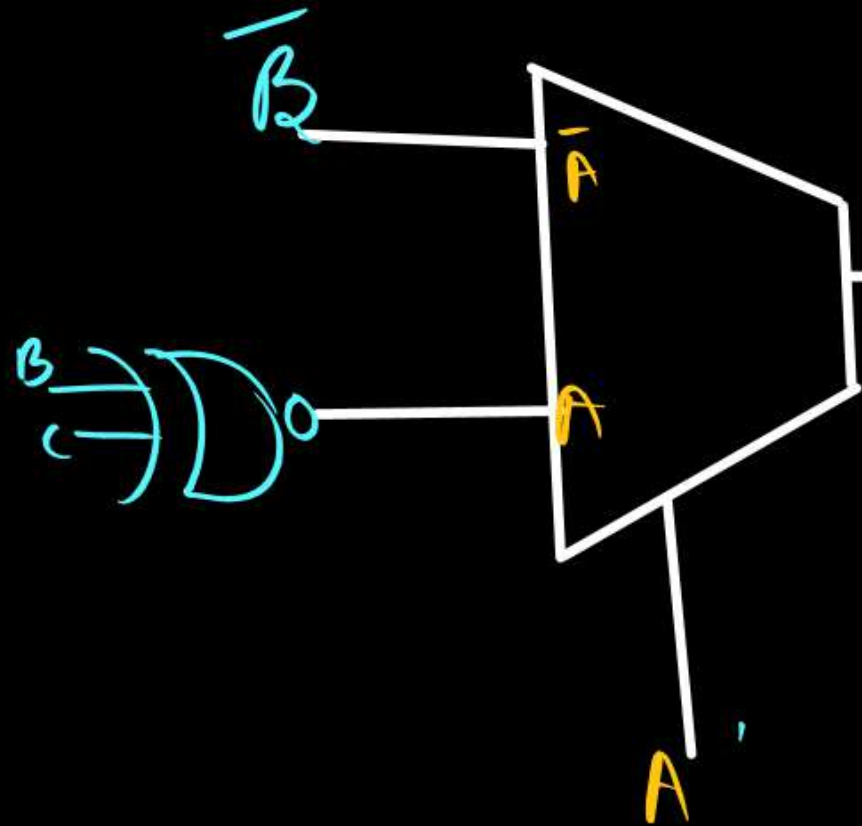
Ex. Implement the function given below

by using 2x1 Mux

$$f(A, B, C) = \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + A\bar{B}\bar{C} + ABC$$

Q $f(A, B, C) = \sum m(0, 1, 4, 7) = \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + A\bar{B}\bar{C} + ABC$

Implement by using 2X1 MUX?



$f(A, B, C)$

$$= \bar{A}\bar{B} + A(\bar{B}\bar{C} + BC)$$

$$= \bar{A}\bar{B}(\bar{C} + C) = \bar{A}\bar{B}\bar{C} + A\bar{B}C$$

$$= \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + A\bar{B}\bar{C} + ABC$$

