

COMPUTER SCIENCE



Database Management System

Introduction of RDBMS,
FD's and Keys Concept,
Finding Multiple
Candidate Key

Lecture_01



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DBMS

Lecture schedule

DBMS GATE Syllabus



(7-9 marks)
8 marks

- Functional dependency and Normalization. ✓
- Transaction and Concurrency control. ✓
- Relational Algebra, TRC and SQL ✓
- File Organization and Indexing ✓
- ER model and Integrity constraints. ✓

Functional Dependency (FD's)

- ❑ FD concepts ✓ (2-4m)
- ❑ FD types ✓
- ❑ Attribute closure ✓
- ❑ Keys Concept
 - ❖ Super key
 - ❖ Candidate key ✓
 - ❖ Primary key
 - ❖ Alternative / secondary key
- ❑ Finding multiple candidate keys ✓
- ❑ Membership set ✓

- ❑ Equality between 2 FD sets. ✓
- ❑ Minimal cover (Canonical cover). ✓
- ❑ Lossy and Lossless Join Decomposition. ✓
- ❑ Dependency preserving Decomposition. ✓

Normalization

❑ Need of Normalization ?

Normal Forms

- ❖ 1 NF
- ❖ 2 NF
- ❖ 3 NF
- ❖ BCNF

& Decomposition

Transaction & Concurrency Control

(2 m)

- ❑ Transaction concept
- ❑ ACID Properties
- ❑ Schedules (serial & non serial schedule)
- ❑ Serializable schedule
 - ❖ conflict Serializable
 - ❖ View serializable
- ❑ Testing method for conflict serializability
- ❑ Conflict equivalent schedule
- ❑ Problem due to concurrent execution
- ❑ Recoverable, cascadeless, strict recoverable schedule.

- ❑ Implementation of concurrency control
 - ❖ Lock based protocol.
- ❑ 2 Phase locking protocol (Basic 2PL, Strict 2PL, Rigorous 2PL, Conservative 2PL)
- ❑ Time stamp based protocol (Thomas write Rule)

Query Language

(2-3m)

□ Introduction of Relational Algebra (RA)

Operations

- ❖ Selection (σ)
- ❖ Projection (π)
- ❖ Union (\cup)
- ❖ Set Difference ($-$)
- ❖ Cross Product (\times)
- ❖ Rename (ρ)
- ❖ Intersection (\cap)
- ❖ Division ($/$)
- ❖ Join & its type.

(RA) SQL TRC

- ❑ TRC (Tuple Relational Calculus)
- ❑ SQL & its clauses
 - ❖ Aggregate operators
 - ❖ Set operators
- ❑ Nested Query

File Organization & Indexing

(1-2m)



- ❑ Spanned and unspanned organization ✓
- ❑ Sparse & Dense Index ✓
- ❑ Indexing type (primary, clustered, secondary index) ✓
- ❑ Multi level indexing ✓
- ❑ B Tree
- ❑ B + Tree

ER Model & Integrity Constraints.

- ✓ ☐ Introduction of ER Model
- ✓ ☐ Attributes and its type
- ✓ ☐ Relationship set
- ✓ ☐ Participation constraints
- ✓ ☐ Cardinality Ratio
- ✓ ☐ Strong and weak entity set

8:11 AM

Foreign key concept and its constraint

Conversion of ER model to Relations (Tables).

Books:

Henry F. Korth }
Navathe
Raghu Ramakrishnan



Crystal Clear



DBMS

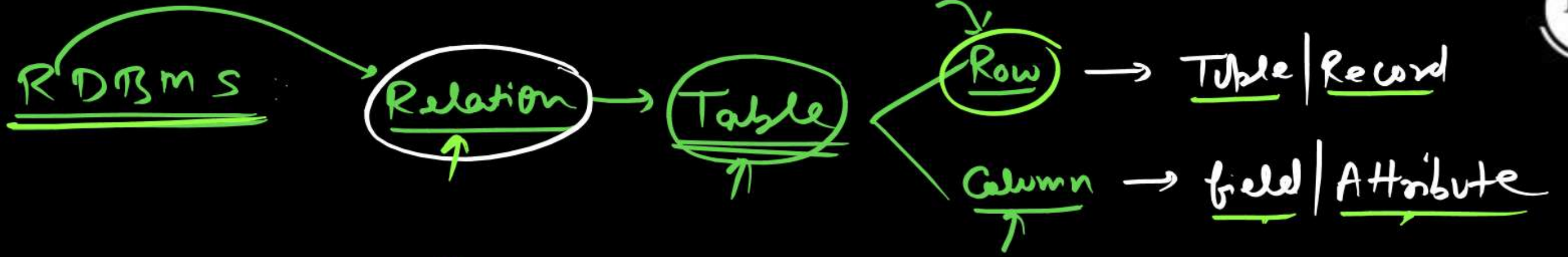
- Data → Row material | Facts



- Database (Collection of logically Related Data)



- DBMS



Domain

STUDENT

Sid	Name	Marks	Branch
S ₁	A	9	CS
S ₂	B	10	IT
S ₃	C	9	CS
S ₄	D	10	CS
S ₅	E	9	IT
S ₆	F	10	IT

Degree of Relation

of Attributes

Ariety # of Attributes [4]

Cardinality # of Tuples [6]

Relational Schema: Table Heading
 STUDENT(Sid, Name, Marks, Branch)

Relational Instance: Set of Records.

