

Q.1)

What is the time complexity of the following code

```
sum=0;
for(i=n;i>=0;i--)
{
    for(j=1;j<n;j=j*2)
    {
        sum+=(j+i);
    }
}
```

- A $\Theta(\log n)$
- B $\Theta(m \log n)$
- C $\Theta(n^2)$
- D $\Theta(n \log n)$

Max Marks: 1



Solution: (D)

The outer loop is executed n times, and the inner loop is executed $\log n$ times as at each iteration j is multiplied by 2 and each time, it will require $\Theta(\log n)$ steps to reach n . Therefore total time complexity $\Theta(n \log n)$

Correct Option

Q.2)

The time complexity of an algorithm following the given recurrence relation is

Max Marks: 1



- $T(n)=5T(n/3)+\log n$
- A $\Theta(1)$
 - B $\Theta(n \log n)$
 - C $\Theta(\sqrt{n})$
 - D $\Theta(n^2)$

Correct Option

Solution: (D)

On solving the recurrence relation using masters theorem $a=5$ $b=3$ $k=0$ we get $T(n)=\Theta(n^{\log_3 5})$
The closes among all the options is D.

Q.3)

The worst case running time to search for an element in a balanced in a binary

Max Marks: 1

search tree with n^*2^n elements is:

- A $\Theta(n \log n)$
- B $\Theta(n 2^n)$
- C $\Theta(n)$

Correct Option

Solution: (C)

Solution: Ans is (C) $\Theta(n)$

Balanced binary tree means AVL tree then:

Time taken to search an element is $\Theta(\log n)$ where n is no. of elements in AVLtree. As number of elements given is n^*2^n , the searching complexity will be $\Theta(\log(n^*2^n))$ which can be written as:

$$= \Theta(\log(n^*2^n))$$

$$= \Theta((\log n) + \Theta(\log(2^n)))$$

$$= \Theta((\log n) + \Theta(n \log(2)))$$

$$= \Theta((\log n) + \Theta(n))$$

As $\log n$ is asymptotically smaller than n , $\Theta(\log(n)) + \Theta(n)$ can be written as $\Theta(n)$

which matches option C.

D

$$\Theta(\log n)$$

Q.4)

An AVL tree of height $h=4$ with minimum nodes is given then find the number of leaf nodes in this tree.

Max Marks: 1

A

$$h$$

B

$$h-1$$

C

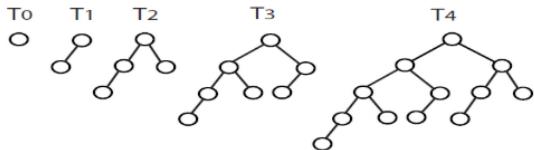
$$h+1$$

Correct Option

Solution: (C)

Solution: Ans is (C) $h+1$

AVL tree are height balanced tree. In these trees height balanced factor for nodes can be 0, 1, +1 so height balanced trees will be like this.



By the above figures of AVL tree, of different heights we can check that. In the AVL tree of height 4, there are total 5 leaf nodes. So answer will be $h+1$.

D

$$h+2$$

Q.5)

The time complexity to topologically sort the vertices of a given graph G with n vertices and m edges is given by

Max Marks: 1

A

$$\Theta(n \log m)$$

B

$$\Theta(nm)$$

C

$$\Theta(n+m)$$

Correct Option

Solution: (C)

Topological sorting of the vertices can be done using DFS and additional linked list to maintain the topological order, once a particular vertex is explored in DFS it is added to the first node in the linked list once the DFS of the graph is completed the linked list gives us the topological ordering. Time for DFS = $\Theta(n+m)$ and Time for inserting into linked list is $\Theta(n)$, total time required = $\Theta(n+m)$.

D

None of the above.

Q.6)

Consider the following segment of code

Max Marks: 1

```
for(i=0;i<2*n;i=i+n)
{
    for(j=1;j<n;j=j*2)
    {
        printf("%d%d",i,i);
    }
    printf("\n");
}
```

What is the number of new lines printed by the above fragment of code

A

$$\Theta(\log n)$$

B

$$\Theta(n)$$

C

$$\Theta(n \log n)$$

D

None of the above.

