

# CS & IT ENGINEERING

## Theory of Computation

Lecture No.- 01

Mallesham Devasane Sir



# Topics to be Covered



Topic

Regular Expression



## Regular Expression: NAT



Q1. Consider the following regular expressions:

$$r_1 = (a + b)^* = \Sigma^*$$

$$r_2 = (ab^*a + b^*)$$

$$r_3 = (ab^+a + b^+ + \epsilon) = ab^+a + b^*$$

if  $r_4 = r_1 \cap r_2 \cap r_3$  then the number of strings in  $r_4$  which not contain "bbb" are

—

$$\gamma_1 \cap \gamma_2 = \gamma_2$$

= 5 //

$$\gamma_2 \cap \gamma_3 = \underbrace{ab^+a}_{babaa} + \underbrace{b^*}_{\begin{array}{l} \epsilon \\ bbb \end{array}}$$



## Regular Expression: MCQ



Q2.  $(a+b)^*$  is equivalent to

- A  $(aa^*+bb^*)^* = (a+b)^*$
- B  $(aa+bb)^* \quad \begin{matrix} \checkmark \\ ax \end{matrix}$
- C  $(aaa+bbb)^* \quad \begin{matrix} \checkmark \\ ax \end{matrix}$
- D  $(ab^*+ba^*)^* = (a+b)^*$



## Regular Expression: MSQ

P  
W

Q3. Which of the following is/are correct?

- A  $a(ba)^* = (ab)^*a$   
 $\overbrace{a, aba, ababa, \dots}^a$
- B  $(a^*b)^* = (a + b)^*$   
 $\overbrace{a, aba, ababa, \dots}^{a, a}$
- C  $a + ba = (a + b)(a + a)$
- D  $\phi^* = \epsilon$

$$(a^*b)^* \xleftarrow{\epsilon} ax$$

$$(a^*b^*)^* = (a+b)^*$$

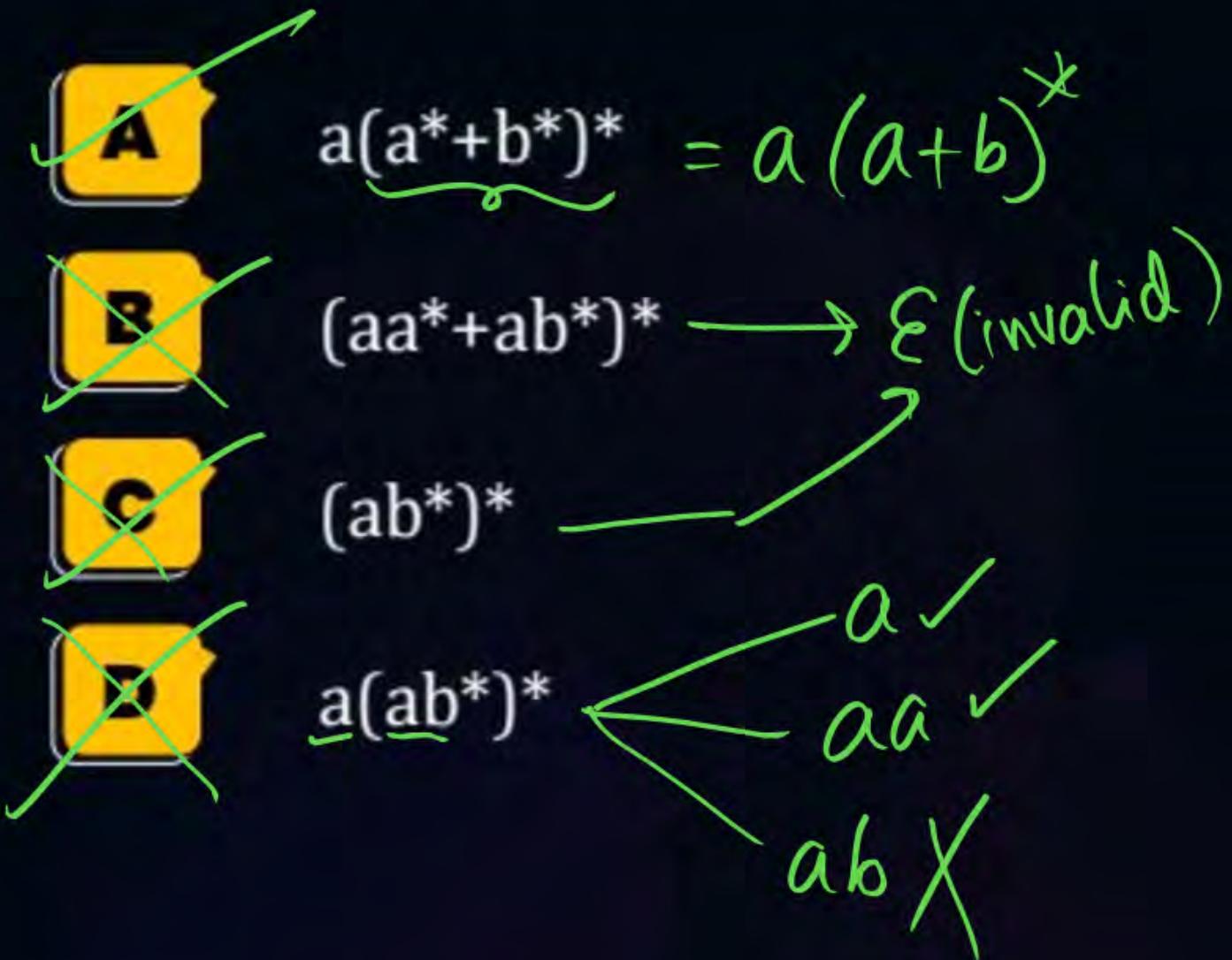
$$(a^*b)^* \neq (a+b)^*$$



## Regular Expression: MSQ

Q4.  $a(a+b)^*$  is equivalent to

$$a(a+b)^* \Rightarrow \{ a, aa, ab, \dots \}$$





## Regular Expression: MCQ



Q5. Consider the following regular expression on input symbol {a, b}:

$$\text{Regular expression } R = \boxed{(b + aa^* b)}^+ \boxed{(b + aa^* b) (a + ba^* b)^* (a + ba^* b)}$$

Which of the following string is not generated by R?

A

epsilon  $\notin R$

B

a  $\notin R$

C

b  $\in R$

D

ab  $\in R$

b  
ab  
aab

b.E.Q = ba  
b.Q.a = baa



## Regular Expression: MCQ

$\{w \mid w \in \{0,1\}^* \text{ and } n_1(w) = \text{even}\}$

Q6. Which of the following represents set of all binary numbers with even number of 1's?

A

Some STAND  
 $(11)^*$   $\xrightarrow{0} 110$

B

Some  
 $(01010)^*$   $\xrightarrow{0} 0$

C

$(0^*10^*10^*)^*$

D

None of these.

$(0^*10^*10^*)^* + 0^*$

$\{\epsilon, 0, 00, 11, 110, 011, 101, 000, \dots\}$   
Zero no. of 1's  
Two 1's



# Regular Expression: NAT



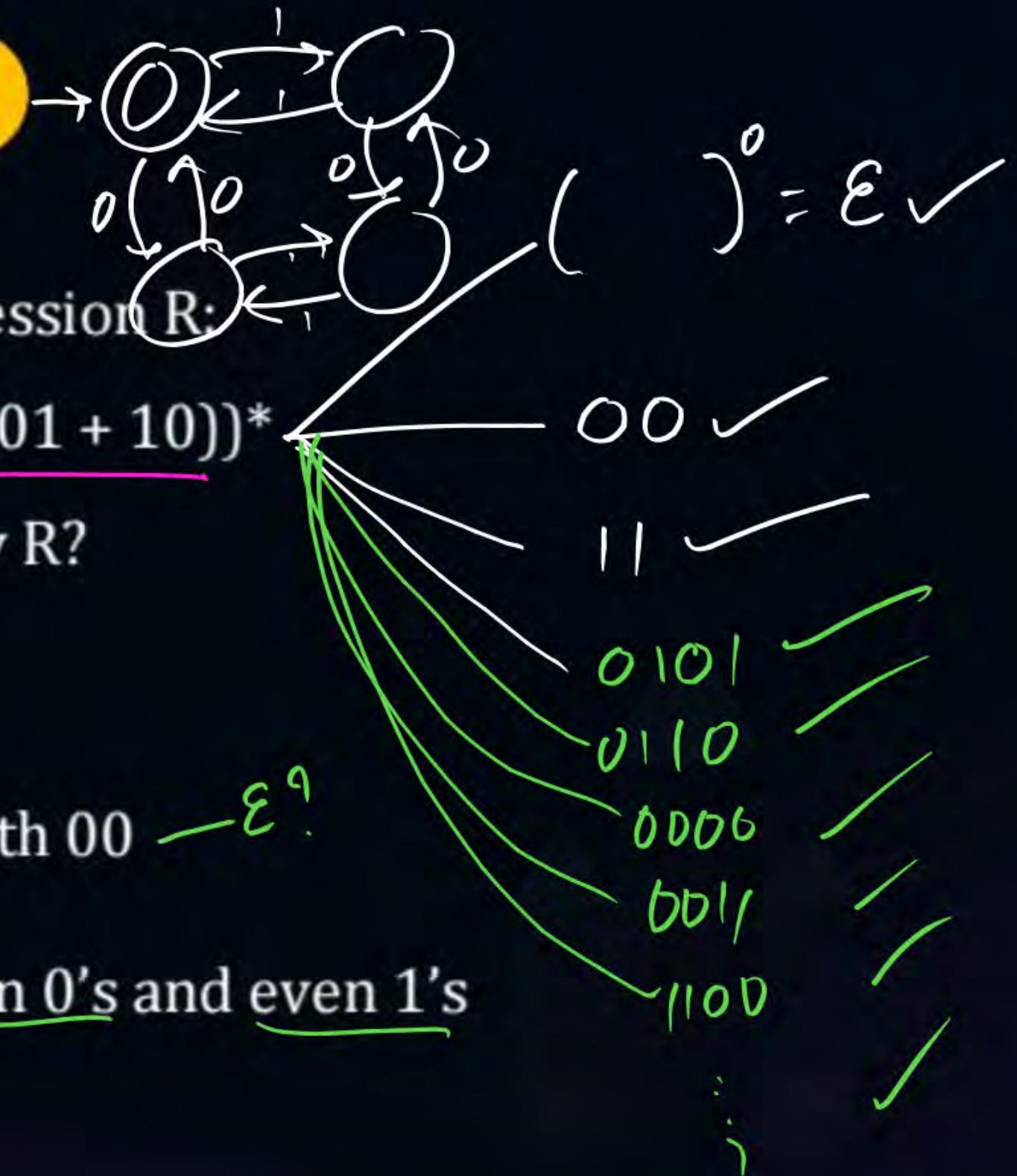
Q7.

Consider the following regular expression:

$$R = (\underline{00} + \underline{11} + (01 + 10)(00 + 11)^* (01 + 10))^*$$

What is the language represented by R?

- A Set of all binary strings  $\{0, 1\}^*$
  - B Set of all binary strings starting with 00  $\{0, 1\}^* \{00\}$
  - C Set of all binary strings having even 0's and even 1's
  - D None of these.





## Regular Expression: MCQ



Q8. Consider the regular expression R:

$$R = \epsilon + a + b + (aa + ba + bb) (a + b)^*$$

$$(a^x b)^+$$

The language recognize by R is

- A  $\{\epsilon \in \{a, b\}^* \mid \text{all strings of } a \text{ and } b \text{ not starting with } a \text{ or not end with } b\}$  X
- B  $\{w \in \{a, b\}^* \mid \text{all strings of } a \text{ and } b \text{ not starting with } ab\}$  ✓
- C  $\{w \in \{a, b\}^* \mid \text{all the strings of } a \text{ and } b \text{ contain either } a \text{ or } b \text{ as a substring}\}$  X
- D  $\{w \in \{a, b\}^* \mid \text{all the strings of } a \text{ and } b \text{ are not ending with } ab\}$  X



## Regular Expression: MSQ



Q9.  $L = \{ w \mid w \in \{0,1\}^*, \underbrace{n_1(w)}_{\text{No. of } 1\text{s in } w} \text{ is divisible by 3} \}$

$(0^* 1 0^* 1 0^*)^*$

- A**  $(111)^*$
- B**  $(01010)^*$
- C**  $(0^* 1 0^* 1 0^*)^*$
- D** None of these



## Regular Expression: MSQ

Q10.

$$\begin{array}{l} A \rightarrow (00)^* \longrightarrow \{ \varepsilon, 00, 0^4, 0^6, \dots \} \\ B \rightarrow 0(00)^* \longrightarrow \{ 0^3, 0^5, 0^7, 0^9, \dots \} \\ C \rightarrow A + B \\ D \rightarrow A \cap B \end{array}$$

$A \cap B = \emptyset$

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**A**

Even zero's

**B**

odd no. of 0's

**C**

All strings

**D**

Empty set



## Regular Expression: MSQ



Q11.  $(a+b)^*$  =

**A**  $a^* (ba^*)^*$

**C**  $b^* (ab^*)^*$

**B**  $(a^*b)^* a^*$

**D**  $(b^*a)^* b^*$



## Regular Expression: MSQ



Q12.  $a(a+b)^*$  = { $a, aa, ab, aaa, aab, aba, abb, \dots$ }

~~A~~  $(ab^*)^+$

~~C~~  $(a^+ b^*)^+$

~~B~~  $(a^+ b^*)^* = \{\epsilon\}$

~~D~~  $(a b^*)^* = \{\epsilon\}$



## Regular Expression: MCQ



Q13. Which of the following regular expression describes the language over  $\{a, b\}$

consisting of strings that do not start with 'a' or do not end with 'b'.

A

$b(a + b)^* + (a + b)^*a + \epsilon$

$$b\underbrace{\Sigma^*}_{\text{do not start with 'a'}} + \epsilon + \underline{\quad} \quad \Sigma^*a + \epsilon$$

B

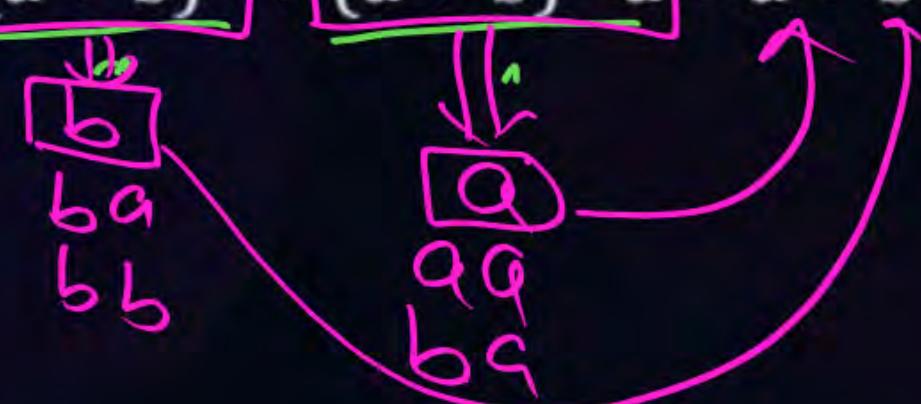
$ab(a + b)^* + \epsilon$

C

$(a + b)(a + b)^* + \epsilon$

D

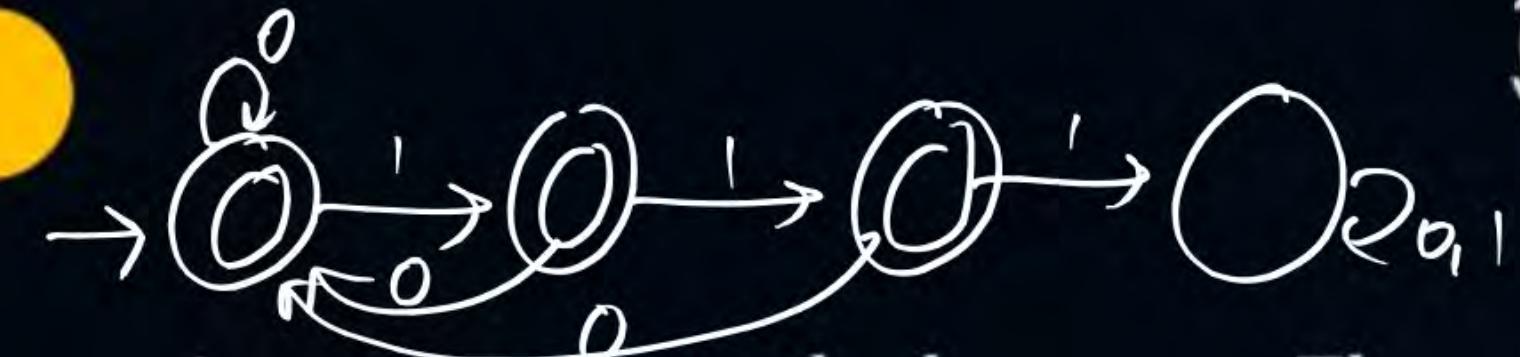
$b(a + b)^* + (a + b)^*a + a + b + \epsilon$





## Regular Expression: MSQ

P  
W



Q14. Which of the following regular expressions represents the language: The set of all binary strings not having three consecutive 1's?

A

$(110 + 10 + 0)^* (\epsilon + 11 + 1)$   $\rightarrow \{ \epsilon, 0, 1, 00, 01, 10, 11, 000, 001, 010, 011, 100, 101, 110, \cancel{111}, \dots \}$

B

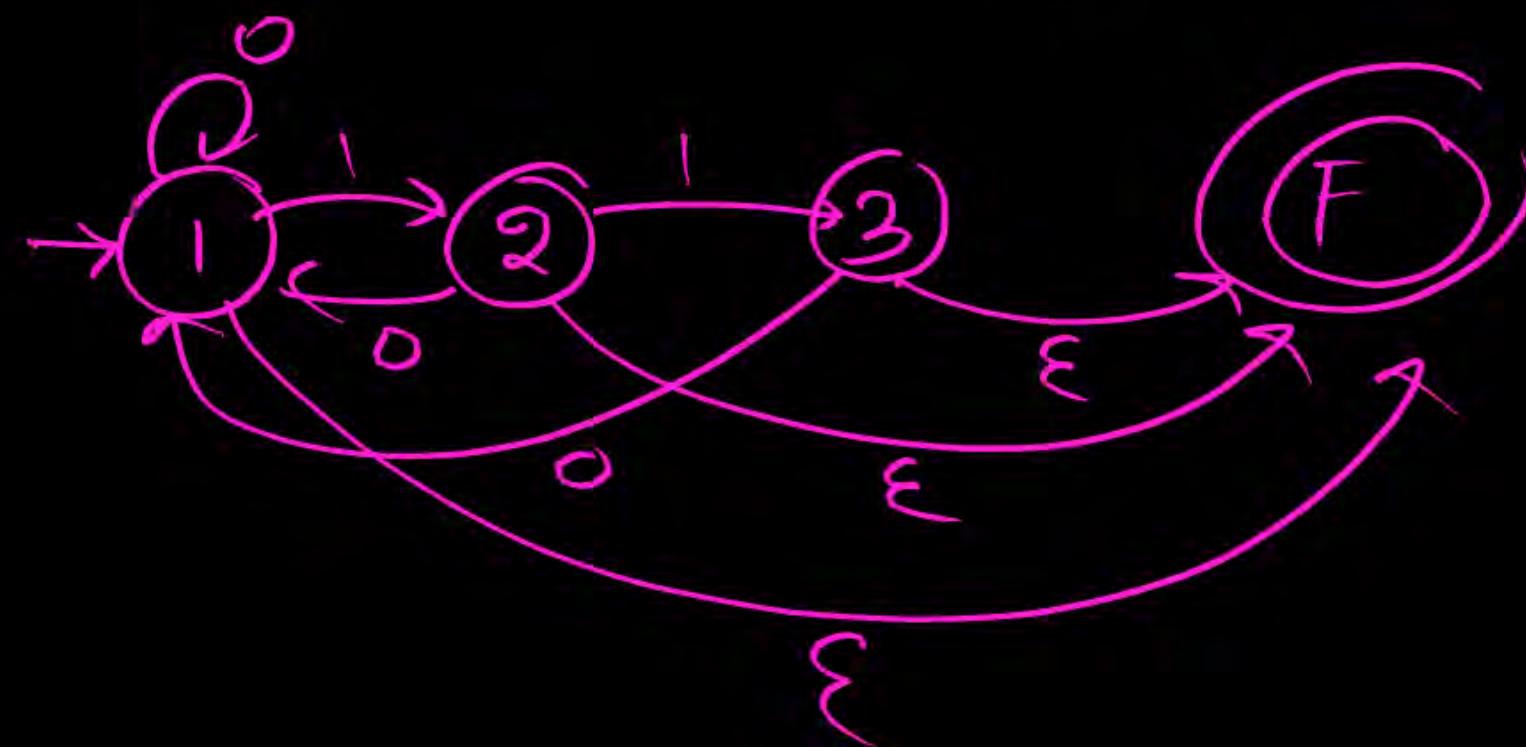
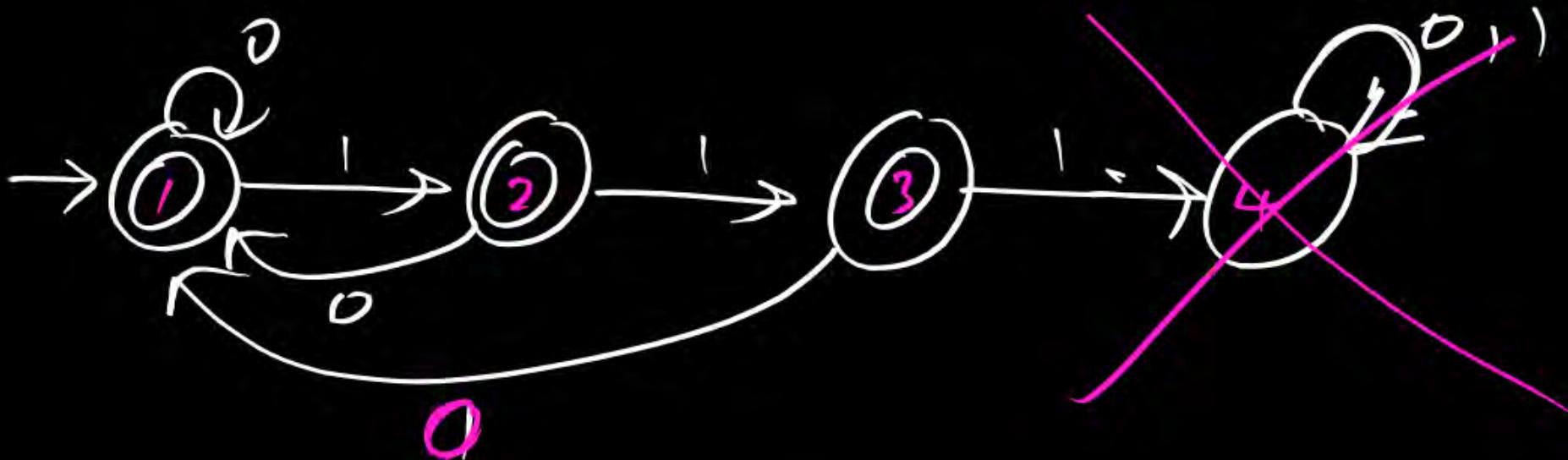
$(\epsilon + \underline{11} + 1) (\underline{110} + \underline{10} + 0)^*$

C

$(011 + \underline{01} + 0)^* (\epsilon + \underline{11} + 1)$

D

$(\epsilon + \underline{11} + 1) (011 + \underline{01} + 0)^*$



Eliminate state 2 and  
state 3  
≡



## Regular Expression: MCQ



Q15. Consider the following regular language L:

$$L = \{w \mid \text{number of } a\text{'s (}w\text{)} \bmod 3 \neq 1 \text{ where } w \in (a, b)^*\}$$

Which one of the following represents above language L?

A

$$(\epsilon + b^* ab^* ab^* + ab^*) (a + b)^*$$

B

$$[(b^* ab^* ab^* ab^*)^* + b^*] (b^*ab^*ab^*)$$

C

$$[(b^*a b^*a b^*ab^*)^* + (b^* + \epsilon + b^*ab^*ab^*)]$$

D

$$[b^*a b^*ab^* ab^*)^* + b^*] (\epsilon + b^*ab^*ab^*)$$



## Regular Expression: MCQ



Q16. Which of the following represents set of all strings starts and ends with different symbols over a's and b's?

**A**

$a(a + b)^* b$

**C**

$a(a + b)^* b + b(a + b)^* a$

**B**

$a(a + b)^* a + b(a + b)^* b$

**D**

None of these



## Regular Expression: MCQ



Q17. Which of the following is TRUE ?

A  $|((|))^* = ((|((|))^*)^*$

C  $((|((|))^*)^* = |^*$

B  $((|)^* = ((|((|))^*)^*$

D  $((|)^* = |^*$



## Regular Expression: MCQ

Q18. Consider the following regular expression given below:

$$R_1 = (01 + (1 + 01)0)^* (1 + 01)$$

$$R_2 = (01)^* (1 + 01) (0(01)^* (0 + 01))^*$$

Which of the following is correct about  $R_1$  and  $R_2$ ?

A

String “0110” generated by  $R_2$  but not  $R_1$ .

B

String “0110” generated by  $R_1$  but not  $R_2$ .

C

Both expression generates the same language.

D

None of these



## Regular Expression: MCQ

Q19. Suppose the length of language  $|L_1| = 5$  and  $|L_2| = 4$  then, which of the following is correct?

- A  $|L_1 \cdot L_2| \geq 5$
- B  $|L_1 \cdot L_2| \geq 20$
- C  $|L_1 \cdot L_2| \geq 9$
- D  $|L_1 \cdot L_2| \leq 20$



## Regular Expression: MCQ



Q20. Choose correct statement.

- A  $R + \phi = R \cdot \phi$
- B  $R + R = R \cdot R$
- C  $R + \epsilon = R + \phi$
- D  $R + R = R \cdot \epsilon$

# THANK - YOU

# CS & IT ENGINEERING

## Theory of Computation

Lecture No.- 02

Mallesham Devasane Sir



# Topics to be Covered



Topic

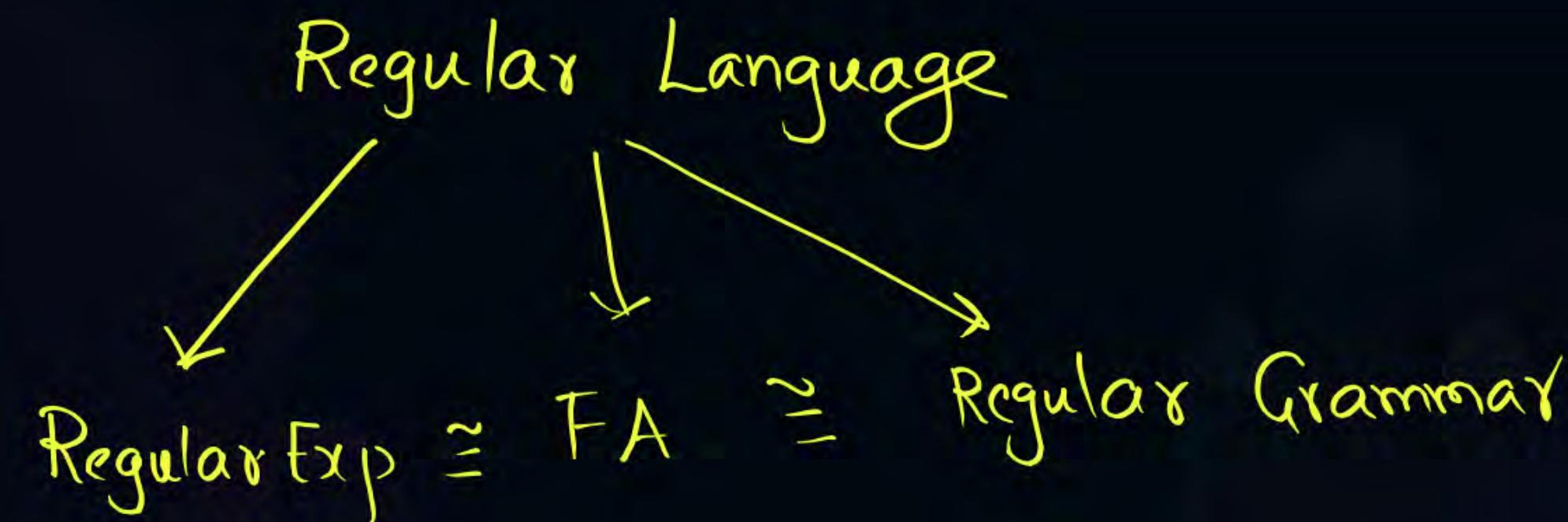
Regular Expression

Topic

Finite Automata



# Regular Expression & Finite Automata





## Regular Exp & FA : MCQ

P  
W

$$L = \{\epsilon, b^*, aa, babab^*, \dots\}$$

Q15. Consider the following regular language L:

$$L = \{w \mid \text{number of } a's (w) \bmod 3 \neq 1 \text{ where } w \in (a, b)^*\}$$

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Which one of the following represents above language L?