FD : $X \rightarrow Y$ (Functional Dependency)

$R(X, Y)$ $X \rightarrow Y$

X	Y
1	5
2	6
3	7
4	8
2	5
4	9

(i)



X	Y
1	5
2	6
3	5
4	6
5	7

(ii)



X	Y
1	6
2	6
3	6
4	6
5	6

(iii)



X	Y
x_1	y_1
x_2	y_2
x_3	y_3
x_4	y_5
x_5	y_7
x_2	y_2
x_3	y_3

(iv)



X	Y
x_1	y_1
x_2	y_5
x_3	y_5
x_4	y_1

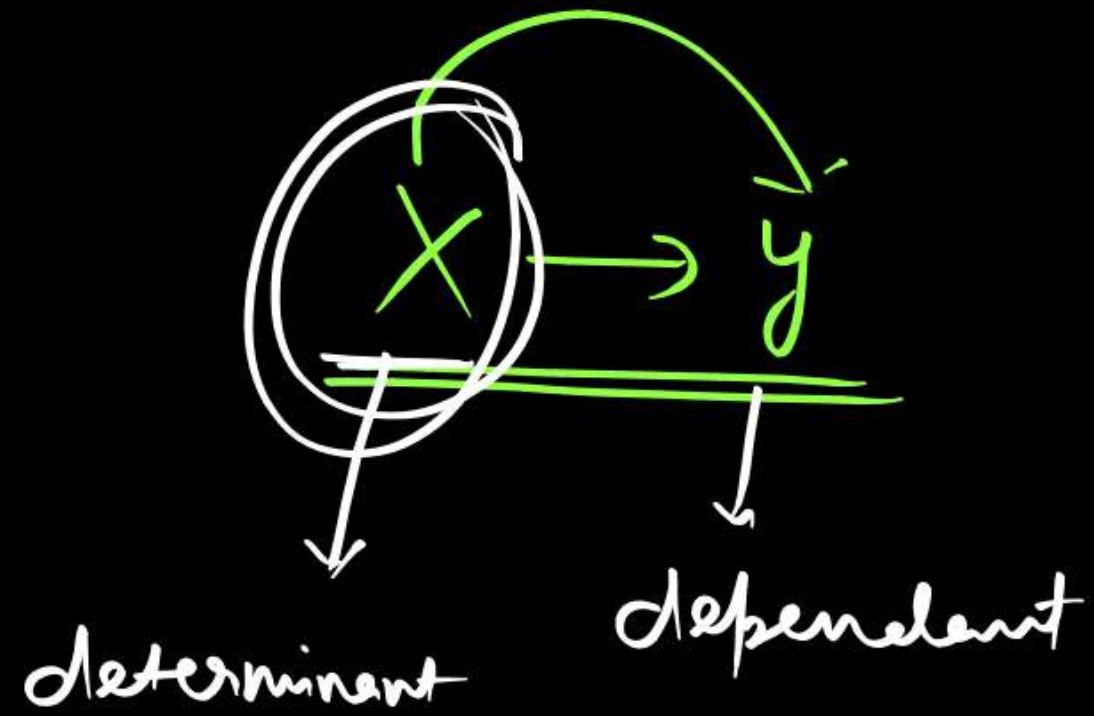
(v)



X	Y
1	5
2	6
3	7
4	8
5	9
1	5
4	8
5	9

(vi)





$X \rightarrow Y$
 ① \rightarrow Abhay

24 \rightarrow Prashant

56 \rightarrow Vijay Agarwal

$R(X, Y)$

FD

$X \rightarrow Y$

Relation Schema R in which X & Y be the attribute set of R . t_1 & t_2 Any

Two Tuple Such that

$X \rightarrow Y$

If $t_1.X = t_2.X$ then $t_1.Y = t_2.Y$ must be same

Note

: In $X \rightarrow Y$ Whenever X Value Repeat, Corresponding Y Value Must be same.

Type of FD

- ① Trivial FD
- ② Non Trivial FD
- ③ Semi Non Trivial FD

① Trivial FD

(Always Valid)

$X \rightarrow Y$ is Trivial FD

if $X \supseteq Y$ (R.h.s Attribute equal or Part of L.h.s Attribute.)

