

# CS & IT ENGINEERING

## Database Management System

Lecture No.- 01

By- Vijay Agarwal Sir



# Recap of Previous Lecture



Topic

Topic

# Topics to be Covered



Topic

Functional Dependencies

Topic

Key Concept

Topic

Minimal Cover

Topic

Properties of Decomposition

#Q. Consider the following relation:

A	B	C	TUPLE#
10	b1	c1	1
10	b2	c2	2
11	b4	c1	3
12	b3	c4	4
13	b1	c1	5
14	b3	c4	6

$B \rightarrow C$  May Hold

Given the previous extension (state), which of the following dependencies may hold in the above relation? If the dependency cannot hold, explain why by specifying the tuples that cause the violation.

- i.  $A \rightarrow B$ ,
- ii.  $B \rightarrow C$ ,
- iii.  $C \rightarrow B$ .
- iv.  $B \rightarrow A$ ,
- v.  $C \rightarrow A$

What we can conclude:

A does not functionally determine B.

$A \not\rightarrow B$

C " " " " " B.

$C \not\rightarrow B$

B " " " " " A.

$B \not\rightarrow A$

C " " " " " A.

$C \not\rightarrow A$

$A \rightarrow A \checkmark$

$AB \rightarrow A \checkmark$

$B \rightarrow B \checkmark$

$AB \rightarrow B \checkmark$

$C \rightarrow C \checkmark$

$AB \rightarrow AB \checkmark$

# Common Data Question for Q1 & Q2



Consider the relation shown in Figure

1. List all the functional dependencies that this relation instance satisfies.

$$\begin{array}{l} \checkmark x \rightarrow y \\ x \rightarrow z \\ x \rightarrow yz \end{array}$$

$$\begin{array}{l} y \rightarrow x \\ y \rightarrow z \\ y \rightarrow xy \\ \cancel{z \rightarrow x} \\ \cancel{z \rightarrow y} \\ \cancel{xz \rightarrow y} \end{array}$$

X	Y	Z
x <sub>1</sub>	y <sub>1</sub>	z <sub>1</sub>
x <sub>1</sub>	y <sub>1</sub>	z <sub>2</sub>
x <sub>2</sub>	y <sub>1</sub>	z <sub>1</sub>
x <sub>2</sub>	y <sub>1</sub>	z <sub>3</sub>

$$\boxed{\begin{array}{l} x \rightarrow y \\ z \rightarrow y \\ xz \rightarrow y \end{array}} \quad \text{Ans}$$

# Common Data Question for Q1 & Q2



Consider the relation shown in Figure

2. Assume that the value of attribute Z of the last record in the relation is changed from  $z_3$  to  $z_2$ . Now list all the functional dependencies that this relation instance satisfies.

No Changes.

Ans (3)

$X \rightarrow Y$   
 $Z \rightarrow Y$   
 $XZ \rightarrow Y$

Ans

X	Y	Z
$x_1$	$y_1$	$z_1$
$x_1$	$y_1$	$z_2$
$x_2$	$y_1$	$z_1$
$x_2$	$y_1$	<del><math>z_3</math></del> <u><math>z_2</math></u>

#Q. Consider the following set F of functional dependencies on the relation schema  $r(A, B, C, D, E, F)$ :

$$A \rightarrow BCD$$

$$BC \rightarrow DE$$

$$B \rightarrow D$$

$$D \rightarrow A$$

$$[B]^+ = \{BDACE\}$$

a. Compute  $B^+$ .

b. Prove that AF is a super key.

$$[AF]^+ = \overline{\{ABCDF\}}$$

AF is Super key.

#Q. Which is true about functional dependency?

- I. If FD  $A \rightarrow B$ ,  $B \rightarrow C$  holds on  $R(A, B, C)$  we can infer the FD  $A \rightarrow C$  holds on  $R$ .  $(A)^+ = (ABC)^\leq$

- II. If FD  $\alpha \rightarrow \beta$  is a trivial only if  $\beta$  is a subset of  $\alpha$ .

$$\alpha \supseteq \beta.$$

A

I

B

II

C

I and II

Ans(C)

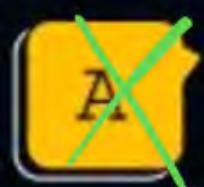
D

None of these

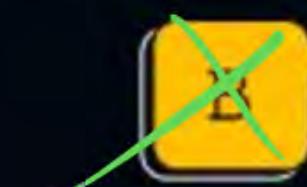
#Q. Consider relation R(A, B, C, D, E) with functional dependencies

$$AB \rightarrow C, C \rightarrow D, BD \rightarrow E$$

Which of the following sets of attributes does not functionally determine E?



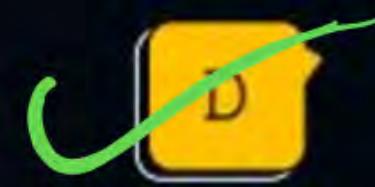
BC



AB



ABC



AD

$$(AD)^+ = [AD]$$

$$\begin{aligned}(BC)^+ &= [BCDE] \\ (AB)^+ &= [ACDE]\end{aligned}$$

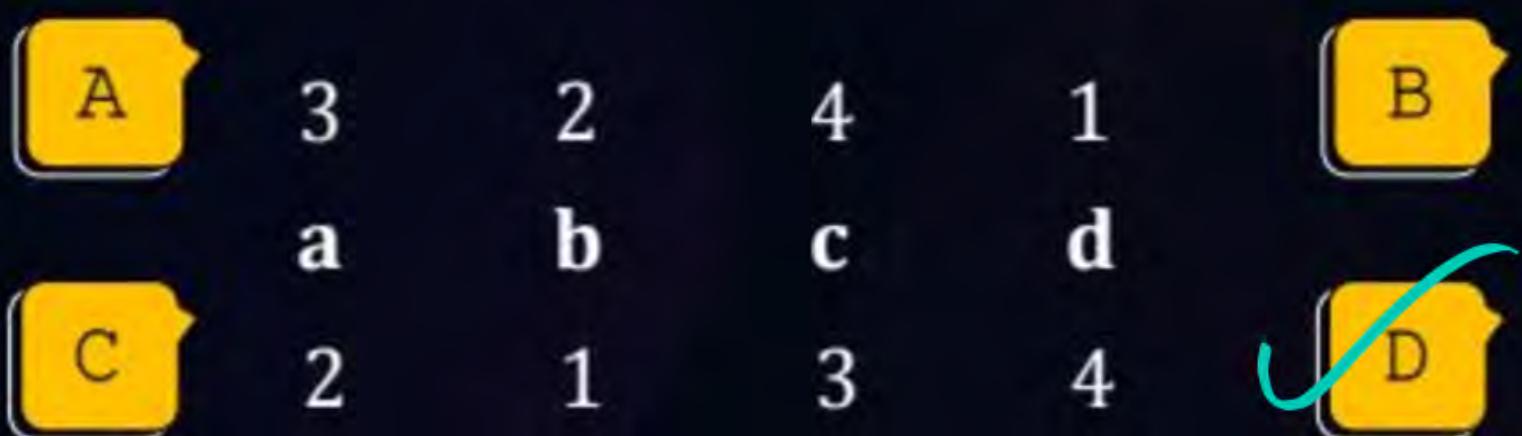
Ans (D)

#Q. Armstrong (1974) proposed systematic approach to derive functional dependencies. Match the following with respect to functional dependencies.

List-I		List-II	
a.	Decomposition rule - 4	1.	If $X \rightarrow Y$ and $Z \rightarrow W$ then $\{X, Z\} \rightarrow \{Y, W\}$
b.	Union rule - 3	2.	If $X \rightarrow Y$ and $\{Y, W\} \rightarrow Z$ then $\{X, W\} \rightarrow Z$
c.	Composition rule - 1	3.	If $X \rightarrow Y$ and $X \rightarrow Z$ then $X \rightarrow \{Y, Z\}$
d.	Pseudo transitivity rule - 2	4.	If $X \rightarrow \{Y, Z\}$ then $X \rightarrow Y$ and $X \rightarrow Z$

a	b	c	d
3	2	4	1

a	b	c	d
1	3	4	2



Ans (D)

Decomposition

$x \rightarrow yz$  then  $x \rightarrow y$  &  $x \rightarrow z$

Union

$x \rightarrow y, x \rightarrow z$  then  $x \rightarrow yz$

#Q. Consider a relation schema  $R(A, B, C, D, E)$  and following table is an instance of relation  $R$ .  $F$  is set of functional dependencies hold on  $R$ .

S1: B does not functionally determine D. **True**

S2: B functionally determine C and D not functionally determine E.

S3: C functionally determine E. : **May or May Not**

S4: C does not functionally determine D. **True**

The Number of statements definitely always true (or we conclude)   ?

A	B	C	D	E
$a_1$	1	5	$d_2$	3
$a_2$	2	6	$d_3$	4
$a_3$	2	6	$d_4$	4
$a_4$	3	7	$d_5$	5
$a_5$	3	7	$d_6$	5

**Ans (2)**

Relational Instance : set of Records (Relation State).

Relation (extension)

By watching the Instances we  
conclude:

✓ ① Trivial FD's are Valid.

$$\begin{array}{ll} A \rightarrow A & BC \rightarrow C \\ B \rightarrow B & BD \rightarrow D \\ AB \rightarrow B & BD \rightarrow BD \end{array}$$

✓ ② Rule out the FD Based on the Extension (instance)

## RDBMS

arity / Degree

Cardinality

Domain

Relation Schema

Relational Instance: set of Record (Snapshot)

RDBMS



Relation Extension

Relation State

Schema → Table Abstraction

↳ STUDENT (Roll : integer , Name : String , CGPA ; integer)

Relation Instance : Set of Records

#Q. Let a relation R(A, B, C, D, E) contain the following  
FDs:  $A \rightarrow B$ ,  $BC \rightarrow E$ ,  $E \rightarrow D$ ,  $D \rightarrow B$   
then which of the following dependencies is member of the relation R.

- |  |                   |                |   |                   |                       |
|--|-------------------|----------------|---|-------------------|-----------------------|
|  A | $D \rightarrow C$ | $(D)^+ = (DB)$ |  B  | $E \rightarrow B$ | $(E)^+ = (EDR \dots)$ |
|  C | $A \rightarrow E$ | $(A)^+ = (AB)$ |  D | $B \rightarrow E$ | $(B)^+ = (B)$         |

**Ans(B)**

#Q. If a functional dependency is reflexive, B is a subset of A and A is the set of attributes, then

A

$B \rightarrow A$  holds

B

$A \rightarrow B$  holds

C

$AB \rightarrow C$  holds

D

None of the mentioned

$A \rightarrow B : A \supseteq B$  ( $B$  is subset of  $A$ )

$A \supseteq B$ .

#Q. Let relation  $R(A, B, C, D, E, F, G, H)$  satisfy the following functional dependencies

$$A \rightarrow B, \underline{CH} \rightarrow A, B \rightarrow E, BD \rightarrow C, EG \rightarrow H, DE \rightarrow F$$

Which of the following FDs is also guaranteed to be satisfied by R?



$$ACG \rightarrow \underline{DH}$$



$$CGH \rightarrow BF$$

$$(CGH)^+ = (CGHABE)$$



$$BFG \rightarrow \underline{AE}$$



$$BDG \rightarrow AE$$

$$(ACG)^+ = (ACGBEH)$$

$$(BFG)^+ = (BFGEH)$$

**Ans (D)**

$$(BDG)^+ = (BDGEGHCA)$$

#Q. Consider the relation R(A, B, C) with the following set of functional dependencies

$$F = \{A \rightarrow B, B \rightarrow C\}$$

Where  $F^+$  is closure of F, the total number of functional dependencies in  $F^+$  is

$$\phi \rightarrow \phi$$

$$(A)^+ = [ABC] \Rightarrow 2^3 = 8$$

$$(B)^+ = [BC] = 2^2 = 4$$

$$(C)^+ = [C] = 2^1 = 2$$

$$(AB)^+ = [ABC] = 2^3 = 8$$

$$(BC)^+ = [BC] = 2^2 = 4$$

$$(AC)^+ = [AC] = 2^3 = 8$$

$$A \rightarrow \phi, A \rightarrow A, A \rightarrow B, A \rightarrow C, A \rightarrow AB, A \rightarrow BC, A \rightarrow AC$$

$$C \rightarrow \phi, C \rightarrow C$$

$$(ABC)^+ = [ABC] = 8$$

Ans(43)

#Q. R {X, Y, Z, W} having FD's  $\{X \rightarrow Y; Y \rightarrow Z; Z \rightarrow W; W \rightarrow X\}$  so number of candidate keys

A

1

C

3

B

2

D

4

$$(X)^+ = \{XYZW\}$$

X is C.K

If  $X_{\text{Attribute}} \rightarrow (\text{Prime Attribute})$

$$W \rightarrow X$$

W is CK

$$Z \rightarrow W$$

Z is CK

$$Y \rightarrow Z$$

Y is CK

Ans(D)

#Q. If a relation R(A, B, C, D, E) holds the following dependencies:

$AB \rightarrow C, C \rightarrow D, D \rightarrow E, E \rightarrow A, D \rightarrow B.$

Then how many candidate keys can be made out of it \_\_\_\_\_.

A

2

C

1

$(A)^+ = [A]$

3

$P_A = [A, B, E]$

B

4

$(AB)^+ = [ABCDE]$

$(B)^+ = [B]$

$(AB)$  is CK. -①

E

5

$E \rightarrow A$

$(EB)^+ = [ABCDE]$

$(E)^+ = [EA]$

6

$EB$  is CK -②

B

3

D

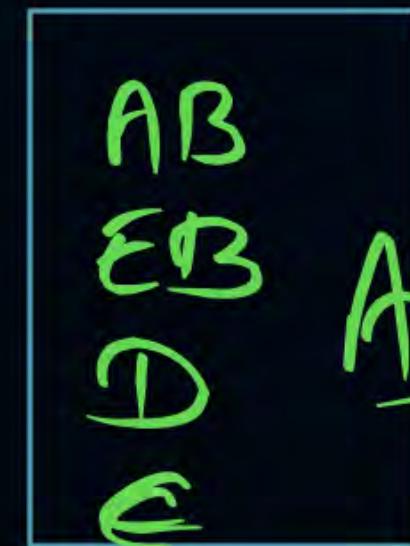
4

$D \rightarrow B$

$(D)^+ = [DBEAC]$

D is CK. -③

$C \rightarrow D$   
C is CK



Ans

#Q. A relation schema  $R = (A, B, C, D, E)$

$A \rightarrow BC$

$CD \rightarrow E$

$B \rightarrow D$

$E \rightarrow A$

The candidate keys are

A

A, CD, B, E

B

A, BC, CD and E

C

A, B, E

D

A, BC, CD

#Q. Let R (A, B, C, D, E, F) be a relational schema in which the following dependencies are known to hold.

$$A \rightarrow BC$$

$$E \rightarrow AF$$

Which of the following is a candidate key of R?



DE



AE



DEA



AF

$$(E)^+ = [E \underline{A} F \underline{B} \underline{C}]$$

$$(ED)^+ = [A \underline{B} \underline{C} D \underline{E} \underline{F}]$$

- #Q. Consider the universal relation  $R = \{A, B, C, D, E, F, G, H, I, J\}$  and the set of functional dependencies  $F = \{\{A, B\} \rightarrow \{C\}, \{A\} \rightarrow \{D, E\}, \{B\} \rightarrow \{F\}, \{F\} \rightarrow \{G, H\}, \{D\} \rightarrow \{I, J\}\}$ . What is the key for R? Decompose R into 2NF and then 3NF relations.

$(AB)^+ = \{ABC, DEFGHIJ\}$

$(A)^+ = \{ADEIJ\}$

$(B)^+ = \{BFGH\}$

AB is C.K. Ans

#Q. Compute the closure of the following set F of functional dependencies for relation schema R(A, B, C, D, E).

$$A \rightarrow BC$$

$$CD \rightarrow E$$

$$B \rightarrow D$$

$$E \rightarrow A$$

List the candidate keys for R.

4 CK

A, E, CD, CB.

[NAT]

$$P.A = \{A, \bar{B}, \bar{E}, \bar{G}, F, C\}$$

P  
W

Consider the following relation  $R(ABCDEFGHI)$  and the functional dependencies set  $F$

$$F: [AB \rightarrow CDHI, AF \rightarrow D, DE \rightarrow F, C \rightarrow G, F \rightarrow E, G \rightarrow A]$$

The number of candidate keys is relation  $R$  is 6. Ans

ABE
GBE
ABF
GBF
CBF
CBE

Ans

$$(ABE) = (ABCDEFIGHD)$$

ABE is CK - ①

G → A  
GBE is CK - ②

F → E  
ABF  
GBF

ARDE ABE ✓  
GBDE GBE ✓

C → G  
CBF

CBDE X

[NAT]

P  
W

A relation R(A<sub>1</sub>, A<sub>2</sub>, A<sub>3</sub>, ..., A<sub>11</sub>) and maximum number of candidate key possible is 462. Ans

n: # of Attributes.

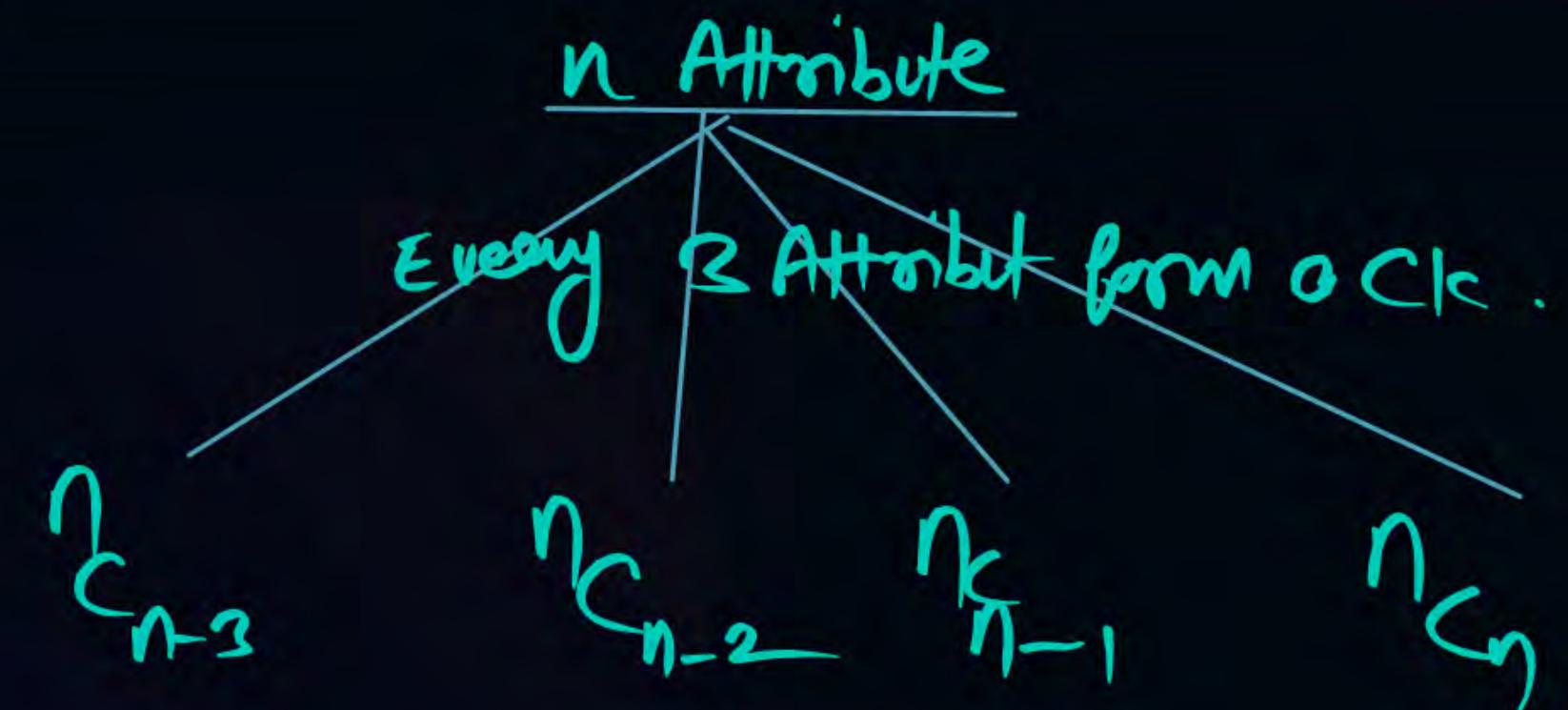
Soln

$$\text{Maximum Number of CK} = {}^nC_{\left[\frac{n}{2}\right]} \Rightarrow {}^{11}C_{\left[\frac{11}{2}\right]} \Rightarrow {}^{11}C_5$$

Ans (462)

$$\begin{aligned} & \Rightarrow \frac{11 \times 10 \times 9 \times 8 \times 7 \times 6!}{5 \times 4 \times 3 \times 2 \times 1 \times 6!} \\ &= 33 \times 14 \\ &= 462 \text{ Ans} \end{aligned}$$

Consider a Relation schema R with A, B, C, D, E, and F attributes R(ABCDEF). If in a relation R every '3' attribute form a candidate keys the total number of super keys are \_\_\_\_.



Max # CK  
 $6_C_3 = 20$

6 Attribute

Every 2 Attribute CK.

$$6C_3 + 6C_4 + 6C_5 + 6C_6.$$

$$20 + 15 + 6 + 1$$

= 42 Subkey Ans

$n$ : is # Attributes

$$\underline{\text{Max } \# SK} = {}^n_C_2$$

$$\underline{\text{Total Maximum } \# SK} = 2^n - 1$$

Consider a relation R(A, B, C, D, E) with the set of functional dependencies:

$$\{A \rightarrow BC, B \rightarrow D, CD \rightarrow E, E \rightarrow A\}$$

Then the number of super keys possible are \_\_\_\_\_

$$\begin{aligned} & (C) \\ & (B) \\ & (D) \\ & (BD) = (BD) \end{aligned}$$

4 C.K :

A, E, CD, CB

C  
B  
D  
BD

Not a key.

Total Maximum Number of Super keys =  $2^5 - 1 \Rightarrow 2^5 - 1 = 31$  Super key

31 Super key

Total Super key =  $31 - 4 = 27$  Super key

A, E, CD, CB

$$\cancel{A} B C D E = 2^4 = 16$$

$$\cancel{E} B C D = 2^3 = 8$$

$$\cancel{C} D B = 2^1 = 2$$

$$\cancel{C} \underline{B} = 1$$

(27)

**H.W**

#Q. Consider

 $F = \{A \rightarrow BC, B \rightarrow A, C \rightarrow A\}$  The set of FD's $G = \{A \rightarrow B, B \rightarrow C, C \rightarrow A\}$  The set of FD's

Then which of the following is true?

A

F covers G

B

G cover F

C

F and G are equivalent

D

None of the above

**H.W**

#Q. Consider the following three relation schemas

$R_1 (A, B, C, D)$  with FD's:  $A \rightarrow B$ ,  $B \rightarrow C$ ,  $AC \rightarrow D$

$R_2 (A, B, C, D)$  With FD's:  $A \rightarrow B$ ,  $B \rightarrow C$ ,  $A \rightarrow D$

$R_3 (A, B, C, D)$  With FD's:  $A \rightarrow B$ ,  $B \rightarrow C$ ,  $C \rightarrow D$

Which of the following options is correct with respect to above three schemas?

A

$R_1$  and  $R_2$  are functionally equivalent

B

$R_1$  and  $R_3$  are functionally equivalent

C

$R_2$  and  $R_3$  are functionally equivalent

D

All  $R_1$ ,  $R_2$  and  $R_3$  are functionally equivalent

**H.W**

#Q. Which of the following is equivalent minimal cover for relation R(A, B, C, D, E, F) with FD's:  $AB \rightarrow C$ ;  $B \rightarrow CD$ ;  $D \rightarrow EF$ ;  $B \rightarrow F$

- A       $B \rightarrow C$   
 $AB \rightarrow C$   
 $D \rightarrow E$   
 $B \rightarrow F$

- B       $B \rightarrow C$   
 $B \rightarrow D$   
 $D \rightarrow F$   
 $B \rightarrow F$

- C       $B \rightarrow C$   
 $B \rightarrow D$   
 $D \rightarrow E$   
 $D \rightarrow F$

- D       $AB \rightarrow C$   
 $B \rightarrow CD$   
 $D \rightarrow E$   
 $D \rightarrow B$

**H.W**

Consider the following set of FD's F

F:{A→B, ABCD→E, EE→G, EF→H, ACDF→EG}

Which of the following is a minimal cover for the above given FD set?

- A A→B , ACD→E, EE→H, ADF→G
- B A→B , EF→G, EF→H, ADF→G
- C A→B , ACD→E, EF→G, EF→H
- D A→B , AD→E, EF→H, ADF→G

H.W

#Q. Suppose that we decompose the schema  $r(A, B, C, D, E)$  into

$r_1(A, B, C)$

$r_2(A, D, E)$

Show that this decomposition is a lossless decomposition if the following set F of functional dependencies holds:

$A \rightarrow BC$

$CD \rightarrow E$

$B \rightarrow D$

$E \rightarrow A$

H.W

#Q. Consider a schema  $R(A, B, C, D)$  and following functional dependencies.

$$A \rightarrow B$$

$$B \rightarrow C$$

$$D \rightarrow B$$

Then decomposition of  $R$  into  $R_1(A, B)$ ,  $R_2(B, C)$  and  $R_3(B, D)$  is

A

dependency preserving and lossless join

B

lossless join but not dependency preserving

C

dependency preserving but not lossless join

D

not dependency preserving and not lossless join



## 2 mins Summary



Topic

DBMS 01 : DBMS (Part-01)

Topic



THANK - YOU

# CS & IT ENGINEERING

## Database Management System

Lecture No.- 02

By- Vijay Agarwal Sir



# Recap of Previous Lecture



Topic

Functional Dependencies

Topic

Key Concept

# Topics to be Covered



Topic

Equalities between FD sets

Topic

Minimal Cover

Topic

Properties of Decomposition

Topic

Normal Form & NF Decomposition

#Q. Consider

$F = \{A \rightarrow BC, B \rightarrow A, C \rightarrow A\}$  The set of FD's

$G = \{A \rightarrow B, B \rightarrow C, C \rightarrow A\}$  The set of FD's

Then which of the following is true?

A F covers G

B G cover F

C F and G are equivalent

D None of the above

F Cover G

$$\checkmark A \rightarrow B \quad (A)^+ = CABC$$

$$\checkmark B \rightarrow C \quad (B)^+ = CBAC$$

$$\hookrightarrow C \rightarrow A \quad (C)^+ = CA$$

True

G Cover F

$\checkmark A \rightarrow BC \quad (A)^+ = CABC$

$\checkmark B \rightarrow A \quad (B)^+ = BCA$

$C \rightarrow A \quad (C)^+ = CA$

True

#Q. Consider the following three relation schemas

$R_1 (A, B, C, D)$  with FD's:  $A \rightarrow B$ ,  $B \rightarrow C$ ,  $AC \rightarrow D$

$R_2 (A, B, C, D)$  With FD's:  $A \rightarrow B$ ,  $B \rightarrow C$ ,  $A \rightarrow D$

$R_3 (A, B, C, D)$  With FD's:  $A \rightarrow B$ ,  $B \rightarrow C$ ,  $C \rightarrow D$

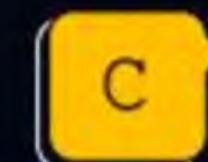
Which of the following options is correct with respect to above three schemas?



A R<sub>1</sub> and R<sub>2</sub> are functionally equivalent



B R<sub>1</sub> and R<sub>3</sub> are functionally equivalent



C R<sub>2</sub> and R<sub>3</sub> are functionally equivalent



D All R<sub>1</sub>, R<sub>2</sub> and R<sub>3</sub> are functionally equivalent

$R_1(ABCD) [A \rightarrow B, B \rightarrow C, AC \rightarrow D]$

$\checkmark A \rightarrow B$

$\checkmark B \rightarrow C$

$\checkmark AC \rightarrow D \quad (A)^+ = (ABC \underline{CD})$

$R_1 = R_2$

$R_2(ABCD) \left[ \checkmark A \rightarrow B, \checkmark B \rightarrow C, A \rightarrow D \right]$

$A \rightarrow B \quad \checkmark$

$B \rightarrow C \quad \checkmark$

$AC \rightarrow D \quad \checkmark (AC)^+ = (ABC \underline{CD})$

True.

(R1)  $\frac{R_1(ABCD) [A \rightarrow B, B \rightarrow C, C \rightarrow D]}{(A)^+ = (ABC \underline{CD})}$

$A \rightarrow B$

$\cancel{B \rightarrow C}$

$\checkmark C \rightarrow D \quad (C)^+ = (ABC \underline{D}) \quad \times C \rightarrow D \quad (C)^+ = (C)$

$\checkmark A \rightarrow B$

$\checkmark B \rightarrow C$

#Q. Which of the following is equivalent minimal cover for relation R(A, B, C, D, E, F) with FD's:  $AB \rightarrow C$ ;  $B \rightarrow CD$ ;  $D \rightarrow EF$ ;  $B \rightarrow F$

- A       $B \rightarrow C$   
 $AB \rightarrow C$   
 $D \rightarrow E$   
 $B \rightarrow F$

- B       $B \rightarrow C$   
 $B \rightarrow D$   
 $D \rightarrow F$   
 $B \rightarrow F$

- C       $B \rightarrow C$   
 $B \rightarrow D$   
 $D \rightarrow E$   
 $D \rightarrow F$

- D       $AB \rightarrow C$   
 $B \rightarrow CD$   
 $D \rightarrow E$   
 $D \rightarrow B$

$$AB \rightarrow C \quad B \rightarrow CD \quad D \rightarrow EF \quad B \rightarrow F$$

Step 1  $AB \rightarrow C, B \rightarrow C, B \rightarrow D, D \rightarrow E, D \rightarrow F, B \rightarrow F$

Step 2  $AB \rightarrow C \quad (A)^t = [A] \quad B \text{ is Not extg}$   
 $(B)^t = [BCDEF] \quad A \text{ is Not extg}$

Step 3 ~~①  $AB \rightarrow C$~~  ~~②  $B \rightarrow C$~~  ~~③  $B \rightarrow D$~~  ~~④  $D \rightarrow E$~~  ~~⑤  $D \rightarrow F$~~  ~~⑥  $B \rightarrow F$~~   
 $(AB)^t = [ABCDEF]$   $(B)^t = [BCDEF]$   $(B)^t = [BCF]$   $(D)^t = [DF]$   $(D)^t = [DE]$   $(B)^t = [BCDEF]$

$B \rightarrow C, B \rightarrow D, D \rightarrow E, D \rightarrow F$

## [MCQ]

Consider the following set of FD's F

F:{ $A \rightarrow B$ ,  $ABCD \rightarrow E$ ,  $EE \rightarrow G$ ,  $EF \rightarrow H$ ,  $ACDF \rightarrow EG$ }

Which of the following is a minimal cover for the above given FD set?

A  $A \rightarrow B$ ,  $ACD \rightarrow E$ ,  $EE \rightarrow H$ ,  $ADF \rightarrow G$

B  $A \rightarrow B$ ,  $EF \rightarrow G$ ,  $EF \rightarrow H$ ,  $ADF \rightarrow G$

C  $A \rightarrow B$ ,  $ACD \rightarrow E$ ,  $EF \rightarrow G$ ,  $EF \rightarrow H$

D  $A \rightarrow B$ ,  $AD \rightarrow E$ ,  $EF \rightarrow H$ ,  $ADF \rightarrow G$

Ans [C]

#Q. Suppose that we decompose the schema  $r(A, B, C, D, E)$  into

$$r_1(A, B, C)$$

$$r_2(A, D, E)$$

Show that this decomposition is a lossless decomposition if the following set F of functional dependencies holds:

$$A \rightarrow BC$$

$$CD \rightarrow E$$

$$B \rightarrow D$$

$$E \rightarrow A$$

$$\delta_1(A \rightarrow BC) \wedge R_2(A \rightarrow DE) \stackrel{F}{\Rightarrow} r_1(A, B, C) \cup r_2(A, D, E)$$

CHASE TEST

A	B	C	D	E
ABC	a	a	a	
ADE	a	a	a	a

lossless

#Q. Consider a schema  $R(A, B, C, D)$  and following functional dependencies.

$$A \rightarrow B \quad B \rightarrow C$$

$$C \rightarrow D \quad D \rightarrow B$$

Then decomposition of  $R$  into  $R_1 (A, B)$ ,  $R_2 (B, C)$  and  $R_3 (B, D)$  is

- A dependency preserving and lossless join Ans (A)
- B lossless join but not dependency preserving
- C dependency preserving but not lossless join
- D not dependency preserving and not lossless join

$R(ABCD)$  ( $A \rightarrow B$ ,  $B \rightarrow C$ ,  $C \rightarrow D$ ,  $D \rightarrow B$ )

$R_1(AB)$   $R_2(BC)$   $R_3(BD)$

Lossless?

$R_1(AB) \cap R_2(BC) = B \Rightarrow (R)^+ = (BC) \subseteq R_2$

$R_{12}(ABC) \cap R_3(BD) = B \Rightarrow (R)^+ = (BCD) \subseteq R_3$

$R_{123}(ABCD)$  Lossless Join

$R(ABCD) \quad [A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow B]$

$R_1(AB)$	$R_2(BC)$	$R_3(BD)$
$A \rightarrow B$	$B \rightarrow C$ $C \rightarrow B$	$B \rightarrow D$ $D \rightarrow B$

$$(C)^+ = (CDB)$$

$$C \rightarrow B \wedge B \rightarrow D \Rightarrow C \rightarrow D.$$

#Q. If  $D_1, D_2, \dots, D_n$  are domains in a relational model, then the relation is a table, which is a subset of

$$R \subseteq D_1 \times D_2 \times D_3 \times \dots \times D_n$$

- A  $D_1 \oplus D_2 \oplus \dots \oplus D_n$
- B  $\underbrace{D_1 \times D_2 \times \dots \times D_n}$
- C  $D_1 \cup D_2 \cup \dots \cup D_n$
- D  $D_1 \cap D_2 \cap \dots \cap D_n$

#Q. Which one is correct with respect to RDBMS?

A

Primary key  $\subseteq$  super key  $\subseteq$  candidate key

B

Primary key  $\subseteq$  candidate key  $\subseteq$  super key

C

Super key  $\subseteq$  candidate key  $\subseteq$  primary key

D

Super key  $\subseteq$  primary key  $\subseteq$  candidate key

#Q. The maximum number of super keys for the relation schema R(A, B, C, D) with AB and CD as Keys is



7



16



8



None of these

AB, CD

$$\# \text{Super key} = 2^{4-2} + 2^{4-2} - 2^{4-4}$$

$$\Rightarrow 2^2 + 2^2 - 2^0$$

$$= 4 + 4 - 1 \Rightarrow \textcircled{7} \text{ Ans}$$

AB, CD

AB

A B C D

A B,

A B C

A B D

A B C D

C D

C D A

C D B



= 7 Ans

## [MCQ]



#Q. Which of Primary keys following can be options called is as correct?

- S<sub>1</sub>: Primary keys can be called as minimal super key · True
- S<sub>2</sub>: Candidate keys can store null values
- S<sub>3</sub>: Primary keys can store null values
- S<sub>4</sub>: An attribute of an entity can be composite

A

S<sub>1</sub> and S<sub>3</sub> are true

C

S<sub>2</sub> and S<sub>3</sub> are true

B

S<sub>1</sub> and S<sub>4</sub> are true

D

S<sub>1</sub>, S<sub>2</sub> and S<sub>4</sub> are true

P.T  
Select  
C.k is Minimal of Superkey

#Q. If R is a relation in relational data Model and A<sub>1</sub>, A<sub>2</sub>, ... A<sub>n</sub> are the attributes of relation R, what is the cardinality of R expressed in terms of domain of attributes?



A  $|R| \leq |\text{dom}(A_1) \times \text{dom}(A_2) \dots \times \text{dom}(A_n)|$



B  $|R| \geq |\text{dom}(A_1) \times \text{dom}(A_2) \dots \times \text{dom}(A_n)|$



C  $|R| = \max(|\text{dom}(A_1)|, |\text{dom}(A_2)| \dots |\text{dom}(A_n)|)$



D  $|R| = \min(|\text{dom}(A_1)|, |\text{dom}(A_2)| \dots |\text{dom}(A_n)|)$

# [MCQ]

Consider the relation  $R(ABCDEFGHIJKLM)$  with the following functional dependencies set:

$$\{A \rightarrow E, A \rightarrow BCD, EFG \rightarrow H, F \rightarrow GH, I \rightarrow J, K \rightarrow LM\}$$

The number of redundant FD is 1 Ans

$$\begin{array}{ll}
 \checkmark A \rightarrow E & (A)^t = (ABCD) \\
 \checkmark A \rightarrow B & (A)^t = (ACECD) \\
 \checkmark A \rightarrow C & (A)^t = (AECD) \\
 A \rightarrow D & (A)^t = (AEBC) \\
 \text{circled } EFG \rightarrow H & (EFG)^t = (EFGH) \\
 \checkmark F \rightarrow G & \\
 \checkmark F \rightarrow H & (F)^t \subseteq CFG \\
 \checkmark I \rightarrow J & \\
 \checkmark K \rightarrow L & \\
 \checkmark K \rightarrow M &
 \end{array}$$

$$EFG \rightarrow H$$

#Q. Consider the following relation with given functional dependencies.

$A(R, S, T, U, V)$

FD's:  $\{RS \rightarrow T, RS \rightarrow U, U \rightarrow R, ST \rightarrow U, ST \rightarrow V\}$

What is the highest normal form of relation A?

key/prime attribute =  $[R, S, U, T]$

A

1 NF

Candidate key:  $[SR, SU, ST]$

B

2 NF

Check 2NF ?  $R$  is 2NF

C

3 NF

Check 3NF  $\checkmark R$  is in 3NF

$U \rightarrow R$ ;  $U$  is Not Subkey  
BUT  
 $R$  is Key/Prime Attribut

D

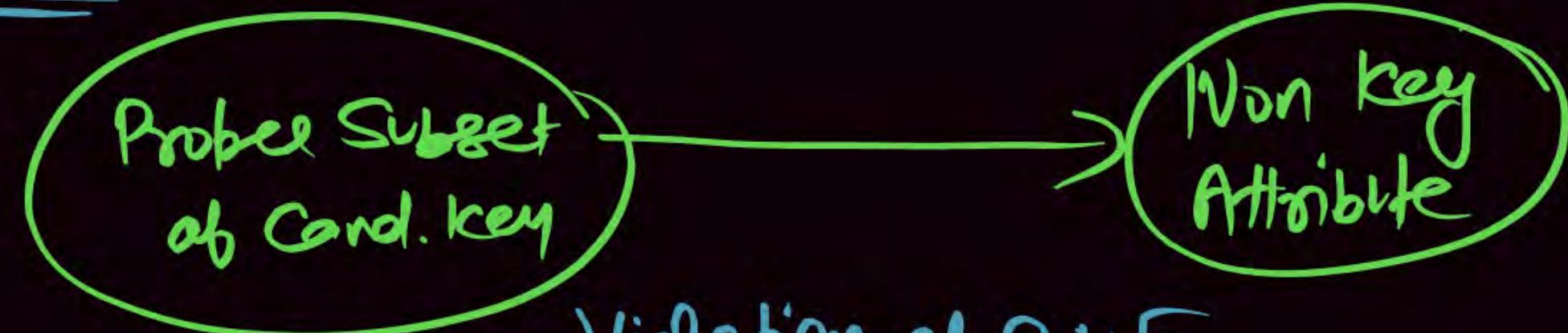
BCNF

Check BCNF

$U \rightarrow R$ ;  $U$  is Not Subkey  
Not in BCNF.

## Checking Condition

2NF :



Violation of 2NF

3NF:  $X \rightarrow y$ ;  $X$ : Super key

$y$ : key | Prime Attribute

BCNF

$X \rightarrow Y$      $X$ : Super key.