~~A~~

$$(\epsilon + b^* ab^* ab^* + ab^*) (a+b)^* = (a+b)^*$$

~~B~~

$$[(b^* ab^* ab^* ab^*)^* + b^*] (b^* ab^* ab^*)$$

$\not\models a's$   
not pos.

~~C~~

$$[(b^* a b^* a b^* ab^*)^* + (b^* + \epsilon + b^* ab^* ab^*)]$$

~~D~~

$$[b^* a b^* ab^* ab^*]^* + b^* (\epsilon + b^* ab^* ab^*)$$

$\not\models a's$   
 $\models a's$   
 $\models a's$

$n_a(w) \% 3 = 0 \text{ or } 2$

$\checkmark \#a's = 0, 2, 3, 5, 6, 8, \dots$

$n_a(w) \% 3 \neq 1$

$\#a's \neq 1, 4, 7, 10, \dots$

#a's % 3 = 0 or 2

$\{a, b\}$

$$= (b^* a b a b a b^*)^* (b^* + b^* a b a b^*)$$

$$= ((b^* a b a b a b^*)^* + b^*) (\epsilon + b^* a b a b^*)$$



## Regular Exp & FA : MCQ



Q16. Which of the following represents set of all strings starts and ends with different symbols over a's and b's?

$$a \sum^* b + b \sum^* a$$

A  $a(a+b)^* b$

C  $a(a+b)^* b + b(a+b)^* a$

D  $a(a+b)^* a + b(a+b)^* b$

D None of these



## Regular Exp & FA : MCQ



Q17. Which of the following is TRUE ?

A

$$1((11)^*)^* = ((1((11)^*))^*)$$

$\underbrace{1}_{\text{Min}=1}$        $\underbrace{((11)^*)^*}_{\text{Min}=\epsilon}$

C

$$((1((11)^*)^*)^* = 1^*$$

$\underbrace{((1((11)^*)^*)^*}_{\epsilon, 1, 11, 111, \dots}$

B

$$((11)^*)^* = ((1((11)^*))^*)$$

$\underbrace{((11)^*)^*}_{1 \text{ not possible}}$

D

$$((11)^*)^* = 1^*$$

$\underbrace{((11)^*)^*}_{\text{even}}$        $\underbrace{1^*}_{\text{All}}$



## Regular Exp & FA : MCQ



Q18. Consider the following regular expression given below:

$$R_1 = (01 + (1 + 01)0)^* (1 + 01)$$

$$R_2 = \underline{(01)^*} \underline{(1 + 01)} \underline{(0(01)^* (0 + 01))^*}$$

Which of the following is correct about  $R_1$  and  $R_2$ ?

A

String “0110” generated by  $R_2$  but not  $R_1$ .

B

String “0110” generated by  $R_1$  but not  $R_2$ .

C

Both expression generates the same language.

D

None of these



## Regular Exp & FA : MCQ



Q19. Suppose the ~~length~~<sup>Size</sup> of language  $|L_1| = 5$  and  $|L_2| = 4$  then, which of the following is correct?

$$|L_1 L_2| \geq 8$$

$$L_1 = \{a, b, c, d, e\}$$

A

$$|L_1 \cdot L_2| \geq 5$$

B

$$|L_1 \cdot L_2| \geq 20$$

C

$$|L_1 \cdot L_2| \geq 9$$

D

$$|L_1 \cdot L_2| \leq 20$$

$$\boxed{8 \leq |L_1 L_2| \leq 20}$$

$$L_2 = \{f, g, h, i\}$$

$$L_1 L_2 = \underbrace{\{ \}}_{5 \times 4}, \dots \}$$

20 strings



## Regular Exp & FA : MCQ



Q20. Choose correct statement.

A

$$\overbrace{R + \phi}^R = \overbrace{R \cdot \phi}^\phi \quad \times$$

B

$$\overbrace{R + R}^R = \overbrace{R \cdot R}^R \quad \times$$

C

$$R + \epsilon = \overbrace{R + \phi}^R \quad \times$$

D

$$\overbrace{R + R}^R = \overbrace{R \cdot \epsilon}^R$$



## Regular Exp & FA : MCQ

Q20.

~~choose correct statement.~~

Which of the following is possible for some  $R$  ?

A

$$R + \phi = R \cdot \phi \text{ possible when } R = \phi$$

B

$$R + R = R \cdot R \text{ possible when } R = \epsilon$$

C

$$R + \epsilon = R + \phi$$

D

$$R + R = R \cdot \epsilon$$

$$\underbrace{\phi + \phi}_{\phi} = \underbrace{\phi \cdot \phi}_{\phi}$$



## Regular Exp & FA : NAT



Q21. Consider the following regular expressions R:

$$R = \underbrace{(ab^* + ba^*)^*}_{\text{H.W.}} \underbrace{(ba^* + ab^*)}_{\text{H.W.}} = (a+b)^+ \Rightarrow 2 \text{ states}$$

Number of states are needed to design a DFA for above expression R is \_\_\_\_.

H.W. :

$$R = (ab^+ + ba^+)^* (ba^* + ab^*)$$

$\epsilon$ , a, b, aa, ab, ba, bb, . . .



## Regular Exp & FA : MCQ



Q22. Consider the following deterministic finite automata (DFA):

In above DFA  $\{S\}$  is starting state and  $F_1$  and  $F_2$  are final states.

Which of the following language belong to above DFA?

A

$$L = \{ \underbrace{wxw^R}_{w, x \in (a, b)^+} \mid w, x \in (a, b)^+ \} = axa + bxb$$

B

$$L = \{ ww^R x \mid w, x \in (a, b)^+ \} \Rightarrow \text{No DFA}$$

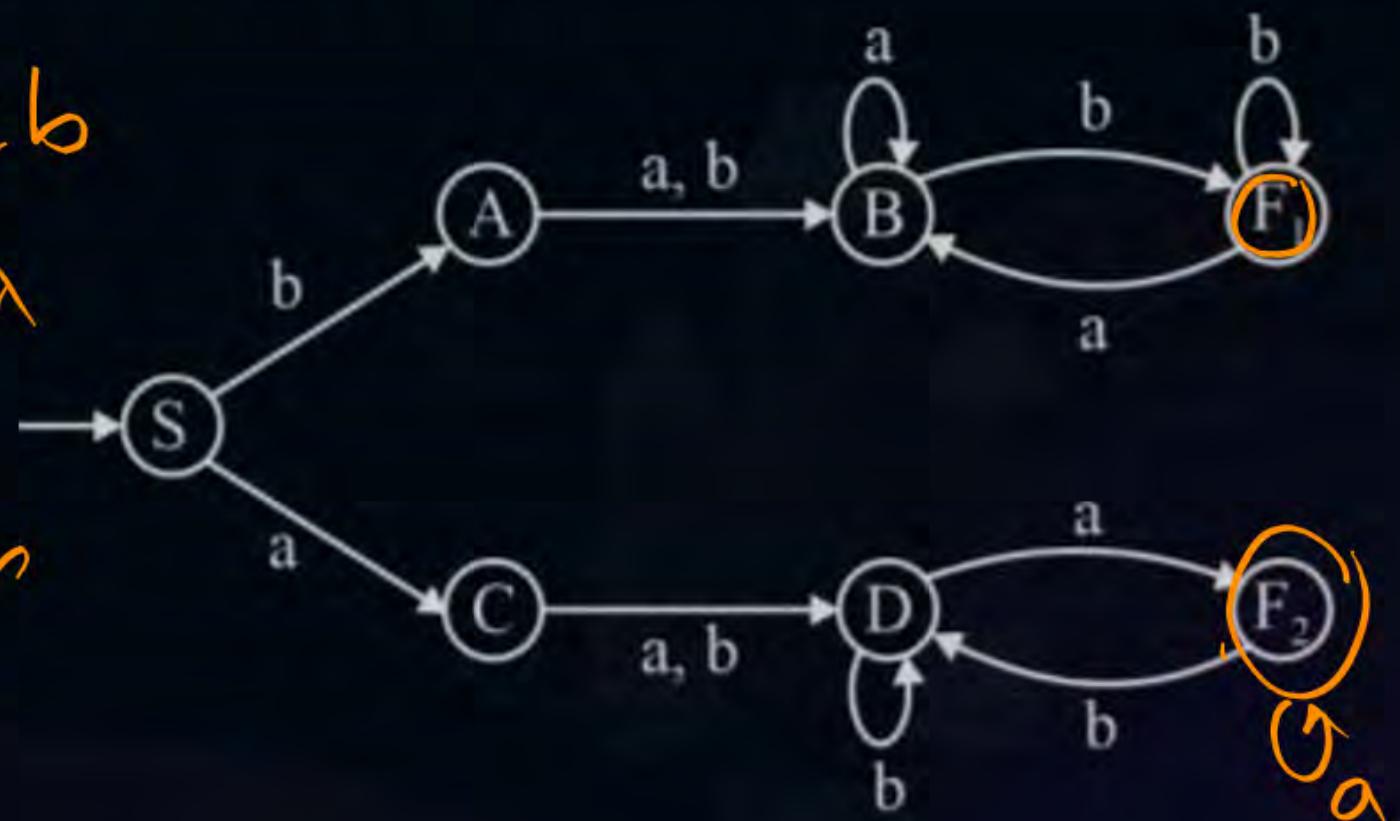
C

$$L = \{ wxw^R \mid w, x \in (a, b)^* \} = (a+b)^*$$

D

None of these.

$$\rightarrow \emptyset \cap a^*$$

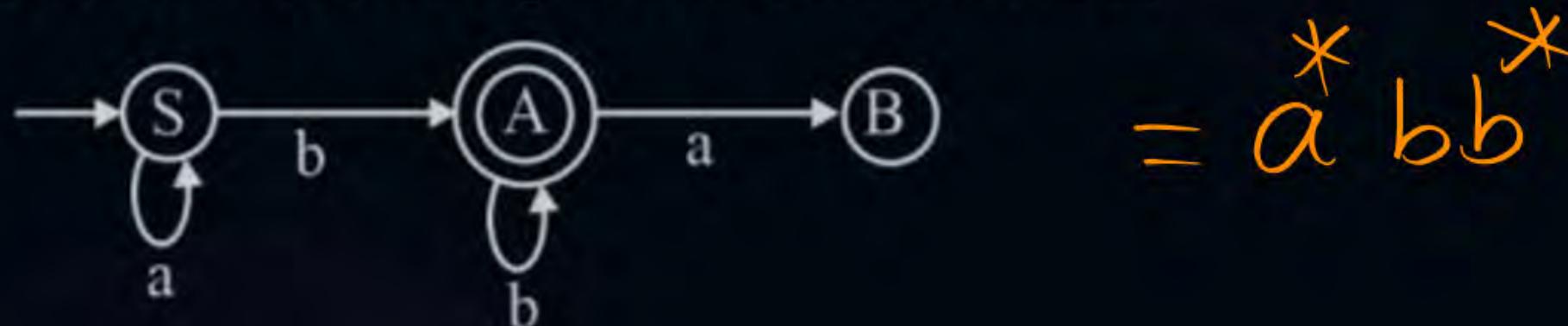




## Regular Exp & FA : MSQ



Q23. Consider the following finite automaton F:



In above finite automata S is starting state and A is final state. Which of the following is/are correct regular expression for above finite automata?

~~A~~

$a^*bb^*a$

~~C~~

$(b + aa^*b) + (b + aa^*b) bb^*$

$$\frac{b + \cancel{aa^*b} + \cancel{bb^*} + \cancel{aa^*b} bb^*}{\cancel{bb} \cancel{bb}} = \overset{a^0}{a^+} b^+$$

~~B~~

$a^*b^+$

~~D~~

$a^*bb^*$

$$\overset{a^0}{a^+} b^+$$



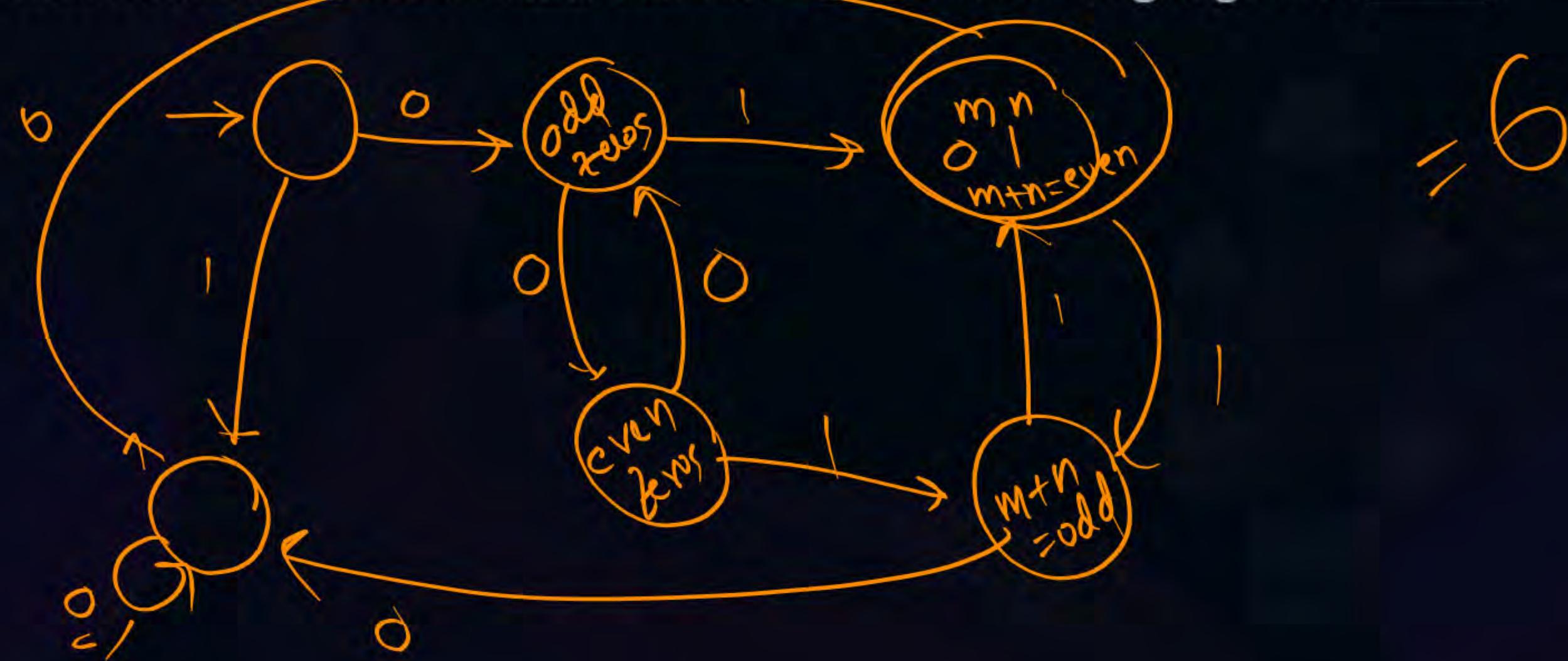
## Regular Exp & FA : NAT



Q24. Consider the language L on  $\Sigma = \{0, 1\}$ :

$$L = \{0^m 1^n \mid m + n = \text{even and } m, n \geq 1\} = \{01, 0011, 0111, 0001, \dots\}$$

The minimum number of states needed for DFA of language L is \_\_\_\_.





## Regular Exp & FA : NAT

Q25. Consider the following regular expression R:

$$R = (00 + 11 + (01 + 10)) (00 + 11)^* (01 + 10)^*$$

Minimum number of states are needed in DFA for above regular expression R is

—  $L = \{w \mid w \in \{0, 1\}^*, n_0(w) \text{ even}, n_1(w) \text{ even}\}$





## Regular Exp & FA : MSQ



$$|w| \% 3 \leq 1$$

Q26. Consider the Language L:

$$L = \{w \mid |w| \% 99 \leq 27 \text{ where, } w \in \{a, b\}^*\}$$

$$(a+b)^3 (\epsilon + a+b)$$

What is the regular expression for above language L?

A

$$((a+b)^{27})^* (a+b)^{99} \quad |w| = 27k+99, k \geq 0$$

B

$$((a+b)^{99})^* (a+b)^{27} \quad |w| = 99k+27, k \geq 0$$

C

$$\underline{((\epsilon + a+b)^{99})^*} \underline{(\epsilon + a+b)^{27}} = (a+b)^* \quad |w| \geq 0$$

D

$$\frac{((a+b)^{99})^* (\epsilon + a+b)^{27}}{\epsilon} \quad |w| = 99k+m, k \geq 0, m \leq 27$$

$$|\omega| \% 99 \leq 27$$

$$\left(\sum_{i=0}^{99}\right)^* (\varepsilon + \Sigma)^{27}$$

$$|\omega| \% 99 = 0$$

OR

$$|\omega| \% 99 = 1$$

OR

$$|\omega| \% 99 = 2$$

OR

$$|\omega| \% 99 = 3$$

$$|\omega| \% 99 = 27$$

$$|\omega| \% 99 = 27$$

remainder

$$\left(\sum_{i=0}^{99}\right)^* \Sigma^{27} \\ ((a+b)^{99})^* (a+b)^{27}$$

$$|\omega| \% 99 = 0$$

$(\sum_{i=0}^{99})^*$  multiple of 99

$$|\omega| \% 99 = 1$$

$$|\omega| = 99k + 1$$

$$\left(\sum_{i=0}^{99}\right)^* \Sigma$$

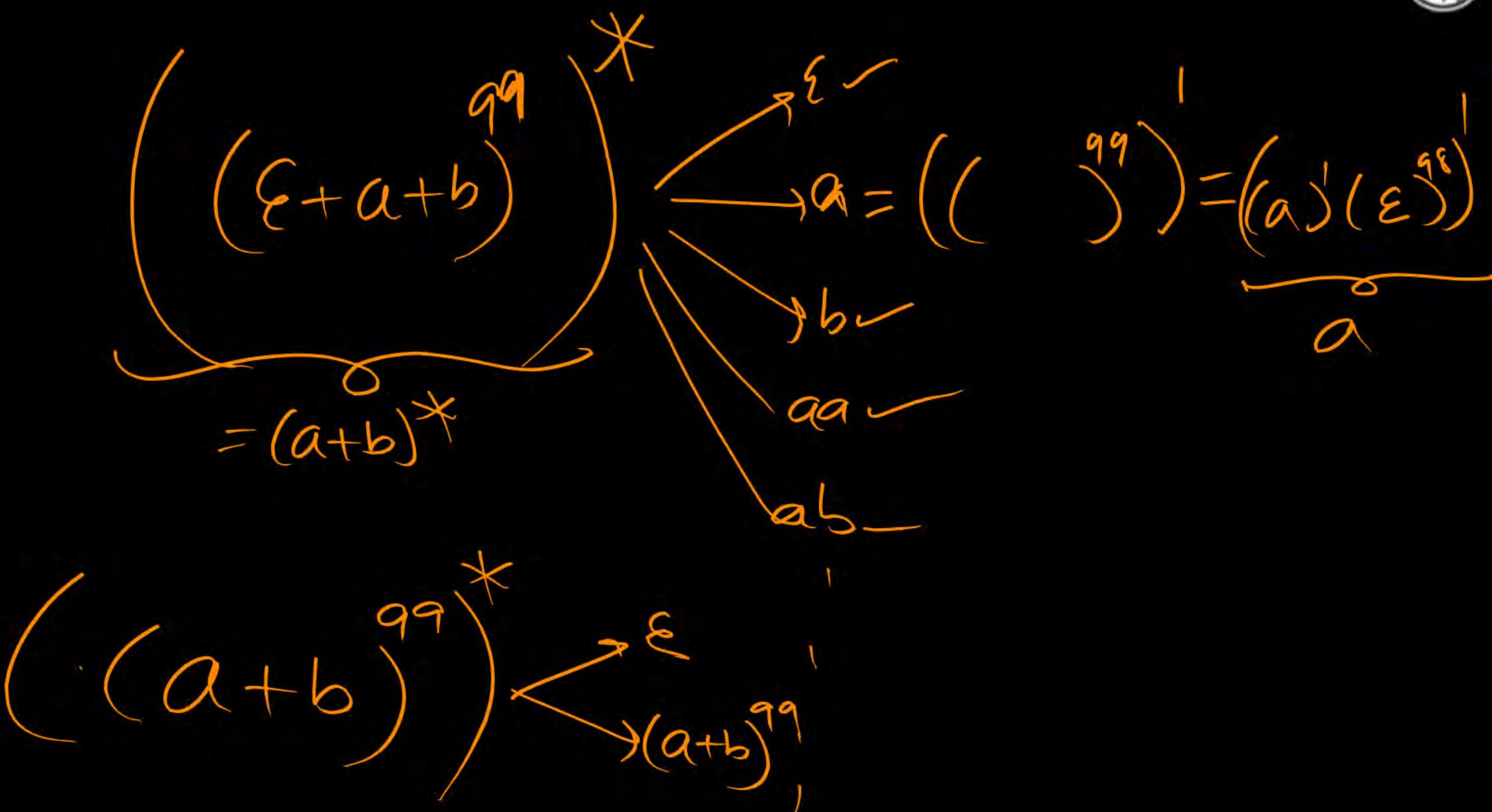
$$|\omega| \% 99 \leq 1$$

$$\left(\sum_{i=0}^{99}\right)^* (\varepsilon + \Sigma)$$

$$|\omega| \% 3 \leq 1$$

$$|\omega| = 0, 1, \cancel{2}, 3, 4, \cancel{5}, 6, 3, \cancel{8}, \dots$$

$$\gamma_{em} = 0, 1, 2, \cancel{3}$$





## Regular Exp & FA : MCQ



Q27. Which of the following regular expression represents the no two consecutive zeros ending with 1?

- A  $(01 + 10 + 11 + 1)^*$   $\xrightarrow{\Sigma} \epsilon \checkmark$
- B  $(01 + 1)^*$   $\xrightarrow{\Sigma} \epsilon \times$
- C  $(01+10+11+1)^*0$   $\xrightarrow{\Sigma} \epsilon \times$
- D None of these

$$L = \{ \epsilon, 0, 1, 00, 01, 10, 11, 000, 001, \dots \}$$



## Regular Exp & FA : MCQ



Q28. Consider the following regular expression R.

$$R = \underbrace{\epsilon + 0}_{\text{A}} \underbrace{(10)^*}_{\text{B}} \underbrace{(\epsilon + 1)}_{\text{C}} + \underbrace{1}_{\text{D}} \underbrace{(01)^*}_{\text{E}} \underbrace{(\epsilon + 0)}_{\text{F}}$$

which one of the following languages over the alphabet {0,1} is described by the above regular expression R?



Set of all binary strings having either 00 or 11 as a substring.

$\epsilon$  is invalid



Set of all binary strings not having 00 as a substring.

$\epsilon, 0, 1, 01, 10, 11$



Set of all binary strings not having 11 as substring.

$\epsilon, 0, 1, 01, 10, 11$   
 $00 \notin R$  → 00 should be in R  
if this option is correct



Set of all binary strings neither having 00 nor 11 as a substring.



## Regular Exp & FA : MCQ

Q29. Suppose  $L_1 = 0^*$

$$L_2 = 10$$

$$L_3 = \{1^m 0^m \mid m \geq 0\}$$

$$L_4 = 1^*$$

If  $L_5 = ((L_2/L_1) - L_4) - \bar{L}_3$  Then, the language  $L_5$  will be:

**A**

$\emptyset$

**C**

$1^*$

**B**

{10}

**D**

{ $\in$ }



## Regular Exp & FA : NAT



- Q30. The number of states in the minimum sized DFA that accepts the language defined by the regular expression  $(00 + 111)^*$  is \_\_\_\_\_.

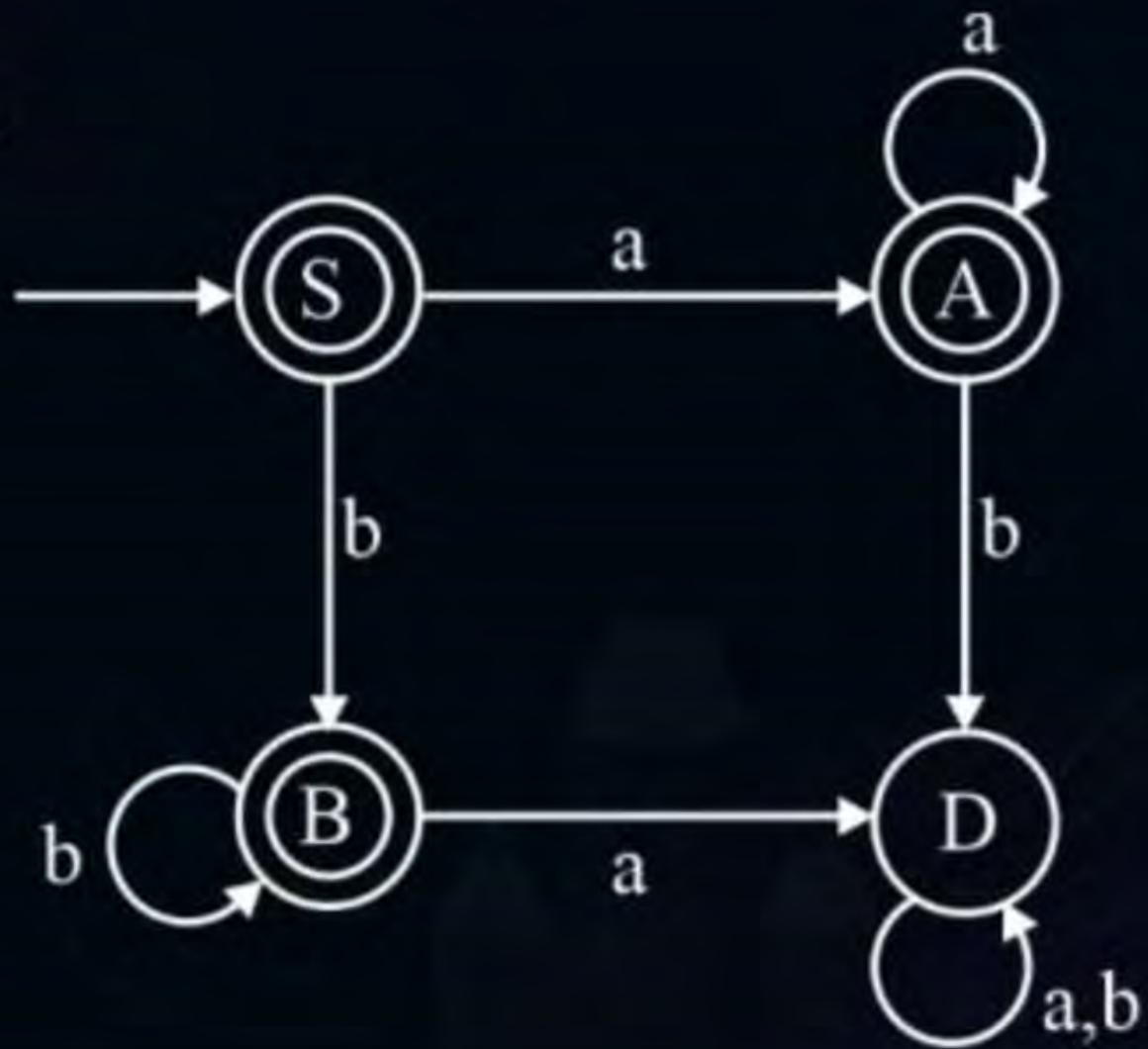


## Regular Exp & FA : MSQ



Q31. Which of the following regular expression is equivalent to the finite automaton?