Correct Option

Solution: (D)

The no of new lines are only printed by the printf statement of the outer for loop. the outer loop only executes 2 times which is $\Theta(1)$ times.

Q.7)

Which of the following sorting algorithm is not an in-place sorting technique

Max Marks: 1

A Heap sort

B Merge sort

Correct Option

Solution: (B)

Heapsort, Bubble Sort and Merge sort do not require additional space and hence are in-place sorting algorithms whereas Mergesort requires additional space, therefore, Merge Sort is not an in-place sorting algorithm.

C Bubble sort

D Insertion sort.

Q.8)

How many queues are required for implementing priority queue

Max Marks: 1

A only 1

B 2

Correct Option

Solution: (B)

Solution: Ans is (B) 2

Priority queue has the priority associated with each element. So 1 queue will store the elements and 2nd queue will give priority to the elements which are stored in the queue. We will need 2-queues.

C 3

D 4

Q.9)

From the given in-order of balanced binary search tree 9, 12, 14, 17, 19, 22, 28, 32, 39, 55, 58 left subtree and right subtree with equal nodes and height 2. And pre-order of this is 22, 14, 12, 9, 17, 19, 39, 32, 28, 55, 58. Then find out sum of all leaf nodes.

Max Marks: 1

A 56

B 58

C 86

D 114

Correct Option

Solution: (D)

Solution: Ans is (D) 114

Here, we are starting with in-order and pre-order
In-order: 9, 12, 14, 17, 19, 22, 28, 32, 39, 55, 58
Pre-order: 22, 14, 12, 9, 17, 19, 39, 32, 28, 55, 58

As we know that in-order traversal is LEFT, ROOT, RIGHT while pre-order traversal is ROOT, LEFT, RIGHT. So 22 will be root node and 14 will be the first node at left subtree. Then construct tree by knowing order of node in in-order traversal and pick the element from the pre-order traversal. So final tree will be like this.



So leaf nodes will be 9, 19, 28, 58 and sum of these elements will be 114.

Q.10)

Find the sum of all the PRIME numbers of the queue after performing all operations.

enqueue(4)enqueue(5)dequeue()enqueue(8)enqueue(9)enqueue(6)dequeue()enqueue(7)

dequeue()enqueue(1)enqueue(2)enqueue(3)dequeue()

Max Marks: 1

A 10

B 11

Solution: (c)**Solution:** Ans is (C) 12

Here, when we go according to question then we need to take a queue and we know queue works on first in first out concept so

4	5				
---	---	--	--	--	--

dequeue () : it will delete 4 from the queue

	5	8	9	6	7
--	---	---	---	---	---

dequeue () : it will delete 5 from the queue

		8	9	6	7
--	--	---	---	---	---

dequeue () : it will delete 8 from the queue

			9	6	7	1	2	3
--	--	--	---	---	---	---	---	---

dequeue () : it will delete 9 from the queue

				6	7	1	2	3
--	--	--	--	---	---	---	---	---

And prime numbers are 2, 3, 7 and the sum of these three is 12 only.

D

13

Q.11)

Max Marks: 2

Consider a Circular Queue 'q' is implemented whose size is given 15 and the locations of elements of the queue are q[0], q[1], q[2].....,q[14]. In this given circular queue currently rear is pointing at q[7] after inserting 11th element, then find the position of front in this queue (as element insertion can be started from anywhere and it will be moved forward in ascending order like (0,1,2,3----,13,14,0,1).

A

q [2]

B

q [3]

C

q [11]

D

q [12]

Correct Option

Solution: (D)**Solution:** Ans is (D). q [12]

If we start insertion from location q[12].