Home work

#Q. Consider a relational Schema R (A, B, C, D, E, F, G, H, I, J) with following FD's set F:  $[AB \rightarrow C, BD \rightarrow EF, AD \rightarrow GH, A \rightarrow I, H \rightarrow J]$

If a relation R is decomposed into Lossless Join and Dependency Preserving 2NF decomposition, then minimum number of table required in this Decomposition is \_\_\_\_.

Candidate key = ABD

Not

If Relation R has Only 1 CK then R always is  
in 1NF But may or may not be in 2NF, 3NF, BCNF.

(Q)

R(ABCDE) [AB → C, C → D, B → E]

Candidate key - (AB)

B → E  
Violation of 2NF } Not in 2NF.

Note If every Candidate key is a Simple Candidate key  
(No Composite key) then R is in 2NF But May @  
May Not in 3NF & BCNF.

Q R(AABCDE) [A  $\rightarrow$  B, B  $\rightarrow$  C, C  $\rightarrow$  D, D  $\rightarrow$  E, C  $\rightarrow$  A]

Candidate key = [A, C, B]

R is in 2NF

But

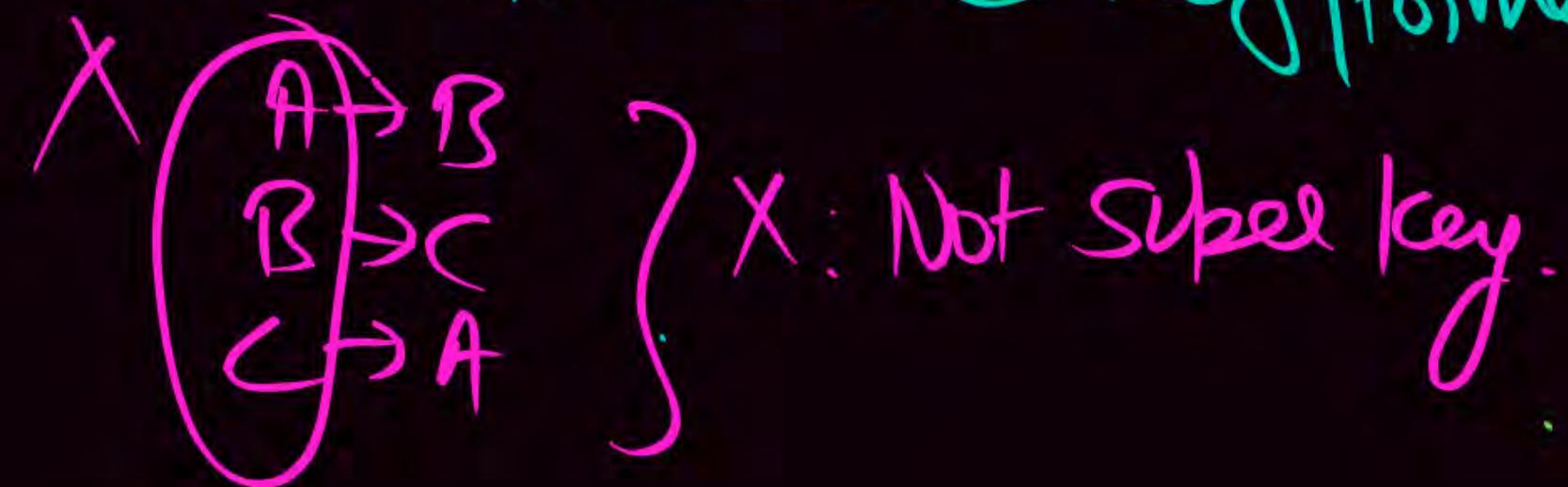
$D \rightarrow E$  [D is Not Subkey]  
Violate 3NF {E is Non Prime Attribute}

(Note) If all attribute are Prime / Key Attribute then R is in 3NF But May ~~or~~ May Not in BCNF

$R(ABCD)$  ( $A \rightarrow B$ ,  $B \rightarrow C$ ,  $C \rightarrow A$ )

$$C.K = (AD, BD, CD)$$

All Attribute are Key / Prime So R is in 3NF



Note If R is in 3NF & every C.K is simple (K then R is in BCNF

$R(ABC)$  ( $A \rightarrow B$ ,  $B \rightarrow C$ ,  $C \rightarrow A$ )

CK :  $(A, B, C)$

$R$  is in BCNF.

Consider a relation schema  $R(ABCDE)$  with the functional dependencies F.

F: [  $A \rightarrow BE$ ,  $A \rightarrow D$ ,  $A \rightarrow C$ ,  $B \rightarrow D$  ]

We decompose the relation R into two relation schemes  $\underline{R_1(ABCE)}$  &  $\underline{R_2(BD)}$ .

$$(A)^t = (ABED)$$

$$(B)^t = (B \rightarrow D)$$

ABCE	BD
$A \rightarrow BE$ $A \rightarrow C$ $A \rightarrow B$	$B \rightarrow D$

$$\underline{\underline{A \rightarrow D}}$$

Decomposition is in 3NF

Lossless Join Decomposition

Dependency Not preserving decomposition

Decomposition is in BCNF.

$R(ABCDE)$  [  $A \rightarrow BE$ ,  $A \rightarrow D$ ,  $A \rightarrow C$ ,  $R \rightarrow D$  ]

$R_1(ABCE) \cap R_2(BD) = (B)$

$(B)^+ = (BD)$  super key of  $R_2$  lossless Join

### CHASE TEST

	$A$	$B$	$C$	$D$	$E$	
$R_1(ABCE)$	a	a	a	a	a	
$R_2(BD)$		a		a		
						Lossless

#Q. Suppose you are given a relation R with four attributes ABCD. For the set of FDs assuming those are the only dependencies that hold for R, do the following

$$(C)^+ = [CDA] \quad R \text{ is } 3\text{NF}$$

$$\underline{C \rightarrow D, C \rightarrow A, B \rightarrow C} \quad (BCDA)$$

Suppose, the relation is decomposed into 3 relations  $R_1, R_2, R_3$ . Which of the following is true about decomposition?

A Lossless, dependency preserving, BCNF

B Lossless, not dependency preserving, BCNF

C Not lossless, dependency preserving, 3NF

D Not lossless, not dependency preserving, 3NF

$R_1$	$R_2$	$R_3$
$A$	$B$	$C \rightarrow D$

Standard Book

#Q. Show that the following decomposition of the schema R is not a lossless decomposition:

 $(A, B, C)$  $(C, D, E)$ 

Hint: Give an example of a relation r on schema R such that

$$\Pi_{A, B, C}(r) \bowtie \Pi_{C, D, E}(r) \neq r$$

Lossy

A	B	C	D	E
$A_1$	$B_1$	$C_1$	$d_1$	$e_1$
$A_2$	$B_2$	$C_1$	$d_2$	$e_2$

H.W

#Q. Consider a relation R(P Q R S T U) with set of FD's : {PQ → R, QR → P, PR → Q, Q → S, R → T}

If the relation R is decomposed into Lossless and Dependency Preserving BCNF decomposing, then the minimum number of relation required in this decomposition?

A

1

B

2

C

3

D

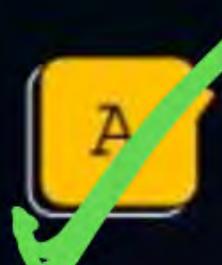
None of these

#Q. Consider the following

S<sub>1</sub>: Foreign key allows null values.

S<sub>2</sub>: Every binary tables is in BCNF.

Which of the following is true?



A Both S<sub>1</sub> and S<sub>2</sub> are true



B S<sub>1</sub> is true



C S<sub>2</sub> is true



D None of these

Ans(A)

#Q. Which of the following is not a condition for  $X \rightarrow Y$  in Boyce code normal form?

- A  $X \rightarrow Y$  is trivial
- B  $X$  is the super-key for the relational schema R
- C  $Y$  is the super-key for the relational schema R
- D All of the mentioned

Ans(C).

**BCNF**

①  $X \rightarrow Y$   
 $X$ : Super key

③ Binary Relation BCNF.

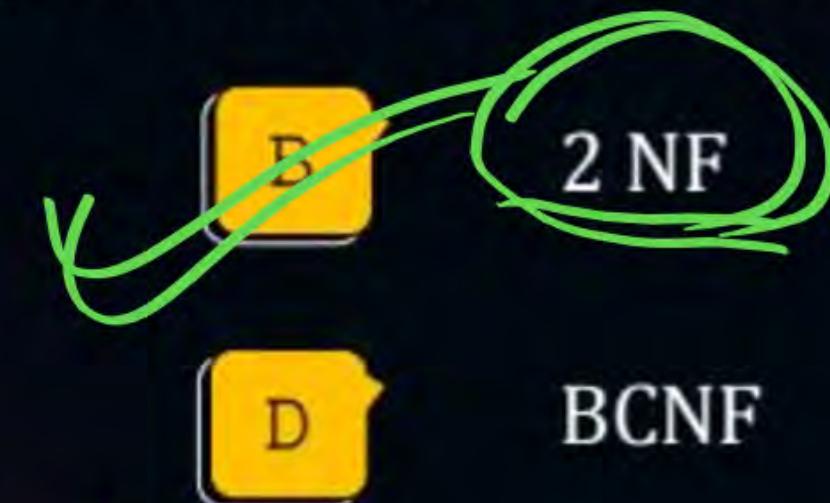
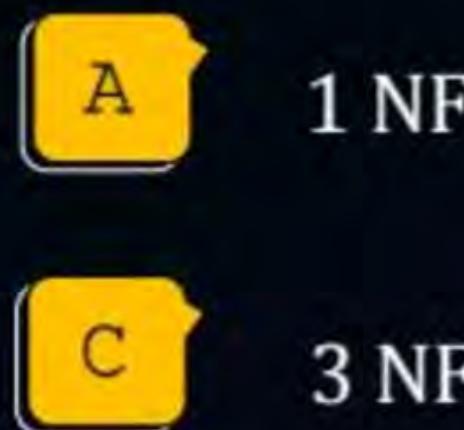
③  $X \rightarrow Y$  Trivial  
 $X \supseteq Y$   ~~$AB \rightarrow A$~~

#Q. Consider the schema together with the functional dependency  $(A \rightarrow B, DE \rightarrow F, B \rightarrow C)$ .

The highest normal form of the above relation is

- |                                       |      |                                |                            |      |
|---------------------------------------|------|--------------------------------|----------------------------|------|
| <input checked="" type="checkbox"/> A | 1 NF | C.R : ADE                      | <input type="checkbox"/> B | 2 NF |
| <input type="checkbox"/> C            | 3 NF | $\underbrace{A \rightarrow B}$ | <input type="checkbox"/> D | BCNF |
- Violation of 2NF*

#Q. Let  $R(ABCDE)$  be a relational schema and  $f = \{AB \rightarrow CD, ABC \rightarrow E, C \rightarrow E\}$  be the set of functional dependencies, what is the highest normal form of  $R$ ?



$$(AB)^+ = (ABCDE)$$

$AB$  is Candidate key.

Non key Attribute =  $\{C, D, E\}$

	2 NF	3 NF	BCNF
$AB \rightarrow CD$	✓	✓	✓
$ABC \rightarrow E$	✓	✓	✗
$C \rightarrow E$	✓	✗	✗

Home Work

Consider a relation R with four Attributes A.B.C & D with the following FD's.

FD-I  $C \rightarrow D$ ,  $C \rightarrow A$ ,  $B \rightarrow C$

FD-II  $ABC \rightarrow D$ ,  $D \rightarrow A$

FD-III  $A \rightarrow B$ ,  $BC \rightarrow D$ ,  $A \rightarrow C$

FD-IV  $AB \rightarrow C$ ,  $AB \rightarrow D$ ,  $C \rightarrow A$ ,  $D \rightarrow B$

How many above FD are satisfied the 3NF (Third Normal Form) for a relation schema R(ABCD) is \_ ?

#Q. Indicate which of the following statements are true:

A relation database which is in 3NF may still have undesirable data redundancy because there may exist

- A transitive functional dependencies.
- B non-trivial functional dependencies involving prime attributes on the right side.
- C non-trivial functional dependencies involving prime attributes only on the left side.
- D non-trivial functional dependencies involving only prime attributes.

Not Non key  $\rightarrow$  Prime Attribute  
Redundancy

3NF ✓

BCNF X

$R(ABCD)$  ( $AB \rightarrow CD$ ,  $D \rightarrow A$ )

C.K :  $(AB, DB)$

$D \rightarrow A$

3NF But Not  
in BCNF.

3NF

$x \rightarrow y$

$x$ : Super key ..

OR

$y$ : key | Prime  
Attribute

BCNF

$x \rightarrow y$

$x$ : Super key ..

Home Work

Consider a relational schema R(ABCDEFGHIJK) with the following FD's set F

$$F: [AB \rightarrow C, BD \rightarrow EF, AD \rightarrow GH, A \rightarrow I, H \rightarrow JK]$$

If a relation R is decomposed into lossless join & Dependency preserving 2NF & 3NF Decomposition. The minimum number of tables (Relation) required for 2NF decomposition R is 'A' and for 3NF decomposition of R is 'B' respectively then the value of  $2A + B$  is \_\_\_\_\_.

## Common Data for question

Suppose you are given relation

$R(X, Y, Z, W)$  with functional dependencies

$XY \rightarrow Z, ZW \rightarrow X$  and  $Y \rightarrow W$

Candidate key:

~~$(XW)^+ = (XW)$~~

$(XY)^+ - (XYZW)$

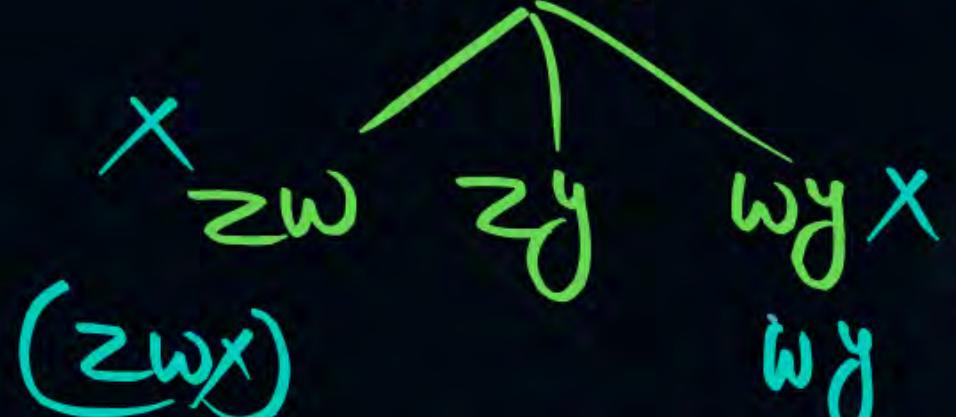
$(X)^+ = [X] \times$

$(Y)^+ = [YW] \times$  XY is ck  $\ominus \emptyset$

$$P.A = [X, Y]$$

$$ZW \rightarrow X$$

$$(ZWY) - [ZWXY]$$



$\checkmark (ZY)^+ - [ZYWX]$

#Q. How many keys (minimal) are there in R?

A 1

B 2

C 3

D 4

Xy, yz Ans

#Q. The highest normal form of R is

A 1 NF

$\text{Ans}(A)$

C 3 NF

B 2 NF

D BCNF

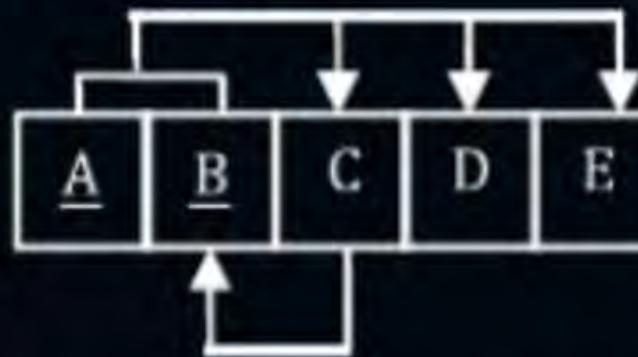
Non key Attribute = w

C.K = [xy, yz]

$R(XYZW)$   $[XY \rightarrow Z, ZW \rightarrow X, Y \rightarrow W]$   
CHECK 2NF ?

proper subset  $Y \rightarrow W$  } Non key Attribute  
 of CK } Not in 2NF

#Q. Consider the following table



The table is in which normal form?

- A First normal form
- B Second normal form
- C Third normal form but not BCNF
- D BCNF

$R(AB\text{CDE})$

$[AB \rightarrow CDE, C \rightarrow B]$

Candidate key =  $(AB, AC)$

Non key Attributk =  $(D, E)$

$AB \rightarrow CDE$       2NF ✓      3NF ✓      BCNF ✓

$C \rightarrow B$       2NF ✓      3NF ✓

Not in BCNF  
C is Not Subkey.

H.W.

Consider the following relational schema R(ABCDE) with functional dependencies:

{AB→C, D→E, E→A, D→B}

The number of additional relations are required to convert it into lossless join & Dependency Presenting 2NF & 3NF Decomposition is \_\_\_\_\_

M.W

#Q. Consider the following table Faculty (facName, dept, office, rank dateHired)

facName	dept	Office	rank	dateHired
Ravi	Art	A101	Professor	1975
Murali	Math	M201	Assistant	2000
Narayanan	Art	A101	Associate	1992
Lakshmi	Math	M201	Professor	1982
Mohan	CSC	C101	Professor	1980
Sreeni	Math	M203	Associate	1990
Tanuja	CSC	C101	Instructor	2001
Ganesh	CSC	C105	Associate	1995

Continue

(Assume that no faculty member within a single department has same name. Each faculty member has only one office identified in office). 3NF refers to third normal form and BCNF refers to Boyce-Codd normal form. Then faculty is

- A not in 3NF, in BCNF
- B in 3 NF, not in BCNF
- C in 3 NF, in BCNF
- D Not in 3 NF, not in BCNF

## Common Data for Question



Let  $R(A, B, C, D, E, F, G)$  be a relational schema with the following functional dependencies

$$AB \rightarrow CD, AF \rightarrow D, DE \rightarrow F, C \rightarrow G, F \rightarrow E, G \rightarrow A$$

## Common Data for Question



Let  $R(A, B, C, D, E, F, G)$  be a relational schema with the following functional dependencies

$AB \rightarrow CD, AF \rightarrow D, DE \rightarrow F, C \rightarrow G, F \rightarrow E, G \rightarrow A$

⑥ ck

H.w

#Q. How many candidate keys does the relation R have?

A 2

C 5

B 4  
 D 6

Let  $R(A, B, C, D, E, F, G)$  be a relational schema with the following functional dependencies

$AB \rightarrow CD, AF \rightarrow D, DE \rightarrow F, C \rightarrow G, F \rightarrow E, G \rightarrow A$

#Q. The highest normal form of above relation is

- A 3NF
- C 1NF

H.W

- B 2NF
- D BCNF

Let  $R(A, B, C, D, E, F, G)$  be a relational schema with the following functional dependencies

$AB \rightarrow CD, AF \rightarrow D, DE \rightarrow F, C \rightarrow G, F \rightarrow E, G \rightarrow A$

#Q. Consider a Relational schema R(A, B, C) with FD set:

$$AB \rightarrow C$$

$$C \rightarrow B$$

Which of the following statements is correct with respect to the question "R(A, B, C) can be decomposed into dependency preserving BCNF form"?

A

Probably YES

C

Not at all possible

B

Probably NO

D

Absolutely it is possible

#Q. Given the following two statements:

$(A \rightarrow B, B \rightarrow C, C \rightarrow A)$  Cr: A, B, C.

- S<sub>1</sub>: A relation where attributes do have cyclic dependencies within themselves will always be in BCNF. (& single attributes keys)
- S<sub>2</sub>: Only the dependency preservation property can differentiate between 3NF and BCNF

Which of the following is correct?

BCNF Definition

A S<sub>1</sub> is true and S<sub>2</sub> is false

B Both S<sub>1</sub> and S<sub>2</sub> are true

D Differentiate

C S<sub>1</sub> is false but S<sub>2</sub> is true

D Both S<sub>1</sub> and S<sub>2</sub> are false

Ans (A)

But

$R(ABCD)$   $\{A \rightarrow B, B \rightarrow C, C \rightarrow A\}$

$C_k : (AD, BD, CD)$

But Not in BCNF

#Q. Given the following two statements

S<sub>1</sub>: 2NF allows Nonprime to non-prime ( $NP \rightarrow NP$ ) dependencies but relocks prime to prime ( $prime \rightarrow prime$ ) dependencies

S<sub>2</sub>: If there is a dependency  $\alpha \rightarrow \beta$  and if only if  $\alpha$  is a super key then the relation is in BCNF.

Which of the following is correct?

A

S<sub>1</sub> is true and S<sub>2</sub> is false

B

S<sub>1</sub> is false and S<sub>2</sub> is true

C

Both are false

D

Both are true



## 2 mins Summary



Topic

DBMS 02 : DBMS (Part-02)

Topic



THANK - YOU

# CS & IT ENGINEERING

## Database Management System

Lecture No.- 03

By- Vijay Agarwal Sir



# Recap of Previous Lecture



Topic

Equalities between FD sets

Topic

Minimal Cover

Topic

Properties of Decomposition

Topic

Normal Form & NF Decomposition

# Topics to be Covered



Topic

Normal Form & NF Decomposition

Topic

Transaction Concept

Topic

Serializable & Recoverable Schedule

Topic

Lock Based Protocol

# COA

24 Nov.



Fast track  
You Tube

## ACID Property

A  
C  
I  
D

#Q. If the following information is found in log of stable storage while performing two transactions

1.  $\langle T_0, \text{START} \rangle$
2.  $\langle T_0 A, 900,890 \rangle$
3.  $\langle T_0, B, 500,510 \rangle$
4.  $\langle T_0, \text{COMMIT} \rangle$  ✓
5.  $\langle T_1, \text{STARTS} \rangle$
6.  $\langle T_0, C, 2000,1900 \rangle$
7.  $\langle T_1, \text{COMMIT} \rangle$

If the data base is crashed after instruction set 6, and sub-term is using "differed data base modification technique to retrieve the information back, then which options is correct with respect to recovery condition

**Commit** ⇒ successfully executed

Redo List

Not Commit ↳ Undo List

~~Check point~~

- A UNDO( $T_1$ )  
REDO ( $T_0$ )  
RESTART ( $T_1$ )
- B UNDO ( $T_1$ )  
UNDO( $T_0$ ) RESTART ( $T_1$ )
- C REDO ( $T_0$ )  
REDO ( $T_1$ )
- D Ans(A)
- None of the above

#Q. Assertion (a): The following schedule is conflict serializable schedule.

Reason (r): There is a cycle in this schedule.

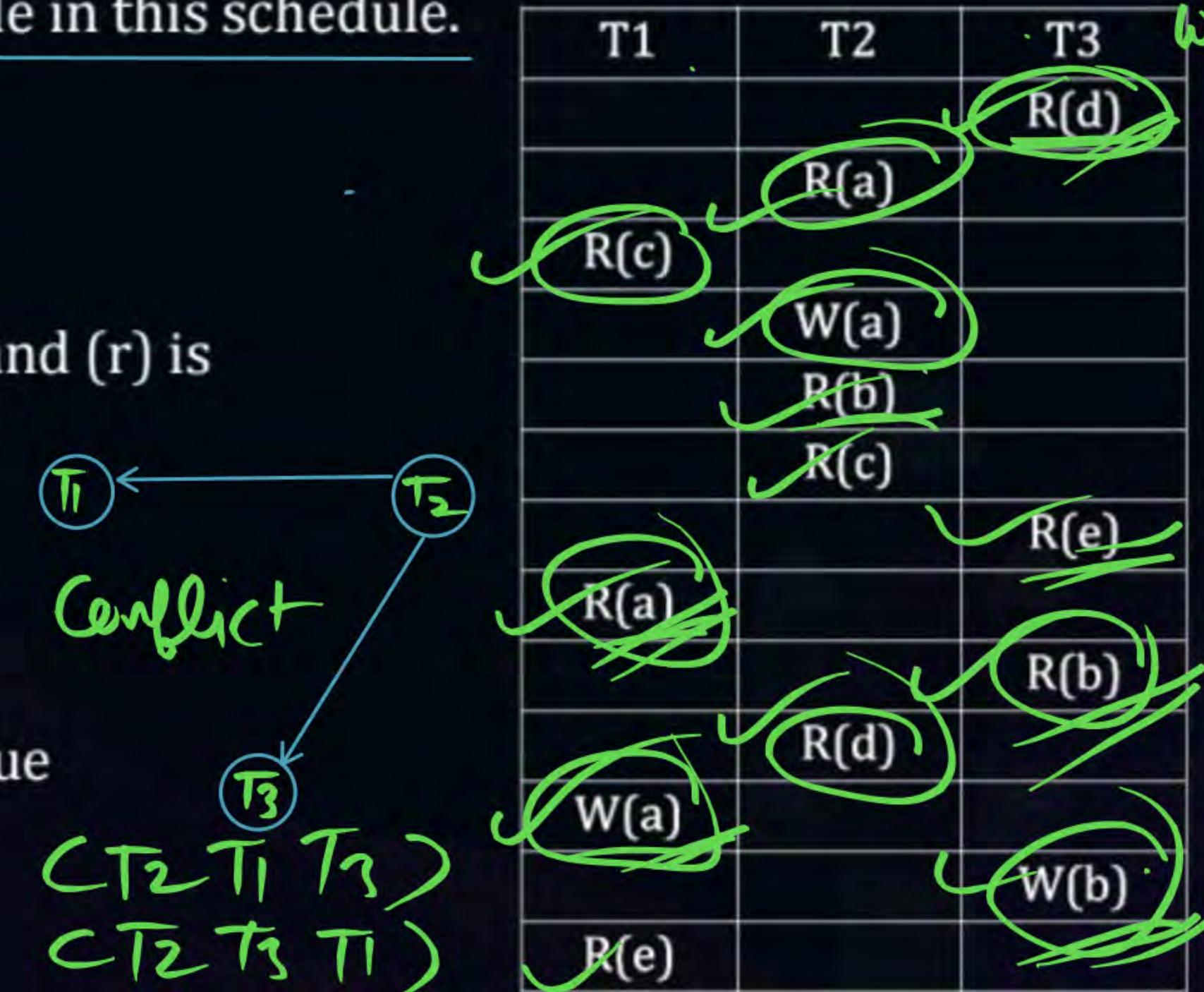
R-W  
W-R  
W-W

- A Both (a) and (r) are true and (r) is not correct reason for (a) T ← Conf

B Both (a) and (r) are false

C (a) is true but (r) is not true

D None of these



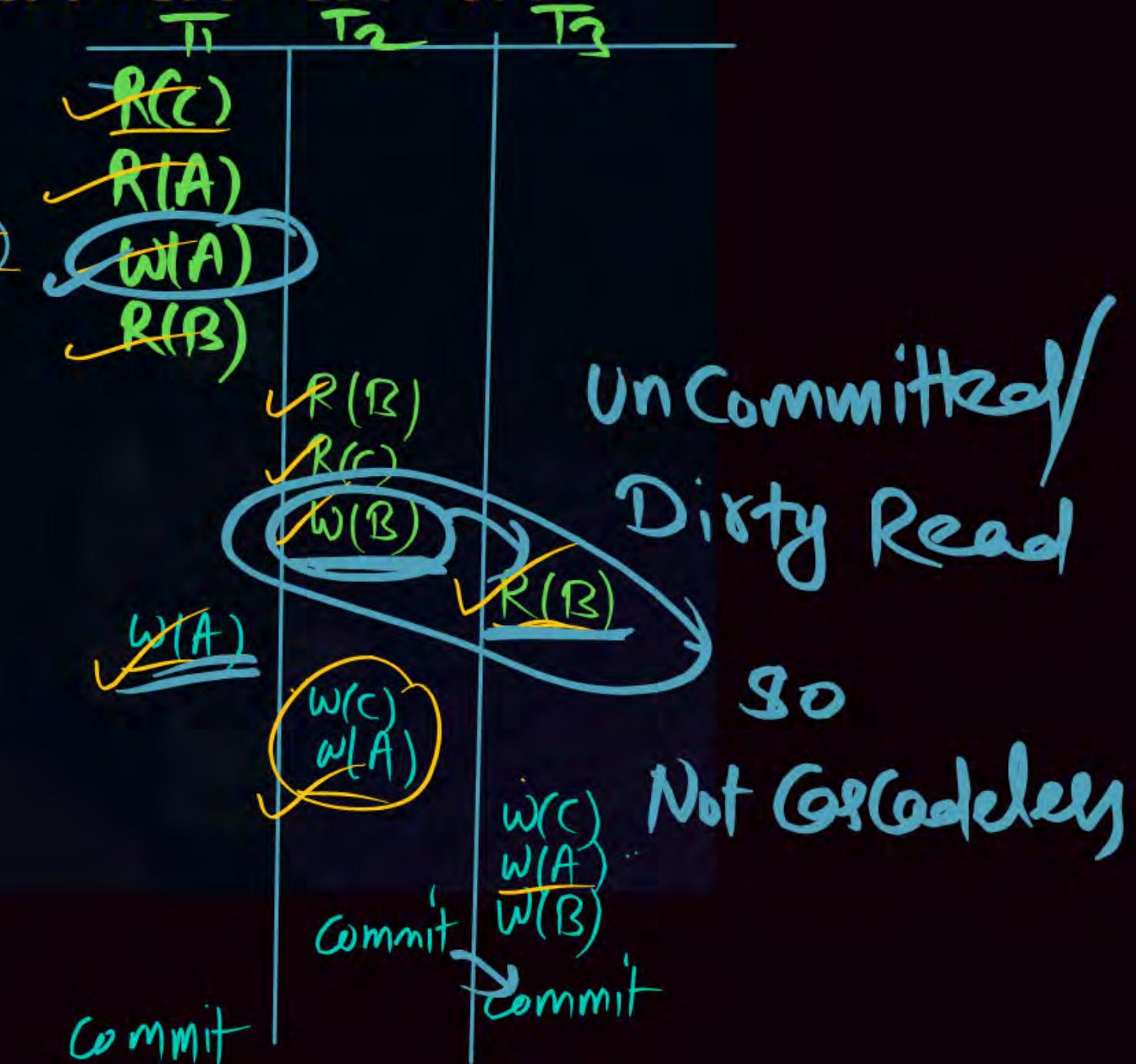
Consider the following schedules:

S:  $R_1(C) R_1(A) W_1(A) R_1(B) R_2(B) R_2(C) W_2(B) R_3(B) W_1(A) W_2(C) W_2(A) W_3(C)$   
 $W_3(A) W_3(B) C_2 C_3 C_1$ .

Which of the following is/are true about the schedule S?

- A Schedule is conflict serializable
- B Schedule is Not Recoverable
- C Schedule is not conflict serializable
- D Schedule is Recoverable but not cascadeless

**Ans (A) & (D)**



[MCQ]

#Q. A schedule

S: T<sub>2</sub>: Read A; T<sub>3</sub>: Read B; T<sub>2</sub>: Write A; T<sub>1</sub> Read A; T<sub>3</sub>: Write B

T<sub>2</sub>: Read B; T<sub>1</sub> Write A; T<sub>2</sub>: Read C; T<sub>2</sub>: Write C; T<sub>1</sub> Read C;

Is the above schedule is serializable if yes it is equivalent to which serial schedule.

A

T<sub>1</sub>: T<sub>2</sub>: T<sub>3</sub>

C

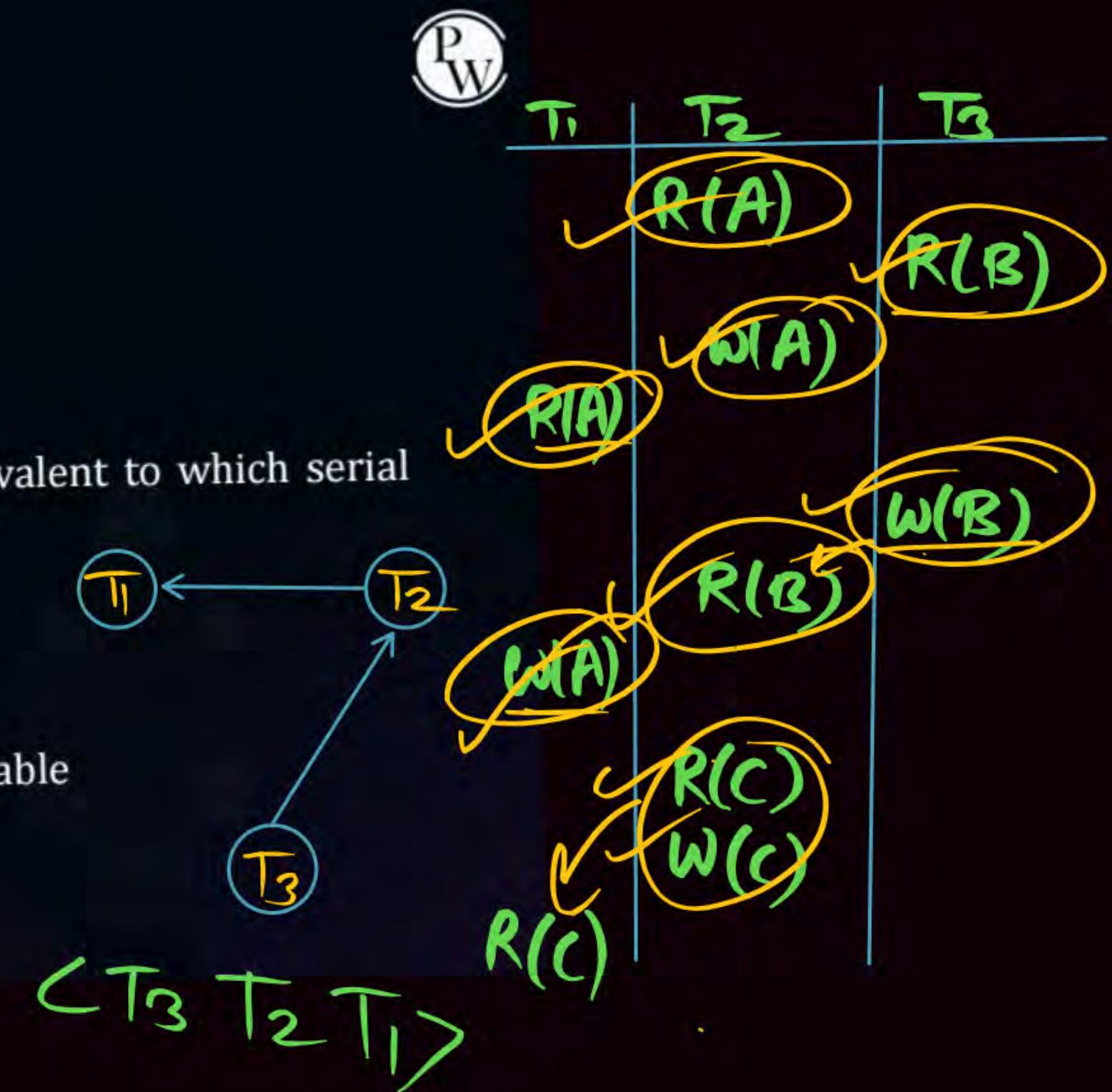
T<sub>2</sub>: T<sub>1</sub>: T<sub>3</sub>

B

~~T<sub>3</sub>: T<sub>2</sub>: T<sub>1</sub>~~

It is not serializable

Ans (D)



#Q. Consider the following two statements:

S<sub>1</sub>: A serial schedule with 'n' number of transactions can generate n.

different conflict serialization schedule. *Depends on the Read & Write operation on Data Item in*

S<sub>2</sub>: A concurrent schedule with 'n' number of transactions can generate a more than n serial schedule. *X Schedule*

Which of the following options are always correct?

*Concurrent = Serial + Non Serial .*

A

SI is true where S2 is false

B

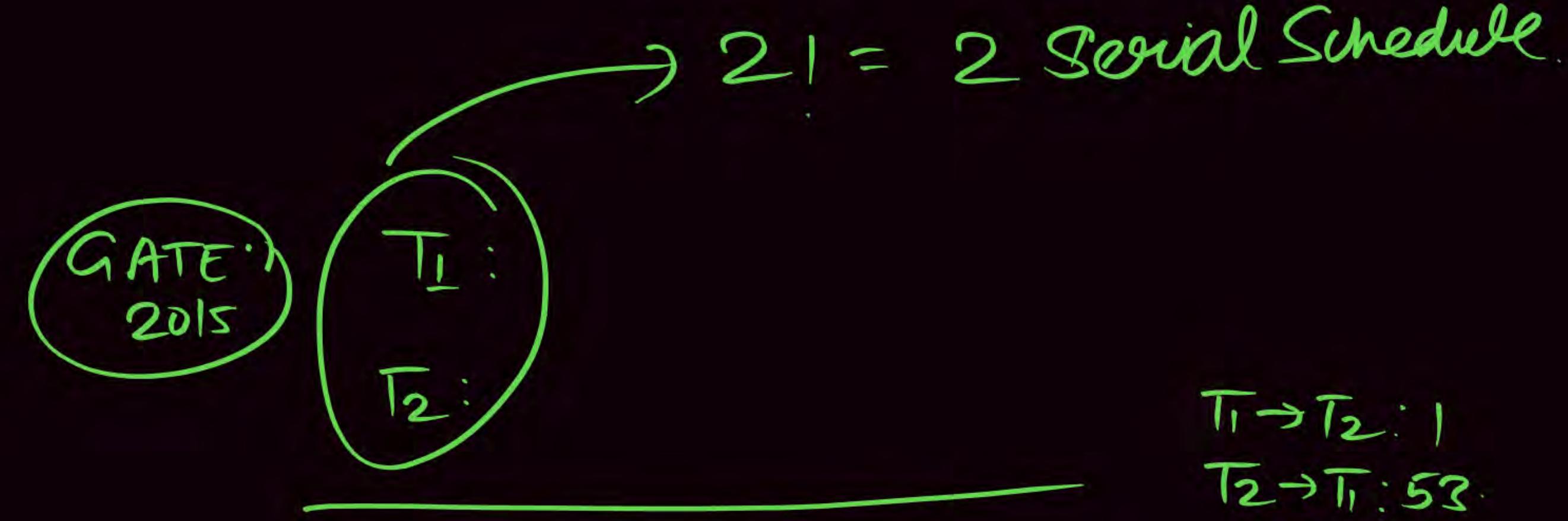
S2 is true where SI is false

C

Both the statements are true

D

Both the statements are false



Total Conflict Serializable = ~~(54)~~ Any

# [MCQ]



#Q. Consider the following transactions:

$T_1: R_1(x) \ W_1(x) \ R_1(y) \ W_1(y)$

$T_2: W_2(y) \ W_2(x)$

The number of non-serial schedules between  $T_1$  and  $T_2$  which are  
serializable?