AB \rightarrow A

AB \rightarrow B

AB \rightarrow AB

Rollno name \rightarrow Roll No

Roll No Name \rightarrow Name

Roll No Name \rightarrow Roll No Name

② Non Trivial FD

$X \rightarrow y$ is Non Trivial

If $X \cap y = \phi$ & must satisfy
FD Definition

$A \rightarrow B$

$A \rightarrow C$

Sid \rightarrow Branch

Sid \rightarrow Grade

③ Semi Non Trivial FD

$X \cap y \neq \phi$

$X \not\supseteq y$

$(AB) \rightarrow \underline{BC}$

Q.1



Q Which - -
Non Trivial
FD Satisfied
by the Instance

A	B	C
2	2	4
2	3	4
3	2	4
3	3	4
3	2	4

$A \rightarrow C$
 $B \rightarrow C$
 $AB \rightarrow C$

Ans

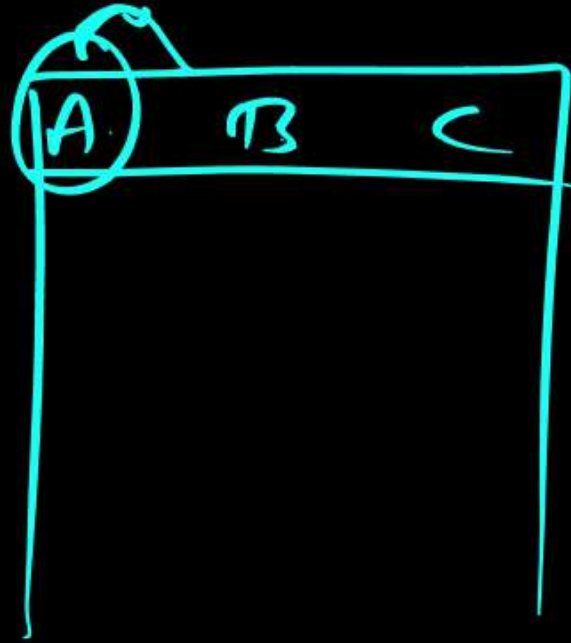
~~$A \rightarrow B$~~
 ~~$A \rightarrow C$~~
 ~~$A \rightarrow BC$~~

~~$B \rightarrow A$~~
 ~~$B \rightarrow C$~~
 ~~$B \rightarrow AC$~~

~~$C \rightarrow A$~~
 ~~$C \rightarrow B$~~
 ~~$C \rightarrow AB$~~

~~$AB \rightarrow C$~~
 ~~$BC \rightarrow A$~~
 ~~$AC \rightarrow B$~~

R(ABC)



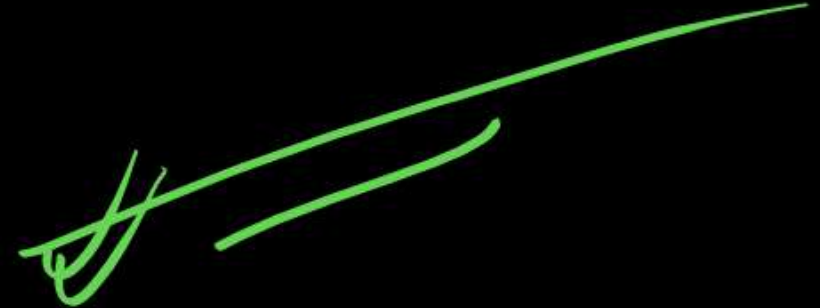
Non Trivial FD Case

$A \rightarrow B$
 $A \rightarrow C$
 $A \rightarrow BC$

$B \rightarrow A$
 $B \rightarrow C$
 $B \rightarrow AC$

$C \rightarrow A$
 $C \rightarrow B$
 $C \rightarrow AB$

$AB \rightarrow C$
 $BC \rightarrow A$
 $AC \rightarrow B$



Q.2

Given the following relation instance.

X	Y	Z
4	4	4
4	7	4
7	4	7
7	4	9
4	9	9

~~$X \rightarrow Y$~~ ~~$Y \rightarrow X$~~
 ~~$X \rightarrow Z$~~ ~~$Y \rightarrow Z$~~
 ~~$X \rightarrow YZ$~~ ~~$Y \rightarrow XZ$~~

~~$Z \rightarrow X$~~ ~~$XY \rightarrow Z$~~
 ~~$Z \rightarrow Y$~~ ~~$YZ \rightarrow X$~~
 ~~$Z \rightarrow XY$~~ ~~$XZ \rightarrow Y$~~

The number of non trivial FD's are satisfied by the instance 1

$YZ \rightarrow X$

Ans 1

Q.3

Given the following relation instance.

[GATE 2 marks]



X	Y	Z
1	4	2
1	5	3
1	6	3
3	2	2

Ans [B]

Which of the following functional dependencies are satisfied by the instance?

