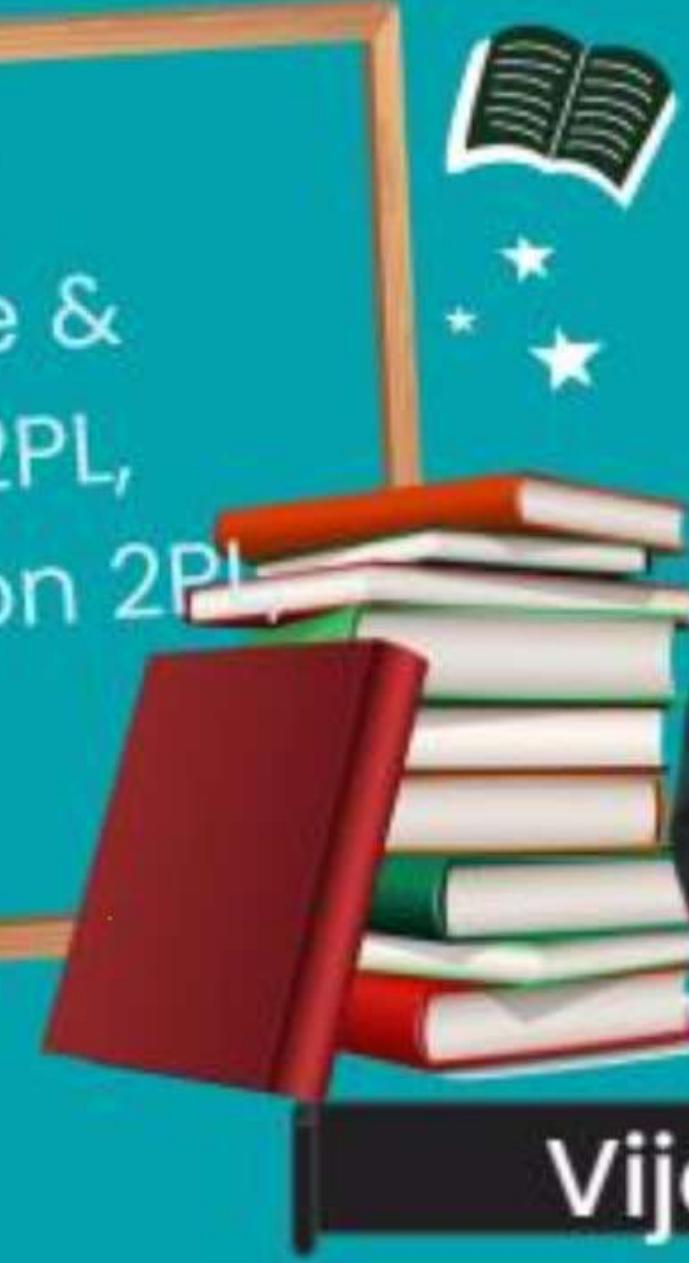


COMPUTER SCIENCE

Database Management System

Transaction Concept:
Recoverable Schedule &
Lock Based Protocol(2PL,
Strict 2PL, Conservation 2PL)
Time stamp Protocol

Lecture_04



Vijay Agarwal sir

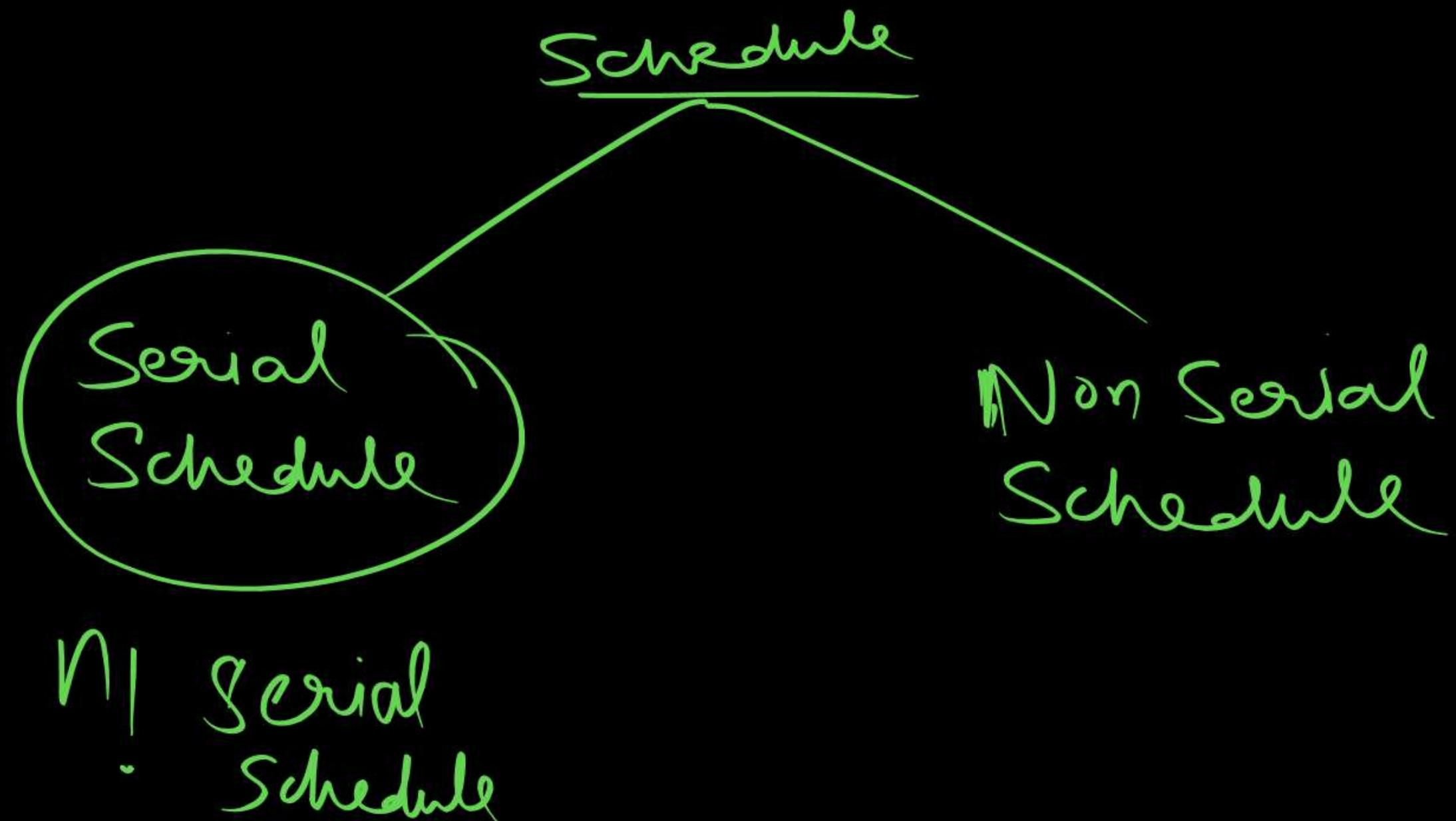


Today Goal



Transaction Concept

↳ A C I D Property



2 Transaction then $2! \Rightarrow 2$ Serial Schedule

$(T_1 \ T_2)$

$(T_2 \ T_1)$

3 Transaction then $3! \Rightarrow 6$ Serial Schedule

$(T_1 \ T_2 \ T_3)$

$(T_1 \ T_3 \ T_2)$

$(T_2 \ T_1 \ T_3)$

$(T_2 \ T_3 \ T_1)$

$(T_3 \ T_1 \ T_2)$

$(T_3 \ T_2 \ T_1)$

Schedules

- ❑ Schedule: a sequences of instructions that specify the chronological order in which instructions of concurrent transactions are executed.
 - ❖ A schedule for a set of transactions must consist of all instructions of those transactions
 - ❖ Must preserve the order in which the instructions appear in each individual transaction.
- ❑ A transaction that successfully completes its execution will have a commit instructions as the last statement
 - ❖ By default transaction assumed to execute commit instruction as its last step

- A transaction that fails to successfully complete its execution will have an abort instruction as the last statement.

~~A = 2000~~
~~T₁~~ transfer 100 Rs from A to B, and T₂ transfer 10% of the balance from A to B.

Schedule 1

T ₁	T ₂
<pre> read (A) A = 2000 A := A - 100 write (A) A = 1900 read (B) B := B + 100 write (B) commit B = 3100 </pre> <p><i>Consistent</i></p> <p><i>A = 1710</i> <i>B = 3290</i> <i>(5000)</i></p> <p><i>S₁ < T₁, T₂ ></i></p>	<pre> read (A) A = 1900 temp := A * 0.1 temp = 190 A := A - temp write (A) A = 1710 read (B) B := B + temp write (B) Commit B = 3290 </pre>

Serial schedule in which T₁ is followed by T₂:

Schedule 2

T ₁	T ₂
<pre> read (A) A = 2000 temp := A * 0.1 temp = 200 A := A - temp write (A) A = 1800 read (B) B := B + temp write (B) Commit B = 3200 </pre> <p><i>Consistent</i></p> <p><i>A = 1800</i> <i>B = 3200</i> <i>(3300)</i> <i>+ B = 5000</i></p> <p><i>S₂ < T₂, T₁ ></i></p>	<pre> read (A) temp := A * 0.1 A := A - temp write (A) read (B) B := B + temp write (B) Commit </pre>

serial schedule where T₂ is followed by T₁

Note

Serial Schedule (all Serial Schedule [n!])

are always consistent

Note

Non Serial Schedule (Concurrent execution)

May ☺ May Not be Consistent

of threads

W

n!

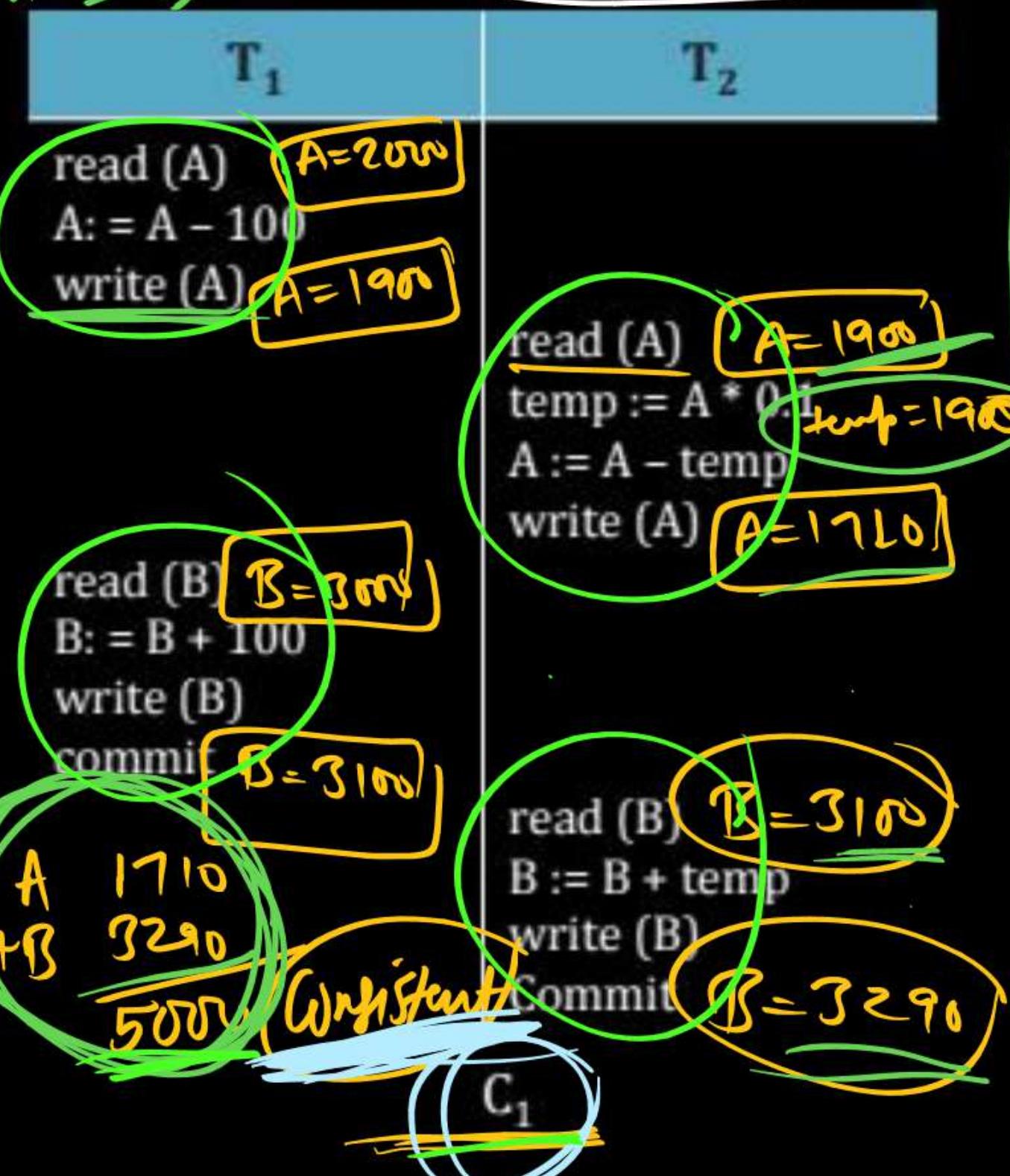
Why Concurrent Execution?

- To Improve CPU Utilization
- Enhanced Throughput
- Effective Resource Utilization
- etc

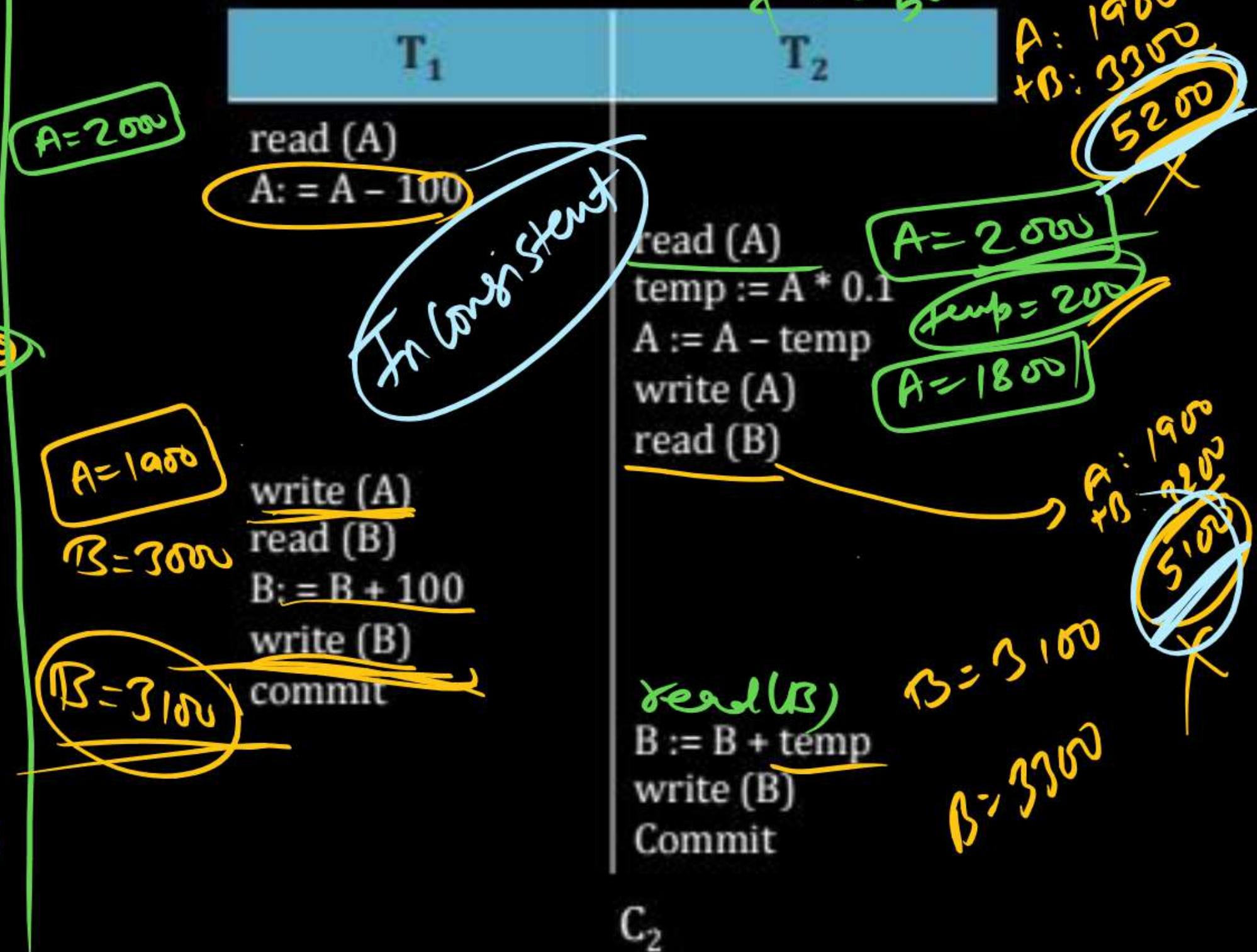
P
W

$$\begin{aligned} A &= 2000 \\ \times B &= 3500 \\ \hline A+B &= 5500 \end{aligned}$$

Schedule 3



Schedule 4



C₁ ⇒ Equal to Serial Schedule S₁(T₁, T₂)

Serializable



Consistent

Serializable Schedule

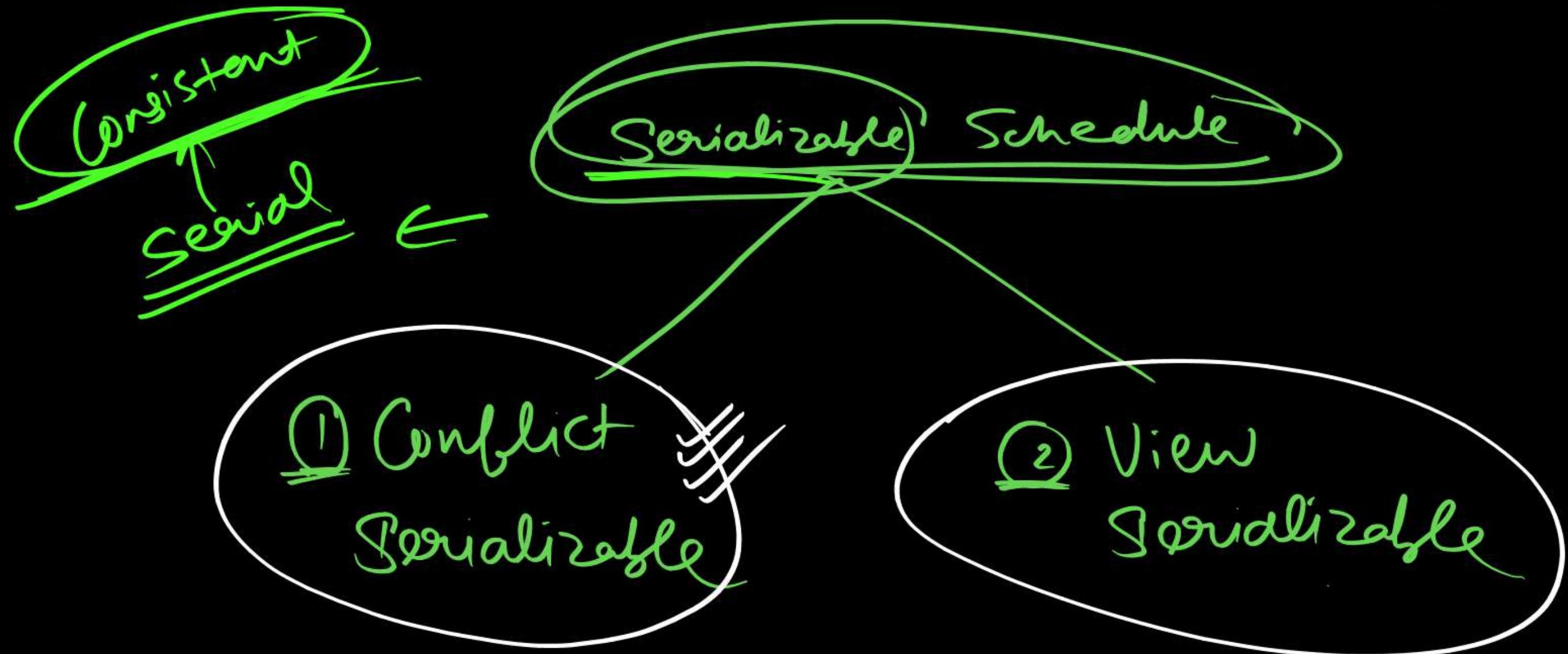
If a Concurrent Execution (Non Serial Schedule)

has been exerted, that could have the same effect on the Database, as a Schedule exerted without any Concurrent Execution (Any Serial Schedule).
Called Serializable Schedule.

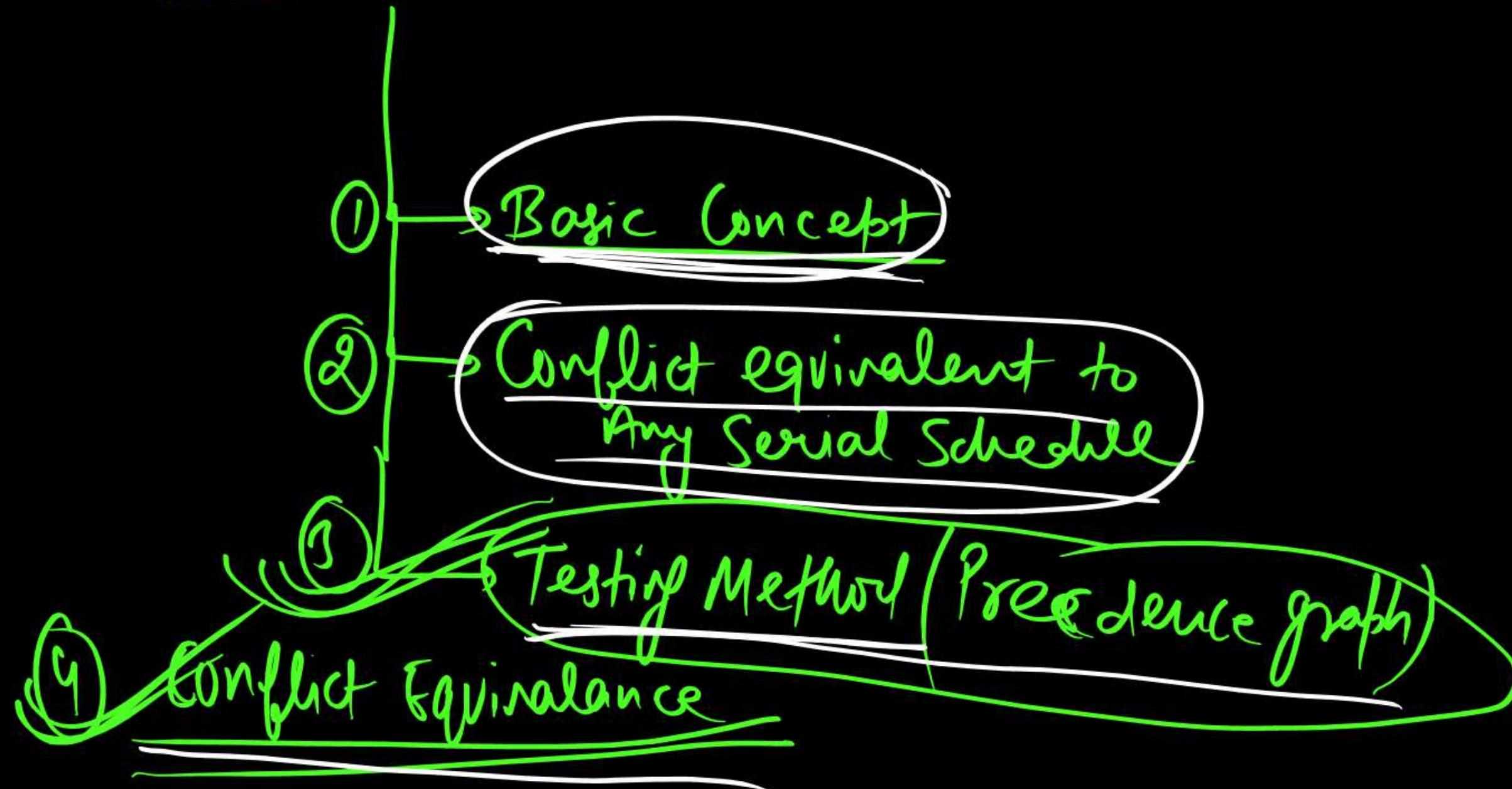
NIR

Serializable Schedule always consistent

P
W



Conflict Serializable



Conflict InstnSame
Date

$$R(A) - W(A)$$

$$W(A) - R(A)$$

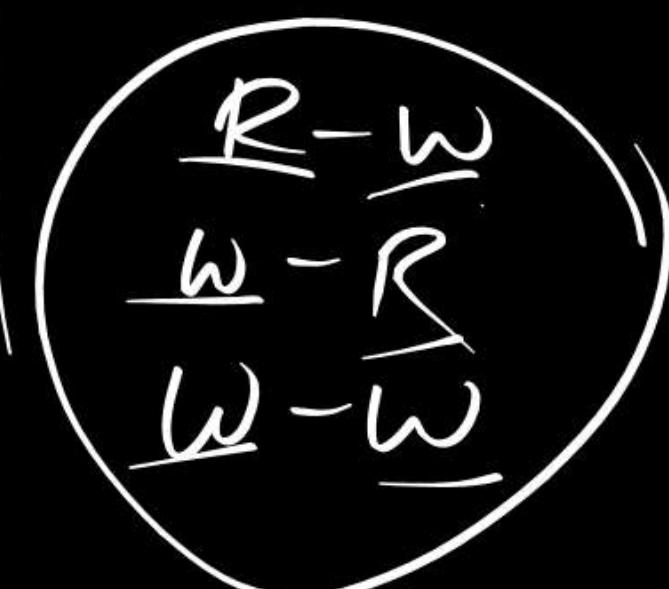
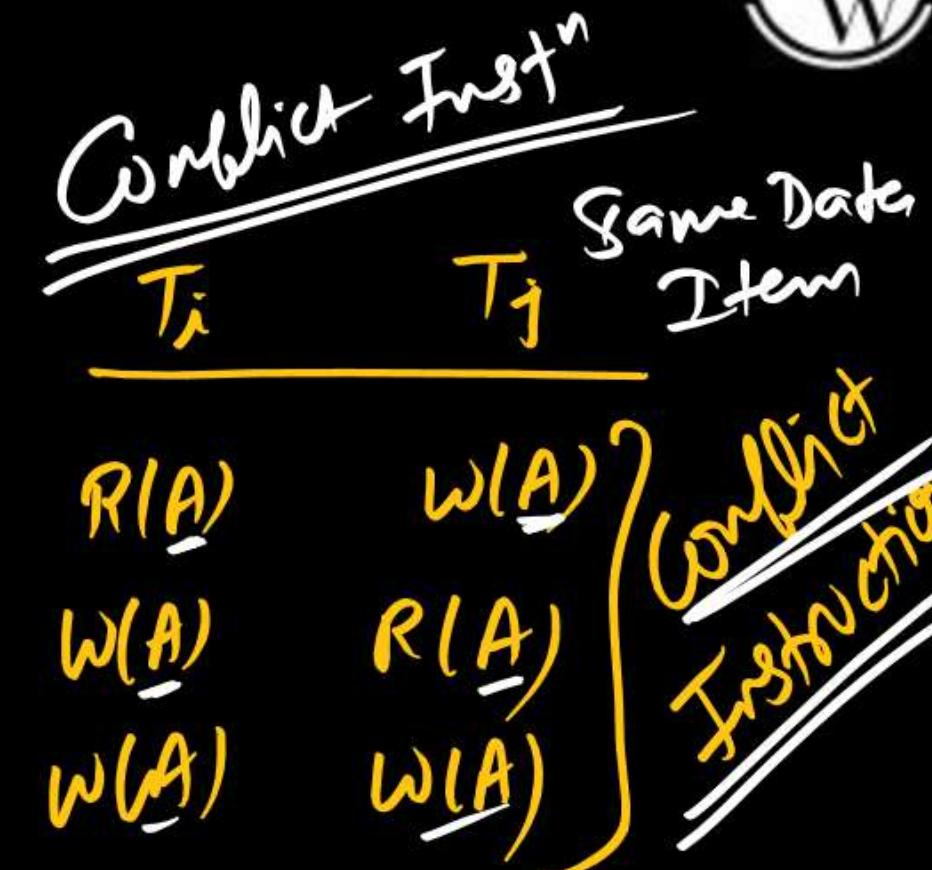
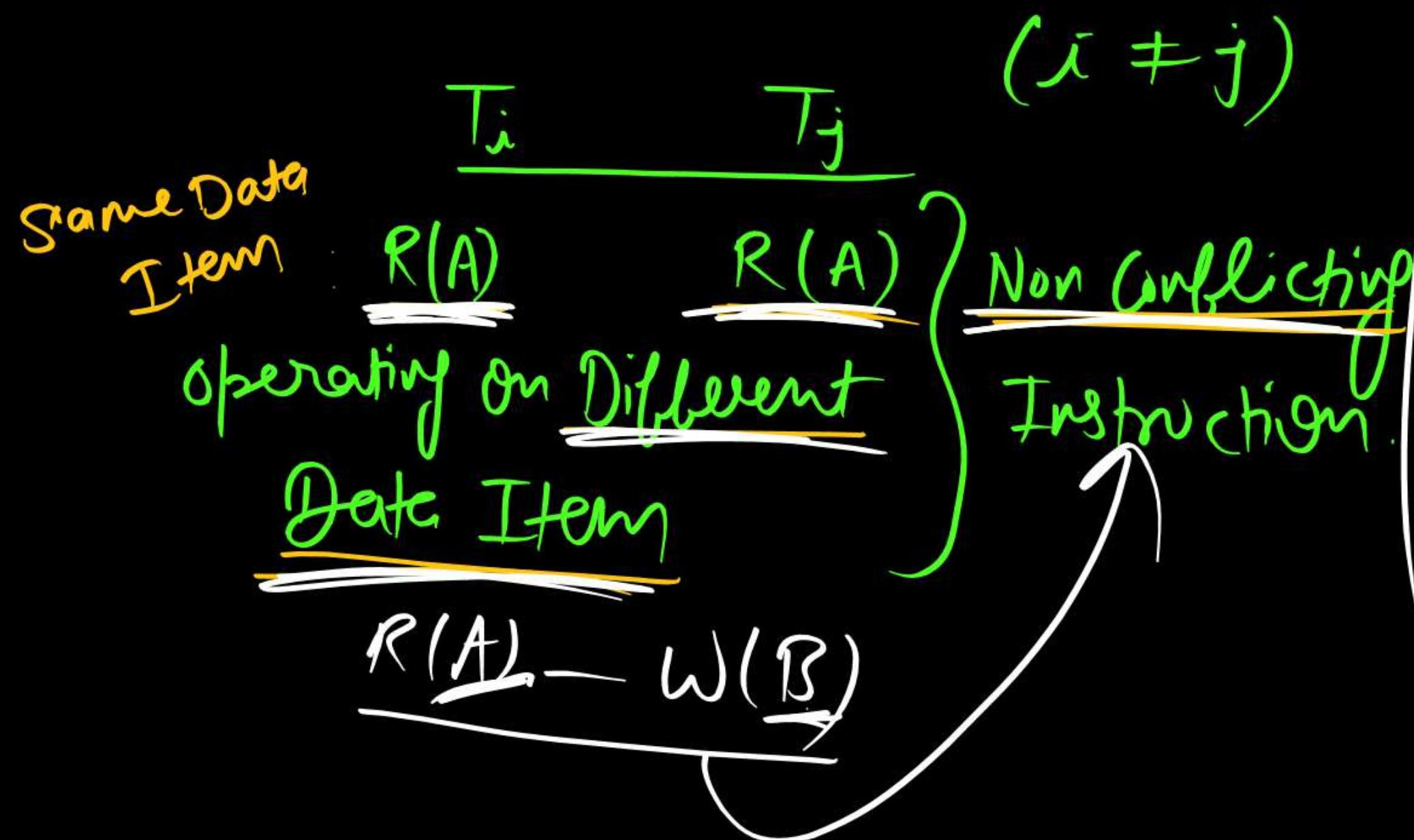
$$W(A) - W(A)$$

~~Non Conflict~~

$$R(A) - R(A)$$

Different Date
exam

Non Conflict Instruction



Serializability

- Basic Assumption: Each transaction preserves database consistency.
- Thus, serial execution of a set of transactions preserves database consistency.
- A (possibly concurrent) schedule is serializable if it is equivalent to a serial schedule. Different forms of schedule equivalence give rise to the notions of:
 1. Conflict serializability
 2. view serializability

Conflicting Instructions

- **S.** Instructions l_i and l_j of transactions T_i and T_j respectively, conflict if and only if there exists some item Q accessed by both l_i and l_j , and at least one of these instructions wrote Q .