A 2

C 15

Any(D)

B 13  
D None of these

O Any

$T_1: R_1(x) \quad W_1(x), \quad R_1(y), \quad W_1(y)$

$T_2: W_2(y) \quad W_2(x)$

$T_1: 4$

$T_2: 2$

$T_1 \rightarrow n_1$  operation

$T_2 \rightarrow n_2$  operation

Total #  
Concurrent  
schedule

$$= \frac{(n_1 + n_2)!}{(n_1)! (n_2)!} \Rightarrow \frac{(4+2)!}{(4!)(2!)}$$

$$\text{Serial Schedule} = \frac{2!}{2!} = \frac{2 \times 1}{2 \times 1} = 1$$

*2 Serial Schedule*

Concurrent = Serial Schedule + Non Serial Schedule

$$\text{Non Serial} = 15 - 1 = 14$$

$T_1: R_1(x) \ w_1(x), \ R_1(y), \ w_1(y)$

$T_2: w_2(y) \ w_2(x)$

Serial

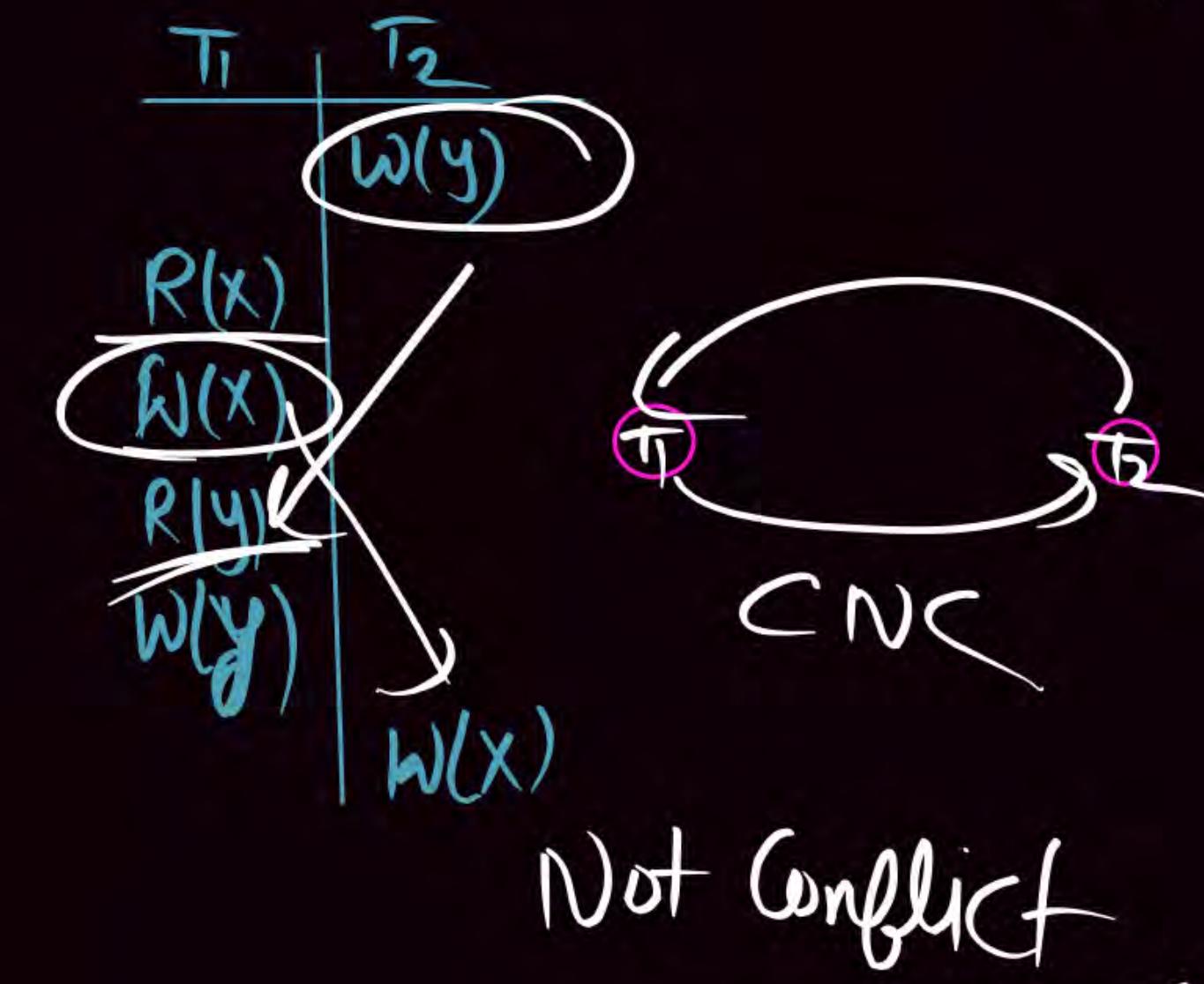
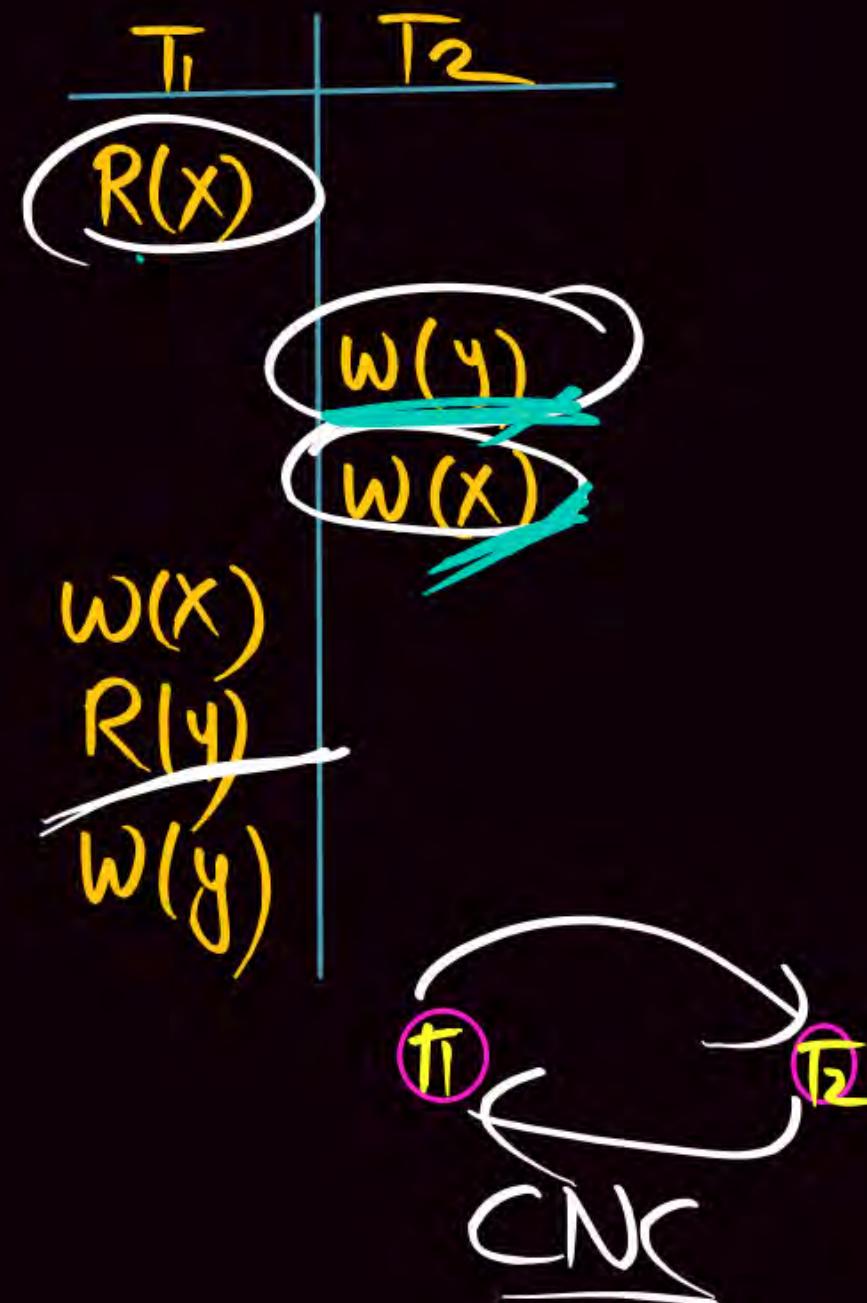
$T_1$	$T_2$
$R(x)$	
$w(x)$	
$R(y)$	
$w(y)$	
	$w(y)$
	$w(x)$
$(T_1, T_2)$	

$T_1$	$T_2$
	$w(y)$
	$w(x)$
$R(x)$	
$w(x)$	
$R(y)$	
$w(y)$	
	$(T_2, T_1)$

$T_1: R_1(x) \text{ } w_1(x), \text{ } R_1(y), \text{ } w_1(y)$  Non Serial  $\Rightarrow$  Serializable

$T_2: w_2(y) \text{ } w_2(x)$

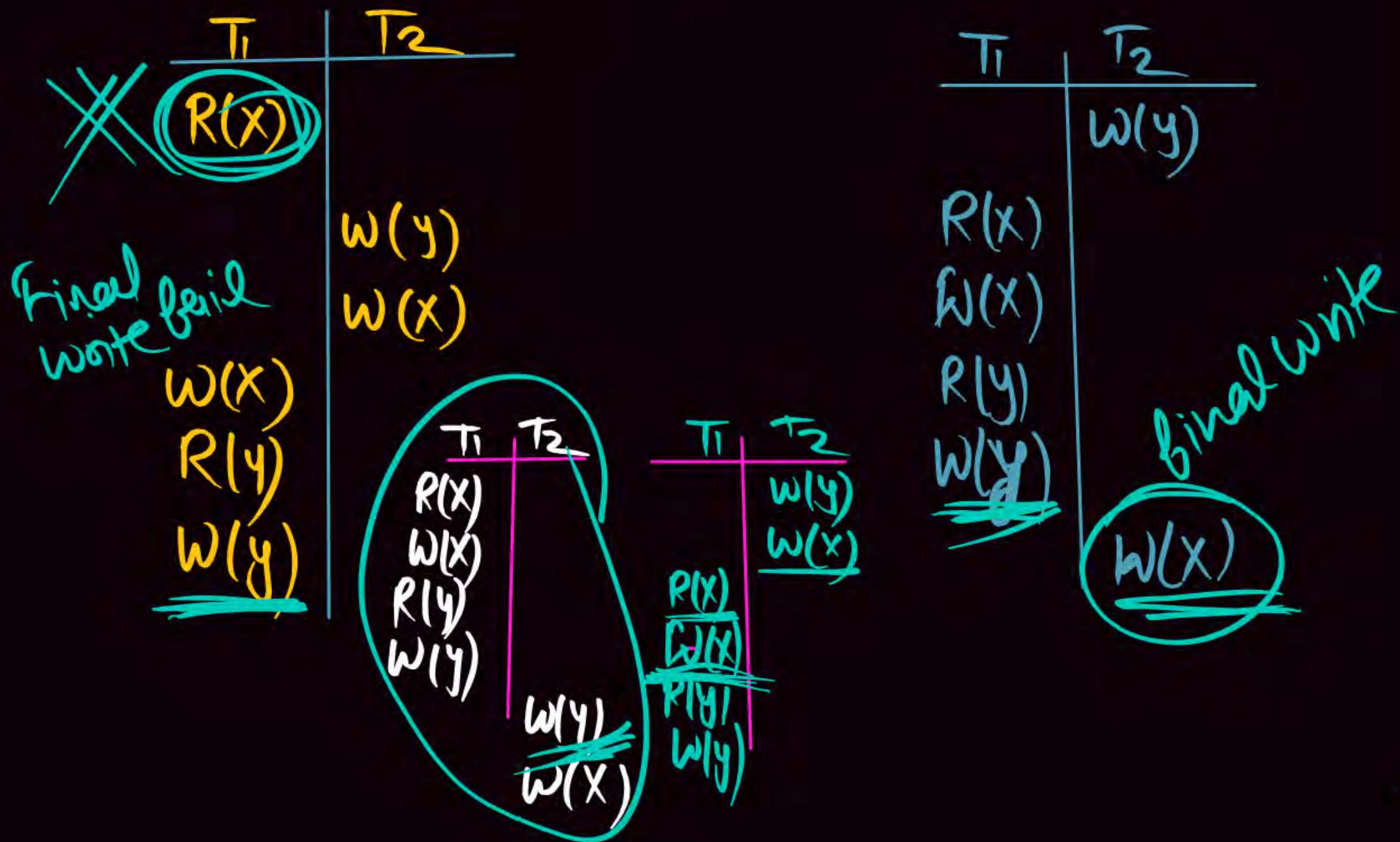
- (i) Conflict ?
- (ii) View ?



$T_1: R_1(x) \text{ } w_1(x), \text{ } R_1(y), \text{ } w_1(y)$  Non Serial  $\Rightarrow$  Serializable

$T_2: w_2(y) \text{ } w_2(x)$

- (i) Conflict  
(ii) View · ?



# Lock Based Protocol :

Consider the two transaction  $T_1$  and  $T_2$  with time stamp with 10 and 20 respectively.  $r(x)$  &  $w(x)$  denote read & write operation respectively on Data item X.

Consider the following schedule:

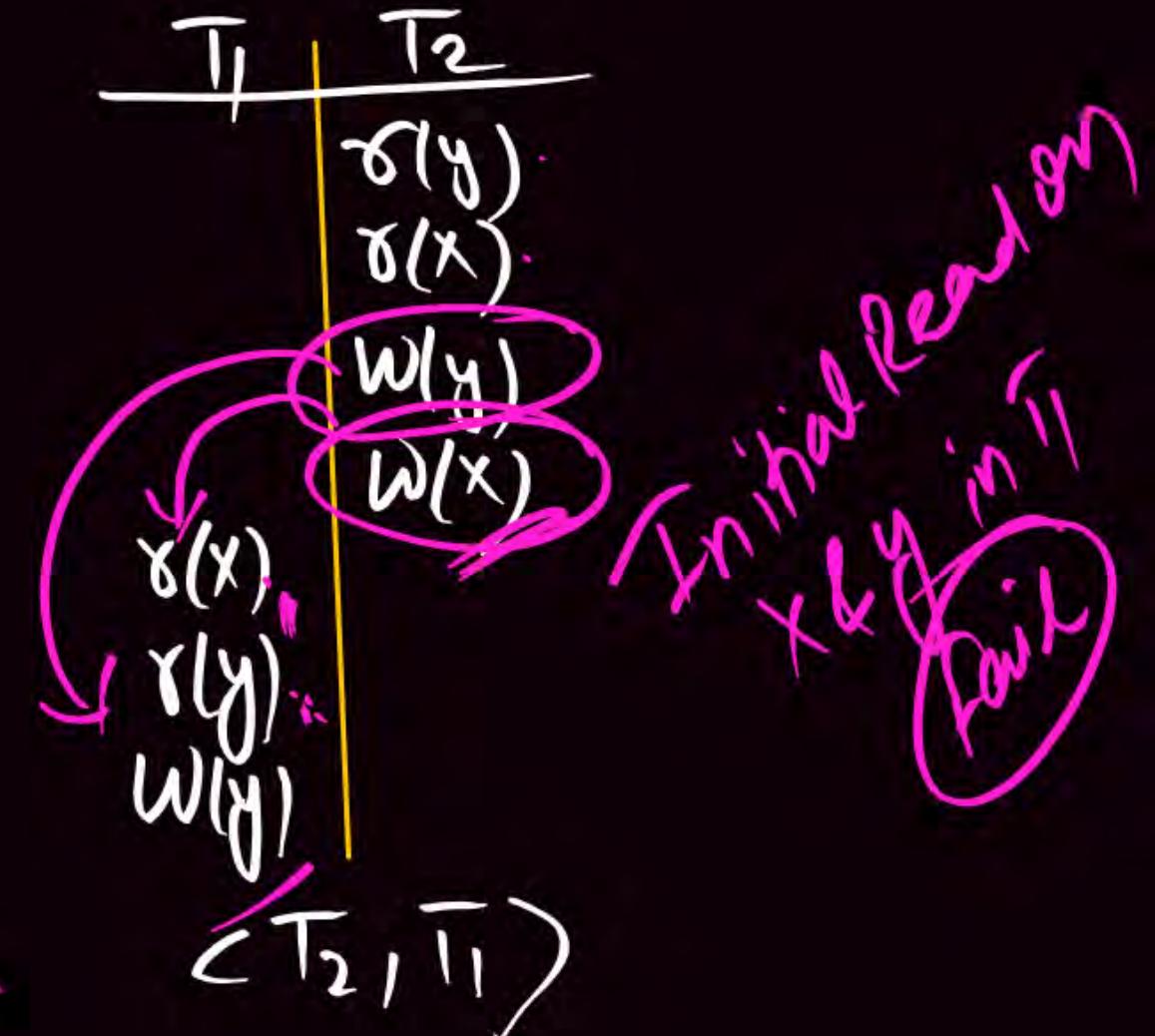
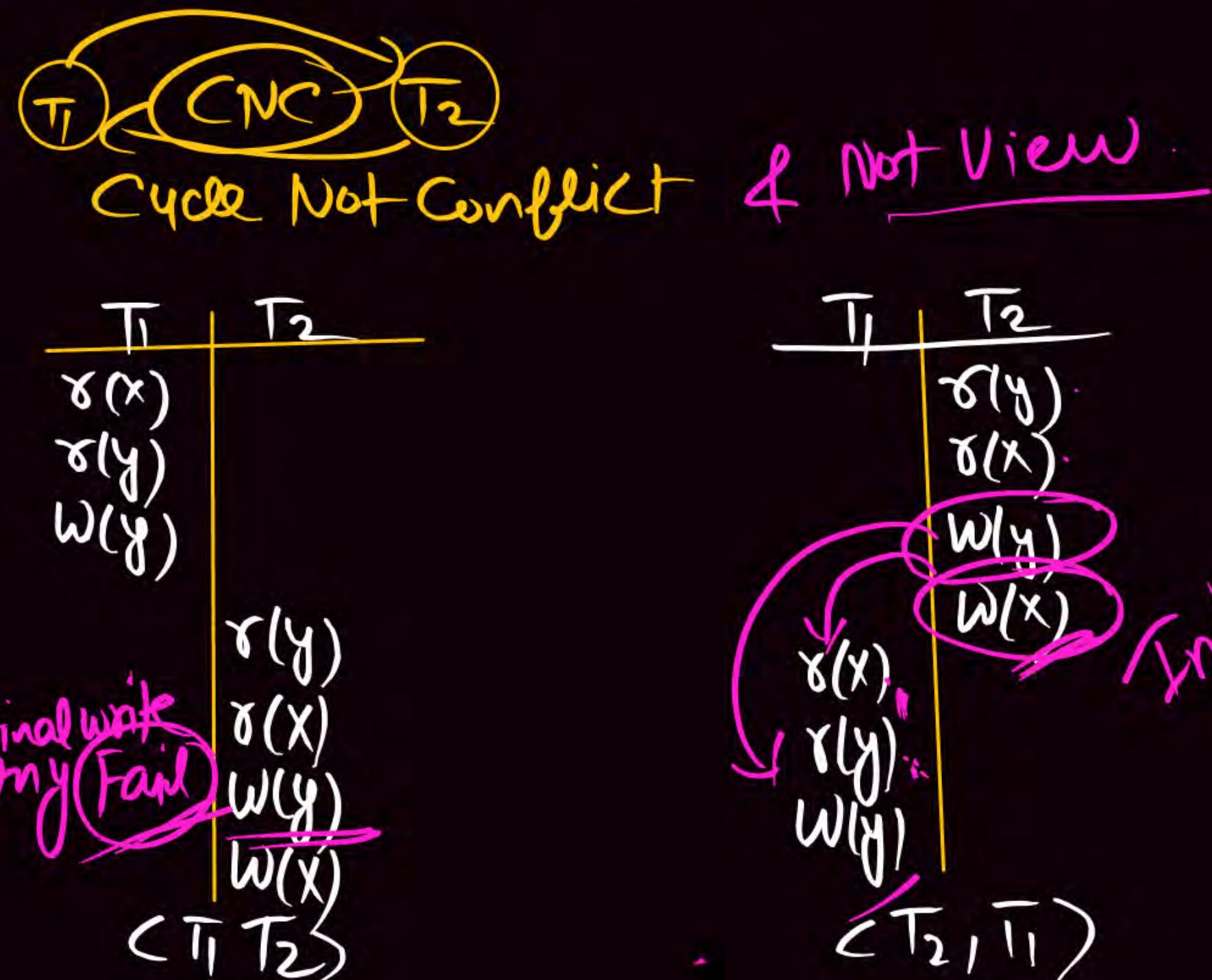
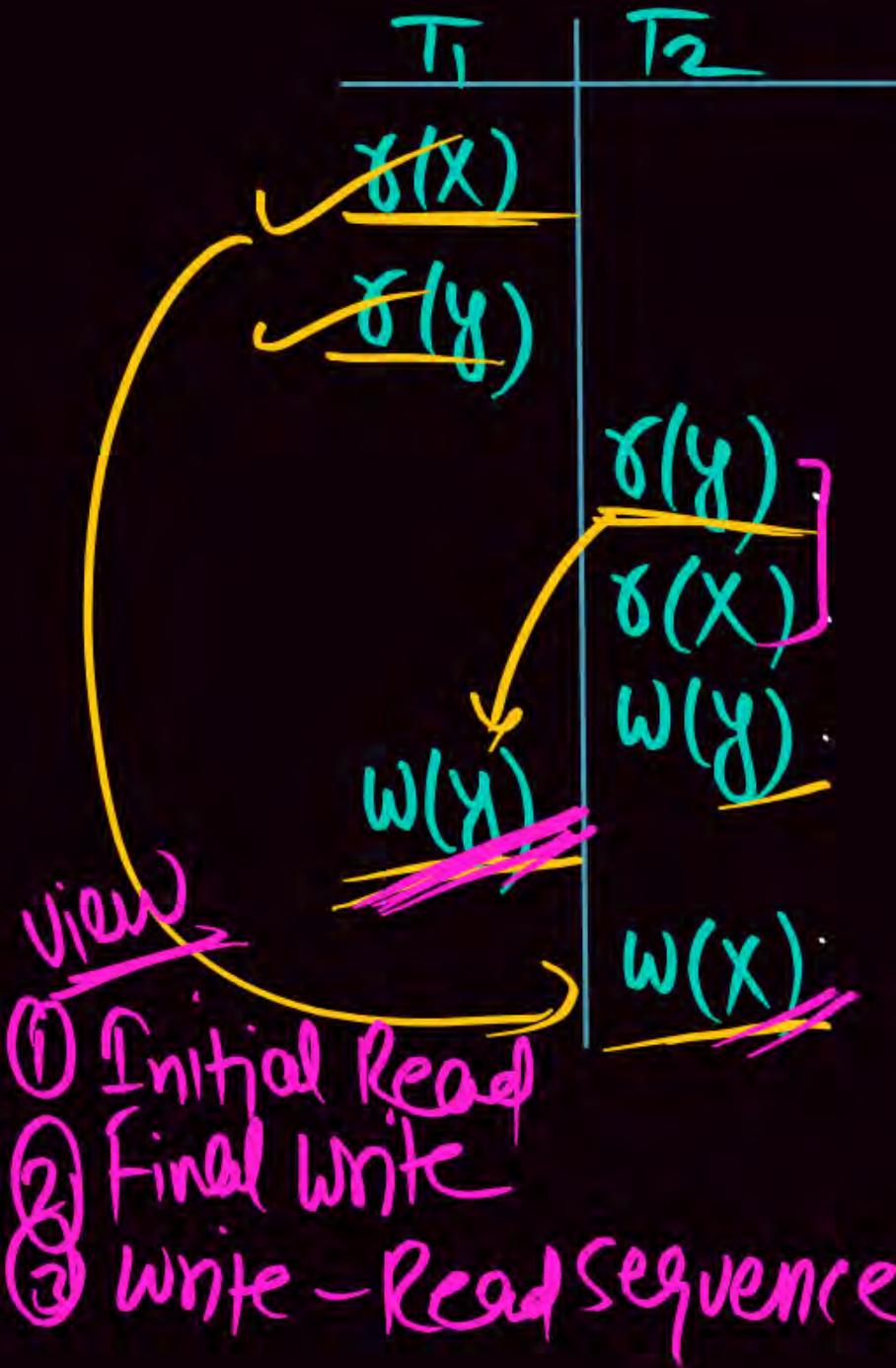
S:  $r_1(x) r_1(y) r_2(y), r_2(x) w_2(y) w_1(y) w_2(x)$

Which of the following statements is correct?

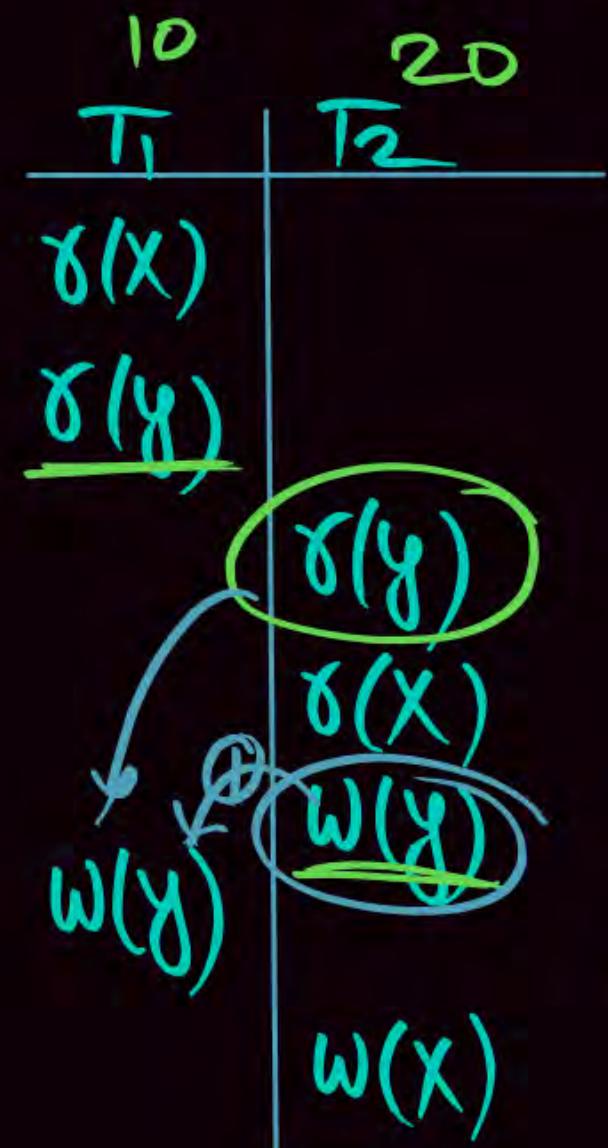
Ans(C)

- A Schedule S is allowed under Time stamp protocol.
- B Schedule S is allowed under Thoms write Rule.
- C Schedule S is Not Serializable.
- D Schedule S is view Serializable.

$S: \delta_1(x) \delta_1(y) \delta_2(y) \delta_2(x) w_2(y) w_1(y) w_2(x)$



$S: \delta_1(x) \delta_1(y) \delta_2(y) \delta_2(x) w_2(y) w_1(y) w_2(x)$



$\mathcal{T}: \underline{\text{TSP}}$

$R \rightarrow W$   
 $W \rightarrow R$   
 $W \rightarrow W$

$TS(T_1) : 10, TS(T_2) : 20$

$TS(T_1) < TS(T_2)$

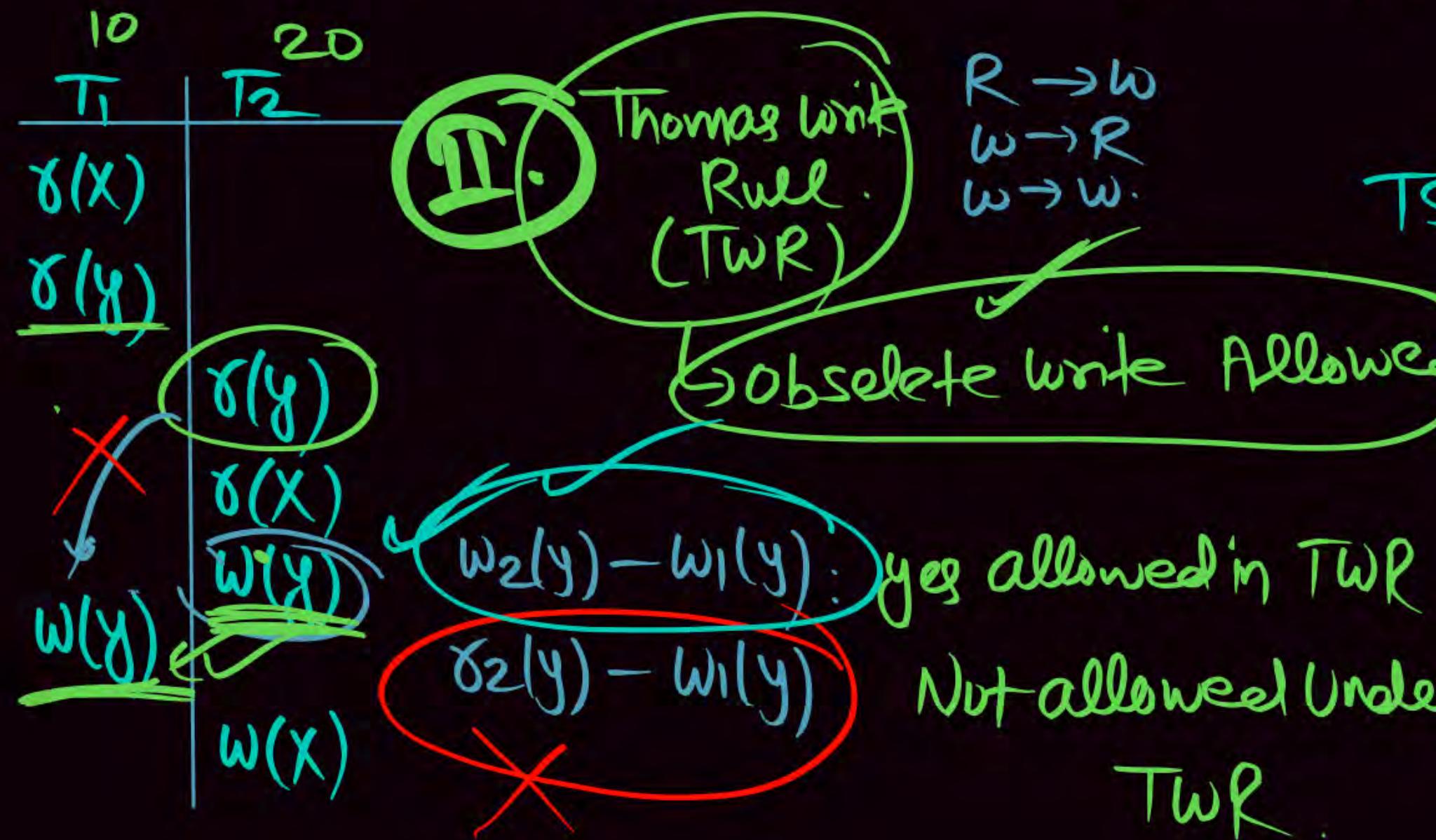
$T_1 \rightarrow T_2$

All conflict operations  
order must be

$T_1 \rightarrow T_2$  ( $T_1$  followed  
by  $T_2$ )

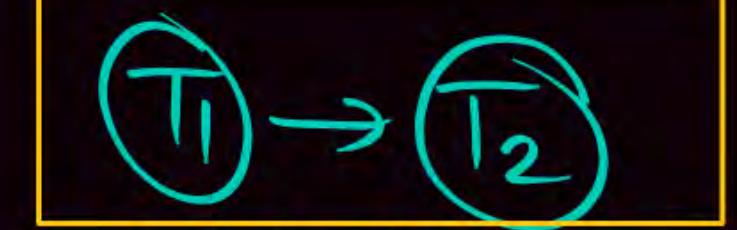
$w_2(y) - w_1(y)$ : Not TSP  
 $\delta_2(y) - w_1(y)$  Not TSP.

S:  $\delta_1(x) \delta_1(y) \delta_2(y) \delta_2(x) w_2(y) w_1(y) w_2(x)$



$TS(T_1) : 10, TS(T_2) : 20$

$TS(T_1) < TS(T_2)$

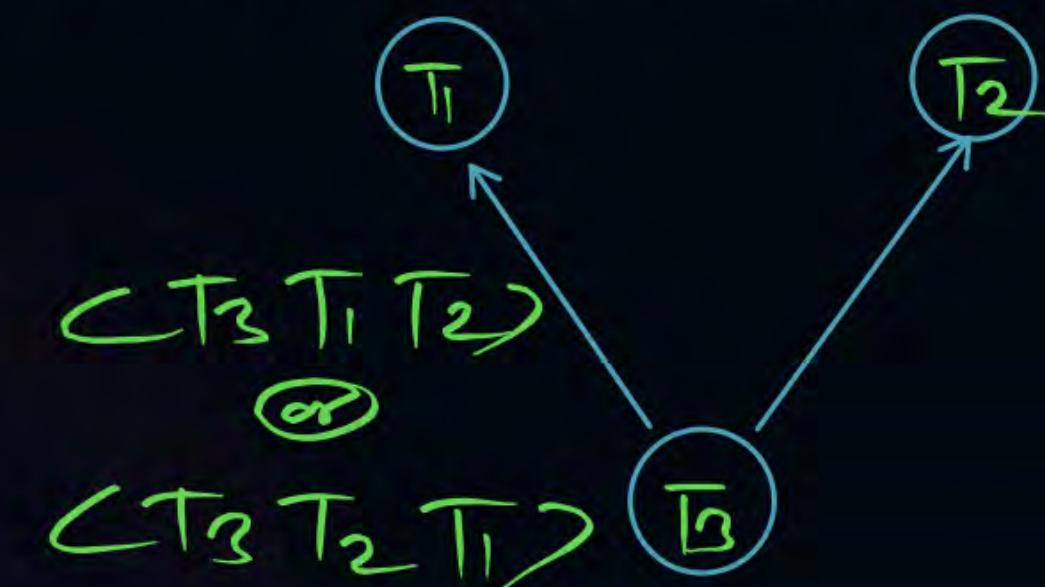


All conflict operations  
order must be  
 $T_1 \rightarrow T_2$  ( $T_1$  followed  
by  $T_2$ )

#Q. Consider the following schedule for transactions  $T_1$ ,  $T_2$  and  $T_3$

Which options is true in relating to serialization of the above?

- A  $T_3 \rightarrow T_1 \rightarrow T_2$
- B  $T_3 \rightarrow T_2 \rightarrow T_1$
- C Both  $T_3 \rightarrow T_1 \rightarrow T_2$  and  $T_3 \rightarrow T_2 \rightarrow T_1$
- D None of the above



AB(C)

	$T_1$	$T_2$	$T_3$
	$R(X)$		
	$W(X)$		
		$R(Y)$	
		$R(Z)$	
		$W(Y)$	
		$W(Z)$	
		$R(Z)$	
	$R(Y)$		
	$W(Y)$		

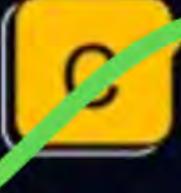
#Q. Consider the following schedule S of transactions  $T_1$  &  $T_2$  with A as data item S:  
 $r_1(a)$   $w_2(a)$   $w_1(a)$   $c_1, c_2$   
Which of the following is true, about the schedule S?



S is conflict serializable but also recoverable.



S is view serializable but also recoverable.



S is recoverable but not view serializable.



None of the above

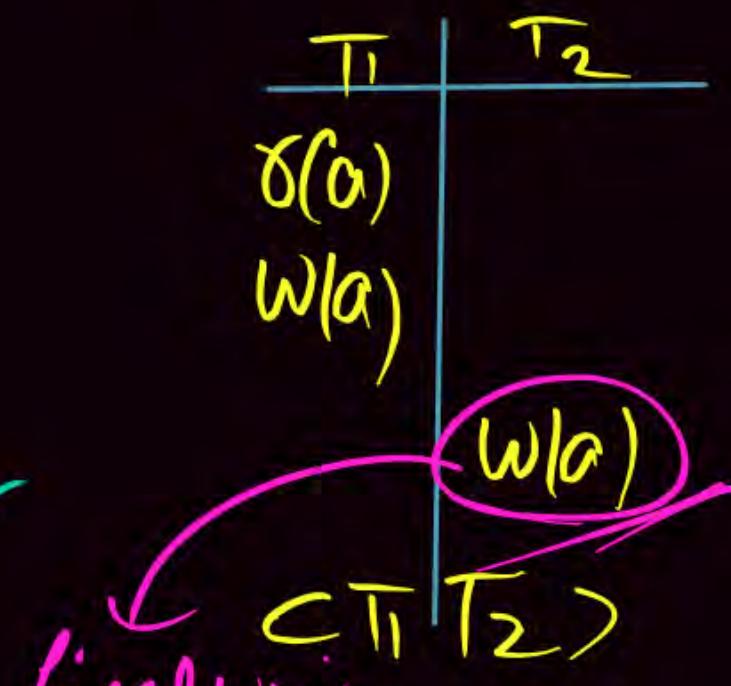
Ans(C).

$\delta_1(a)$   $w_2(a)$   $w_1(a)$   $c_1, c_2$

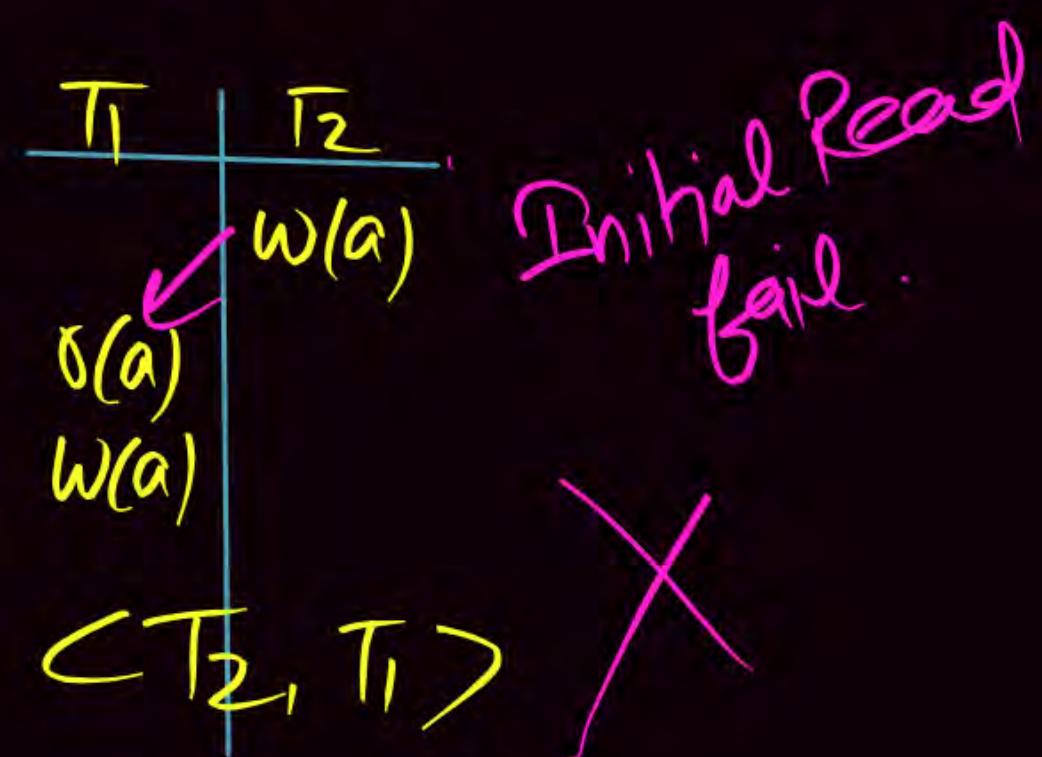


No WR  
So Recoverable ✓  
Consistent ✓  
Not Strict Recoverable

$T_1 \xrightarrow{CNC} T_2$   
Code Not Conflict, & Not View



$(T_2, T_1) >$   
final work fail.



$T_1$	$T_2$	$T_1$	$T_2$	$T_1$	$T_2$
w(A)			R(A)		R(A)/w(A)
clr			cas(delete)	clr	commit

• Commit  
 Recoverable

[MCQ]

P  
W

$T_1: 1 \quad T_2: 2 \quad T_3: 3.$

#Q. Which of the following schedule is allowed under basic timestamp protocol?

$S_1: r_1(x), r_3(x), w_1(x), r_2(x), w_2(x)$

$S_2: r_1(x), r_3(x), w_3(x), w_1(x), r_2(x)$

$S_3: r_3(x), r_2(x), w_3(x), r_1(x), w_1(x)$

$S_4: r_1(x), r_3(x), r_2(x), w_1(y), w_3(x)$

A

$S_1$

C

$S_3$

B

$S_2$

D

$S_4$

	$T_1$	$T_2$	$T_3$
$r_1(x)$			
$w_1(x)$			
$r_3(x)$			
$w_3(x)$			
$r_2(x)$			
$w_2(x)$			

NOT TSP  
NOT TWR

	$T_1$	$T_2$	$T_3$
$r_1(x)$			
$w_1(x)$			
$r_3(x)$			
$w_3(x)$			
$r_2(x)$			
$w_2(x)$			

NOT TSP  
NOT TWR

[MCQ]

P  
W

$T_1: 1 \quad T_2: 2 \quad T_3: 3.$

#Q. Which of the following schedule is allowed under basic timestamp protocol?