~~A~~

$X \rightarrow Y$ and $Z \rightarrow Y$

~~B~~

$YZ \rightarrow X$ and $Y \rightarrow Z$

~~C~~

$YZ \rightarrow X$ and $X \rightarrow Z$

~~D~~

$XZ \rightarrow Y$ and $Y \rightarrow X$

FD
 \Downarrow
 Instance

✓ Rule out the FD Based on
the Relation

Trivial FD

Q.4

From the following instance of a relation scheme $R(A, B, C)$, we can conclude that:

[GATE 2 marks]

A	B	C
1	1	1
1	1	0
2	3	2
2	3	2

A

A functionally determines B and B functionally determines C

~~B~~

A functionally determines B and B does not functionally determines C

C

B does not functionally determines C

D

A does not functionally determines B and B does not functionally determines C

Attribute closure $[X]^+$: R be the Relational Schema
 X be the attribute Set of R

(The set of all possible Attributes determined from Attribute X
is called Attribute closure of X $[X]^+$)

Attribute closure $[x]^+$

$R(A, B, C, D, E) \quad [A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow E]$

$$[A]^+ = [A B C D E]$$

$$[B]^+ = [B C D E]$$

$$[C]^+ = [C D E]$$

$$[D]^+ = [D E]$$

$$[E]^+ = [E]$$

$$[B E]^+ = [B E C D]$$

$$[C D]^+ = [C D E]$$



Q.5

R (ABCDEFGG)

F : (AB \rightarrow C, BC \rightarrow AD, D \rightarrow E, E \rightarrow G, CE \rightarrow B)

Find closure of ...

$$[AB]^+ = [ABCDEFGG]$$

$$[BC]^+ = [BCADEGG]$$

$$[CE]^+ = [\underline{C} \underline{E} \underline{B} ADG]$$

$$[E]^+ = [EG]$$

$$[F]^+ = [F]$$

$$[D]^+ = [DEG]$$

Q.6



The following functional dependencies are given

$\{PQ \rightarrow RS, PU \rightarrow S, ST \rightarrow U, R \rightarrow V, U \rightarrow T, V \rightarrow P\}$

Which of the following option (s) is/are true ?

[MSQ]

☒ A $\{RU\}^+ = \{PRSTUV\}$

$$[RU]^+ = [RUVTPS] \Rightarrow [PRSTUV]$$

☐ B $\{PU\}^+ = \{PRSTUV\}$

$$[PU]^+ = [PUTS]$$

☒ C $\{QV\}^+ = \{PQRSV\}$

$$[QV]^+ = [QVPRS] \Rightarrow [PQR \underline{SV}]$$

☐ D $\{PQ\}^+ = \{PQRSUV\}$

$$[PQ]^+ = [PQRSV]$$

Ans (A & C)

Q.7

The following functional dependencies are given:

$AB \rightarrow CD$, $AF \rightarrow D$, $DE \rightarrow F$, $C \rightarrow G$, $F \rightarrow E$, $G \rightarrow A$.

Which one of the following options is false?

GATE: 2M.

(MSQ)

~~True~~ **A**

$\{CF\}^+ = \{ACDEFG\}$

$[CF]^+ = [CFGEAD] \Rightarrow [ACDEFG]$

~~True~~ **B**

$\{BG\}^+ = \{ABCDG\}$

$[BG]^+ = [BGACD]$

C

$\{AF\}^+ = \{ACDEFG\}$

$[AF]^+ = [AFDE]$

D

$\{AB\}^+ = \{ABCDFG\}$

$[AB]^+ = [ABCDG]$

Ans [C] & [D]

Keys Concept

$R(ABCDE)$

$A \rightarrow B$, $B \rightarrow C$, $C \rightarrow D$, $D \rightarrow E$

Solⁿ

$[A]^+ = [ABCDE]$

A is Super Key

$[B]^+ = [BCDE]$

Note

Every Key is a Super Key

$[C]^+ = [CDE]$

Note

Any Super Set of Super Key is also Super Key

$[D]^+ = [DE]$

$[E]^+ = [E]$

A is Super Key then Any Super Set of A is also Super Key

AB
AC
AE
ABC

ABCDE

$$[A]^+ = (AB CDE)$$

$$[AB]^+ = (AB CDE)$$

$$[AE]^+ = (AB CDE)$$

$$[AC]^+ = (AB CDE)$$

Note

Any Super set of Super key is
Super key.