- A**  $(a + b)^* a + (a + b)^* b$
- B**  $a^* + b^*$
- C**  $\epsilon + a^+ + b^+$
- D**  $\epsilon + aa^* + bb^*$





## Regular Exp & FA : NAT



Q32. Consider grammar G:

G:

$$S \rightarrow aSa \mid a \mid b \mid \epsilon$$

Let  $L = \{w \mid w \in L(G) \text{ and } |w| = 14\}$

Then how many strings are possible in L? \_\_\_\_.



## Regular Exp & FA : MCQ

Q33. Consider two languages  $L_1$  and  $L_2$  on  $\Sigma = \{a, b\}$ .

$L_1 = \{aa, ab\}$  and  $L_2 = \{aa, ab, abab\}$  then which of the following is true?

**A**

$$L_1^* \subset L_2^*$$

**C**

$$L_1^* = L_2^*$$

**B**

$$L_2^* \subset L_1^*$$

**D**

$$(L_1 \cup L_2)^* = (a+b)^*$$



## Regular Exp & FA : MSQ



Q34. Which of the following is/are correct regular expression for  $L = \{ \text{starting and ending with } a \}$ ?

- A**  $a (a + b)^* a$
- B**  $a (a + b)^* a + a$
- C**  $a (a + bb^*a)^*$
- D**  $a (a + bb^*a + aa)^*$

# THANK - YOU

# CS & IT ENGINEERING

## Theory of Computation

Lecture No.- 03

Mallesham Devasane Sir



# Topics to be Covered



Topic

Regular Expression

Topic

Finite Automata

Topic

Regular Grammar



## Regular Languages : MCQ



Q29. Suppose  $L_1 = 0^*$

$$L_2 = 10$$

$$L_3 = \{1^m 0^m \mid m \geq 0\}$$

$$L_4 = 1^*$$

$$L_2 / L_1 = 10 / 0^* = \underbrace{\{10/\epsilon, 10\}}_{10} \cup \underbrace{\{100, 1000, \dots\}}_1 = \phi$$

$$\left[ (L_2 / L_1) - L_4 \right] = \{10, 1\} - 1^* = \{10\}$$

If  $L_5 = ((L_2 / L_1) - L_4) - \bar{L}_3$  Then, the language  $L_5$  will be:

A  $\phi$



C  $1^*$

- B  $\{10\}$
- D  $\{\epsilon\}$

$$\{10\} - \bar{L}_3 = \{10\}$$

$$L_3 = \{0^n\}$$

$$= \{\epsilon, \boxed{10}, 1100, 111000, 11110000, \dots\}$$

$$\overline{L}_3 = \underbrace{(0+1)^*}_{\text{all strings}} - L_3$$

$$\{10\} - \overline{L}_3 = \{10\}$$

$$10\% = 1$$

$$\boxed{uv/v = u}$$

$$10 \cdot \varepsilon / \varepsilon = 10$$

$$10/\square = 1$$

$$\varepsilon \cdot \square / \square = \varepsilon$$





## Regular Languages : NAT

- Q30. The number of states in the minimum sized DFA that accepts the language defined by the regular expression  $(00 + 111)^*$  is \_\_\_\_.





## Regular Languages : MSQ



Q31. Which of the following regular expression is equivalent to the finite automaton?

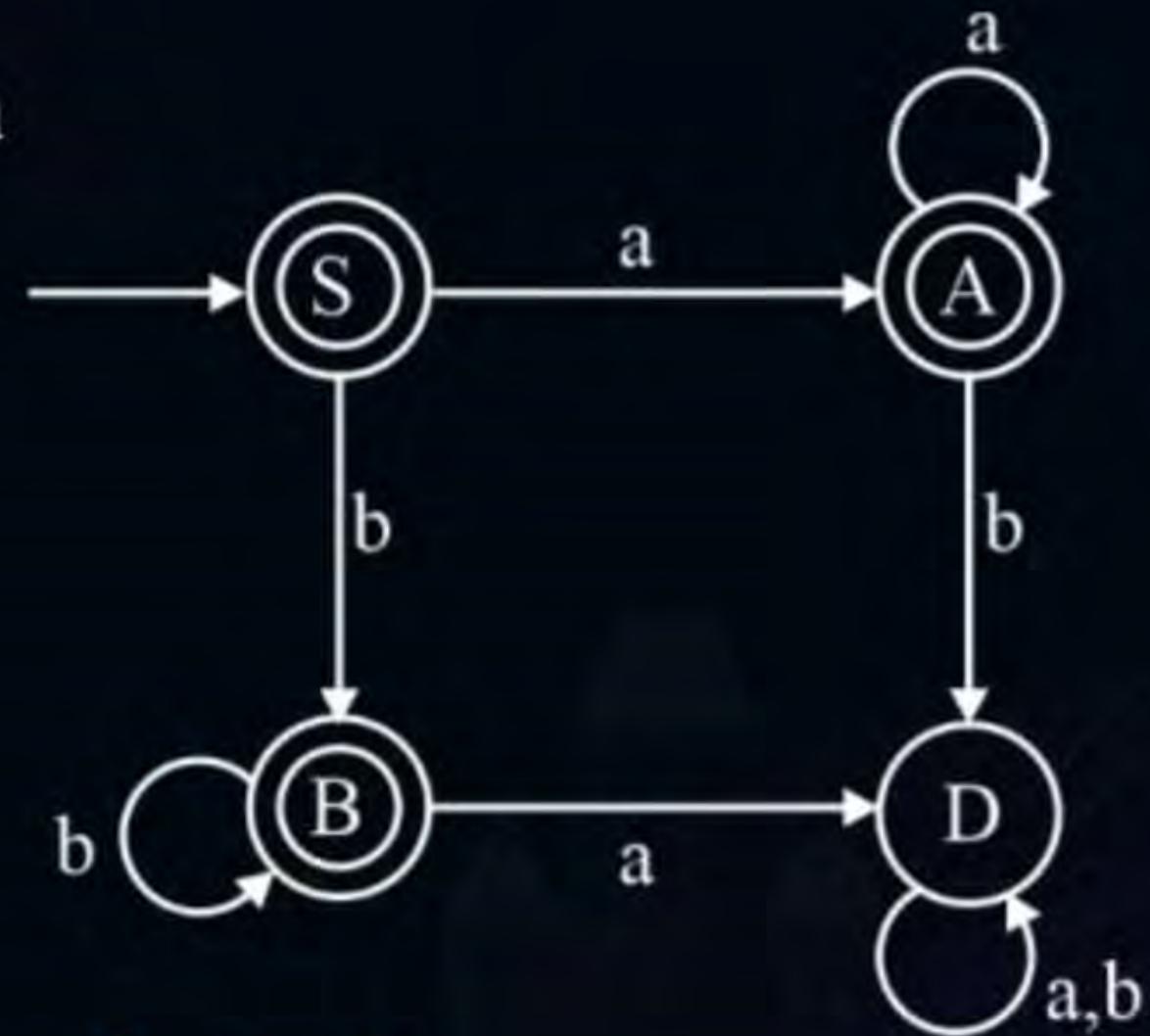
- A
- B
- C
- D

$$(a + b)^* a + (a + b)^* b$$

$$a^* + b^*$$

$$\epsilon + a^+ + b^+$$

$$\epsilon + aa^* + bb^*$$



$$\begin{aligned} & S + A + B \\ & \epsilon + aa^* + bb^* \end{aligned}$$



## Regular Languages : NAT



Q32. Consider grammar G:

G:

$$S \rightarrow aSa \mid a \mid b \mid \epsilon$$

Let  $L = \{w \mid w \in L(G) \text{ and } |w| = 14\}$

$$\begin{array}{c} a^7 S a^7 \xrightarrow{\epsilon} a^{14} \\ \swarrow \qquad \searrow \\ \end{array}$$

Then how many strings are possible in  $L$ ?   .



## Regular Languages : MCQ

Q33. Consider two languages  $L_1$  and  $L_2$  on  $\Sigma = \{a, b\}$ .

(a)

$L_1 = \{\underline{aa}, \underline{ab}\}$  and  $L_2 = \{\underline{aa}, \underline{ab}, \underbrace{abab}\}$  then which of the following is true?

$$L_1 \subset L_2$$

A

$$L_1^* \subset L_2^*$$

B

$$L_2^* \subset L_1^*$$

C

$$L_1^* = L_2^*$$

D

$$(L_1 \cup L_2)^* = (a+b)^*$$

$$L_1^* = (aa+ab)^*$$

$$L_2^* = (aa+\underline{ab}+\underbrace{abab})^* = L_1^*$$



## Regular Languages : MCQ



Q33. Consider two languages  $L_1$  and  $L_2$  on  $\Sigma = \{a, b\}$ .

(b)

$L_1 = \{aa, ab\}$  and  $L_2 = \{aa, ab, \underbrace{abab}\}$  then which of the following is true?

A

$$L_1^* \subseteq L_2^*$$

C

$$L_1^* = L_2^*$$

B

$$L_2^* \subseteq L_1^*$$

D

$$(L_1 \cup L_2)^* = (a+b)^*$$



## Regular Languages : MSQ



Q34. Which of the following is/are correct regular expression for  $L = \{ \text{starting and ending with } a \}$ ?

wilk

$L = \{ w \mid w \in \{a, b\}^*, w \text{ starting & ending with } a \}$

~~A~~  $a(a+b)^*a \rightarrow a \text{ is missing}$

~~B~~  $a(a+b)^*a + a$

~~C~~  $a(a+bb^*a)^*$

~~D~~  $a(a+bb^*a + aa)^*$

$a(a+b)^*a \rightarrow \text{min=aa}$

$\curvearrowleft$  It can't generate all strings

$a$  is missing



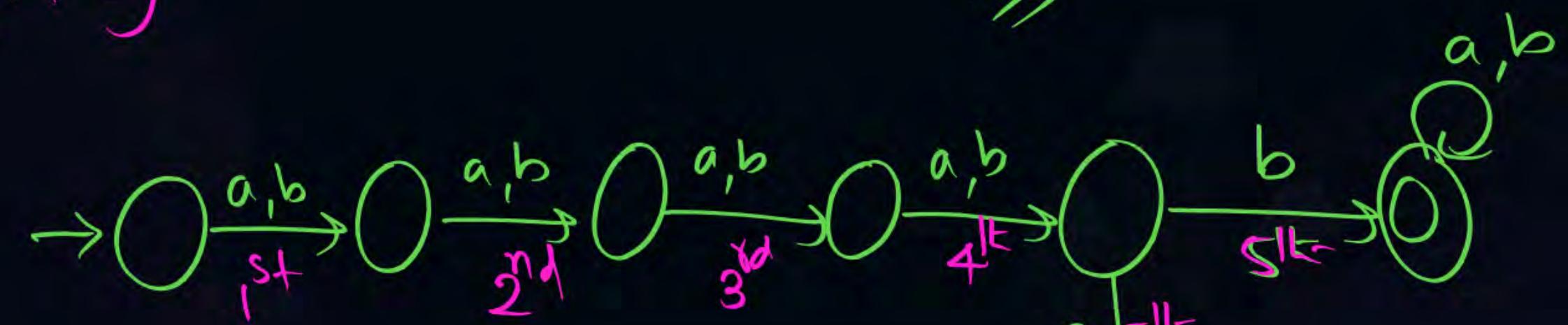
## Regular Languages : NAT



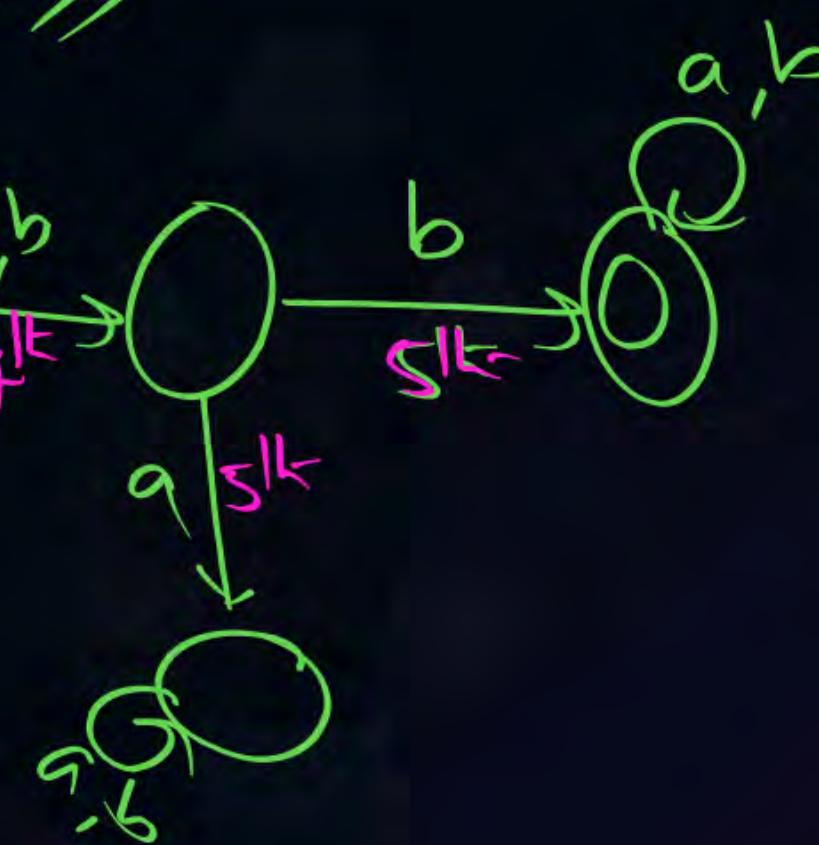
Q35. How many minimal states are needed in DFA to design a language over  $\Sigma = \{a, b\}$  where 5<sup>th</sup> symbol from left is b? \_\_\_

$$(a+b)^4 b (a+b)^*$$

$$5 + 2 = 7,$$



a/b a/b a/b a/b b any





## Regular Exp & FA : NAT



Q36. The number of minimal states in DFA that accepts all the strings over  $\Sigma = \{a, b\}$ . Where “2nd symbol from right hand side is a” are \_\_\_\_.

$$2^K = 2^2 \Rightarrow 4 //$$



## Regular Languages : NAT



Q37. Construct a minimal DFA that accepts all the strings over  $\Sigma = \{a, b\}$ . where, number of occurrence of substring “ab” is even. If number of trap states are  $x$ , number of final states are  $y$  and number of non-final states are  $z$  then the value of “ $xy + z$ ” is \_\_\_\_.

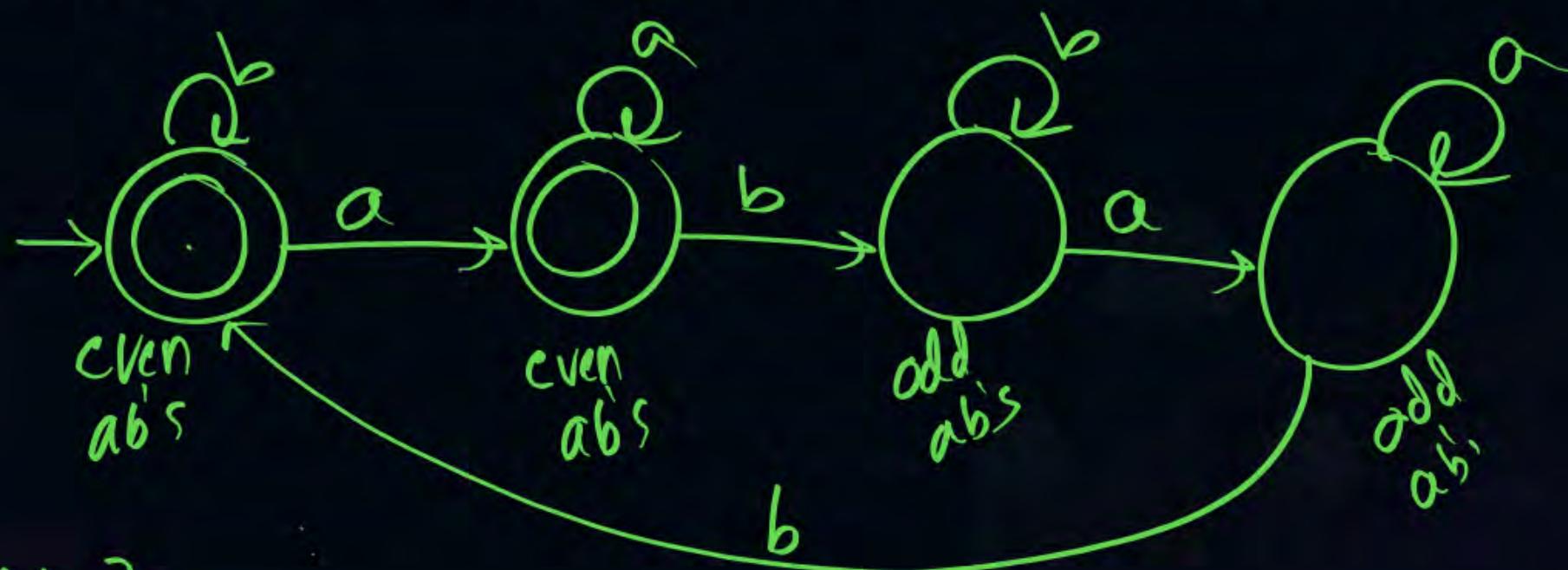
$$x = 0$$

$$y = 2$$

$$z = 2$$

$$xy + z$$

$$0 + 2 = 2,$$



$$L = \{ \check{\epsilon}, \check{a}, \check{b}, \check{aa}, \cancel{\check{ab}}, \cancel{\check{ba}}, \check{bb}, \check{aaa}, \cancel{\check{aab}}, \dots \}$$

$$= \{ w \mid n_{ab}(w) = \text{even} \}$$

$$\underbrace{\#_{ab}(w) = \text{even}}$$

$$= 0, 2, 4, 6, 8, \dots$$

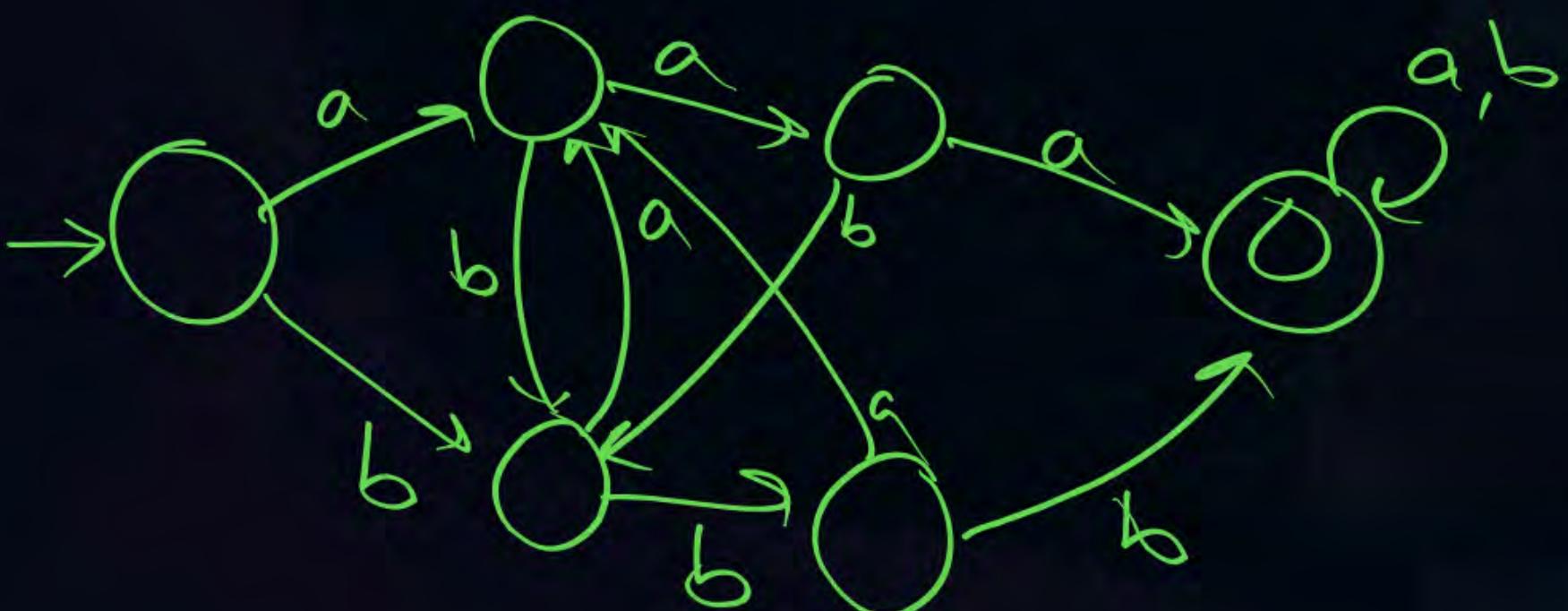


## Regular Languages : NAT

- Q38. How many minimal states are needed to design a DFA that accepts language  
(a) over  $\Sigma = \{a, b\}$ . Where each string contains “aaa or bbb” as a substring? \_\_\_\_

$$L = \{aaa, bbb, \dots\}$$

= 6 //

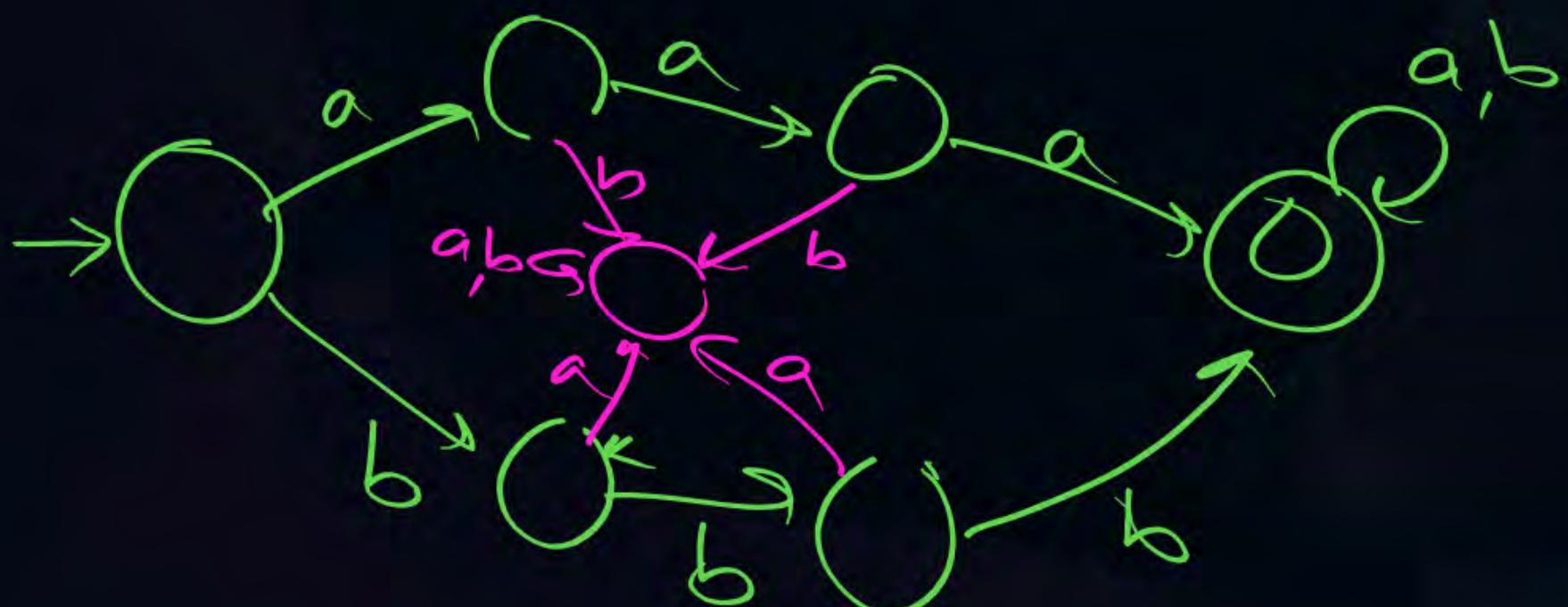




## Regular Languages : NAT

- Q38. How many minimal states are needed to design a DFA that accepts language  
(b) over  $\Sigma = \{a, b\}$ . Where each string ~~contains~~ "aaa or bbb" as a substring? \_\_\_\_\_  
starts with

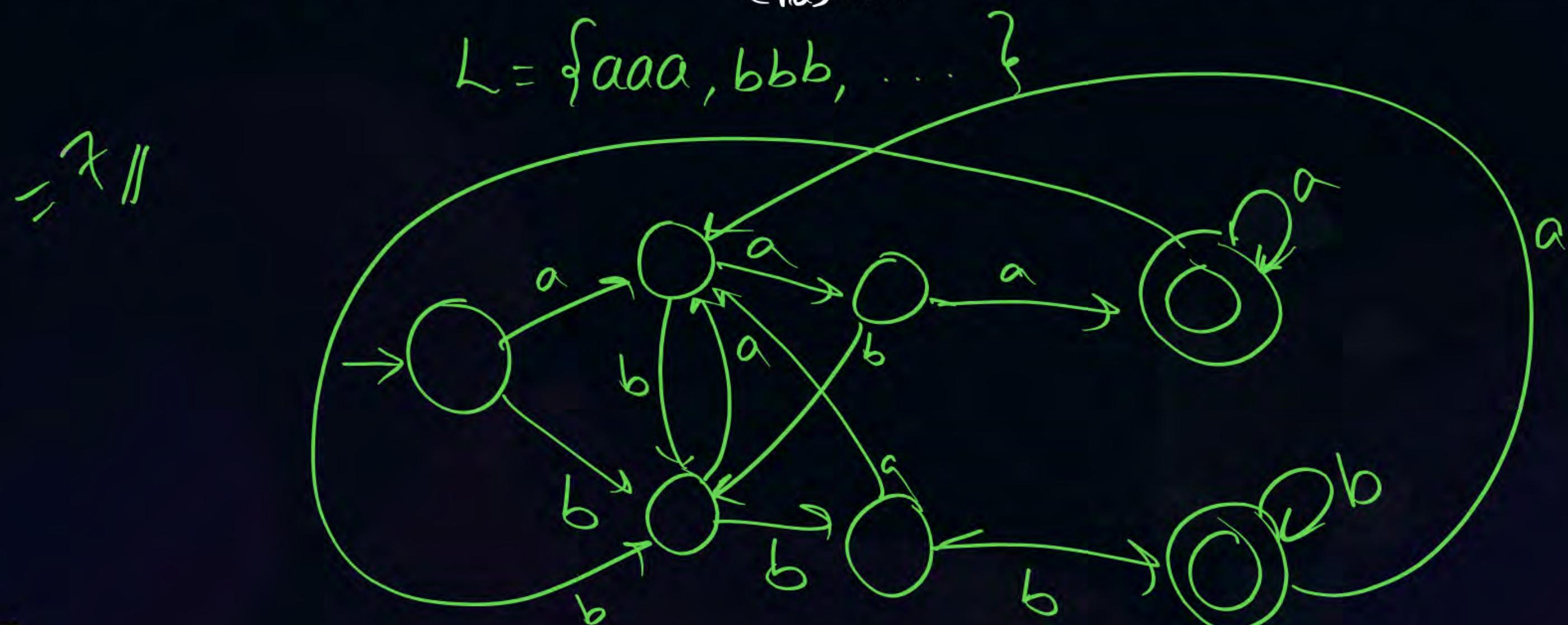
$= \lambda''$





## Regular Languages : NAT

- Q38. How many minimal states are needed to design a DFA that accepts language  
(C) over  $\Sigma = \{a, b\}$ . Where each string ~~contains~~ <sup>ends with</sup> "aaa or bbb" as a substring? \_\_