1. $l_i = \text{read}(Q), l_j = \text{read}(Q)$. l_i and l_j don't conflict.
 2. $l_i = \text{read}(Q) l_j = \text{write}(Q)$. They conflict.
 3. $l_i = \text{write}(Q) l_j = \text{read}(Q)$. They conflict
 4. $l_i = \text{write}(Q) l_j = \text{write}(Q)$. They conflict
- Intuitively, a conflict between l_i and l_j forces a (logical) temporal order between them.
 - ❖ If l_i and l_j are consecutive in a schedule and they do not conflict, their results would remain the same even if they had been interchanged in the schedule.

Conflict Serializable

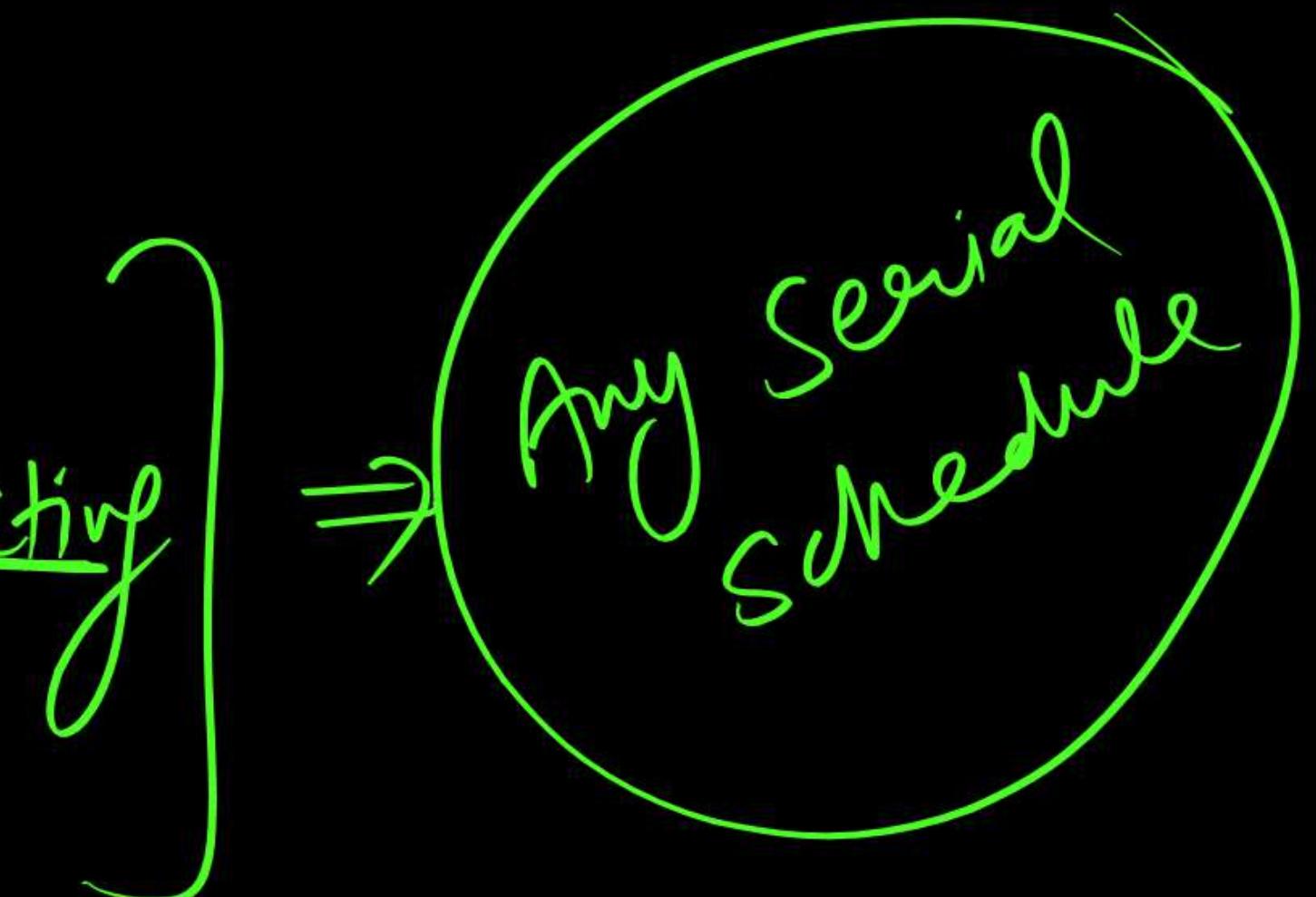


Non Serial Schedule

consists into

Swap of series of Non Conflicting

Instruction

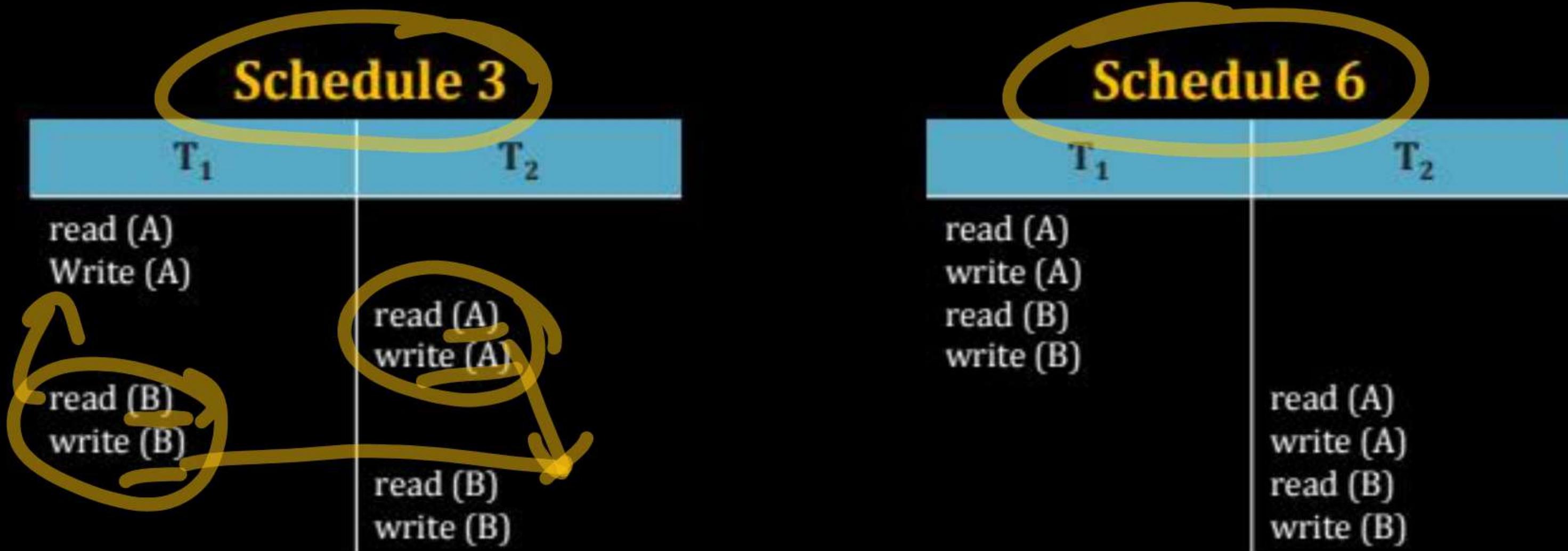


Conflict Serializability

-  If a schedule S can be transformed into a schedule S' by a series of swaps of non-conflicting instructions, we say that S and S' are conflict equivalent.
-  We say that a schedule S is conflict serializable if it is conflict equivalent to a serial schedule.

Conflict Serializability (Cont.)

- Schedule 3 can be transformed into Schedule 6, a serial schedule where T_2 follows T_1 , by series of swaps of non-conflicting instructions. Therefore Schedule 3 is conflict serializable.



P
W

Conflict + Serializable

$S_1 \subset T_1 \cap T_2$



T_1	T_2
$R(A)$	
$W(A)$	
$R(B)$	
$W(B)$	
$R(A)$	
$W(A)$	
$R(B)$	
$W(B)$	
$R(B)$	
$W(B)$	

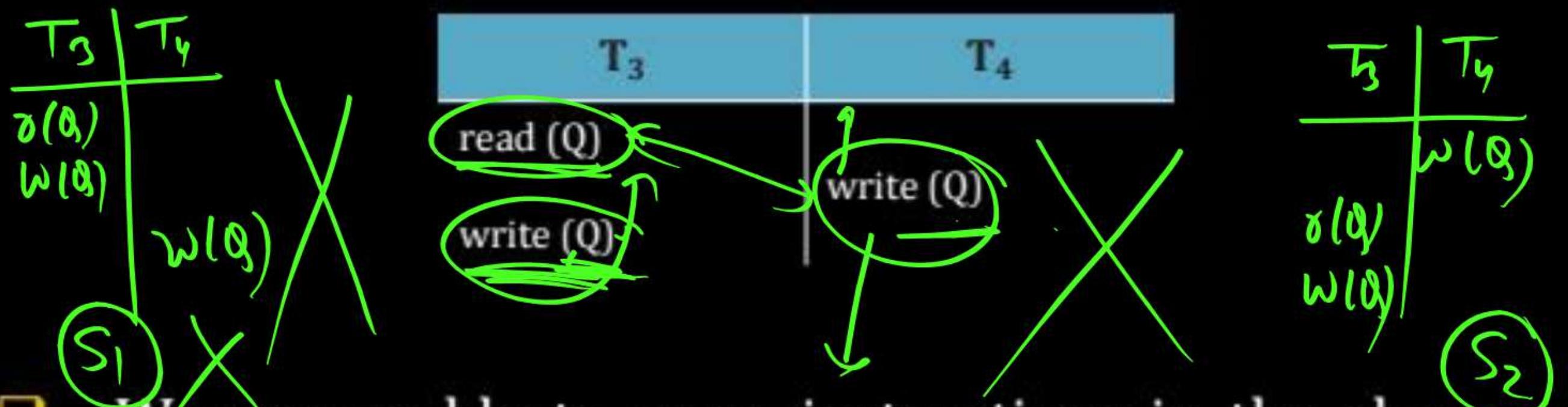
$S_2 \subset T_2 \cap T_1$

T_1	T_2
$R(A)$	
$W(A)$	
$R(B)$	
$W(B)$	
$R(A)$	
$W(A)$	
$R(B)$	
$W(B)$	

$S_3 \subset T_1 \cap T_2$

Conflict Serializability (Cont.)

- Example of a schedule that is not conflict serializable:



- We are unable to swap instructions in the above schedule to obtain either the serial schedule $< T_3, T_4 >$, or the serial schedule $< T_4, T_3 >$



Testing for Conflict Serializability

Directed edge

Directed graph

Precedence Graph Method

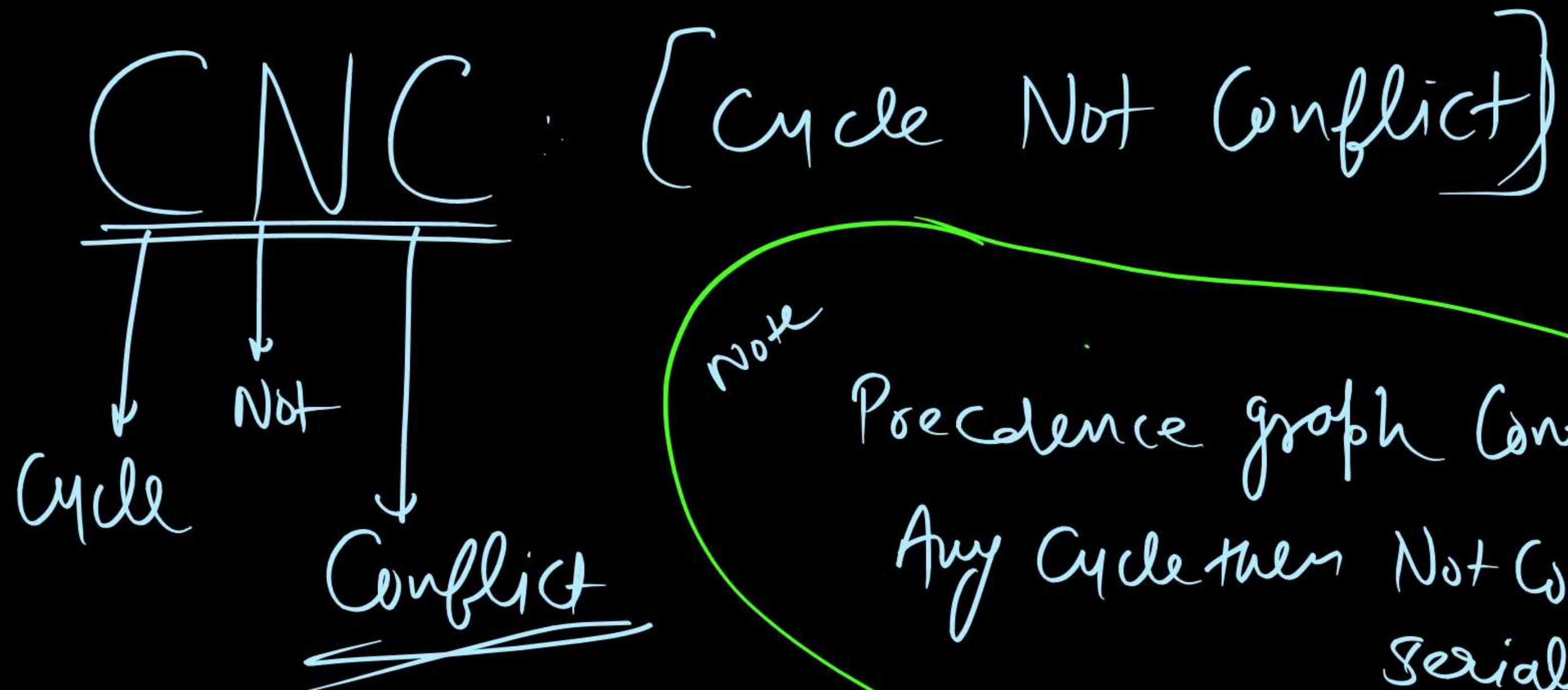
$$G : (V, E)$$

V: Vertex: Set of Transaction

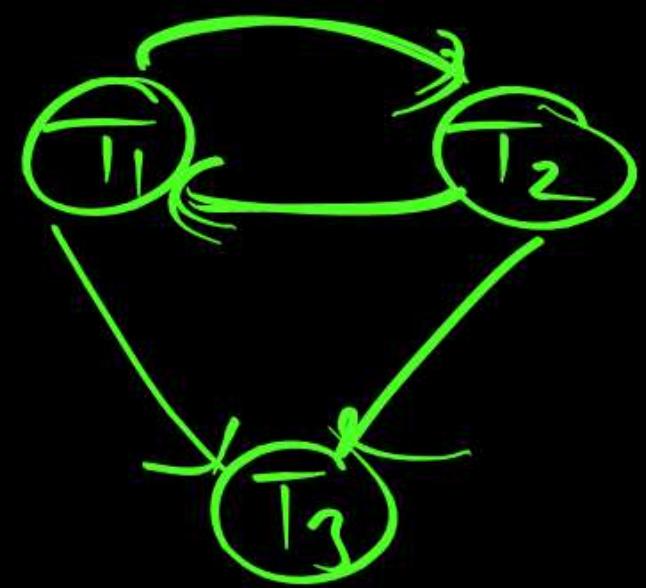
E: Edge

$$\underline{T_i \rightarrow T_j}$$

<u>Conflict Instn</u>
$T_i : R(Q)$
$T_j : W(Q)$
$R(Q)$
$W(Q)$



Note : Precedence graph Contains
Any cycle then Not Conflict
Serializable



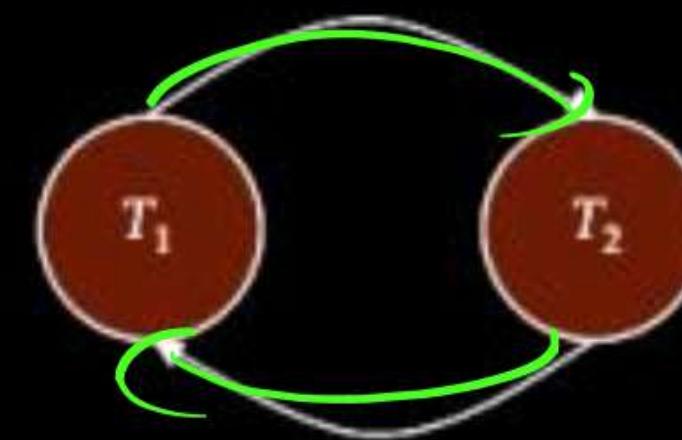
cycle Not Conflict .

Testing for Serializability

□ Testing for conflict serializability.

- ❖ Consider some schedule of a set of transactions T_1, T_2, \dots, T_n
- ❖ Precedence graph — a direct graph where the vertices are the transactions (names).
- ❖ We draw an arc from T_i to T_j if the two transaction conflict, and T_i accessed the data item on which the conflict arose earlier.
- ❖ We may label the arc by the item that was accessed.

Example:



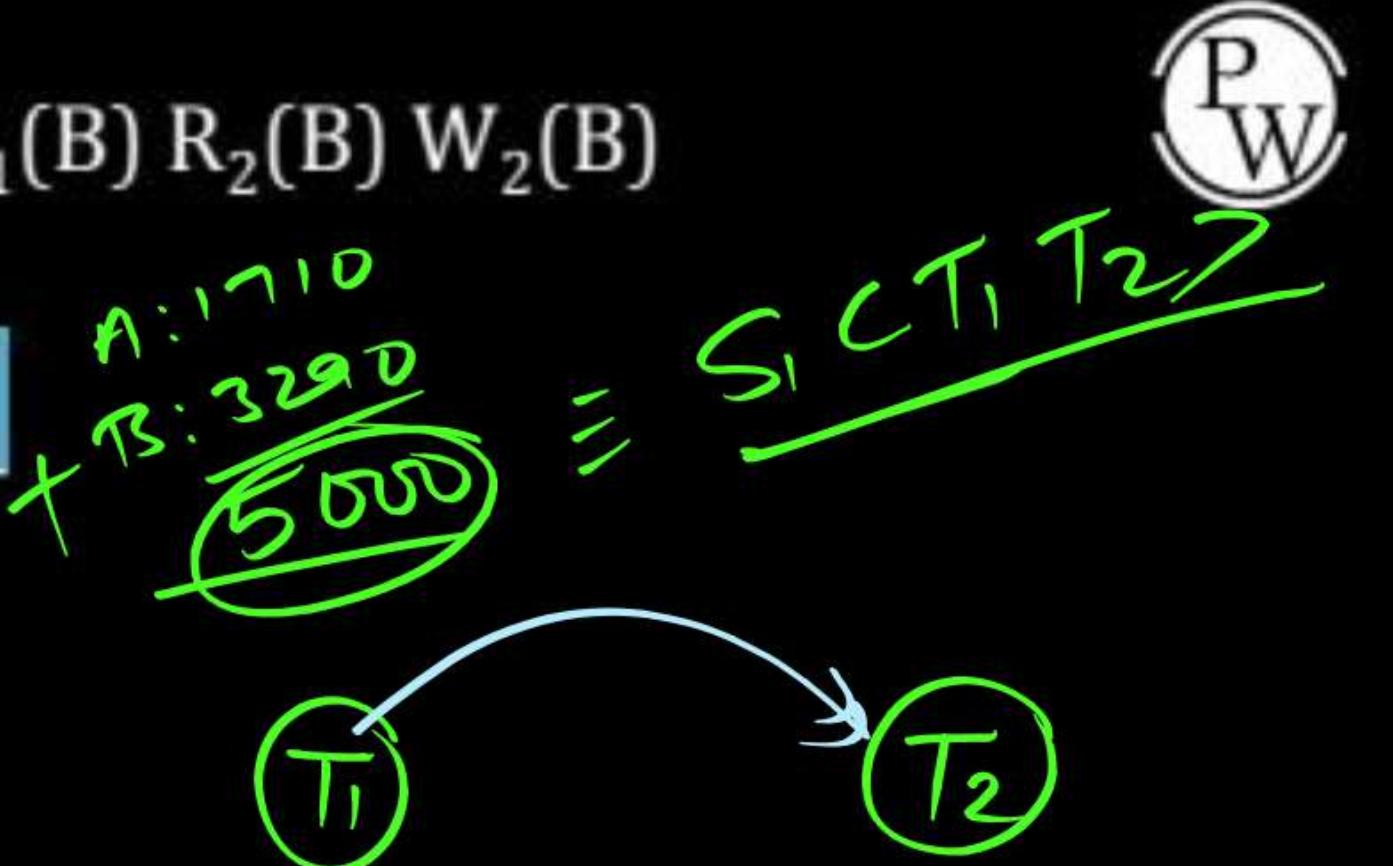
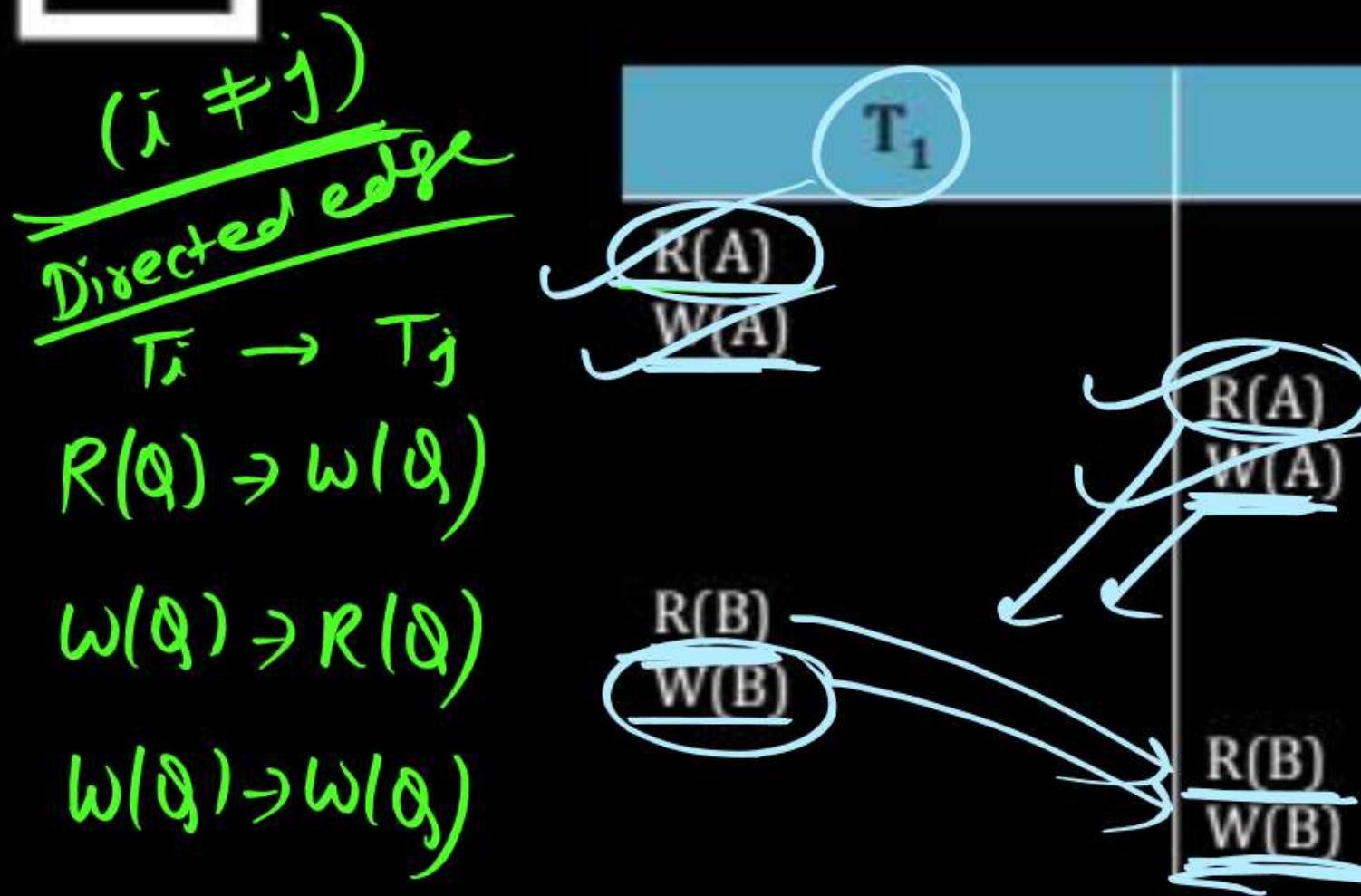
CNC: Cycle Not Conflict.

A schedule is conflict serializable if and only if its precedence graph is acyclic.

NOTE: CNC [Cycle not conflict serializable]

Q.

S: R₁(A) W₁(A) R₂(A) W₂(A) R₁(B) W₁(B) R₂(B) W₂(B)



Conflict Serializable

$\langle T_1 \overline{T_2} \rangle$

Q.