Then q[7] = 11th elementq[6] = 10th elementq[5] = 9th elementq[4] = 8th elementq[3] = 7th elementq[2] = 6th elementq[1] = 5th elementq[0] = 4th elementq[14] = 3rd elementq[13] = 2nd elementq[12] = 1st element**Q.12)**

Max Marks: 2

Given the following set of jobs to be scheduled on a single processor machine and their deadlines and profit, what is the optimum profit which can be obtained by any schedule _____

Job	Finish Time (Deadline)	Profit
1	4	20
2	3	10
3	2	12
4	5	17
5	5	12
6	2	14
7	3	15

Correct Answer

Solution: (78)

For job sequencing within deadlines, we have to schedule the most profitable jobs as late as possible here is the optimum schedule.

Time	1	2	3	4	5
Job	3 or 5	6	7	1	4
Profit	12	14	15	20	17

Total profit =78

Q.13)

The number of comparisons in the bubble sort sorting is given by

Max Marks: 2

A $O(n^2)$

Correct Option

Solution: (A)

In bubble sort the comparisons are in the following pattern,

1st iteration - n-1 comparisons

2nd iteration n-2 comparisons

3rd iteration n-3 comparisons

....

N-1 th iteration 1 comparison,

Total no of comparisons= $n(n-1)/2= O(n^2)$

B $O(n)$

C $O(n \log n)$

D None of the above.

Q.14)

Max Marks: 2

Given string "gateappliedcourse" is stored in the stack character by character. When we get null character then we start popping characters from stack and enqueue into modified queue. Then what will be the output of modified queue for dequeued characters if it is working with three functions enqueue, reverse, dequeue. (Assume it is reversing all the elements before performing dequeue operation)

A esruocdeilppaetag

Correct Option

B gateappliedcourse

Solution: (B)

Solution: Ans is (B) gateappliedcourse

Here, we need to remember two concepts stack- LIFO and queue- FIFO

First, we are inserting string characters one by one into the stack and after the end of string when we get null character. Null character is always found at the end of string. So after pushing string characters in the stack we get null characters.

G	a	t	e	a	p	p	l	l	e	d	c	o	u	r	s	e
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

Then characters are removed from the stack and inserted in the modified queue. After insertion of characters, it is performing reverse operation so characters are reversed and at the time of dequeue it will simply print the same string as characters will be printed in the same order.

C gatedeilppacourse

D etagapplieddesruoc

Q.15)

Max Marks: 2

If we are hashing given array elements as $h(k) \bmod 9$ in the hash table of 9 slots starting from zero index element and collisions are resolved using linear probing then find out which element of highest array index(given) is inserted without collision. Array is given as follows:

Index	0	1	2	3	4	5	6	7
keys	26	2	5	9	14	38	49	87

Choose the correct option for the above scenario.

A. 87

B. 49

C. 38

D. 9

A

87

87

Solution: (B)**Solution:** Ans is (B)49For inserting elements we are using $h(k) \bmod 9$, hash table is given as follows:

0	9
1	
2	2
3	38
4	49
5	5
6	14
7	87
8	26

26 mod 9 = at 8th place in hash table

2 mod 9 = at 2nd place in hash table

5 mod 9 = at 5th place in hash table

9 mod 9 = at 0th place in hash table

14 mod 9 = at 5th place but it's not empty then at 6th place

38 mod 9 = at 2nd place but it's not empty then at 3rd place.

49 mod 9 = at 4th place

87 mod 9 = at 6th place but it's not empty then at 7th place

By this we can conclude, element 49 which has highest array index is inserted without collision in hash table.

C

38

D

9

Q.16)

Max Marks: 2

What is the length of the longest common subsequence for the given strings is_____

“abracadabra”

“abcdefabcdef”

Correct Answer

Solution: (6)

The longest common subsequence of the two strings is “abcdab”

Q.17)

Max Marks: 2

There is a queue q with enqueue, dequeue operations, which already has 8 elements with it as 4, 5, 6, 9, 1, 2, 3, 7 (4 is enqueued first and 7 at last). Then run the following given code. Here, s is the stack with push and pop operations.

```
for ( i=1; i<=5; i++)
{
x = q.dequeue();
s.push(x);
}
for ( i=1; i<= 3; i++)
{
x= s.pop();
enqueue(x);
}
```

Find the order of elements after performing all operations.