$$= \sum m(0, 1, 4, 7)$$

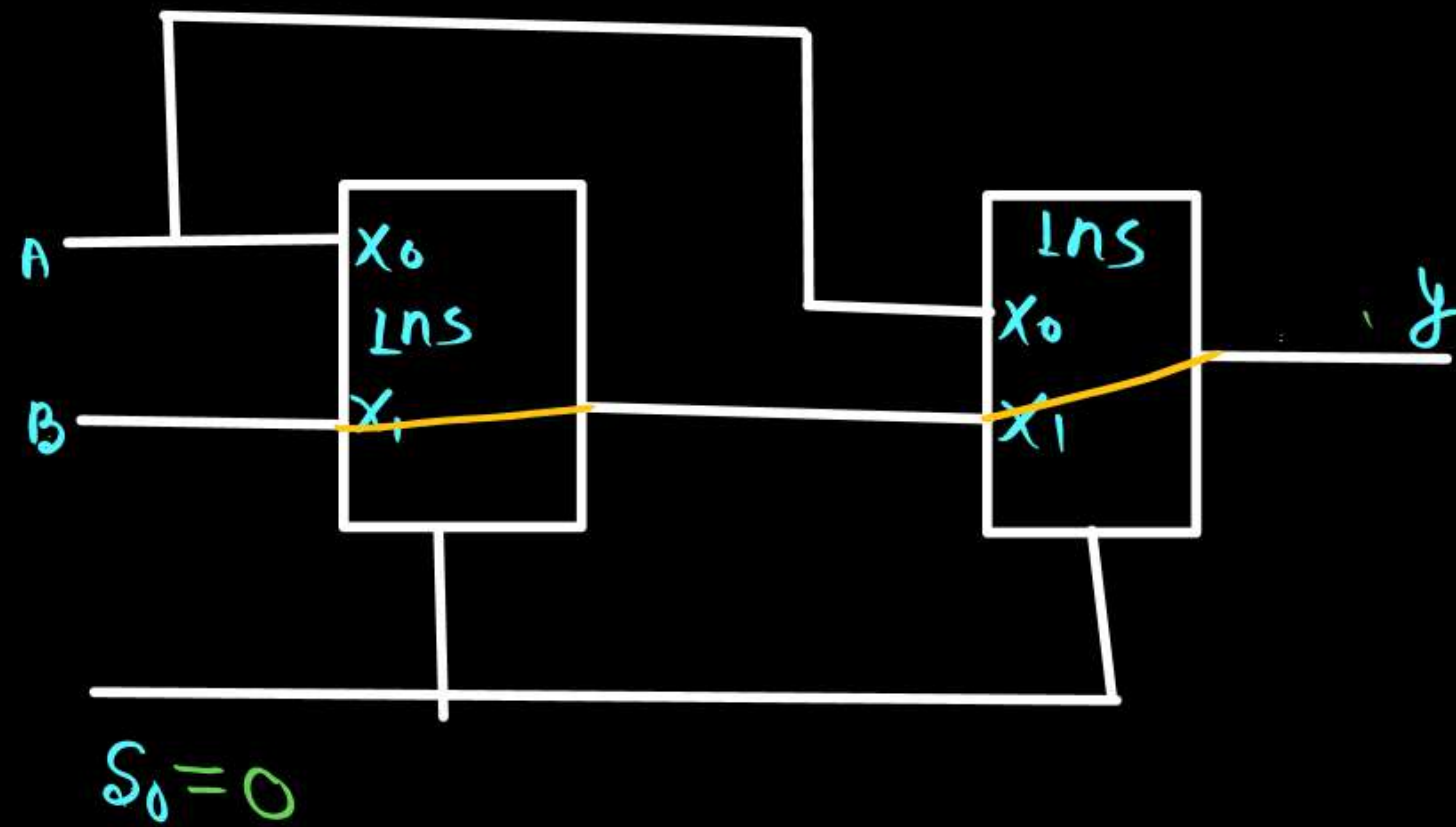
| | \bar{A} | A |
|------------------|--|--|
| $\bar{B}\bar{C}$ | $\bar{A}\bar{B}\bar{C}$ 0 | $A\bar{B}\bar{C}$ 4 |
| $\bar{B}C$ | $\bar{A}\bar{B}C$ 1 | $A\bar{B}C$ 5 |
| $B\bar{C}$ | $\bar{A}B\bar{C}$ 2 | $AB\bar{C}$ 6 |
| BC | $\bar{A}BC$ 3 | ABC 7 |
| | $\bar{B}\bar{C} + \bar{B}C$ $\bar{B}(\bar{C} + C)$ \bar{B} | $\bar{B}\bar{C} + BC$ $B \oplus B$ B |

Ex. ^{Hw} $f(\underline{A}, \underline{C}, \underline{B}, \underline{D}) = \sum m(0, 1, 3, 5, 7, 9, 12, 15)$

1. ABD as select line

2. ACD as a select line.





Minimum Delay = 1ns.

Maximum Delay
(Delay) = 2ns

Case (1) $S_0=0$

Delay = 1ns.