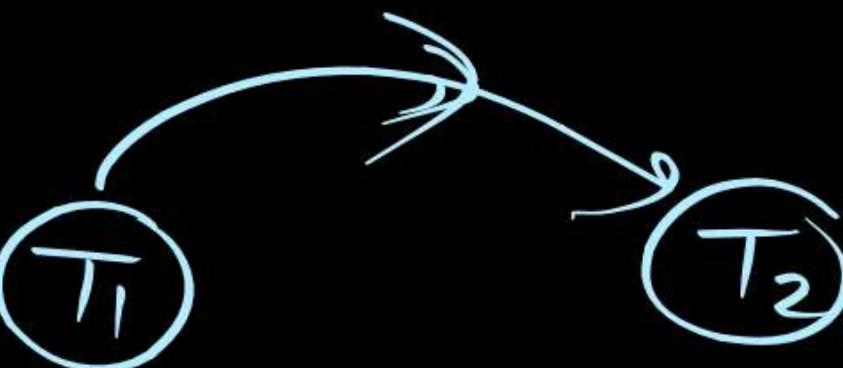
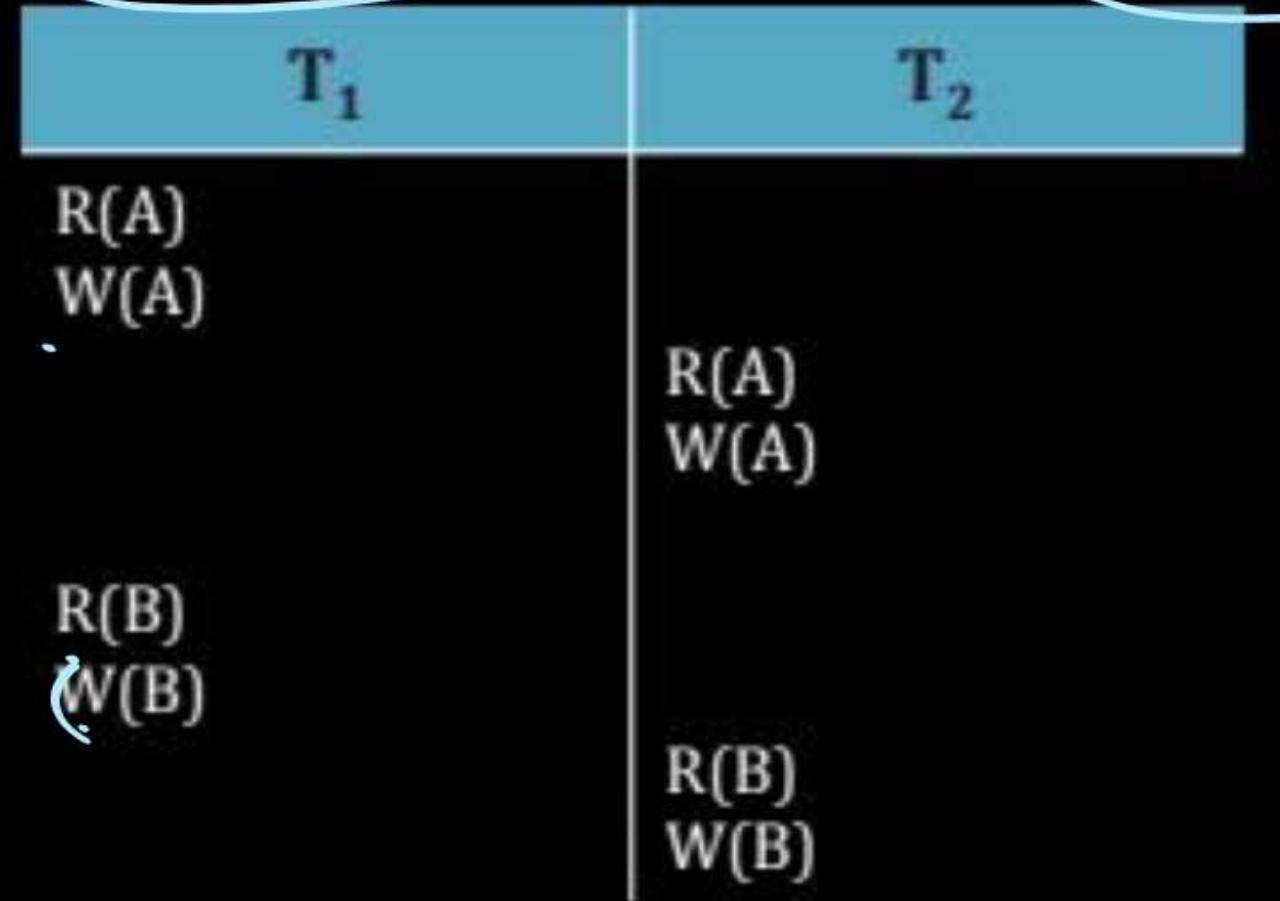
S: ~~R₁(A) W₁(A) R₂(A) W₂(A) R₁(B) W₁(B) R₂(B) W₂(B)~~

$(i \neq j)$
Directed edge
 $T_i \rightarrow T_j$

$R(Q) \rightarrow W(Q)$

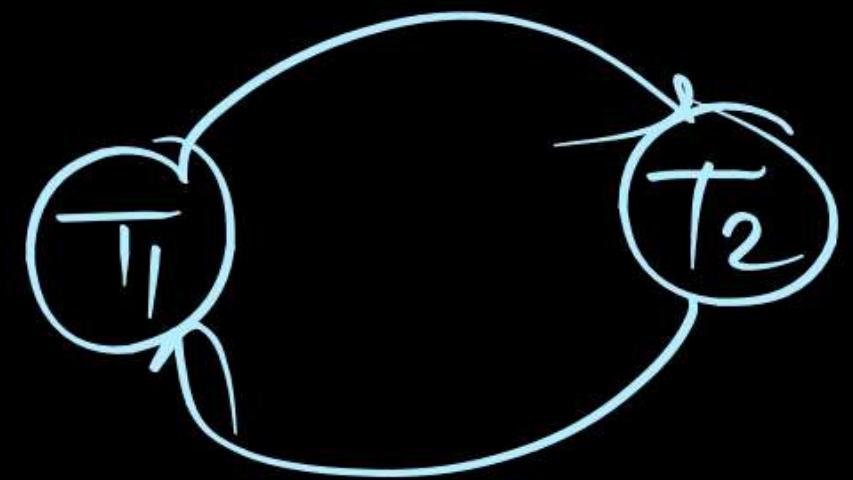
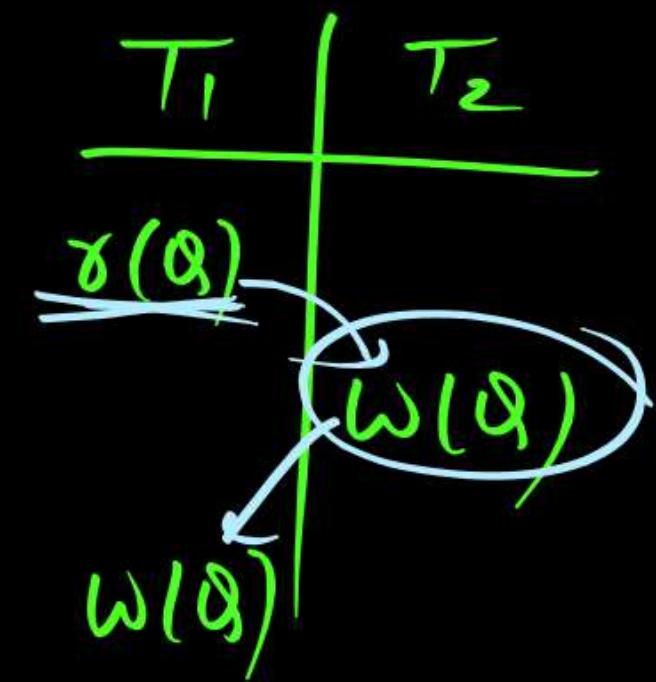
$W(Q) \rightarrow R(Q)$

$W(Q) \rightarrow W(Q)$



P
W



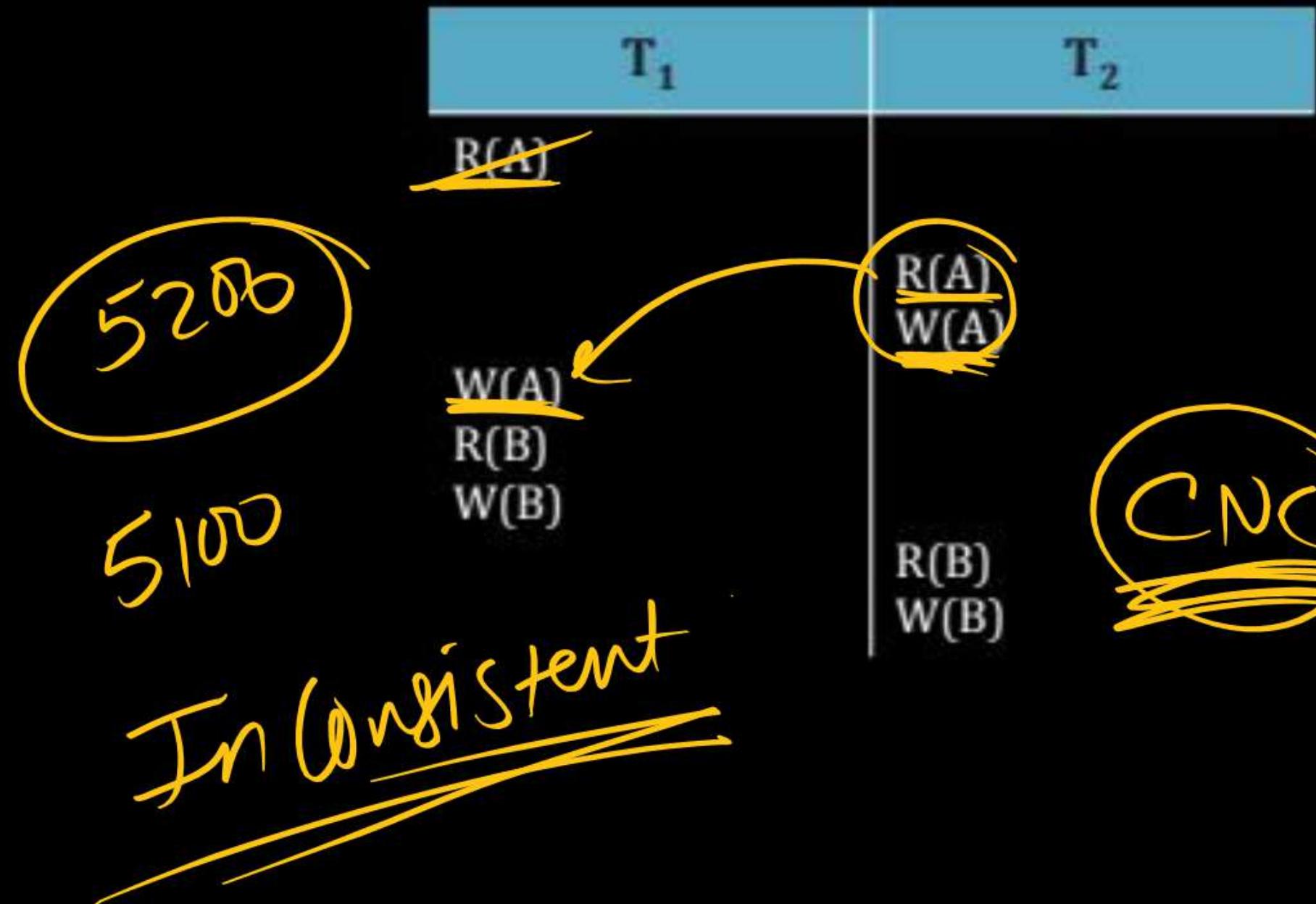


Cycle Not Conflict .

Q.

$R_1(A) R_2(A) W_2(A) W_1(A) R_1(B) W_1(B) R_2(B) W_2(B)$

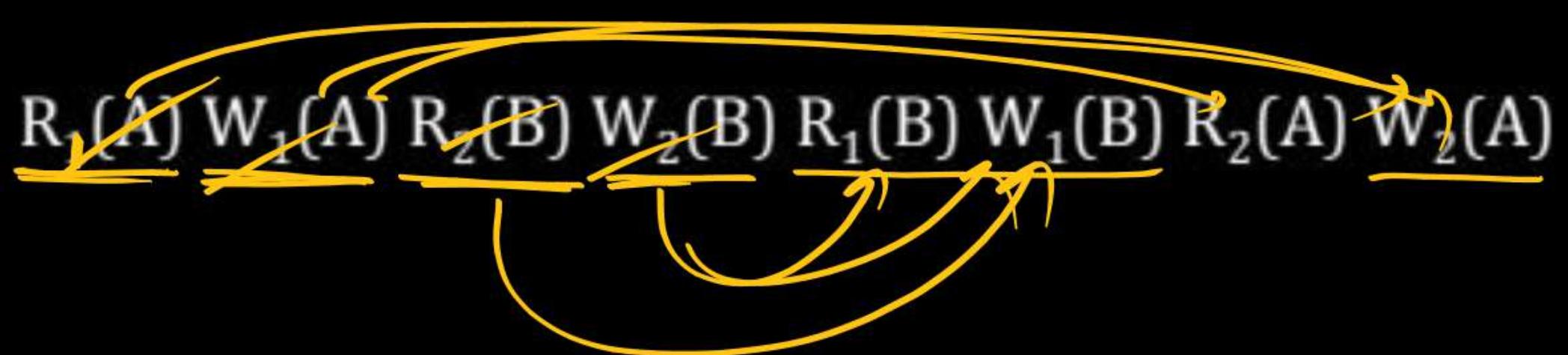
P
W



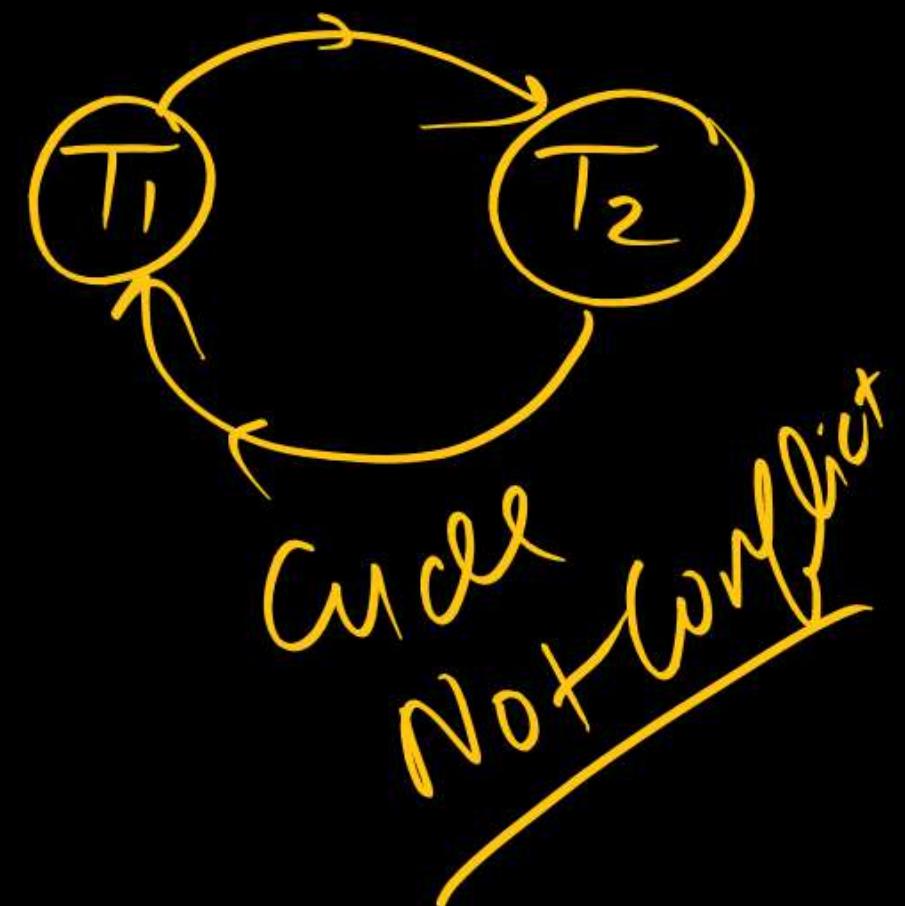
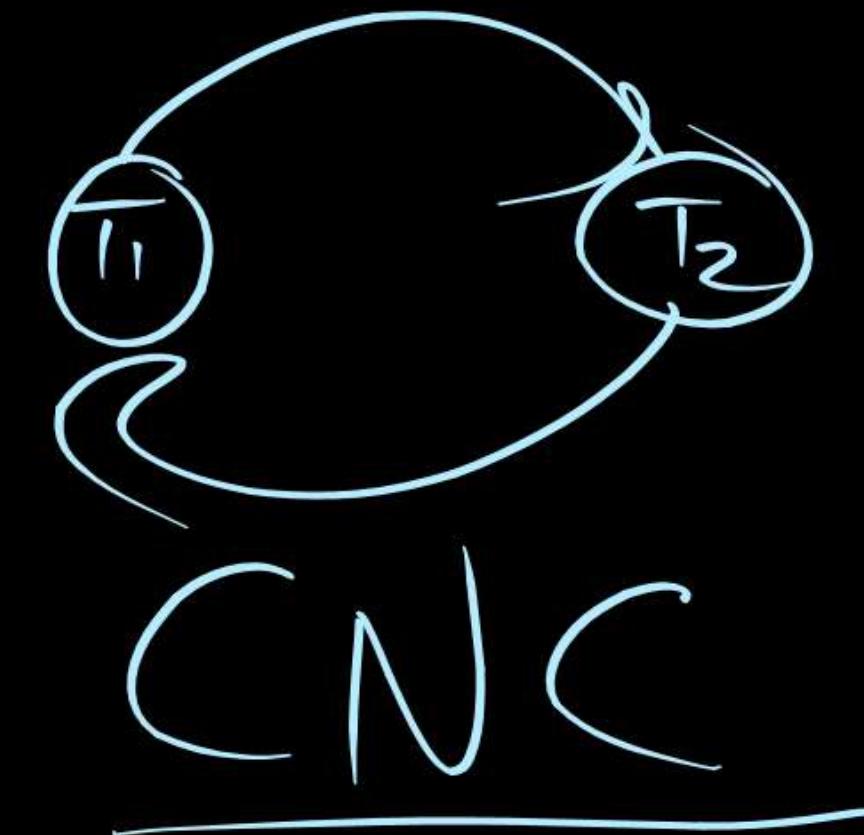
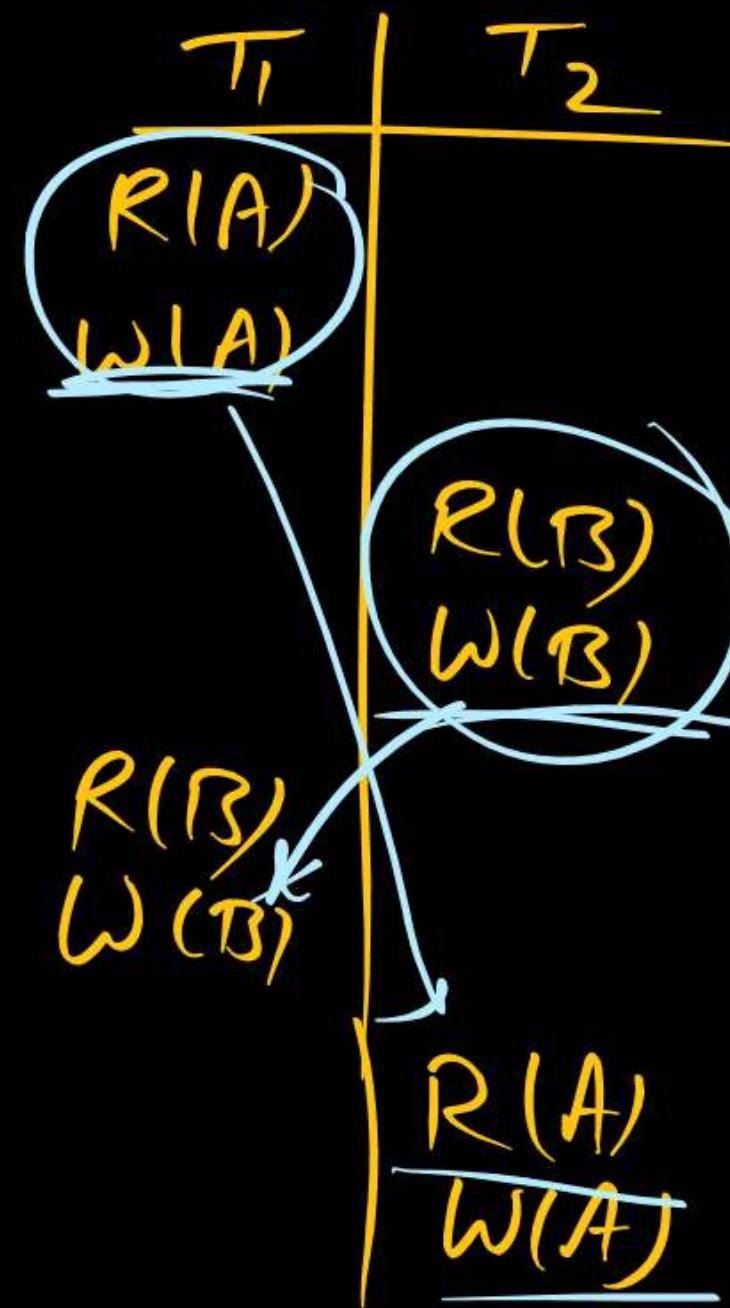
CNC

Cycle Not Conflict

Q.



P
W



Start from T_i which
Indegree = 0 \Rightarrow No Incoming edge

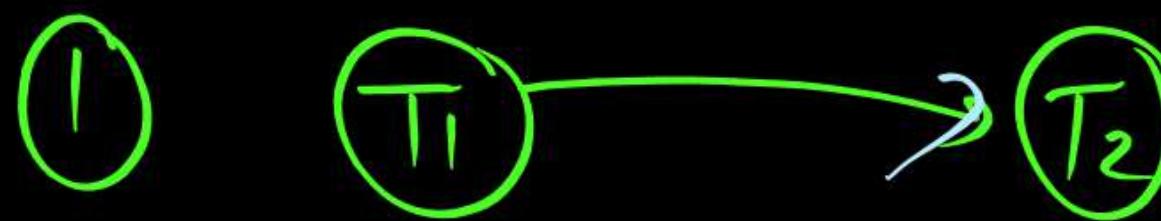
(S)

Serializability Order

P
W

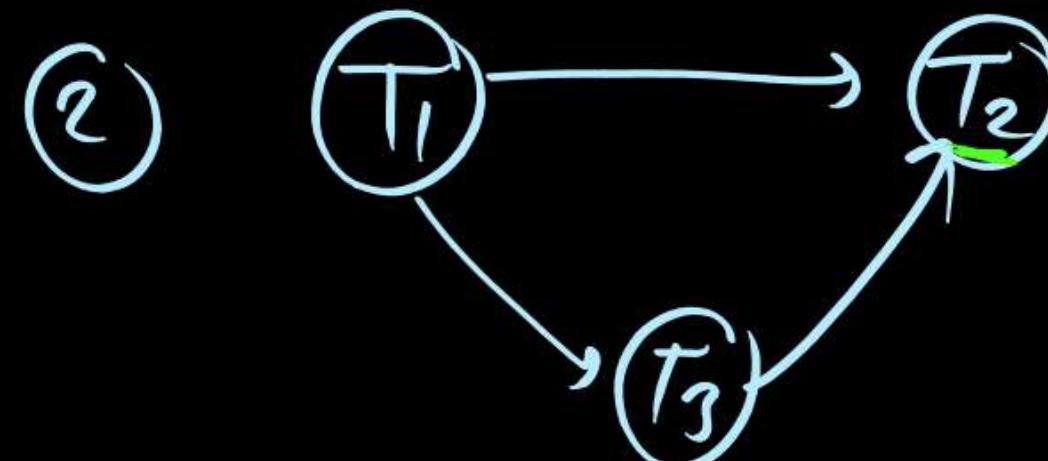
(Topological Sorting)

If Conflict Serializable schedule equivalent to Which Serial Schedule ab
Serializability order S.



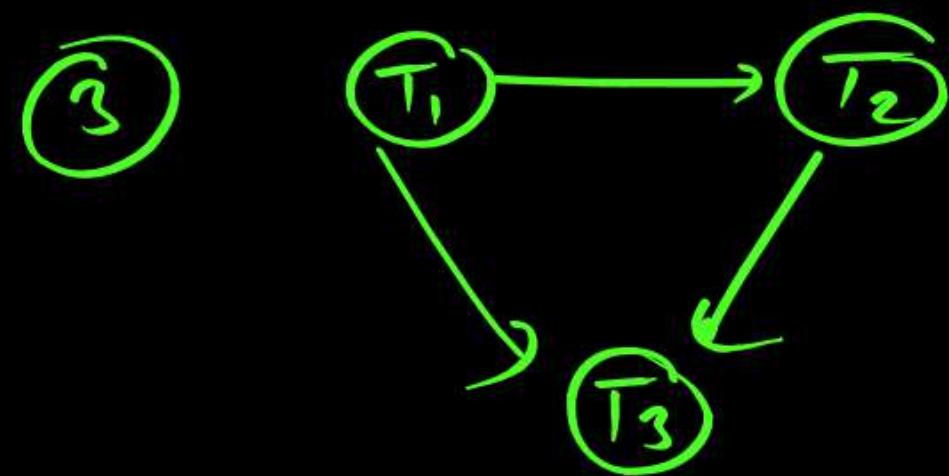
(T_1, T_2)

Serial Schedule
 (T_1, T_2)

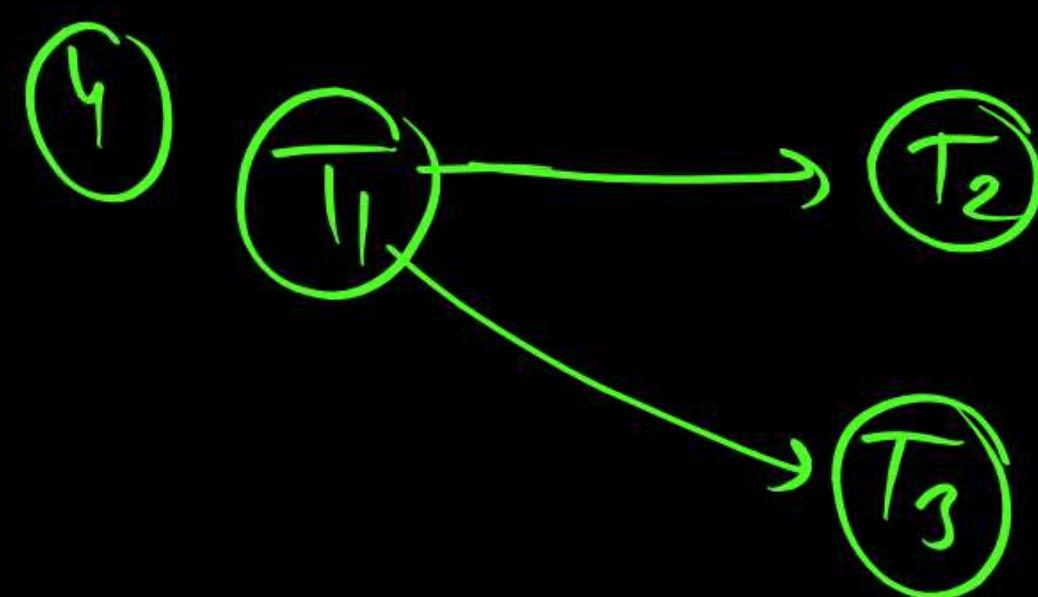


(T_1, T_3, T_2)

P
W



$\langle T_1 \ T_2 \ T_3 \rangle$



$\langle T_1 \ T_2 \ T_3 \rangle$

⑤

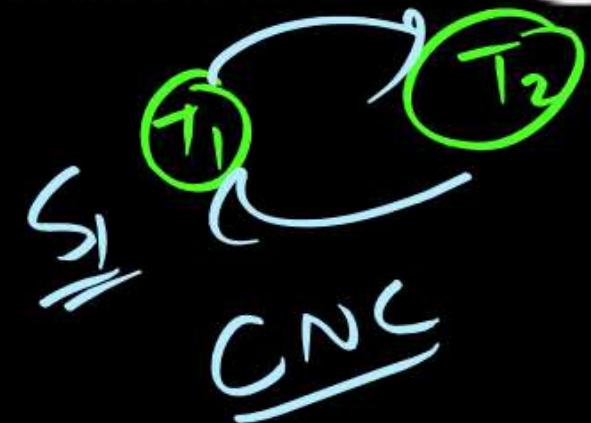
$\langle T_1 \ T_3 \ T_2 \rangle$

Q.

Consider the following schedules involving two transactions.
Which one of the following statements is TRUE?

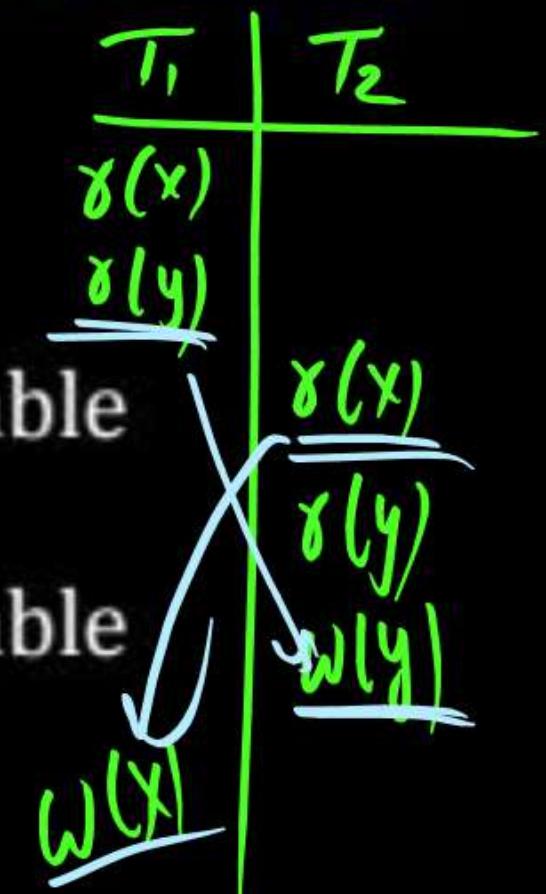
S_1 : $r_1(X); r_1(Y); r_2(X); r_2(Y); w_2(Y); w_1(X)$

S_2 : $r_1(X); r_2(X); r_2(Y); W_2(Y); r_1(Y); w_1(X)$



[2007: 2 Marks]

- A Both S_1 and S_2 are conflict serializable
- B S_1 is conflict serializable and S_2 is not conflict serializable
- C S_1 is not conflict serializable and S_2 is conflict serializable
- D Both S_1 and S_2 are not conflict serializable

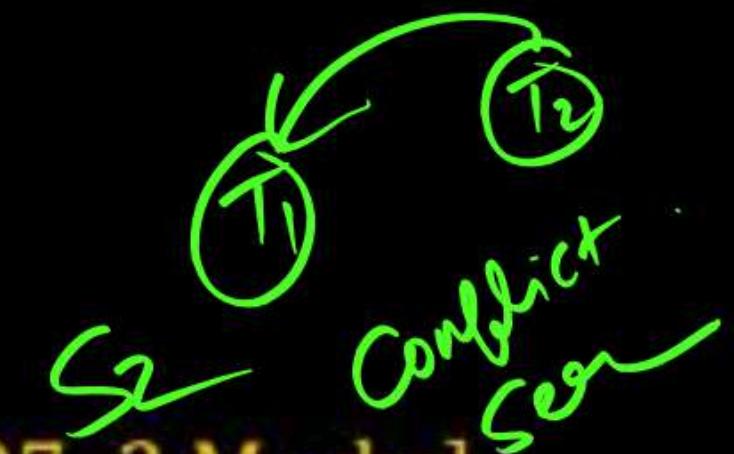


Q.