A

4, 5, 6, 7, 3, 2

B

4, 5, 6, 9, 1, 2

C

2, 3, 7, 4, 5, 6

D

2, 3, 7, 1, 9, 6

Correct Option

Solution: (D)**Solution:** Ans is (D) 2, 3, 7, 1, 9, 6

In the starting q have elements as

Q = 4, 5, 6, 9, 1, 2, 3, 7

After performing dequeue operation 5 times as loop is given up to 5, remaining Q will be as Q = 2, 3, 7

And stack s will be s = 4, 5, 6, 9, 1 (top)

Then for the second for loop, which will be executed three times, so the remaining elements in the stack s = 4, 5

And popped elements are 1, 9, 6 which we enqueue in the q

Then order of elements in the q after inserting these elements is 2, 3, 7, 1, 9, 6

So option D is correct

Q.18)

Consider the following sorting algorithm if "A" represents the array to be sorted and i, j represent the index to the first and the last element of the array, the time complexity of the such an algorithm is

```
STOOGES-SORT(A, i, j)
1. if A[i] > A[j]
2.   then exchange A[i] ↔ A[j]
3. if i + 1 ≥ j
4.   then return
5. k ← ⌊(j - i + 1)/3⌋
6. STOOGES-SORT(A, i, j - k)
7. STOOGES-SORT(A, i + k, j)
8. STOOGES-SORT(A, i, j - k)
```

 A $O(n^{(\log 3) \log 1.5})$

Correct Option

Solution: (A)

The recurrence relation for the above can be given by

$$T(n)=3(T(n/3)+1)$$

On solving using Masters Theorem or by recursion tree method we get

$$O(n^{(\log 3) \log 1.5})$$

 B

$$O(n^{(\log 2)})$$

 C

$$O(n^2)$$

 D

$$O(n^{(\log 2)^{(\log 2)}})$$

Q.19)

Consider the following singly linked-list.

P = A(2000) → B(3000) → C(4000) → D(5000) → E(6000) → F(7000) → G (NULL)

And then after executing following four statement

- (I). struct node *Q;
- (II). Q = P → next → next → next
- (III). P → next → next → next → next = Q → next → next
- (IV). printf("%d", Q → next);

Choose the correct option for the above scenario

 A

D

 B

68

 C

E

 D

69

Correct Option

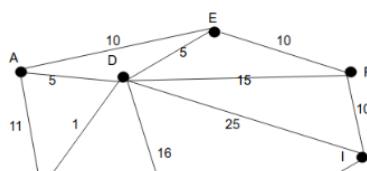
Solution: (D)

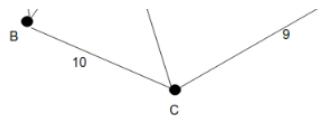
Solution: Ans is (D) 69

- (I). struct node *Q; // initializing one more variable for storing linked list
 - (II). Q = P → next → next → next // start pointing at 4000
 - (III). P → next → next → next → next // start pointing at 5000 and 5000 → next
= Q → next → next // Q was pointing at 4000 here also 5000 → next
 - (IV). printf("%d", Q → next); // we will print content of 5000 → next i.e. E and its ascii value is 69
- So answer (C) E is true.

Q.20)

The number of minimal spanning trees for the given graph below are _____

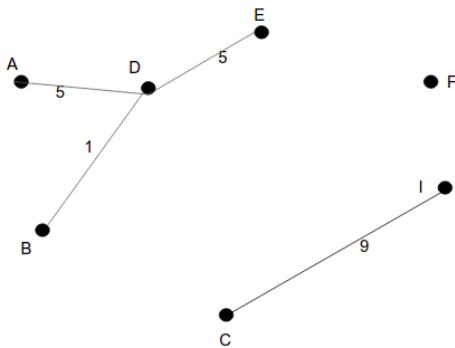




Correct Answer

Solution: (3)

If we apply Kruskal's algorithm for MST we get the following graph till the weight of the edges ≤ 9



Now we have 4 edges of weight 10 AE (this forms a cycle so it is ruled out), now we have (EF), (FI) and BD adding any two edges will make it a MST this can be done in $C(3,2)$ ways. Therefore the no of minimal spanning tree is 3.

close