S<sub>1</sub>:  $r_1(x), r_3(x), w_1(x), r_2(x), w_2(x)$

S<sub>2</sub>:  $r_1(x), r_3(x), w_3(x), w_1(x), r_2(x)$

S<sub>3</sub>:  $r_3(x), r_2(x), w_3(x), r_1(x), w_1(x)$

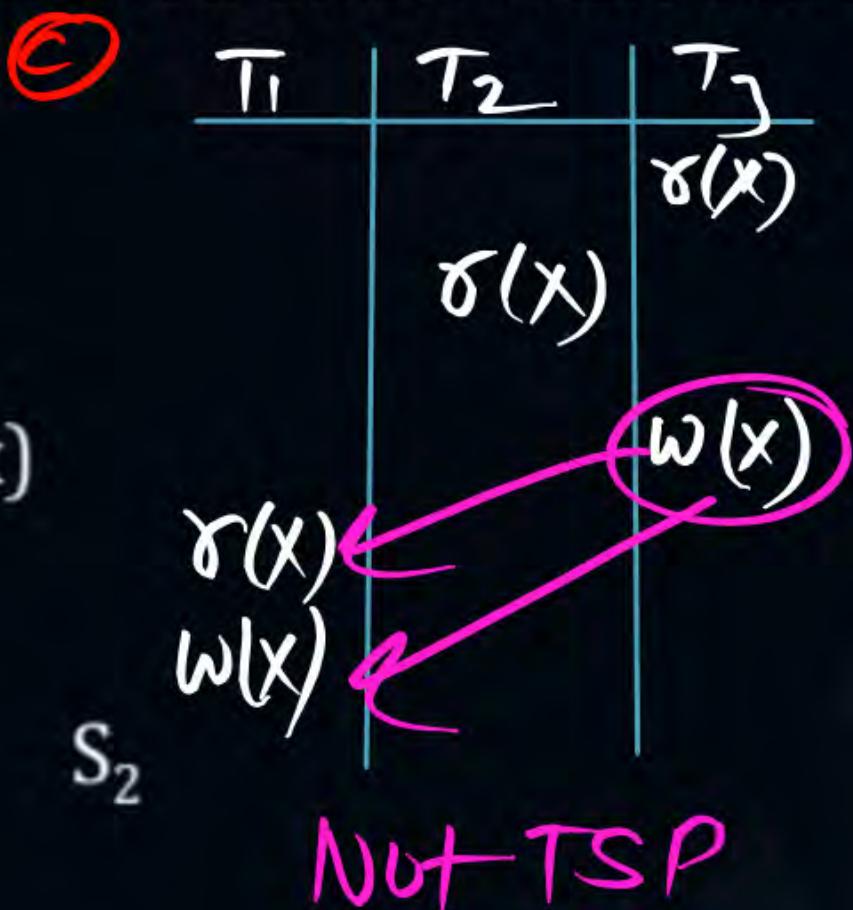
S<sub>4</sub>:  $r_1(x), r_3(x), r_2(x), w_1(y), w_3(x)$

A S<sub>1</sub>

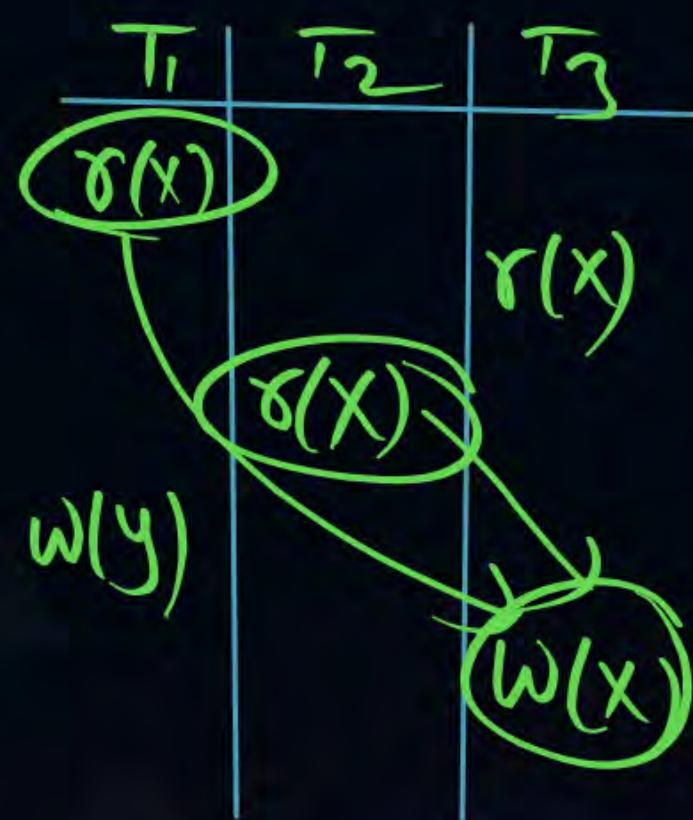
B S<sub>2</sub>

C S<sub>3</sub>

D S<sub>4</sub>



Not TSP



$T_1 \rightarrow T_2 \rightarrow T_3$

YES TSP ✓

YES TWR ✓

**[MCQ]****H.W**

Consider the following four schedule involving Two Transactions (Indicated by the subscript using read & write on data item a denoted by R(A) & W(B) respectively.  
Which of the following schedule is view serializable but not conflict serializable?

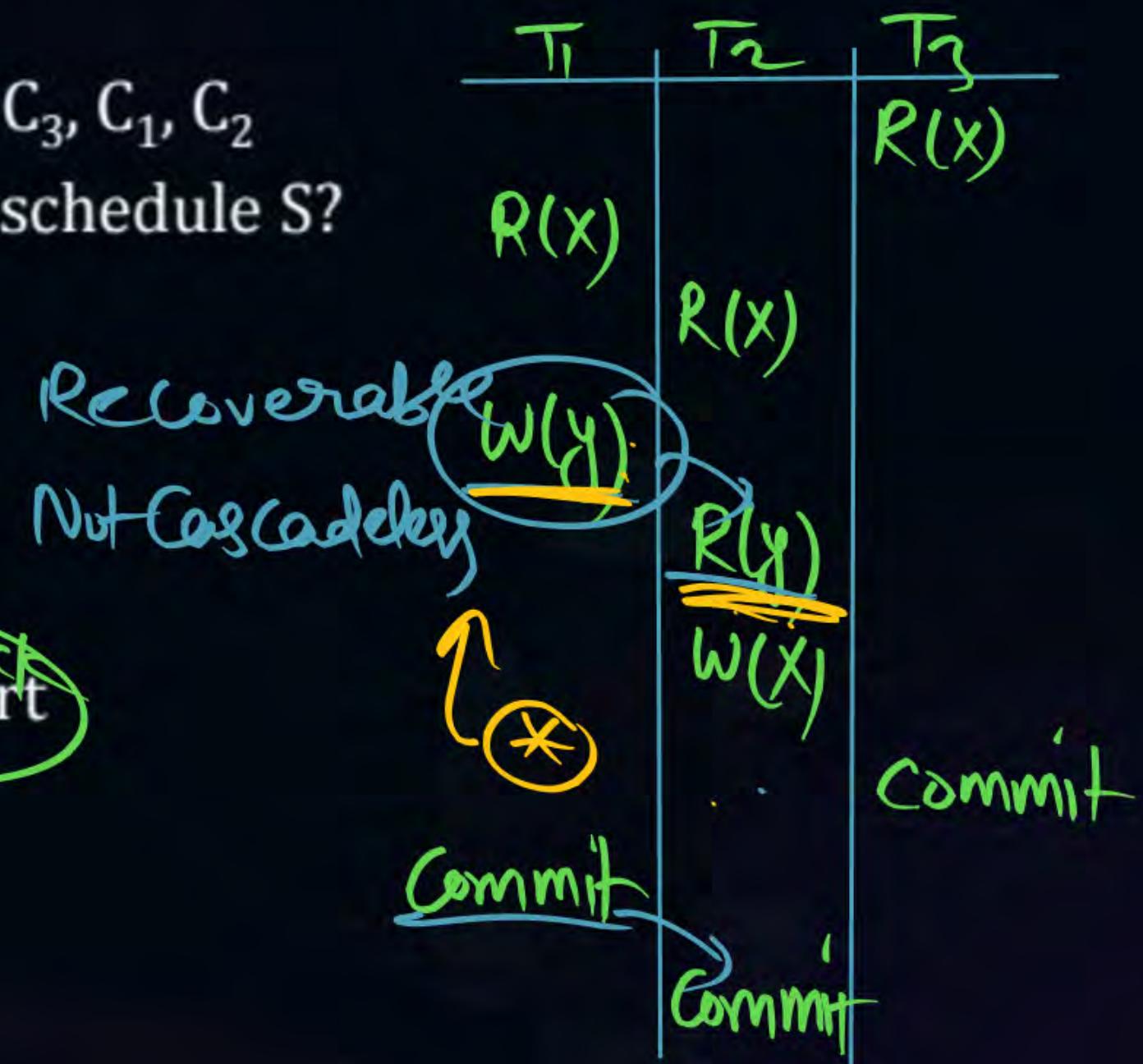
- A    R<sub>1</sub>(A) W<sub>1</sub>(A) R<sub>2</sub>(A) R<sub>1</sub>(B) R<sub>2</sub>(B)  $\xrightarrow{W_2(B)}$
- B    R<sub>1</sub>(A) W<sub>1</sub>(A) W<sub>2</sub>(A) R<sub>1</sub>(B) W<sub>1</sub>(B) R<sub>2</sub>(B)
- C    R<sub>1</sub>(A) W<sub>2</sub>(A) W<sub>1</sub>(A) R<sub>1</sub>(B) W<sub>1</sub>(B) W<sub>2</sub>(B)
- D    R<sub>2</sub>(A) W<sub>1</sub>(A) W<sub>2</sub>(B) W<sub>1</sub>(B) W<sub>2</sub>(A) W<sub>1</sub>(A)

#Q. Consider the following schedule S of transactions  $T_1, T_2 \& T_3$  with x, y data items,  $C_1, C_2$  &  $C_3$  are commit

S:  $R_3(x), R_1(x), R_2(x), W_1(y), R_2(y), W_2(x), C_3, C_1, C_2$

Which of the following is true, about the schedule S?

- A S is non-recoverable
- B S is recoverable, but has a cascading abort
- C S does not have a cascading abort
- D S is strict



#Q. Which of the following statement is/are incorrect?

1. A schedule following strict two phase locking protocol is conflict serializable as well as recoverable → True.
2. Checkpoint in schedules are inserted to ensure recoverability

A

Only 1

Minimize the  
Redo - Undo  
operation.

B

Only 2

C

Both 1 and 2

D

None

H.W

#Q. Consider the following schedule S of transaction  $T_1$  and  $T_2$

Which of the following statements is correct?

- A S is conflict-Serializable but not recoverable
- B S is conflict-Serializable and also recoverable
- C S is neither conflict-Serializable nor recoverable
- D S is not conflict-Serializable but recoverable

$T_1$	$T_2$
Read(X)	
Write(X)	
	Read(X) Write(X) Commit:
	Read(X) Write(X) Commit

#Q. Consider the following schedules S<sub>1</sub>& S<sub>2</sub>

S<sub>1</sub>: Lock -s(A); r(A); lock-x(B); unlock(A);r(B); w(B); commit unlock(B)

S<sub>2</sub>: Lock-s(A); r(A); Lock-x(B); r(B); w(B); commit unlock(A); unlock(B);

Which of the following true?

A

S<sub>1</sub> is rigorous 2PL and S<sub>2</sub> is conservative 2 PL.

B

S<sub>1</sub> is simple 2PL and S<sub>2</sub> is strict 2PL.

C

S<sub>1</sub> is strict 2PL and S<sub>2</sub> is rigorous 2PL.

D

None

#Q. Consider the following schedule  $S_1, S_2$

$S_1: r_2(x), r_2(y), r_1(x), r_1(y), w_1(x), w_2(x)$

$S_2: r_2(x), r_2(y), w_2(x), r_1(x), r_2(y)$

Which of the following is correct?

A

$S_1$  results in lost-update problem & dirty read  $S_2$  results in dirty read

B

$S_1$  results in lost-update problem & unrepeatable read &  $S_2$  results in unrepeatable read

C

$S_1$  results in lost-update problem & unrepeatable read &  $S_2$  results in dirty read

D

None



## 2 mins Summary



Topic One

Topic Two

Topic Three

Topic Four

Topic Five

43

Lock Based Protocol :



THANK - YOU

# CS & IT ENGINEERING

## Database Management System

Lecture No.- 04

By- Vijay Agarwal Sir



# Recap of Previous Lecture



Topic

Normal Form & NF Decomposition

Topic

Transaction Concept

Topic

Serializable & Recoverable Schedule

Topic

Lock Based Protocol

# Topics to be Covered



Topic

ER Model Concept

Topic

ER Model to RDBMS Conversion

Topic

Foreign Key Concept

#Q. Match the following

List-I	List-II
a.	1. One to one relationship
b.	2. Relationship
c.	3. Many to many relationship
d.	4. Many to one relationship

Codes:

Ans (C)

	a	b	c	d
A	3	4	2	1
C	2	3	4	1

	a	b	c	d
B	4	3	2	1
D	3	4	1	2

#Q. Database \_\_ which is the logical design of the database, and the database \_\_ \_ which is a snapshot of the data in the database at a given instant in time.

A

instance, schema

B

relation, schema

C

relation, domain

D

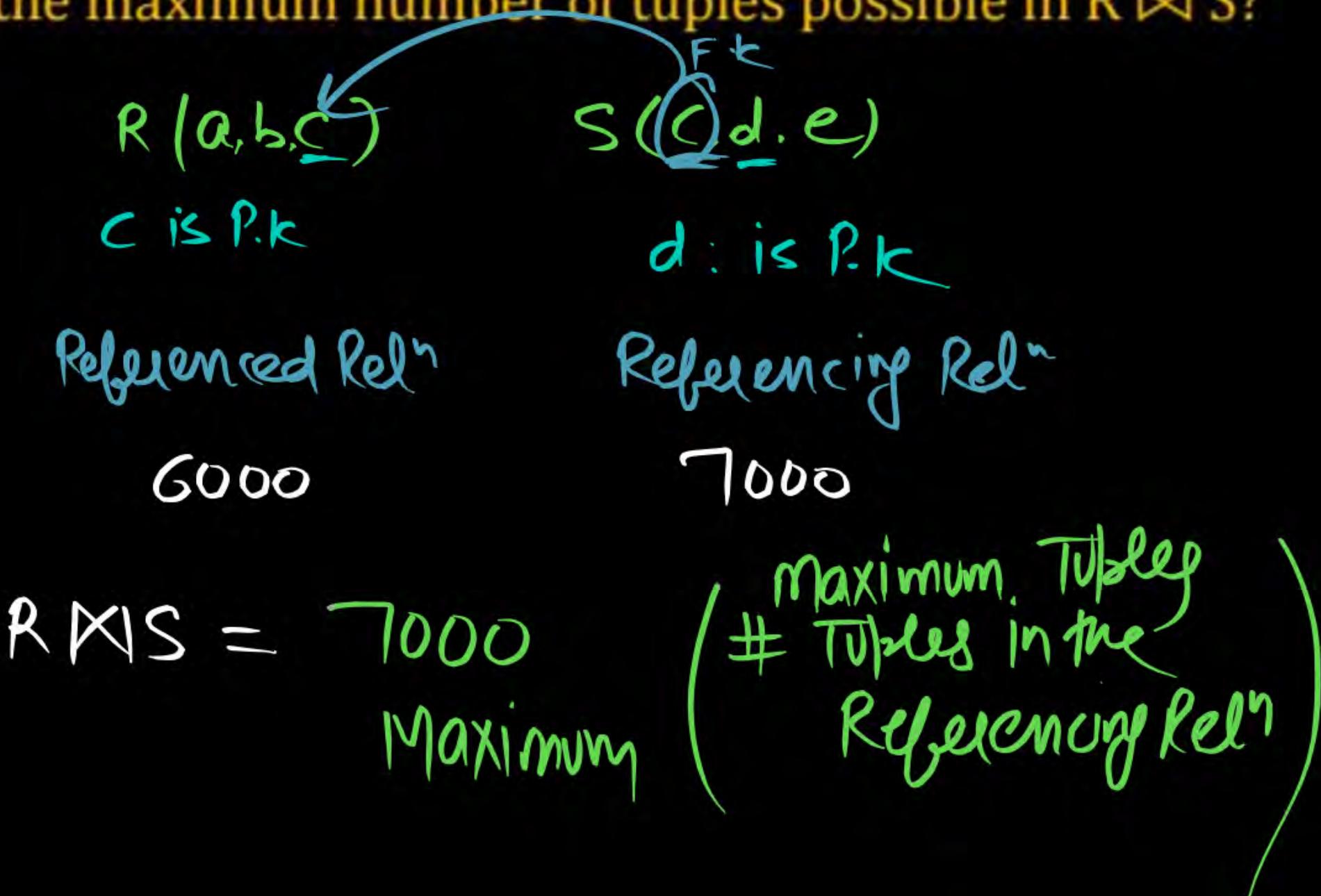
schema, instance

Ans(D)

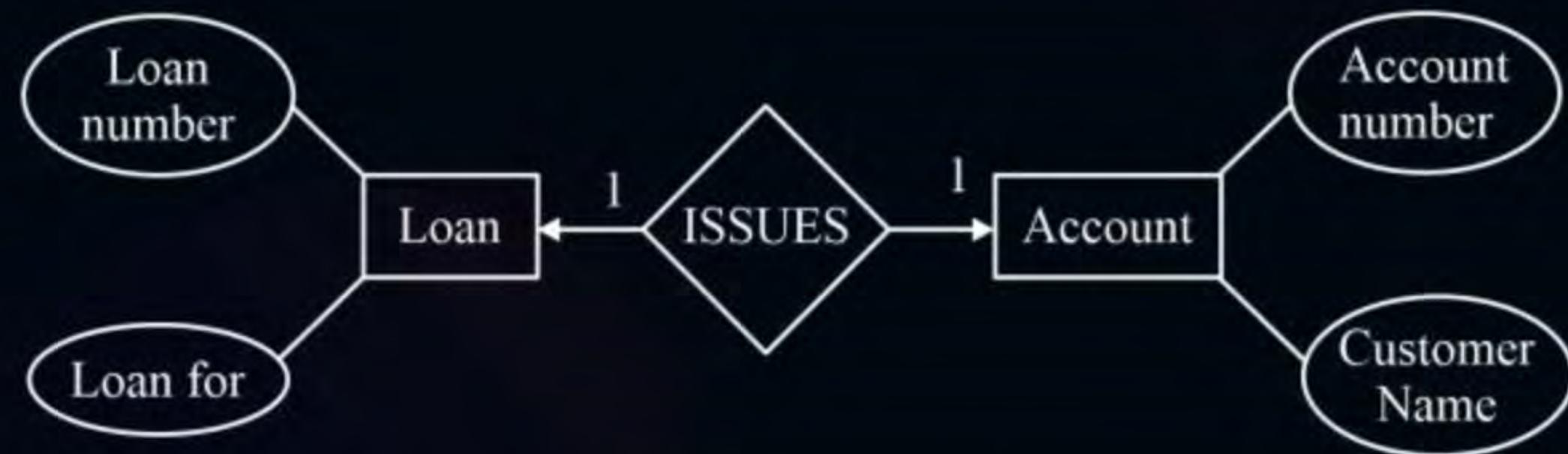
## [MCQ]

Consider the Relation R(a, b, c) and S(c, d, e) where c is primary key of R and d is the primary key of S. Relation R contain 6000 tuples and relation S contains 7000 tuples, what will be the maximum number of tuples possible in  $R \bowtie S$ ?

- A 6000
- B 12000
- C 13000
- D 7000



#Q. Consider the following ER model



The minimum number of tables needed to represent the given ER model is

A

2

C

1

B

3

D

None of these

## Foreign key Concept



### Referencing Relation

- ① ON DELETE NO ACTION
- ② ON DELETE CASCADE
- ③ ON DELETE SET NULL

Consider the following table with two attributes A and C, where A is primary key and C is foreign key referencing A with on delete cascade.

The number of tuples that must be additionally deleted to preserve referential integrity when the tuple (4, 5) deleted is \_\_\_?

(4,5) Primary key '4' Deleted

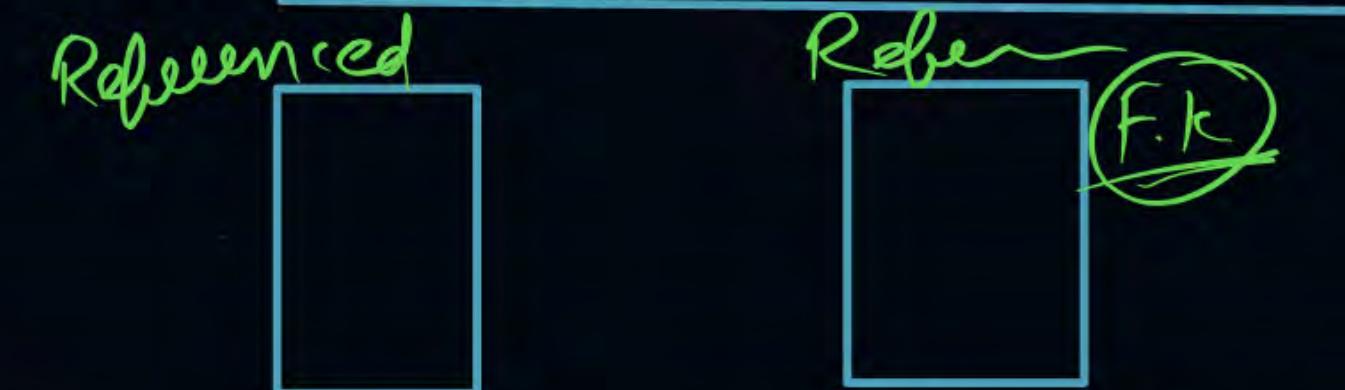
(3,4) (7,4) (11,4)  
(C (10,9)

Q. 5

A	C
3	4
4	5
5	6
7	4
9	7
11	4
8	6
12	13
10	9
6	8
13	12

⑤ Ans

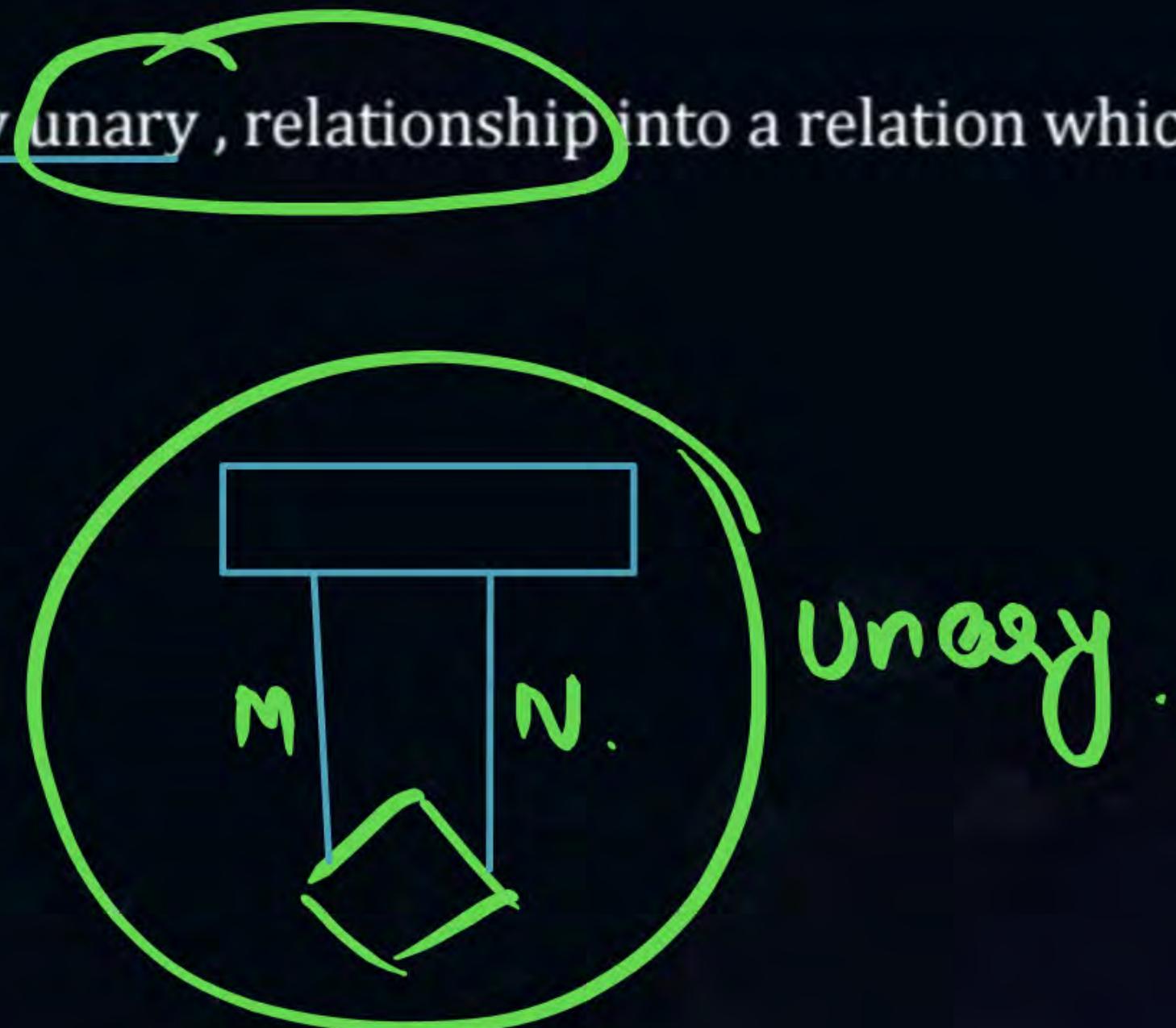
#Q. Which of the following is true regarding referential integrity?



- A  Every primary-key value must match a primary-key value in an associated table.
- B  Every primary-key value must match a foreign-key value in an associated table.
- C  Every foreign-key value must match a primary-key value in an associated table.
- D  Every foreign-key value must match a foreign-key value in an associated table.

#Q. When mapping a many-to-many **unary**, relationship into a relation which of the following is true?

- A One relation is created
- B Two relations are created
- C Three relations are created
- D Four relations are created



Q.

Let R (a, b, c) and S(d, e, f) be two relations in which d is the foreign key of S that refers to the primary key of R. Consider the following four operations on R and S.

(i) Insert into R

(ii) Insert into S

(iii) Delete from R

(iv) Delete from S

R(a,b,c)

S(d,e,f)

Delete X

Insert X

Which of the following is true about the referential integrity constraint above?

A

None of (i), (ii), (iii), or (iv) can cause its violation

B

All of (i), (ii), (iii), and (iv) can cause its violation

C

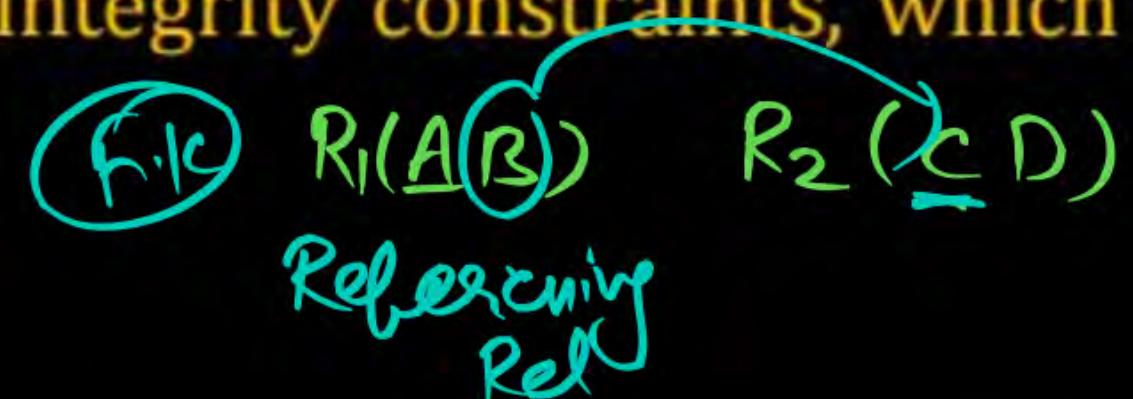
Both (i) and (iv) can cause its violation

D

Both (ii) and (iii) can cause its violation

# MCQ

Suppose  $R_1(A, B)$  and  $R_2(C, D)$  are two relation schemes. Let  $r_1$  and  $r_2$  be the corresponding relation instances. B is a foreign key that refers to C in  $R_2$ . If data in  $r_1$  and  $r_2$  satisfy referential integrity constraints, which of the following is ALWAYS TRUE?



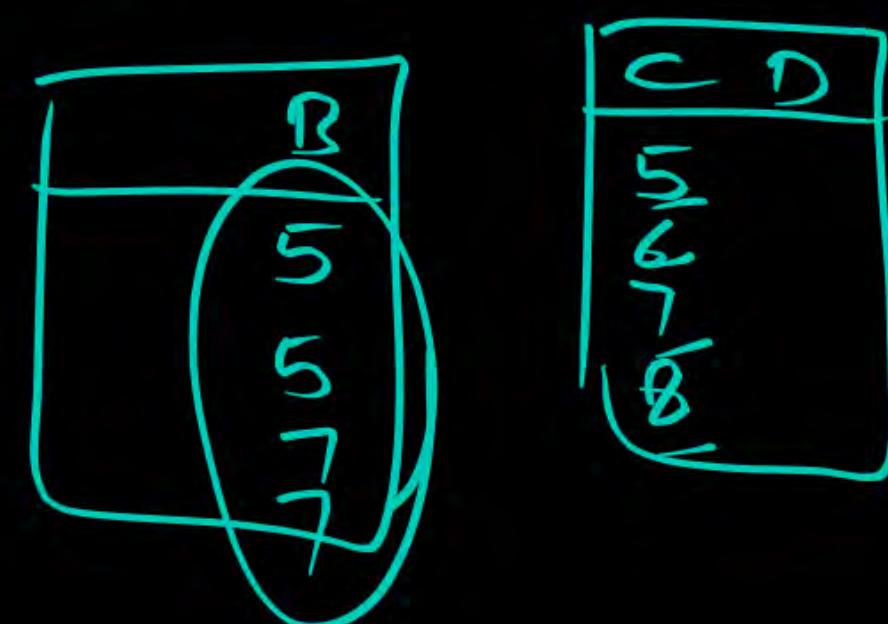
A  ~~$\Pi_B(r_1) \cdot \Pi_C(r_2) = \phi$~~

C  $\Pi_B(r_1) = \Pi_C(r_2)$

Ans (A)

B  $\Pi_C(r_2) \cdot \Pi_B(r_1) = \phi$

D  $\Pi_B(r_1) \cdot \Pi_C(r_2) \neq \phi$



R		S	
B	C	C	D
5	5	5	5
5	7	6	6
7	7	7	7
7	7	8	8

# [MCQ]



#Q Consider the following schema with 3 relation P, Q and R. In relation P having 3 attributes C, D and E in which C is the primary key. Relation Q having 2 attributes B and C in which B is primary key and attribute C is foreign key reference to the primary key of relation P, with on delete cascade. Relation R having 2 attributes A and B in which A is primary key and attribute B is foreign key reference to the primary key of relation Q on delete set NULL. Here domain of all attributes A, B, C, D and E are integer. Suppose the content of relation P, Q and R are given below:

R(A B)	
A	B
1	1
2	2

ON DELETE  
SETNULL

Q(B C)	
B	C
1	1
2	1
3	1

PK 1,2,3

2Delete

P(C D E)		
C	D	E
1	1	2
2	1	3
3	1	4
4	2	5

PK [1,2,3,4]

Continue

When all record in the table P deleted (Deleted from P) then what tuples will relation R contain?

A

(1, NULL) (2, NULL) (3, NULL)

B

(1, NULL) (2, NULL) (3, 1)

C

(1, 1) (2, 2)

D

(1, NULL) (2, NULL)

Ans (D)

# NAT

Consider the following tables T1 and T2.

In table T1, P is the primary key and Q is the foreign key referencing R in table T2 with on-delete cascade and on-update cascade. In table T2, R is the primary key and S is the foreign key referencing P in table T1 with on-delete set NULL and on-update cascade. In order to delete record  $\langle 3,8 \rangle$  from table T1, the number of additional records that need to be deleted from table T1 is

T <sub>1</sub>		T <sub>2</sub>	
P	Q	R	S
2	2	2	2
3	3	3	3
7	3	3	2
5	8	9	7
6	9	5	7
8	5	7	2
9	8		

ON DELETE CASCADE  
ON UPDATE CASCADE

Domain  
Age  
+ve Integer

#Q. Match the following with respect to RDBMS:

List-I	List-II
a. Entity integrity — 4	1. Enforces some specific business rule that do not fall into entity or domain
b. Domain integrity — 3	2. Rows can't be deleted which are used by other
c. Referential integrity — 2	3. Enforces valid entries for a column
d. User defined integrity — 1	4. No column duplicate rows in a table

Codes:

	a	b	c	d
A	3	4	1	2
C	4	2	3	1

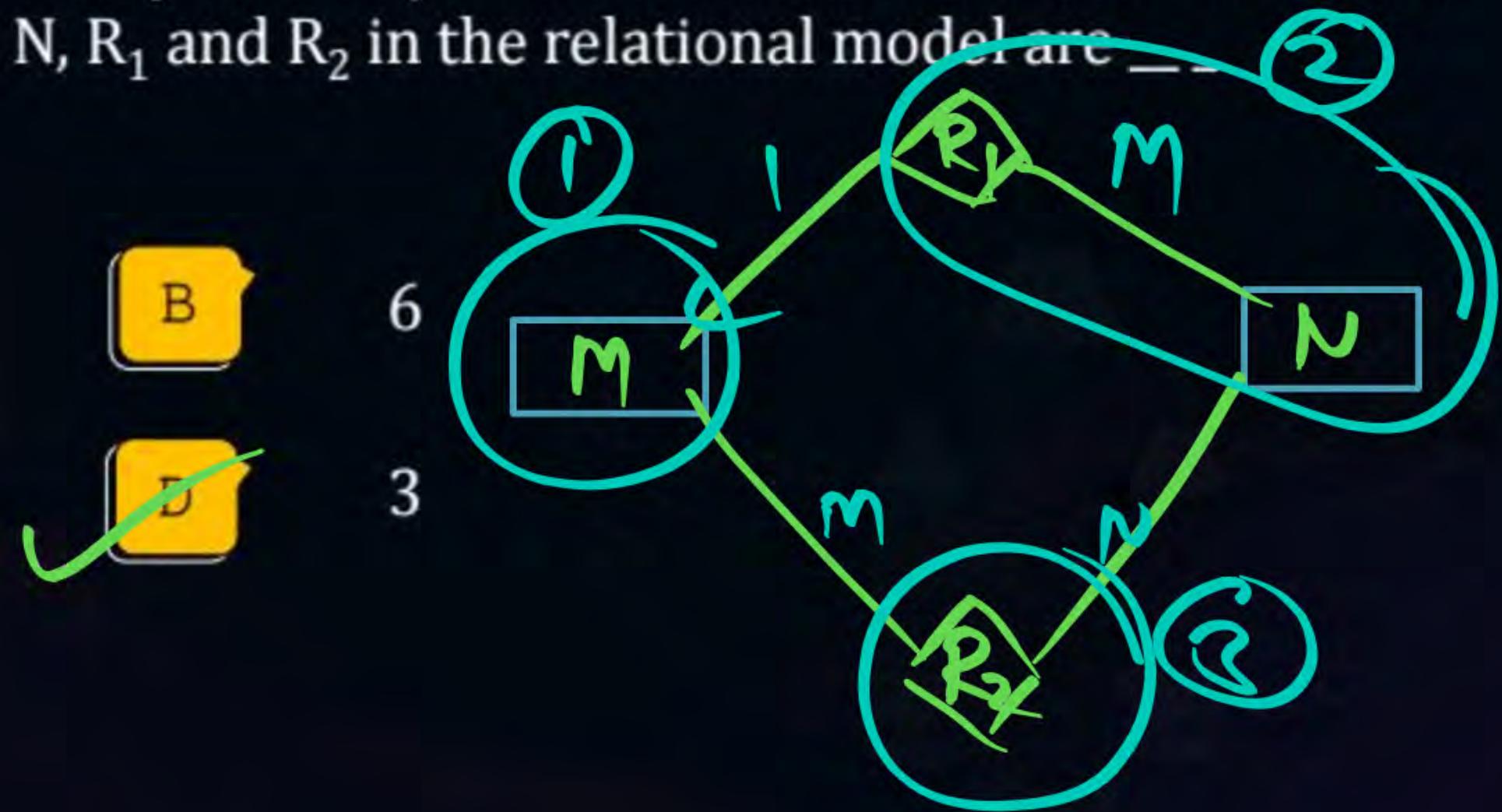
Ans (R)