Consider the following schedules involving two transactions.
Which one of the following statements is TRUE?

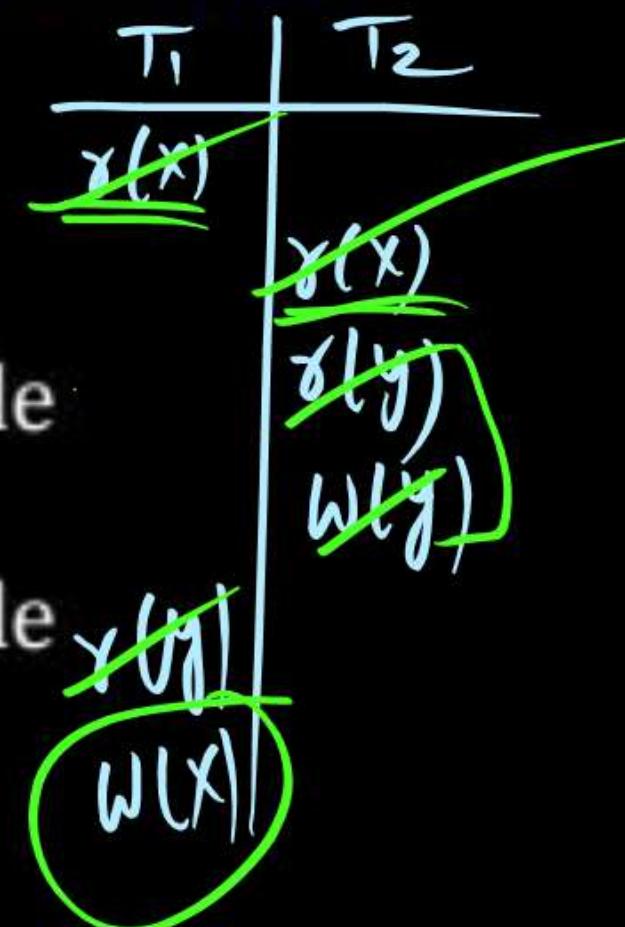
S_1 : $r_1(X); r_1(Y); r_2(X); r_2(Y); w_2(Y); w_1(X)$

S_2 : $r_1(X); r_2(X); r_2(Y); W_2(Y); r_1(Y); w_1(X)$



[2007: 2 Marks]

- A Both S_1 and S_2 are conflict serializable
- B S_1 is conflict serializable and S_2 is not conflict serializable
- C S_1 is not conflict serializable and S_2 is conflict serializable
- D Both S_1 and S_2 are not conflict serializable



Q.

Consider the following four schedules due to three transactions (indicated by the subscript) using read and write on a data item x , denoted by $r(x)$ and $w(x)$ respectively. Which one of them is conflict serializable?

[2014(Set-1): 2 Marks]

- A $r_1(x); r_2(x); w_1(x); r_3(x); w_2(x)$
- B $r_2(x); r_1(x); w_2(x); r_3(x); w_1(x)$
- C $r_3(x); r_2(x); r_1(x); w_2(x); w_1(x)$
- D $r_2(x); w_2(x); r_3(x); r_1(x); w_1(x)$

Q.

Let $R_i(z)$ and $W_i(z)$ denote read and write operations on a data element z by a transaction T_i , respectively. Consider the schedule S with four transactions.

P
W

$S: \underline{R_4(x)}, \underline{R_2(x)}, \underline{R_3(x)}, R_1(y), \underline{W_1(y)}, W_2(x), W_3(y), R_4(y)$

Which one of the following serial schedules is conflict equivalent to S ?

[2022: 2 Marks]

A

 $T_1 \rightarrow \underline{T_3} \rightarrow \underline{T_4} \rightarrow T_2$

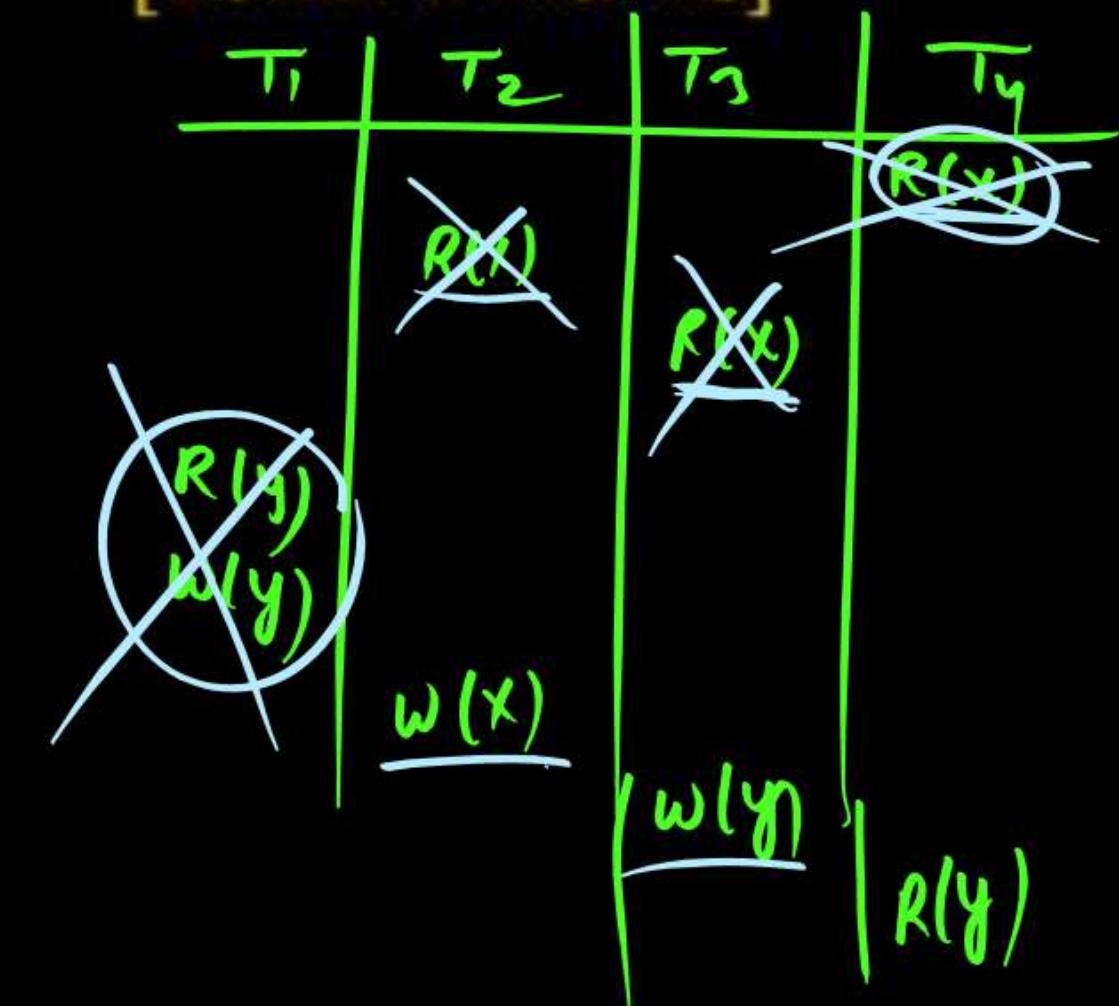
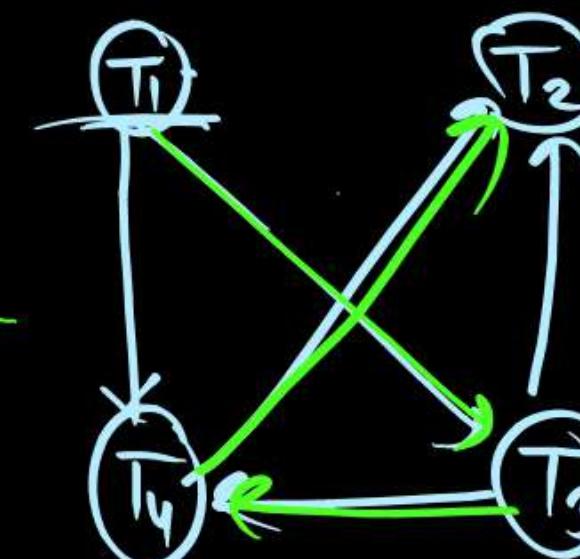
B

 $T_1 \rightarrow T_4 \rightarrow T_3 \rightarrow T_2$

C

 $\cancel{T_4} \rightarrow T_1 \rightarrow T_3 \rightarrow T_2$

D

 $\cancel{T_3} \rightarrow T_1 \rightarrow T_4 \rightarrow T_2$


Q.

Let $R_i(z)$ and $W_i(z)$ denote read and write operations on a data element z by a transaction T_i , respectively. Consider the schedule S with four transactions.

$S: R_4(x), R_2(x), R_3(x), R_1(y), W_1(y), W_2(x), W_3(y), R_4(y)$

Which one of the following serial schedules is conflict equivalent to S ?

[2022: 2 Marks]

A

$T_1 \rightarrow T_3 \rightarrow T_4 \rightarrow T_2$

B

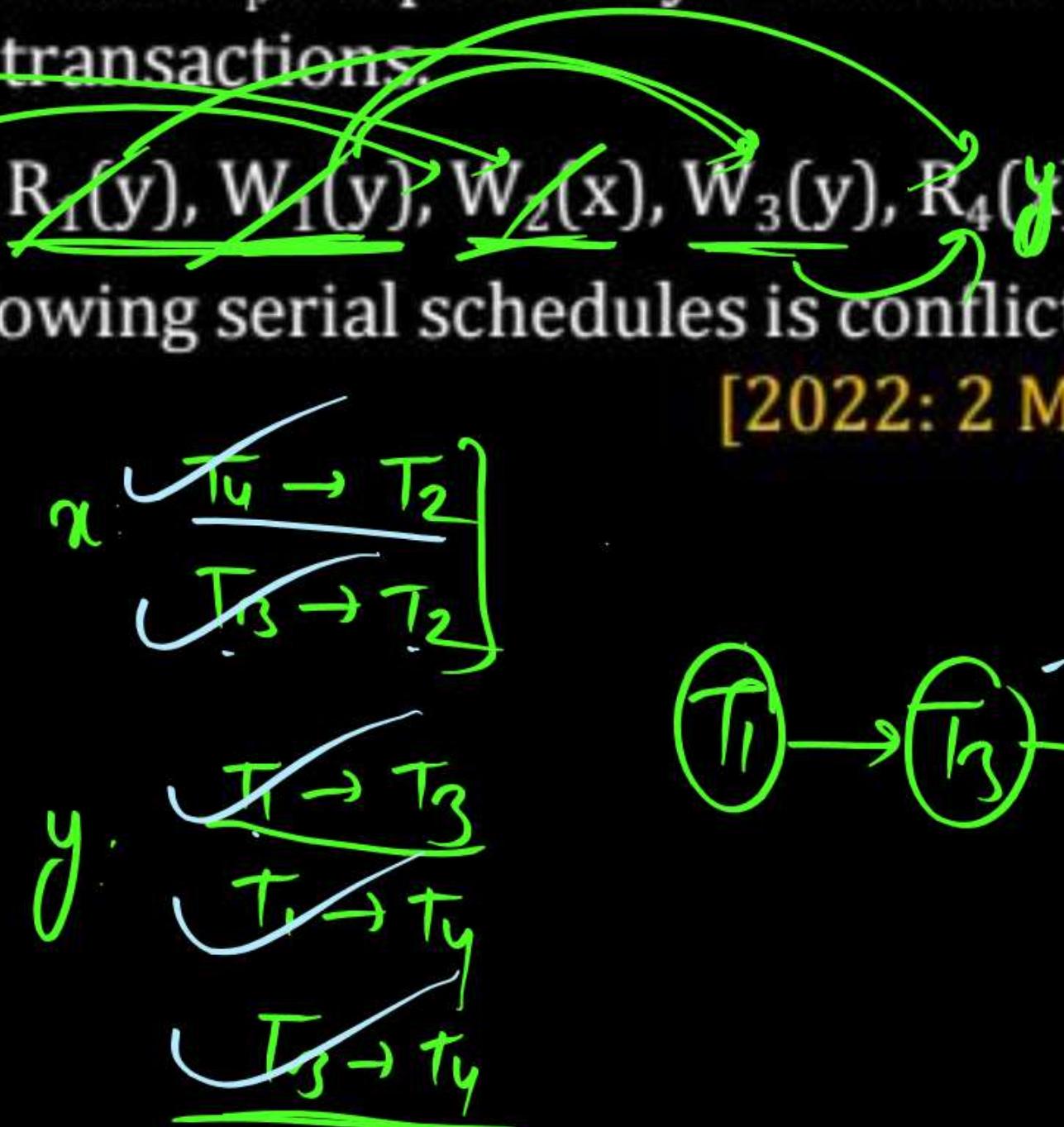
$T_1 \rightarrow T_4 \rightarrow T_3 \rightarrow T_2$

C

$\cancel{T_4 \rightarrow T_1 \rightarrow T_3 \rightarrow T_2}$

D

$T_3 \rightarrow T_1 \rightarrow T_4 \rightarrow T_2$



Q.

Consider the following transaction involving two bank accounts x and y.

read(x); x: = x - 50; write (x); read (y); y: = y + 50; write (y)

The constraint that the sum of the accounts x and y should remain constant is that of

[2015(Set-2): 1 Marks]

- A Atomicity
- B Consistency
- C Isolation
- D Durability

Conflict Serializable \Rightarrow Core Concept

Testing Method

Conflict Equivalence

Conflict Serializable

Swap of Non Conflict Instr \Rightarrow Any serializable

P
W

S_1 S_2

Conflict Equivalence

S_1 : $T_1 \rightarrow T_2$

①

Graph

Generalize
Order
Game

S_2 : $T_1 \rightarrow T_2$

②
Graph

Cycle

CNC

③

Next Poff (P, T, O)

check Direction of
each Conflict other
edge

Conflict Equivalence

$S_1 \& S_2$ Conflict equivalence

If all Conflict operation Must be
executed in same Order in $S_1 \& S_2$.

$$\begin{array}{cc} \frac{T_i}{R(A)} & \frac{T_j}{\omega(A)} \\ R(A) & \omega(A) \\ \omega(A) & R(A) \\ \omega(A) & \omega(A) \end{array} \left. \right\} \text{Conflict Operation}$$

Conflict Equivalent Schedule

Two schedule are said to be conflict equivalent, if all conflicting operations in both the schedules must be executed in the same order.

Q.

$S_1: R_1(x) W_1(x) R_2(y) W_2(y) R_1(y)$

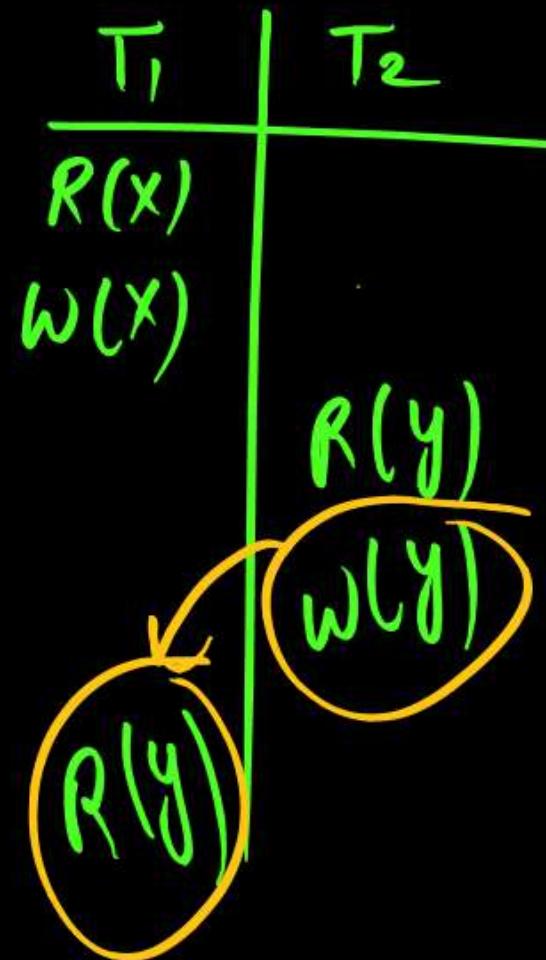
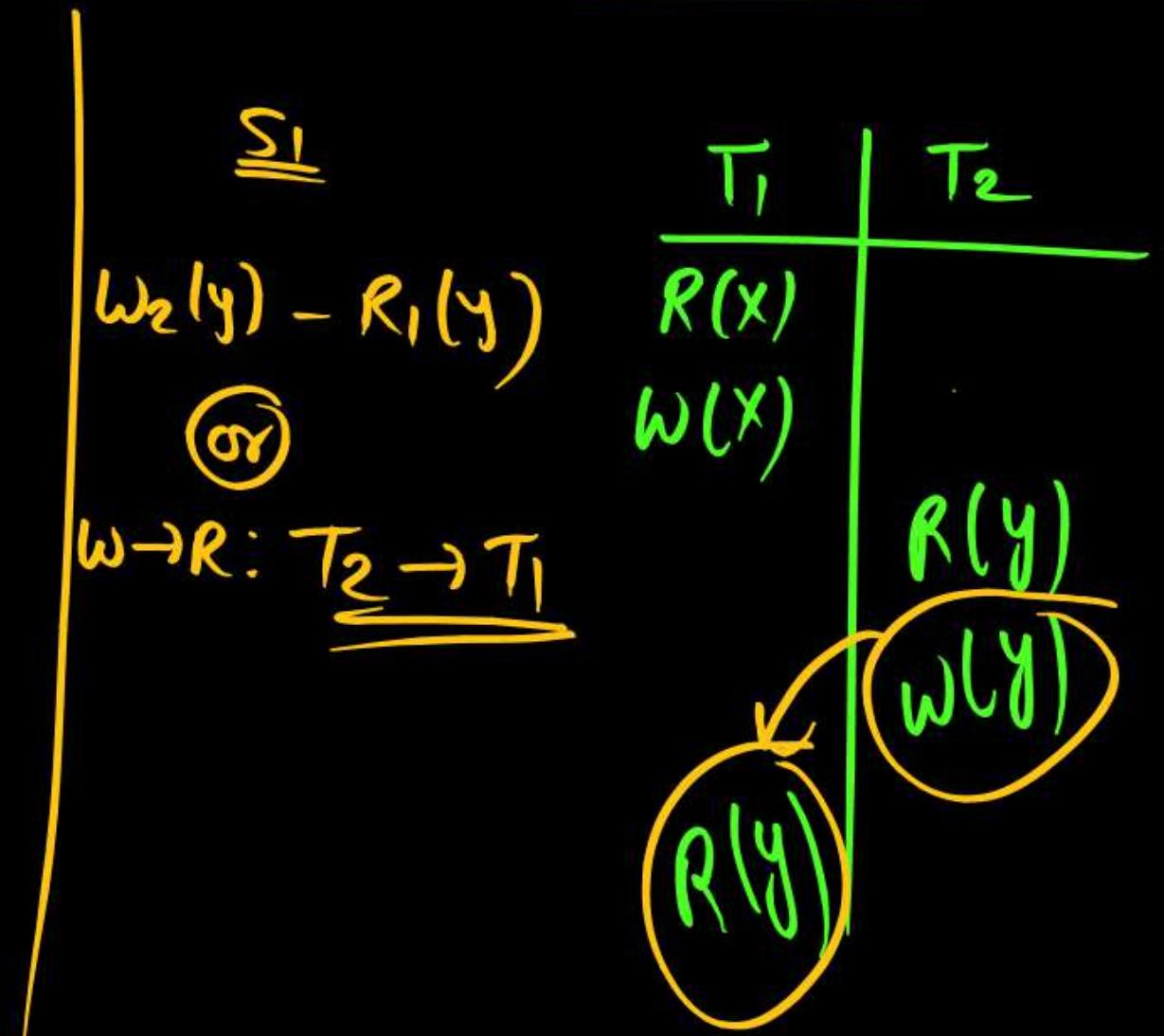
$S_2: R_1(x) W_1(x) R_1(y) R_2(y) W_2(y)$

$\cancel{S_1 \text{ Not C. eq}}$

	T_1	T_2
$R(x)$		
$w(x)$		
$R(y)$		

$R_1(y) - W_2(y)$

\circlearrowleft
 $R-W: \overline{T_1} \rightarrow T_2$

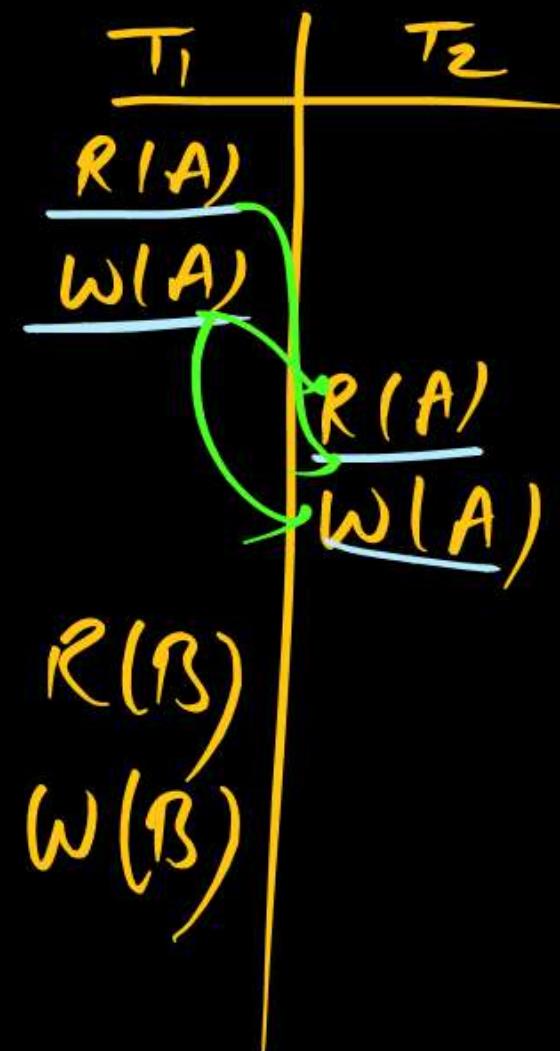


Q.

$$S_1: \underline{R_1(A)} W_1(A) R_2(A) W_2(A) R_1(B) W_1(B)$$

$$S_2: R_1(A) W_1(A) R_2(A) R_1(B) W_2(A) W_1(B)$$

(S)



$$\begin{aligned} & R_1(A) - W_2(A) \\ & W_1(A) - R_2(A) \\ & W_1(A) - W_2(A) \end{aligned}$$

$$\begin{aligned} & R(A) - W(A) : T_1 \rightarrow T_2 \\ & W(A) - R(A) : T_1 \rightarrow T_2 \\ & W(A) - W(A) : T_1 \rightarrow T_2 \end{aligned}$$

S₁



$$\begin{aligned} & R_1(A) - W_2(A) \\ & W_1(A) - R_2(A) \\ & W_1(A) - W_2(A) \end{aligned}$$

$T_1 \rightarrow T_2$

P
W

Q.

Consider a schedule of transactions T_1 and T_2 :

T_1	RA			RC	WD	WB	(B)	Commit	
T_2		RB	WB		RD		WC		Commit

curve nor

Here, RX stands for “Read(X)” and WX stands for “Write(X)”. Which one of the following schedules is conflict equivalent to the above schedule?

[2020: 2 Marks]

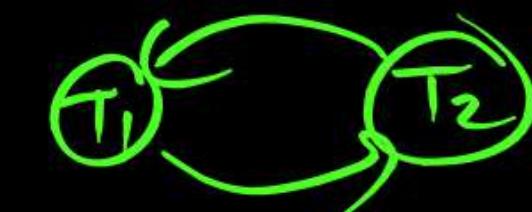
A

T_1				RA	RC	WD	WB	Commit	
T_2	RB	WB	RD	WC					Commit



B

T_1			RA	RC	WD	WB	Commit		
T_2	RB	WB	RD				WC		Commit



C

T_1	RA	RC	WD	WB				Commit	
T_2					RB	WB	RD	WC	Commit



D

T_1	RA	RC	WD	WB				Commit	
T_2					RB	WB	RD	WC	Commit

Q.

Consider a schedule of transactions T_1 and T_2 :

T_1	RA			RC	WD	WB	Commit	
T_2		RB	WB	RD		WC		Commit

 $R_2(B) - W_1(B)$ $W_2(B) - W_1(B)$ $R_1(C) - W_2(C)$ $R_2(D) - W_1(D)$

T_1				RA	RC	WD	WB	Commit	
T_2	RB	WB	RD	WC				Commit	

T_1			RA	RC	WD	WB	Commit		
T_2	RB	WB	RD			WC		Commit	

T_1	RA	RC	WD	WB			Commit		
T_2				RB	WB	RD	WC		Commit

T_1	RA	RC	WD	WB			Commit		
T_2				RB	WB	RD	WC		Commit

[2020: 2 Marks]

 $R_2(B) - W_1(B)$ $W_2(B) - W_1(B)$ $R_2(D) - W_1(D)$ $R_1(C) - W_2(C)$

Q.

Consider a schedule of transactions T_1 and T_2 :

T_1	RA			RC		WD		WB	(B) Commit	
T_2		RB	WB		RD		WC			Commit

Here, RX stands for “Read(X)” and WX stands for “Write(X)”. Which one of the following schedules is conflict equivalent to the above schedule?

[2020: 2 Marks]

A

T_1					RA	RC	WD	WB	Commit	
T_2	RB	WB	RD	WC						Commit

B

T_1				RA	RC	WD	WB		Commit	
T_2	RB	WB	RD					WC		Commit

C

T_1	RA	RC	WD	WB					Commit	
T_2					RB	WB	RD	WC		Commit

D

T_1	RA	RC	WD	WB					Commit	
T_2					RB	WB	RD	WC		Commit

Conflict Serializable

A schedule is said to be conflict serializable if it is conflict equivalent to a serial schedule.