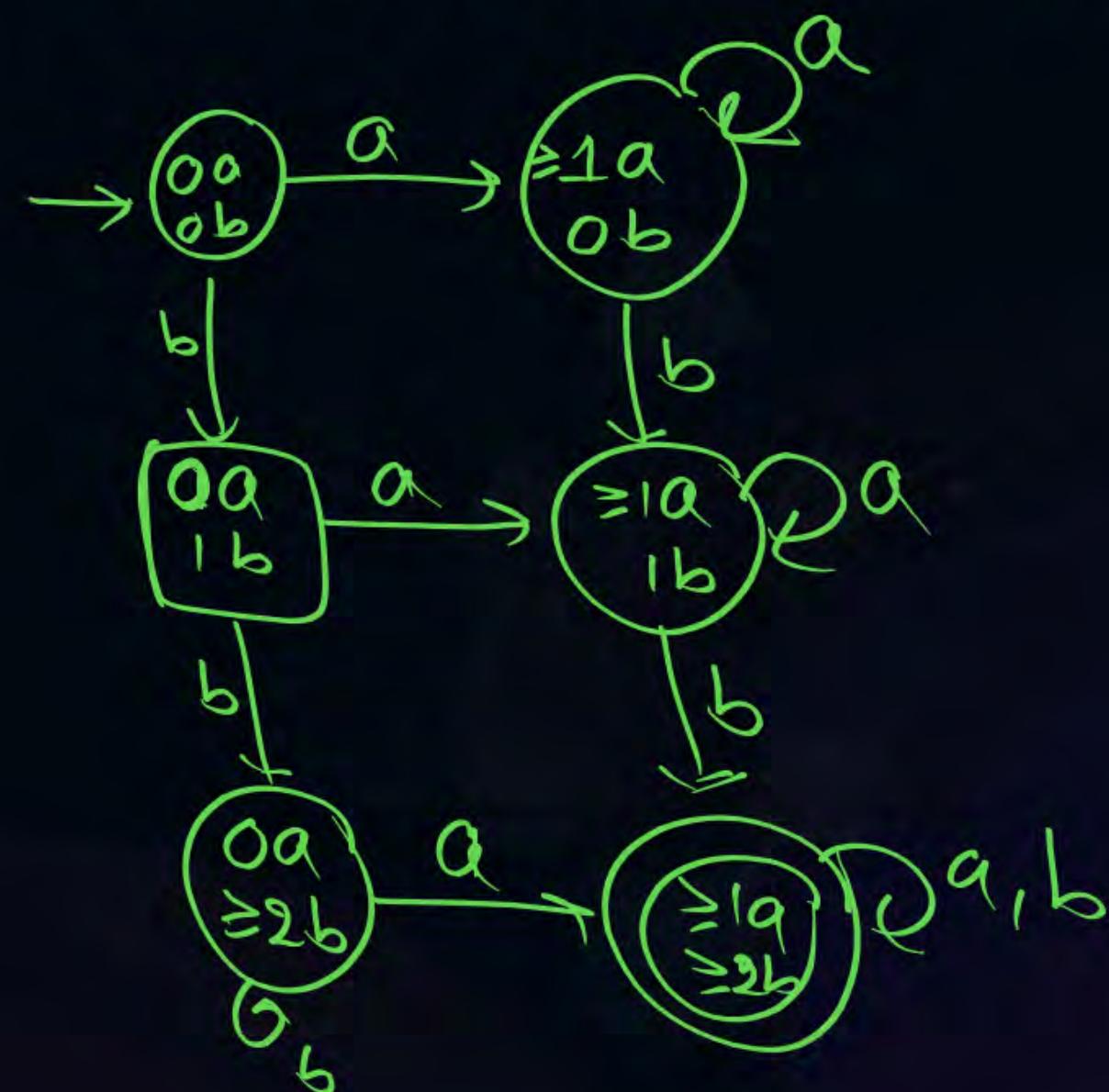
## Regular Languages : NAT

Q39. Consider the language ( $L$ ) over  $\Sigma = \{a, b\}$  if number of a's in a string ~~are~~ is at least 1  
 and number of b's in a string ~~are~~ is at least 2 then total number of states in a  
 minimal DFA is \_\_\_\_\_

$$\begin{array}{l} \#a's \geq 1 \\ \#b's \geq 2 \end{array}$$

$$L = \{abb, bab, bba, \dots\}$$

$$= 6 //$$



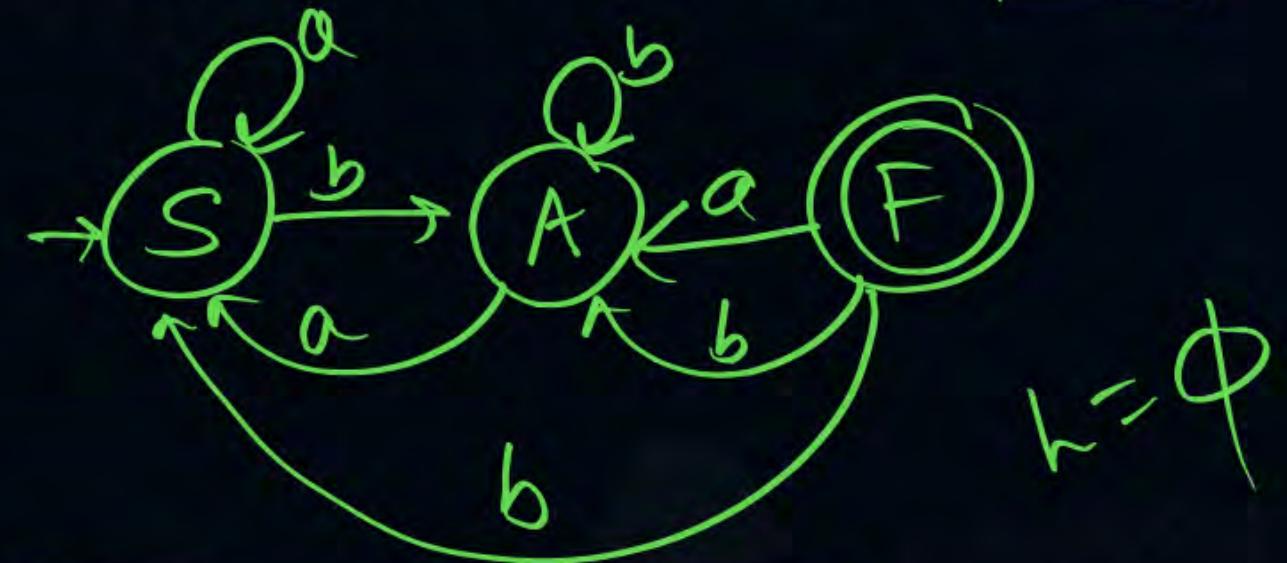


## Regular Languages : MCQ

Q40. Consider the following transition table (T) on input alphabet  $\{a, b\}$  for NFA.

T:

$\delta$	a	b
$\rightarrow S$	{S}	{A}
A	{S}	{A}
*F	{A}	{S,A}



How many states are needed to design equivalent minimal DFA for above NFA?

**A**

4

**C**

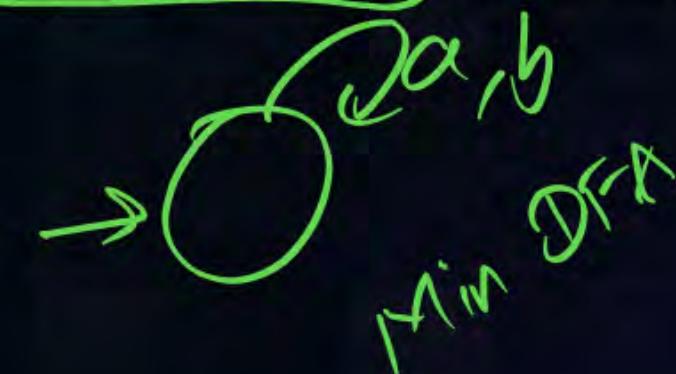
2

**B**

1

**D**

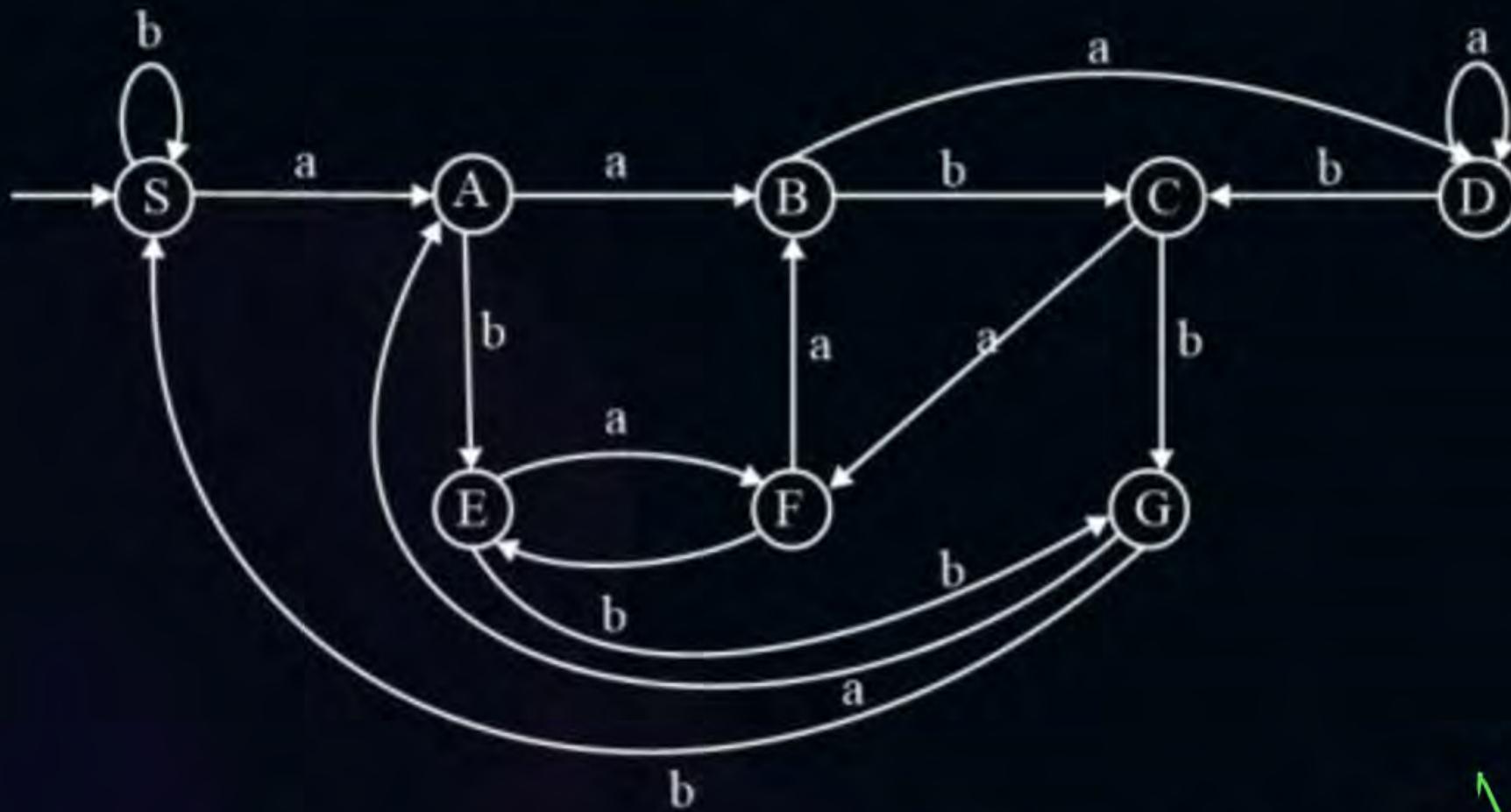
3





## Regular Languages : NAT

Q41. Consider the following DFA.



How many states are possible in minimal DFA? 7



## Regular Languages : MSQ



Q42. Which of the following is/are correct?

A  $(r + \epsilon)^* = r^*$

$$(r + \epsilon)^* = r^*$$

B  $\epsilon \cdot (r^* s^*)^* \cdot (rs + \epsilon) \cdot (r + s)^* + s^* r^* = (r + s)^*$

$$\epsilon \cdot (r^* s^*)^* \cdot (rs + \epsilon) \cdot (r + s)^* + s^* r^* = (r + s)^*$$

C  $\epsilon + rss^* + \cancel{rss^*} (r + s)^* = (rss^*)^*$

$$\epsilon + rss^* + \cancel{rss^*} (r + s)^* = (rss^*)^*$$

D  $(r^* s^*)^+ = (r^+ s^+)^*$

$$(r^* s^*)^+ = (r^+ s^+)^*$$

✓ ✗

$$\epsilon \cdot \epsilon \cdot (r+s)^* + \text{Any} = (r+s)^*$$

$$(rss^*)^*$$
  
$$(rs^*)^*$$
  
$$(rs^*)^*$$

$$\left(\gamma^* \zeta^*\right)^+ = \left\{ \underbrace{\left(\gamma^0 \zeta^0\right)}_{\epsilon}, \underbrace{\left(\gamma^1 \zeta^0\right)}_{\gamma}, \underbrace{\left(\gamma^0 \zeta^1\right)}_{\zeta}, \dots \right\}$$

$$\left(\gamma^+ \zeta^+\right)^* = \left\{ \epsilon, \gamma\zeta, \gamma\gamma\zeta, \gamma\zeta\zeta, \gamma\zeta\gamma\zeta, \dots \right\}$$

$$\boxed{\gamma + \epsilon \neq \gamma}$$

$$\boxed{\gamma \cdot \epsilon = \gamma}$$



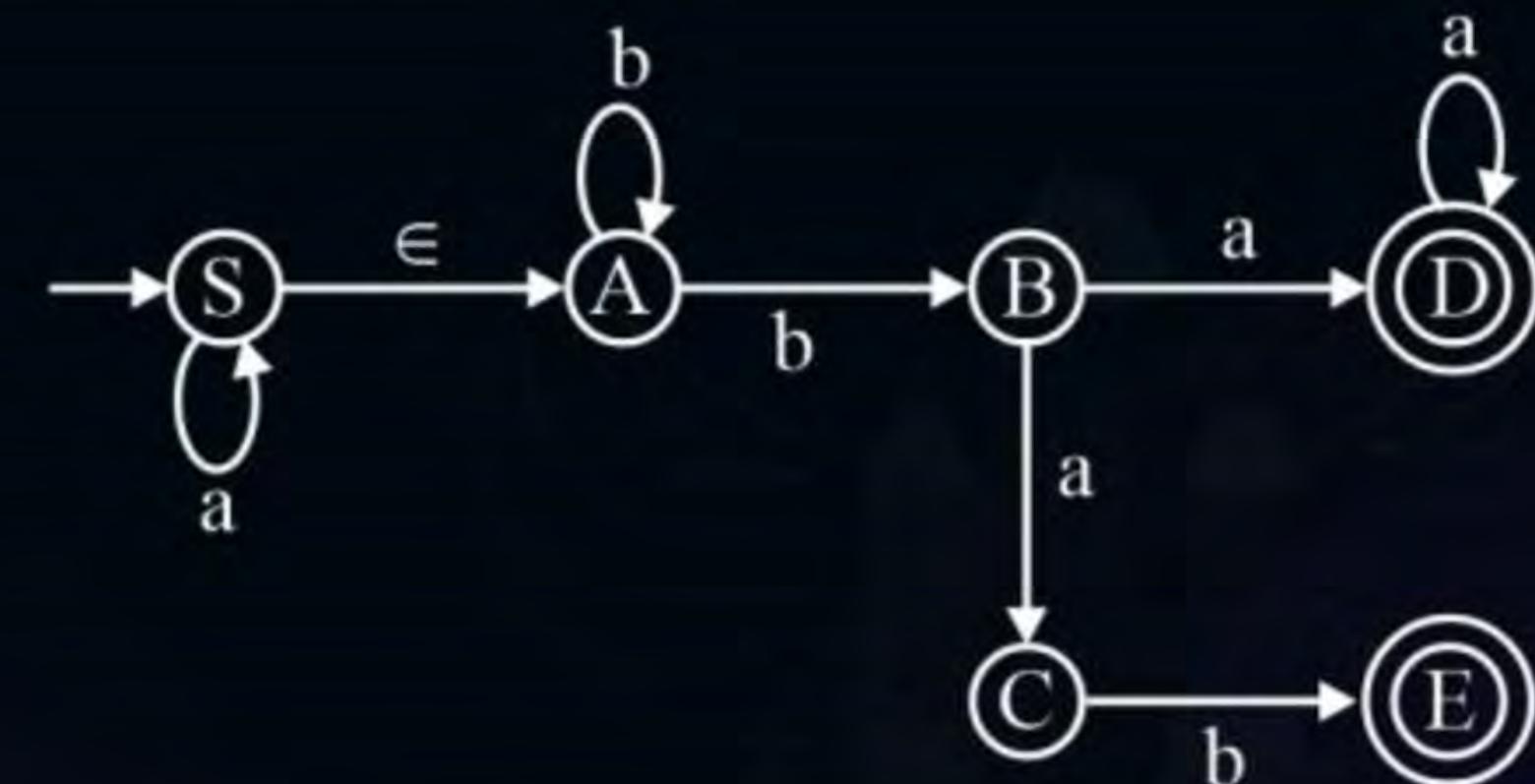
## Regular Languages : MSQ



Q43. Consider the following  $\epsilon$ -NFA:

Which of the following strings are accepted?

- A** abab
- B** baab
- C** bbaa
- D** abaa





## Regular Languages : MCQ

P  
W

[MCQ]

Q44. let L be the set of all the languages accepted by all grammars where every production is in the form of  $V \rightarrow VT^*$  or  $V \rightarrow T^*$ .

Let Q be the set of all languages accepted by all grammars where every production of grammar is in the form of  $V \rightarrow T^*V$  or  $V \rightarrow T^*$

Which of the following is correct?

(Note: T is terminals and V is non-terminals)

A

$$L \geq Q$$

C

$$L = Q$$

B

$$L \leq Q$$

D

$$L \neq Q$$



## Regular Languages : MSQ



Q45. Consider the following grammar G:

$$G: \quad S \rightarrow aS \mid bS \mid aaS \mid bbS \mid a$$

Which of the following is correct regular expression for above grammar G?

A

$$(a + b)^* a$$

B

$$(a + b + aa + bb)^* a$$

C

$$(a + b + aa + bb + ba)^* a$$

D

None of these

# THANK - YOU

# CS & IT ENGINEERING

## Theory of Computation

Lecture No.- 04

Mallesham Devasane Sir



# Topics to be Covered



Topic

Regular Expression

Topic

Finite Automata

Topic

Regular Grammar

Topic

Closure Properties



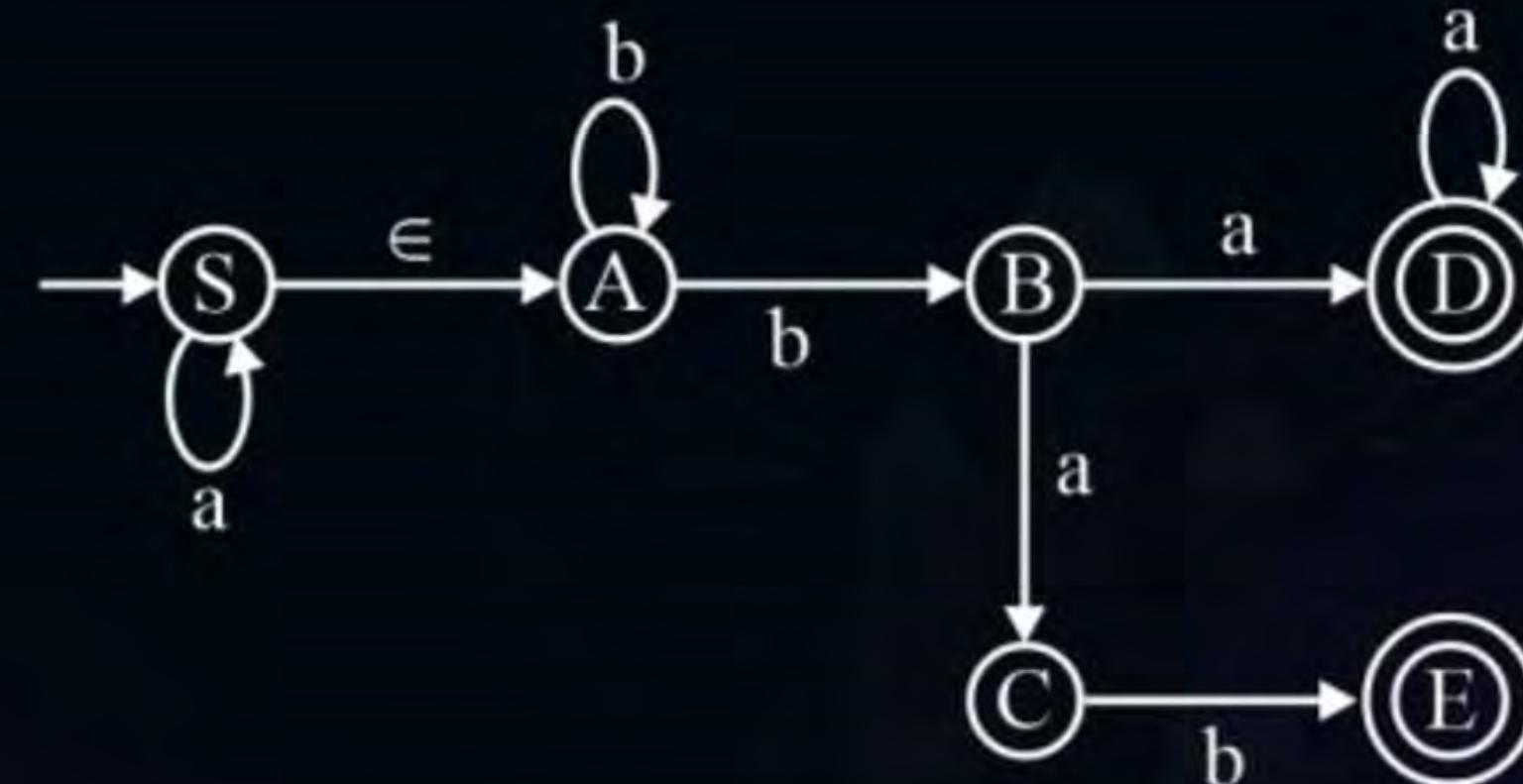
## Regular Languages : MSQ



Q43. Consider the following  $\epsilon$ -NFA:

Which of the following strings are accepted?

- A** abab ✓  $a \epsilon b a b$
- B** baab
- C** bbaa ✓  $\epsilon b b a a$
- D** abaa ✓  $a \epsilon b a a$





## Regular Languages : MCQ

$L = \text{Set of all languages generated by LLGs}$

[MCQ]

Q44. let L be the set of all the languages accepted by all grammars where every production is in the form of  $V \rightarrow VT^*$  or  $V \rightarrow T^*$ .

Let Q be the set of all languages accepted by all grammars where every production of grammar is in the form of  $V \rightarrow T^*V$  or  $V \rightarrow T^*$

Which of the following is correct?

(Note: T is terminals and V is non-terminals)

$Q = \text{Set of all language generated by RLGs}$

A

$L \geq Q$

B

$L \leq Q$

$L_s(LLGs) = L$

C

$L = Q$

D

$L \neq Q$

$L_s(RLGs) = Q$

$L = Q = \text{Set of all regular languages}$

$L = Q$



## Regular Languages : MSQ



Q45. Consider the following grammar G:

$$G: \quad S \rightarrow aS \mid bS \mid \cancel{aaS} \mid \cancel{bbS} \mid a \quad (a+b)^* a$$

Which of the following is correct regular expression for above grammar G?

A

$$(a + b)^* a$$

B

$$(a + b + \cancel{aa} + \cancel{bb})^* a = (a+b)^* a$$

C

$$(a + b + aa + bb + \cancel{ba})^* a = (a+b)^* a$$

D

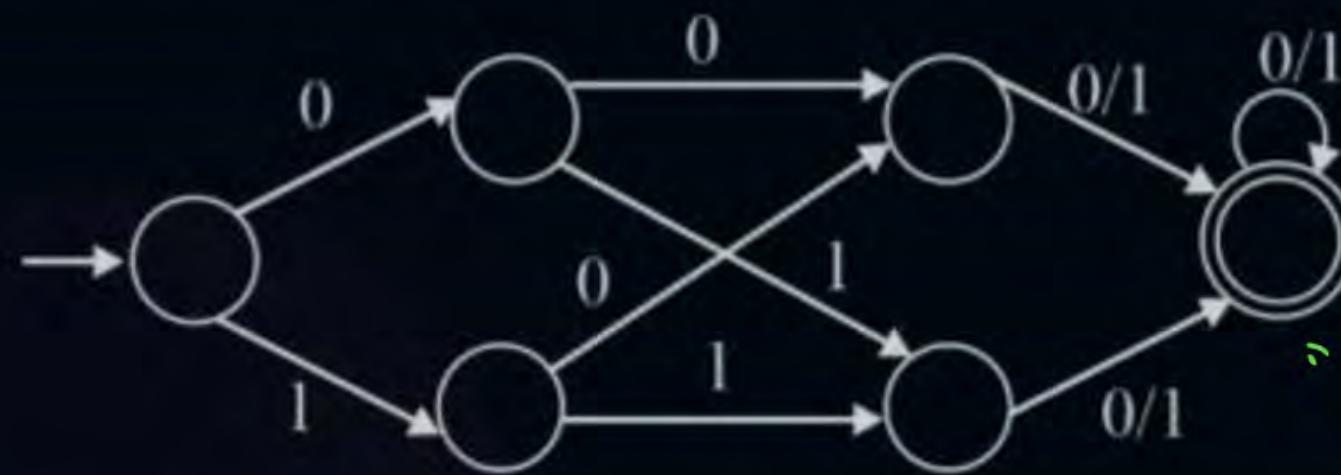
None of these



## Regular Languages : MCQ



Q46. Consider the following deterministic finite automaton (DFA).



000  
001  
010  
011  
100  
101  
110  
111 } 8 strings

The number of strings of length 3 accepted by the above automaton is \_\_\_\_.