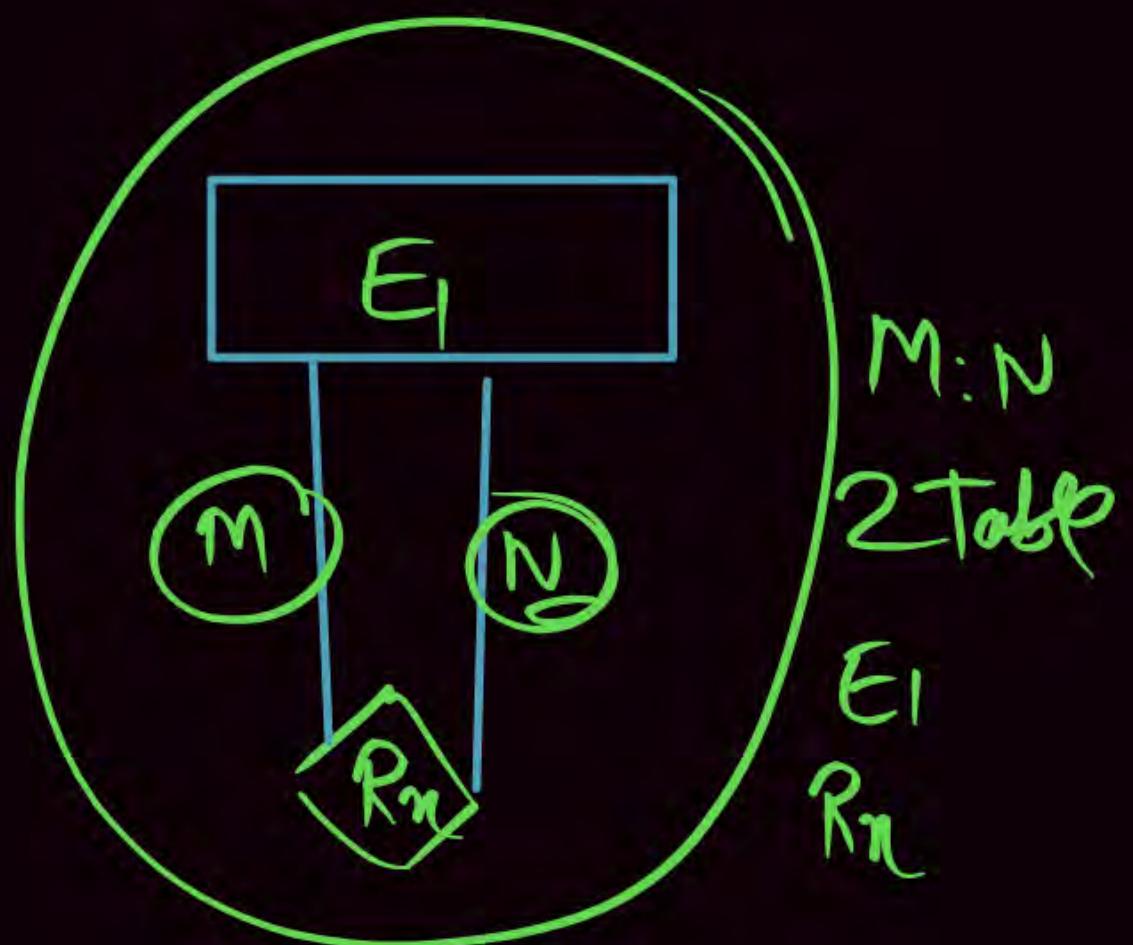
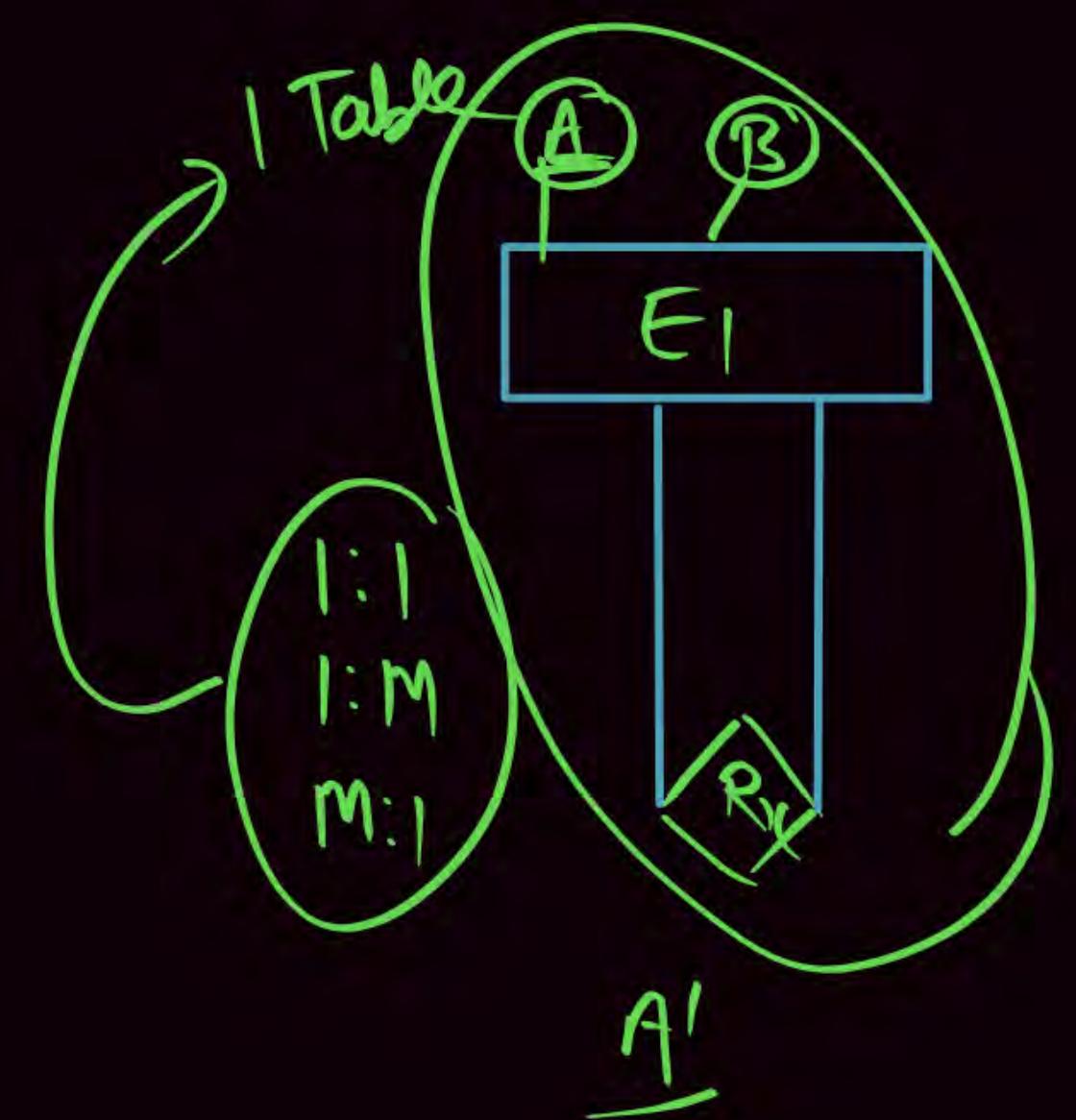
	B	D
X	4	2

	a	b	c	d
	4	3	2	1
	2	3	4	1

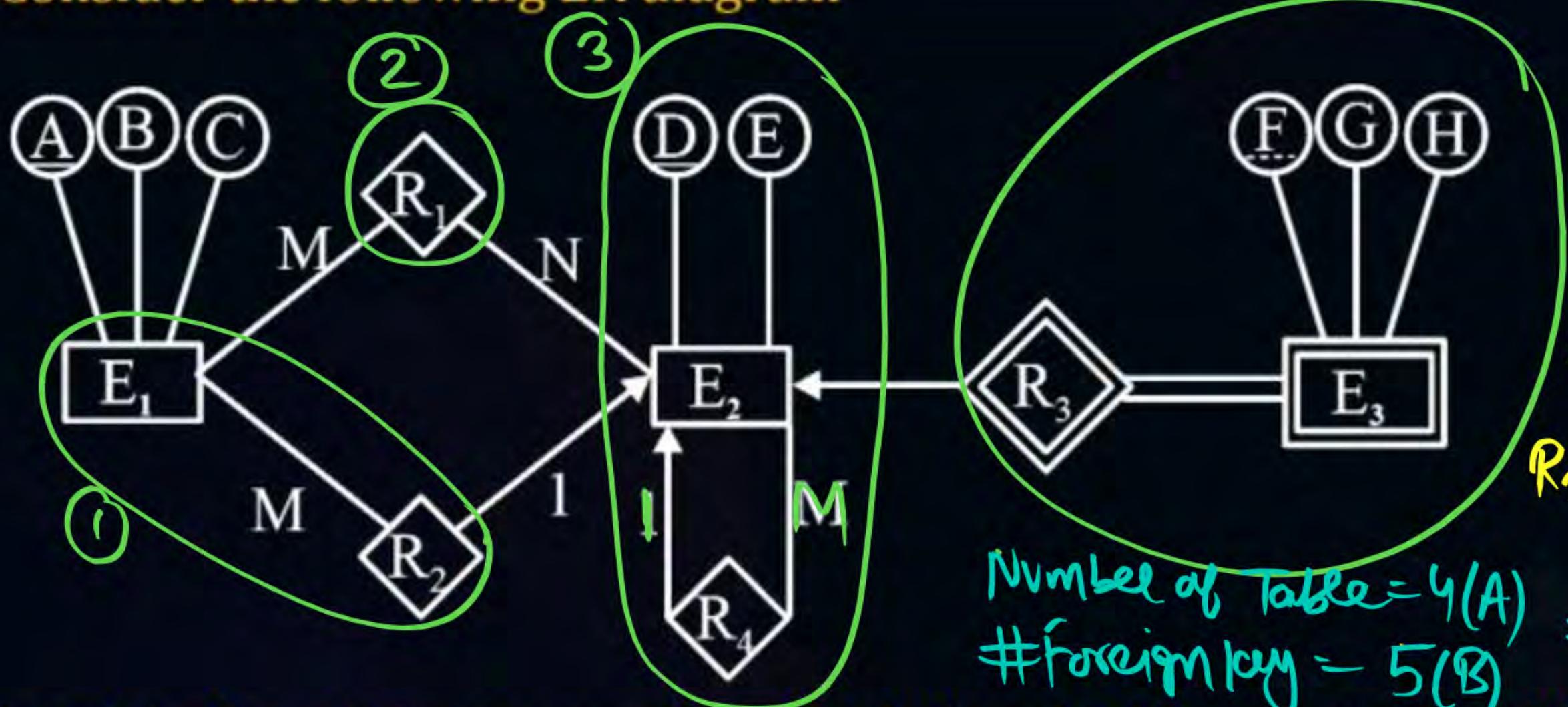
#Q. Let M and N be two entities in an E-R diagram with simple single value attributes. R<sub>1</sub> and R<sub>2</sub> are two relationship between M and N, where as R<sub>1</sub> is one-to-many and R<sub>2</sub> is many-to-many. The minimum number of tables required to represent M, N, R<sub>1</sub> and R<sub>2</sub> in the relational model are \_\_\_.

- A 4
- B 6
- C 7





Consider the following ER diagram



Let A is the minimum number of relational table required and B is the minimum number of foreign key required for conversion of ER into relational table then value of  $2A + B$  is 13. Ans

1Fk

↑

 $\underline{D}$ 

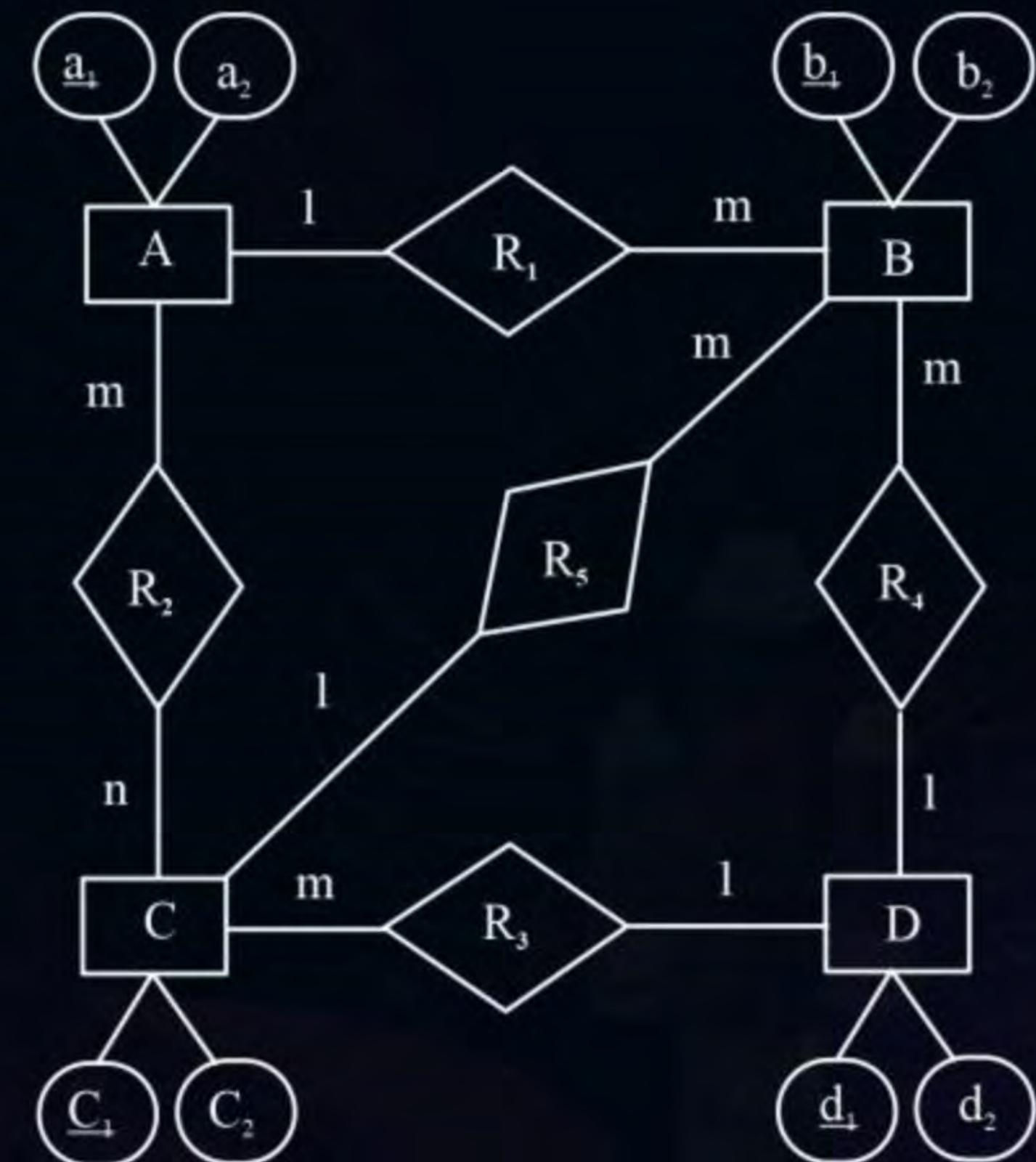
1Fk

 $E_1 R_2 (A B C \quad \underline{D})$  $R_1 (\underline{A} \underline{D}) : 2 Fk(A, D)$  $E_2 R_3 (D E \quad \underline{D}_1) : 1 Fk(D)$  $R_3 E_3 (F G H \quad \underline{D}) : 1 Fk(D)$ 

Number of Table = 4(A)  
# Foreign key = 5(B)

$$2A + B \Rightarrow 2 \times 4 + 5 = 13$$

Common data for Question No. 1,2  
& 3 Consider the following ER-diagram



#Q. The minimum number of tables needed to represent A, B, C, D, R<sub>1</sub>, R<sub>2</sub>, R<sub>3</sub>, R<sub>4</sub>, R<sub>5</sub> is

A

3

C

5

B

4

D

6

#Q. Above ER diagram, consists of Entity types B and D. These are connected by R4 which does not have its own attribute.

Which one of the following is correct?

A

Relationship R4 is many to one so R4 can be merged with that of B.

B

Relationship R4 is many to one so R4 can be merged with that of D.

C

Both a and b

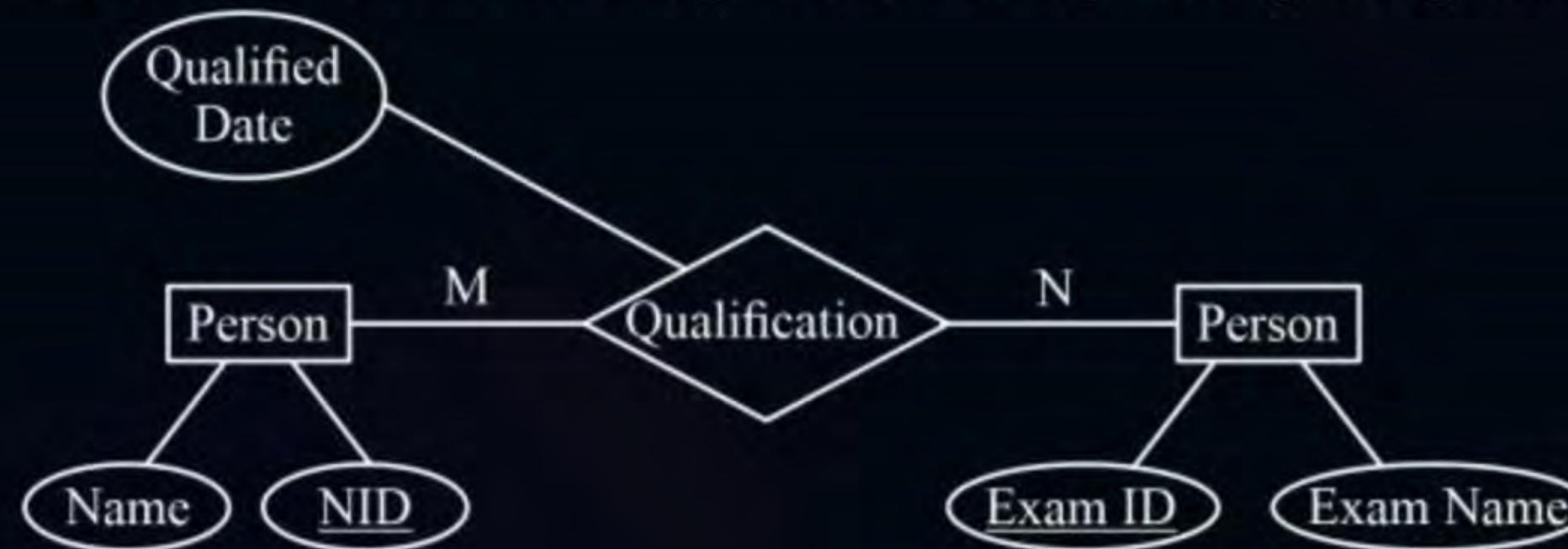
D

None of these

#Q. Which of the following is a correct attribute set for one of the tables for the correct answer to the above question?

- A (a<sub>1</sub>,b<sub>1</sub>,c<sub>1</sub>)
- B (b<sub>1</sub>,b<sub>1</sub>,c<sub>1</sub>,a<sub>1</sub>)
- C (c<sub>1</sub>,c<sub>2</sub>)
- D (a<sub>1</sub>,a<sub>2</sub>)

#Q. Consider the following relationship entity diagram (ERD)



Which of the following possible relations will not hold if the above ERD is mapped into a relation model?

A

Person (NID, Name)

B

Qualification (NID, ExamID, QualifiedDate)

C

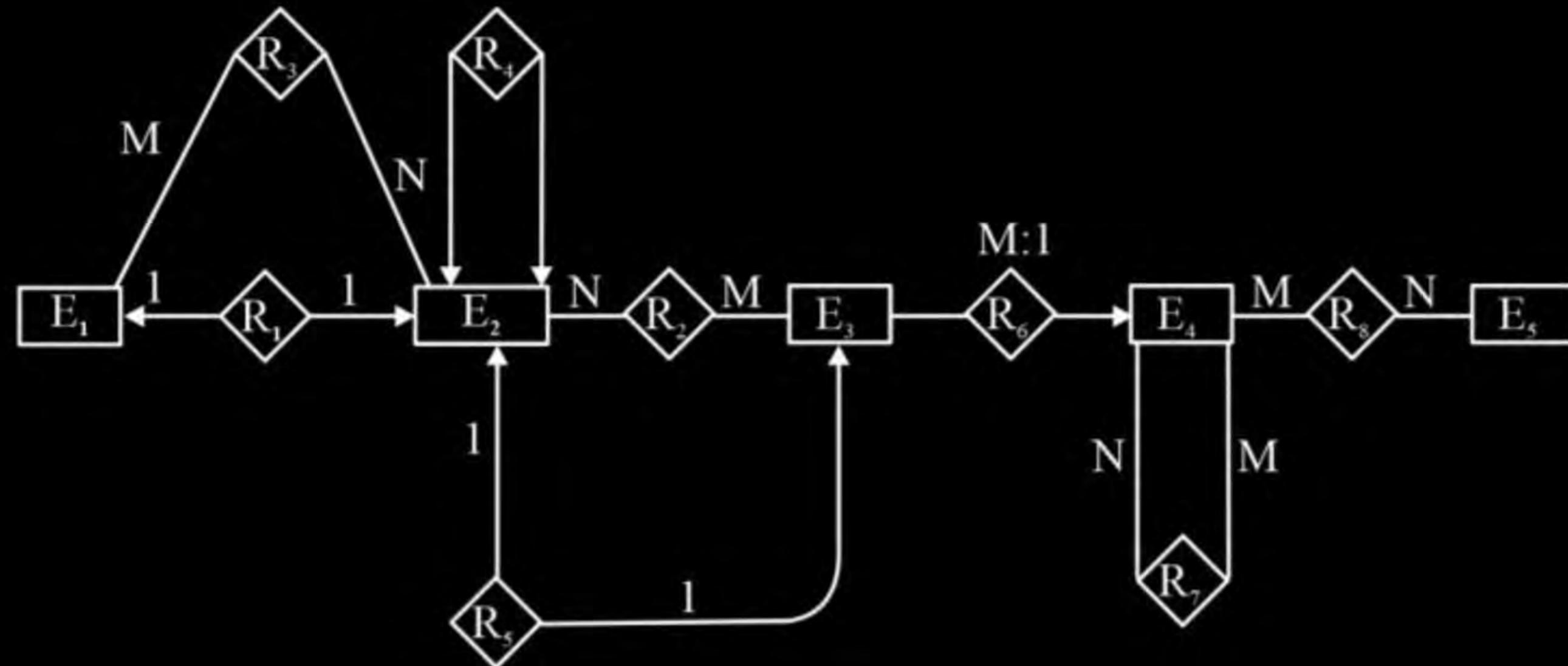
Exam (ExamID, NID, ExamName)

D

Exam (ExamID, ExamName)

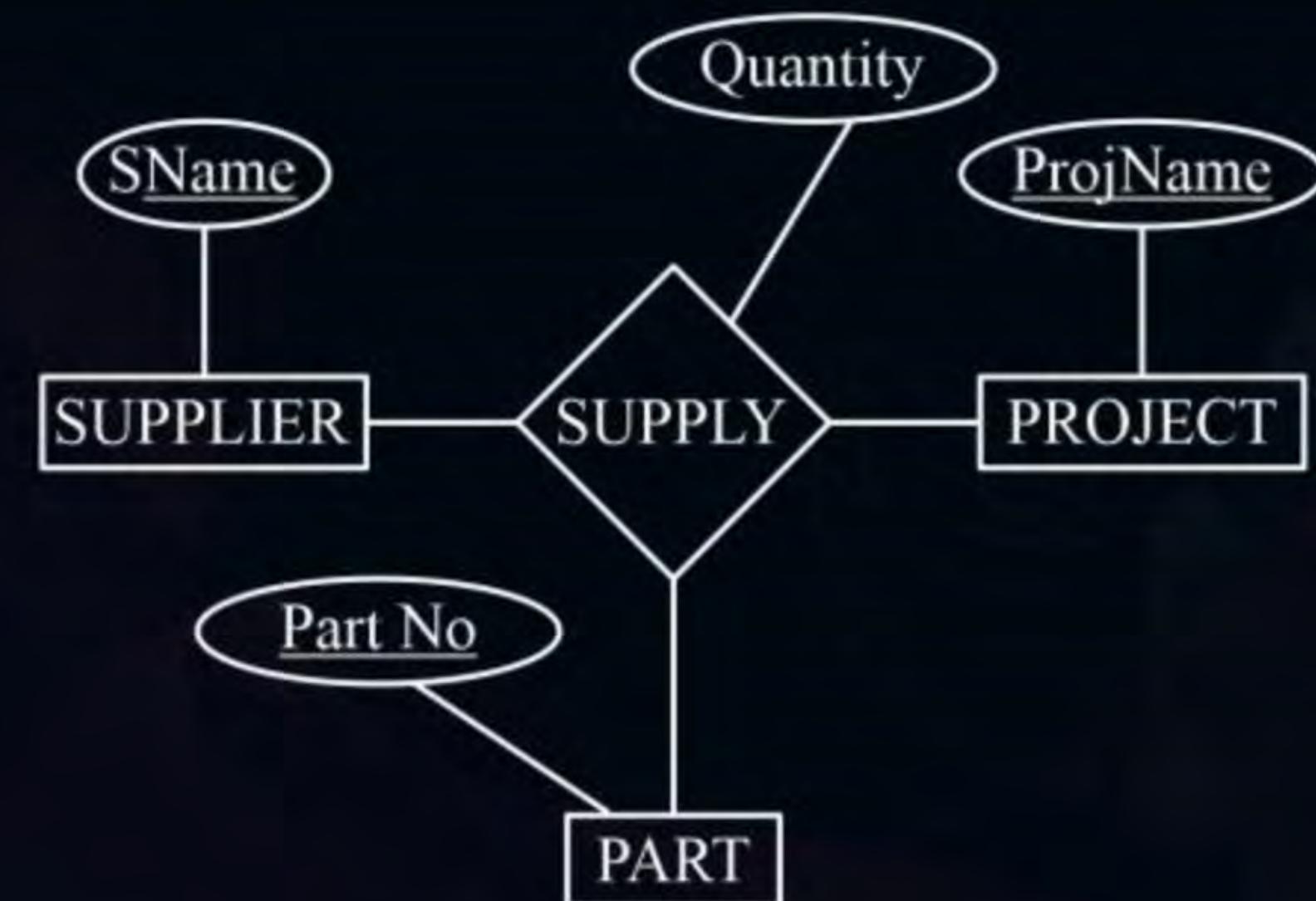
Consider the following ER diagram:

The minimum number of RDBMS table required for this ER diagram is \_\_\_\_.



#Q. What will be the number of relations if we follow ER-to-Relational Mapping Algorithm?

- A 3
- B 4
- C 5
- D 6





## 2 mins Summary



Topic

DBMS (Part 04)

Topic



THANK - YOU

# CS & IT ENGINEERING

Database  
Management System

Lecture No.- 05

By- Vijay Agarwal Sir



# Recap of Previous Lecture



Topic

ER Model Concept

Topic

ER Model to RDBMS Conversion

Topic

Foreign Key Concept

# Topics to be Covered



Topic

Foreign Key Concept

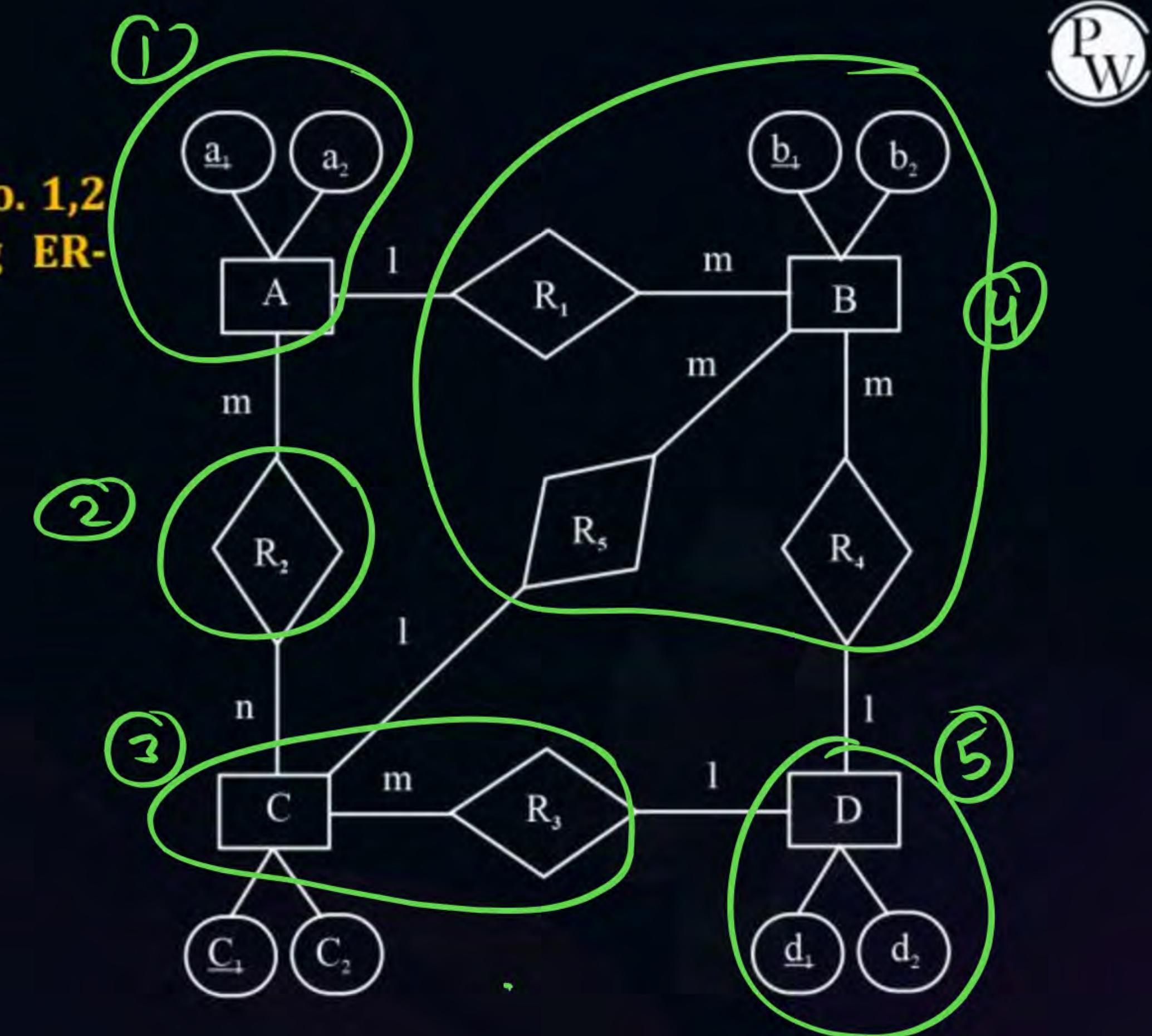
Topic

Relational Algebra

Topic

Structured Query Language

**Common data for Question No. 1,2  
& 3 Consider the following ER-  
diagram**



#Q. The minimum number of tables needed to represent A, B, C, D, R<sub>1</sub>, R<sub>2</sub>, R<sub>3</sub>, R<sub>4</sub>, R<sub>5</sub> is

A

3

C

5

B

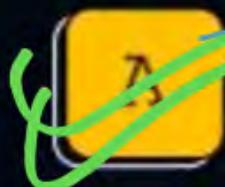
4

D

6

#Q. Above ER diagram, consists of Entity types B and D. These are connected by R4 which does not have its own attribute.

Which one of the following is correct?



A Relationship R4 is many to one so R4 can be merged with that of B.



B Relationship R4 is many to one so R4 can be merged with that of D.



C Both a and b

**Ans(A)**



D None of these

#Q. Which of the following is a correct attribute set for one of the tables for the correct answer to the above question?

A  $(a_1, b_1, c_1)$

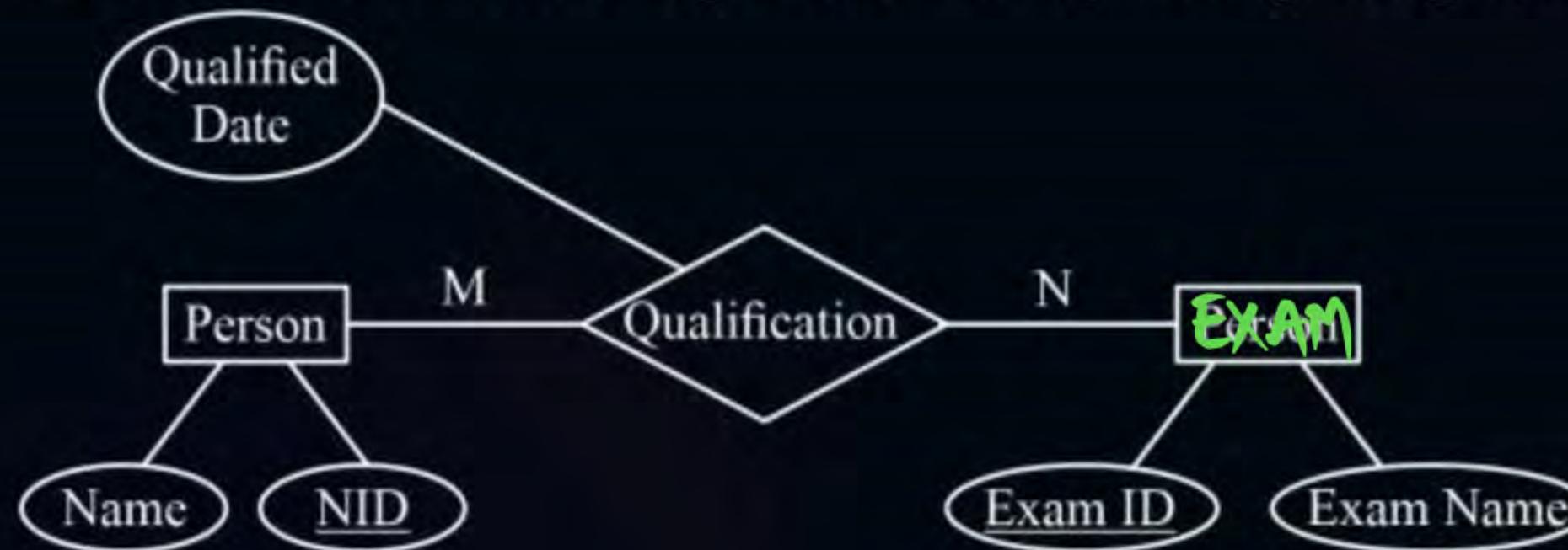
B  $(b_1, b_1, c_1, a_1)$

C  $(c_1, c_2)$

D  $(a_1, a_2)$

Ans (D).

#Q. Consider the following relationship entity diagram (ERD)



Ans (C).

Which of the following possible relations will not hold if the above ERD is mapped into a relation model?

A

Person (NID, Name)

B

Qualification (NID, ExamID, QualifiedDate)

C

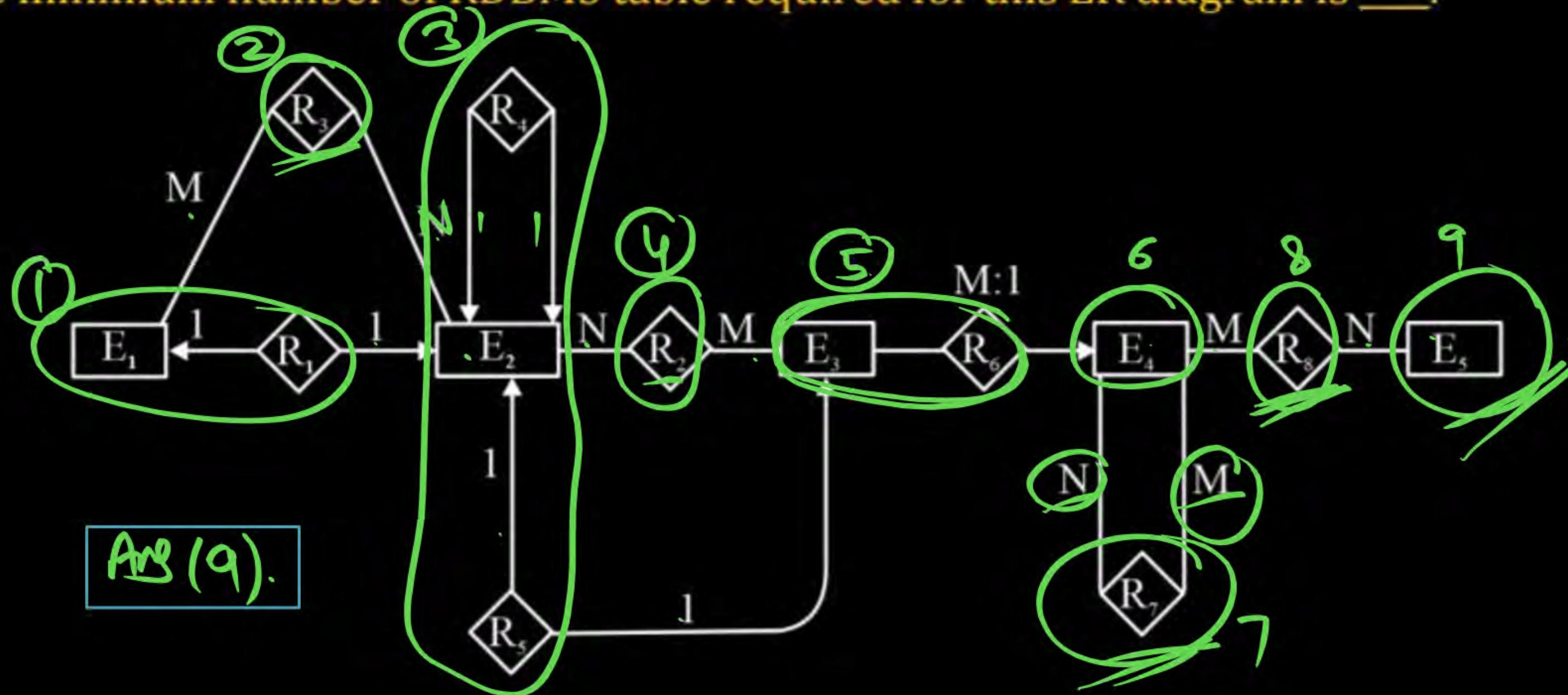
Exam (ExamID, NID, ExamName)

D

Exam (ExamID, ExamName)

Consider the following ER diagram:

The minimum number of RDBMS table required for this ER diagram is \_\_\_\_.



#Q. In SQL, relations can contain null values, and comparisons with null values are treated as unknown. Suppose all comparisons with null value are treated as false. Which of the following pairs in not equivalent?

- A     $x = 5, \text{not}(\text{not}(x = 5))$
- B     $x = 5, x > 4 \text{ and } x < 6 \text{ where } x \text{ is an integer}$
- C     $x \neq 5, \text{not}(x = 5)$
- D    None of the above

#Q. A table T1 in a relational database has the following rows and columns.

Roll no.	Marks
1	15
2	25
3	30
4	Null

The following sequence of SQL statements was successfully executed on table T1.

Update T1 set marks = marks + 5

Select avg(marks) from T1

What is the output of the select statement?

## Direction for the Question

A company maintains records of sales made by its salespersons and pays them commission based on each individual's total sales made in a year.

This data is maintained in a table with following schema:

`salesinfo = (salespersonid, totalsales, commission)`

In a certain year, due to better business results, the company decides to further reward its salespersons by enhancing the commission paid to them as per the following formula:

If `commission <= 50000`, enhance it by 2%

If `50000 < commission <= 100000`, enhance it by 4%

If `commission > 100000`, enhance it by 6%

The IT staff has written three different SQL scripts to calculate enhancement for each slab, each of these script is to run as a separate transaction as follows:

**Continues..**

T1 Update salesinfo

Set commission = commision \* 1.02

Where commission <= 50000;

T2 Update salesinfo

Set commission = commission \* 1.04

Where commission <= 50000 and commission

is <= 100000;

T3 Update salesinfo

Set commission = commission \* 1.06

Where commission > 100000;

Continues..

#Q. Which of the following options of running these transactions will update the commission of all salespersons correctly?

- A Execute T1 followed by T2 followed by T3
- B Execute T2, followed by T3; T1 running concurrently throughout
- C Execute T3, followed by T2; T1 running concurrently throughout
- D Execute T3 followed by T2 followed by T1

#Q. Which of the following query transformations (i.e. replacing the LHS expression by the RHS expression) is incorrect?  $R_1$  and  $R_2$  are relations,  $C_1, C_2$  are selection conditions and  $A_1, A_2$  are attributes of  $R_1$ ?

A

$$\sigma_{C1}(\sigma_{C2}(R_1)) \rightarrow \sigma_{C2}(\sigma_{C1}(R_1))$$

B

$$\sigma_{C1}(\pi_{A1}(R_1)) \rightarrow \pi_{A1}(\sigma_{C1}(R_1))$$

C

$$\sigma_{C1}(R_1 \cup R_2) \rightarrow \sigma_{C1}(R_1) \cup \sigma_{C1}(R_2)$$

D

$$\pi_{A1}(\sigma_{C1}(R_1)) \rightarrow \sigma_{C1}(\pi_{A1}((R_1)))$$

## Direction for Question



Consider a database with three relation instances shown below. The primary keys for the Drivers and Cars relation are did and cid respectively and the records are stored in ascending order of these primary keys as given in the table. No indexing is available in the database.

**D : Drivers relation**

did	dname	rating	Age
22	Karthikeyan	7	25
29	Salman	1	33
31	Boris	8	55
32	Amoldt	8	25
58	Schumacher	10	35
64	Sachin	7	35
71	Senna	10	16
74	Sachin	9	35
85	Rahul	3	25
95	Ralph	3	53

**R : Reserves relation**   **C : Cars relation**

did	cid	Day
22	101	10/10/06
22	102	10/10/06
22	103	08/10/06
22	104	07/10/06
31	102	10/11/06
31	103	06/11/06
31	104	12/11/06
64	101	05/09/06
64	102	08/09/06
74	103	08/09/06

did	cname	colour
101	Renault	Blue
102	Renault	Red
103	Ferrari	Green
104	Jaguar	red

#Q. What is the output of the following SQL query?

```
select D.dname
from Drivers D
where D.did in (
    select R.did
    from Cars C, Reserves R
    where R.cid=C.cid and C.colour = 'red'
    intersect
    select R.did
    from Cars C, Reserves R
    where R.cid=C.cid and C.colour='green')
```

A

Karthikeyan, Boris

B

Sachin, Salman

C

Karthikeyan, Boris, Sachin

D

Schumacher, Senna

#Q. The relation book (title, price) contains the titles and prices of different books. Assuming that no two books have the same price, what does the following SQL gives as output:

```
select title
  from book as B
 where (select count (*)
        from book as T
       where T. price > B. Price) < 5
```

A

Titles of the four most expensive books

B

Titles of the fifth most inexpensive books

C

Titles of the fifth most expensive books

D

Titles of the five most expensive books

#Q. Consider the table employee (empId, name, department, salary) and the two queries  $Q_1$ ,  $Q_2$  below. Assuming that department 5 has more than one employee, and we want to find the employees who get higher salary than anyone in the department 5, which one of the statements is TRUE of any arbitrary employee table?