Same conflicting operation order in $C_1 \& S_1$

\therefore Its $\{C_1\}$ conflict is $R_1(B) - W_2(B)$
 conflict serializable.
 $W_1(B) - R_2(B)$
 $W_1(B) - W_2(B)$

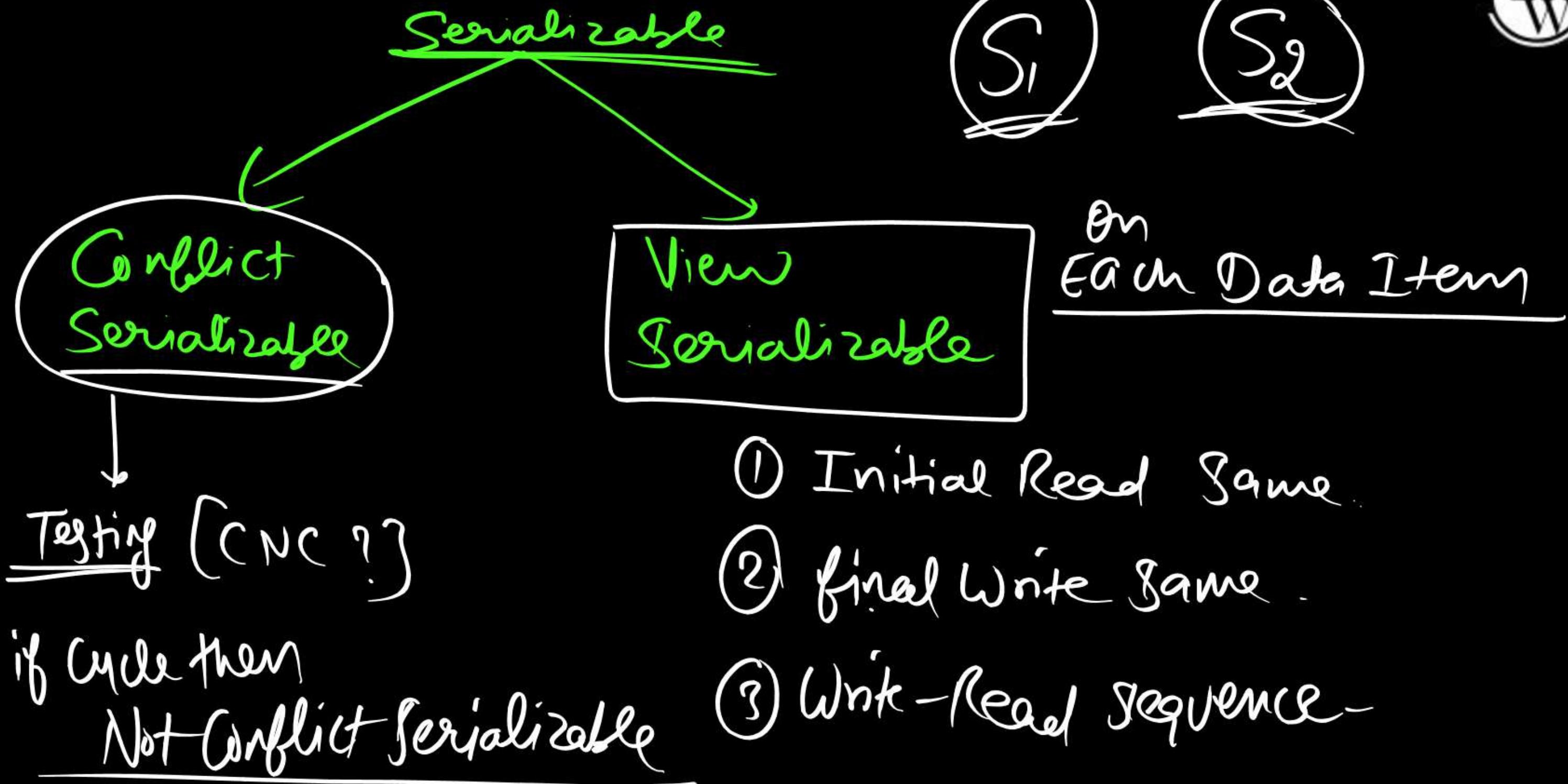
$R_1(A) - W_2(A)$
 $W_1(A) - R_2(A)$
 $W_1(A) - W_2(A)$

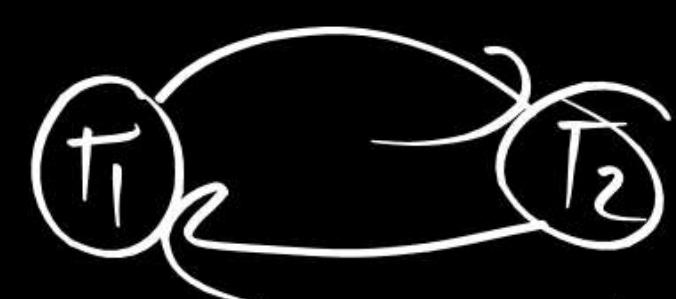
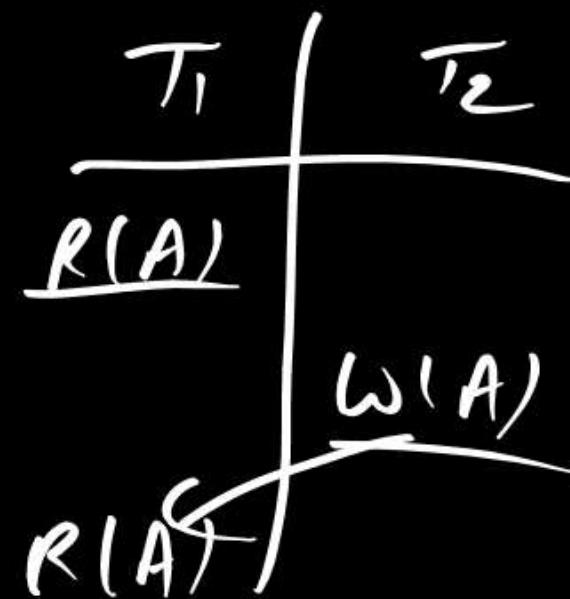
T_1	T_2
read(A)	write(A)
read(B)	write(A)
read(B)	write(B)

C_L

T_1	T_2
read(A)	write(A)
read(A)	write(A)
read(B)	write(B)
read(B)	write(B)

S_L



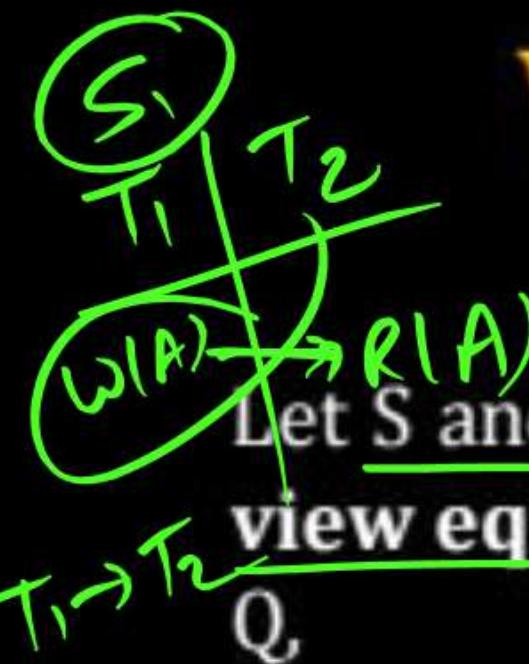


Will Not Conflict

- ① Initial Read
- ② Final Write
- ③ Write - Read

View Serializability

P
W



Let S and S' be two schedules with the same set of transactions. S and S' are view equivalent if the following three conditions are met, for each data item Q.

1. If in schedule S, transaction T_i reads the initial value of Q, then in schedule S' also transaction T_i must read the initial value of Q.
2. If in schedule S transaction T_i executes read(Q), and that value was produced by transaction T_j (if any), then in schedule S' also transaction T_i must read the value of Q that was produced by the same write(Q) operation of transaction T_j.
3. The transaction (if any) that performs the final write(Q) operation in schedule S must also perform the final write(Q) operation in schedule S'.

S_1

\leq

VIEW

S_2

S'

P
W

① Initial Read

② final Write

③ Update Read [Write-Read Sequence]

View Serializability

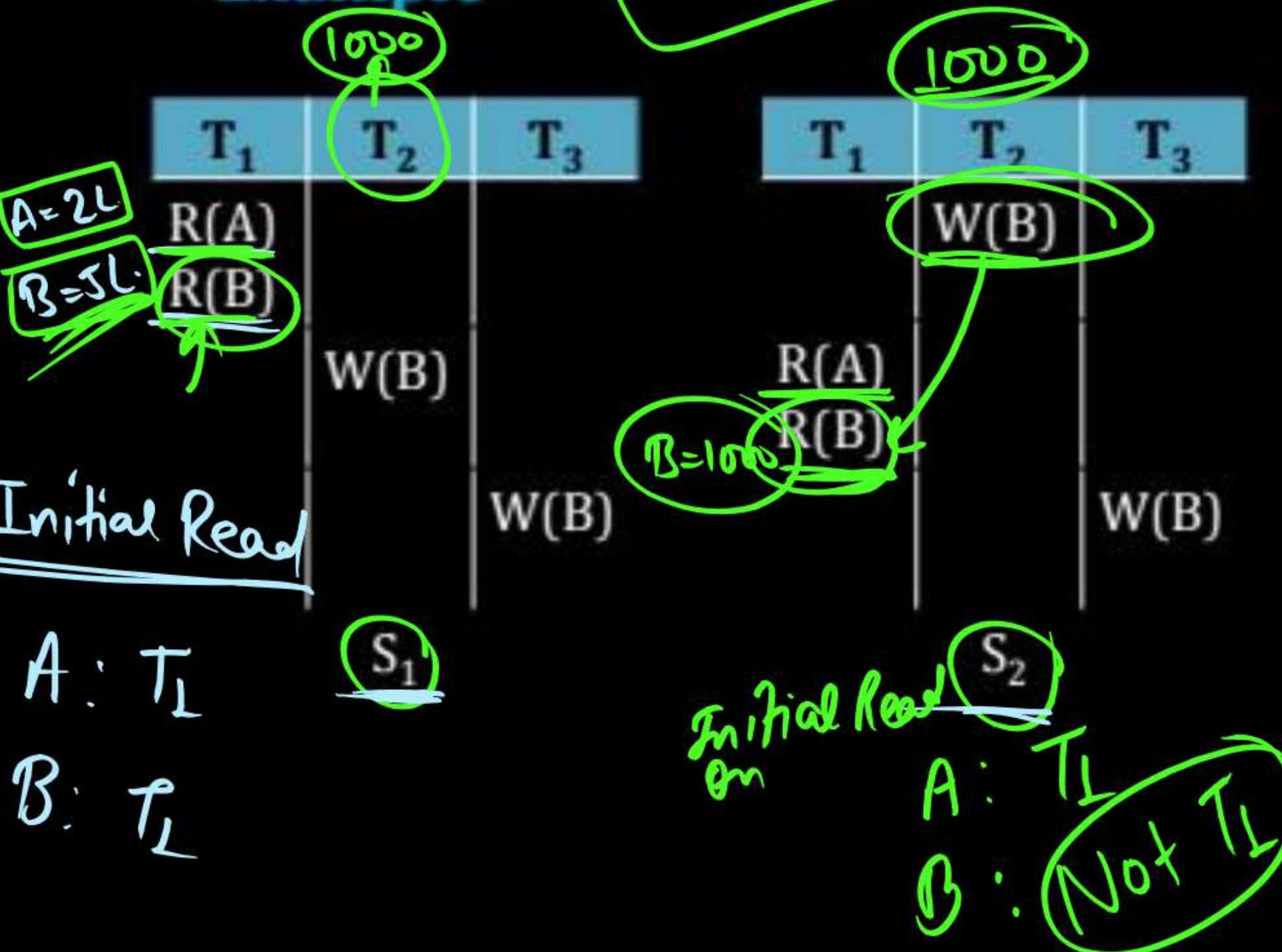
- View Serializable Schedule: View equivalent serial schedule.

- View Equivalent: S_1 and S_2 said to be view equivalent.

Only if

- (1) initial reads of S_1 and S_2 should be same.

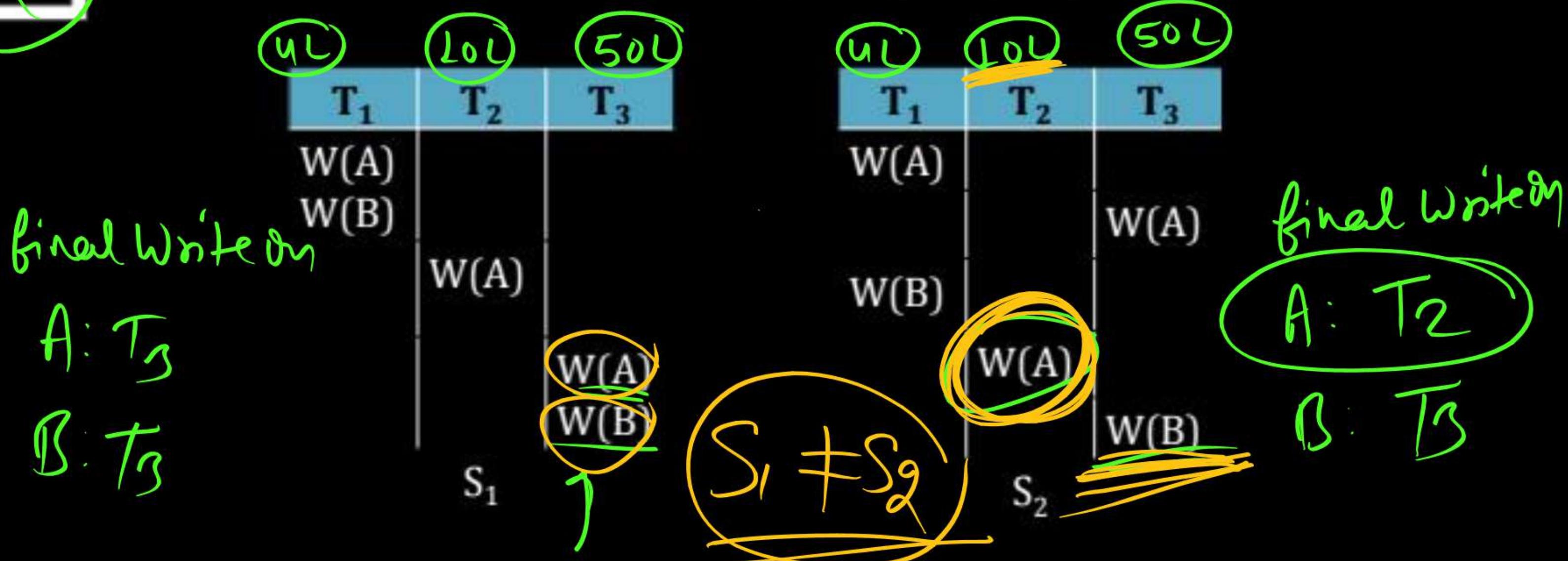
A & B
Example



View Serializability



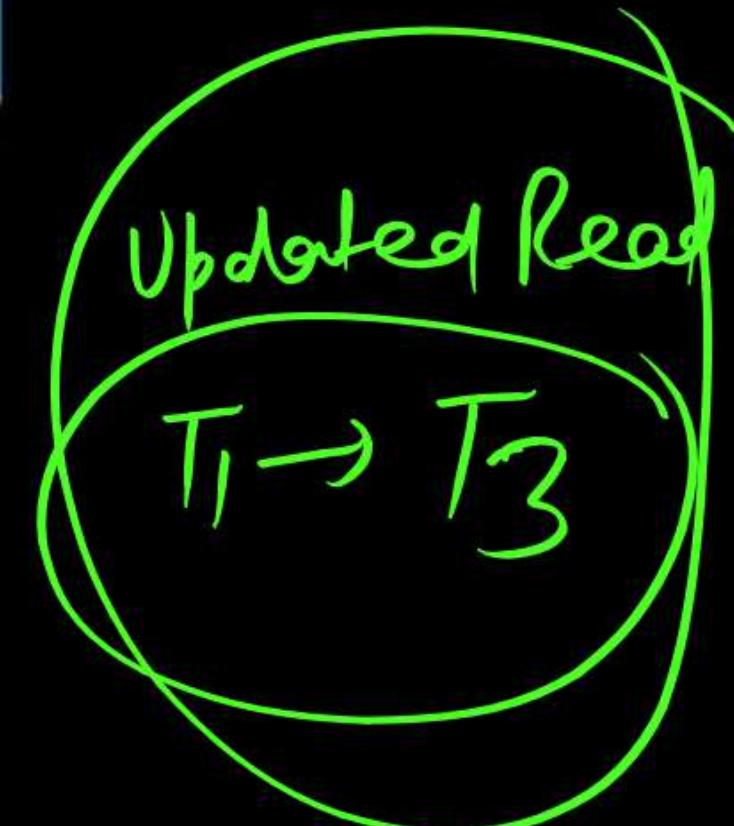
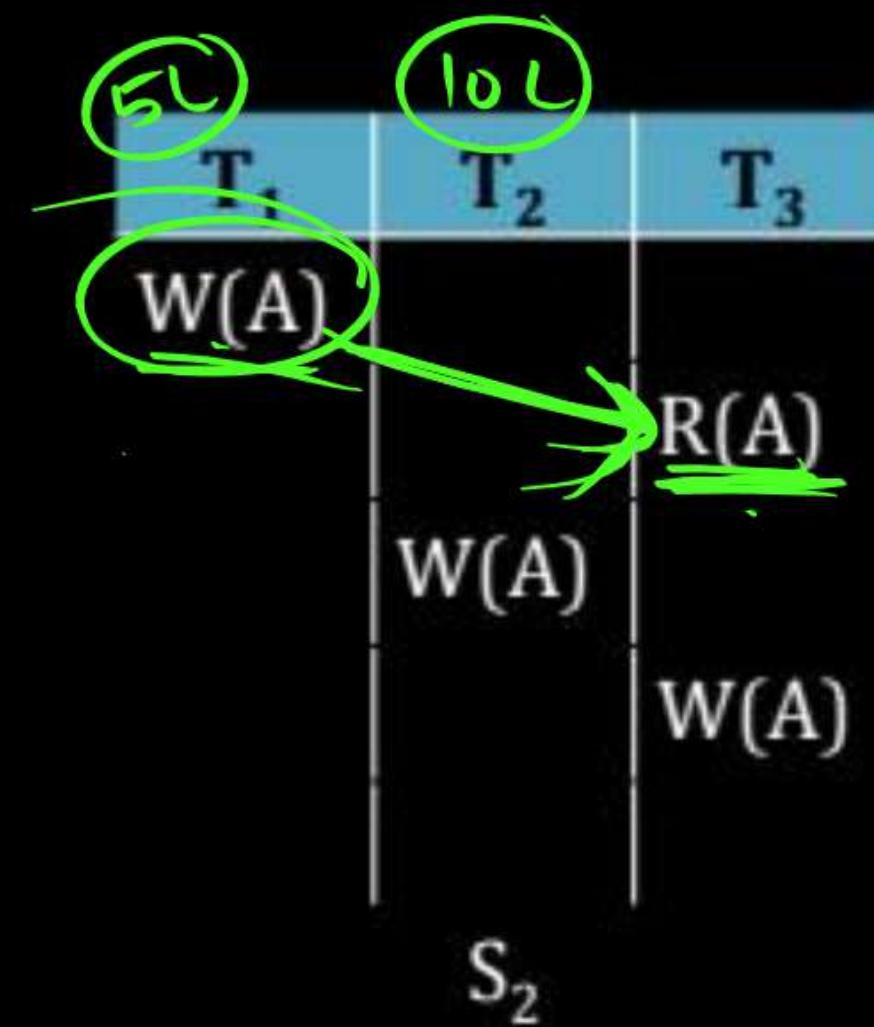
Final updations for every data item should be same in S_1 and S_2



View Serializability

3.

Write-Read sequence should also be equal. (Updated Reads should be same)



View Serializability (Cont.)

- A schedule S is **view serializable** if it is view equivalent to a serial schedule.
- Every conflict serializable schedule is also view serializable.
- Below is a schedule which is view-serializable but not conflict serializable.

T_{27}	T_{28}	T_{29}
read(A)		
	write(Q)	
	write(Q)	write(Q)

Note:

Every view serializable schedule that is not conflict serializable has blind writes.

Conflict Serializable

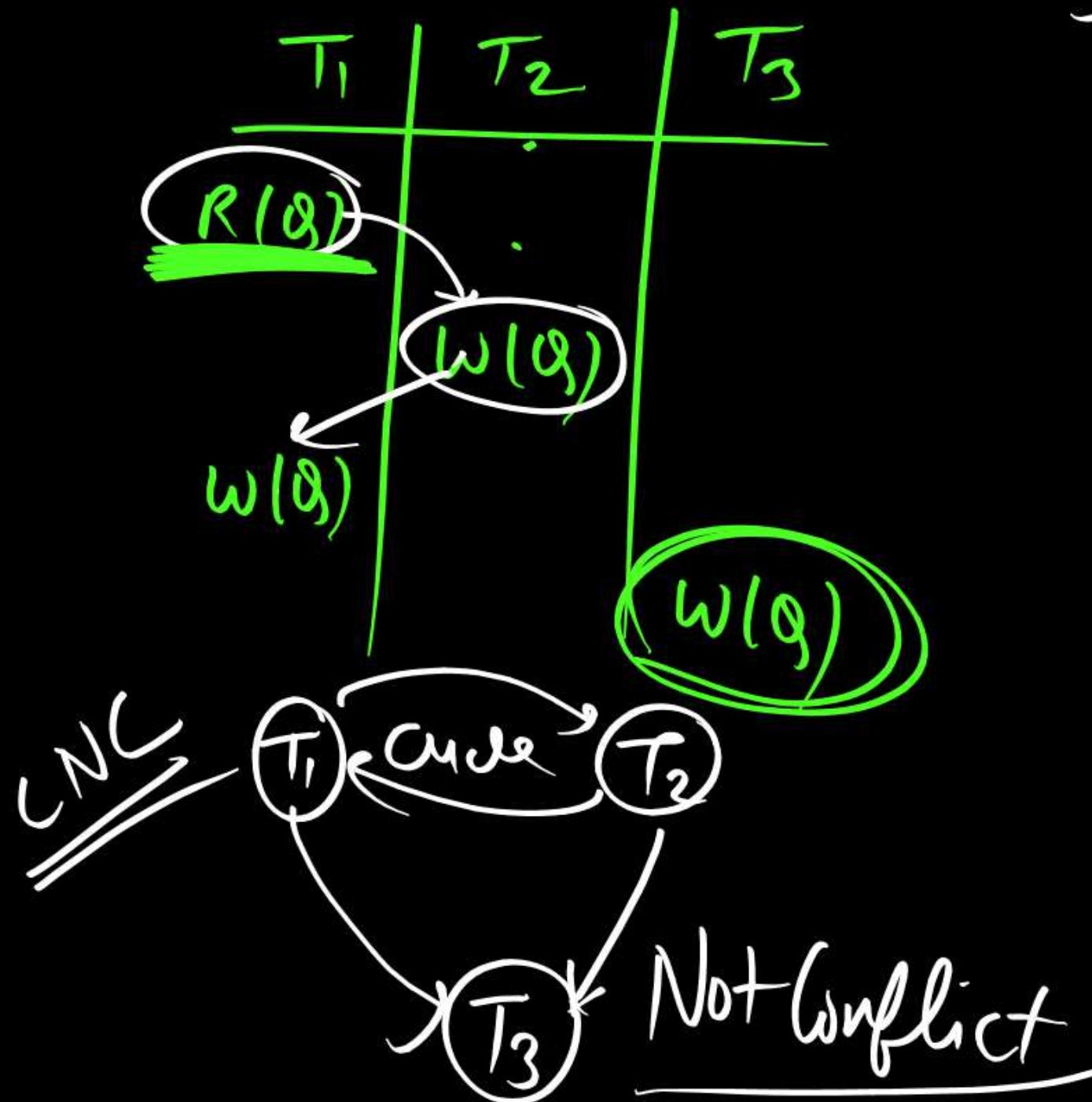
~~Testing~~ \Rightarrow Precedence Graph



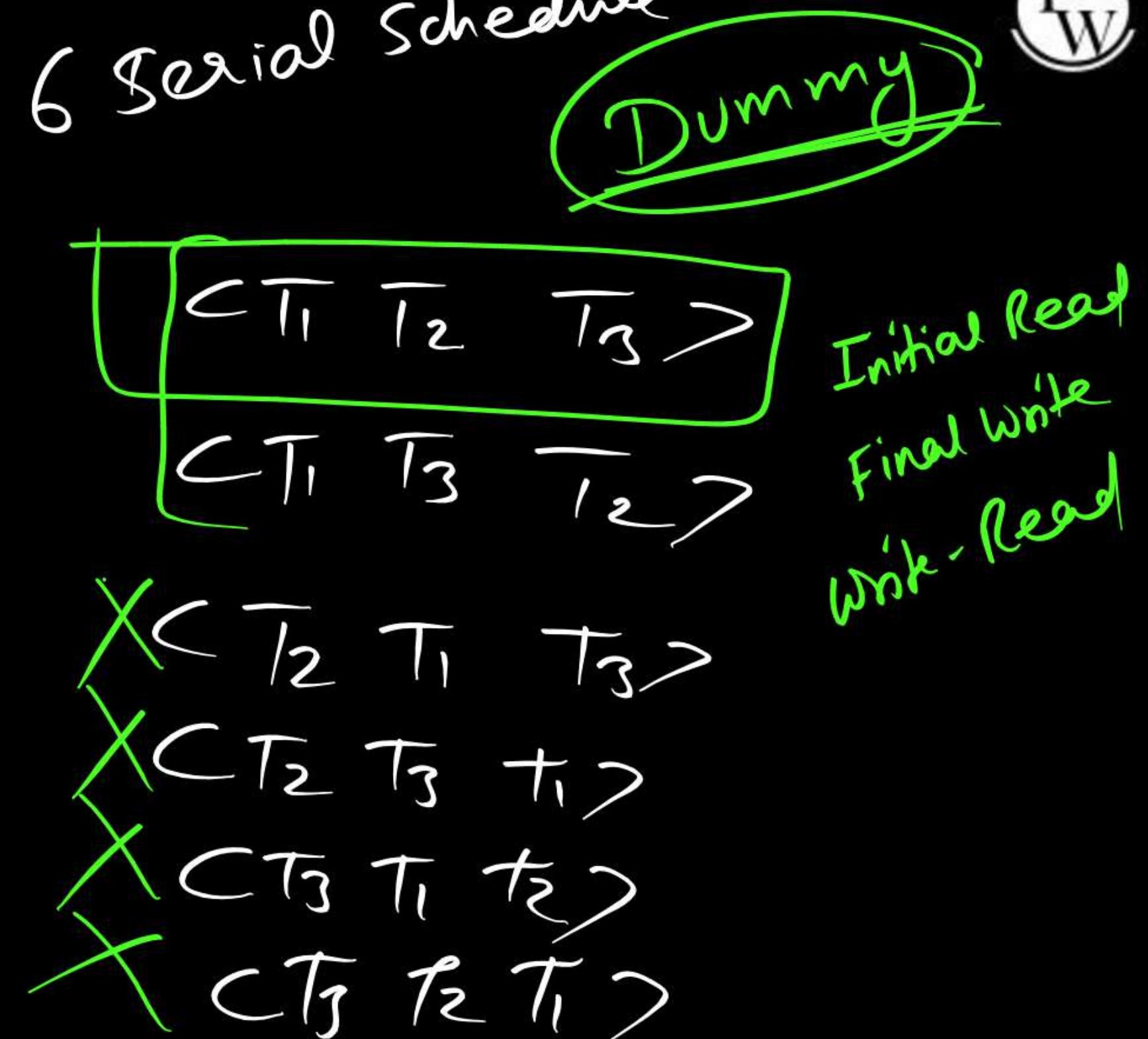
CNC

If Conflict \rightarrow then Definitely its View
S.