X be the attribute set of 'R'

Super key: If set of Attr Attribute determined by the Attribute closure of X $[X]^+$ then X is a Super key.

key Set of Attribute which Uniquely

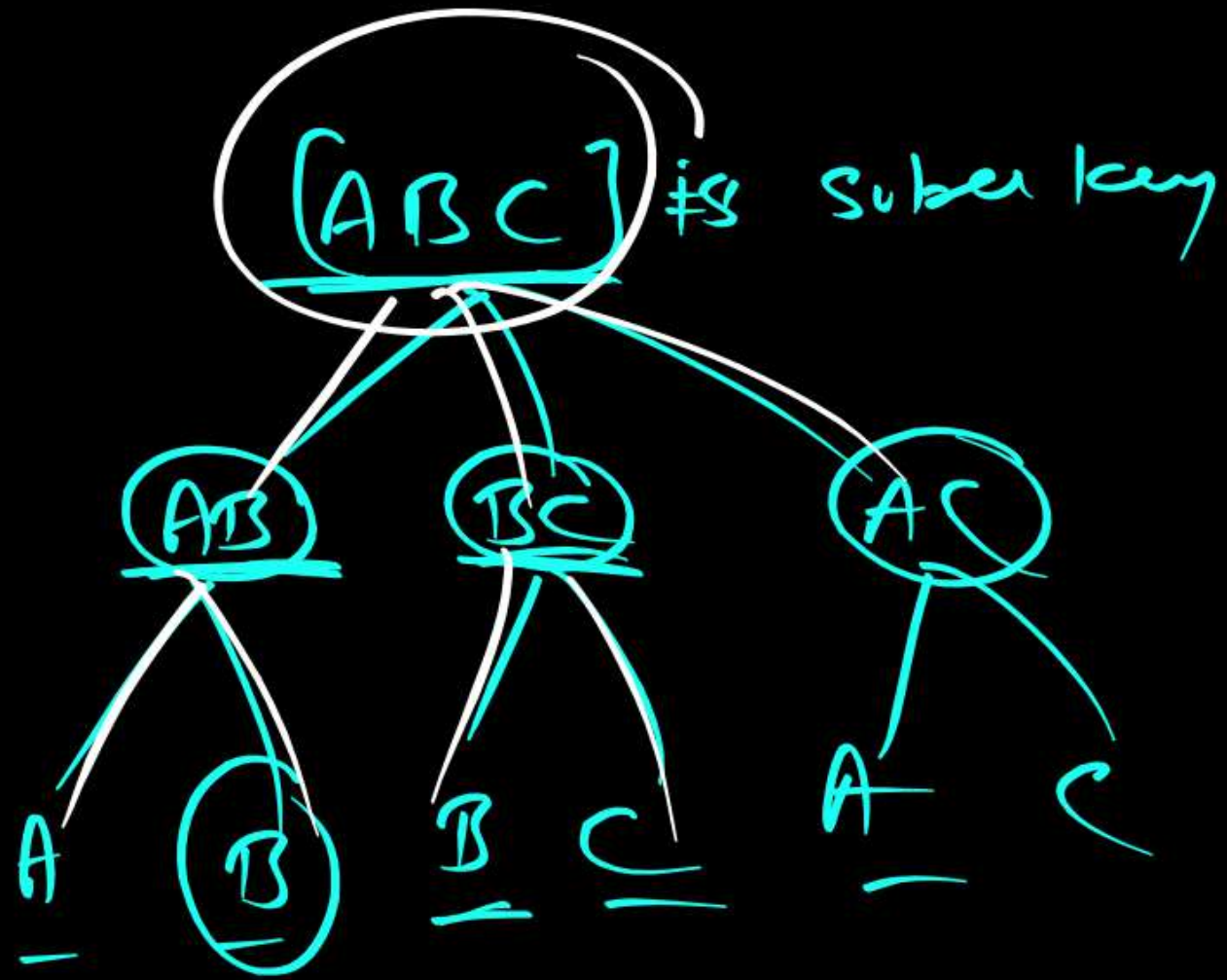
Determine each tuple in the Relation

	A	B	C	D	E
→					
→					

Candidate Key : Minimal of Super Key

If Any proper Subset of Super Key is also Super Key