$Q_1$  : Select e.empId  
From employee e  
Where not exists

(Select \* From employee s Where s.department = "5" and s.salary  
 $\geq e.salary$ )

$Q_2$  : Select e.empId  
From employee e  
Where e.salary > Any

(Select distinct salary From employee s Where s.department = "5")

- A Q<sub>1</sub> is the correct query
- B Q<sub>2</sub> is the correct query
- C Both Q<sub>1</sub> and Q<sub>2</sub> produce the same answer
- D Neither Q<sub>1</sub> nor Q<sub>2</sub> is the correct query

## Direction for Question



Consider two tables in a relational database with columns and rows as follows:

Table : Student

Roll_no	Name	Dept_id
1	ABC	1
2	DEF	1
3	GHI	2
4	JKL	3

Table : Department

Dept_id	Dept_name
1	A
2	B
3	C

Roll\_no is the primary key of the Student table, Dept\_id is the primary key of the Department table and Student. Dept\_id is a foreign key from Department. Dept\_id

#Q. What will happen if we try to execute the following two SQL statements?

- (i) update Student set Dept\_id = Null where Roll\_no = 1
- (ii) update department set Dept\_id = Null where Dept\_id = 10

- A Both (i) and (ii) will fail
- B (i) will fail but (ii) will succeed
- C (i) will succeed but (ii) will fail
- D Both (i) and (ii) will succeed

NULL  
UNKNOWN

Truth Table

NULL

unknown Value

Un existed Value

2 NULL are Not equal

Random ASCII Value  
Assigned by the DBMS.



# Topic : Database Management System



## NOTE:

- I. Arithmetic operation with NULL gives result NULL.

NULL

Any arithmetic  
operation

Any value = NULL (Result)



## Topic : Database Management System



II.

Comparison operation with NULL gives result unknown (Truth value)

NULL

Comparison  
operation

Anything = Unknown (Truth value)

$<$ ,  $>$ ,  $\leq$ ,  $\geq$ ,  $\neq$ ,  $=$

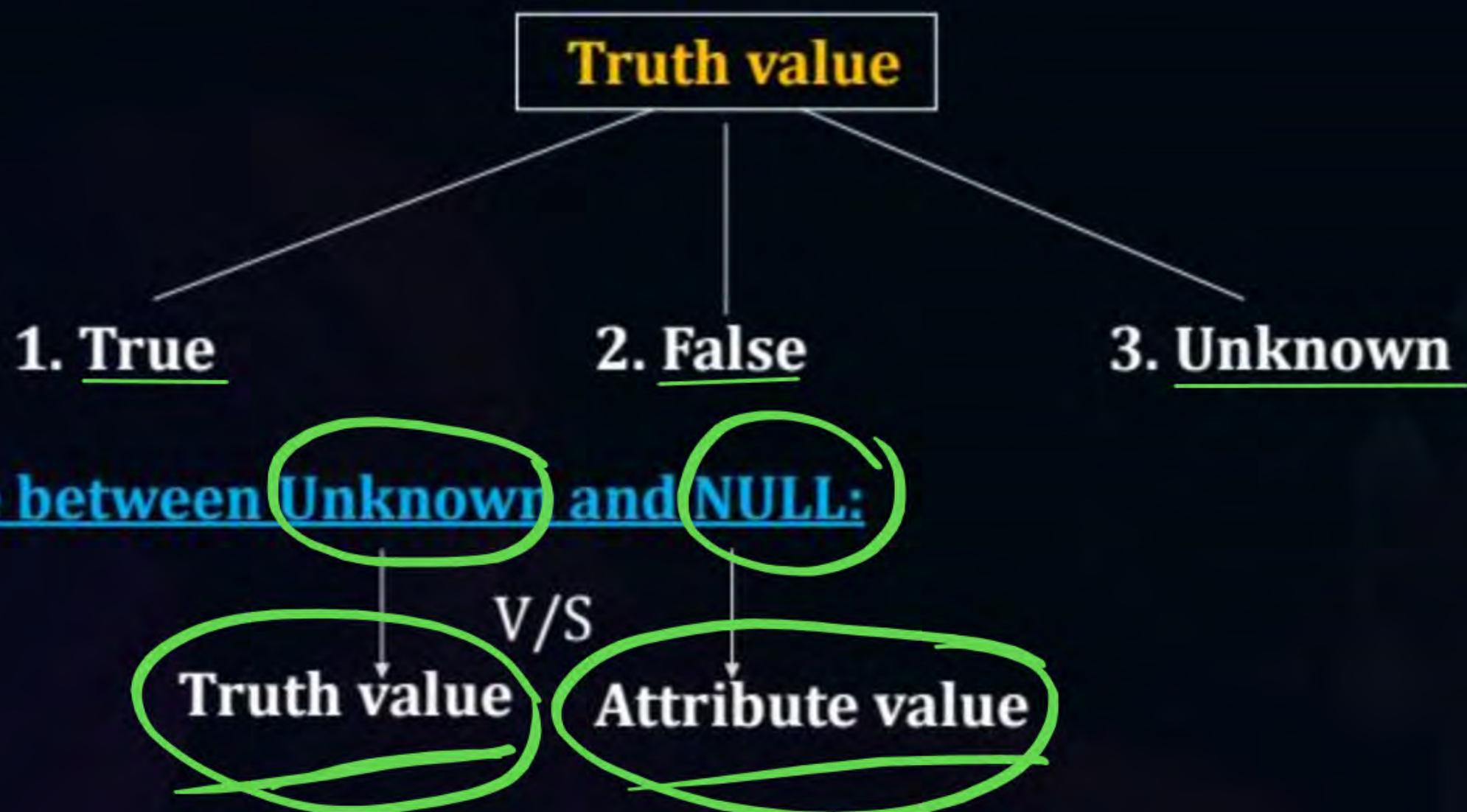
↑  
Not  
equal



# Topic : Database Management System

**NOTE:** Unknown is the third truth value.

In SQL



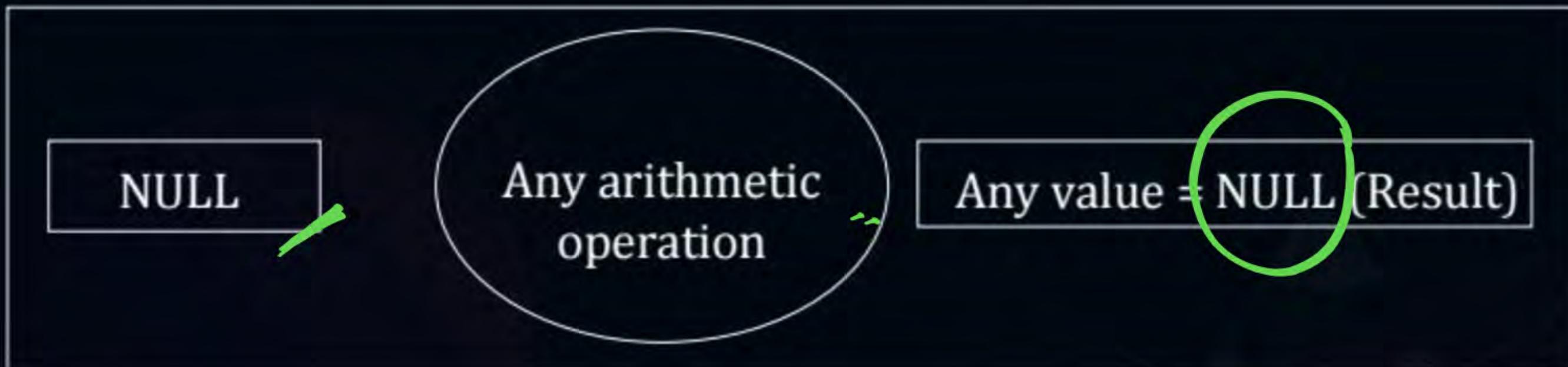


# Topic : Database Management System



**T:**

**NOTE:** Arithmetic operation with NULL gives result NULL.



**Example:**

$$\text{NULL} + \text{100} \Rightarrow \text{NULL}$$

$$\text{NULL} - \text{100} \Rightarrow \text{NULL}$$

$$\text{NULL} \times \text{100} \Rightarrow \text{NULL}$$

$$\text{NULL} \div \text{100} \Rightarrow \text{NULL}$$



# Topic : Database Management System

NOTE: ①

II. Comparison with NULL gives result unknown (Truth value)

NULL

Comparison  
operation

Anything = Unknown (Truth value)

<, >, <=, >=, <> =

Example:

NULL > 50  $\Rightarrow$  Unknown ✓

NULL = 100  $\Rightarrow$  Unknown ✓

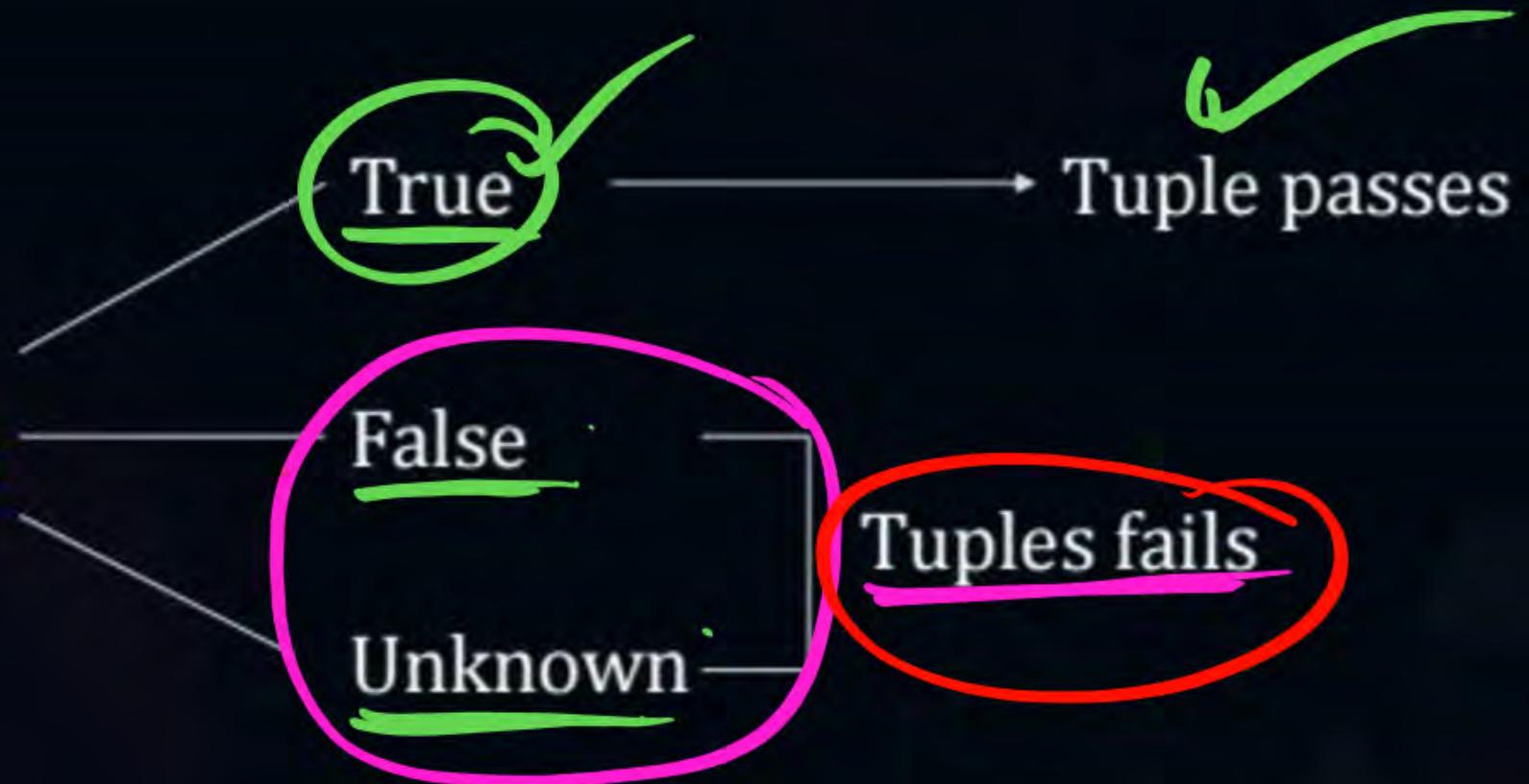
NULL = NULL  $\Rightarrow$  Unknown ✓

NULL <> 400  $\Rightarrow$  Unknown ✓

# Topic : Database Management System

NOTE:

In general : if  
Condition result



OR

Discard the tuple when result is false or unknown.

True [T] = 1

False [F] = 0

Unknown [U] =  $\frac{1}{2}$

$\text{NOT}(\text{True}) = \text{O}[F]$

$\text{NOT}(\text{False}) = \perp[T]$

$\text{NOT}(\text{Unknown}) = 1 - k = \frac{1}{2}(\text{unknown})$

$A \textcircled{OR} B = \max(A, B)$

$A \textcircled{AND} B = \min(A, B)$



# Topic : Database Management System



OR

Truth Table

OR (max) OPERATION	Truth	False	Unknown
True [1]	T	T	T
False [0]	T	F	U
Unknown [½]	T	U	U

Hint:

True = 1

False = 0

Unknown = 1/2

NOT  
operation

AND

min AND operation	Truth	False	Unknown
1 T	T	F	U
0 F	F	F	F
½ U	U	F	U

NOT(True) = False[0]

NOT[False] = True[1]

NOT[Unknown] = Unknown[1/2]

1 - 1/2 = ½ [Unknown]

Hint:

A or B = Max (A, B)

A and B = Min (A, B)

True = 1

False = 0

Unknown = 1/2

A **OR** B = Max(A, B)

A **AND** B = Min(A, B)

T: OR

False  $\vee$  False = F  $\Rightarrow \max(0, 0) = 0(F)$

True  $\vee$  False = T  $\Rightarrow \max(1, 0) = 1(F)$

True  $\vee$  True = T  $= \max(1, 1) = 1(T)$

False  $\vee$  True = T  $= \max(0, 1) = 1(\text{True})$

True = 1

False = 0

Unknown =  $\frac{1}{2}$

### AND

$$\text{True} \wedge \text{False} = \text{False}$$

$$\text{False} \wedge \text{True} = \text{False}$$

$$\text{True} \wedge \text{True} = \text{True}$$

$$\text{False} \wedge \text{False} = \text{False}$$

$$\min(1, 0) = 0[F]$$

$$\min(0, 1) = 0[F]$$

$$\min(1, 1) = 1[T]$$

$$\min(0, 0) = 0[F]$$

$$A \textcircled{OR} B = \text{Max}(A, B)$$

$$A \textcircled{AND} B = \text{Min}(A, B)$$



# Topic : Database Management System

Number 1 **AND** Number 2  $\Rightarrow$  Output minimum value

Number 1 **OR** Number 2  $\Rightarrow$  Output maximum value

$$A \text{ or } B = \underline{\text{Max}}(A, B)$$

$$A \text{ and } B = \underline{\text{Min}}(A, B)$$

False = 0

True = 1

OR

$$A \text{ or } B = \underline{\text{Max}}(A, B)$$

$$A \text{ and } B = \underline{\text{Min}}(A, B)$$

(**AND**)



F  $\vee$  F

I.

**OR**

Eg:  $\text{False} \vee \text{False} = \max(0, 0) = 0 = \underline{\text{False}}$

$\text{False} \vee \text{True} = \max(0, 1) = 1 = \underline{\text{True}}$

$\text{True} \vee \text{True} = \max(1, 1) = 1 = \underline{\text{True}}$



# Topic : Database Management System

II.

## AND

Eg:  $\text{True} \wedge \text{False} = \underline{\min}(1, 0) = \underline{0} = \text{False}$

$\text{True} \wedge \text{True} = \underline{\min}(1, 1) = \underline{1} = \text{True}$

$\text{False} \wedge \text{False} = \underline{\min}(0, 0) = \underline{0} = \text{False}$

True = 1

False = 0

Unknown = 1/2

NOT<sub>A</sub> = 1 - A

NOT (True) = False

NOT (false) = True

NOT (unknown) = unknown

NOT(True) = 1 - 1 = 0 [false]

NOT (False) = 1 - 0 = 1 [True]

NOT (unknown) = 1 - 1/2 = 1/2 [unknown]

True = 1

False = 0

Unknown =  $\frac{1}{2}$

A OR B = Max(A, B)

A AND B = Min(A, B)

T: 

False V Unknown = U  $\Rightarrow \max(0, \frac{1}{2}) = \frac{1}{2} [U]$

True V Unknown = T  $\Rightarrow \max(1, \frac{1}{2}) = 1 [T]$

Unknown V Unknown = U  $= \max(\frac{1}{2}, \frac{1}{2}) = \frac{1}{2} [U]$

True = 1

False = 0

Unknown =  $\frac{1}{2}$

### AND

True  $\wedge$  Unknown = U

False  $\wedge$  Unknown = F

Unknown  $\wedge$  Unknown = U

A  B = Max(A, B)

A  B = Min(A, B)

$\min(1, \frac{1}{2}) = \frac{1}{2} [U]$

$\min(0, \frac{1}{2}) = 0 [F]$

$\min(\frac{1}{2}, \frac{1}{2}) = \frac{1}{2} [U]$



# Topic : Database Management System



## OR (Max).

### Unknown Truth table

#### I. OR

Number 1 **OR** Number 2  $\rightarrow$  Output maximum value.

Unknown **OR** True = True

Unknown **OR** False = Unknown

Unknown **OR** Unknown = Unknown

#### Example

$\text{Max}(1/2, 1) = 1$  [True]

$\text{Max}(1/2, 0) = 1/2$  [Unknown]

$\text{Max}(1/2, 1/2) = 1/2$  [Unknown]



# Topic : Database Management System



Unknown Truth table

**AND**

II. **AND**

Number 1 **AND** Number 2  $\Rightarrow$  Output minimum value.

Unknown AND True = Unknown

Unknown AND False = False

Unknown AND Unknown = Unknown

**Example**

$\text{Min}(1/2, 1) = 1/2$  [Unknown]

$\text{Min}(1/2, 0) = 1/2$  [False]

$\text{Max}(1/2, 1/2) = 1/2$  [Unknown]



# Topic : Database Management System

## Hint:

True: 1

False 0

Unknown :  $\frac{1}{2}$

So Truth table

## Max

OR	True	False	Unknown
True	T	T	T
False	T	F	U
Unknown	T	U	U

## Min

AND	True	False	Unknown
True	T	F	U
False	F	F	F
Unknown	U	F	U



# Topic : Database Management System



OR

## Standard Book

x	y	x AND y	x OR y	NOT x
True	True	True	True	False
True	Unknown	Unknown	True	False
True	False	False	True	False
Unknown	True	Unknown	True	Unknown
Unknown	Unknown	Unknown	Unknown	Unknown
Unknown	False	False	Unknown	Unknown
False	True	False	True	True
False	Unknown	False	Unknown	True
False	False	False	False	False

Truth table for three-Valued logic

#Q. 1

Consider the following Query

X	Y
7	7
NULL	NULL
5	4
1	NULL
NULL	NULL
NULL	0
9	7

Select \*  
 FROM R  
 WHERE  $x - y = 0$

$x - y$  Comparison operator

- $= 0 = 0 \Rightarrow \text{True}$
- $= \text{NULL} = 0 = \text{Unknown}$
- $= 1 = 0 = \text{False}$
- $= \text{NULL} = 0 = \text{Unknown}$
- $= \text{NULL} = 0 = \text{Unknown}$
- $= \text{NULL} = 0 = \text{Unknown}$
- $= 2 = 0 = \text{False}$ .

Ans (1)

What is the number of tuples returned by the above SQL query?

Ans. (1)

Sol.

WHERE  $x - y = 0$  comparison operation

$$7 - 7 \Rightarrow 0$$

$$\text{Null} - \text{Null} \Rightarrow \text{Null}$$

$$5 - 4 \Rightarrow 1$$

$$1 - \text{Null} \Rightarrow \text{Null}$$

$$\text{Null} - \text{Null} \Rightarrow \text{Null}$$

$$\text{Null} - 0 \Rightarrow \text{Null}$$

$$9 - 7 = 2$$

$$= 0 \Rightarrow \text{True}$$

$$= 0 \Rightarrow \text{Unknown}$$

$$= 0 \Rightarrow \text{False}$$

$$= 0 \Rightarrow \text{Unknown}$$

$$= 0 \Rightarrow \text{Unknown}$$

$$= 0 \Rightarrow \text{Unknown}$$

$$= 0 \Rightarrow \text{False}$$

Only 1 tuple in the output.

X	Y
7	7
NULL	NULL
5	4
1	NULL
NULL	NULL
NULL	0
9	7

#Q. Consider the following SQL query:

R

A	B	C	
10	35	65	✓
20	45	60	✓
30	15	NULL	→ Unknown
40	25	55	→ False
50	30	70	✓

Select \*  
From R  
WHERE C > 55.

What is the number of tuples returned by the above SQL query?

Ans. (3)

Sol.

A	B	C
10	35	65
20	45	60
30	15	NULL
40	25	55
50	30	70

True ✓

True ✓

Unknown

False

True ✓

$C > 55$

3 Tuples returned in the output.

#Q. Consider the given relation R and S.

R(AB)	
A	B
5	16
8	9
11	5
14	7
17	6
20	3

C	S(CD)	D
8	9	
6	5	
11	3	
NULL	12	
16	13	
NULL	14	

Any  $\exists$  or

Select \*

FROM R

~~OR~~

WHERE B > Any (Select C from S)

The number of tuples return in the result of given SQL queries is \_\_\_\_\_

Ans. (3)

Sol. Any  $\Rightarrow$  Work like 'OR'

$B > \text{Any}$

$$\begin{pmatrix} 8 \\ 6 \\ 11 \\ \text{NULL} \\ 16 \\ \text{NULL} \end{pmatrix}$$

$16 > \text{Any}$

$$\begin{array}{ll} \begin{pmatrix} 8 \\ 6 \\ 11 \\ \text{NULL} \\ 16 \\ \text{NULL} \end{pmatrix} & \begin{array}{l} \text{True} \\ \text{True} \\ \text{True} \\ \text{Unknown} \\ \text{True} \\ \text{Unknown} \end{array} \\ \hline & \text{True} \end{array}$$

$9 > \text{Any}$

$$\begin{array}{ll} \begin{pmatrix} 8 \\ 6 \\ 11 \\ \text{NULL} \\ 16 \\ \text{NULL} \end{pmatrix} & \begin{array}{l} \text{True} \\ \text{True} \\ \text{False} \\ \text{Unknown} \\ \text{False} \\ \text{Unknown} \end{array} \\ \hline & \text{True} \end{array}$$

$5 > \text{Any}$

$$\begin{array}{ll} \begin{pmatrix} 8 \\ 6 \\ 11 \\ \text{NULL} \\ 16 \\ \text{NULL} \end{pmatrix} & \begin{array}{l} \text{False} \\ \text{False} \\ \text{False} \\ \text{Unknown} \\ \text{False} \\ \text{Unknown} \end{array} \\ \hline & \text{False} \end{array}$$

$$\begin{array}{ll} 7 > \text{Any} \\ \left( \begin{array}{c} 8 \\ 6 \\ 11 \\ \text{NULL} \\ 16 \\ \text{NULL} \end{array} \right) & \begin{array}{l} \text{False} \\ \text{True} \\ \text{False} \\ \text{Unknown} \\ \text{False} \\ \text{Unknown} \end{array} \\ \hline & \text{True} \end{array}$$

$$\begin{array}{ll} 6 > \text{Any} \\ \left( \begin{array}{c} 8 \\ 6 \\ 11 \\ \text{NULL} \\ 16 \\ \text{NULL} \end{array} \right) & \begin{array}{l} \text{False} \\ \text{False} \\ \text{False} \\ \text{Unknown} \\ \text{False} \\ \text{Unknown} \end{array} \\ \hline & \text{False} \end{array}$$

$$\begin{array}{ll} 3 > \text{Any} \\ \left( \begin{array}{c} 8 \\ 6 \\ 11 \\ \text{NULL} \\ 16 \\ \text{NULL} \end{array} \right) & \begin{array}{l} \text{ } \\ \text{ } \end{array} \\ \hline & \text{False} \end{array}$$

#Q. Consider the following Query:

```
Select *  
FROM R  
WHERE A > 6 and (B > C or C > 5)
```

R

A	B	C
5	8	NULL
9	NULL	9
11	7	5
NULL	9	7

What is the number of tuple (record) resulted by the above SQL query.

Ans.

Sol.

A	B	C
5	8	NULL
9	NULL	9
11	7	5
Null (1)	9	7

$A > 6 \text{ and } (B > C \text{ or } C > 5)$

A	B	C
5	8	NULL

$A > 6 \text{ and } (B > C \text{ or } C > 5)$

False and (unknown or unknown)

False and Unknown = False

(ii)

A	B	C
9	NULL	9

$A > 6$  and  $(B > C \text{ or } C > 5)$

True and (unknown or True)

True and True = True.

This tuple return in the output.

(iii)

A	B	C
11	7	5

$A > 6$  and  $(B > C \text{ or } C > 5)$

True and (True or False)

True and True = True.

This tuple return in the output.

(iv)

A	B	C
NULL	9	7

$$A > 6 \text{ and } (B > C \text{ or } C > 5)$$

unknown AND (True or True)

Unknown AND True = unknown.

So, 2 tuple in the output.

A	B	C
9	NULL	9
11	7	5

#Q. In SQL, relations can contain null values, and comparisons with null values are treated as unknown. Suppose all comparisons with null value are treated as false. Which of the following pairs in not equivalent?

A  $x = 5, \text{not}(\text{not}(x = 5))$

B  $\underline{x = 5}, x > 4 \text{ and } x < 6$  where x is an integer

C  $\underline{x \neq 5}, \text{not}(\underline{x = 5})$

D None of the above

$x=5$  ?

$x=5$

$x \neq 5$

$x=NULL$ .



## 2 mins Summary



Topic

DBMS (Part 05)

Topic



THANK - YOU

# CS & IT ENGINEERING

Database  
Management System

Lecture No.- 06

By- Vijay Agarwal Sir



# Recap of Previous Lecture



Topic

Foreign Key Concept

Topic

Relational Algebra

Topic

Structured Query Language

# Topics to be Covered



Topic

Relational Algebra

Topic

Structured Query Language

#Q. A table T1 in a relational database has the following rows and columns.

Roll no.	Marks
1	15
2	25
3	30
4	Null

R.No	Marks
1	20
2	30
3	35
4	NULL

$$\frac{20+30+35}{3} = \frac{85}{3} = 28.3$$

The following sequence of SQL statements was successfully executed on table T1.

Update T1 set marks = marks + 5

Select avg(marks) from T1

What is the output of the select statement? \_\_\_\_\_

$$\text{NULL} + 5 = \text{NULL}$$

**Note** Aggregate function (min, max, AVG, SUM, Count) Always  
Discard / Ignore the NULL Value then Perform the  
Operation.

## Direction for the Question

A company maintains records of sales made by its salespersons and pays them commission based on each individual's total sales made in a year.

This data is maintained in a table with following schema:

`salesinfo = (salespersonid, totalsales, commission)`

In a certain year, due to better business results, the company decides to further reward its salespersons by enhancing the commission paid to them as per the following formula:

If  $\text{commission} \leq 50000$ , enhance it by 2%

If  $50000 < \text{commission} \leq 100000$ , enhance it by 4%

If  $\text{commission} > 100000$ , enhance it by 6%

The IT staff has written three different SQL scripts to calculate enhancement for each slab, each of these script is to run as a separate transaction as follows:

Continues..

T1 Update salesinfo

Set commission = commision \* 1.02

Where commission <= 50000;

T2 Update salesinfo

Set commission = commission \* 1.04

Where commission <= 50000 and commission

is <= 100000;

T3 Update salesinfo

Set commission = commission \* 1.06

Where commission > 100000;

$T_b < T_1, T_2, T_3$

$\text{es } 49990 + 2\%$

$T_1 < 50000$

$\Rightarrow 50k$

$T_2 \underline{50k \text{ to } 1 \text{ Lakh}} \Rightarrow 4\%$

$T_3 > 1 \text{ Lakh}$

$99990 \Rightarrow 4\% \Rightarrow 1.01 \text{ Lakh}$

$T_3 6\%$

Continues..

#Q. Which of the following options of running these transactions will update the commission of all salespersons correctly?

A

Execute T1 followed by T2 followed by T3

B

Execute T2, followed by T3; T1 running concurrently throughout

C

Execute T3, followed by T2: T1 running concurrently throughout

D

Execute T3 followed by T2 followed by T1

#Q. Which of the following query transformations (i.e. replacing the LHS expression by the RHS expression) is incorrect?  $R_1$  and  $R_2$  are relations,  $C_1, C_2$  are selection conditions and  $A_1, A_2$  are attributes of  $R_1$ ?

A

$$\sigma_{C1}(\sigma_{C2}(R_1)) \rightarrow \sigma_{C2}(\sigma_{C1}(R_1))$$

B

$$\sigma_{C1}(\pi_{A1}(R_1)) \rightarrow \pi_{A1}(\sigma_{C1}(R_1))$$

C

$$\sigma_{C1}(R_1 \cup R_2) \rightarrow \sigma_{C1}(R_1) \cup \sigma_{C1}(R_2)$$

D

$$\pi_{A1}(\sigma_{C1}(R_1)) \rightarrow \sigma_{C1}(\pi_{A1}((R_1)))$$

## Direction for Question

Consider a database with three relation instances shown below. The primary keys for the Drivers and Cars relation are did and cid respectively and the records are stored in ascending order of these primary keys as given in the table. No indexing is available in the database.

**D: Drivers relation**

did	dname	rating	Age
22	Karthikeyan	7	25
29	Salman	1	33
31	Boris	8	55
32	Amoldt	8	25
58	Schumacher	10	35
64	Sachin	7	35
71	Senna	10	16
74	Sachin	9	35
85	Rahul	3	25
95	Ralph	3	53

**R : Reserves relation**   **C : Cars relation**

did	cid	Day
22	101	10/10/06
22	102	10/10/06
22	103	08/10/06
22	104	07/10/06
31	102	10/11/06
31	103	06/11/06
31	104	12/11/06
64	101	05/09/06
64	102	08/09/06
74	103	03/09/06

did	cname	colour
101	Renault	Blue
102	Renault	Red
103	Ferrari	Green
104	Jaguar	Red

Red Did : [22, 22, 31, 31, 64]

INTERSECT

GREEN Did [22, 31, 74]

22, 31

#Q. What is the output of the following SQL query?

```
select D.dname
```

```
from Drivers D
```

```
where D.did in
```

22. BL

```
select R.did
```

```
from Cars C, Reserves R
```

```
where R.cid=C.cid and C.colour = 'red'
```

```
intersect
```

```
select R.did
```

```
from Cars C, Reserves R
```

```
where R.cid=C.cid and C.colour='green')
```

A

Karthikeyan, Boris

B

Sachin, Salman

C

Karthikeyan, Boris, Sachin

D

Schumacher, Senna

**[MCQ]**

#Q. The relation book (title, price) contains the titles and prices of different books. Assuming that no two books have the same price, what does the following SQL gives as output:

```
select title
from book as B
where (select count (*)
       from book as T
      where T. price > B. Price) < 5
```

A Titles of the four most expensive books

B Titles of the fifth most inexpensive books

C Titles of the fifth most expensive books

D Titles of the five most expensive books

T	B
A	10
B	20
C	30
D	40
E	50
F	2
G	60
H	5

#Q. Consider the table employee (empId, name, department, salary) and the two queries  $Q_1$ ,  $Q_2$  below. Assuming that department 5 has more than one employee, and we want to find the employees who get higher salary than anyone in the department 5, which one of the statements is TRUE of any arbitrary employee table?

$Q_1$  : Select e.empId  
From employee e  
Where not exists

(Select \* From employee s Where s.department = "5" and s.salary  
 $\geq e.salary$ )

$Q_2$  : Select e.empId  
From employee e  
Where e.salary > Any

(Select distinct salary From employee s Where s.department = "5")

- A Q<sub>1</sub> is the correct query
- B Q<sub>2</sub> is the correct query
- C Both Q<sub>1</sub> and Q<sub>2</sub> produce the same answer
- D Neither Q<sub>1</sub> nor Q<sub>2</sub> is the correct query

## Direction for Question



Consider two tables in a relational database with columns and rows as follows:

Table : Student

Roll_no	Name	Dept_id
1	ABC	1
2	DEF	1
3	GHI	2
4	JKL	3

Table : Department

Dept_id	Dept_name
1	A
2	B
3	C

Roll\_no is the primary key of the Student table, Dept\_id is the primary key of the Department table and Student. Dept\_id is a foreign key from Department. Dept\_id

#Q. What will happen if we try to execute the following two SQL statements?

- (i) update Student set Dept\_id = Null where Roll\_no = 1
- (ii) update department set Dept\_id = Null where Dept\_id = 10

- A Both (i) and (ii) will fail
- B (i) will fail but (ii) will succeed
- C (i) will succeed but (ii) will fail
- D Both (i) and (ii) will succeed

UNKNOWN

True : 1

False : 0

Unknown :  $\frac{1}{2}$

$A \text{ (OR) } B \Rightarrow \text{Max}(A, B)$

$A \text{ (AND) } B = \text{Min}(A, B)$ .



# Topic : Database Management System

## NOTE:

- I. Arithmetic operation with NULL gives result NULL.

NULL

Any arithmetic  
operation

Any value = NULL (Result)



## Topic : Database Management System



- II. Comparison operation with NULL gives result unknown (Truth value)

NULL

Comparison  
operation

<, >, <=, >=, < >

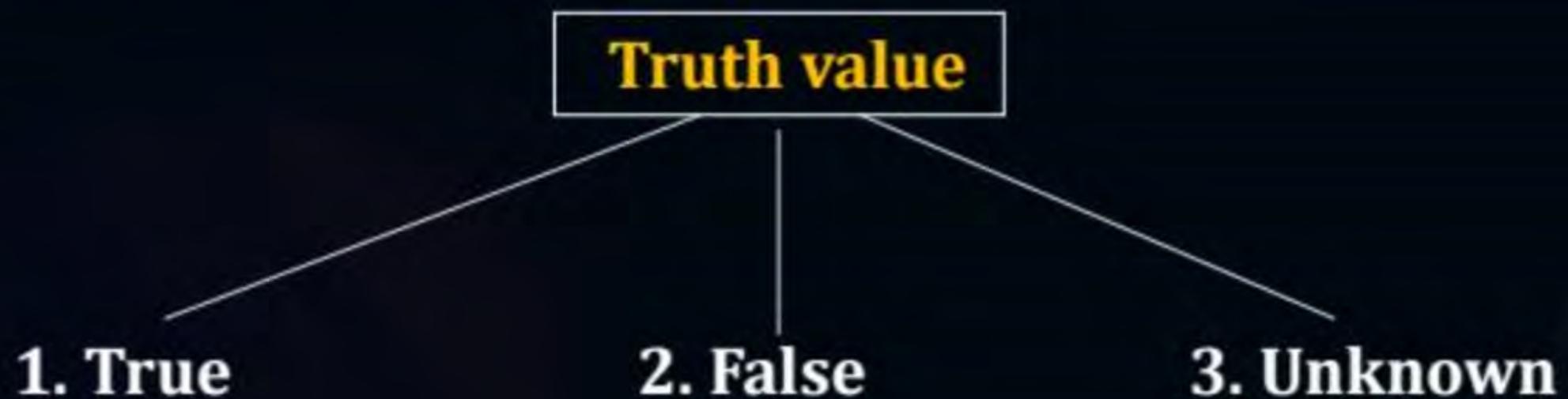
Anything = Unknown (Truth value)



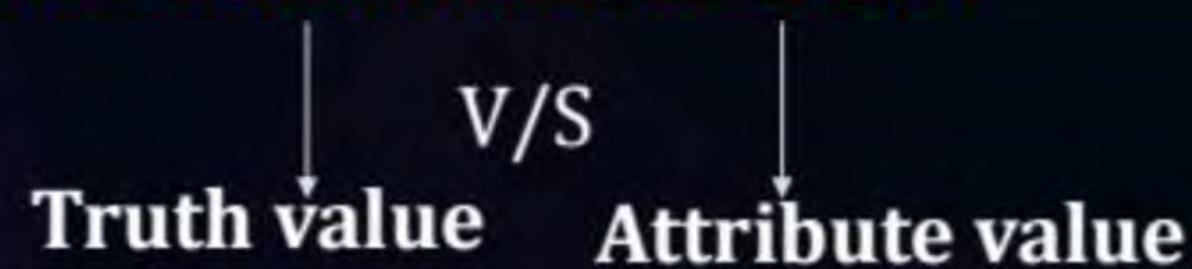
# Topic : Database Management System

**NOTE:** Unknown is the third truth value.

In SQL



**Difference between Unknown and NULL:**





# Topic : Database Management System

**NOTE:** Arithmetic operation with NULL gives result NULL.

NULL

Any arithmetic  
operation

Any value = NULL (Result)



**Example:**

$$\text{NULL} + 100 \Rightarrow \text{NULL}$$

$$\text{NULL} - 100 \Rightarrow \text{NULL}$$

$$\text{NULL} \times 100 \Rightarrow \text{NULL}$$

$$\text{NULL} \div 100 \Rightarrow \text{NULL}$$



# Topic : Database Management System



## NOTE:

II. Comparison with NULL gives result unknown (Truth value)

NULL

Comparison  
operation

Anything = Unknown (Truth value)

<, >, <=, >=, <>

## Example:

$\text{NULL} > 50 \Rightarrow \text{Unknown}$

$\text{NULL} = 100 \Rightarrow \text{Unknown}$

$\text{NULL} = \text{NULL} \Rightarrow \text{Unknown}$

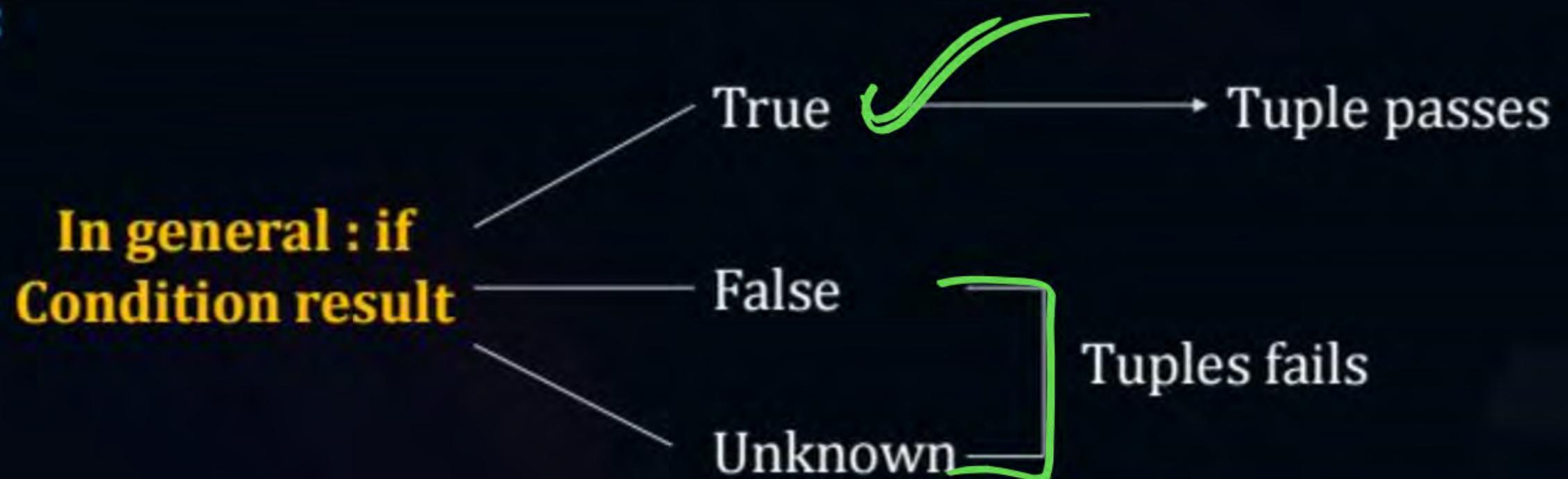
$\text{NULL} <> 400 \Rightarrow \text{Unknown}$



# Topic : Database Management System



**NOTE:**



**OR**

Discard the tuple when result is false or unknown.