P
W

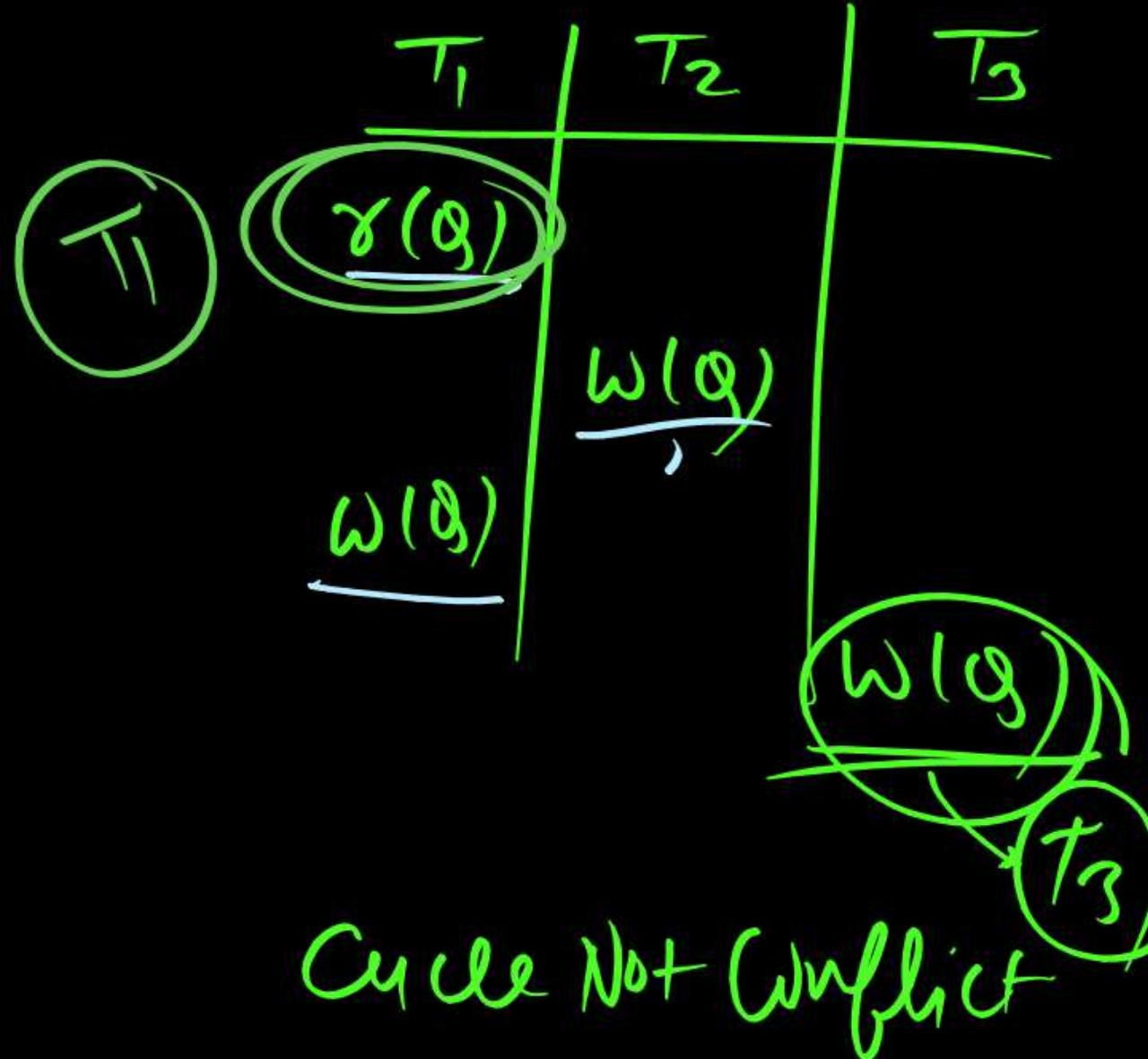


$3! \Rightarrow 6$ Serial Schedule

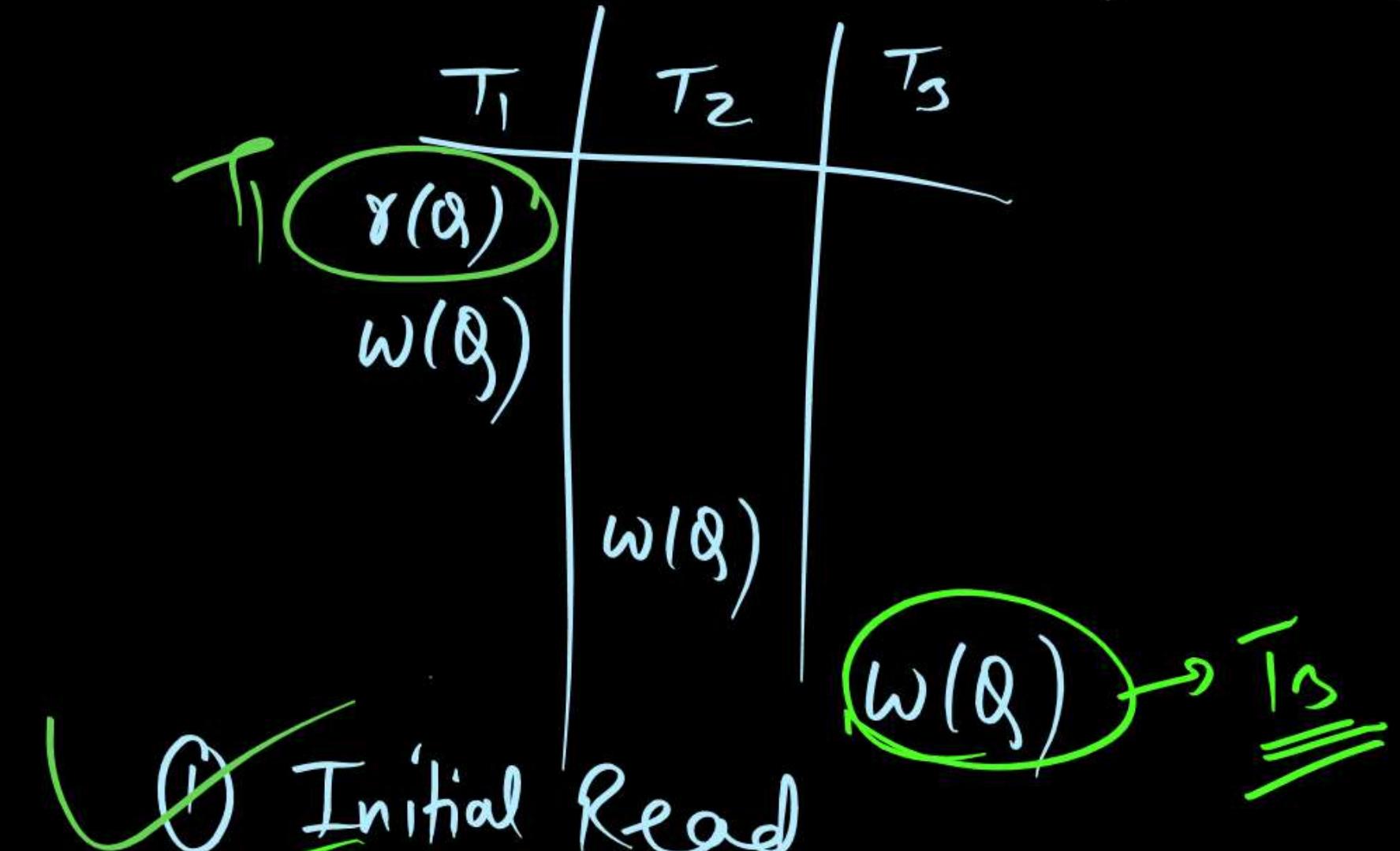


P
W

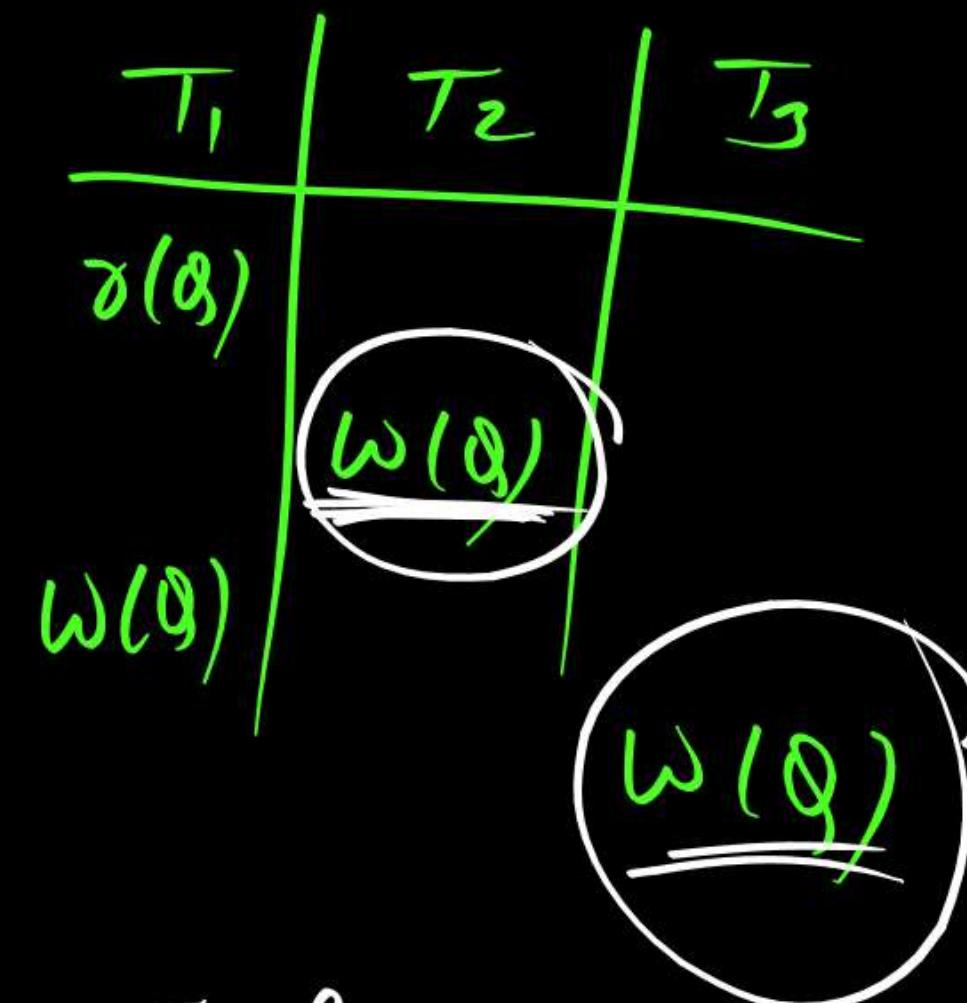
S'



S(T_1 , T_2 , T_3)



~~Initial Read~~
~~Final Write~~
Write-Read [Updated Read]



Blind Write
↳ write without reading

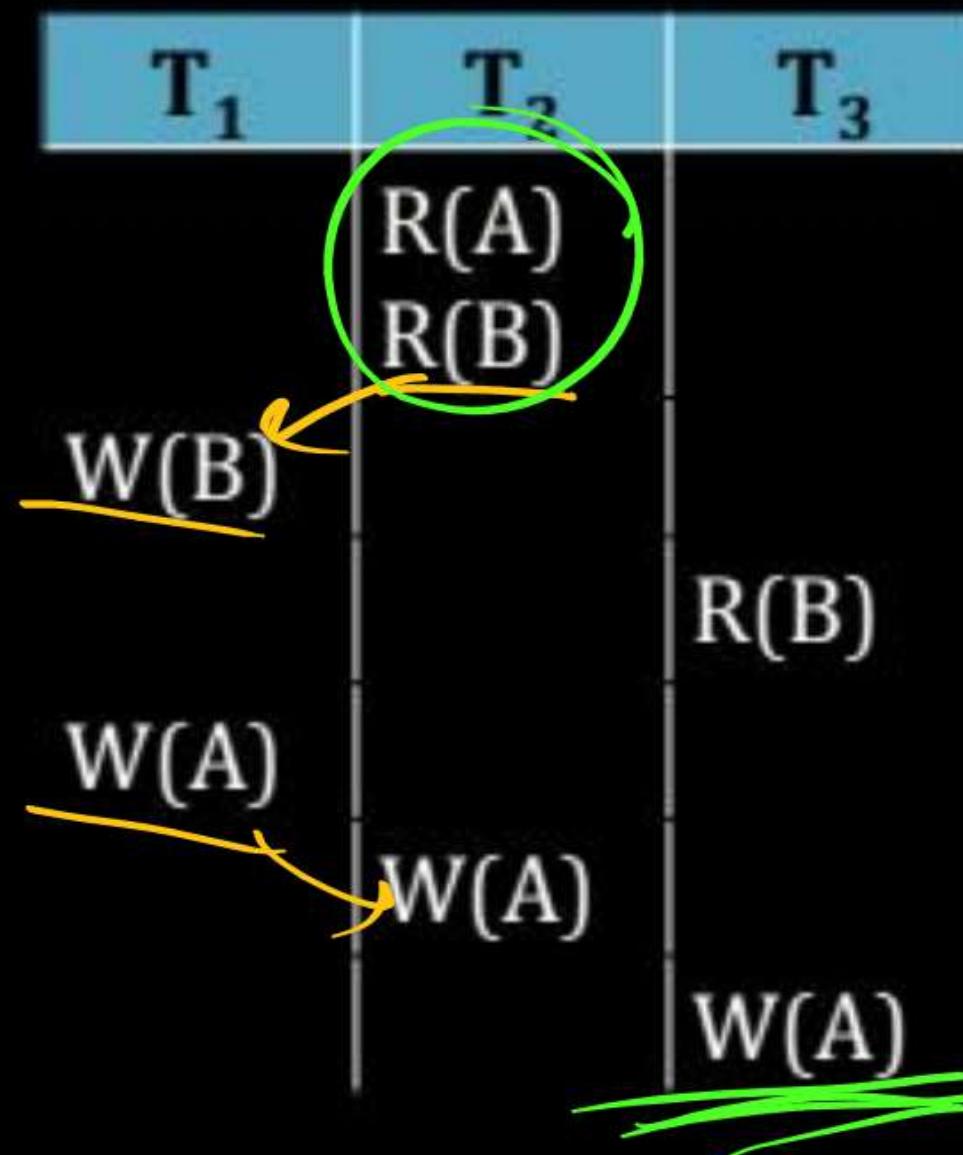
Not Conflict Serializable
But View Serializable
∴ It's Serializable Schedule

T₂ & T₃: Blind Write

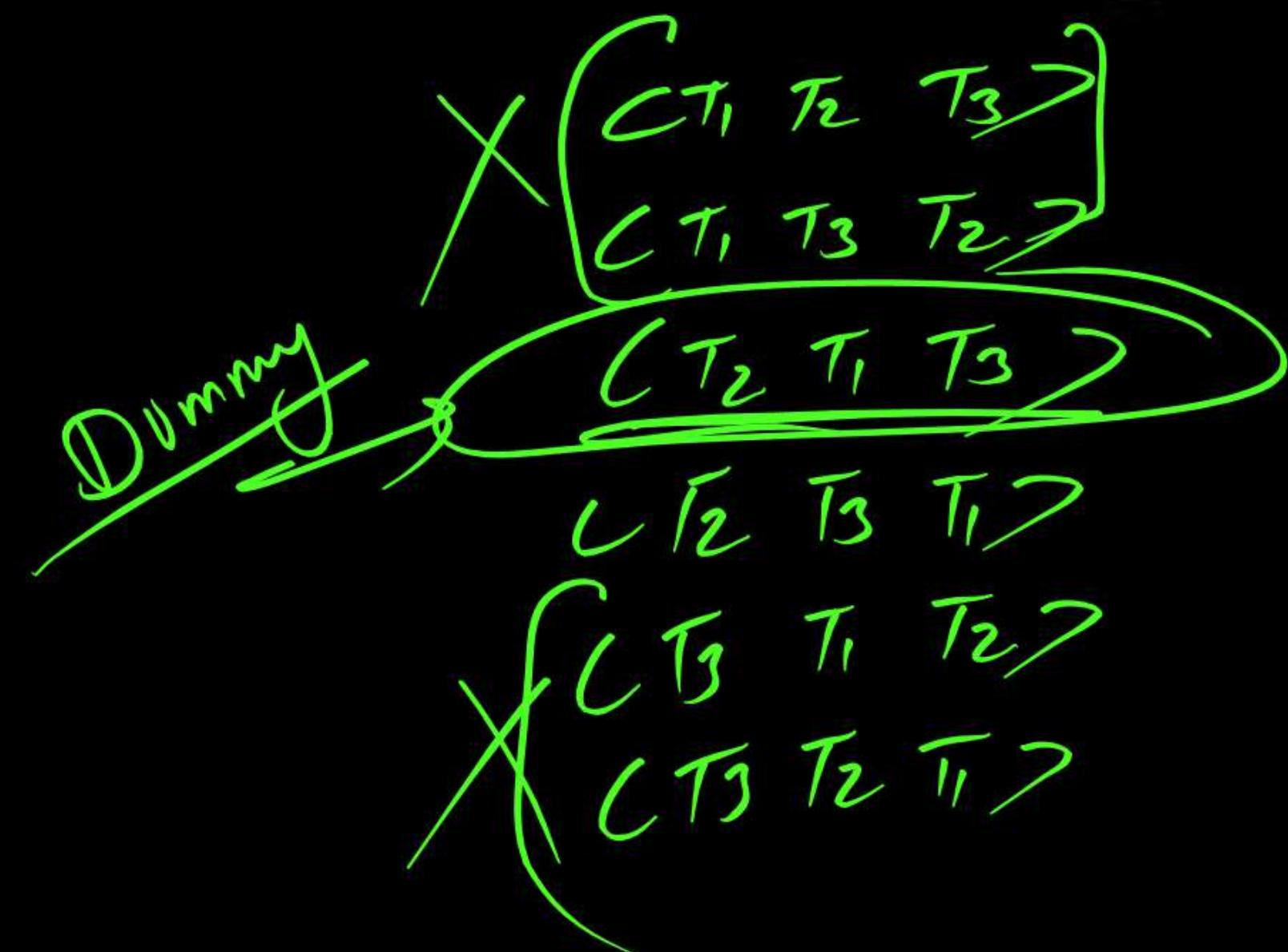
		<u>Blind write</u>		
Conflict	<u>YES</u>	<u>NO</u>	<u>NO</u>	<u>YES</u>
View	<u>No Need to check, already View</u>	<u>YES</u>	<u>NO</u>	<u>NO</u>
	<u>Conflict Serializable</u>	<u>View Serializable</u> or <u>Serializable</u>	<u>Not Serializable</u>	
	<u>View Serializable</u>			

Q.

P
W



T_2
cycle
not
conflict



Q.

P
W

Not Conflict
But View Segi
Serializable

T_1	T_2	T_3
-------	-------	-------

① Initial Read

A: T_2

B: T_2



② Final Write

A: T_3

B: T_1



③ Update Read
 $T_1 \rightarrow T_3$

(T_2, T_1, T_3)		
T_1	T_2	T_3
$R(A)$		
$R(B)$		

(T_2, T_1, T_3)		
T_1	T_2	T_3
$W(B)$		
$W(A)$		

④ Updated Read
 $T_1 \rightarrow T_3$

① Initial Read

A: T_2

B: T_2

② Final Write

A: T_3

B: T_1

Q.

Consider the following schedule S of transactions T_1 and T_2 :

Which of the following is TRUE about the schedule S? [2004: 2 Marks]

P
W

- A
- B
- C
- D

S is serializable only as T_1, T_2

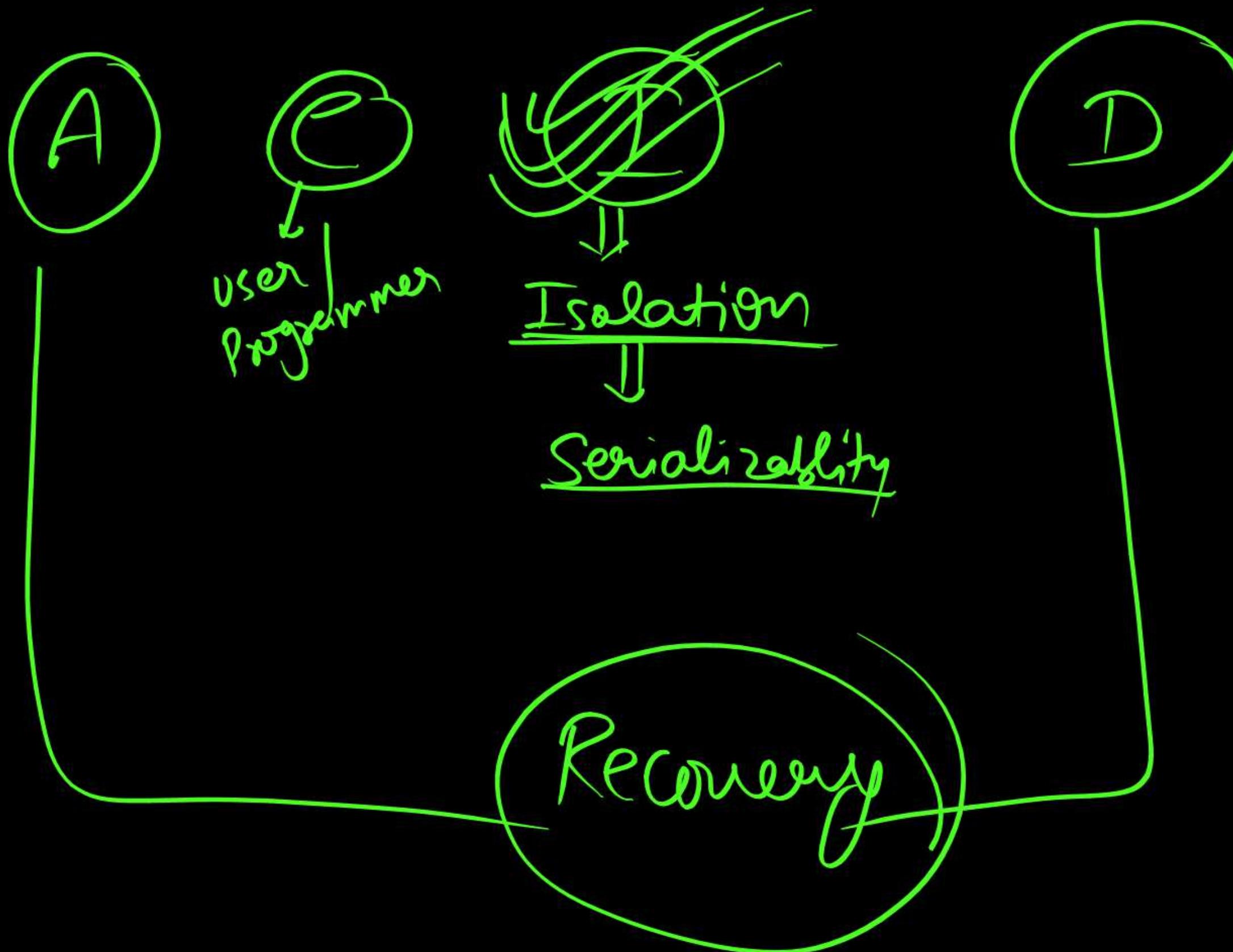
S is serializable only as T_2, T_1

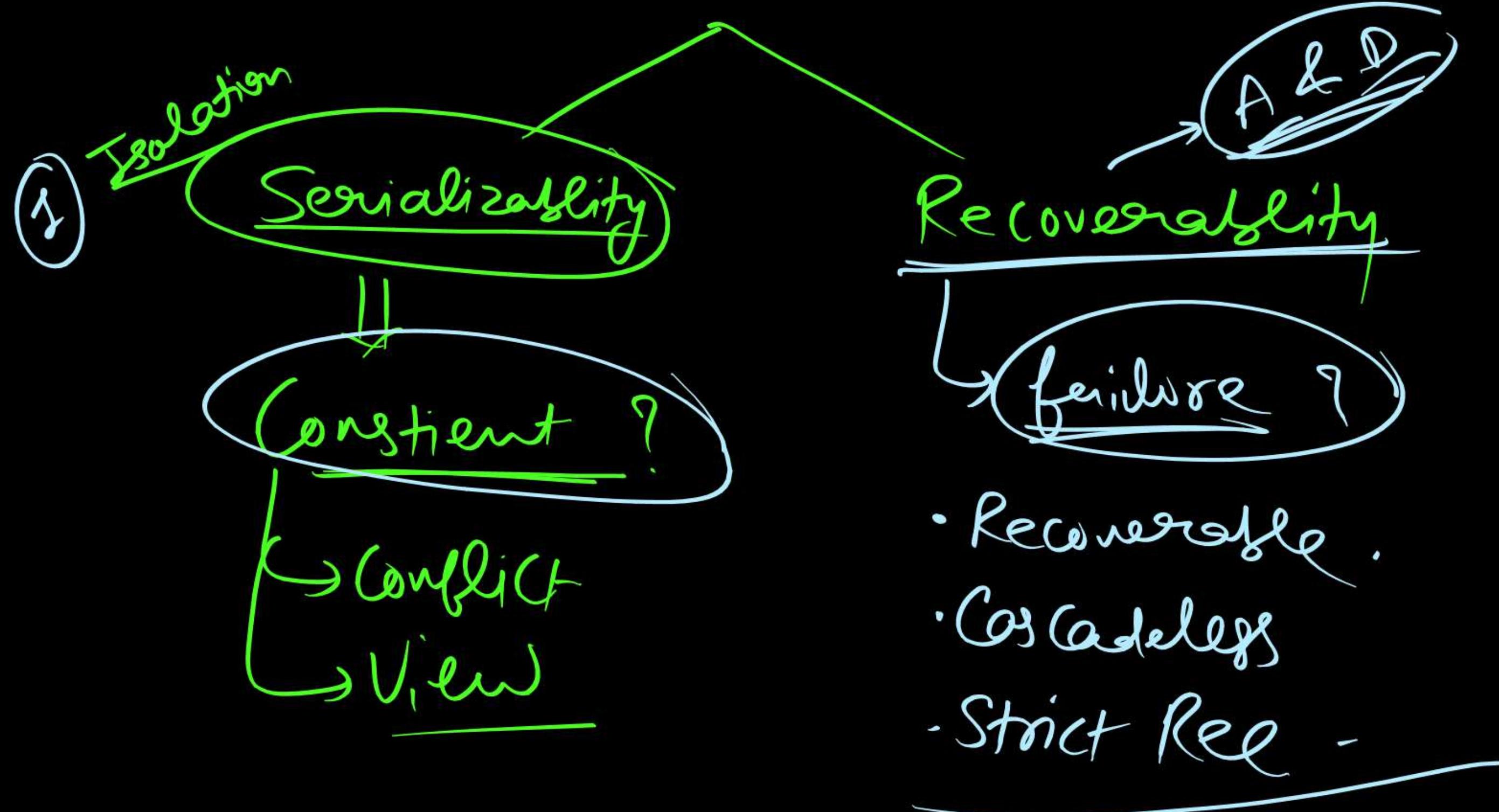
S is serializable both as T_1, T_2 and T_2, T_1

S is not serializable either as T_1 or as T_2

T_1	T_2
Read(A) $A = A - 10$	Read(A) $Temp = 0.2 * A$ Write(A) Read(B)
Write(A) Read(B) $B = B + 10$ Write(B)	$B = B + Temp$ Write(B)

P
W

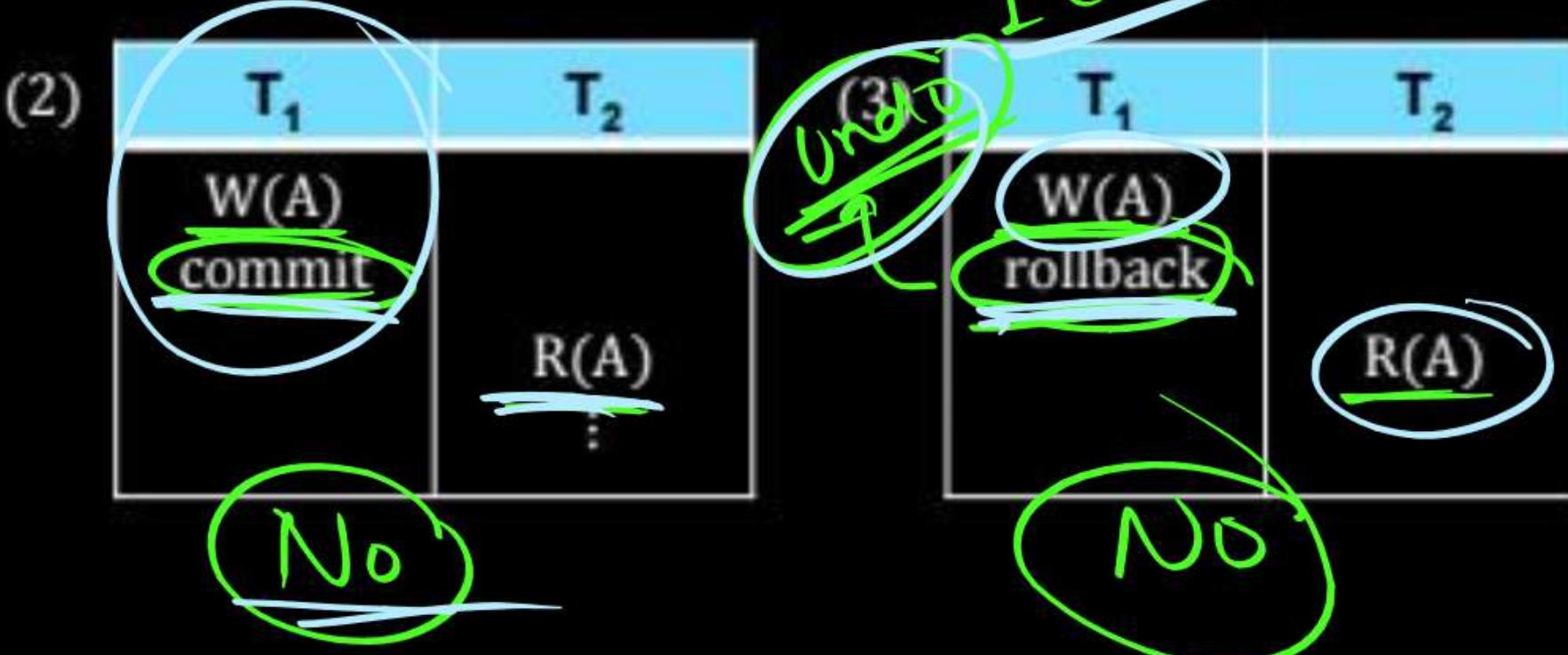




Dependency

T ₁	T ₂
W(A)	R(A)
Commit	

T₂ Depends on T₁



T ₁	T ₂
W(A)	w(A)

No

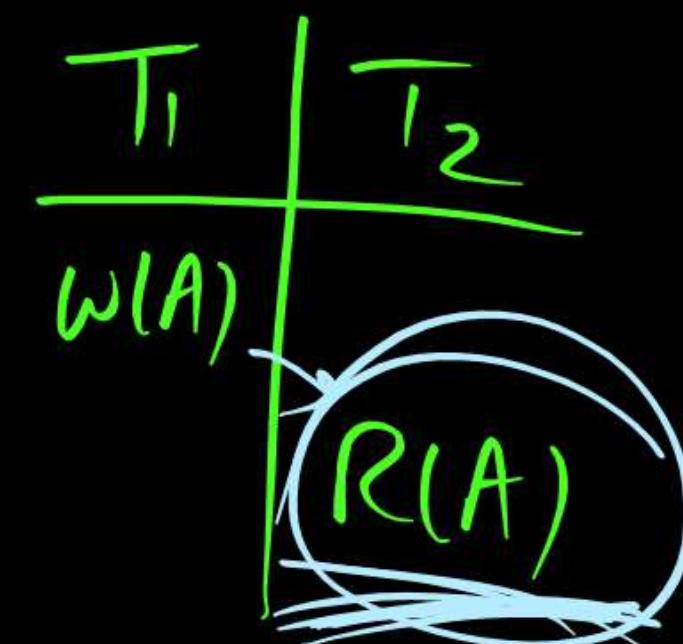
T ₁	T ₂
W(A)	
	W(A) R(A)

No

T ₁	T ₂
W(A)	
R(B)	W(B) R(A)