Case (2) $S_0=1$

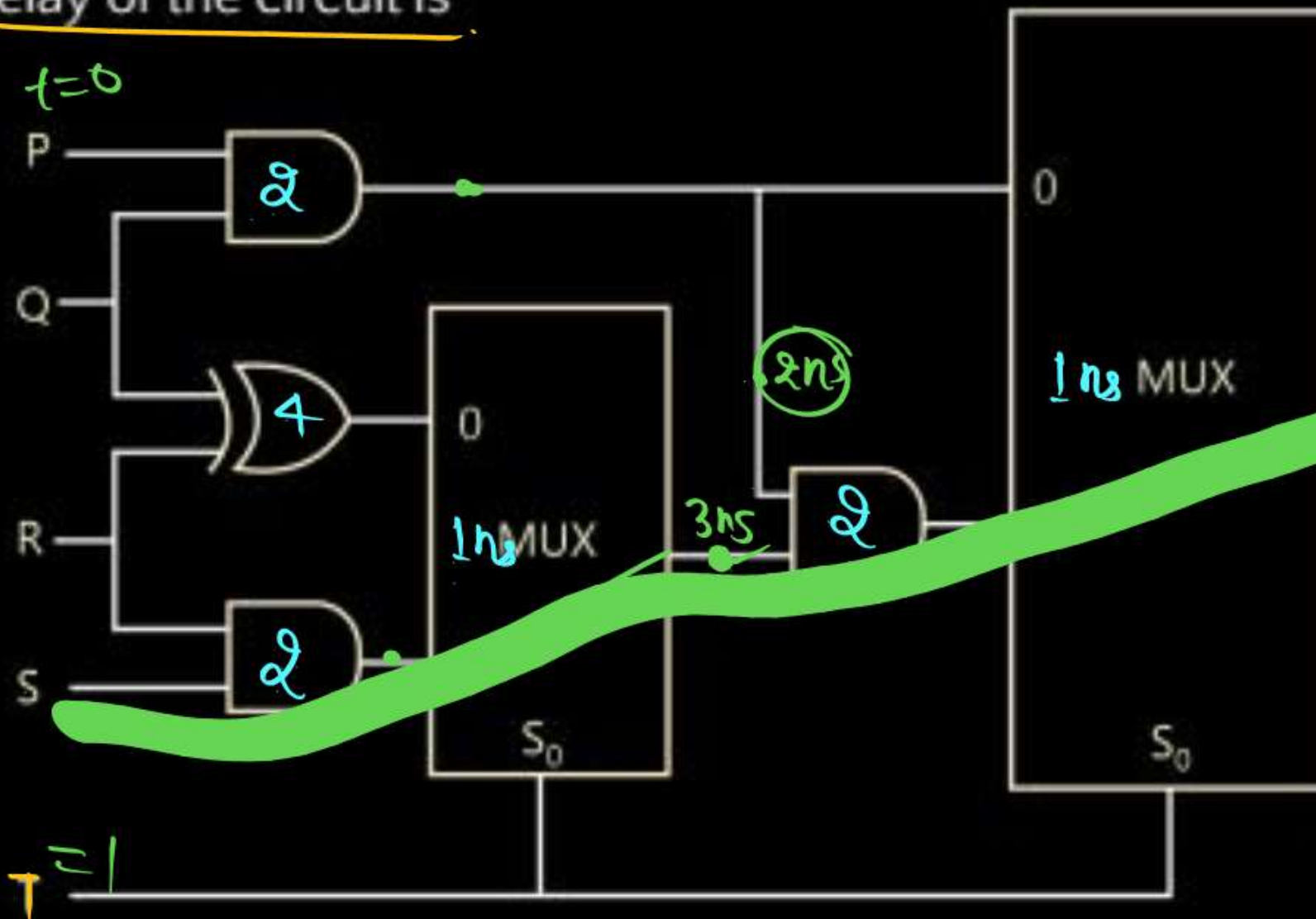
Delay = 2ns

Type -6. Delay in MUX



Q. The propagation delays of the XOR gate, AND gate and multiplexer (MUX) in the circuit shown in the figure are 4 ns, 2 ns and 1 ns, respectively.

If all the inputs P, Q, R, S and T are applied simultaneously and held constant, the maximum propagation delay of the circuit is



Case (1) $T=0$

$$\text{AND} + \text{MUX}(2) \\ 2 + 1 = \underline{\underline{3 \text{ ns}}}$$

Case (2) $T=1$

$$\text{AND} + \text{MUX}(1) + \text{AND} + \text{MUX}(2) \\ 2 + 1 + 2 + 1 = \underline{\underline{6 \text{ ns}}}$$

6 ns

DESIGNING OF COMBINATIONAL CIRCUIT

- ✓ Step 1. Find the number of inputs and outputs.
- ✓ Step 2. Write the truth table.
- ✓ Step 3. Write the logical expression.
- ✓ Step 4. Minimize the logical expression.
- ✓ Step 5. Hardware implementation.