# Topic : Database Management System

## Truth Table

OR (Max)		Truth	False	Unknown	Min		AND		Truth	False	Unknown
		T	F	U	T	F	F	T	F	U	
True	0	T	T	T	T	F	F	T	F	U	
False	1	T	F	U	F	F	F	F	F	F	
Unknown	2	T	U	U	U	U	U	U	F	U	

Hint:

True = 1

False = 0

Unknown = 1/2

NOT(True) = False[0]

NOT[False] = True[1]

NOT[Unknown] = Unknown[1/2]

1 - 1/2 = 1/2 [Unknown]

Hint:

A or B = Max (A, B)

A and B = Min (A, B)



# Topic : Database Management System

Number 1 AND Number 2  $\Rightarrow$  Output minimum value

Number 1 AND Number 2  $\Rightarrow$  Output maximum value

$$A \text{ or } B = \underline{\text{Max}}(A, B)$$

$$A \text{ and } B = \underline{\text{Min}}(A, B)$$

OR

$$A \vee B = \text{Max}(A, B)$$

$$A \wedge B = \text{Min}(A, B)$$

False = 0

True = 1

## I. OR

Eg:  $\text{False} \vee \text{False} = \text{max}(0, 0) = 0 = \text{False}$

$\text{False} \vee \text{True} = \text{max}(0, 1) = 1 = \text{True}$

$\text{True} \vee \text{True} = \text{max}(1, 1) = 1 = \text{True}$



# Topic : Database Management System

## II. AND

Eg:  $\text{True} \wedge \text{False} = \min(1, 0) = 0 = \text{False}$

$\text{True} \wedge \text{True} = \min(1, 1) = 1 = \text{True}$

$\text{False} \wedge \text{False} = \min(0, 0) = 0 = \text{False}$

True = 1

False = 0

Unknown = 1/2

$\text{NOT}_A = 1 - A$

$\text{NOT}(\text{True}) = \text{False}$

$\text{NOT}(\text{false}) = \text{True}$

$\text{NOT}(\text{unknown}) = \text{unknown}$

$\text{NOT}(\text{True}) = 1 - 1 = 0$  [false]

$\text{NOT}(\text{False}) = 1 - 0 = 1$  [True]

$\text{NOT}(\text{unknown}) = 1 - \frac{1}{2} = \frac{1}{2}$  [unknown]



# Topic : Database Management System

## Unknown Truth table

### I. OR

Number 1 **OR** Number 2  $\rightarrow$  Output maximum value.

### Example

Unknown **OR** True = True

$\text{Max}(1/2, 1) = 1$  [True]

Unknown **OR** False = Unknown

$\text{Max}(1/2, 0) = 1/2$  [Unknown]

Unknown **OR** Unknown = Unknown

$\text{Max}(1/2, 1/2) = 1/2$  [Unknown]



# Topic : Database Management System

## Unknown Truth table

### II. AND

Number 1 AND Number 2  $\Rightarrow$  Output minimum value.

#### Example

Unknown AND True = Unknown

$\text{Min}(1/2, 1) = 1/2$  [Unknown]

Unknown AND False = False

$\text{Min}(1/2, 0) = 1/2$  [False]

Unknown AND Unknown = Unknown

$\text{Max}(1/2, 1/2) = 1/2$  [Unknown]



# Topic : Database Management System

## Hint:

True: 1

False 0

Unknown :  $\frac{1}{2}$

So Truth table

## Max

OR	True	False	Unknown
True	T	T	T
False	T	F	U
Unknown	T	U	U

## Min

AND	True	False	Unknown
True	T	F	U
False	F	F	F
Unknown	U	F	U



# Topic : Database Management System



**OR**

x	y	x AND y	x OR y	NOT x
True	True	True	True	False
True	Unknown	Unknown	True	False
True	False	False	True	False
Unknown	True	Unknown	True	Unknown
Unknown	Unknown	Unknown	Unknown	Unknown
Unknown	False	False	Unknown	Unknown
False	True	False	True	True
False	Unknown	False	Unknown	True
False	False	False	False	False

Truth table for three-Valued logic

#0: Consider the following Query

X	Y
7	7
NULL	NULL
5	4
1	NULL
NULL	NULL
NULL	0
9	7

```
Select *  
FROM R  
WHERE x - y = 0
```

What is the number of tuples returned by the above SQL query?

Ans. (1)

Sol. WHERE  $x - y = 0$  comparison operation

$$7 - 7 \Rightarrow 0$$

$$\text{Null} - \text{Null} \Rightarrow \text{Null}$$

$$5 - 4 \Rightarrow 1$$

$$1 - \text{Null} \Rightarrow \text{Null}$$

$$\text{Null} - \text{Null} \Rightarrow \text{Null}$$

$$\text{Null} - 0 \Rightarrow \text{Null}$$

$$9 - 7 = 2$$

$= 0 \Rightarrow \text{True}$

$= 0 \Rightarrow \text{Unknown}$

$= 0 \Rightarrow \text{False}$

$= 0 \Rightarrow \text{Unknown}$

$= 0 \Rightarrow \text{Unknown}$

$= 0 \Rightarrow \text{Unknown}$

$= 0 \Rightarrow \text{False}$

Only 1 tuple in the output.

X	Y
7	7
NULL	NULL
5	4
1	NULL
NULL	NULL
NULL	0
9	7

#Q. 2

Consider the following SQL query:

R

A	B	C
10	35	65
20	45	60
30	15	NULL
40	25	55
50	30	70

T

Unknown

False

True

Select \*

From R

WHERE C > 55.

What is the number of tuples returned by the above SQL query?

Ans. (3)

Sol.

A	B	C
10	35	65
20	45	60
30	15	NULL
40	25	55
50	30	70

True

True

Unknown

False

True

$C > 55$

3 Tuples returned in the output.

#Q.3

Consider the given relation R and S.

R(AB)	
A	B
5	16
8	9
11	5
14	7
17	6
20	3

C	S(CD)
8	9
6	5
11	3
NULL	12
16	13
NULL	14

16 > ANY

8 → T
6 → T
11 → T
NULL → U
16 → F
NULL → U

True

Ans(3)

Select \*

FROM R

WHERE B &gt; ANY (Select C from S)

The number of tuples return in the result of given SQL queries is \_\_\_\_\_

Ans. (3)

Sol. Any  $\Rightarrow$  Work like 'OR'

$B > \text{Any}$

8	
6	
11	
NULL	
16	
NULL	

$\checkmark 16 > \text{Any}$

8	True
6	True
11	True
NULL	Unknown
16	False
NULL	Unknown

---

True

$9 > \text{Any}$

8	True
6	True
11	False
NULL	Unknown
16	False
NULL	Unknown

---

True

$5 > \text{Any}$

8	False
6	False
11	False
NULL	Unknown
16	False
NULL	Unknown

---

Unknown

7 > Any	
8	False
6	True
11	False
NULL	Unknown
16	False
NULL	Unknown
<hr/>	
True	

6 > Any	
8	False
6	False
11	False
NULL	Unknown
16	False
NULL	Unknown
<hr/>	
Unknown	

3 > Any	
8	F
6	F
11	F
NULL	U
16	F
NULL	U
<hr/>	
<del>False</del> Unknown	

**[MCQ]**P  
W

#Q4

Consider the following Query:

Select \*

FROM R

WHERE A &gt; 6 and (B &gt; C or C &gt; 5)

R

A	B	C
5	8	NULL
9	NULL	9
11	7	5
NULL	9	7

What is the number of tuple (record) resulted by the above SQL query.

A > 6 **AND** (B > C **or** C > 5)5 > 6 **[F]** **AND** (Unk **or** U. = False)

Ans.

Sol.

② Ans

A	B	C
5	8	NULL
9	NULL	9
11	7	5
Null (1)	9	7

 $A > 6 \text{ and } (B > C \text{ or } C > 5)$ 1<sup>st</sup> Tuple

A	B	C
5	8	NULL

 $A > 6 \text{ and } (B > C \text{ or } C > 5)$ False and (unknown or unknown)False and Unknown = False

✓ (ii)

A	B	C
9	NULL	9

A > 6 and (B > C or C > 5)

True and (unknown or True)

True and True = True.

This tuple return in the output.

✓ (iii)

A	B	C
11	7	5

A > 6 and (B > C or C > 5)

True and (True or False)

True and True = True.

This tuple return in the output.

(iv)

A	B	C
NULL	9	7

$$A > 6 \text{ and } (B > C \text{ or } C > 5)$$
unknown AND (True or True)Unknown AND True = unknown.

So, 2 tuple in the output.

A	B	C
9	NULL	9
11	7	5

#Q.

In SQL, relations can contain null values, and comparisons with null values are treated as unknown. Suppose all comparisons with null value are treated as false. Which of the following pairs in not equivalent?

A

$x = 5, \text{not}(\text{not}(x = 5))$  Equivalent

B

$x = 5, x > 4 \text{ and } x < 6$  where  $x$  is an integer Equivalent.

C

$x \neq 5, \text{not}(x = 5)$

D

None of the above

@  $x=5, \quad \text{not}(\text{not}(x=5))$

$x=5$

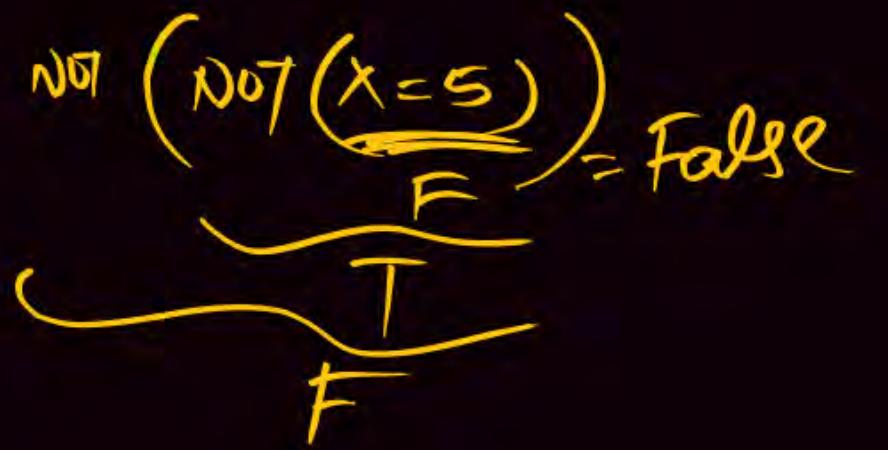
L.H.S  $\Rightarrow$  True

R.H.S  $\text{not}(\text{not}(x=5))$ : Tree.



$x \neq 5$

$x \neq 5 : \text{False}$



$x=\text{NULL}$

$x=\text{NULL} \Rightarrow \text{False}$

$\text{not}(\text{not}(x=\text{NULL})) = \text{False}$

b)  $x=5$ ,  $x > 4 \ \& \ (x < 6)$   $x$  is an integer

$x=5$

$x=5$  True

$T \& T = \text{True}$

$x \neq 5$

$x \neq 5$  : False

$F \& T = \text{False}$   
 $T \& F = \text{False}$

$x=\text{NULL}$

$x=\text{NULL} \Rightarrow \text{False}$

$\underline{N} \& \underline{N} = \text{False}$

①  $x \neq 5, \quad \text{NOT}(x=5)$

$x=5$

$x \neq 5$ : False

$\text{NOT } \underbrace{x=5}_{T} = \text{False}$   
 $\underbrace{\text{F}}_{F}$

$x \neq 5$

L.H.S = True

RHS

$\text{NOT } \underbrace{x=5}_{F} = \text{True}$   
 $\underbrace{\text{True}}_{\text{True}}$

$x=\text{NULL}$

$x=\text{NULL} = \text{False}$

$\text{NOT } (x=\text{NULL})$   
 $\underbrace{\text{False}}_{\text{True}}$   
 $\underbrace{\text{True}}_{\text{True}}$

Consider the relation R and S & following Query Executed.

SELECT \*  
FROM R

WHERE A >  $\left( \begin{array}{l} \text{SELECT Count(*)} \\ \text{FROM } S \\ \text{WHERE } \underline{RC=SC} \end{array} \right)$

R (ABC)			S (CDE)		
A	B	C	C	D	E
1	7	5	5	5	3
3	3	6	6	2	8
5	4	7	6	4	1

Ans (2)

The number of tuples Returned by the above query is \_\_\_\_\_.

$\boxed{1 \ 7 \ 5} \Rightarrow \text{Count} = 1 \Rightarrow A > \text{Count} \Rightarrow 1 > 1 \Rightarrow \text{False}$

$\boxed{3 \ 3 \ 6} \Rightarrow \text{Count} = 2 \Rightarrow A > \text{Count} \Rightarrow 3 > 2 \Rightarrow \text{True} \checkmark$

$\boxed{5 \ 4 \ 7} \Rightarrow \text{Count} = 0 \Rightarrow A > \text{Count} \Rightarrow 5 > 0 : \text{True} \checkmark$

#Q.  $[(\text{Select eno from emp where deptno} = 10) \text{ UNION}$   
 $(\text{Select eno from emp where deptno} = 20)]$  is query 1,  
 $(\text{Select eno from emp where deptno} = 10 \text{ or}$   
 $\text{deptno} = 20)$  is query 2

- I. Query 1 and Query 2 give same no. of rows.
- II. Query 1 and Query 2 gives same no. of rows if there are no duplicates in  
eno.
- III. The output of query 1 and query 2 look alike row by row if eno is a primary key for the relation emp.

A

I only

C

III only

B

II only

D

I & III

#Q. Select ename

From deposit

Where bal < any (select assets from branch);

What is the output of the above query?

10  
20  
30  
40

A

It prints the customer names whose balance amount is greater than at least one asset.

B

It prints the customer names whose balance amount is less than at least one asset.

C

It prints the customer names whose balance amount is less than maximum amount of assets.

D

None of the above

**H.W**

#Q. Consider the Query

```
SELECT student name FROM student WHERE class name = (SELECT class-  
name FROM students WHERE math_marks = 100);
```

What will be the output?

A

The list of names of student with 100 marks in mathematics.

B

The names of all students of all classes in which at least one student has 100 marks in mathematics.

C

The names of all students in all classes having 100 marks in mathematics.

D

The names and class of all students whose marks in mathematics is 100.

#Q. Consider the following ORACLE relations:

$$R(A, B, C) = \{<1, 2, 3>, <1, 2, 0>, <1, 3, 1>, <6, 2, 3>, <1, 4, 2>, <3, 1, 4>\}$$

$$S(B, C, D) = \{<2, 3, 7>, <1, 4, 5>, <1, 2, 3>, <2, 3, 4>, <3, 1, 4>\}$$

Consider the following two SQL queries  $SQ_1$  and  $SQ_2$ :

$SQ_1$ : `SELECT RB, AVG(SB) FROM R, S  
WHERE R · A = S · C AND S · D < 7 GROUP BY R · B;`

$SQ_2$ : `SELECT DISTINCT S · B, MIN (S · C) FROM S GROUP BY S · B  
HAVING COUNT (DISTINCT S · D) > 1;`

If M is the number of tuples returned by  $SQ_1$  and N is the number of tuples returned by  $SQ_2$  then

A  
 M = 4, N = 2

C  
 M = 2, N = 2

B  
 M = 5, N = 3

D  
 M = 3, N = 3

$RA = SC$  AND  $SD < 7$ .

SOL:

$R(ABC)$

A	B	C
1	2	3
2	0	
3	1	
2	3	
4	2	
3	1	4

$S(RCD)$

R	C	D
2	3	7*
1	4	
1	2	3
2	3	4
3	1	4

$RB \text{ Avg } SB$

2	3
3	3
4	3
1	2

2

3

4

1

$\frac{3+3}{2} (\text{Avg } SB)$

3

3

1

2

RA	RB	RC	SB	SC	SD
1	2	3	3	1	4
1	2	0	3	1	4
1	3	1	3	1	4
1	4	2	3	1	4
3	1	4	2	3	4

GROUP

$M=4$

$2-2$   
~~1-2~~  
 $3-1$

# [MCQ]

Consider the two relation Enrolled and course are given below

Enrolled		
Sid	Cid	Fee
S <sub>1</sub>	C <sub>1</sub>	11K
S <sub>1</sub>	C <sub>2</sub>	25K
S <sub>2</sub>	C <sub>3</sub>	38K
S <sub>3</sub>	C <sub>4</sub>	40K
S <sub>3</sub>	C <sub>3</sub>	29K

Course		
Cid	Cname	Dept
C <sub>1</sub>	OS	CS
C <sub>2</sub>	DBMS	IT
C <sub>3</sub>	EDC	EC
C <sub>4</sub>	FM	ME

Ans(3)

S<sub>1</sub>  
S<sub>2</sub>  
S<sub>3</sub>

Ans

$$\pi_{\text{Sid}, \text{cid}}(\text{Enrolled}) / \pi_{\text{cid}}(\sigma_{\text{Dept} = 'CE'}(\text{Course}))$$

The Number of tuples there in the Result when the above relational algebra Query executes is \_\_\_\_\_

$\frac{\pi_{AB}(R)}{\pi_B(S)}$   $\Rightarrow$  'A' which pair every B value

$\frac{\pi_{AB}(R)}{\pi_B(S)} =$   
RA: Distinct A  
No Duplicates

$\boxed{\pi_A(R)}$  -  $\pi_A \left[ \pi_A(R) \times \pi_B(S) - R \right]$   
Empty  
Empty  
Empty

[MCQ]

P  
W

$$R \cap S \equiv S \cap R$$

#Q. If R and S are two relations then R intersection S can be represented as

1.  $R \cup (R - S)$

$$R - (R - S), \quad S - (S - R)$$

$$R \cap S = 3, 4, 5$$

2.  $S - (S - R)$

$$(R \cup S) - [(R - S) \cup (S - R)]$$

3.  $R - (R - S)$

$$R: [1, 2, 3, 4, 5]$$

4.  $(R \cup S) - [(R - S) \cup (S - R)]$

$$S: [3, 4, 5, 6, 7]$$

A

2 and 3 only

B

1, 2 and 3 only

C

3 and 4 only

D

2, 3 and 4 only

Ans(D)

$$\textcircled{d} \quad (1, 2, 3, 4, 5, 6, 7) - (1, 2, 6, 7) = (3, 4, 5)$$



#Q. Consider a schema  $R(A, B)$  and  $S(B, C)$ .  $Q_1$  and  $Q_2$  are queries expressed in relation algebra.  $Q_1 = \sigma_{(A=1)}(R \times S)$   $Q_2 = (\sigma_{(A=1)} R) \times S$  ("X" symbol refer to natural join)

A

Q<sub>1</sub> and Q<sub>2</sub> produce the same result

B

The answer of Q<sub>1</sub>, always contain answer of Q<sub>2</sub>

C

The answer of Q<sub>2</sub> always contain answer of Q<sub>1</sub>

D

No relation between Q<sub>1</sub> and Q<sub>2</sub>

$R(A\textcolor{blue}{B}) \quad S(\textcolor{teal}{B}C)$

$Q_1 : \sigma_{A=1} (R \bowtie S)$

$Q_2 : \sigma_{A=1}(R) \bowtie S$

[MCQ]



X : Sid  
Y : Sid

#Q. What is the condition for the below expression to be true?

$$\begin{aligned}\Pi_x(\Pi_y(R)) &= \Pi_y(\Pi_x(R)) \quad \checkmark \\ &= \Pi_x(\Pi_y(R)) \quad \checkmark \\ &= \Pi_x(\Pi_y(\Pi_z(R)))\end{aligned}$$

X : RollNo Name  
Y : Name RollNo

Z : Name RollNo EGPA



A

y ⊆ z, x ⊆ z, y = x

C

y ⊆ x, x ⊇ z, z ⊇ y

B

y ⊆ z, x ⊆ z, x ⊂ y

D

x ⊆ y, y ⊆ z

Selection is Commutative

$$\sigma_{C_2}(\sigma_{C_1}(R)) = \sigma_{C_1}(\sigma_{C_2}(R))$$

But Projection is Not Commutative

$$\Pi_A(\Pi_{AB}(R)) \neq \Pi_{AB}(\Pi_A(R))$$

[MCQ]



#Q. Consider three relations that are

$$R(a, b) = \{(0,1), (4,5), (8,9)\}$$

$$S(b, c) = \{(1,2), (5,2), (5,6), (5,10), (13,10)\}$$

$$T(c, d) = \{(2,3), (6,7), (10,11), (10,3)\}$$

The number of tuples in  $R \bowtie S \bowtie T$ , where  $\bowtie$  is natural join is

A  
 B  
 C

5

10

A	B
0	1
4	5

B	C
1	2
5	2
5	6
5	10
13	10

R $\bowtie$ S		
A	B	C
0	1	2
4	5	2
4	5	6
4	5	10

B  
 D

T	
C	D
2	3
6	7
10	11
10	3

8

13

A	B	C	D
0	1	2	3
4	5	2	3
4	5	6	7
4	5	10	11
4	5	10	3

5

Ans

[NAT]

P  
W

✓ Consider the following relations given below:

A

sno	pno
s1	p1
s1	p2
s1	p3
s1	p4
s2	p1
s2	p2
s3	p2
s4	p2
s4	p4

B1

pno
p2

B2

pno
p2
p4

B3

pno
p1
p2
p4

The number of tuples return by A/B<sub>1</sub> is x.

The number of tuples return by A/B<sub>2</sub> is y.

The number of tuples return by A/B<sub>3</sub> is z.

The value of x + y + z is \_\_\_\_\_?

x

S<sub>1</sub>  
S<sub>2</sub>  
S<sub>3</sub>  
S<sub>4</sub>

X=4

y

S<sub>1</sub>  
S<sub>4</sub>

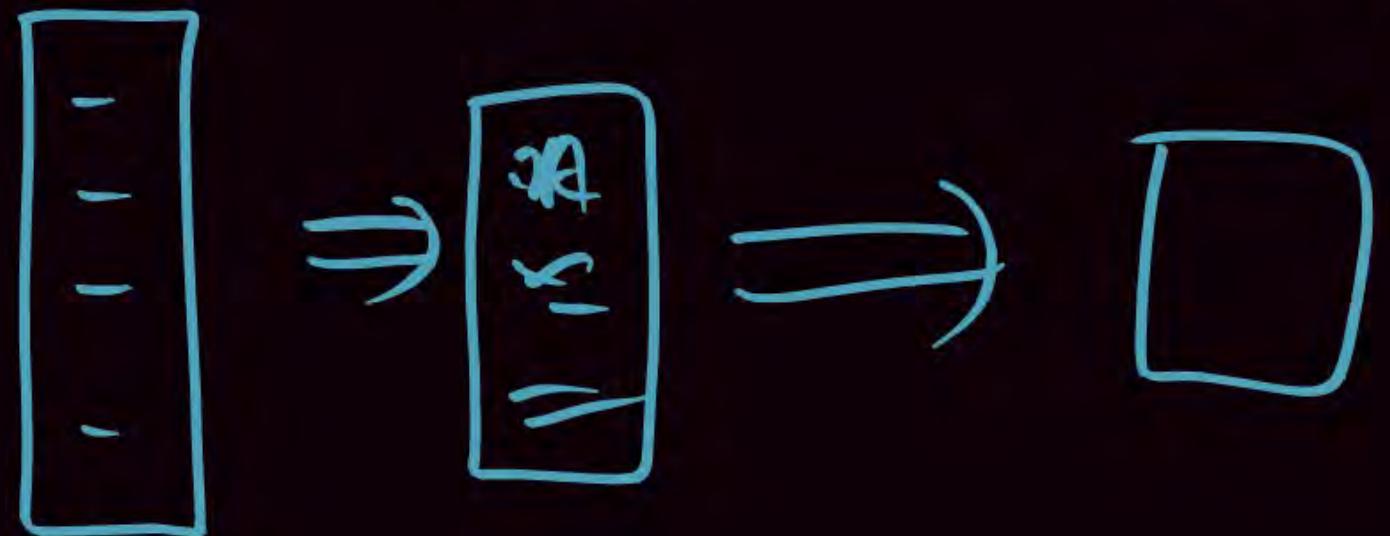
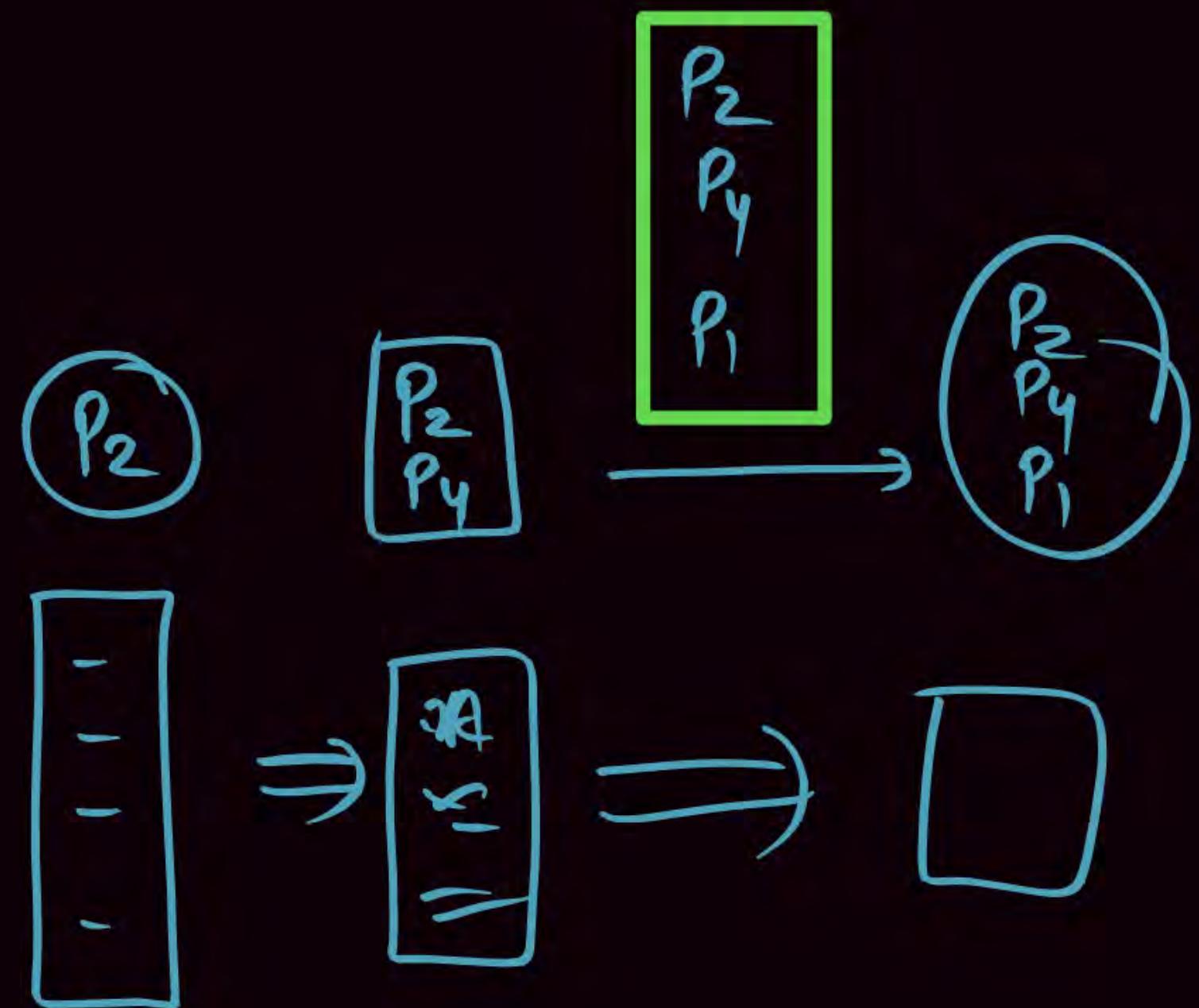
y=2

z

S<sub>1</sub>

z=1

$$4+2+1 = 7 \text{ Ans}$$



Consider the following relations given below:

A

sno	pno
<u>s1</u>	<u>p1</u>
<u>s1</u>	p2
<u>s1</u>	p3
<u>s1</u>	p4
<u>s2</u>	<u>p1</u>
<u>s2</u>	p2
<u>s3</u>	p2
<u>s4</u>	p2
<u>s4</u>	p4

B1

pno
p2

B2

pno
p2
p4

 $A \setminus B_3$ 

B3

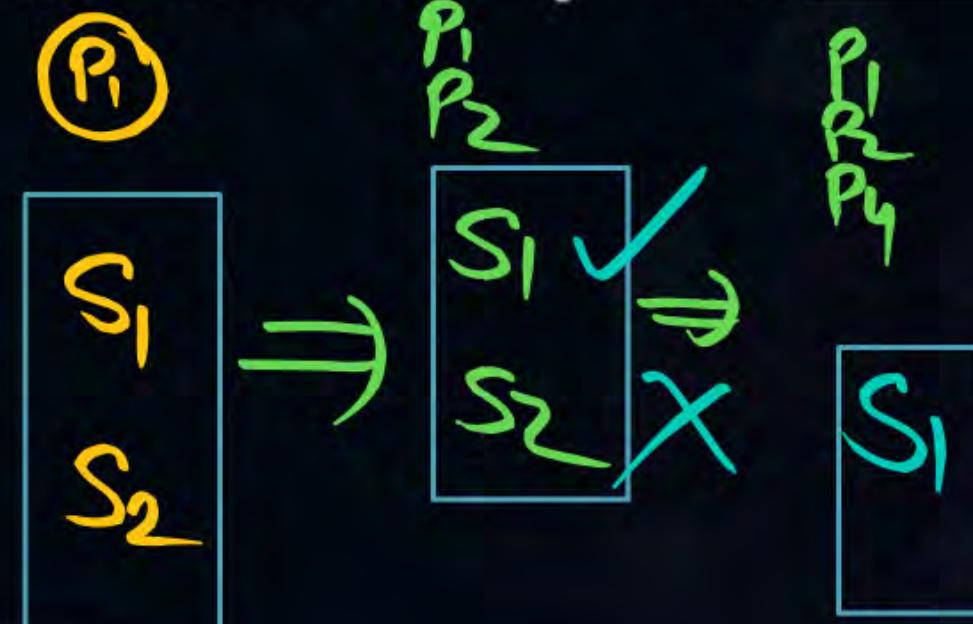
pno
p1
p2
p4

The number of tuples return by  $A/B_1$  is x.

The number of tuples return by  $A/B_2$  is y.

The number of tuples return by  $A/B_3$  is z.

The value of  $x + y + z$  is \_\_\_\_\_?



Consider the following relation:

Student(snum: integer, sname: string, major: string, level: string, age: integer)

Class (name: string, meets-at: string, room: string, fid: integer)

Enrolled (snum: integer, cname: string)

Faculty (fid: integer, fname: string, deptid: integer)

The following query executed on above relations

```
SELECT DISTINCT F.fname
FROM Faculty F
WHERE S > (SELECT COUNT (E.snum)
            FROM Class C, Enrolled E
            WHERE C.name = E.cname
            AND C.fid = F.fid)
```

The output of above Query is-

- A Distinct Name is the faculty for whom the combined enrollment of the course that they teach is greater than five.
- B Distinct Name of the faculty for whom the combined enrollment of the course that they Not teach is greater than five.
- C Distinct Name of the faculty for whom the combined enrollment of the course that they teach is less than Five.
- D The Query give the Syntax Error.



## 2 mins Summary



Topic

DBMS (Part 06)

Topic



THANK - YOU

# CS & IT ENGINEERING

Database  
Management System

Lecture No.- 07

By- Vijay Agarwal Sir



# Recap of Previous Lecture



Topic

Relational Algebra

Topic

Structured Query Language

# Topics to be Covered



- Topic
- Topic
- Topic

Relational Algebra

Structured Query Language

File Org & Indexing

## [MCQ]

#Q. The relation book (title, price) contains the titles and prices of different books. Assuming that no two books have the same price, what does the following SQL gives as output:

```
select title
from book as B
where (select count (*)
       from book as T
      where T. price > B. Price) < 5
```

A Titles of the four most expensive books

B Titles of the fifth most inexpensive books

C Titles of the fifth most expensive books

D Titles of the five most expensive books

B	Price
A	10
B	20.
C	30.
D	40.
E	50.
F	60.
G	70.

T	Price
A	10
B	20
C	30
D	40
E	50
F	60
G	70

Ans (D)

B	
A	10
B	20
C	30
D	40
E	50
F	60
G	70

T	
A	10
B	20
C	30
D	40
E	50
F	60
G	70

(T.Price > B.Price) Count < 5

$A \Rightarrow 10 \Rightarrow T.Price > B.Price$  Count < 5  
 $A \Rightarrow 6 \times$   
 $B = 20 \Rightarrow B = 5 \times$   
 $C = 30 \Rightarrow C = 4$   
 $D = 40 \Rightarrow D = 3$   
 $E = 50 \Rightarrow E = 2$   
 $F = 60 \Rightarrow F = 1$   
 $G = 70 \Rightarrow G = 0$

CDEFG

✓✓✓✓✓

✓ A: 150  
 ✓ B: 100  
 ✓ C: 90  
 ✓ D: 70  
 ✓ E: 60  
 ✓ F: 50  
 ✓ G: 40  
 ✓ H: 30  
 ✓ I: 20  
 ✓ J: 10

A	10
B	90
C	70
D	25
E	5
F	60
G	20
H	100
I	150
J	40

A	10
B	90
C	70
D	25
E	5
F	60
G	20
H	100
I	150
J	40

(T.Price > B.Price)		Cont	< 5	PW
(10) A	⇒ 8	X		
(90) B	⇒ 2	✓		
(70) C	⇒ 3	✓		
(25) D	= 6	X		
(5) E	⇒ 9	X		
(60) F	4	✓		
(20) G	7	X		
(100) H	1	✓		
150 I	0	✓		
40 J	5	X		



#Q. Consider the table employee (empId, name, department, salary) and the two queries  $Q_1$ ,  $Q_2$  below. Assuming that department 5 has more than one employee, and we want to find the employees who get higher salary than anyone in the department 5, which one of the statements is TRUE of any arbitrary employee table?

$Q_1$  : Select e.empId  
From employee e  
Where not exists

(Select \* From employee s Where s.department = "5" and s.salary  
 $\geq e.salary$ )

$Q_2$  : Select e.empId  
From employee e  
Where e.salary > Any

(Select distinct salary From employee s Where s.department = "5")

- A Q<sub>1</sub> is the correct query
- B Q<sub>2</sub> is the correct query
- C Both Q<sub>1</sub> and Q<sub>2</sub> produce the same answer
- D Neither Q<sub>1</sub> nor Q<sub>2</sub> is the correct query

## Direction for Question

Consider two tables in a relational database with columns and rows as follows:

Table : Student

<u>Roll_no</u>	Name	<u>Dept_id</u>
1	ABC	1
2	DEF	1
3	GHI	2
4	JKL	3

*Referencing Relation*

FK

Table : Department

<u>Dept_id</u>	Dept_name
1	A
2	B
3	C

*Referenced Reln*

Roll\_no is the primary key of the Student table, Dept\_id is the primary key of the Department table and Student. Dept\_id is a foreign key from Department. Dept\_id

#Q. What will happen if we try to execute the following two SQL statements?

(i) update Student set Dept\_id = Null where Roll\_no = 1

X (ii) update department set Dept\_id = Null where Dept\_id = 1

A

Both (i) and (ii) will fail

B

(i) will fail but (ii) will succeed

D

Both (i) and (ii) will succeed

C

(i) will succeed but (ii) will fail

#Q. Consider the schema:

Sailors (sid, sname, rating, age) with the following data:

<i>Sq</i>	sid	sname	rating	age
	22	Dustin	7	45 ✓
	29	Borg	1	33 ✓
	31	Pathy	8	55 ✓
	32	Robert	8	25 ✓
	58	Raghu	10	17
	64	Herald	7 ✓	35
	71	Vishnu	10	16
	74	King	9	35 ✓
	85	Archer	3	26 ✓
	84	Bob	3	64 ✓
	96	Flinch	3	17

Outer → Inner → Outer

For the query

SELECT S. rating, AVG(S.age) AS average  
 FROM Sailors S  
 Where S.age >= 18  
 GROUP BY S. rating

HAVING 1 < (SELECT COUNT (\*) FROM  
 Sailors S2 where S. rating = S2.rating)

The number of rows returned is

- |   |   |   |   |
|---|---|---|---|
| A | 6 | B | 5 |
| C | 4 | D | 3 |

outer Query Result	
X	1 33
X	3. 45
X	3. 45
X	3. 45
8	40
9	35

✓ 3  
 ✓ 7 Avg  
 ✓ 8

1	33	1
3.	45	3
3.	45	3
3.	45	3
7	7	7
8	8	8
9.	9	7.

Count(\*)

$\Rightarrow 1 > 1$  False

$\Rightarrow 3 > 1$  True

$\Rightarrow 2 > 1$  True

$\Rightarrow 2 > 1$  True

$\Rightarrow 0 > 1$  False

22	Dustin	7	45	$\frac{45+35}{2}$	1	33
29	Bog	1	33		3	45
31	Pathy	8	55		7	40
32	Robert	8	25		8	40
74	King	9	35		9	35
85	Archer	3	26	$\frac{26+64}{2} = 45$		
84	Bob	3	64			
64	Herbal	7	35			

1	33
3	43
7	40
8	40
9	35

# Fundamental Practices

FROM  
↓  
WHERE  
↓  
GROUP BY.

## Correlated Nested Query



#Q. Database table by name Overtime allowance is given blow:

Employee	Department	OT-allowance
RAMA	Mechanical	5000
GOPI	Electrical	2000
SINDU	Computer	6000
MAHESH	Civil	1500

Ans(B).

- A 16
- B 4
- C 8
- D None of the above

Which is the output of the following SQL query?

Select count (\*)

From ((Select Employee, Department

From Overtime\_allowance as S natural join (Select Department, OT\_ allowance

From Overtime\_allowance) as T)

Emp.	Dept.		Dept	O.T
RAMA	ME		ME	5000
GOPAL	EE		EE	2000
SINDHU	CS	X	CS	6000
MAMESI	CE		CE	1500

CROSS Product  $\Rightarrow$  16 Tuple

But Natural Join = 4 Tuple

Common Data for next 2 Questions:

Consider the following database schema

SUPPLIERS(sid: integer, sname: string, address: string)

PART(pid: integer, pname: string, color: string)

CATALOG(sid: integer, pid: integer, cost: real)

#Q. What does the following SQL query return?

SELECT c.sid FROM CATLOG c, PART p WHERE (p.color = 'red' and p.color = 'green') and p.pid = c.pid;

OTable

$p_1$	A	Red
$p_3$	C	Green



find sids of catalog who supply some red and green part



find the sids of catalog who supply some red or green parts



find sids of catalog who supply every red and every green part



None of these.