T₂ Dep T₁
T₁ Dep T₂

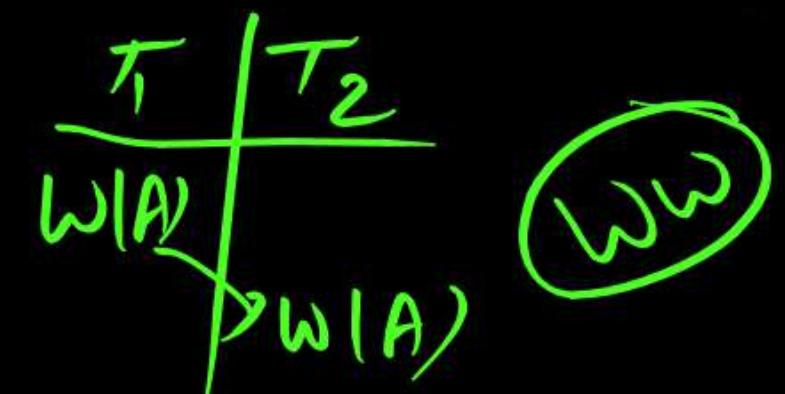
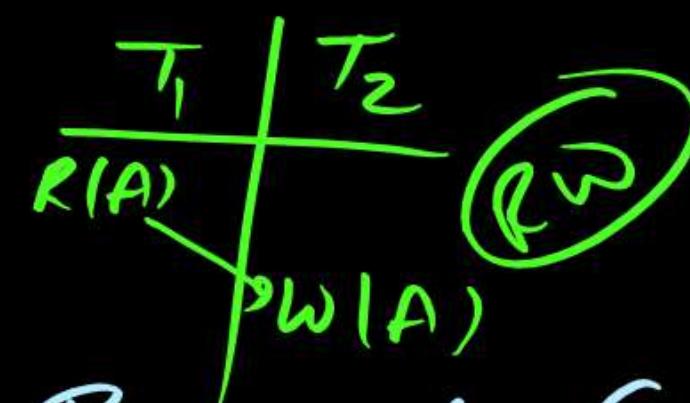
Uncommitted Read | Dirty Read | WR



Modify (Updated) by One Transaction
& Read by another Transaction

P
W

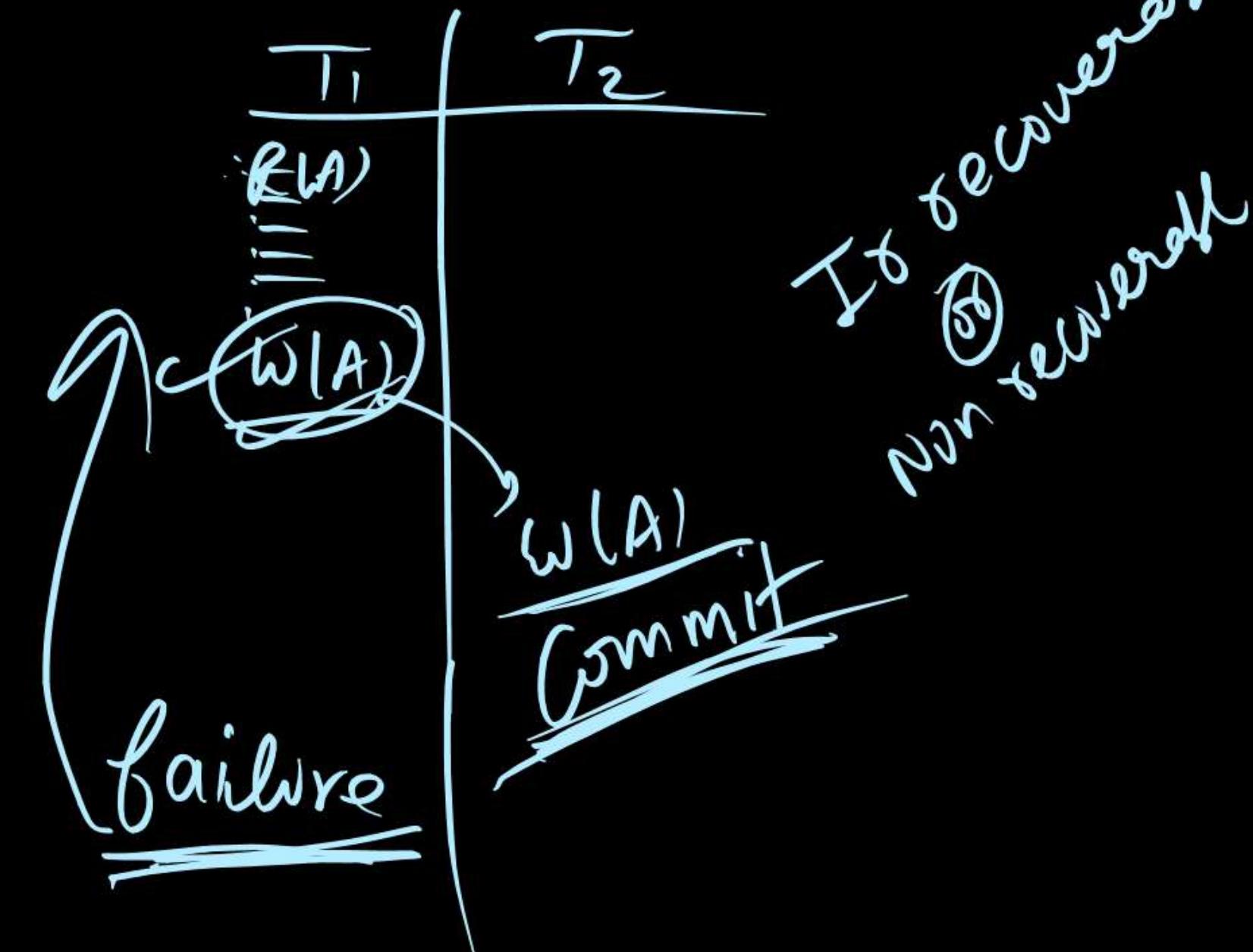
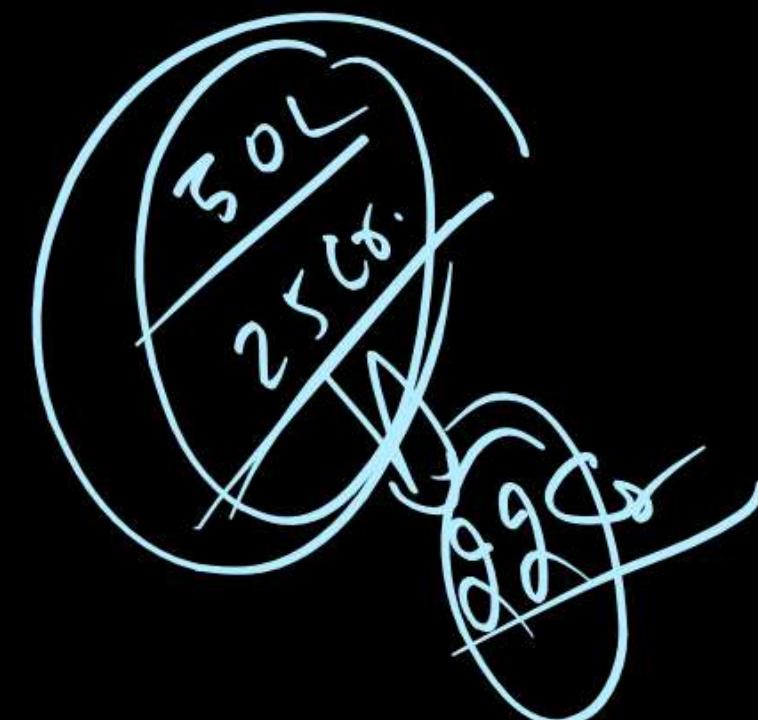
WT



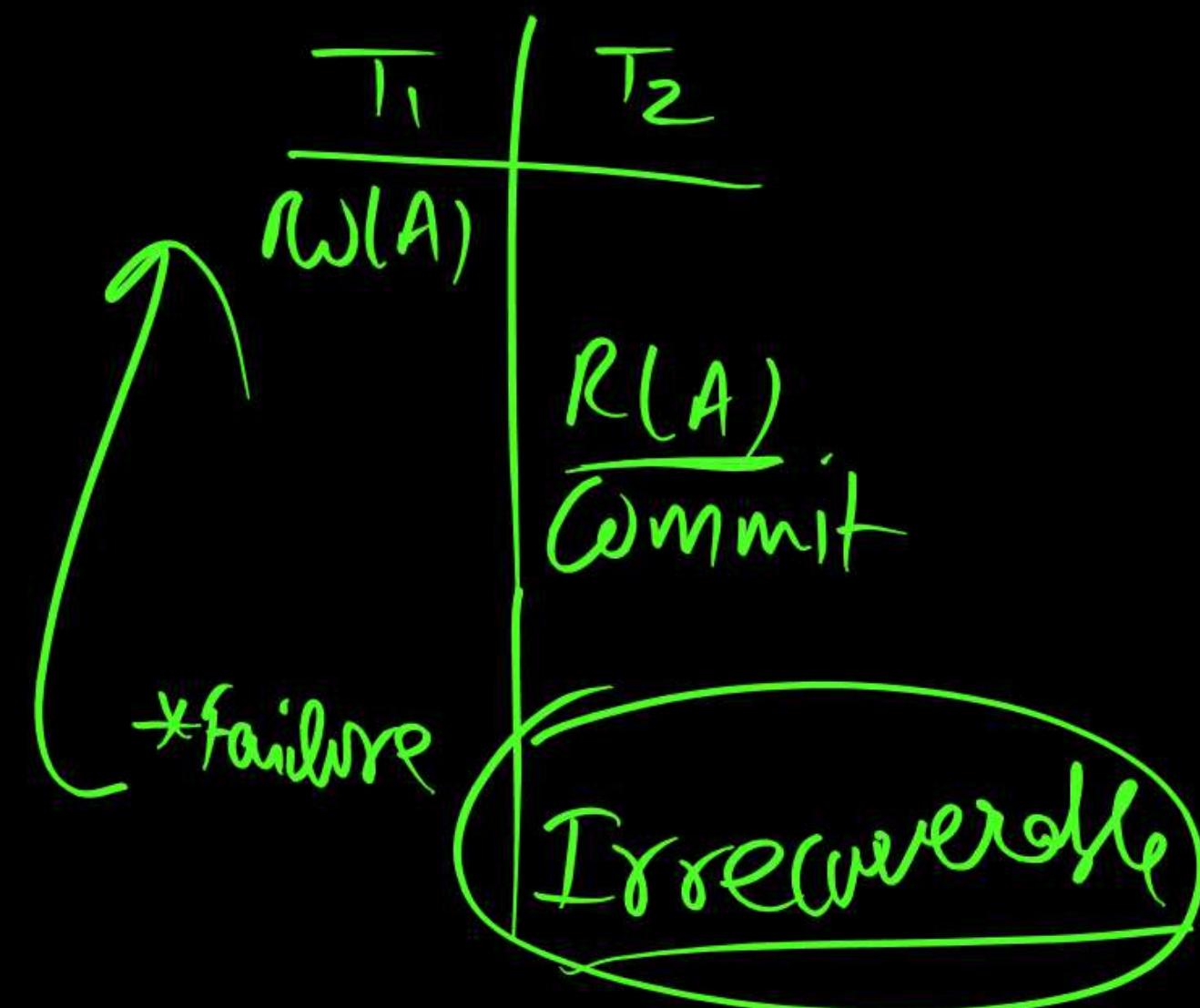
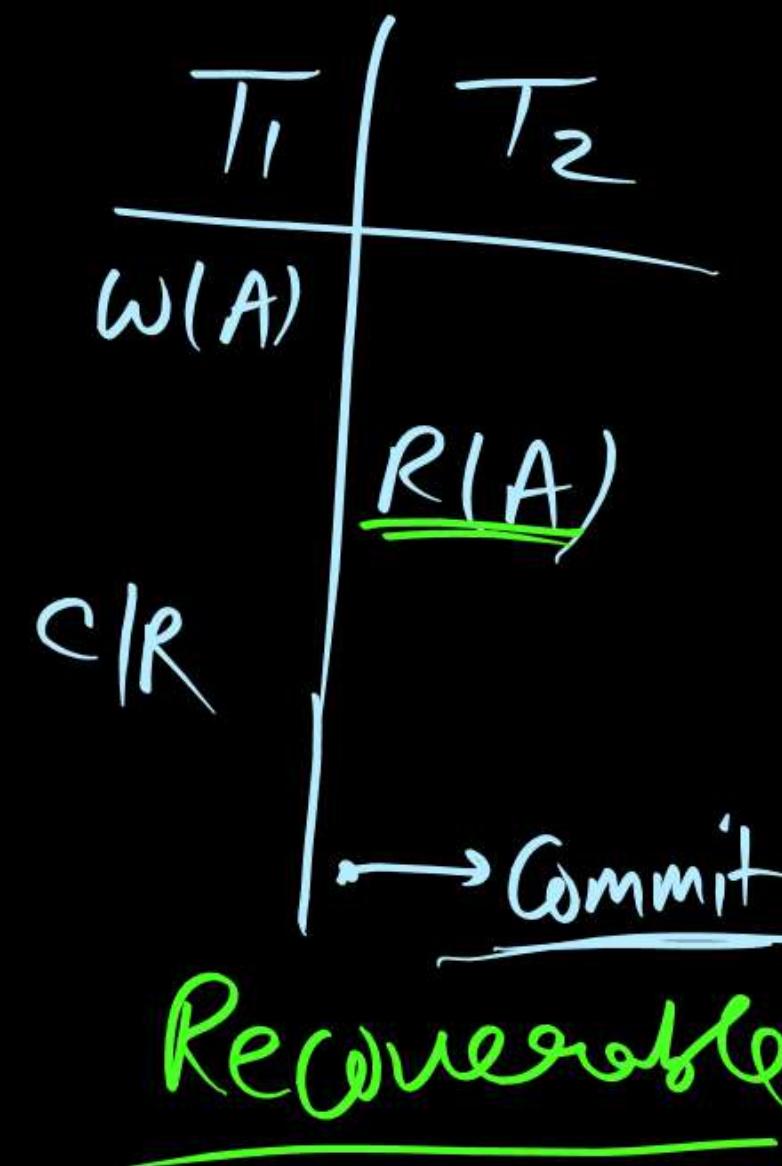
Problem Bcz of Concurrent Execution

- Conflict
- ① WR (Write - Read) / Dirty Read / Uncommitted Read
 - ② RW (Read - Write)
 - ③ WW (Write - Write) / Lost Update Problem
 - ④ Phantom Table Problem

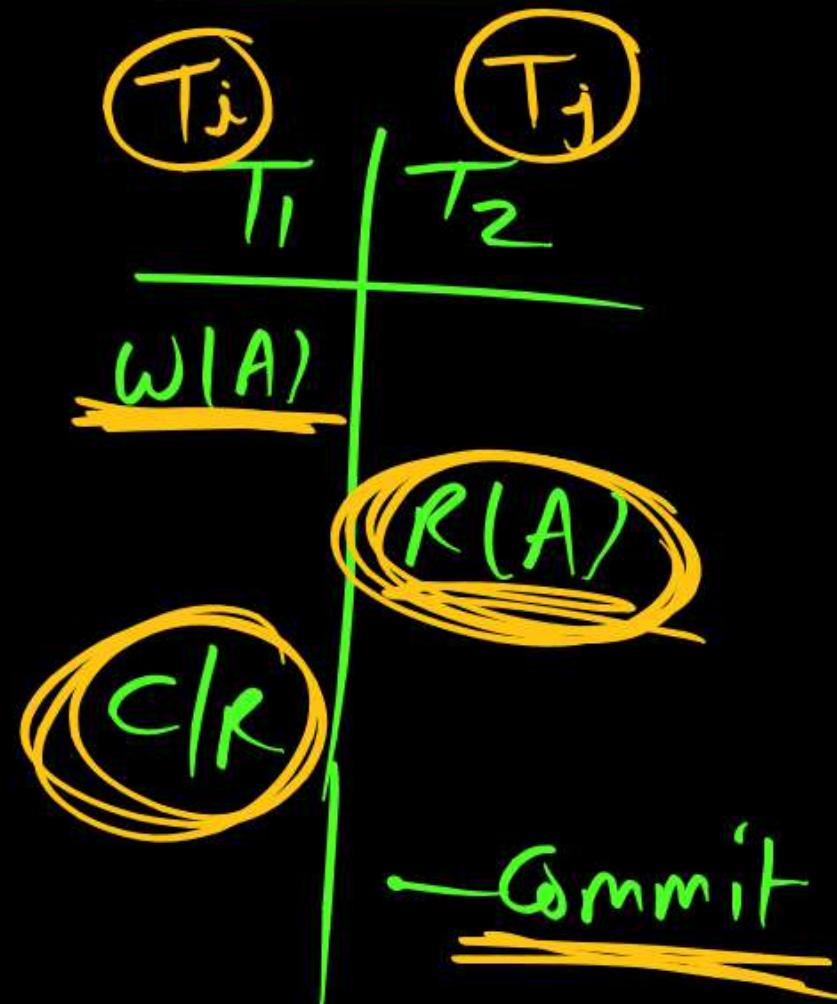
Recoverable Schedule



Recoverable Schedule



Recoverable Schedule



If T_2 depend on T_1 , then
Commit of T_2 must be delayed
Until C/R of T_1 .

Recoverable Schedules

Need to address the effect of transaction failures on concurrently running transactions.

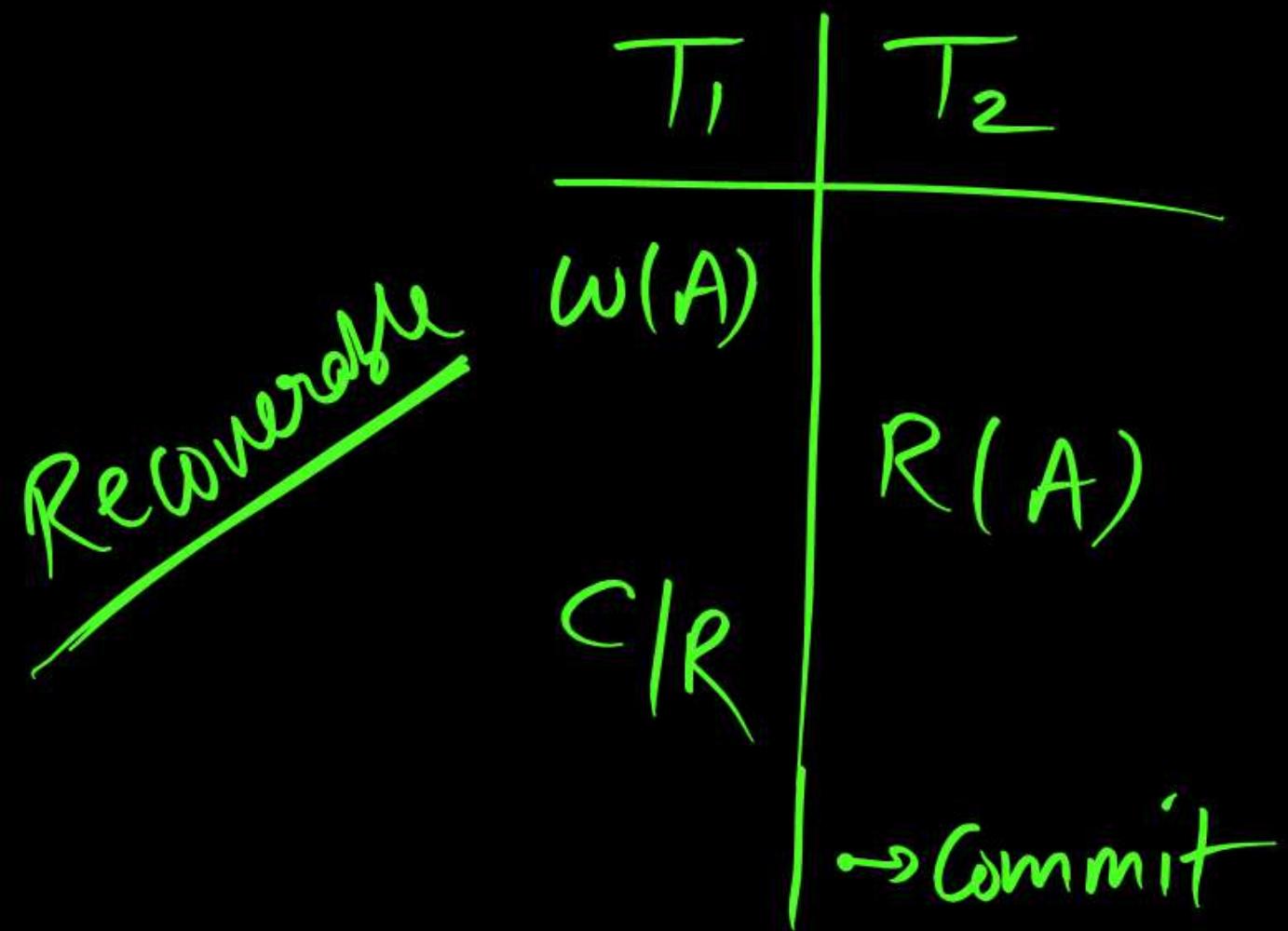
- Recoverable schedule — if a transaction T_j reads a data item previously written by a transaction T_i , then the commit operation of T_i appears before the commit operation of T_j .
- The following schedule is not recoverable

Irrecoverable

T_8	T_9
read(A)	
write(A)	Read(A) commit
read(B)	



- If T_8 should abort, T_9 would have read (and possibly shown to the user) an inconsistent database state. Hence, database must ensure that schedules are recoverable.



Examples

(1)	T ₁	T ₂
	w(A)	R ₁ (A) C ₂ (commit)

X

Rollback

Irrecoverable

① & ②

(3)	T ₁	T ₂
	w(A)	C R R(A)

yes

Rec

(5)	T ₁	T ₂
	w(A)	R A rollback

C|R

Rel ✓

(2)	T ₁	T ₂
	w(A)	R(A) C ₂

X

Non Recoverable

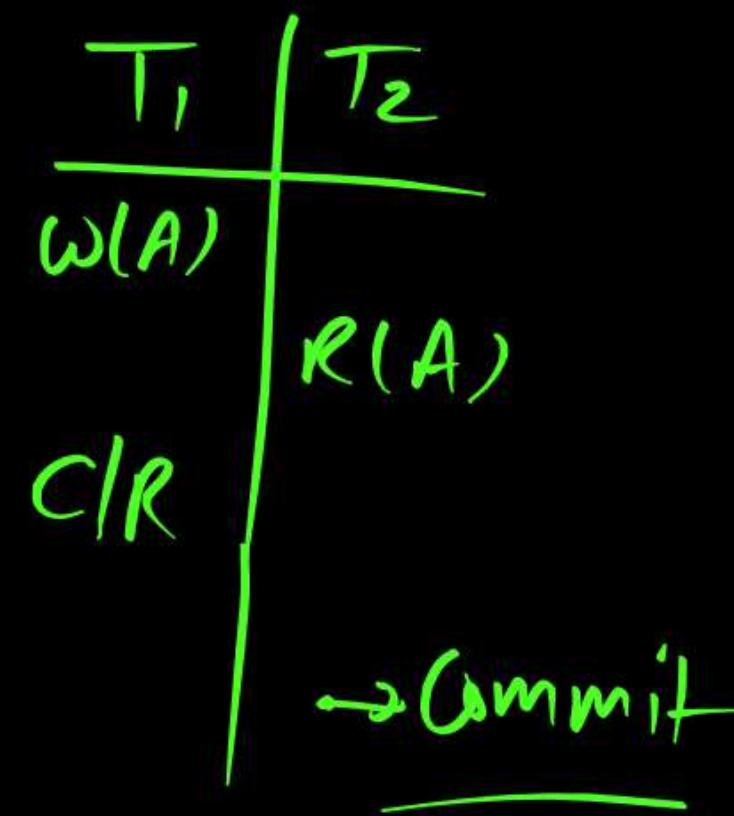
(4)	T ₁	T ₂
	w(A)	w(A) R(A) commit

Commit/
Rollback

(6)	T ₁	T ₂
	w(A)	R(A) C R

Rel

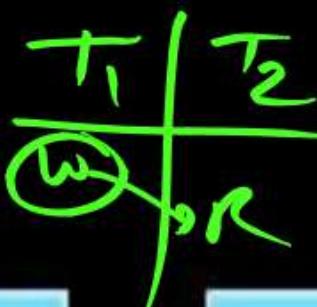
Recoverable Schedule



- ① WR
- ② RW
- ③ WW
- ④ Coordinating Rollback

NOTE: Recoverable schedule may or may not be free from

- WR problem / uncommitted Read
- RW Problem
- WW Problem



T ₁	T ₂
<u>R(A)</u>	<u>W(A)</u> Commit
Commit	

Recoverable
But RW Problem

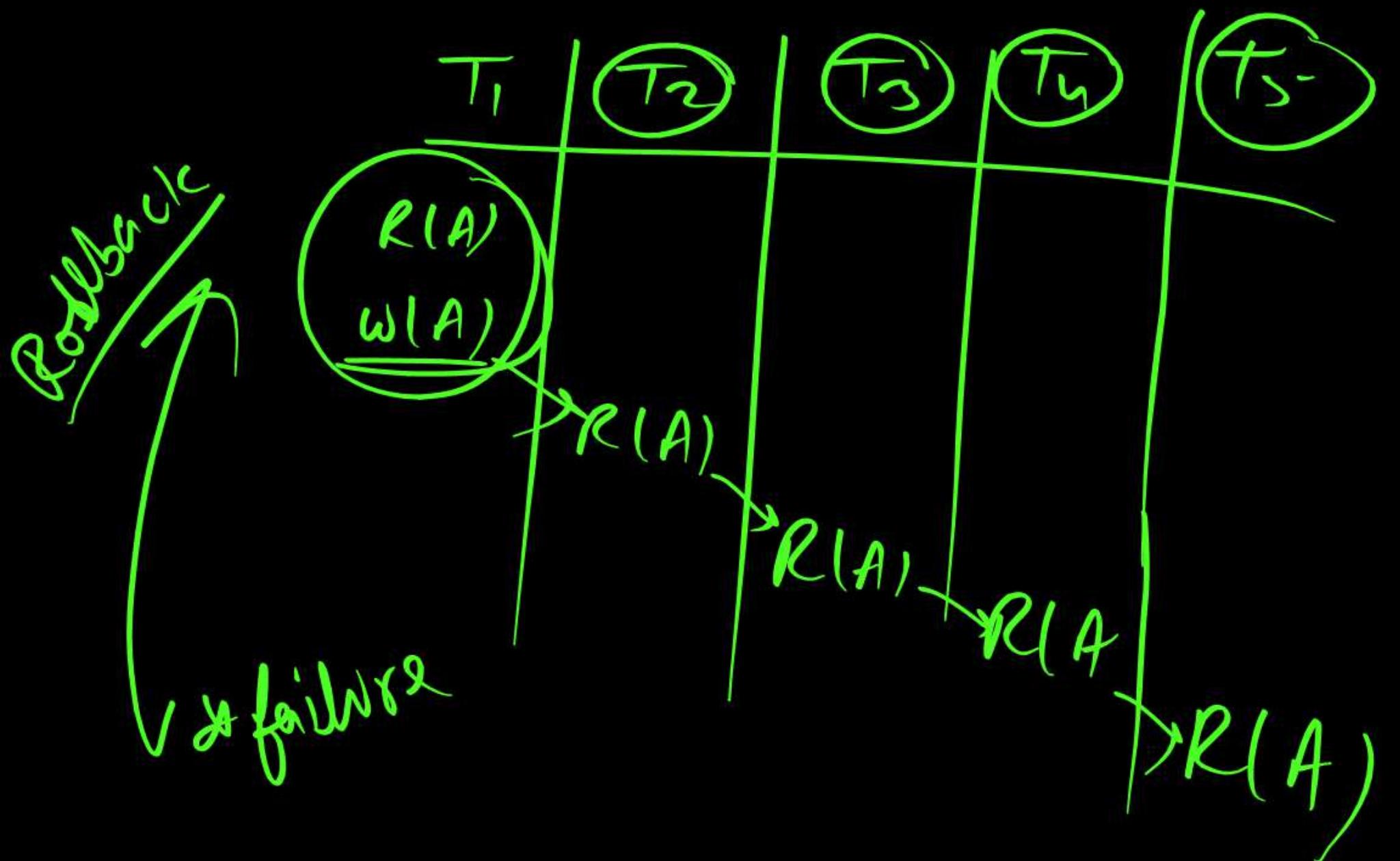
T ₁	T ₂
<u>W(A)</u>	<u>W(A)</u> Commit
Commit	