Magnitude.

Single digit 75-80 EC (20)
Comparator

World

CHATE

ISRO

~~SAI~~

{ K-MAP
Network }

ONE BIT MAGNITUDE COMPARATOR

Step-1



Step-2. Truth table

| | | (A > B) | (A < B) | (A = B) |
|---|---|---------|---------|---------|
| A | B | X | Y | Z |
| 0 | 0 | 0 | 0 | 1 |
| 0 | 1 | 0 | 1 | 0 |
| 1 | 0 | 1 | 0 | 0 |
| 1 | 1 | 0 | 0 | 1 |

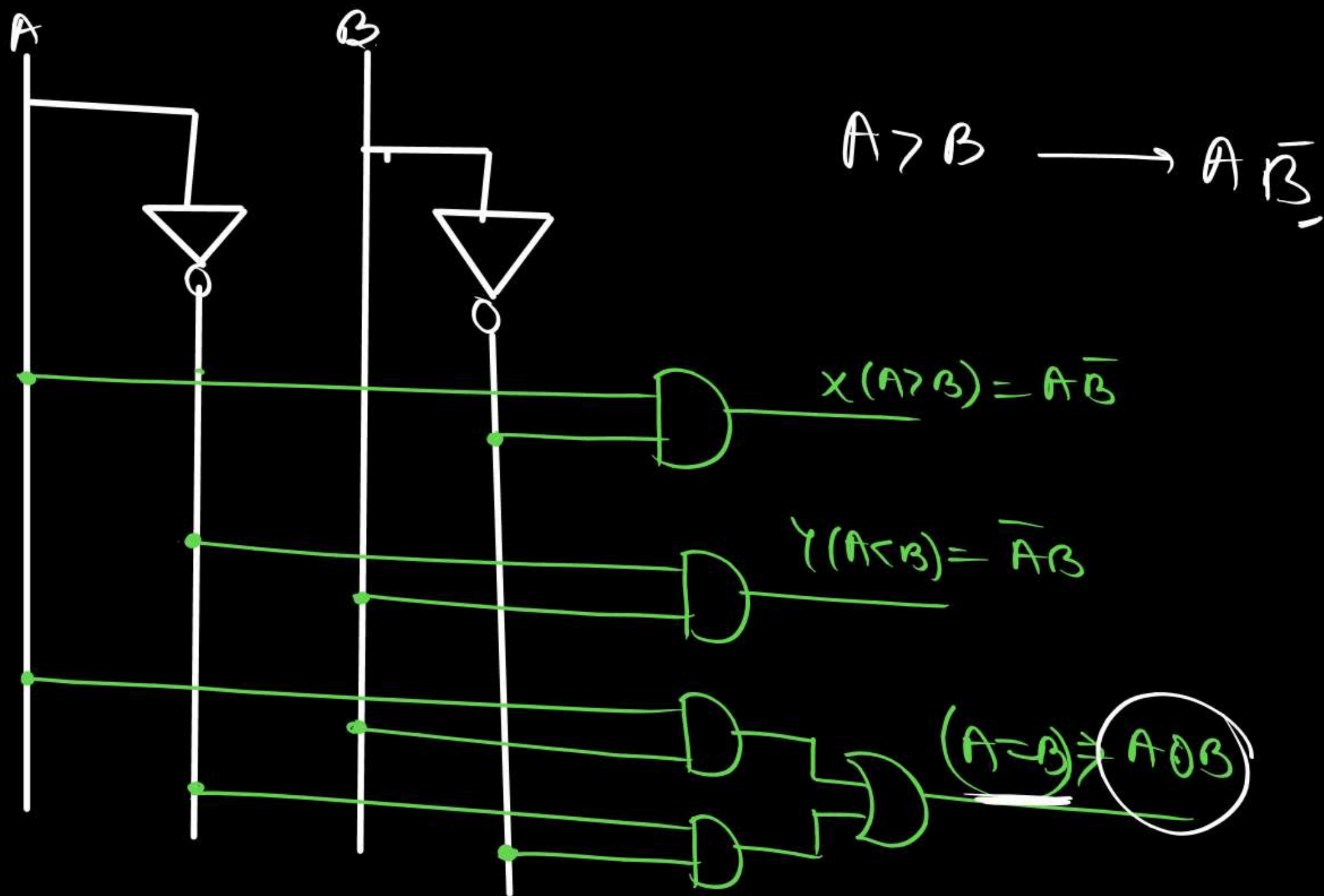
Step 3.