then that proper Subset is called Candidate Key & So on



$R(\underline{A} \underline{BCD})$

C.K : A

Superkey = $2^3 = 8$ Superkey

A
AB
AC
AD

ABC
ACD
ABD
ABCD

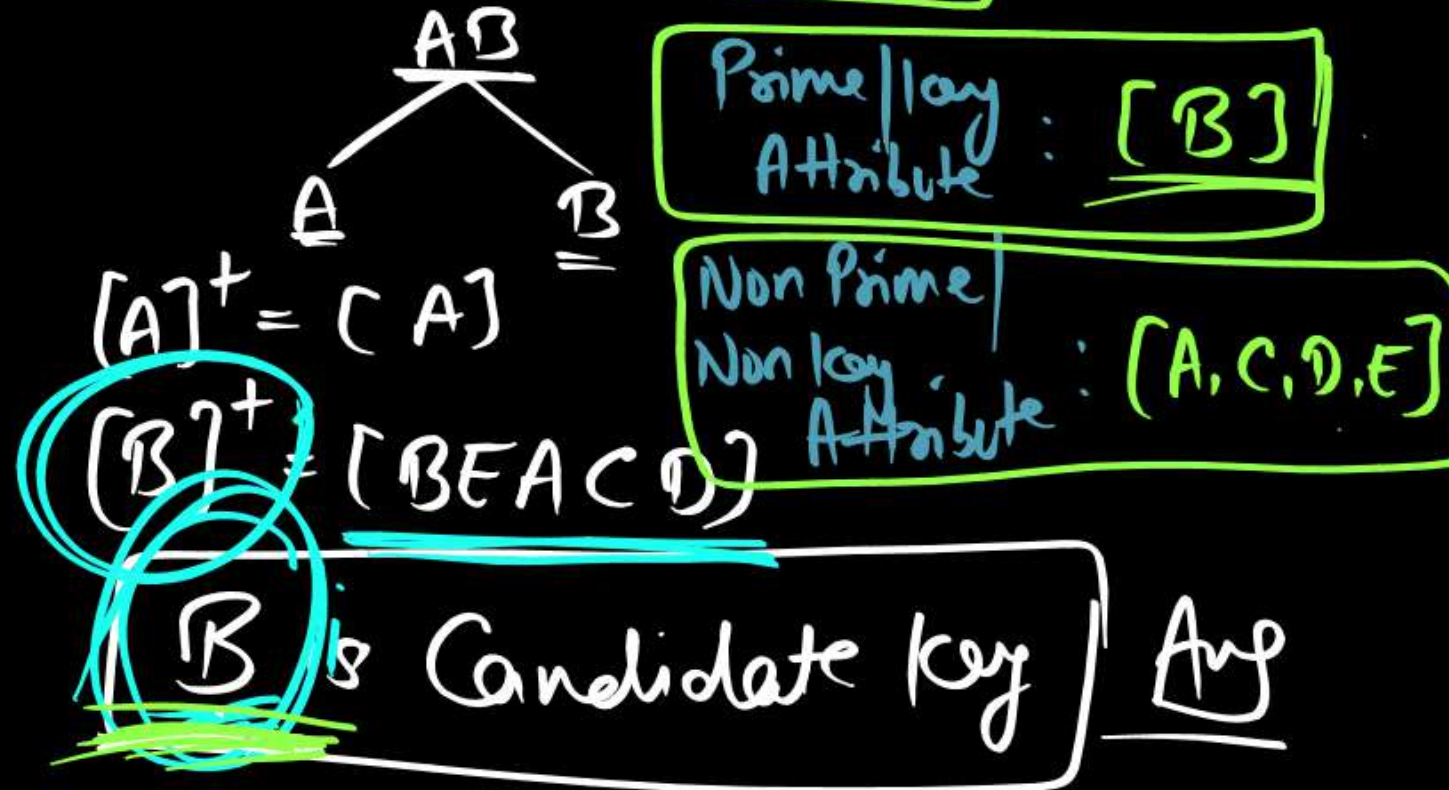
Candidate key: Minimal of Super key

$R(AB CDE) \{AB \rightarrow C, C \rightarrow D, \underline{B \rightarrow E}\}$

(Solⁿ)