Recoverable
But WW Problem

T ₁	T ₂
<u>R(A)</u> <u>W(A)</u>	<u>R(A)</u>
<u>W(B)</u>	<u>R(B)</u> Commit

Recoverable
But WR Problem

P
W



Cascading Rollbacks

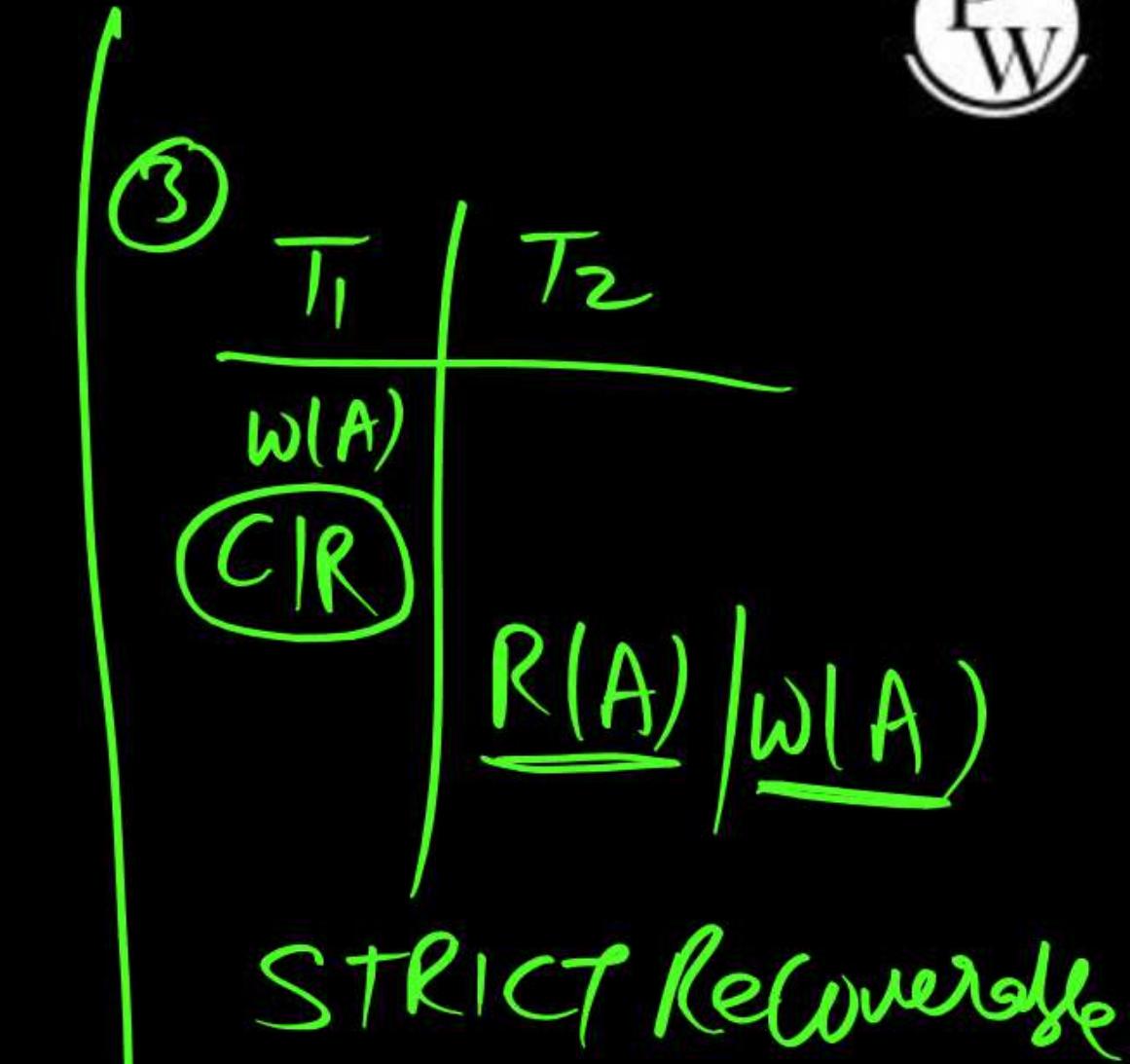
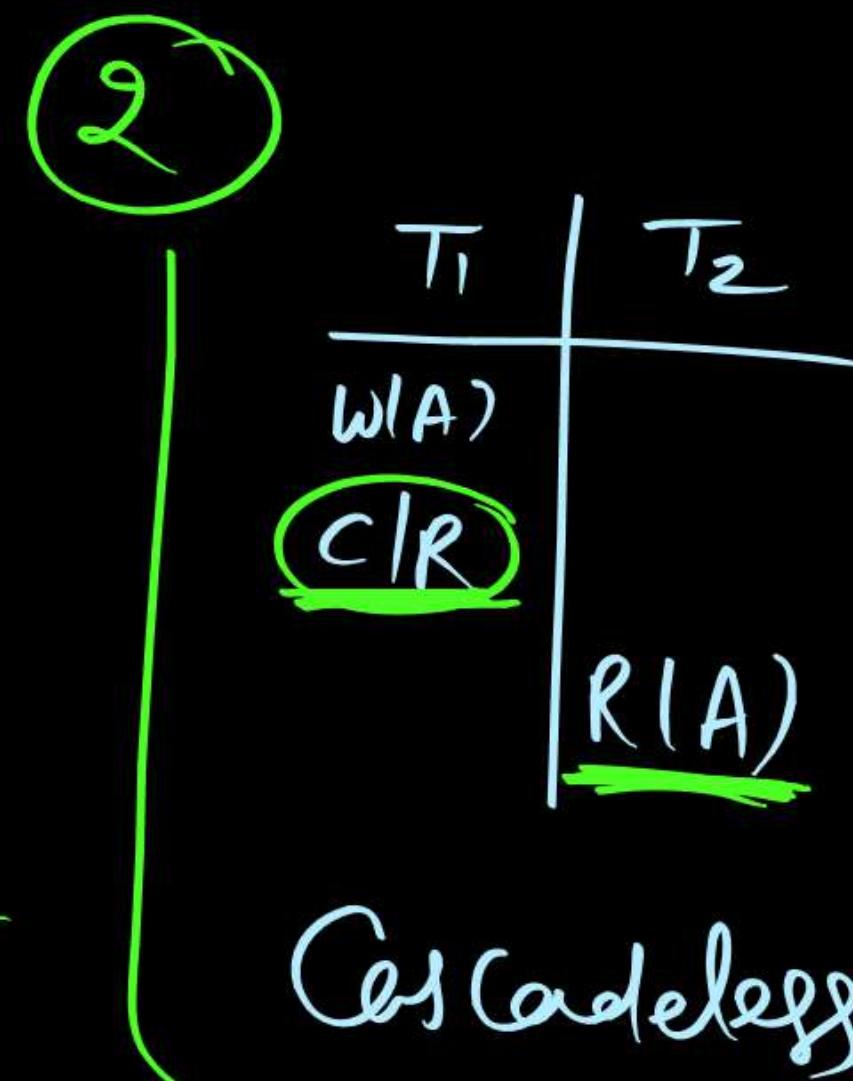
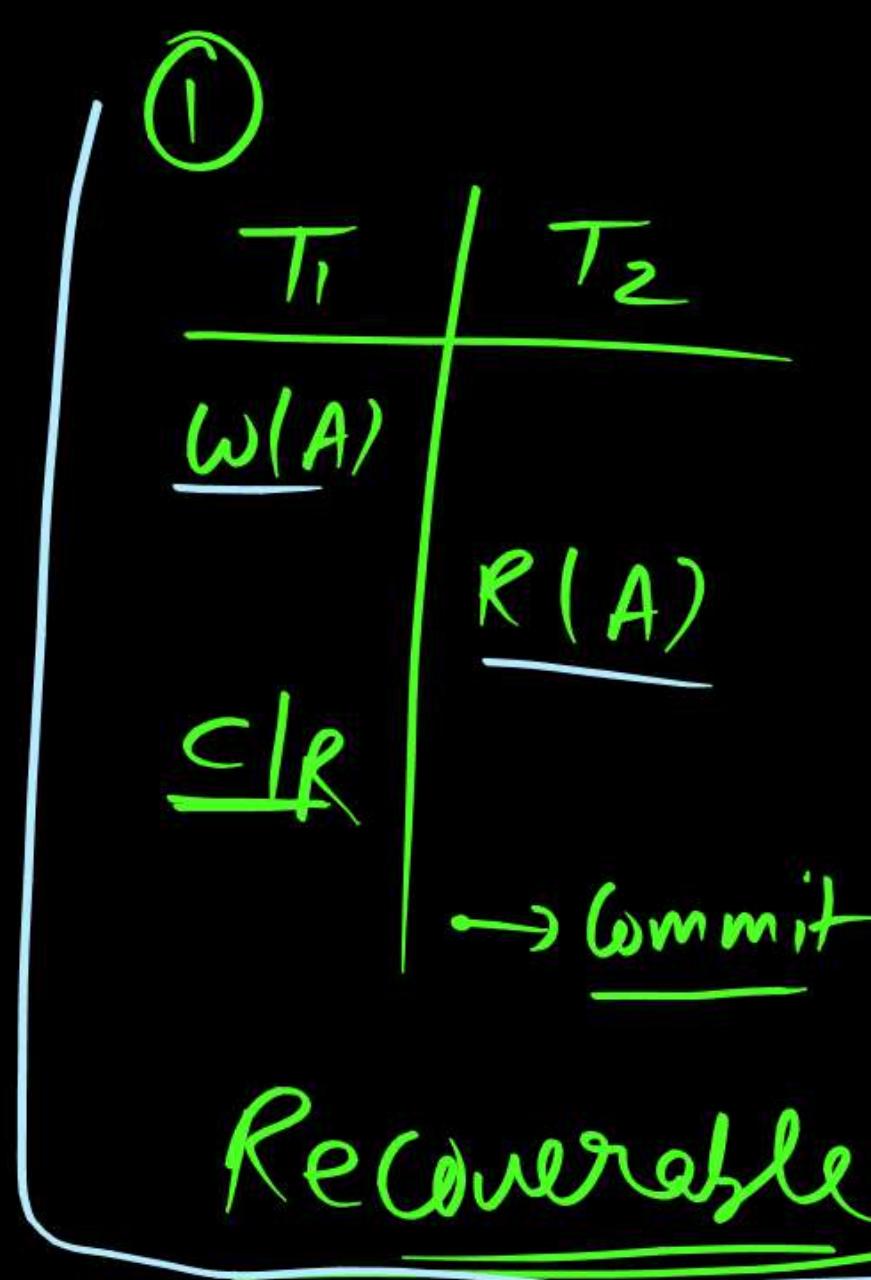
- ❑ Cascading rollback - a single transaction failure leads to a series of transaction rollbacks. Consider the following schedule where none of the transactions has yet committed (so the schedule is recoverable)

T_{10}	T_{11}	T_{12}
read(A)		
read(B)		
<u>write(A)</u>	read(A)	
	<u>write(A)</u>	read(A)
abort		

If T_{10} fails, T_{11} and T_{12} must also be rolled back.

- ❑ Can lead to the undoing of a significant amount of work

P
W



- Allowed Uncommitted Read (UR)
- Cascading Rollback
- RW & WW Problem

No Uncommitted Read
No Cascading Rollback
Only RW & WW

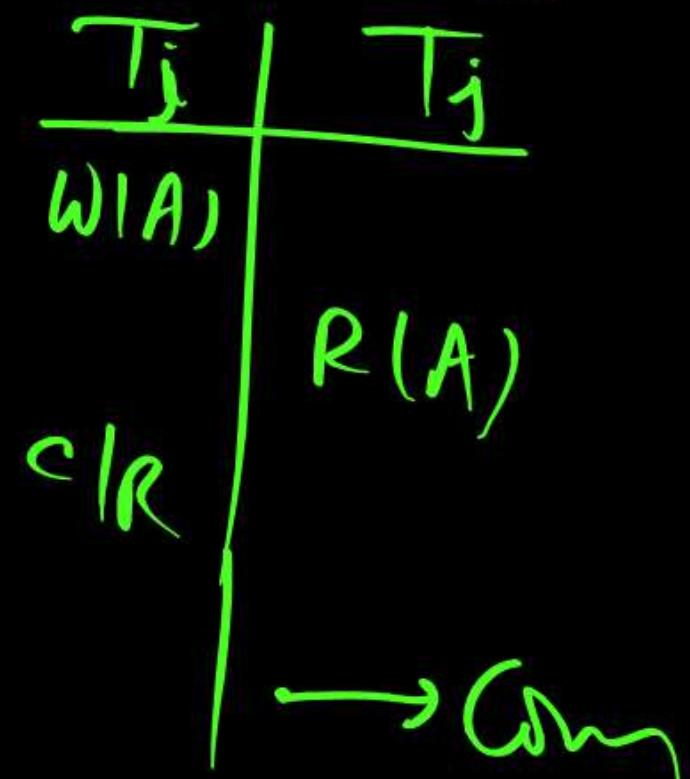
only RW Exist

Cascadeless Schedules

- ❑ Cascadeless schedules — cascading rollbacks cannot occur;
- ❖ For each pair of transactions T_i and T_j such that T_j reads a data item previously written by T_i , the commit operation of T_i appears before the read operation of T_j .
- ❑ Every cascadeless schedule is also recoverable

T_1	T_2
$W(A)$ $C R$	$R(A)$

Cascadeless Schedule



Strict Recoverable Schedule

T_1	T_2
$W(A)$ $C R$	$R(A) w(A)$

P
W

T_1	T_2
<u>W(A)</u>	<u>R(A)</u>
<u>C R</u>	<u>Commit</u>

T_1	T_2
<u>W(A)</u>	<u>C R</u>
	<u>R(A)</u>

T_1	T_2
<u>W(A)</u>	<u>C R</u>
	<u>R(Q)/W(Q)</u>

Recoverable

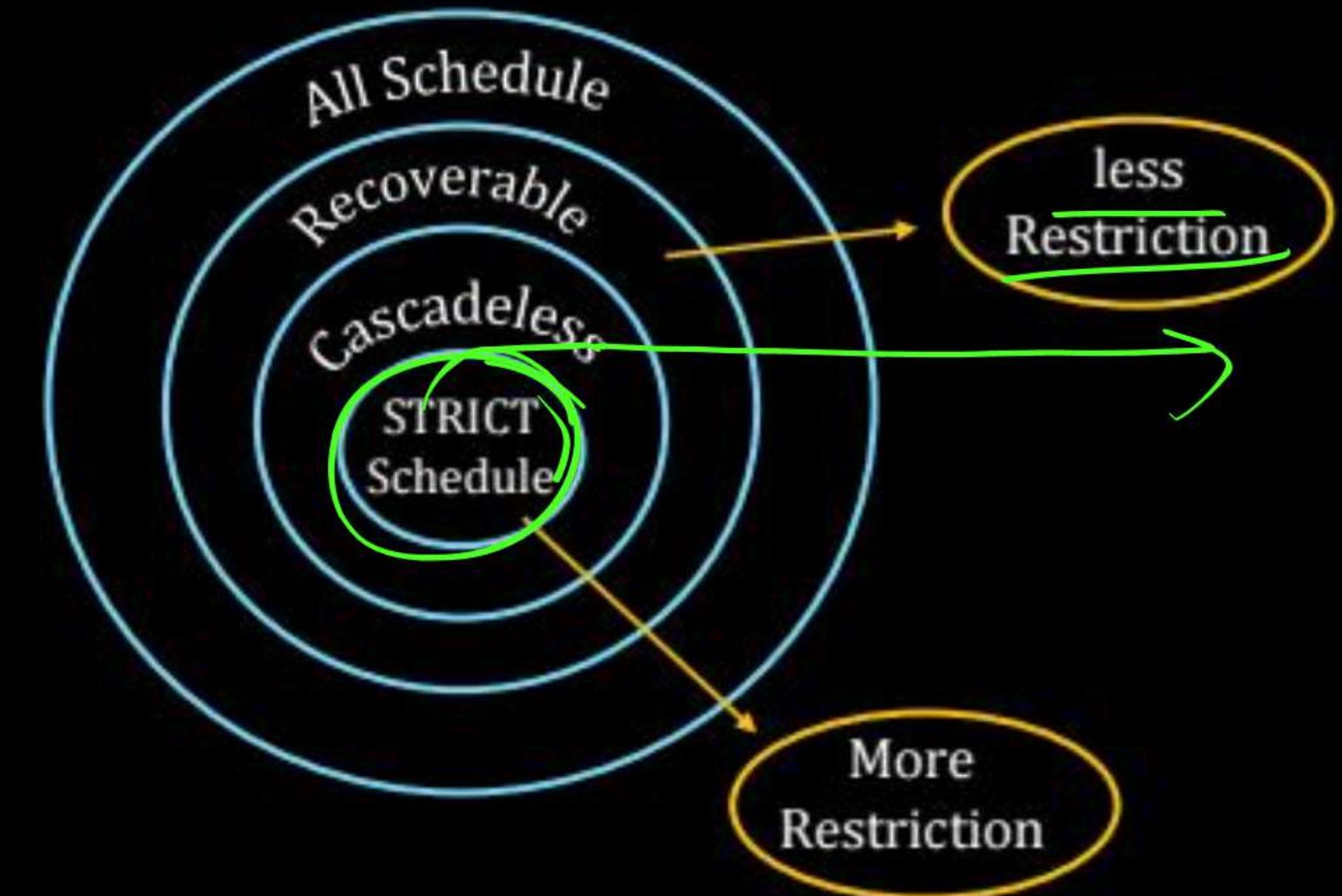
- Un Committed Read (WR)
- RW
- WU
- Other

Cascadeless

- RW Problem
- WW Problem

Strict
schedule

Only RW



Q.

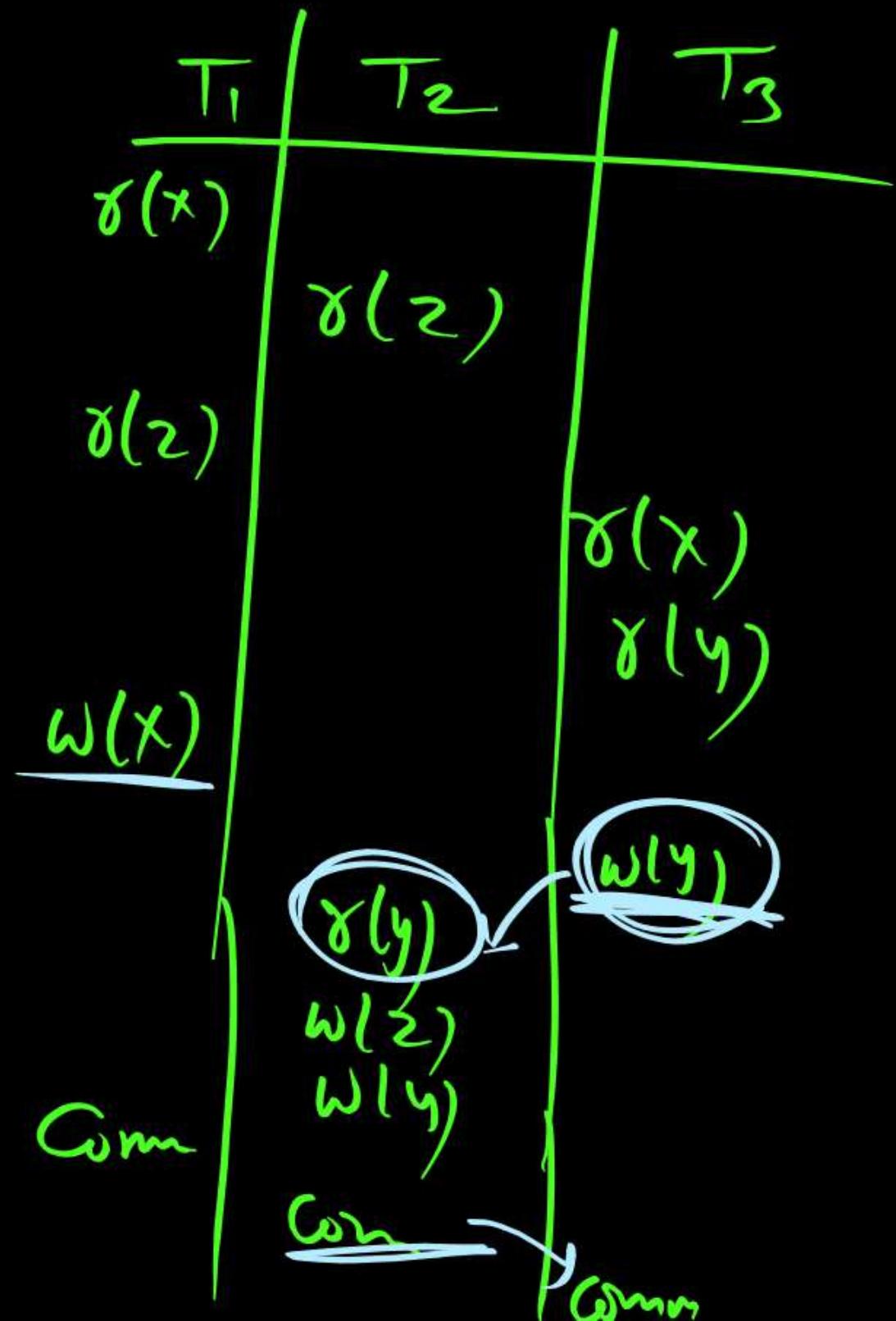
$$r_1(x)r_2(z)r_1(z)r_3(x)r_3(y)w_1(x)w_3(y)r_2(y)w_2(z)w_2(y) C_1 C_2 C_3$$



Commit 3

each Data Item

$$\underline{w \rightarrow R}$$



Recoverable

~~Irrecoverable~~

Q.

$$r_1(x) r_2(x) w_1(y) w_2(y) r_2(y) C_1 C_2.$$

P
W

$$\begin{array}{c|c} T_1 & T_2 \\ \hline L_1 & L_3 \\ L_2 & L_4 \end{array}$$

$\{L_1, L_2, L_3, L_4\}$
 $\{L_3, L_4, L_1, L_2\}$

$$\begin{array}{c|c} T_1 & T_2 \\ \hline 0 & 1 \\ 0 & 1 \end{array}$$

0011
 1100
 0101
 0110
 1010
 1001

$L_1, L_3, L_2, L_4 \oplus L_1, L_3, L_4, L_2$
 $L_3, L_4, L_1, L_2 \oplus L_3, L_1, L_2, L_4$

Finding Total Number of concurrent Schedule

T ₁	T ₂
R ₁ (A) W ₁ (A)	
	R ₂ (B) W ₂ (B)

T ₁	T ₂
L ₁ L ₂	L ₃ L ₄

T ₁	T ₂
0	1
0	1

$L_1 L_2 L_3 L_4$] } Serial
 $L_3 L_4 L_1 L_2$] } Non Serial
 $L_1 L_3 L_2 L_4$ (or) $L_1 L_3 L_4 L_2$] } Non Serial
 $L_3 L_1 L_4 L_2$ (or) $L_3 L_1 L_2 L_4$] } Non Serial

T ₁	T ₂
R(A) W(A)	
	R(B) W(B)

$S_1 < T_1 T_2 >$
(1)

T ₁	T ₂
	R(B)
R(A)	W(B)

$S_2 < T_2 T_1 >$
(2)

T ₁	T ₂
R(A)	
	W(A)

(3)

T ₁	T ₂
R(A)	
	R(B)

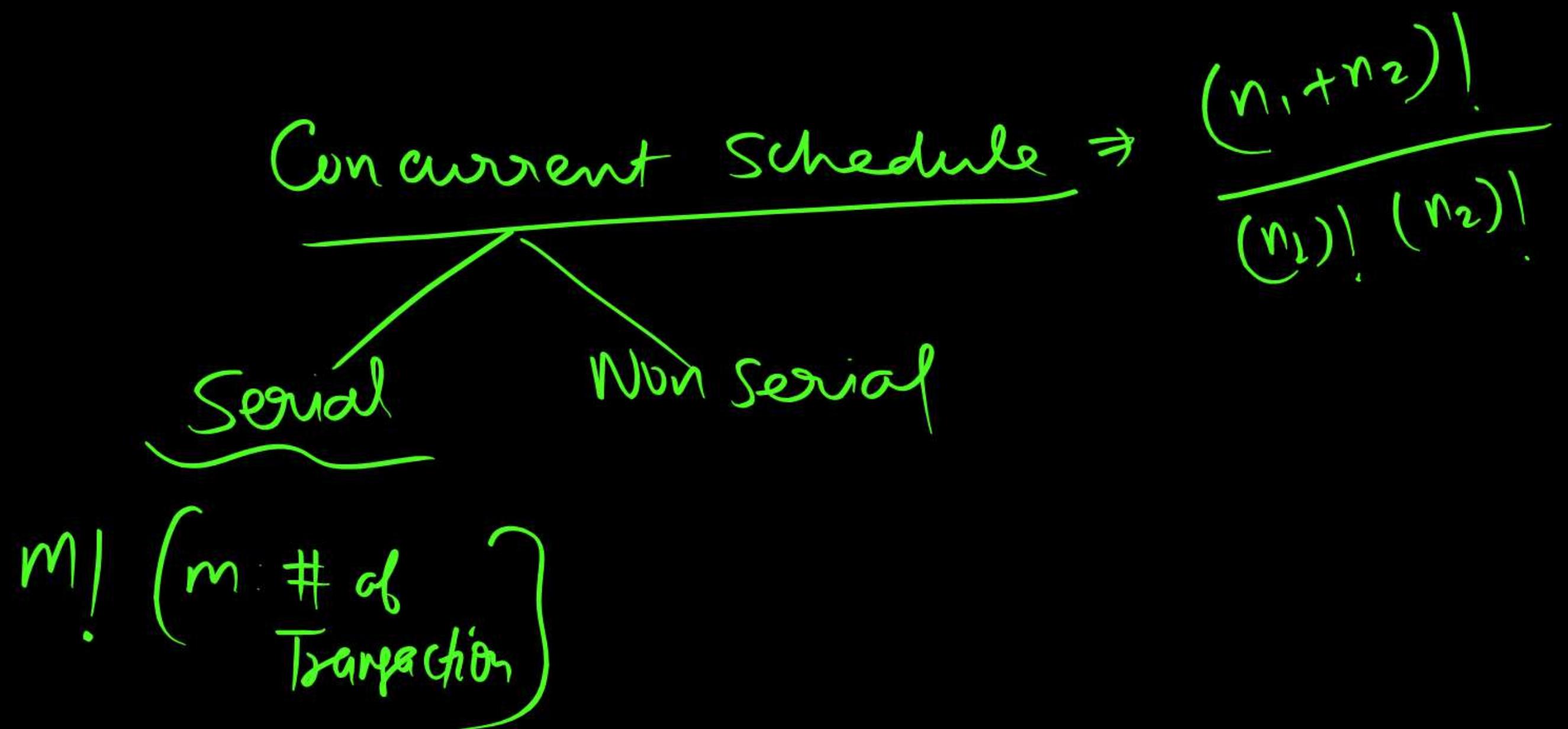
(4)

T ₁	T ₂
R(A)	R(B)
	W(B)

(5)

T ₁	T ₂
	R(B)
R(A)	

(6)



$$\text{Total # Concurrent} = \frac{(n_1+n_2)!}{(n_1)!(n_2)!}$$

Schedule

$$= \frac{(2+2)!}{(2)!(2)!} = \frac{4 \times 3 \times 2}{2 \times 2} = 6$$

 $T_1 \rightarrow \underline{n_1 \text{ operation}}$

2 operation

 $T_2 \rightarrow \underline{n_2 \text{ operation}}$

2 operation

$$\text{Total Concurrent} = 6$$

$$\text{Total non serial Schedule} = \text{Total Concurrent} - \underline{\text{Serial schedule}(m!)} \\ m: \# \text{ of transaction}$$

$$= 6 - 2$$

$$\text{Serial} = 2$$

$$\text{Total non Serial} = 4$$

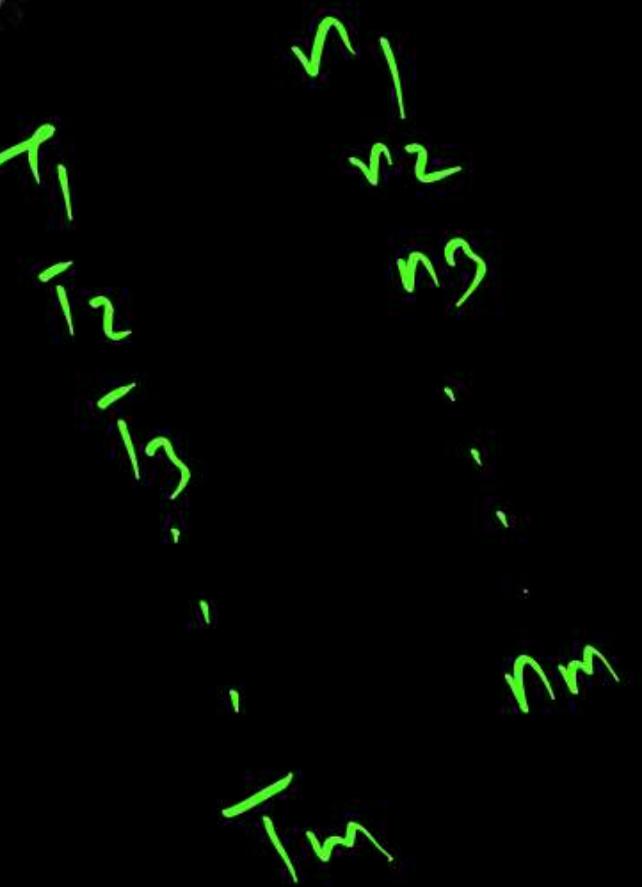
2) = 2

NOTE:

The Number of Concurrent schedule that can be formed
Over m transaction having $n_1 \ n_2 \ n_3 \dots n_m$ operation respectively

$$\text{Total # of Concurrent Schedule} = \frac{(n_1+n_2+n_3+\dots+n_m)!}{(n_1!)(n_2!)(n_2!) \dots (n_m!)}$$

$$\text{Total # of Non Serial Schedule} = \frac{(n_1+n_2+n_3+\dots+n_m)!}{(n_1!)(n_2!)(n_2!) \dots (n_m!)} - m!$$



Q. Find total number of Concurrent & non serial schedule over these transaction T_1 T_2 & T_3 having 2, 3 & 4 operation respectively?



Total # of Concurrent Schedule

$$\frac{(2+3+4)!}{(2!)(3!)(4!)} = \frac{9!}{2!3!4!} = \frac{9 \times 8 \times 7 \times 6 \times 5 \times 4!}{2 \times 3 \times 2 \times 4!} = 1260$$

Non Serial = $1260 - [3!]$

Non serial = 1254

~~1260 - 6~~ - 1254

3 transaction Serial schedule = $3! = 3 \times 2 = 6$

3! = 6

**THANK
YOU!**