A

2

C

6

B

4

D

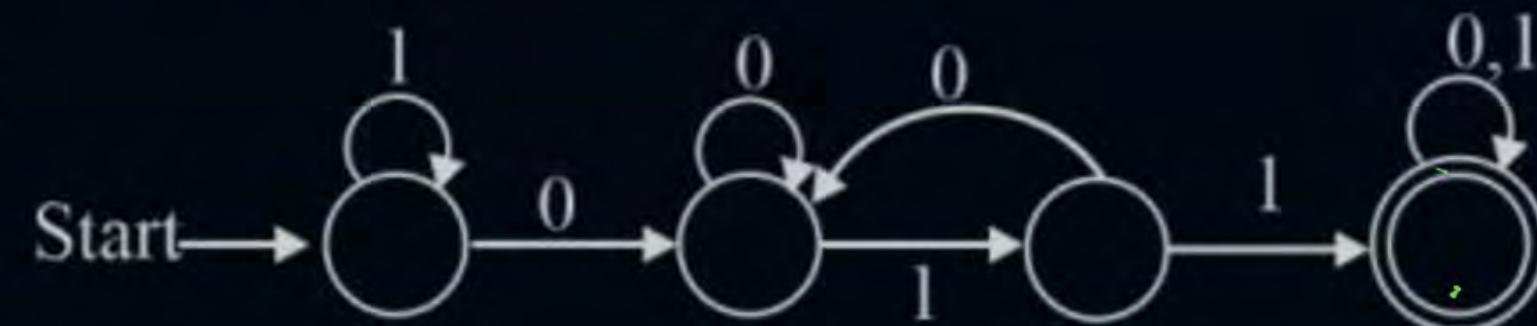
8



## Regular Languages : MCQ



Q47. Consider the following DFA.



Which one of the following language L accepted by above DFA?

A

$L = \{w \in \{0, 1\}^* \mid w \text{ ends with } 011\}$

B

$L = \{w \in \{0, 1\}^* \mid w \text{ starts with } 011\}$

C

$L = \{w \in \{0, 1\}^* \mid w \text{ has substring } 011\}$

D

$L = \{w \in \{0, 1\}^* \mid w \text{ ends with } 11\}$

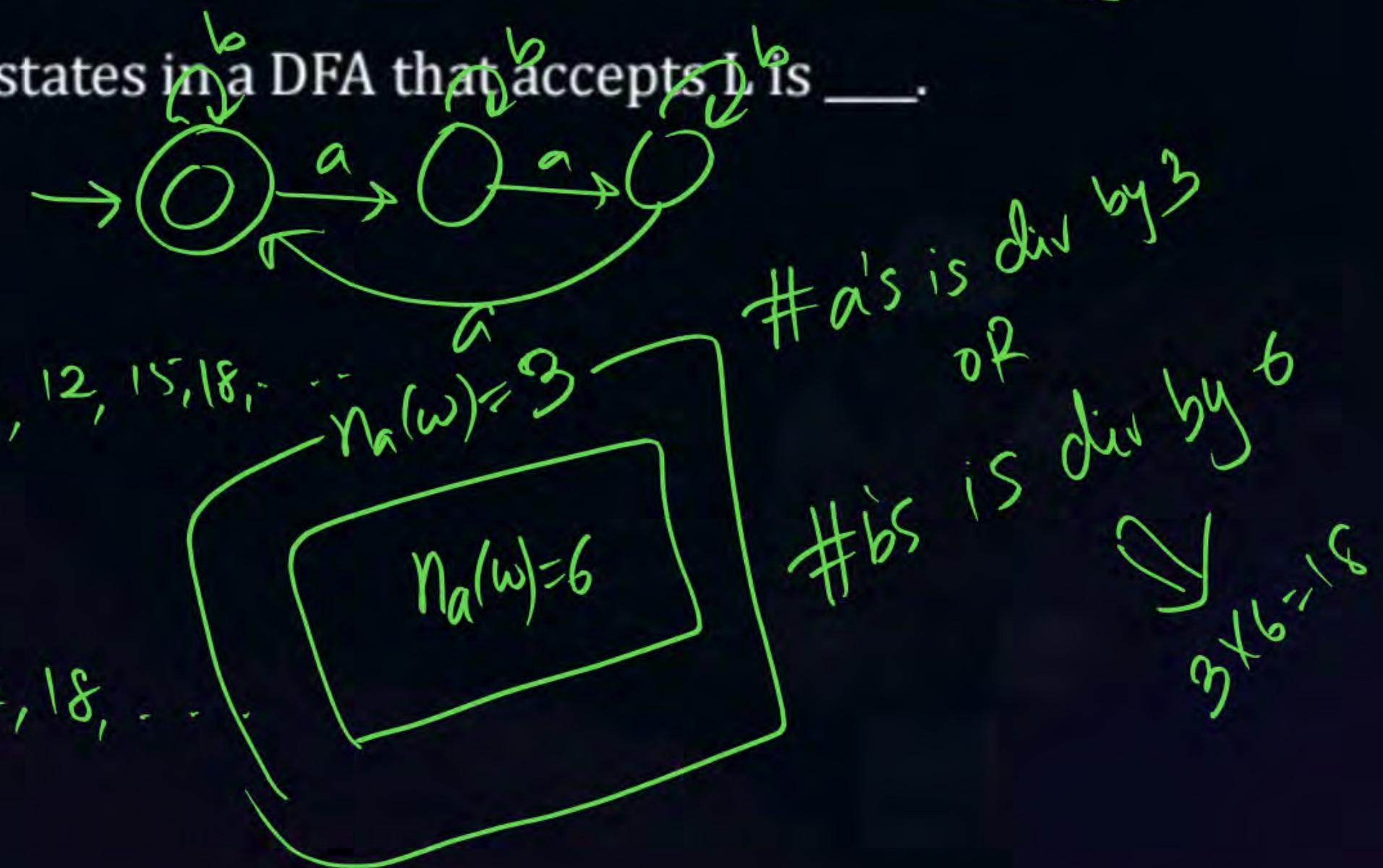


## Regular Languages : MSQ

Q48. Consider the following language:

$$L = \{x \mid x \in \{a, b\}^*, \text{ number of } a's \text{ in } x \text{ is } \boxed{\text{divisible by 3 or divisible by 6}}\}$$

The minimum number of states in a DFA that accepts  $L$  is \_\_\_\_.





## Regular Languages : NAT



Q49. Consider the following statements:

- I. If  $L_1 \cup L_2$  is regular, then both  $L_1$  and  $L_2$  must be regular.  $\rightarrow F$
- II. If  $L_1 \cap L_2$  is regular, then both  $L_1$  and  $L_2$  must be regular.  $\rightarrow F$
- III. If Complement of  $L$  is regular, then  $L$  must be regular.  $\rightarrow \text{True}$
- IV. If  $L_1 - L_2$  is regular, then both  $L_1$  and  $L_2$  must be regular.  $\rightarrow \text{False}$
- V. If  $L^*$  is regular, then  $L$  must be regular.  $\rightarrow \text{False}$

How many of above statements are FALSE?

- 4 /

$L^*$  is Reg

$\{a^{\text{prime}}\}^*$  is Reg

$\sqcup$   
 $L$  need not be Reg

If  
 $a^{\text{prime}}$  is not reg

$L_1 - L_2$  is Reg

↓

$L_1$  and  $L_2$  need not be Regular

$$a^n b^n - a^n b \supseteq \phi$$

$L_1 \cap L_2 = \text{Regular}$



$L_1$  and  $L_2$  need not be Regular

$$a^n b^n \cap b^n a^n \Rightarrow \text{Reg}$$

q.e.d.

If  $L_1 \cup L_2$  is Regular then  $L_1$  need not be reg  
 $L_2$  need not be reg

$$\{a^n b^n\} \cup \overline{\{a^n b^n\}} \Rightarrow \text{Regular}$$
$$(a+b)^*$$

$$\boxed{L \cup \bar{L} = \Sigma^*}$$



## Regular Languages : MCQ

$$\Sigma = \{f_1, f_2\}$$

Q50. Let  $\Sigma$  be the set of all bijections from  $\{1, 2\}$  to  $\{1, 2\}$ , where  $id$  denotes the identity function, i.e.  $id(j) = j, \forall j$ .

Let  $\circ$  denote composition on functions.

For a string  $x = x_1 x_2 \dots x_n \in \Sigma^n$ ,  $n \geq 0$ , let  $\underline{\pi(x)} = x_1 \circ x_2 \circ \dots \circ x_n$ .

Consider the language  $L = \{x \in \Sigma^* \mid \pi(x) = id\}$ .

The minimum number of states in any DFA accepting  $L$  is \_\_\_\_.

Identity Function ✓

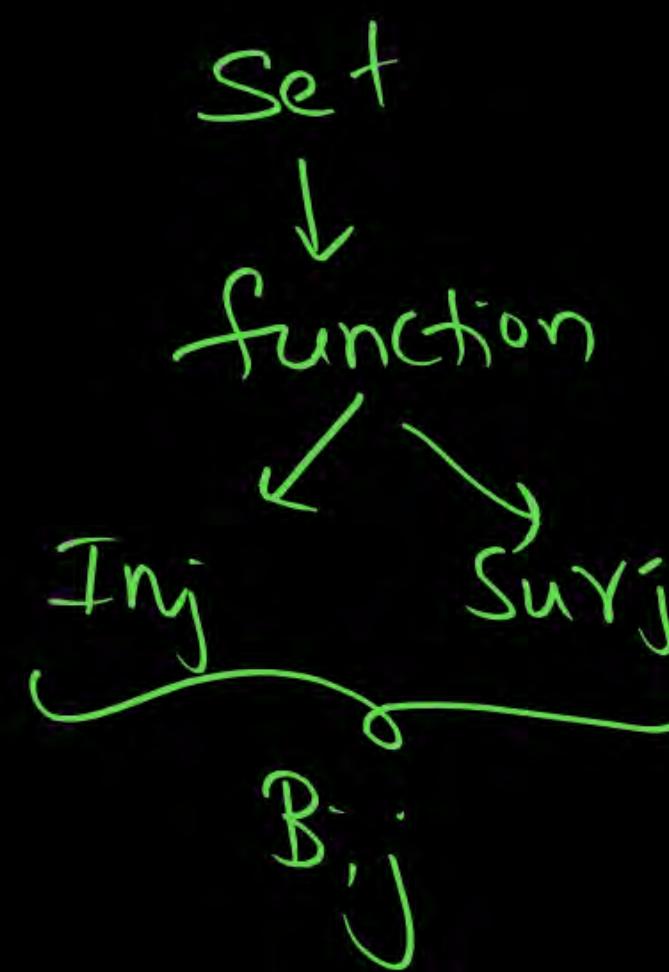
Bijective Function ✓

Composition .

$$L = \left\{ x \mid \pi(x) = id \right\}$$

PW  
Bijective Function : [one to one correspondence]

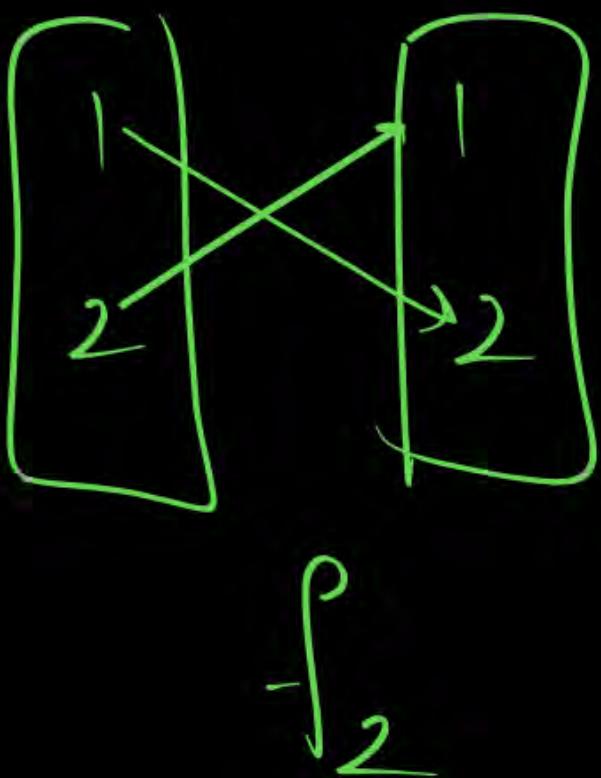
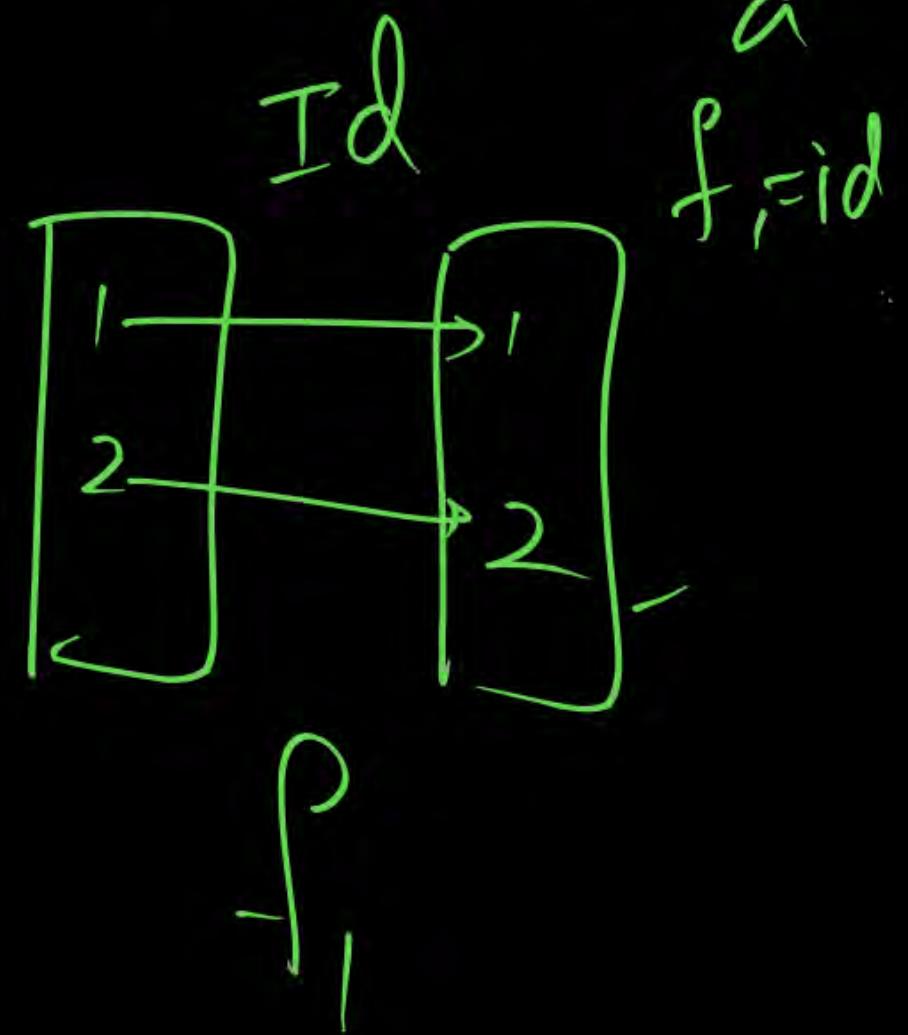
It is Injective & Surjective  
One to one func  
onto func



$$\Sigma = \{ \boxed{f_1}^{\text{id}}, f_2 \} = \{a, b\}$$

$$\Sigma^* = \{ \epsilon, f_1, f_2, f_1 f_1, f_1 f_2, f_2 f_1, f_2 f_2, \dots \}$$

$a$        $b$        $a a$        $a b$        $b a$        $b b$



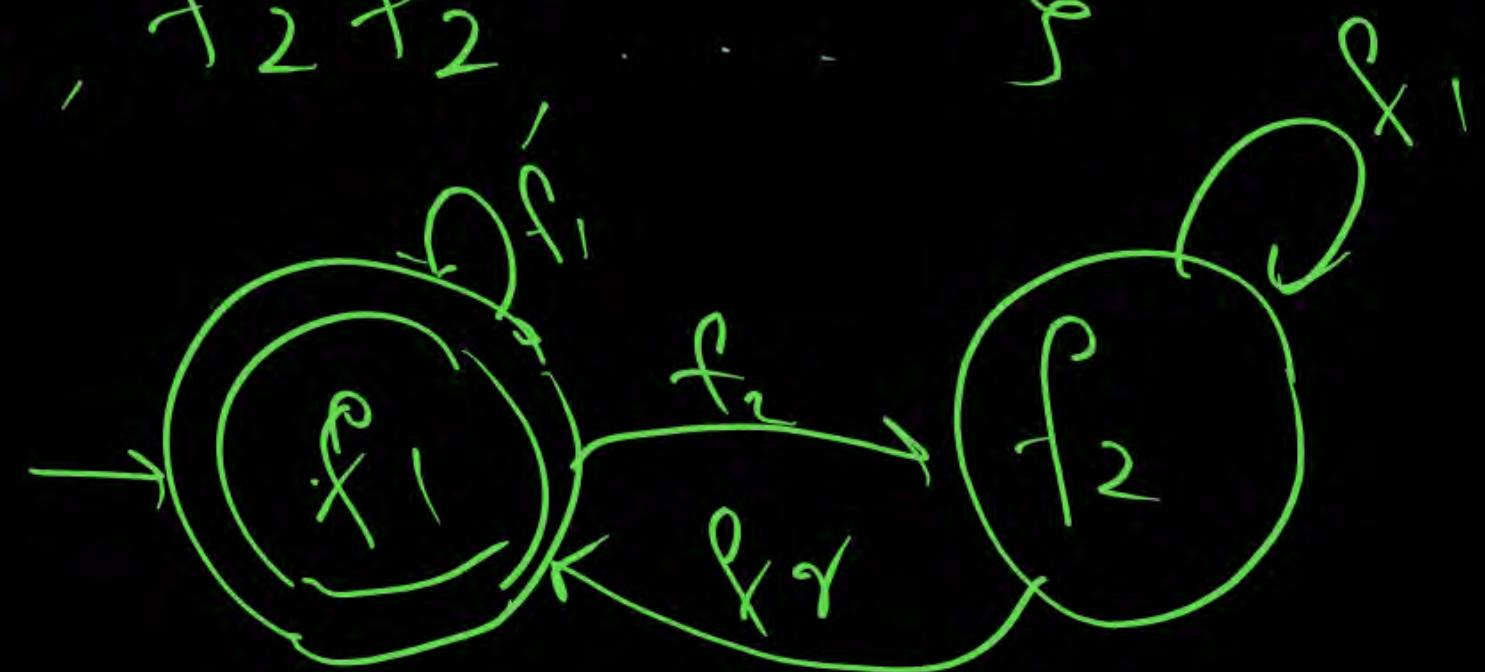
$$\Sigma = \{ f_1, f_2 \} \quad \{ = \{a, b\}$$



$$\Sigma^* = \{ \epsilon, f_1, f_1 f_1, f_1 f_2, f_2 f_1, f_2 f_2, f_1 f_1 f_1, f_1 f_1 f_2, f_1 f_2 f_1, f_1 f_2 f_2, \dots \}$$

$$L = \{ \underbrace{\epsilon}_{\text{choice}}, f_1, f_1 f_1, f_1 f_2, f_2 f_1, f_2 f_2, \dots \}$$

$$\pi(f_1) = \text{id}$$





## Regular Languages : MSQ



Q51. If  $L$  is a regular language over  $\Sigma = \{a, b\}$ , which one of the following languages is TRUE?

- A  $\{xy \mid x \in L, y^R \in L\}$  is Regular       $L \cdot L^R$  is Reg  
*yel<sup>R</sup>*
- B  $\{y \in \Sigma^* \mid \exists x \in \Sigma^* \text{ such that } xy \in L\}$  is Regular      Suffix( $L$ )
- C  $\{x \in \Sigma^* \mid \exists y \in \Sigma^* \text{ such that } xy \in L\}$  is Regular      Prefix( $L$ )
- D  $\{ww^R \mid w \in L\}$  is Regular      is FALSE

$$\text{Suffix}(L) = \{ y \mid xy \in L, x \in \Sigma^* \}$$

$$= \{ y \in \Sigma^* \mid \exists x \in \Sigma^* \quad xy \in L \}$$

$$\text{Prefix}(L) = \{ x \mid xy \in L, y \in \Sigma^* \}$$

$$\{xy \mid x \in L, y^R \in L\} = \{xy \in LL^R\}$$

$$\{xy \mid x \in L, y \in L^R\}$$

$$L \cdot L^R$$

Given  $L$  is Reg }  
 $L^R$  is also Reg } }  $L \cdot L^R$  is Reg

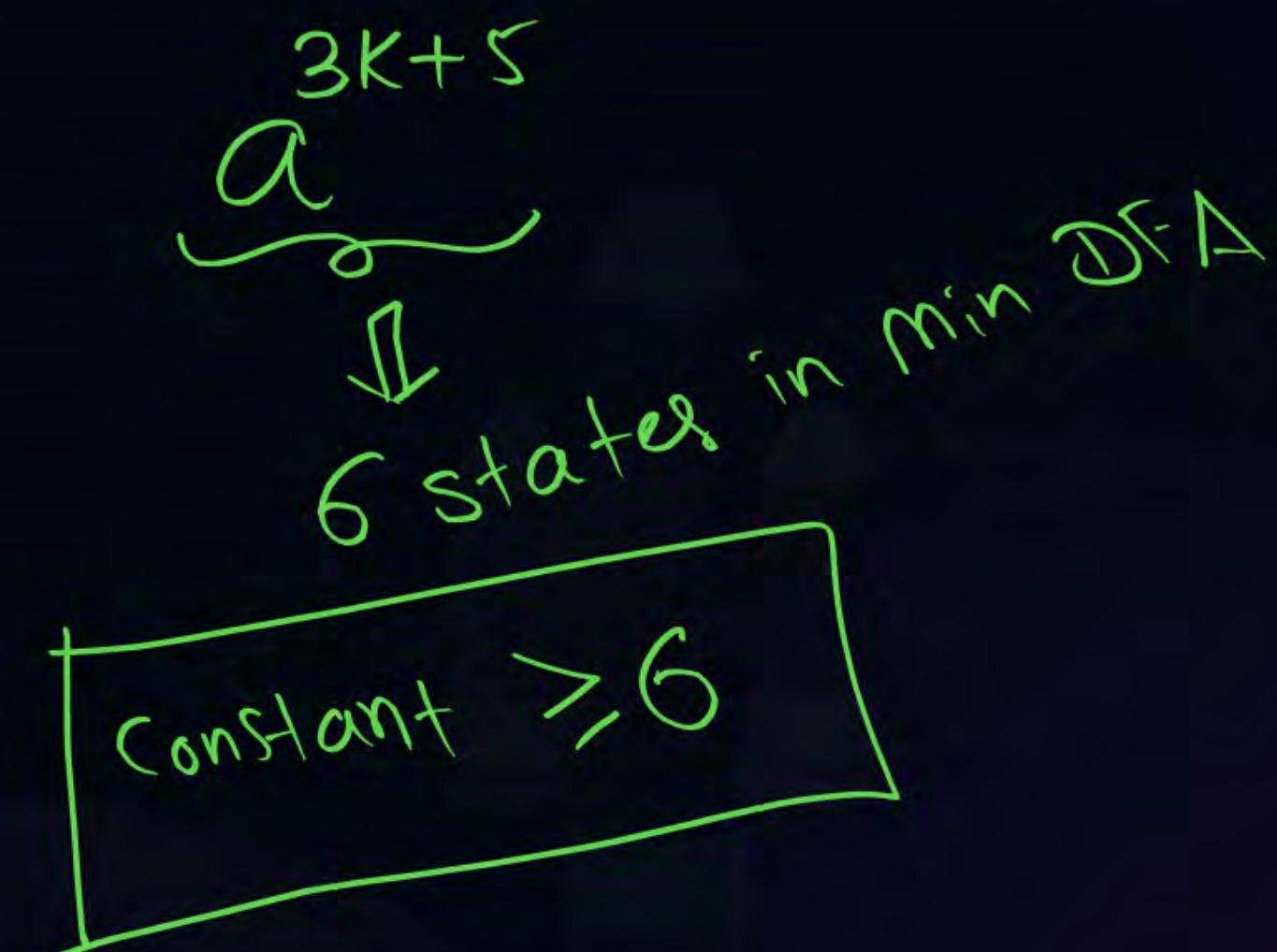


## Regular Languages : ~~NAT~~ MCQ



Q52. For  $\Sigma = \{a, b\}$ , let us consider the regular language  $L = \{x \mid x = a^{5+3k}, k \geq 0\}$ . Which one of the following can be a pumping length (the constant guaranteed by the pumping lemma) for L?

- A 5
- B 3
- C 7
- D 4





# Regular Languages : NAT



Q53. Given a language  $L$ , define  $L^i$  as follows:

$$\begin{cases} L^0 = \{\epsilon\} \\ L^i = L^{i-1} \cdot L \text{ for all } i > 0 \end{cases}$$

The order of a language  $L$  is defined as the smallest  $k$  such that  $L^k = L^{k-1}$ .