$[AB]^+ = (AB CDE)$

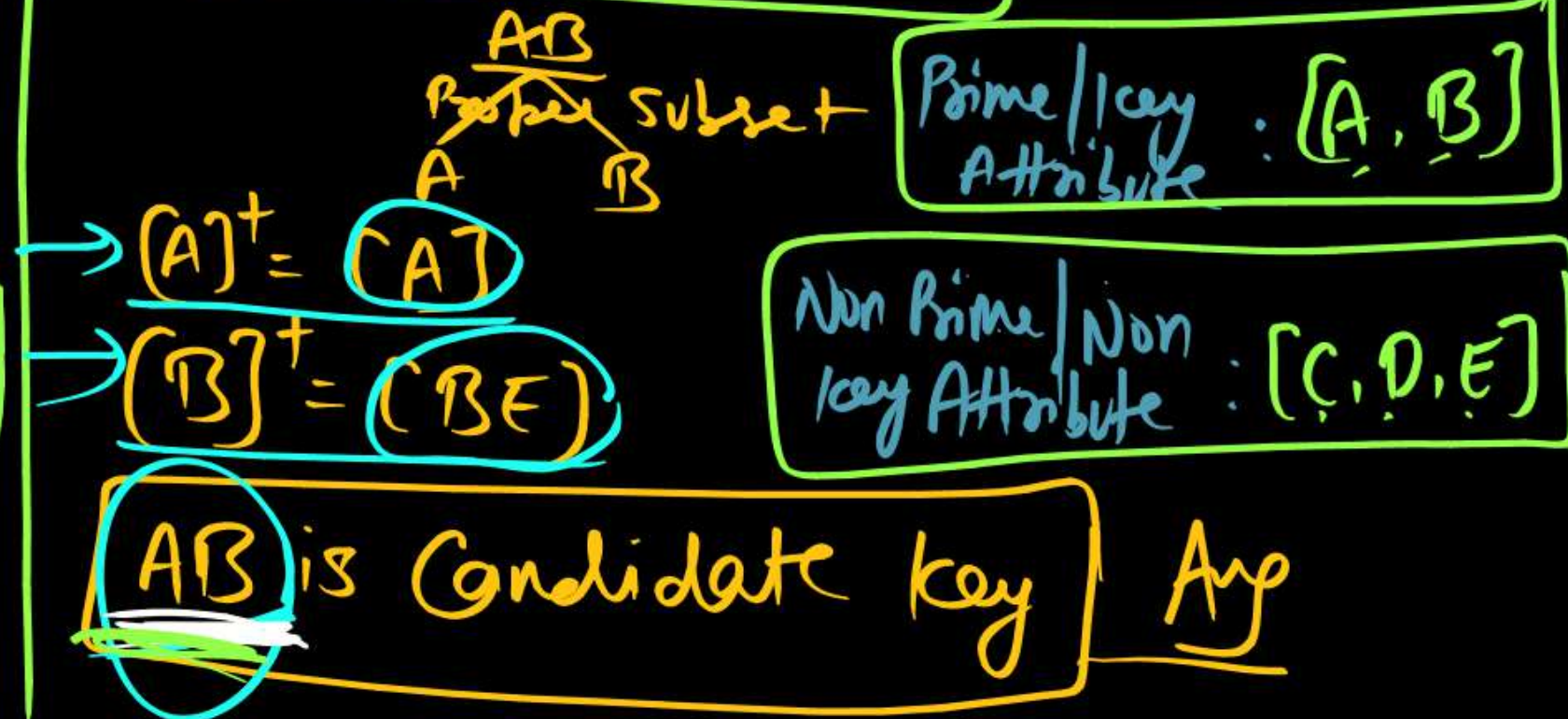
AB is Super key



$R(AB CDE) \{AB \rightarrow C, C \rightarrow D, \underline{B \rightarrow E}\}$

(Solⁿ) $(AB)^+ = (AB CDE)$

AB is Super key





Prime Attribute / Key Attribute :

Attribute that belongs (Present)
in any Candidate Key

Non Prime / Non Key Attribute :

Attribute that Not belongs (Not Present)
in any Candidate Key

R(A(B)CDE)

B is C.K

Subkey

Any Super Set of B is Super key

B A

B C

B D

= 16 Super key

R(AB(CDE))

[AB is Candidate key]

Subkey : (AB)

Any Super Set of AB is Super key

AB

AB C

$2^3 = 8$ Super key

Key Concept

Super Key

minimal

Candidate Key

Lets Assume
4 C.K

1 Select as

Primary Key (1)

Remaining Candidate key
except Primary key

Secondary / Alternative key
(3)

Note

Every key is a Super Key

Minimal of Super key

Candidate key

eg

AB is Candidate key

A
X

B
X

Finding Multiple Candidate key

first find any One Candidate key

then that Attribute (Present in c.k) is Prime/Key Attribute.

If $X_{\text{Attribute}} \rightarrow [\text{Prime/Key Attribute}]$

then Multiple Candidate keys are there.