#Q. What does the following SQL query return?

```
SELECT s.sid FROM SUPPLIERS s where s.address = '229 park street' OR  
s.sid IN (SELECT c.sid FROM PART p, CATALOG c where p.color ='red' AND  
p.pid = c.pid);
```

- A find sid of supplier who supply some red part or are at 229 park street
- B find sid of supplier who supply some red part and at 229 park street
- C find sid of supplier who supply all red part and at 229 park street
- D None of the above



#Q. Consider the following relational schema:

- ↳ Suppliers(sid:integer, sname: string, saddress: string)
- ↳ Parts(pid:integer, pname:string, pcolor:string)
- Catalog (sid:integer, pid:integer, pcost:real)

What is the result of the following query?

(SELECT Catalog.pid from Suppliers, Catalog  
WHERE Suppliers.sid = Catalog.pid)

MINUS

(SELECT Catalog.pid from Suppliers, Catalog  
WHERE Suppliers.sname <> 'sachin' and  
Suppliers.sid = catalog.sid)

RAM  
SHYAM  
SACHIN  
Ramesh

Pid = SACHIN

RAM  
SHYAM  
RAMESH

- A pid of parts supplied by all except Sachin
- B pid of parts supplied only by Sachin
- C pid of parts available in catalog supplied by Sachin
- D pid of parts available in catalogs supplied by all except Sachin

#Q. Consider a relation book (title, price) which contains the titles and prices of different books. Assuming that no two books have the same price, what does the following SQL query list?

```
SELECT title
FROM book AS B
WHERE (SELECT COUNT (*) FROM book AS T
WHERE T.price > B.price) < 7
```

A

Titles of the six most expensive books

B

Title of the sixth most expensive books

C

Titles of the seven most expensive book

D

Title of the seventh most expensive books



## Common data for next 2 Questions:

Consider the schema:

<u>Book</u> ( <u>bookid</u> , <u>name</u> , <u>publisherid</u> )
<u>Author</u> ( <u>authorid</u> , name)
<u>Publisher</u> ( <u>publisherid</u> , name)
<u>Details</u> ( <u>publisherid</u> , <u>bookid</u> , <u>authorid</u> )

#Q. What does the following query output?

Select distinct a.name

from author a, publisher p, book b, details d

Where b.bookid = d.bookid

and a.authorid = d.authorid

and d.publisherid = 'NewPub';



author names whose books are published by NewPub



unique author names whose books are published by NewPub



unique author names with books not published by NewPub



author names with books not published by NewPub

#Q. Which query will print authorid, publisherid and the number of books of this combination sorted by author name?

A

```
select a.name, p.publisherid, count (*) from author a, publisher p, details d
where d.publisherid = p.publisherid and a.authorid = d.authored group by
a.name, p.publisherid order by a.name;
```

B

```
select d.authorid, d.publisherid count (*) from author a, details d where
a.authorid = d.authored group by d.authorid, d.publisherid order by a.name;
```

C

```
select d.authorid, d.publisherid, sum (*) from author a, details d where
a.authorid = d.authorid group by d.authorid, d.publisherid order by
a.authorid;
```

D

```
select a.name, d.publisherid, sum (*) from author a, details d
where a.authorid = d.authorid group by d.authorid, d.publisherid order by
a.authorid;
```

#Q. Consider the following relation schema

Employee (Eid, Ename, Dno, salary, address)

and

Department (Dno, Dname), then what does the following SQL query retrieve?

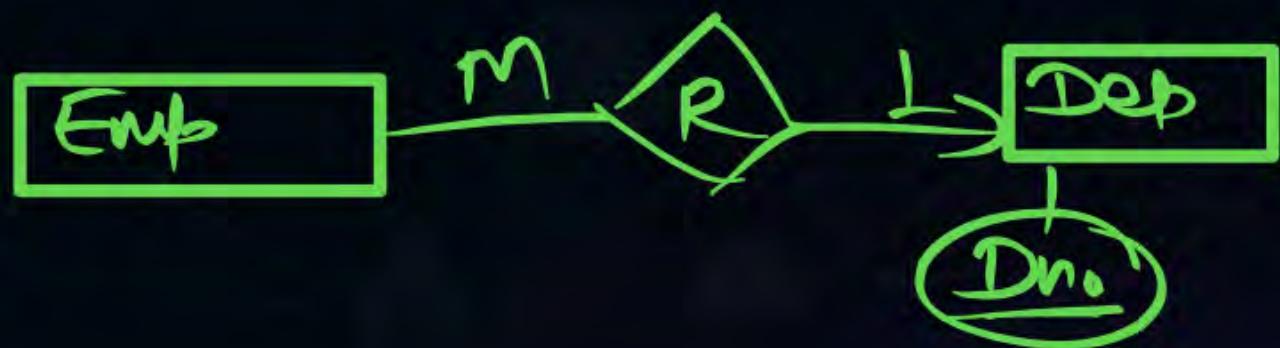
Select Dname, Count (\*)

From Department D, Employee E

Where D. Dno=E.Dno AND E. Salary > 40000

Group by Dname

Having count (\*) > 5;



- ① RDBMS
- ② Transaction
- ③ ER & F.K
- ④ Query Lang.
- ⑤ File og Læsning

- A selects only department that have more than 5 employees who earns more than 40,000.
- B selects all departments employees who earn more than 40,000.
- C select all employees who earn 40,000.
- D None of these

#Q. Consider a B<sup>+</sup> tree in which the maximum number of child nodes is 6. What is the minimum and maximum number of keys in such a tree?

$$\text{ORDER}(P) = 6$$

$$\text{Min \# keys} = \lceil \frac{P}{2} \rceil - 1 \Rightarrow \lceil \frac{6}{2} \rceil - 1 \Rightarrow 3 - 1 = 2$$

$$\text{Max \# keys} = P - 1 \Rightarrow 6 - 1 = 5$$

- A 3 and 4
- B 3 and 5
- C 2 and 5
- D 2 and 4

#Q. Match the following

List-I	List-II
a. Primary index → 3	1. Non key and ordering
b. Clustering index → 1	2. Non-key and Non-ordering
c. Secondary index (key) → 4	3. Key and ordering
d. Secondary Index(Non key) → 2	4. Key and Non ordering

Codes:

	a	b	c	b
A	4	1	3	2
C	3	2	4	1

	a	b	c	b
B	3	1	4	2
D	4	2	3	1

In a B<sup>+</sup> tree, if the search key field value is 13 bytes and records pointer is a bytes long and block pointer 7 bytes, block size is 1024 bytes. Then the order of internal (non-leaf) node in B<sup>+</sup> tree is \_\_\_\_\_.

A file has  $r = 20,000$  STUDENT records of fixed length. Each record has the following fields: Name (30 bytes), Ssn (9 bytes), Address (40 bytes), PHONE (10 bytes), Birth\_date (8 bytes), Sex (1 byte), Major\_dept\_code (4 bytes), Minor\_dept\_code (4 bytes), Class\_code (4 bytes, integer), and Degree\_program (3 bytes). An additional byte one additional byte is used as a deletion marker. Having block size of 512 byte & Assume using unpanned origination.

Suppose the file is ordered by key filed Ssn & construct a sparse primary index on Ssn, with pointer size is 7 byte.

- A: is the number of data block required.
- B: is the total number of index block required [using] in multilevel index.
- C: Is the number of level required is multilevel indexing then value of  $A + 2B + 4C$  is\_\_\_\_\_.



## 2 mins Summary



Topic

DBMS (Part 07)

Topic



THANK - YOU

# CS & IT ENGINEERING

## Database Management System

Lecture No.- 08

By- Vijay Agarwal Sir



# Recap of Previous Lecture



Topic

Relational Algebra

Topic

Structured Query Language

Topic

File Org & Indexing

# Topics to be Covered



Topic

File Org & Indexing

Topic

B & B+ Tree

#Q. Consider a B<sup>+</sup> tree in which the maximum number of child nodes is 6. What is the minimum and maximum number of keys in such a tree?

①

- A 3 and 4
- B 3 and 5
- C 2 and 5
- D 2 and 4

#Q. Match the following

②

List-I	List-II
a. Primary index	1. Non key and ordering
b. Clustering index	2. Non-key and Non-ordering
c. Secondary index (key)	3. Key and ordering
d. Secondary Index(Non key)	4. Key and Non ordering

Codes:

	a	b	c	b
A	4	1	3	2
C	3	2	4	1

*Done*

	a	b	c	b
B	3	1	4	2
D	4	2	3	1

- ③ In a B<sup>+</sup> tree, if the search key field value is 13 bytes and records pointer is a bytes long and block pointer 7 bytes, block size is 1024 bytes. Then the order of internal (non-leaf) node in B<sup>+</sup> tree is \_\_\_\_\_.

B<sup>+</sup> Tree : ORDER of Internal Node :

$$P \times B_P + (P - 1) \text{ keys} \leq \frac{\text{Block Size}}{7}$$

$$P \times 7 + (P - 1) \times 13 \leq 1024$$

$$7P + 13P - 13 \leq 1024$$

$$20P \leq 1037$$

$$P = \left\lceil \frac{1037}{20} \right\rceil = \left\lceil 51.85 \right\rceil = 52 \text{ Ans}$$

Q

Novathe Book

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- A: is the number of data block required.
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- C: Is the number of level required is multilevel indexing then value of  $A + 2B + 4C$  is 5338. Ans

Ans (5338)

# Records = 20,000.

$$\text{Record size} = 30 + 9 + 40 + 10 + 8 + 1 + 4 + 4 + 4 + 3 + 1 = 114 \text{ Byte}$$

Block Size = 512      Key Size = 9 Byte      Pointer = 7 Byte.

$$\text{Block factor of DB file} = \left\lfloor \frac{512}{114} \right\rfloor = 4 \text{ Record/Block}$$

$$\text{Total # DB Blocks} = \left\lceil \frac{20000}{4} \right\rceil = 5000 \text{ Data Block}$$

$$\text{One Index Record Size} = 9 + 7 = 16 \text{ Byte}$$

$$\text{Block factor of Index file} = \left\lfloor \frac{512}{16} \right\rfloor = 32 \text{ Index Record Per Block.}$$

Primary: Sparse: Total # Index entries = 5000 (# DB Block)

I<sup>st</sup> Level: Total # Index Block =  $\lceil \frac{5000}{32} \rceil = 157$  Index Block

2<sup>nd</sup> Level Total # Index Block =  $\lceil \frac{157}{32} \rceil = 5$  Index Block

3<sup>rd</sup> Level Total # Index Block =  $\lceil \frac{5}{32} \rceil = 1$  Index Block  
Total 3 level Required.

$$A = 5000$$

$$B = 157 + 5 + 1 = B = 163$$

$$C = 3$$

$$\begin{aligned} & A + 2B + 4C \\ & 5000 + 2(163) + 4(3) \\ & 5000 + 326 + 12 \\ & = 5338 \text{ Ans} \end{aligned}$$

5

19  
2

Consider a file of 5, 24, 288 records. Each record is 64 byte long and its key field is of size 8 byte. The file is ordered on a non-key field and the file organization is unspanned. The file is stored in a file system with block size 1024 byte and the size of block pointer is 8 byte. If the secondary index built on the key field of the file and multilevel index scheme is used to store the secondary Index. The number of block required in the third level index is 2 Ans

Ans(2)

$$\text{Total # Records} = 2^{19}$$

$$\text{key - 8 Byte} \quad \& \text{BP - 8 Byte} \quad \text{Block Size} = 1024 \text{ Byte}$$

$$\text{One Index Record Size} = 8 + 8 = 16 \text{ Byte}$$

$$B_f \text{ of Index file} = \frac{1024}{16} = \frac{2^{10}}{2^4} = 2^6 = 64 \text{ Records/Block.}$$

Ans

# Index entries =  $2^{19}$

First level

$$\text{Total \# Index Block} = \frac{2^{19}}{2^6} = 2^{13} \text{ Index Block}$$

2nd Level

$$\text{Total \# Index Block} = \frac{2^{13}}{2^6} = 2^7 \text{ Index Block}$$

3rd Level

$$\text{Total \# Index Block} = \frac{2^7}{2^6} = 2 \text{ Index Block} \quad \text{Avg}$$

4th Level

$$\text{Total \# Index Block} : \left\lceil \frac{2^7}{2^6} \right\rceil = 1 \text{ Index}$$

Total 4 level

⑥

#Q. Given a block can hold either 3 records or 10 key pointers. A database contains n records, then how many blocks do we need to hold the data file and the dense index

A

$$\frac{13n}{30}$$

C

$$\frac{n}{10}$$

Ans(A)

B

$$\frac{n}{3}$$

D

$$\frac{n}{30}$$

Block factor of DB File = 3  $\Rightarrow$  Total # Data Block =  $\frac{n}{3}$   
 Block factor of Index file = 10  $\Rightarrow$  Total # Index Block =  $\frac{n}{10}$

$$\text{Total Block} = \frac{n}{3} + \frac{n}{10} \Rightarrow$$

$$\frac{13n}{30} \text{ Ans}$$

7

#Q. Calculate the order of leaf ( $P_{leaf}$ ) and non leaf (P) nodes of a B<sup>+</sup> tree based on the information given below.

Search key field = 12 field

Record pointer = 10 bytes

Block pointer = 8 bytes

Block size = 1 KB

A

$P_{leaf} = 51$  and  $P = 46$

B

$P_{leaf} = 47$  and  $P = 52$

C

$P_{leaf} = 46$  and  $P = 51$

D

$P_{leaf} = 52$  and  $P = 47$



## Internal Node

$$P \times B_o + (P-1) \text{key} \leq B.S$$

$$P \times 8 + (P-1) \times 12 < 1024$$

$$8P + 12P - 12 \leq 1024$$

$$20P \leq 1036$$

$$\begin{aligned} P &= \left\lfloor \frac{1036}{20} \right\rfloor = \lfloor 51.8 \rfloor \\ &= 51 \end{aligned}$$

#Q. The order of a leaf node in  $B^+$  tree is the maximum number of (value, data record pointer) pairs it can hold. Given that the block size is 1K bytes, data record pointer is 7 bytes long, the value field is 9 bytes long and a block pointer is 6 bytes long.

What is the order of the leaf node?

- A 63
- B 64
- C 67
- D 68

$$\begin{aligned} P(\text{key} + R_p) + LB_p &\leq \text{Block Size} \\ P(7 + 9) + 6 &\leq 1024 \\ 16P + 6 &\leq 1024 \\ 16P &\leq 1018 \\ P = \left\lfloor \frac{1018}{16} \right\rfloor &= 63 \text{ Ans} \end{aligned}$$

(9)

Navette Book

#Q.

Suppose that the search field is a non-ordering key filed, and we construct a B-tree on this field with  $p = 23$ . Assume that each node of the B-tree is 69% full on an average. Assume the level of the root Node in a B tree is 1. Then the total number of keys stored at height 2 (level 3) is \_\_\_\_\_. 

Actual ORDER = 16

$$\text{ORDER} = 23 \Rightarrow 69\% \text{ Full.} \Rightarrow 23 \times 0.69 = 16$$

16 Pointers & 15 keys.  
Avg Fanout = 16

$$ORDER = P [16]$$

Weight   Level	Max # Node	Max # BP	Max # Keys	$(P-1) = k-1 = 15$
0 1	1	P	$P-1$	$15 = 15$
1 2	P	$P^2$	$P(P-1)$	$16 \times 15 = 240$
2 3	$P^2$	$P^3$	$P^2(P-1)$	$16^2 \times 15 = 3840$

$$\begin{aligned} \text{Total # keys} &= 15 + 240 + 3840 \\ &= 4095 \underline{\text{Ans}} \end{aligned}$$

(10) &amp; (11)

**Common data for next Two Questions**

Consider the following description

To construct B+ tree use the following values. Consider the database block size as 512 bytes, block pointer as 6 bytes, record pointer as 7 bytes and search key value as 9 bytes.

Block Size = 512 Byte

B<sub>p</sub> = 6 Byte

R<sub>p</sub> = 7 Byte

key = 9 Byte.

#Q. What is the order of B<sup>+</sup> tree internal node

A

23

C

34

B

32

D

44

$$P \times B_P + (P-1) \leq BS$$

$$P \times 6 + (P-1)9 \leq 512$$

$$6P + 9P - 9 \leq 512$$

$$15P \leq 521$$

$$P = \frac{521}{15} = \underline{\underline{34}}$$

key order  
Leaf Node

$$P(\text{key} + R_P) + L R_P \leq BS$$

$$\Rightarrow P(9+7) + 6 \leq 512$$

$$\Rightarrow 16P \leq 506$$

$$P = \left\lceil \frac{506}{16} \right\rceil = \cancel{31}$$

Order  $\rightarrow$  (key, Record Pair)

$$P(\text{key} + R_p) + LB_p.$$

Block Pointer  
order  $\Rightarrow (P-1)(\text{key} + R_p) + LB_p.$

Consider a data with 4700 keys (records) are going to be inseresting into B+ tree.  
Can hold 15 pointer (P = 15) Database using dense B+ tree for indexing assume  
level of the root node is 1. Let x is the minimum number of levels required y is the  
maximum number of levels required then what is the value of  $2x + y$

$$\left\lceil \frac{P}{2} \right\rceil - \left\lceil \frac{P-1}{2} \right\rceil - \left\lceil \frac{P-2}{2} \right\rceil = 8 \quad \text{ORDER} = 15$$

$$\text{Maximum # keys} = P-1 = 15-1 = 14 \quad \text{Max keys}$$

$$\text{Minimum # keys} = \left\lceil \frac{P}{2} \right\rceil - 1 = \left\lceil \frac{15}{2} \right\rceil - 1 = 8 - 1 = 7 \quad \text{Min key}$$

We Maximum level getting if Each Node Contain Min keys & Min Bp.

We getting Minimum Level if Each Node Contain Maximum keys & Max Bp.

*Note*

In a R+ Tree all keys are available  
at the Leaf Node.

### Minimum Level (Max keys & $n_{B_0}$ )

$$1^{\text{st}} \text{ level} = \left\lceil \frac{4700}{14} \right\rceil = 336 \text{ Node}$$

$$2^{\text{nd}} \text{ level} = \left\lceil \frac{336}{15} \right\rceil = 23 \text{ Node}$$

$$3^{\text{rd}} \text{ level} = \left\lceil \frac{23}{15} \right\rceil = 2 \text{ Node}$$

$$4^{\text{th}} \text{ level} = \left\lceil \frac{2}{15} \right\rceil = 1$$

Minimum 4 Level  $\cdot x=4$

### Maximum Level (min key & min BP)

$$1^{\text{st}} \text{ level} = \left\lceil \frac{4700}{7} \right\rceil = 672 \text{ Node}$$

$$2^{\text{nd}} \text{ level} = \left\lceil \frac{672}{8} \right\rceil = 84$$

$$3^{\text{rd}} \text{ level} = \left\lceil \frac{84}{8} \right\rceil = 11$$

$$4^{\text{th}} \text{ level} = \left\lceil \frac{11}{8} \right\rceil = 2$$

$$5^{\text{th}} \text{ level} = \left\lceil \frac{2}{8} \right\rceil = 1$$

$y=5$   
Maximum 5 Level

$$2x + y$$

$$2 \times 4 + 5$$

$$8 + 5 = \textcircled{13} \text{ Avg}$$

(13)

Assume the level of Root node in a  $B^+$  Tree is 1. Then the maximum number of nodes in a  $B^+$  Tree possible with order 5 and the number of level 6 is  $x$  & maximum number of distinct keys (Records) in a  $B^+$  Tree of height 5 & order 5 is  $y$ . Then the value of  $x + y$  is \_\_\_\_\_.  
  
↓  
Level 6

$$x = 3906.$$

$$y = 12,500$$

$$x+y = 3906 + 12500$$

$$= 16,406 \text{ Ans}$$

Height/Level	Max # Nodes	Max # BPs	Max # keys.	$R_1 = \frac{P-1}{P}$
0/L	1	P	(P-1)	$\frac{4}{5} = 4$
1/2	P	P2	P(P-1)	$5 \times 4 = 20$
2/3	P2	P3	P^2(P-1)	$5^2 \times 4 = 100$
3/4	P3	P4	P^3(P-1)	500
4/5	P4	P5	P^4(P-1)	2500
5/6	P5	P6	P^5(P-1)	12500

*B+Tree*

Diagram illustrating the B+Tree structure:

- Root Node (Level 0) has 5 children.
- Level 1 has 5^1 = 5 nodes.
- Level 2 has 5^2 = 25 nodes.
- Level 3 has 5^3 = 125 nodes.
- Level 4 has 5^4 = 625 nodes.
- Level 5 has 5^5 = 3125 nodes.
- Total height of the tree is 5.

3906

Height/level	min # Nodes	Min #BP	#keys.
0 L	1	$\lceil P_2 \rceil$	$\lceil P_2 \rceil - 1$
$\frac{1}{2}$	$\lceil P_2 \rceil$	$(\lceil P_2 \rceil)^2$	$\lceil P_2 \rceil (\lceil P_2 \rceil - 1)$
:			

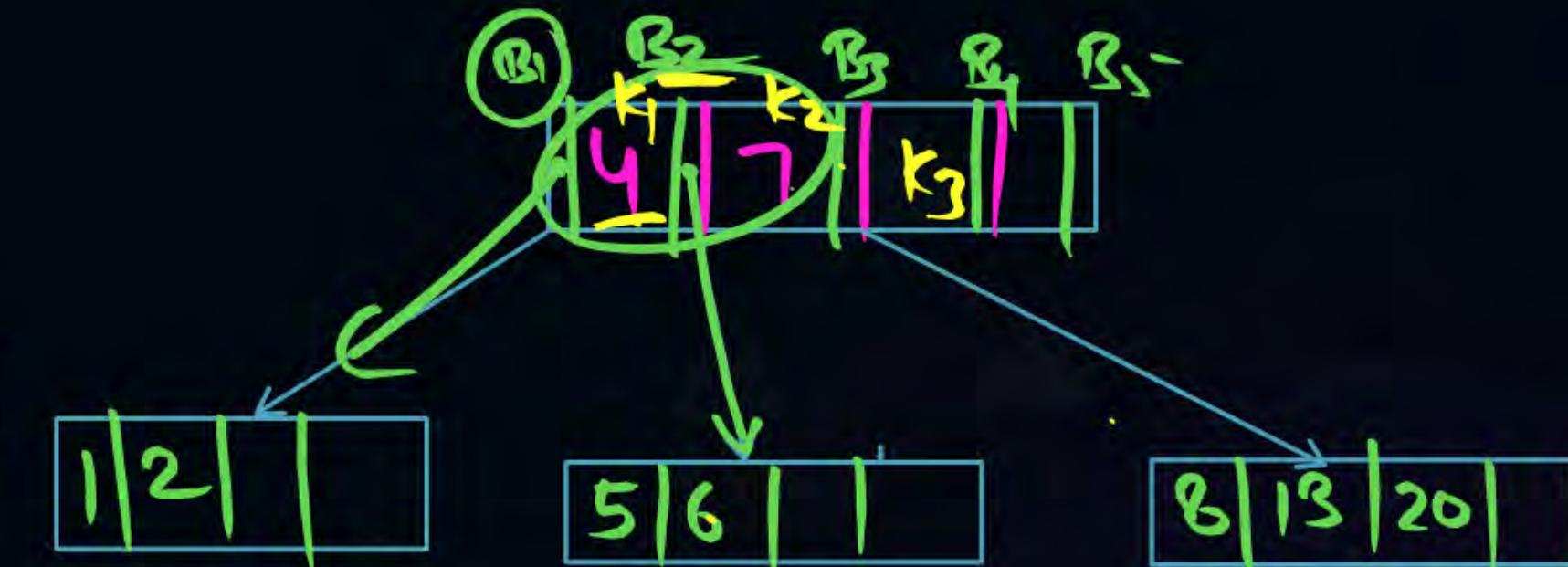
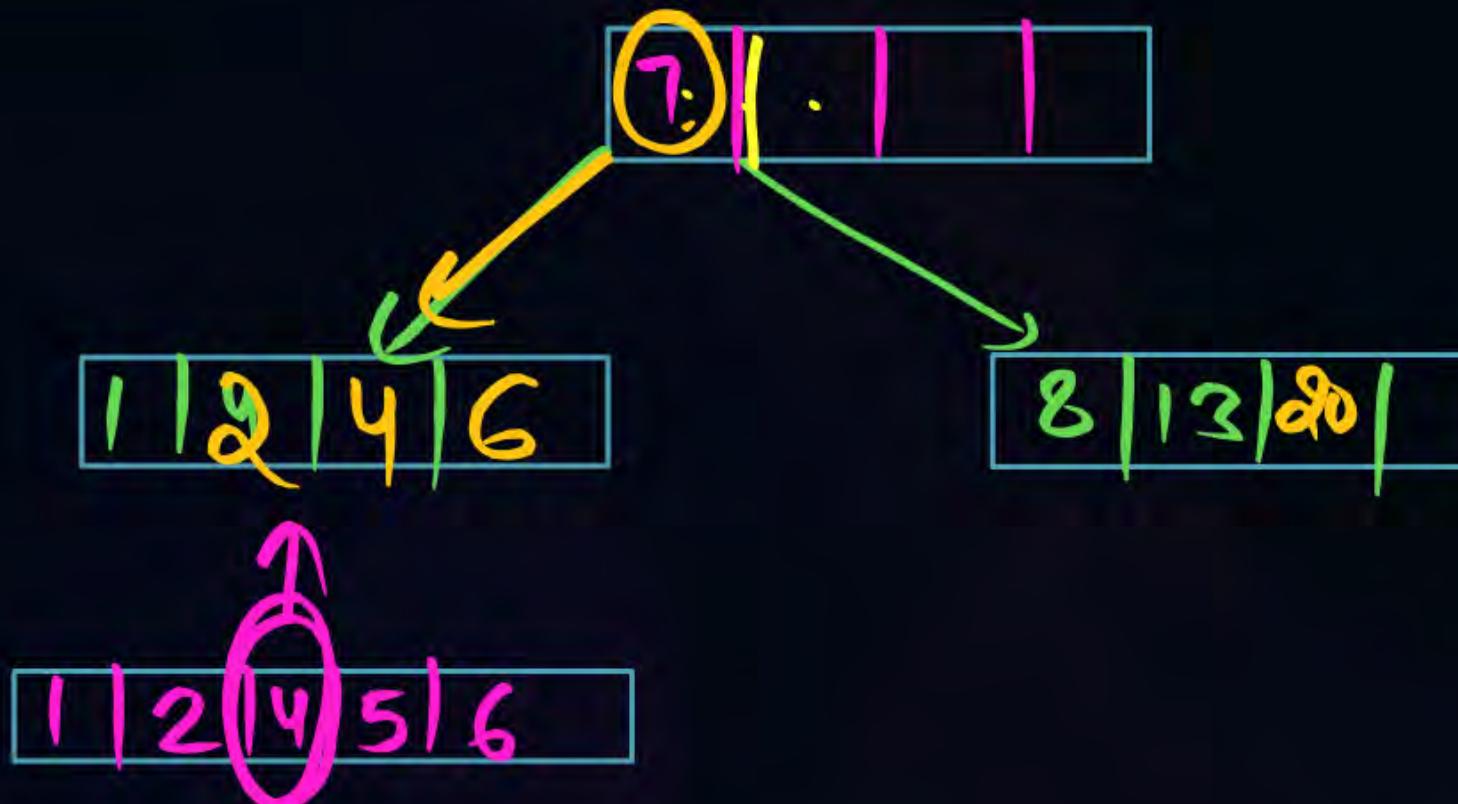
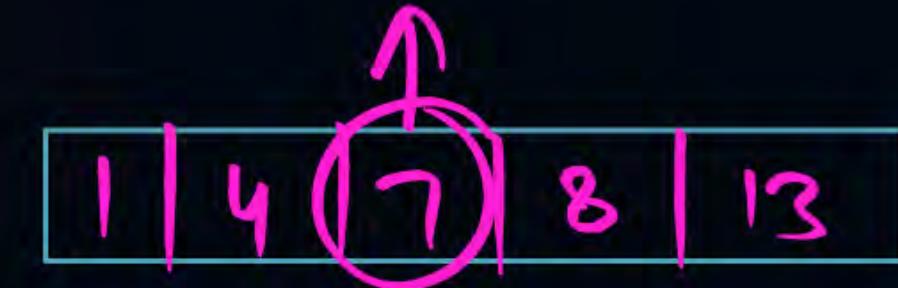


#Q. A B-tree of order 5, the following keys are inserted as follows :  
7,8,1,4,13,20,2,6,5. How many elements are present in the root of the tree?

- A 2
- B 1
- C 3
- D 4

7, 8, 1, 4, 13, 20, 2, 6, 5

ORDER = 5  
Max key = 4

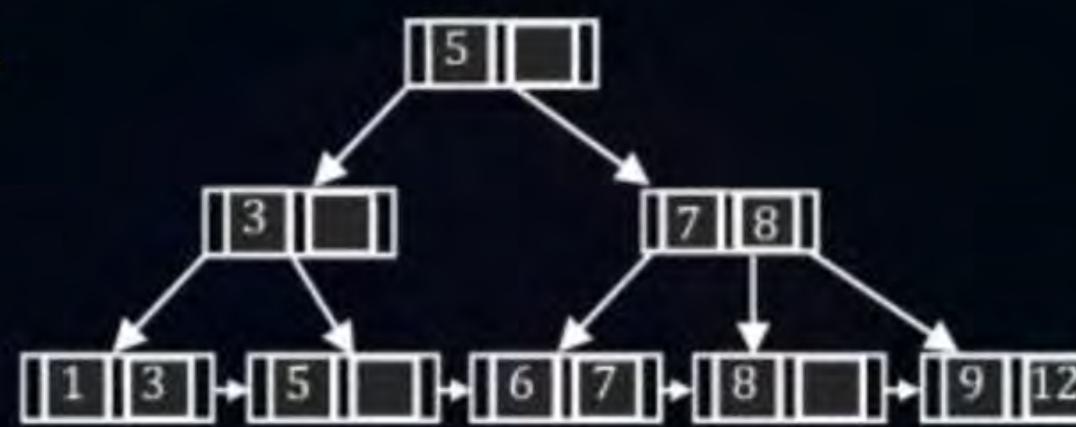


15

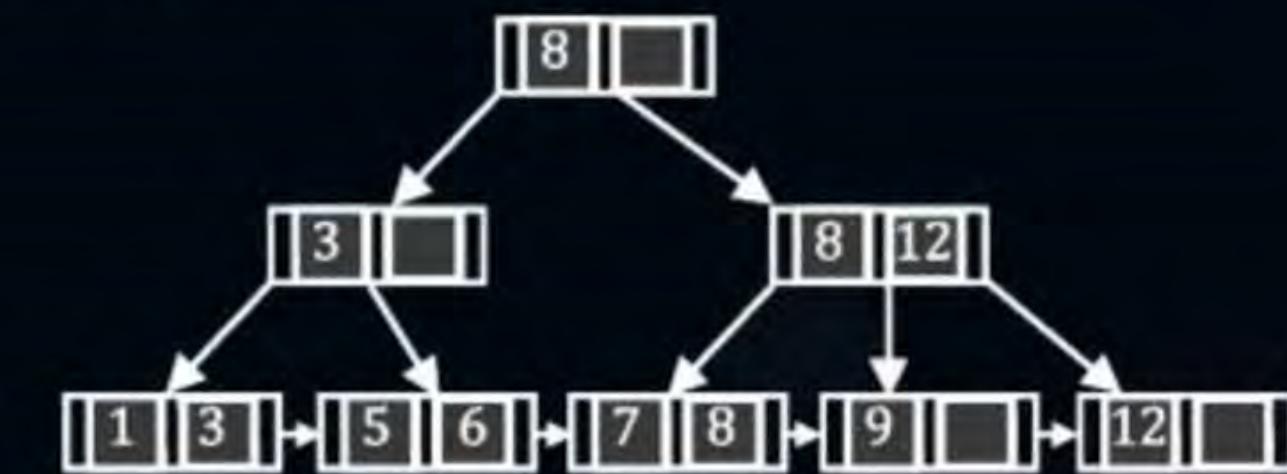
#Q. If following sequence of keys are inserted in a B<sup>+</sup> tree with (K = 3) pointers  
8, 5, 1, 7, 3, 12, 9, 6

Which of the following shall be correct B+ tree?

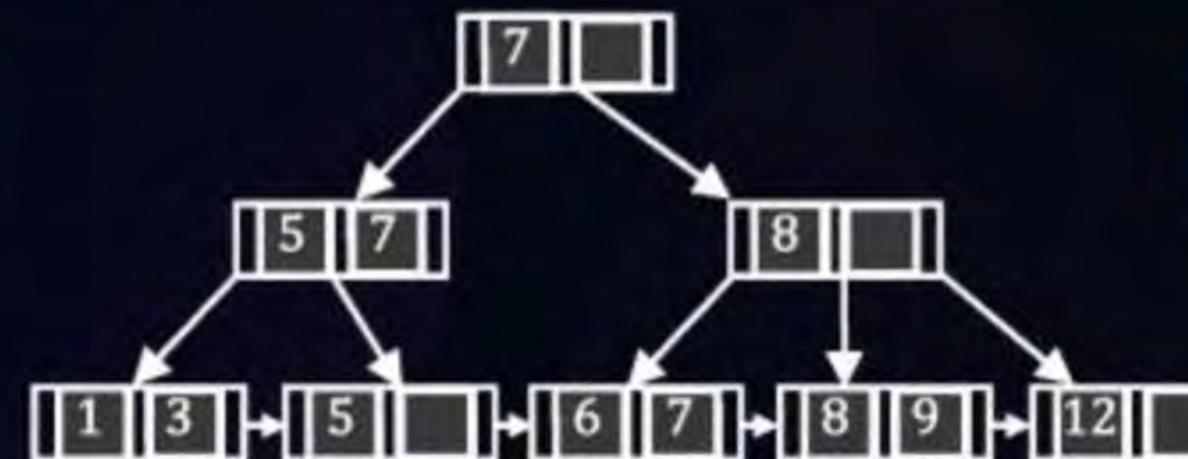
A



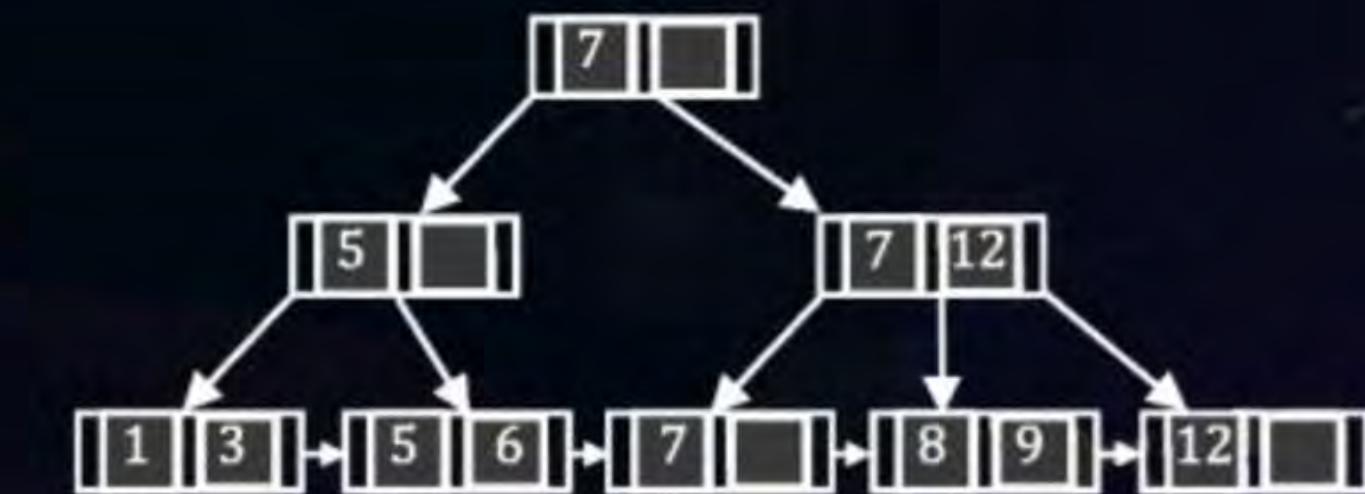
B



C

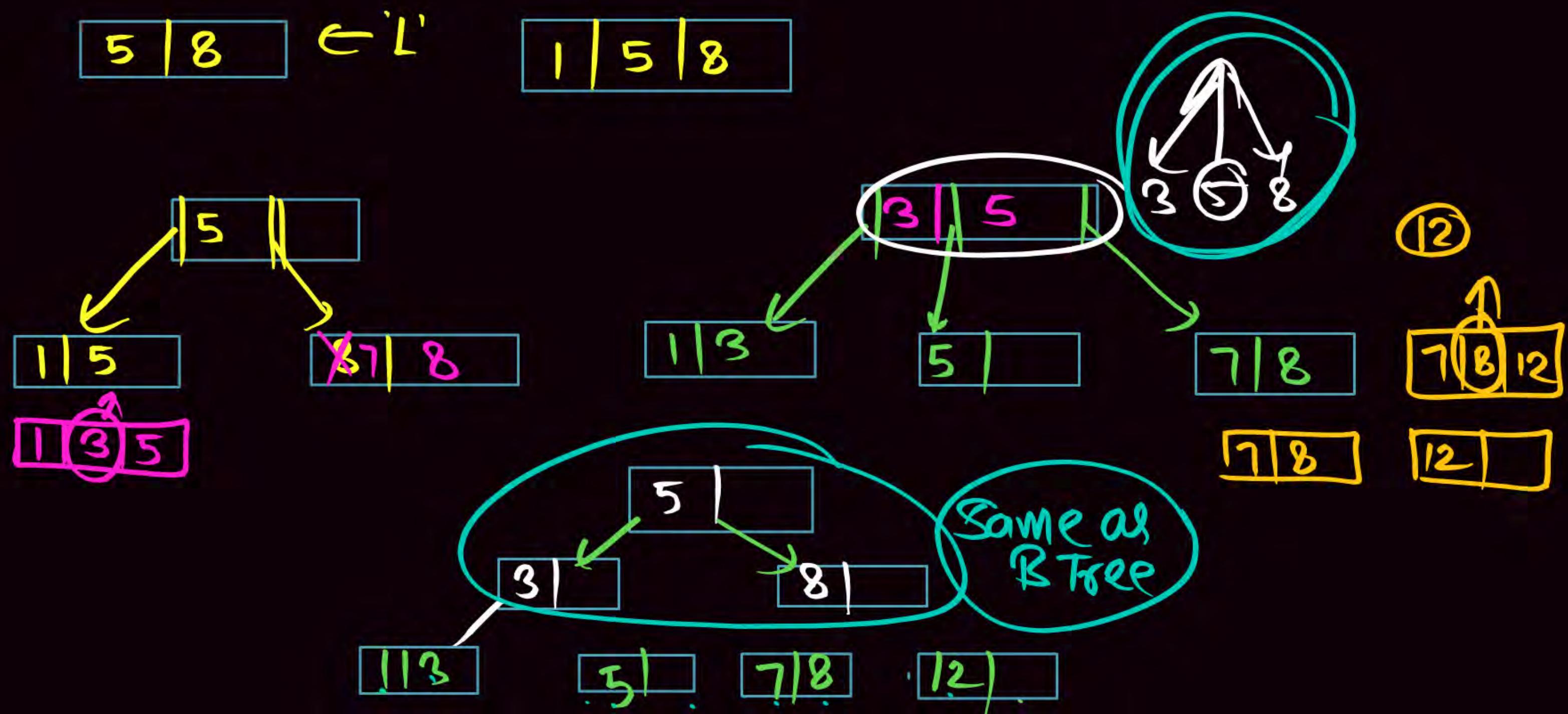


D



8, 5, 1, 7, 3, 12, 9, 6

ORDER = 3      B + Free  
left Biasing



Internal Node  $\Rightarrow$  B & R+ Tree Same

Leaf Node  $\Rightarrow$  keys Copied in R+ Tree



## 2 mins Summary



Topic

DBMS Part 08

Topic



THANK - YOU