$$X(A > B) = A\bar{B}$$

$$Y(A < B) = \bar{A}B$$

$$Z(A = B) = \bar{A}\bar{B} + AB = A \odot B$$

Step 4:



One bit comparator

Total combination = 4
Equal combination = 2
Unequal combination = 2
Greater = Less = 1

TWO BIT MAGNITUDE COMPARATOR

Step-1





| Step 2 | A | | B | | A > B | (A < B) | (A = B) |
|--------|----------------|----------------|----------------|----------------|-------|---------|---------|
| | A ₁ | A ₀ | B ₁ | B ₀ | x | y | z |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |
| 1 | 0 | 0 | 0 | 1 | 0 | 1 | 0 |
| 2 | 0 | 0 | 1 | 0 | 0 | 1 | 0 |
| 3 | 0 | 0 | 1 | 1 | 0 | 1 | 0 |
| 4 | 0 | 1 | 0 | 0 | 1 | 0 | 0 |
| 5 | 0 | 1 | 0 | 1 | 0 | 0 | 1 |
| 6 | 0 | 1 | 1 | 0 | 0 | 1 | 0 |
| 7 | 0 | 1 | 1 | 1 | 0 | 1 | 0 |
| 8 | 1 | 0 | 0 | 0 | 1 | 0 | 0 |
| 9 | 1 | 0 | 0 | 1 | 1 | 0 | 0 |
| 10 | 1 | 0 | 1 | 0 | 0 | 0 | 1 |
| 11 | 1 | 0 | 1 | 1 | 0 | 1 | 0 |
| 12 | 1 | 1 | 0 | 0 | 1 | 0 | 0 |
| 13 | 1 | 1 | 0 | 1 | 1 | 0 | 0 |
| 14 | 1 | 1 | 1 | 0 | 1 | 0 | 0 |
| 15 | 1 | 1 | 1 | 1 | 0 | 0 | 1 |

$$X(A > B) = \sum m(4, 8, 9, 12, 13, 14)$$

| A ₁ A ₀ \ B ₁ B ₀ | 00 | 01 | 11 | 10 |
|---|----|----|----|----|
| 00 | | | | |
| 01 | 1 | | | |
| 11 | 1 | 1 | | 1 |
| 10 | 1 | 1 | | |

$$Y(A < B) = \sum m(1, 2, 3, 6, 7, 11)$$

| A ₁ A ₀ \ B ₁ B ₀ | 00 | 01 | 11 | 10 |
|---|----|----|----|----|
| 00 | | 1 | 1 | 1 |
| 01 | | | 1 | 1 |
| 11 | | | | |
| 10 | | | 1 | |

$$X(A > B) = A_1 \bar{B}_1 + A_0 \bar{B}_1 \bar{B}_0 + A_1 A_0 \bar{B}_0 \quad \leftarrow \text{minimized expression}$$