Consider the language  $L_1$  (over alphabet 0) accepted by the following FA.

$$L^0 = \{\epsilon\}$$

$$L^1 = L^0 \cdot L = L = \epsilon + 0(00)^*$$

$$L^2 = L^1 \cdot L = (\epsilon + 0(00)^*) \cdot (\epsilon + 0(00)^*) = 0(00)^*$$

$$L^3 = L^2 \cdot L = 0^* \cdot L = 0^*$$

The order of  $L_1$  is \_\_\_\_.



$$L^3 = L^2$$

$$\boxed{L^3 = L^2} \quad \text{for smst} \quad L = \epsilon + 0(00)^*$$

*TOL & Palgo*

$$\begin{array}{l} L^0 \\ \times L^1 = L^0 \quad k=1 \\ \times L^2 = L^1 \quad k=2 \\ \times L^3 = L^2 \quad k=3 \end{array}$$

$\boxed{-3}$

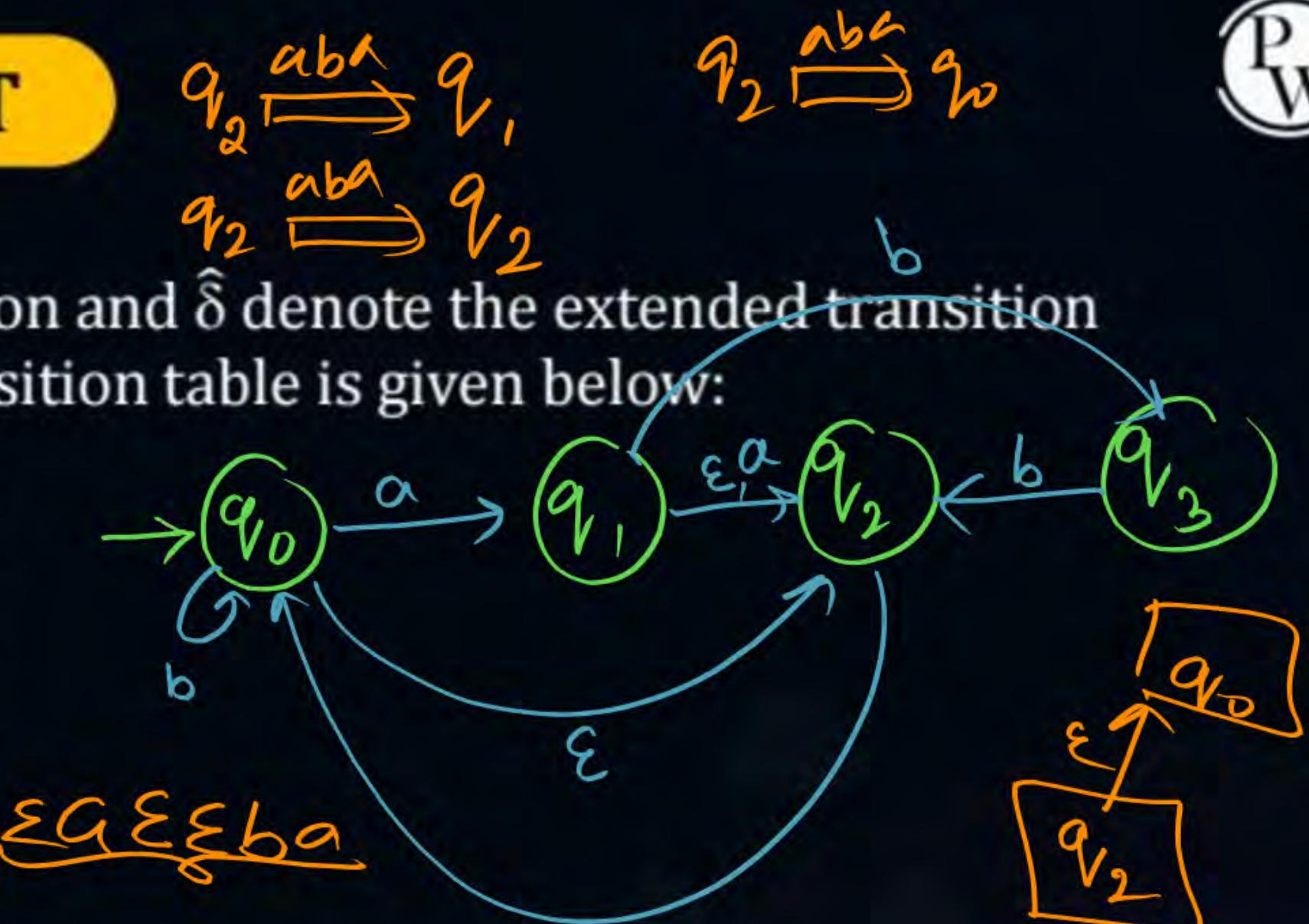


## Regular Languages : NAT

P  
W

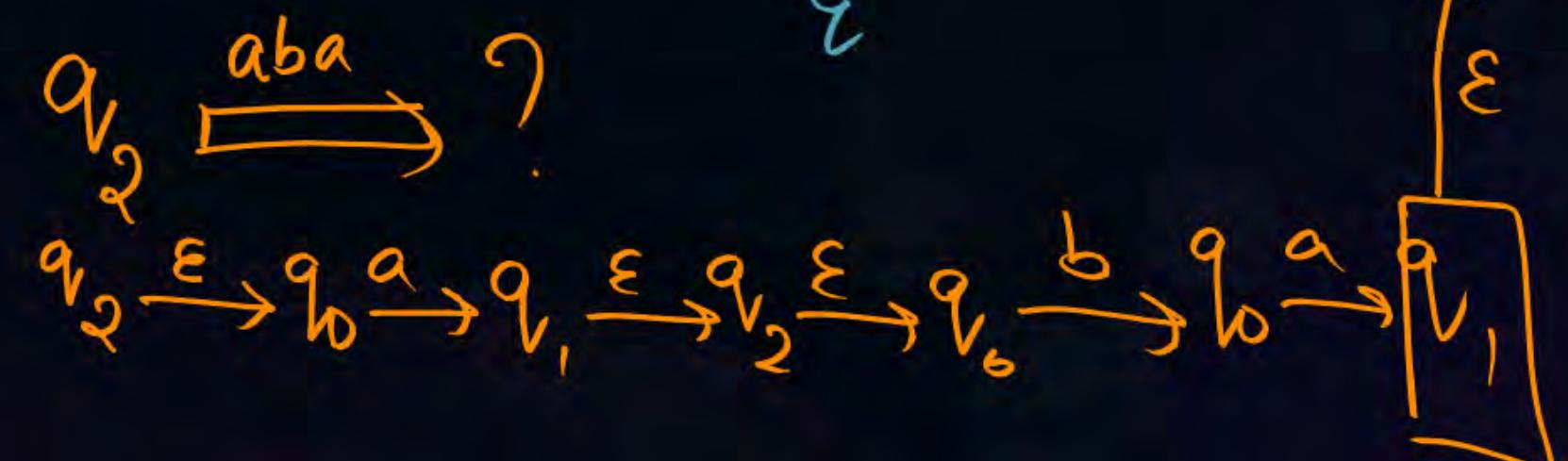
- Q54. Let  $\delta$  denote the transition function and  $\hat{\delta}$  denote the extended transition function of the  $\epsilon$ -NFA whose transition table is given below:

$\delta$	$\epsilon$	a	b
$\rightarrow q_0$	{ $q_2$ }	{ $q_1$ }	{ $q_0$ }
$q_1$	{ $q_2$ }	{ $q_2$ }	{ $q_3$ }
$q_2$	{ $q_0$ }	$\phi$	$\phi$
$q_3$	$\phi$	$\phi$	{ $q_2$ }



Then  $|\hat{\delta}(q_2, aba)|$  is \_\_\_\_\_

$$|\{q_1, q_2, q_0\}| = 3$$

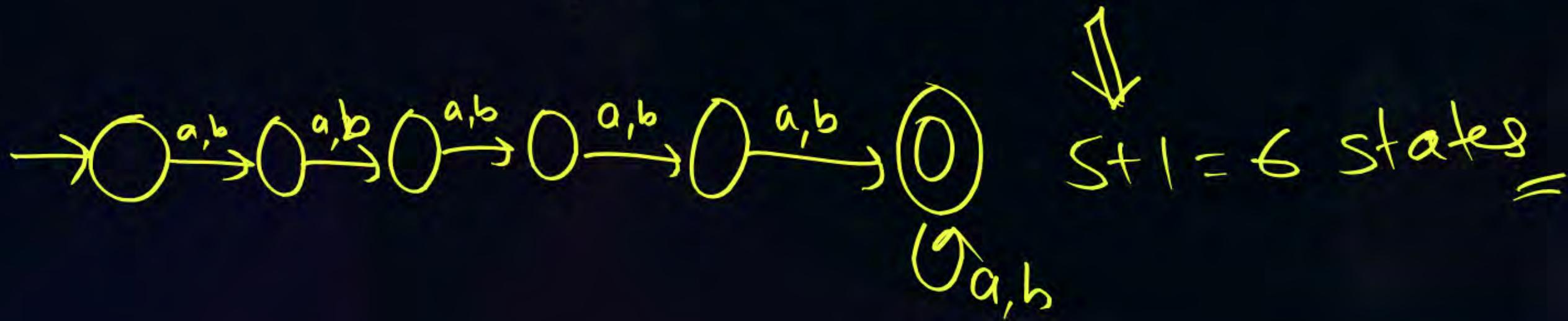


 Regular Exp & FA : NAT

- Q55. Find the minimum possible number of states of a DFA that accepts the regular language  $L = \{w_1 w_2 \mid w_1, w_2 \in \{a, b\}^*, |w_1| \geq 2, |w_2| \geq 3\}$  is \_\_\_\_.

$$\begin{array}{c} \overbrace{\textcircled{a}}^{\geq 2} \quad \overbrace{\textcircled{b}}^{\geq 3} \\ \xrightarrow{\hspace{1cm}} \textcircled{a} \\ \geq 5 \end{array}$$

$$\{w \mid w \in \{a, b\}^*, |w| \geq 5\}$$





## Regular Languages : NAT



Q56. If G is a grammar with productions

$$S \rightarrow Sa \mid Sb \mid Saa$$

where S is the start variable, then which one of the following strings is not generated by G?

- A** abab
- B** aaab
- C** abbaa
- D** babba



## Regular Languages : NAT



Q57. How many of the following languages are regular?

$L_1 = \{wxw^R \mid w, x \in \{a, b\}^*, w^R \text{ is the reverse of string } w\}$

$L_2 = \{a^n b^m \mid m, n \geq 0\}$

$L_3 = \{a^p b^q c^r \mid p, q, r \geq 0\}$

$L_4 = \{\omega \mid \omega \in \{0,1\}^*, \omega \text{ has equal number of (00)'s and (11)'s}\}.$



## Regular Languages : NAT



Q58. If  $L_1 = \{a^n \mid n \geq 0\}$  and  $L_2 = \{b^n \mid n \geq 0\}$ , then how many of the following statements are TRUE?

- I.  $L_1 \cdot L_2$  is a regular language
- II.  $L_1 / L_2$  is a regular language
- III.  $L_1 \cup L_2$  is a regular language



## Regular Languages : MCQ



Q59. Which one of the following is TRUE?

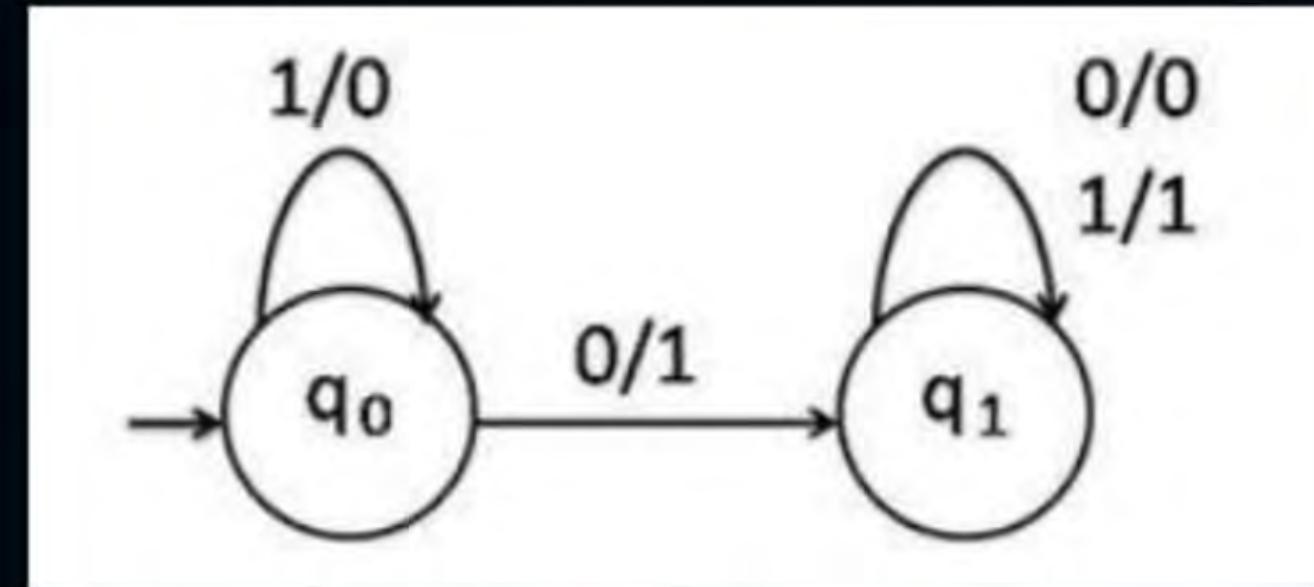
- A** Kleene closure of  $\{a^n b^n \mid n \geq 0\}$  is regular.
- B** Kleene closure of  $\{a^n \mid n \text{ is prime}\}$  is regular.
- C** Kleene closure of  $\{ww \mid w \in \Sigma^* \text{ with } \Sigma = \{0, 1\}\}$  is regular.
- D** Kleene closure of  $\{wxw \mid w, x \in \Sigma^* \text{ with } \Sigma = \{0, 1\}\}$  is regular.



## Regular Languages : NAT

Q60. Consider the following FSM with output. It takes binary input in reverse order of actual binary number and produces binary output. To see actual output, produced output should be considered in reverse. Identify TRUE statement.

- A** It increments given input
- B** It decrements given input
- C** It left shifts given input
- D** It right shifts given input



$$\overbrace{a^n b^n}^{\text{DCFL}} \subset \overbrace{a^* b^*}^{\text{REG}}$$

Set of reg  $\subset$  Set of DCFLs

$$\overbrace{a^n b^n}^{\text{DCFL}} \supset \overbrace{aabb}^{\text{reg}}$$

$$\overbrace{a^*}^{\text{DCFL}} = \overbrace{a^*}^{\text{REG}}$$

# THANK - YOU

# CS & IT ENGINEERING

## Theory of Computation

Lecture No.- 05

Mallesham Devasane Sir



# Topics to be Covered



Topic

Regular Languages

Topic

Context Free Grammars



## Regular Languages : MSQ



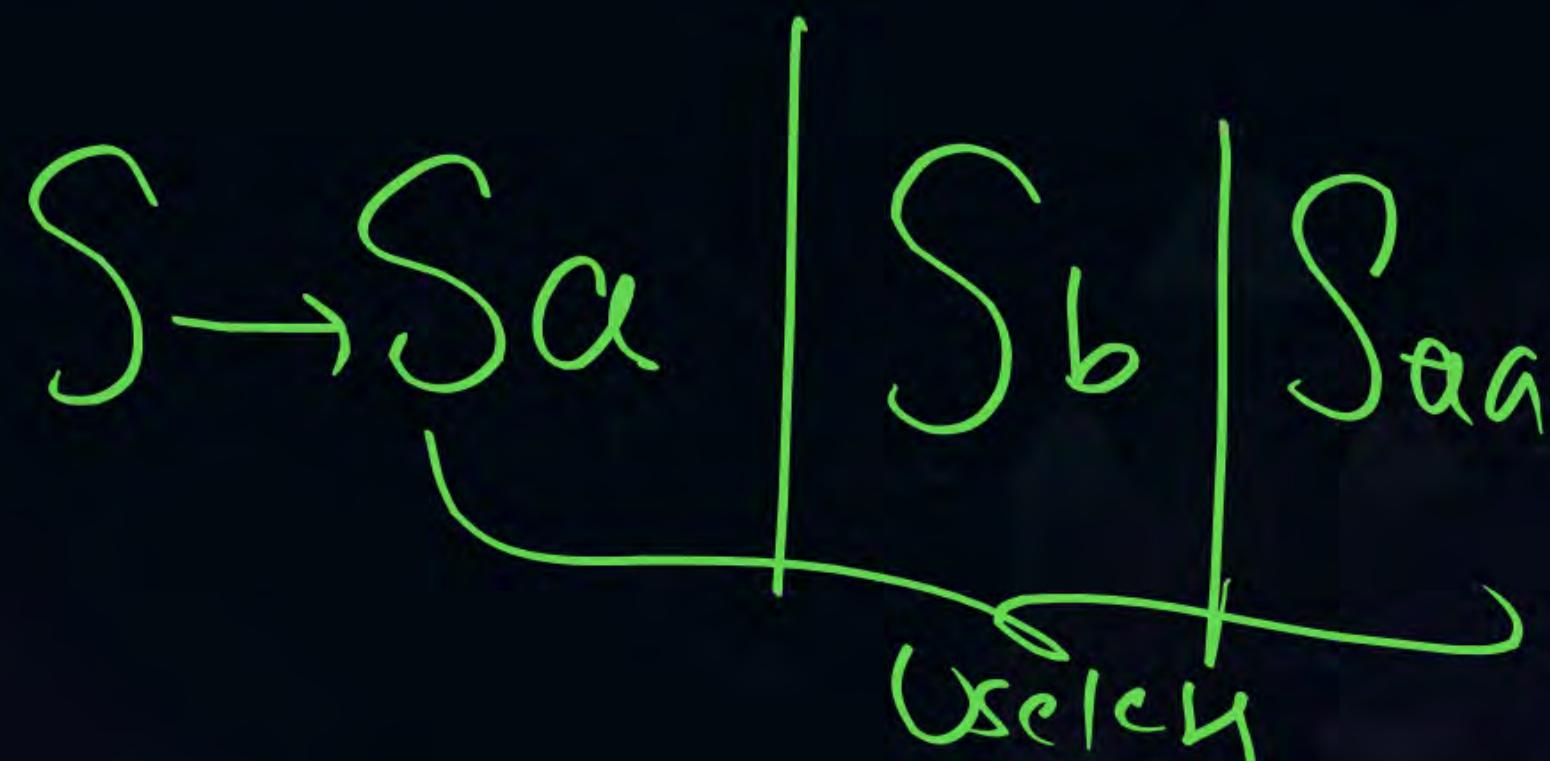
Q56. If G is a grammar with productions

$$S \rightarrow Sa \mid Sb \mid Saa$$

$$L = \emptyset$$

where S is the start variable, then which one of the following strings is **not** generated by G?

- A abab
- B aaab
- C abbaa
- D babba





## Regular Languages : NAT

Q57. How many of the following languages are regular?

Reg  $(a+b)^*$   $\Leftarrow L_1 = \{wxw^R \mid w, x \in \{a, b\}^*, w^R \text{ is the reverse of string } w\}$

Reg  $a^* b^* \Leftarrow L_2 = \{a^n b^m \mid m, n \geq 0\}$

Reg  $a^* b^* c^* \Leftarrow L_3 = \{a^p b^q c^r \mid p, q, r \geq 0\}$

Not Reg  $\Leftarrow L_4 = \{\omega \mid \omega \in \{0,1\}^*, \omega \text{ has equal number of } \underline{00}'\text{s and } \underline{11}'\text{s}\}.$

= 3 //



## Regular Languages : NAT



Q58. If  $L_1 = \{a^n \mid n \geq 0\}$  and  $L_2 = \{b^n \mid n \geq 0\}$ , then how many of the following statements are TRUE?

- I.  $L_1 \cdot L_2$  is a regular language
- II.  $L_1 / L_2$  is a regular language
- III.  $L_1 \cup L_2$  is a regular language

-3 //



## Regular Languages : M~~S~~Q



Q59. Which one of the following is TRUE?



Kleene closure of  $\{a^n b^n \mid n \geq 0\}$  is regular.

$\{a^{n^2}\}^*$  is not reg  
 $\{a^{\text{prime}}\}^*$  is Reg



Kleene closure of  $\{a^n \mid n \text{ is prime}\}$  is regular.



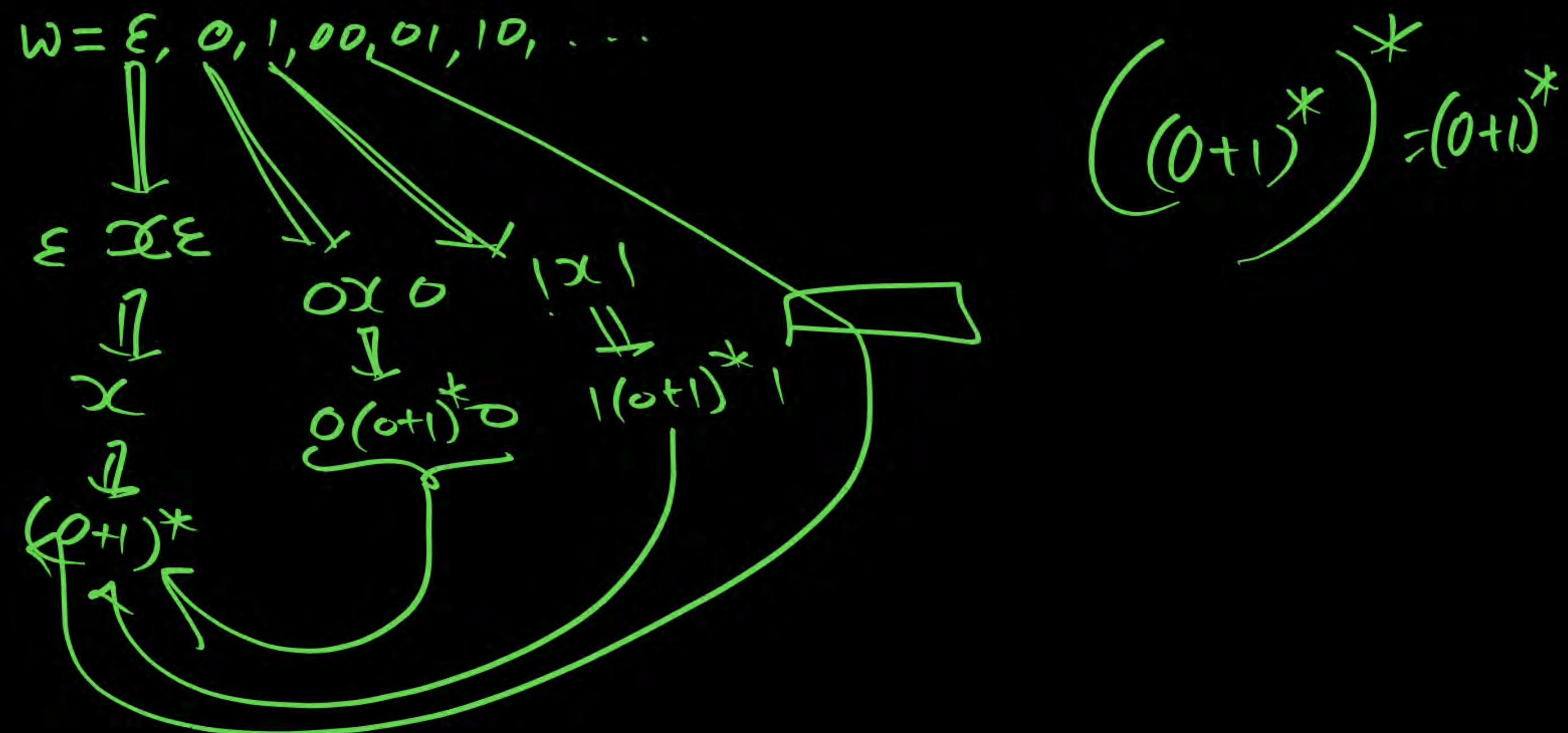
Kleene closure of  $\{ww \mid w \in \Sigma^* \text{ with } \Sigma = \{0, 1\}\}$  is regular.



Kleene closure of  $\{wxw \mid w, x \in \Sigma^* \text{ with } \Sigma = \{0, 1\}\}$  is regular.

$\{0^x\}^*$

$$\{wxw \mid w, x \in \{0,1\}^*\} = (0+1)^*$$



$$\{a^{\text{prime}}\}^* = \{a^2, a^3, a^5, a^7, \dots\}^*$$

$$= \{e, a^2, a^3, a^4, a^5, a^6, a^7, a^8, \dots\}$$

$$= e + a \alpha a^*$$

$$= \{a^n \mid n \neq 1\}$$

$$L = \left\{ \sum_{w \in \Sigma}^{\omega} w \mid w \in \{0,1\}^* \right\} = \{ \epsilon, 00, 11, 0000, 0101, 1010, \dots \}$$

$$L^* = \{ \omega \omega \}^* = \{ \epsilon, 00, 11, 0000, 0101, 1010, \dots \}^*$$

$$= \left\{ w_1 w_1 \ w_2 w_2 \ w_3 w_3 \ w_4 w_4 \ \dots \ w_k w_k \right\}_{k \geq 1}$$

$$L = \{a^n b^n\} = \{\epsilon, ab, aabb, a^3b^3, \dots\}$$

$$L^* = \{a^n b^n\}^* = \{\epsilon, ab, aabb, a^3b^3, \dots\}^*$$

$$= \{\epsilon, ab, \underbrace{abab}, \underbrace{aabb}, \dots\}$$





## Regular Languages : NAT

Q60. Consider the following FSM with output. It takes binary input in reverse order of actual binary number and produces binary output. To see actual output, produced output should be considered in reverse. Identify TRUE statement.



It increments given input



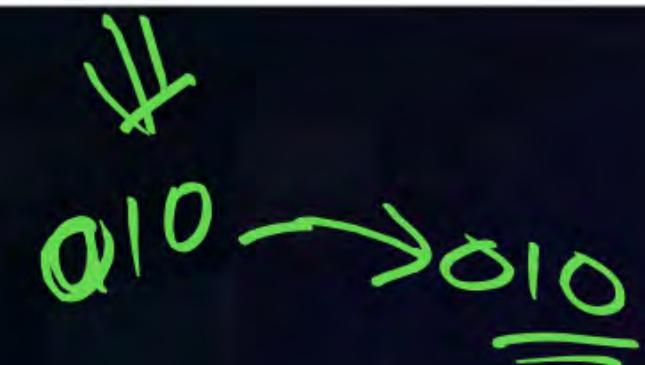
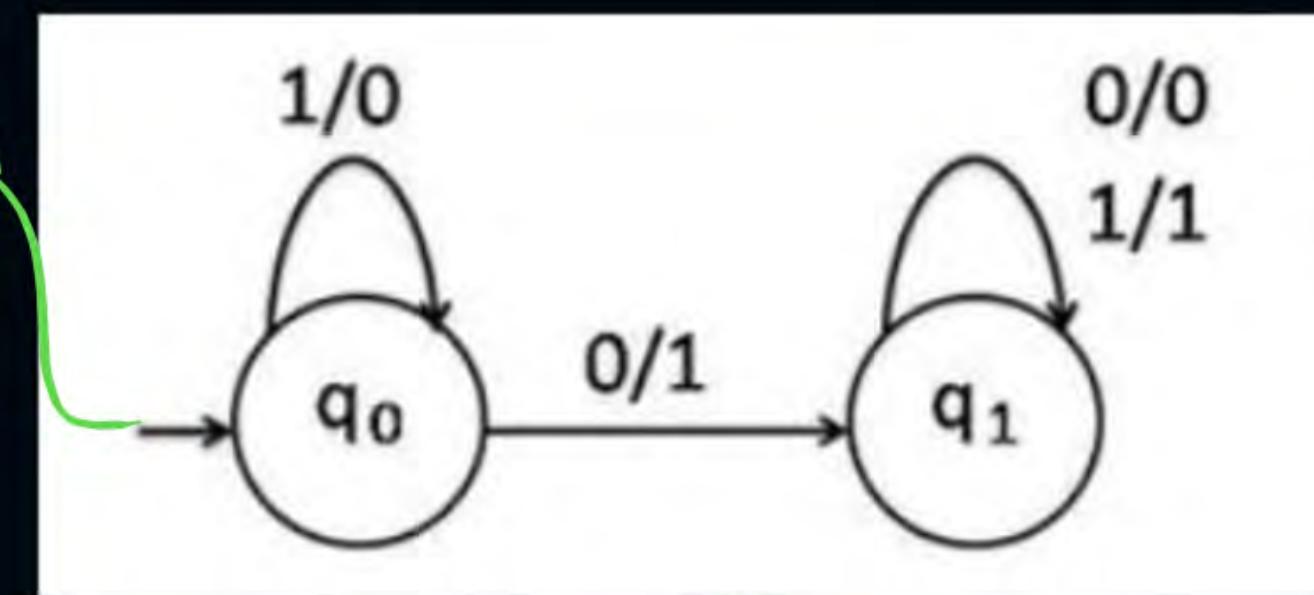
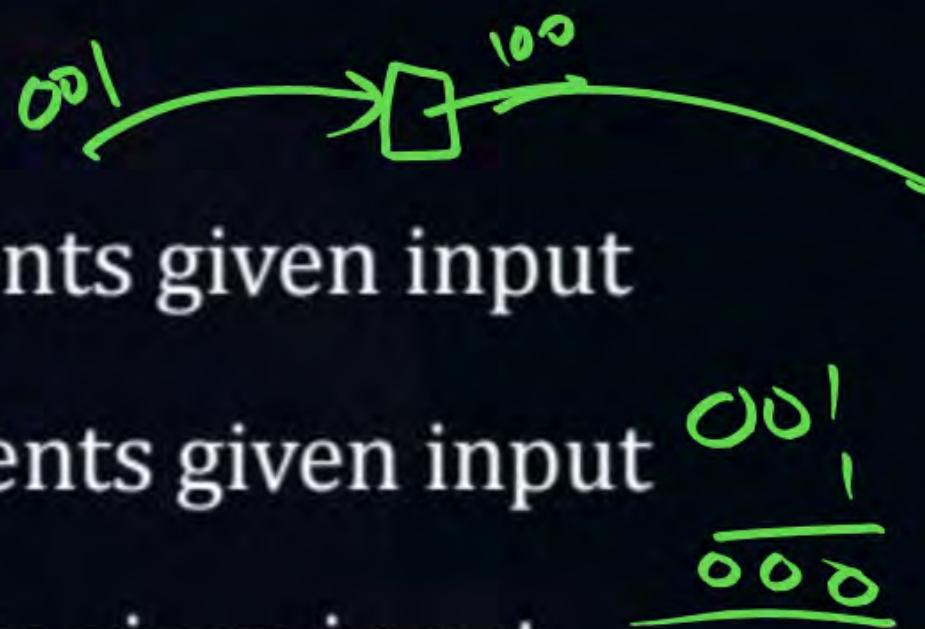
It decrements given input



It left shifts given input



It right shifts given input





## Regulars and CFGs : MSQ



Q61. Consider the following grammar:

$$\begin{array}{ll} S \rightarrow Aa \mid Ab & S = A(a+b) = (a+b)(a+b)^* \\ A \rightarrow aB \mid bB & A = (a+b)B = (a+b)(a+b)^* \\ B \rightarrow Ba \mid Bb \mid \text{epsilon} & B = (a+b)^* \end{array}$$

What is the language generated by above CFG?