D

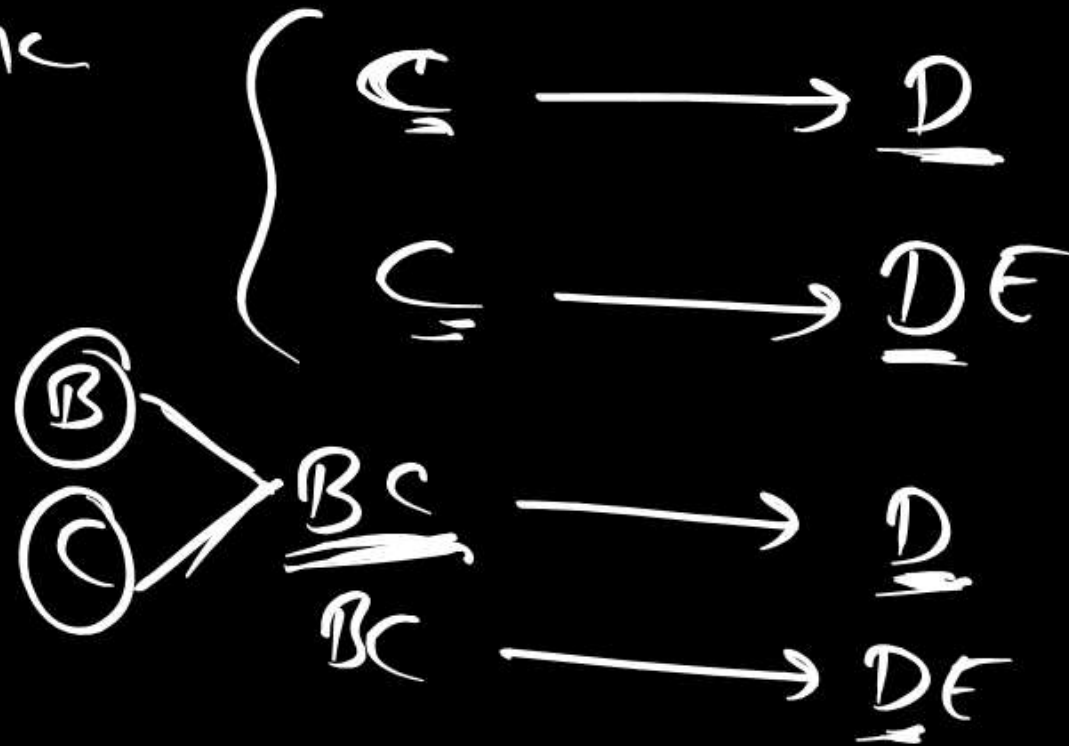
$(D)^+ = [\dots]$

Let Assume D is Candidate Key

$X_{\text{Attribute}} \longrightarrow (\text{Prime Attribute})$

Prime/Key Attribute = $[D]$

C is C.K



Q.8

R(ABCDE) {AB \rightarrow C, C \rightarrow D, D \rightarrow E, B \rightarrow A, C \rightarrow B}

Find candidate keys for the relation R?

Solⁿ

$$[AB]^+ = [ABCDE]$$

AB is Super key

$$[A]^+ = [A]$$

$$[B]^+ = [BACDE]$$

B is Candidate key - (1)

Prime key Attribute = [B, C]

If ~~X~~ Attribute \rightarrow [Prime Attribute]

$$C \rightarrow B$$

$$[C]^+ = [CBADE]$$

C is Candidate key - (2)

~~AB~~

2CK [B, C] Ans

Q.9



$R(ABCDEF) \{ \underline{A} \rightarrow BCDE, BC \rightarrow \underline{AD}, D \rightarrow EF \}$

Find candidate keys for the relation R?

(Solⁿ)

$$[A]^+ = [ABCDEF]$$

Prime Attribute = $\{\check{A}, \check{B}, \check{C}\}$

A is Candidate key — ①

If X Attribute \rightarrow [Prime Attribute]

$$BC \rightarrow \underline{AD}$$

$$[BC]^+ = [BCADEFF]$$

$$[B]^+ = [B]$$

$$[C]^+ = [C]$$

BC is Candidate key — ②

2 Candidate key

A, BC

Q.10

Consider the following relational schema $R(ABCDEF)$ with functional dependency $\{AB \rightarrow C, C \rightarrow D, D \rightarrow E, E \rightarrow F, F \rightarrow B\}$
The number of candidate keys for relation R ?



Q.11

$R(ABCDE) \{A \rightarrow BC, CD \rightarrow E, B \rightarrow D, E \rightarrow A\}$

Find candidate keys for the relation R ?

Q.12

$R(ABCDEFGH)$

$\{AB \rightarrow CD, D \rightarrow EG, F \rightarrow H, C \rightarrow EF, H \rightarrow A, G \rightarrow B, A \rightarrow B\}$

Find candidate keys for the relation R ?

Q.13

Consider a relation scheme $R = (A, B, C, D, E, H)$ on which of the following functional dependencies hold:

$\{A \rightarrow B, BC \rightarrow D, E \rightarrow C, D \rightarrow A\}$

[GATE 2M]

What are the candidate keys of R ?

A

AE, BE

B

AE, BE, DE

C

AEH, BEH, BCH

D

AEH, BEH, DEH

Q.14

Consider a relation R with five attributes V, W, X, Y, and Z. The following functional dependencies hold : $VY \rightarrow W$, $WX \rightarrow Z$, and $ZY \rightarrow V$. Which of the following is a candidate key for R?



[CATE 2M]

A

VXZ

B

VXY

C

VWXY

D

VWXYZ

Q.15

Relation R has eight attributes ABCDEFGH. Fields of R contain only atomic values.



$F = \{CH \rightarrow G, A \rightarrow BC, B \rightarrow CFH, E \rightarrow A, F \rightarrow EG\}$ is a set of functional dependencies (FDs) so that F is exactly the set of FDs that hold for R.

How many candidate keys does the relation R have?

[GATE 2013: 2 marks]

A

3

B

4

C

5

D

6

Q.16

Which of the following is NOT a superkey in a relational schema with attributes V, W, X, Y, Z and primary key VY?



[GATE]

- A VXYZ
- B VWXZ
- C VWXY
- D VWXYZ

Q.17

A prime attribute of a relation scheme R is an attribute that appears



[GATE]

- ☐ A In all candidate keys of R.
- ☐ B In some candidate key of R.
- ☐ C In a foreign key of R.
- ☐ D Only in the primary key of R.

RDBMS Concept

FD & its type

Keys Concept (Superkey, Candidate key, P.K, A.K/S.K)

Finding Multiple Candidate Key



**THANK
YOU!**