$$= A_1 \bar{B}_1 + \bar{A}_1 A_0 \bar{B}_1 \bar{B}_0 + A_1 A_0 B_1 \bar{B}_0$$

$$= A_1 \bar{B}_1 + (\bar{A}_1 \bar{B}_1 + A_1 B_1) \cdot A_0 \bar{B}_0$$

$$= A_1 \bar{B}_1 + (A_1 \odot B_1) \cdot A_0 \bar{B}_0$$

Semimized

$$Y(A < B) = \bar{A}_1 B_1 + \bar{A}_1 \bar{A}_0 B_0 + \bar{A}_0 B_1 B_0$$

$$Y(A < B) = \bar{A}_1 B_1 + (A_1 \odot B_1) \bar{A}_0 B_0$$

Minimized

$$Z(A = B) = (A_1 \odot B_1) \cdot (A_0 \odot B_0)$$



Two bit comparator

Total combination = 16

Equal combination = 4

unequal combination = 12

Greater = Less = 6



Three bit comparator

Total combination = 64

Equal combination = 8

unequal combination = 56

Greater = Less = 28

"n" bit comparator

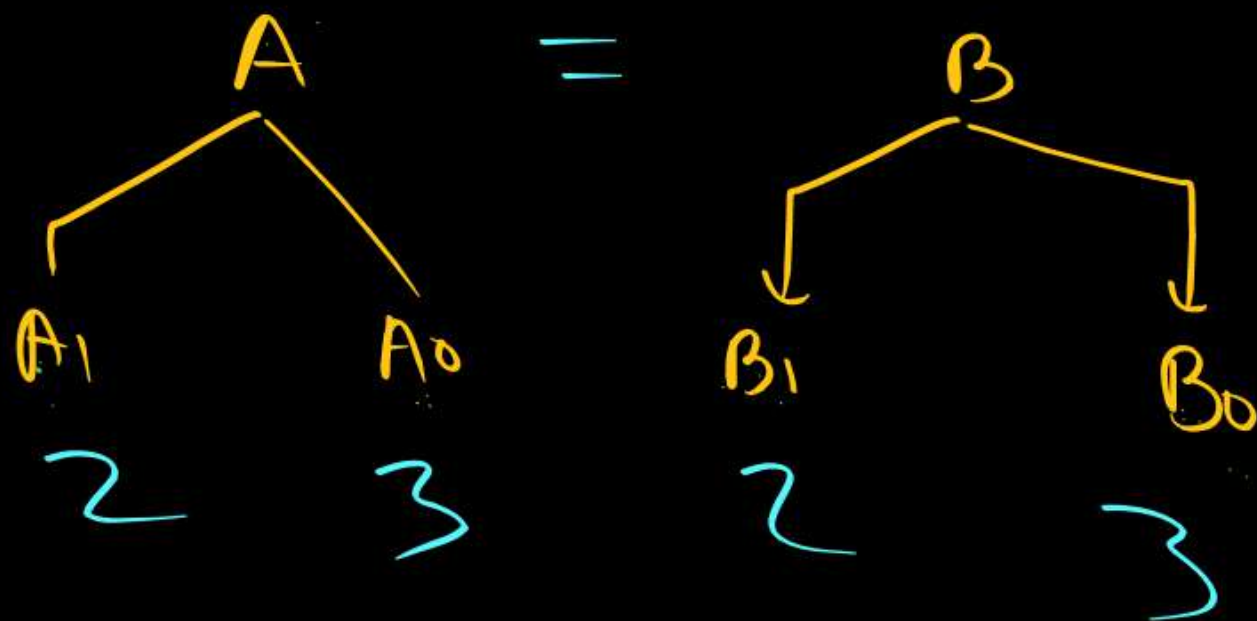
Total combination = 2^{2n}

Equal combination = 2^n

unequal combination = $2^{2n} - 2^n$

Greater = Less = $\frac{2^{2n} - 2^n}{2}$

Semiminimized



$$A > B \Rightarrow A_1 \bar{B}_1 + (A_1 \odot B_1) \cdot A_0 \bar{B}_0$$

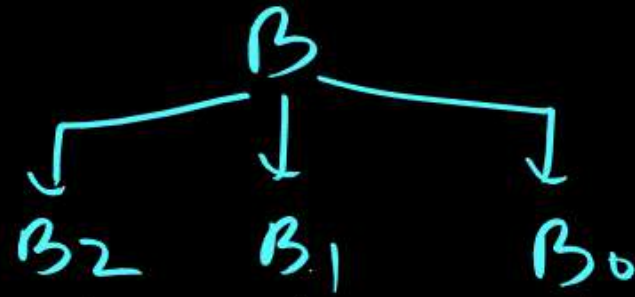
$$A < B \Rightarrow \bar{A}_1 B_1 + (A_1 \odot B_1) \bar{A}_0 B_0$$

$$A = B \Rightarrow (A_1 \odot B_1) \cdot (A_0 \odot B_0)$$

$$A > B \xrightarrow{\checkmark} A \bar{B}$$

$$A < B \Rightarrow \bar{A} B$$

$$A = B \Rightarrow A \odot B$$



$$A > B$$

$$A_2 \bar{B}_2 + (A_2 \odot B_2) \bar{A}_1 \bar{B}_1 + (A_2 \odot B_2) \cdot (A_1 \odot B_1) \bar{A}_0 \bar{B}_0$$