**A**

$(a+b)(a+b)^*$

**B**

$b(a+b)^*$

**C**

$(a+b)(a+b)(a+b)^*$

**D**

None of these



## Regulars and CFGs : MSQ



Q62. Consider the following grammar G:

G :

$$\begin{array}{l} S \rightarrow A \mid B \\ A \rightarrow aCb \\ C \rightarrow aC \mid bC \mid \epsilon \\ B \rightarrow bD \\ D \rightarrow bD \mid aD \mid \epsilon \end{array}$$

*A = a(a+b)^\* b*  
*C = (a+b)^\**  
*B = b(a+b)^\* a*  
*D = (b+a)^\**

$$L = A + B$$

S is start symbol, A, B, C and D are non-terminals and a, b are terminals. The language generated by above grammar G is

**A**

$$a(a+b)^* b$$

**C**

$$a(a+b)^* b + b(a+b)^* a$$

**B**

$$a(a+b)^* a + b(a+b)^* b$$

**D**

None of these



## Regulars and CFGs : MSQ

Q63. Consider the following context-free grammars:

$$G_1: S \rightarrow aS \mid A, A \rightarrow \epsilon \mid bA \quad A = b^*$$

$$G_2: S \rightarrow aA \mid B, A \rightarrow aA \mid \epsilon, B \rightarrow bB \mid \epsilon \quad B = \epsilon$$

Which one of the following pairs of languages is generated by  $G_1$  and  $G_2$ , respectively?

$$B = \epsilon^* \quad B = b^*$$

$$S \rightarrow \emptyset \mid b^* \quad L = a^* b^*$$

$$S \rightarrow aa^* \mid b^* \quad L = a^+ b^*$$

A

$\{a^m b^n \mid m > 0 \text{ or } n > 0\}$  and  $\{a^m b^n \mid m > 0 \text{ and } n > 0\}$ .

B

$\{a^m b^n \mid m \geq 0 \text{ and } n \geq 0\}$  and  $\{a^m b^n \mid m > 0 \text{ and } n \geq 0\}$ .

C

$\{a^m b^n \mid m \geq 0 \text{ or } n > 0\}$  and  $\{a^m b^n \mid m > 0 \text{ and } n > 0\}$ .

D

$\{a^m b^n \mid m \geq 0 \text{ and } n > 0\}$  and  $\{a^m b^n \mid m > 0 \text{ or } n > 0\}$ .



## Regulars and CFGs : NAT



Q64. Consider the following context-free grammar G over the alphabet  $\Sigma = \{a, b, c\}$  with S as the start symbol

$$\left. \begin{array}{l} S \rightarrow abScT \mid abc \\ T \rightarrow b \end{array} \right\} \Rightarrow S \xrightarrow{\cdot} abScb \mid abc$$

Let  $L = \{ w \mid w \text{ is in } L(G), \text{ length of } w \text{ is less than } 9 \}$ . Then size of L is \_\_

$$= \{abc, ababc cb\}$$

$$= \Sigma^*$$

abc ✓

abScb = ababc cb ✓

abScb = ababScbcb = abababc cbcb  
>9 length



## Regulars and CFGs : NAT

Q65. Consider the context-free grammars over the alphabet  $\{a, b, c\}$  given below. S and T are non-terminals.

$$G_1: S \rightarrow abS \mid T, T \rightarrow cT \mid \epsilon \quad L = (ab)^* c^*$$

$$G_2: S \rightarrow aSc \mid T, T \rightarrow bT \mid \epsilon$$

$a^n b^* c^n$        $\uparrow$        $\overbrace{\uparrow}^{T}$       Number of strings in  $L(G_1) \cap L(G_2)$  is 2,

$$(ab)^* c^* \cap a^n b^* c^n$$

$$\{\epsilon, \dots, abc; \dots\} \cap \{\epsilon, abc; \dots\}$$



## Regulars and CFGs : MSQ



Q66. Identify the language generated by the following grammar, where S is the start variable.

$$\begin{array}{l} S \rightarrow XY \\ \boxed{X \rightarrow aX \mid a} \Rightarrow X = a^+ \\ Y \rightarrow YX \mid \epsilon \\ Y \rightarrow \textcircled{Y} \mid \epsilon \Rightarrow (a^*)^* = a^* \end{array} \quad \left. \begin{array}{l} L = X Y = a^+ a^* \\ = a^+ \end{array} \right\}$$

A  $a^*$

B  $aa^* = a^+$

C  $(aa)^*$

D None of these



## Regulars and CFGs : MCQ

Q67. Consider  $L_1 = ab^*$

$L_2 = ba^*$

$L_3 = L_1 / L_2$

Which of the following expression is equivalent to  $L_3$ ?

A

$L_1$

B

$L_2$

$$\begin{aligned}L_1/L_2 &= \frac{ab^*}{ba^*} \\&= \left\{ \frac{ab^*}{b}, \frac{ab^*}{ba} \right\} \times \frac{ab^*}{ba} \times \frac{ab^*}{baaa}\end{aligned}$$

$\frac{ab^*}{b} \times$   
 $\frac{ab^*}{ba} = ab$   
 $\frac{ab^*}{baa} = abbb$

C

a

D

ab

$$ab^*/ba^* = \{ ab/b, ab^*/ba, ab^*/baa, ab^*/baaa, \dots \}$$

↓      X      X      X      X

$$= \left\{ a/b, ab/b, abb/b, ab^3/b, \dots \right\}$$

X      ↓      ↓      ↓  
 a      ab      ab<sup>2</sup>

↓      ↓

$$= ab^* = \{ \}$$

$$ab^*/ba^* = a$$

$$ab^*/ba^* = b$$

$$ab/b = a$$

$$ab/a = \emptyset$$



## Regulars and CFGs : MSQ



Q68. Consider  $L_1 = ab^*$

$$L_2 = ba^*$$

$$L_3 = L_1 \cup L_2 = ab^* + ba^*$$

Which of the following expression is equivalent to  $L_3^*$ ?

$$L_3^* = (ab^* + ba^*)^*$$

$$= (a+b)^*$$



$$(a+b)^*$$



$$(ab)^*$$



$$(ab+ba)^*$$



None of these



## Regulars and CFGs : MCQ



Q69. Consider the following CFG G.

$$G: S \rightarrow abS \mid \epsilon, T \rightarrow abT \mid \epsilon$$

Which of the following is  $L(G)$  ?

$$L = (ab)^*$$

A

$$(ab)^*$$

B

$$(ab)^+$$

C

$$(a+b)^*$$

D

None of these

Note :

$$S \rightarrow abT \mid \epsilon, T \rightarrow abT \mid \epsilon$$

$$\begin{aligned} S &= ab(ab)^* + \epsilon \\ &= (ab)^+ + \epsilon = (ab)^* \end{aligned}$$

$$T = (ab)^*$$



## Regulars and CFGs : NAT



Q70. If  $L = \{b^n a^n \mid n \geq 0\}$ , then how many following statements are TRUE?

$$L = b^n a^n$$



- I.  $L^* = \{b^n a^n\}^*$  is not reg
- II.  $L^{Rev} = \{b^n a^n\}^{Rev} = a^n b^n$  is not reg
- III.  $\bar{L} = \overline{\{b^n a^n\}}$  is not reg



## Regulars and CFGs : MCQ

Q71. How many of the following statements are correct?.

- I. Every regular language is finite language FALSE
- ✓ II. Every finite language is regular language TRUE
- III. Every CFL is regular language FALSE
- ✓ IV. Every regular language is CFL TRUE

A

4

B

3

C

2

D

1



## Regular Languages : NAT



Q72. How many of the following languages are regular?

- $L_1 = \{wxw^R \mid w, x \in \{a, b\}^+, w^R \text{ is the reverse of string } w\}$
- $L_2 = \{w \mid w, x \in \{a, b\}^*, \text{ number of } 01\text{'s in } w \text{ is even}\}$
- $L_3 = \{w \mid w, x \in \{0, 1\}^*, \text{ Dec}(w) \text{ is divisible by } 100\}$
- $L_4 = \{w \mid w, x \in \{a, b\}^*, w \text{ has more } 0\text{'s than } 1\text{'s}\}$



## Regulars and CFGs : MSQ



Q73. Choose FALSE statement.

- A** Substitution is closed for regular languages
- B** Substring is closed for regular languages
- C** Subset is closed for regular languages
- D** Finite subset is closed for regular languages



## Regulars and CFGs : MCQ

Q74. Let  $L = \{ w_1 w_2 w_3 \mid w_1, w_2, w_3 \in \{a, b\}^*, |w_1| = |w_2| = |w_3| \}$ . Choose L from the following.

- A**  $(a+b)^*$
- B**  $(a+b) (a+b)^* (a+b)$
- C**  $((a+b) (a+b) (a+b))^*$
- D**  $(a+b) (a+b)^*$



## Regulars and CFGs : MSQ



Q75. Which of the following operation is closed for finite languages but not closed for infinite languages?

- A** Kleene star
- B** Union
- C** Subset
- D** Substitution

# THANK - YOU

# CS & IT ENGINEERING

## Theory of Computation

Lecture No.- 06

Mallesham Devasane Sir



# Recap of Previous Lecture



Topic

Regular Languages

Topic

Context Free Grammars

Topic

Topic

Topic

# Topics to be Covered



Topic

Regular Languages

Topic

Context Free Languages



## Regulars and CFGs : NAT



Q70. If  $L = \{b^n a^n \mid n \geq 0\}$ , then how many following statements are **TRUE**?

- 1

- I.  $L^*$  is a regular language
- II. Reversal of  $L$  is a regular language
- III. Complement of  $L$  is a regular language  $\overline{\{b^n a^n\}}$
- IV. Finite Subset of  $L$  is always regular language

$$L = b^n a^n$$

$$\bar{L} = \Sigma^* - L$$

$$= (a+b)^* - \{b^n a^n\}$$

$$= \boxed{\Sigma^* a b \Sigma^* \cup \{b^m a^n \mid m \neq n\}}$$

is non reg

$$L \cup \bar{L} = (a+b)^*$$



## Regulars and CFGs : MCQ



Q71. How many of the following statements are correct?

- I. Every regular language is finite language
- II. Every finite language is regular language
- III. Every CFL is regular language
- IV. Every regular language is CFL

A

4

B

3

C

2

D

1



## Regular Languages : NAT



Q72. How many of the following languages are regular?

- ✓  $L_1 = \{wxw^R \mid w, x \in \{a, b\}^+, w^R \text{ is the reverse of string } w\}$
- ✓  $L_2 = \{w \mid w, x \in \{0, 1\}^*, \text{ number of } 01\text{'s in } w \text{ is even}\}$
- ✓  $L_3 = \{w \mid w, x \in \{0, 1\}^*, \text{ Dec}(w) \text{ is divisible by } 100\}$
- ✗  $L_4 = \{w \mid w, x \in \{0, 1\}^*, w \text{ has more } 0\text{'s than } 1\text{'s}\}$

$a^x a^x b^y b^y$   
 $\diagup \quad \diagdown$   
 $a(a+b)^5 a^x b^y b^y$

$$n_0(\omega) > n_1(\omega)$$

= 3 //



## Regulars and CFGs : MSQ



Q73. Choose FALSE statement.

- A** Substitution is closed for regular languages ✓
- B** Substring is closed for regular languages ✓
- C** Subset is closed for regular languages ✗
- D** Finite subset is closed for regular languages ✓



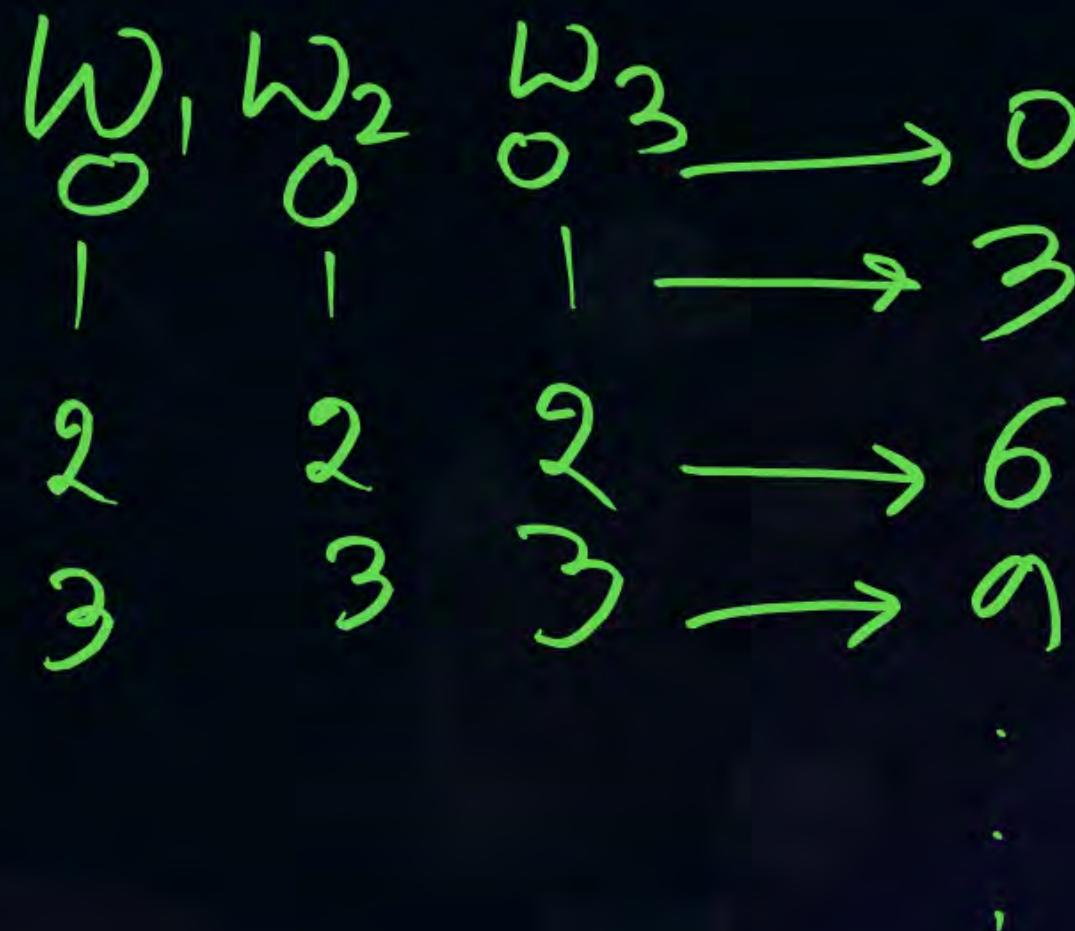
## Regulars and CFGs : MCQ



Q74. Let  $L = \{ w_1 w_2 w_3 \mid w_1, w_2, w_3 \in \{a, b\}^*, |w_1| = |w_2| = |w_3| \}$ . Choose L from the following.

$$L = \{ w \mid |w_1| \text{ is div by } 3 \}$$

- A**  $(a+b)^*$
- B**  $(a+b) (a+b)^* (a+b)$
- C**  $((a+b) (a+b) (a+b))^*$
- D**  $(a+b) (a+b)^*$





## Regulars and CFGs : MSQ



Q75. Which of the following operation is closed for finite languages but not closed for infinite languages?

- A** Kleene star
- B** Union
- C** Subset
- D** Substitution

	Fin	Inf
A	X	✓
B	✓	✓
C	✓	X
D	✓	✓

Subset of Inf lang is may or may not be inf

Subset of Fin lang is Fin lang

$F_i \in \Phi$

$F_2 = \{a\}$

$F_3 = \{\varepsilon\}$

$F_4 = \{0, \varepsilon\}$

$\overset{*}{a}_{I_1}, \overset{*}{b}_{I_2}, \overset{*}{ab}_{I_3}$

$I_4, I_5, I_6$

$I_8, I_9, I_{10}$

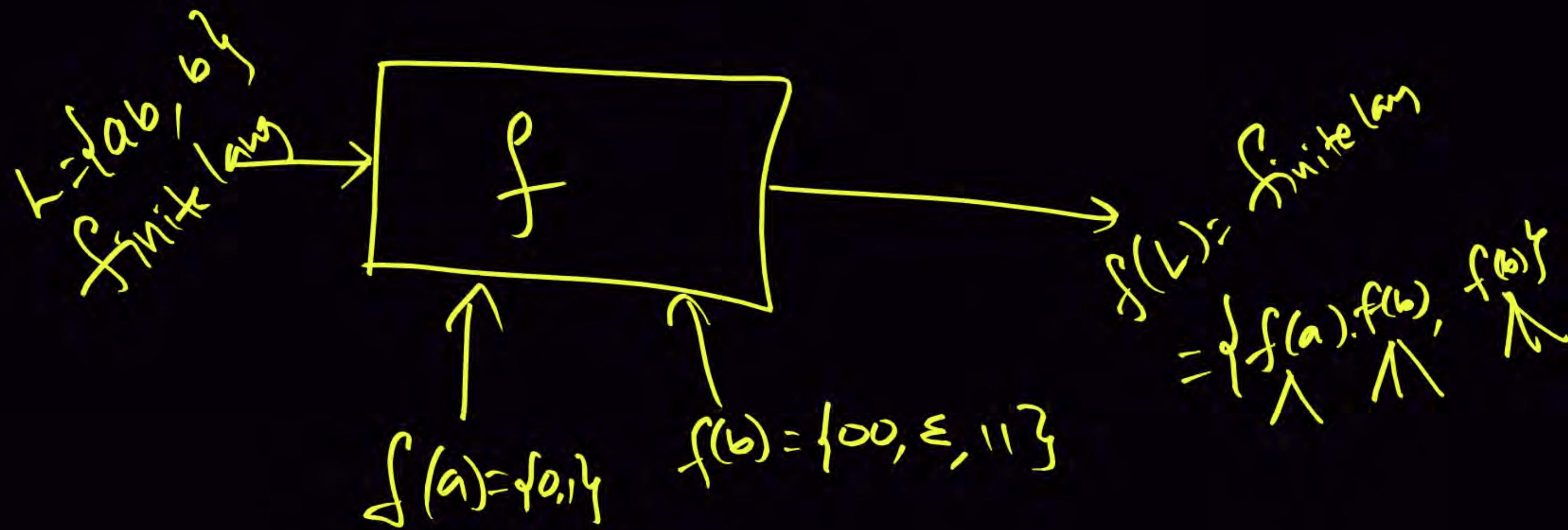
$a^*$ 

Inf lang

 $\emptyset$ 

Not Inf

is subset of  $\bar{a}^*$  $\{\epsilon, \text{aa}\}$   
finite lang



#Q76. Consider the following language L:

$$L = \{a, b, ab, baa\}$$

Which of the following strings are present in the INIT of L?

- A  $\in$
- B aa
- C ba
- D b

Prefix (✓)

$$L = \{a, b, ab, baa\}$$

$$\text{Pref}(L) = \{\text{pref}(a), \text{pref}(b), \text{pref}(ab), \text{pref}(baa)\}$$

$$= \{\epsilon, a, b, ab, ba, baa\}$$

$L$  satisfies prefix property

iff

Every string of  $L$  is not a prefix to every other string in  $L$ .

- ①  $L = \{a, \textcolor{blue}{ba}, \underline{bab}\}$  not satisfy prefix property.
- ②  $L = \{\underline{ab}, \underline{ac}, \underline{bac}\}$  satisfy prefix property.

#Q77. Consider the following statements:

- [I]. Infinite union of regular languages is regular. *Incorrect*
- [II]. Subset of finite language is regular. *Correct*
- [III]. Intersection of two non-regular languages  can be regular. *Possible  
Correct*

Total number of **INCORRECT** statements are = 1.

$$\{a^n b^n\} \cap \{b^n a^n\} = \{\epsilon\}$$

*non reg*                    *non reg*                    *(eg)*

#Q78. Consider the following grammar G:

$$G: \quad S \rightarrow aAa \mid bAb$$

$$A \rightarrow aA \mid bA \mid a \mid b \Rightarrow (a+b)^+$$

$$B \rightarrow aA \mid bA \mid a \mid b \Rightarrow (a+b)^+$$

$$L = a(a+b)^+a + b(a+b)^+b$$

*(u) (v)*

The language generated by above grammar G is:

A

$$L(G) = \{wxw^R \mid w, x \in \{a, b\}^+\} = a \cancel{x} a + b \cancel{x} b + aaxaa + abxbat \dots$$

B

$$L(G) = \{wxw \mid w, x \in \{a, b\}^+\}$$

not by law

C

$$L(G) = \{a(a+b)^+a + b(a+b)^+b\}$$

D

$L(G)$  is CFL but not regular

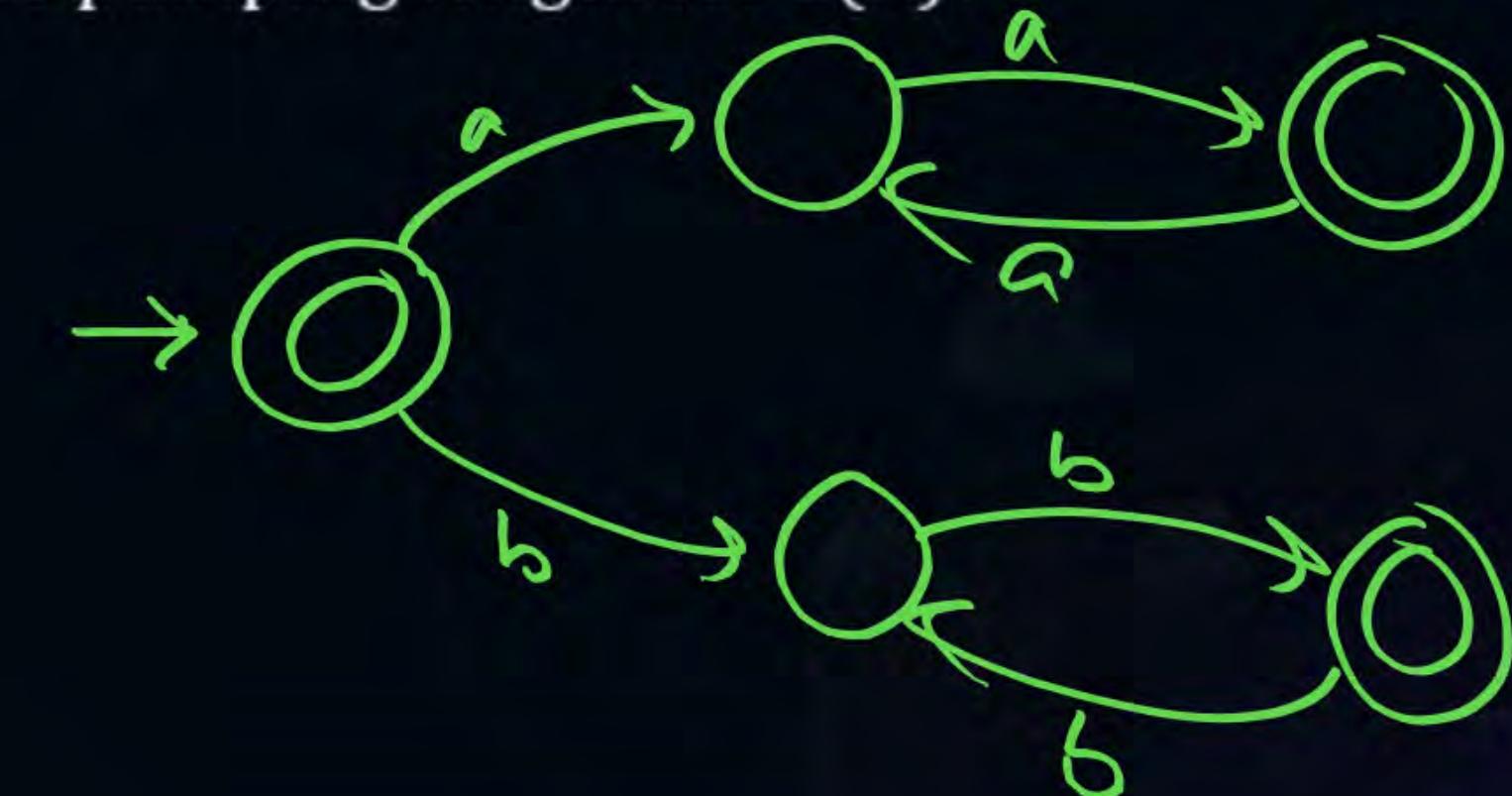
#Q79. Consider the following regular expression:

$$R = (aa)^* \cup (bb)^*$$

Which of the following can't be the pumping length for  $L(R)$ ?

- A 2
- B 5
- C 7
- D 9

→ S  
→ DFA in mind  
(ignore dead)



#Q80. Which of the following does not generate string 'baa'?