$$A < B$$

$$\bar{A}_2 B_2 + (A_2 \odot B_2) \bar{A}_1 B_1 + (A_2 \odot B_2) \cdot (A_1 \odot B_1) \cdot \bar{A}_0 B_0$$

$$A = B$$

$$(A_2 \odot B_2) (A_1 \odot B_1) \cdot (A_0 \odot B_0)$$



$$\longrightarrow 2^{2n}$$

$$\longrightarrow 2^n$$

$$\longrightarrow 2^{2n} - 2^n$$

$$\begin{array}{r} \longrightarrow 2^{2n} - 2^n \\ \hline \end{array}$$

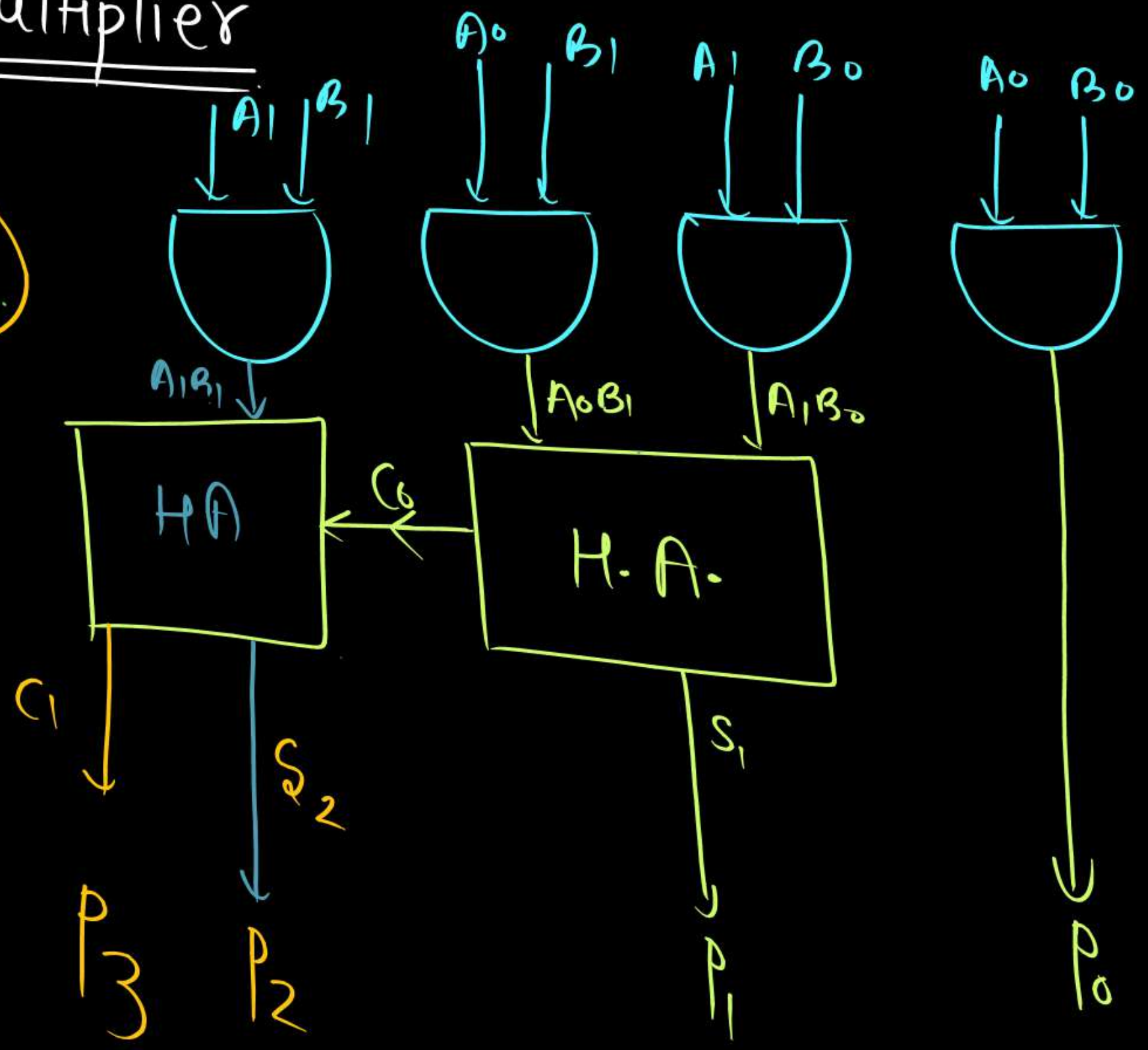
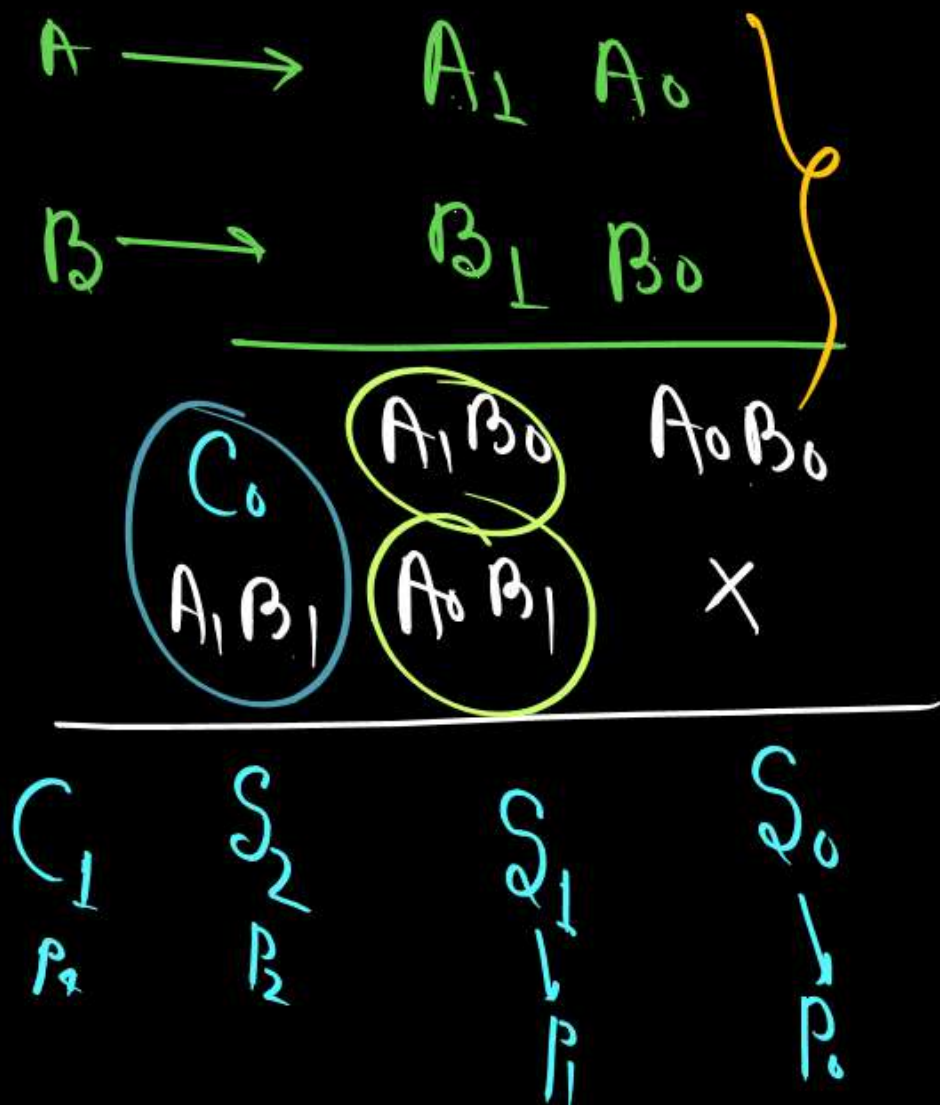
दुनियाभर में

जुनून होना चाहिए
लक्ष्य को पाने के लिए,
सपना तो हर कोई देखता है
दूसरों को बताने के लिए.



Multiplier

2 bit multiplier



"सोचने से मिलते नहीं
तमन्नाओं के शहर मंज़िल को
पाने के लिए चलना भी
जरूरी है"

$$f = A + BC$$

NAND = ?

NOR = ?

8:00 AM

Up