A

$$a^* (ba)^* b^*$$

$$\Sigma \underline{ba} \quad \text{---} \quad \times$$

B

$$a^* b^* (ba)^* a$$

$$\Sigma \Sigma \underline{ba} a \quad \checkmark$$

C

$$(ab^* + a)^* (ab)^* b^* a^*$$

$$\Sigma \quad \Sigma \quad \underline{ba} a \quad \checkmark$$

D

$$(bba^* + b)^* a$$

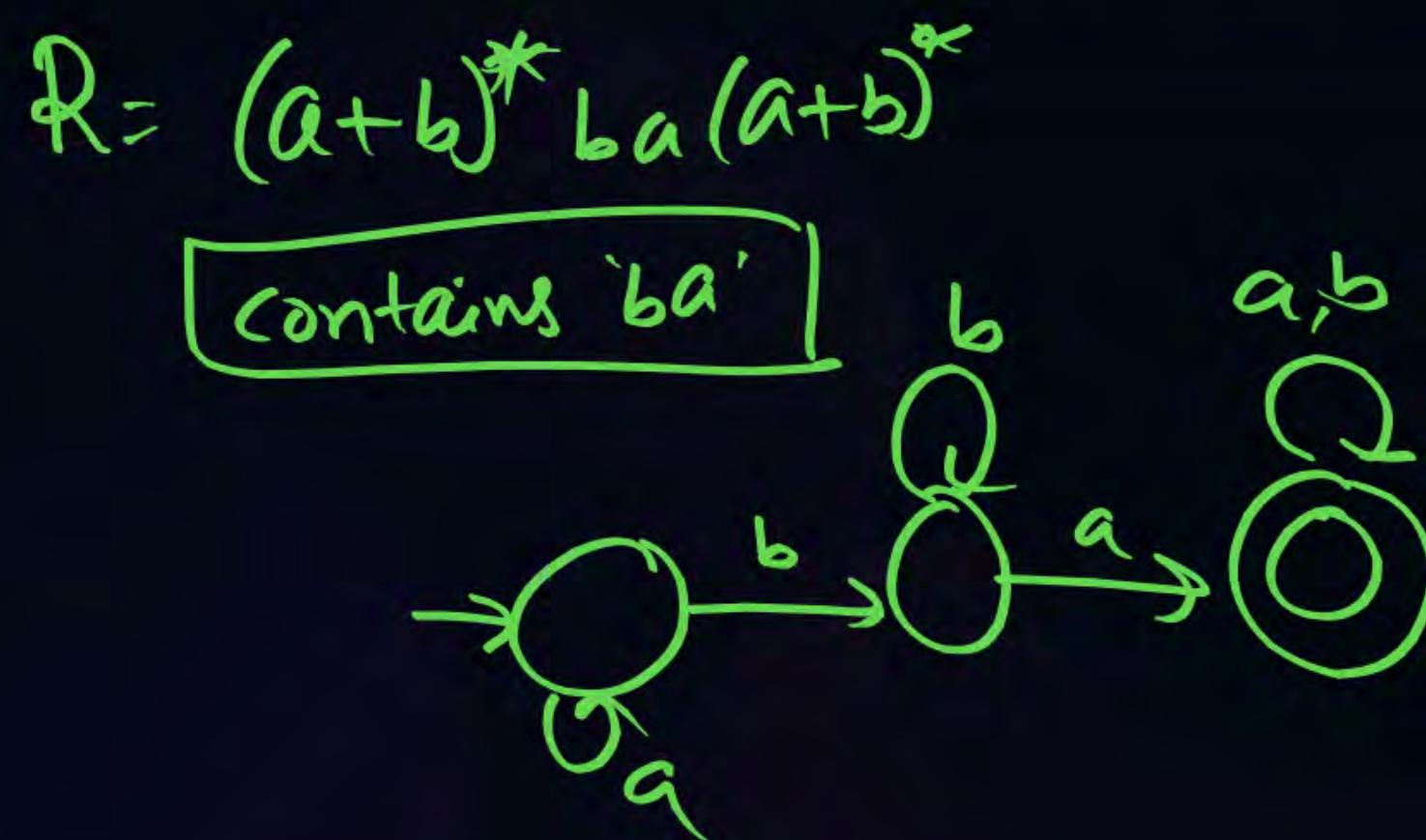
$$\underline{b} \quad \underline{a} \quad \times$$

bbaa

#Q81. Consider the regular expression R:

$$R = (a + ba^*)^* ba (a + b)^*$$

How many states are needed to design a DFA for above regular expression R? \_\_



= 3 //

#Q82. Consider the following grammar G:

$$\begin{aligned} G: \quad S &\rightarrow aaaA \\ A &\rightarrow aA \mid B \quad A = a^*B = a^*(\epsilon + b)^* \\ B &\rightarrow b \mid bb \mid bbb \mid bbbb \mid \epsilon \quad B = \epsilon + b^+ \dots + b^4 = (\epsilon + b)^* \end{aligned}$$

The language generated by above grammar G is

A

$$L(G) = \{a^m b^n \mid m \text{ divisible by 3 and } n \geq 4\}$$

B

$$L(G) = \{a^m b^n \mid m \geq 1 \text{ and } n < 5\}$$

C

$$L(G) = \{a^m b^n \mid \boxed{m > 2} \text{ and } \boxed{n < 5}\}$$

$m \geq 3$

D

None of these

Every string should not be a prefix  
to another string

#Q83. Which of the following language satisfy the prefix property?

A

$$L = \{a^n b^n \mid n \geq 1\} = \{ab, aabb, aaabbb, \dots\}$$

B

$$L = \{wxw^R \mid w, x \in \{a, b\}^*\} = (a+b)^* \times$$

C

$$L = \{a^m b^{2m} \mid m \geq 1\} = \{\underline{aabbb}, aabbwww, \dots\}$$

D

$$L = \{w \in \{0, 1\}^* \mid n_0(w) = n_1(w)\}$$

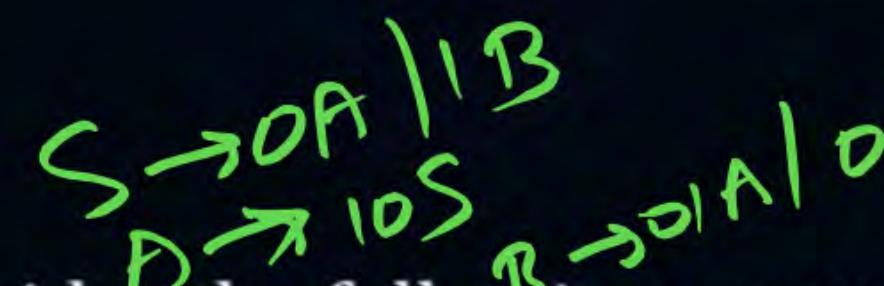


#Q84. Consider a language  $L = \{w \mid w \in \{a, b\}^*, 6^{\text{th}} \text{ symbol from end is 'a'}\}$ .

If number of states in NFA is A and number of states in DFA is B then the value of  $A \times B$  is \_\_\_\_.

$$\begin{aligned} \text{Min DFA : } & 2^6 = 64 \text{ states} = A \\ \text{Min DFA : } & 6+1 = 7 \text{ states} = B \end{aligned}$$

$$\begin{aligned} A \times B &= 64 \times 7 \\ &= \underline{448} \end{aligned}$$



#Q85. Consider the following grammars  $G_1$  and  $G_2$ :

$$\begin{aligned} G_1: \quad S &\rightarrow 0A \mid 1B \\ A &\rightarrow \cancel{101C} \mid 10S \\ B &\rightarrow 01A \mid 0 \\ \cancel{P} &\rightarrow \cancel{00B} \mid \cancel{10A} \end{aligned}$$

Regular Grammar

↳ always generates reg lang

$$\begin{aligned} G_2: \quad S &\rightarrow AB \\ A &\rightarrow 01 \mid 10 \\ B &\rightarrow 00 \mid 11 \end{aligned}$$

Not reg grammar  $\Rightarrow \{0100, 0111, 1000, 1011\}$

Finite lang

Which of the following is/are correct?



L( $G_1$ ) is regular.



L( $G_2$ ) is regular.



L( $G_2$ ) is finite regular.



L( $G_1$ ) is CFL but not regular.

#Q86. Consider the following grammars on  $\Sigma = \{0, 1, 2\}$

$$\begin{aligned} G_1: \quad S &\rightarrow AB \\ A &\rightarrow 0A1 \mid \epsilon \\ B &\rightarrow 1B2 \mid \epsilon \end{aligned}$$

$$\begin{aligned} G_2: \quad S &\rightarrow 0S1 \mid B \\ B &\rightarrow 1B2 \mid \epsilon \end{aligned}$$

$$\begin{aligned} G_3: \quad S &\rightarrow AB \mid B \\ A &\rightarrow 0A1 \mid 01 \\ B &\rightarrow 1B2 \mid \epsilon \end{aligned}$$

Which of the following grammars are equivalent?

**A**

$G_1$  and  $G_2$  only

**C**

$G_1$  and  $G_3$  only

**B**

$G_2$  and  $G_3$  only

**D**

$G_1$  and  $G_2$  only

#Q87. Consider the following statements:

- S<sub>1</sub>: Pumping lemma can be used to prove that some of the languages are not regular using contradiction.
- S<sub>2</sub>: Language L satisfies the pumping lemma iff L is regular.

Which of the following is correct?

**A**

S<sub>1</sub> only

**C**

Both S<sub>1</sub> and S<sub>2</sub>

**B**

S<sub>2</sub> only

**D**

None of the above

#Q88. Finite automata can be used in which of the following?

- A String matching
- C Text editing
- B Lexical analysis
- D Infix to prefix conversion

#Q89. Let  $L$  consist of all binary strings start with 1 and decimal value of binary number is divisible by 3. Which of the following is true?

- A** L can be recognized by NPDA
- C** L can be recognized by DPDA
- B** L can be recognized by DFA
- D** L can be recognized by NFA

#Q90. Consider the following grammar G:

$$S \rightarrow P \mid Q$$

$$P \rightarrow aPb \mid \lambda$$

$$Q \rightarrow aaQb \mid \lambda$$

Which of the following is/are True?

A

G is ambiguous and  $\{\lambda\}$  has two parse tree.

C

$L(G)$  is accepted by PDA but not by DPDA.

B

$L(G)$  is inherently ambiguous.

D

None of these.



THANK - YOU

# CS & IT ENGINEERING

## Theory of Computation

Lecture No.- 07

Mallesham Devasane Sir



# Recap of Previous Lecture



**Topic**

Regular Languages

**Topic**

Context Free Languages

# Topics to be Covered



Topic

Regular Languages

Topic

Context Free Languages

#Q86. Consider the following grammars on  $\Sigma = \{0, 1, 2\}$

$$G_1: \begin{array}{l} S \rightarrow AB \\ A \rightarrow 0A1 \mid \epsilon \xrightarrow{\epsilon} 0^n 1^n \\ B \rightarrow 1B2 \mid \epsilon \xrightarrow{\epsilon} 1^k 2^k \end{array} \left. \begin{array}{l} \\ \Rightarrow 0^n 1^n \\ \Rightarrow 1^k 2^k \end{array} \right\} L_1 = 0^n 1^n 1^k 2^k$$

$$G_2: \begin{array}{l} S \rightarrow 0S1 \mid B \\ B \rightarrow 1B2 \mid \epsilon \xrightarrow{\epsilon} 1^k 2^k \end{array} \left. \begin{array}{l} \\ \Rightarrow 1^k 2^k \end{array} \right\} L_2 = 0^n B 1^n = 0^n 1^k 2^k 1^n$$

$$G_3: \begin{array}{l} S \rightarrow AB \mid B \\ A \rightarrow 0A1 \mid 01 \xrightarrow{\epsilon} 0^n 0^n 1^n \\ B \rightarrow 1B2 \mid \epsilon \xrightarrow{\epsilon} 1^k 2^k \end{array} \left. \begin{array}{l} \\ \Rightarrow 0^n 0^n 1^n \\ \Rightarrow 1^k 2^k \end{array} \right\} L_3 = (A + \epsilon)B = 0^n 1^k 2^k$$

Which of the following grammars are equivalent?

A

G<sub>1</sub> and G<sub>2</sub> only

C

G<sub>1</sub> and G<sub>3</sub> only

B

G<sub>2</sub> and G<sub>3</sub> only

D

G<sub>1</sub> and G<sub>2</sub> only

#Q87. Consider the following statements:

- S<sub>1</sub>: Pumping lemma can be used to prove that some of the languages are not regular using contradiction.  $\top$
- S<sub>2</sub>: Language L satisfies the pumping lemma iff L is regular.  $\top$

Which of the following is correct?

A

S<sub>1</sub> only

C

Both S<sub>1</sub> and S<sub>2</sub>

B

S<sub>2</sub> only

D

None of these

#Q88. Finite automata can be used in which of the following?

- A String matching
- C Text editing
- B Lexical analysis
- D Infix to prefix conversion

⇒ Regular

#Q89. Let L consist of all binary strings start with 1 and decimal value of binary number is divisible by 3. Which of the following is true?

- A L can be recognized by NPDA ✓
- C L can be recognized by DPDA ✓
- B L can be recognized by DFA ✓
- D L can be recognized by NFA ✓

$$S \Rightarrow P \Rightarrow \epsilon$$

$$S \Rightarrow Q \Rightarrow \epsilon$$

#Q90. Consider the following grammar G:

$$S \rightarrow P \mid Q$$

$$P \rightarrow aPb \mid \lambda \Rightarrow a^k b^k$$

$$Q \rightarrow aaQb \mid \lambda \Rightarrow a^{2n} b^n$$

$$L = \{a^k b^k\} \cup \{a^{2n} b^n\} \setminus \emptyset$$

empty string

Which of the following is/are True?

A

G is ambiguous and  $\{\lambda\}$  has two parse tree.

C

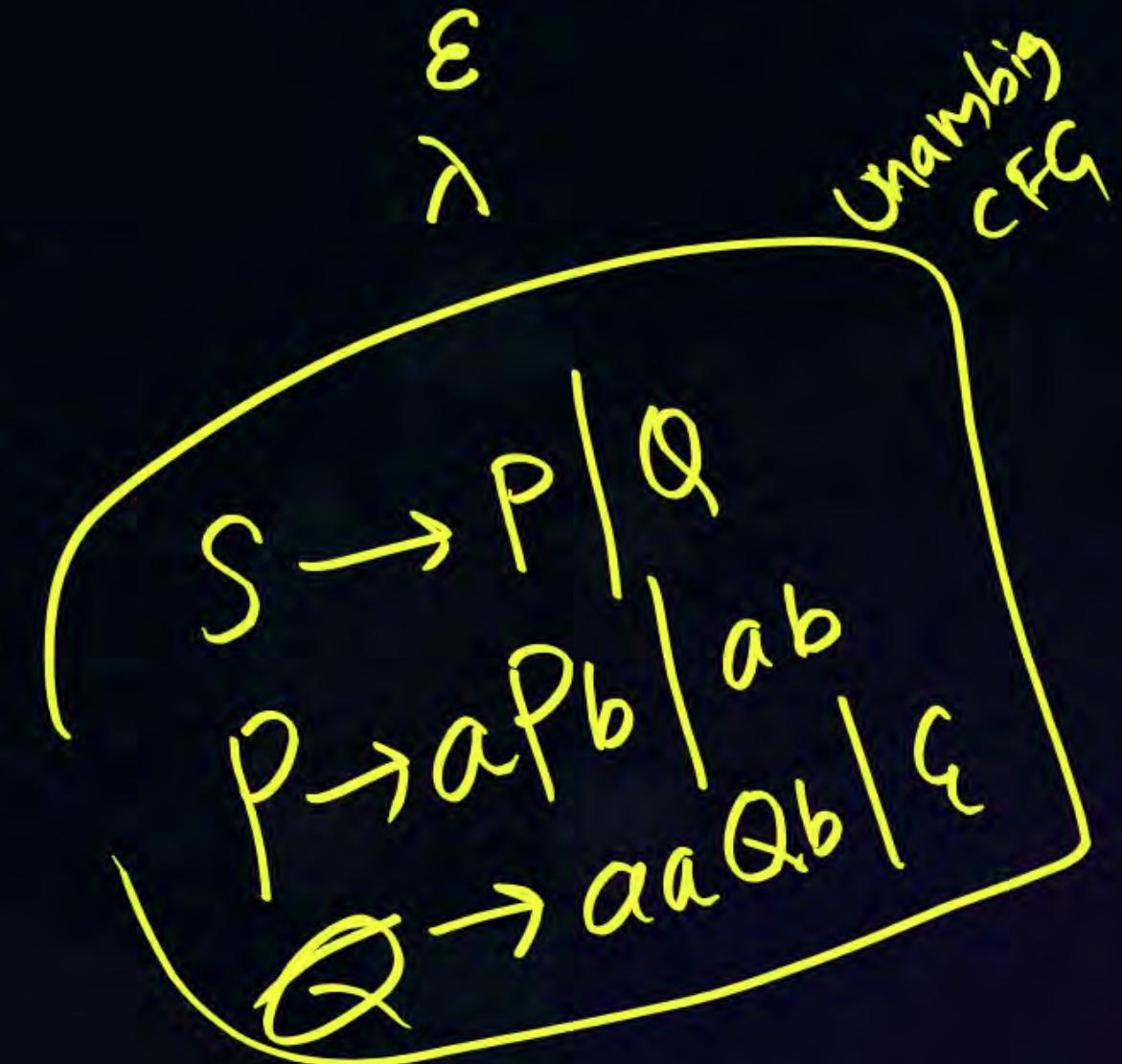
$L(G)$  is accepted by PDA but not by DPDA.

B

$L(G)$  is inherently ambiguous.

D

None of these.



$L$  is Inherently ambiguous

iff

Every CFG that generates  $L$  is Ambiguous CFG.  
( $L$  has no equivalent unamb CFG)

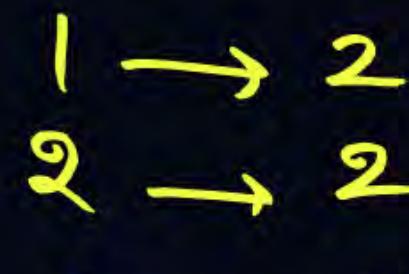
$L = \{ a^m b^n c^k \mid m=n \text{ OR } n=k \}$  is Inherently Amb lang

#Q91. Consider the following grammar G:

$$S \rightarrow aSa \mid bSb \mid a \mid b \mid \epsilon$$

How many strings x belong to  $L(G)$  where  $|x| \leq 11$ ? \_\_\_\_.

length      No. of strings  
 $0 \rightarrow 1$

  $1 \rightarrow 2$   
  $2 \rightarrow 2$

  $3 \rightarrow 4$

  $4 \rightarrow 4$

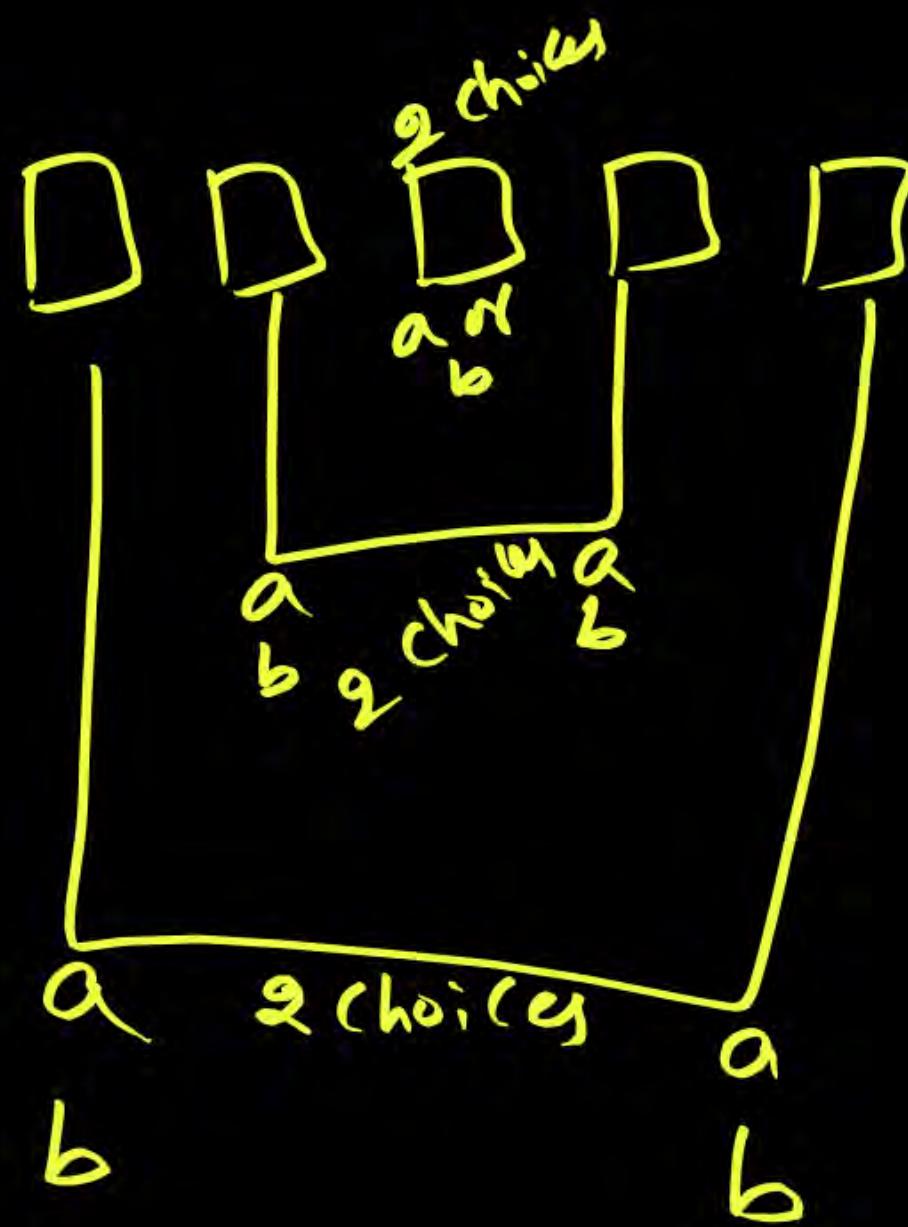
  $5 \rightarrow 8$  strings

$6 \rightarrow 8$  strings  
 $7 \rightarrow 16$  strings  
 $8 \rightarrow 16$  strings  
 $9 \rightarrow 32$  strings

$10 \rightarrow 32$  strings  
 $11 \rightarrow 64$  strings

$$\begin{aligned} & 1 + 2 + 4 + 4 + 8 + 8 + 16 + 16 + 32 \\ & + 64 \\ & = 189 \end{aligned}$$

How many palindromes upto 11 length!



8 strings

b	b	b	b	b
a	a	a	a	a
a	a	b	a	a
a	b	a	b	a
a	b	b	b	a
b	a	a	a	b
b	a	b	a	b
b	b	a	b	b

#Q92. The length of the shortest string not in the language over  $\Sigma = \{a, b\}$  for regular expression  $a^* (b + ab)^* a^*$  is \_\_\_\_.

$\epsilon$ ✓	aaa✓	aaaa✓
a✓	aab✓	aaab✓
b✓	aba✓	aabb✓
aa✓	abb✓	aabs✓
ab✓	baa✓	aabb✓
ba✓	bab✓	abaa✓
bb✓	bba✓	abab✓
	bbb✓	abba✓
		abbb✓
		baaa✓
		baab✓

$$\text{No. of DFAs} = 2^P$$

#Q93. The number of DFA's with 5 states which can be constructed over the alphabet  $\Sigma = \{0, 1\}$  with designated initial state ~~s<sub>0</sub>~~, then the value of P is  $2^5$ .

$2^5$  choices  $\rightarrow P$

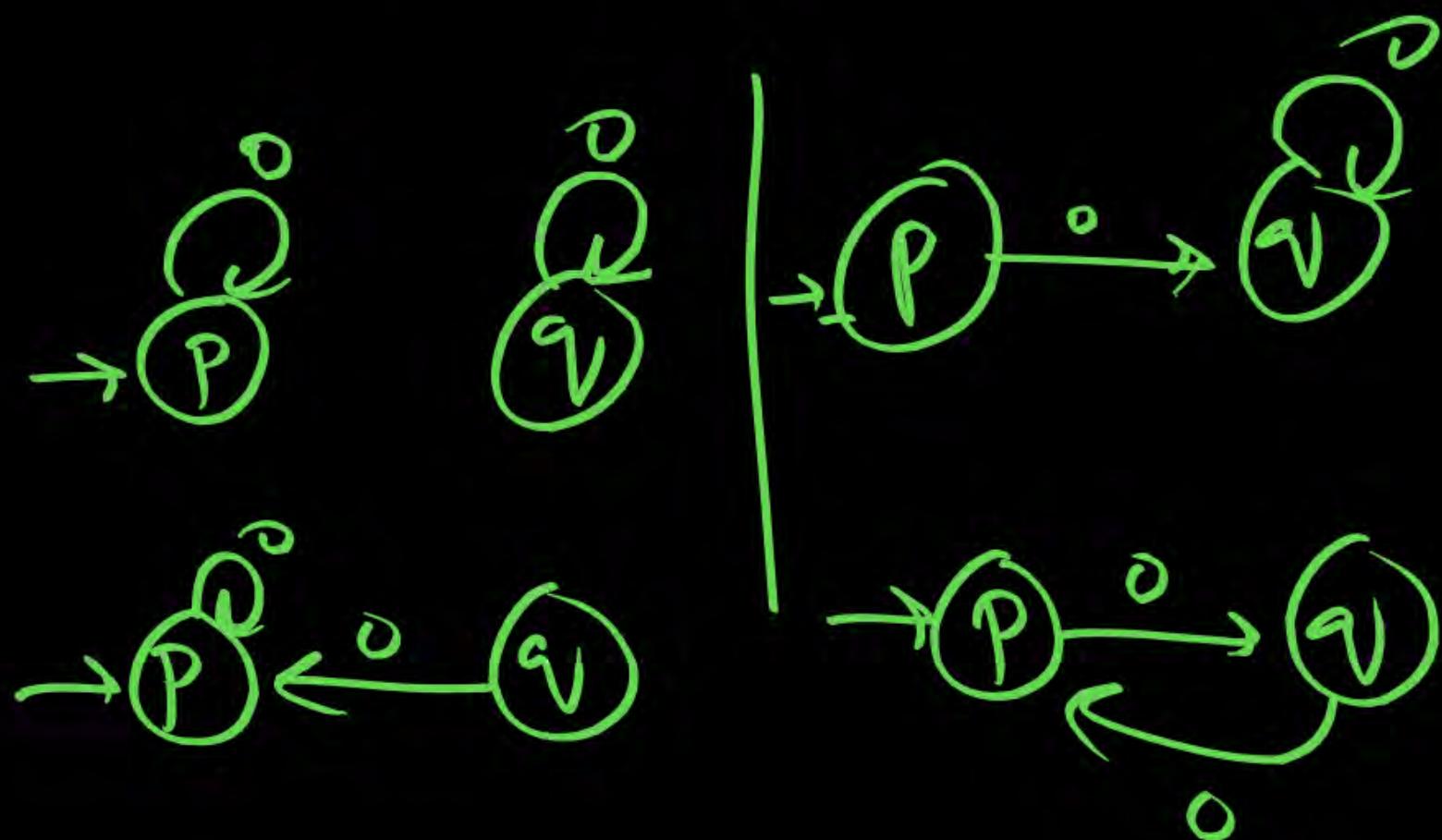
	0	1
$2^5$ choices	s	s
$2^5$ choices	t	s

$$5^{10} \times 2 \text{ DFAs}$$

is  $2^5 \times 5^{10}$

$$\begin{array}{c|cc} & 0 \\ \hline 2 & \rightarrow P & 2 \\ 2 & & 2 \end{array}$$

$$\begin{aligned} \bar{Y} &= \{0, 4\} \\ Q &= \{P, N\} \end{aligned}$$



$$2^2 \times 2 = 2^4 = 16 \text{ DFAs}$$

$\underbrace{\qquad}_{\text{d, q}}$

$\downarrow \text{pq}$

$\downarrow \text{qr}$

$\downarrow \text{rs}$

$\downarrow \text{pqrs}$

[MCQ]

P  
W

$$L = \{ \underline{02}, 0\underline{2}, \underline{021}, 00\underline{2}, 002\underline{1}, 002\underline{11}, \dots \}$$

#Q94. Consider the following CFG G over  $\Sigma = \{0, 1, 2\}$ :

$$G: \quad S \rightarrow 2 \mid 0S \mid 0S1$$

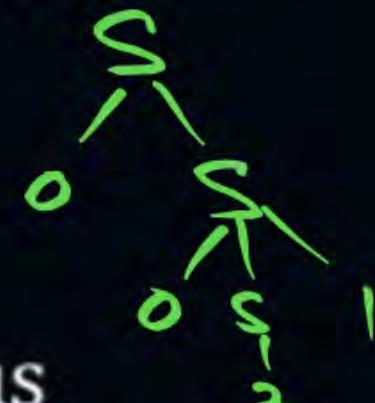
$$= \{ 0^m 2^n 1^{\infty} \} = \{ 0^j 2^i 1^{\infty} \mid i \geq j \}$$

Which of the following is/are true?

A

G is ambiguous

0021



B

L(G) is inherently ambiguous

iff there no unamb

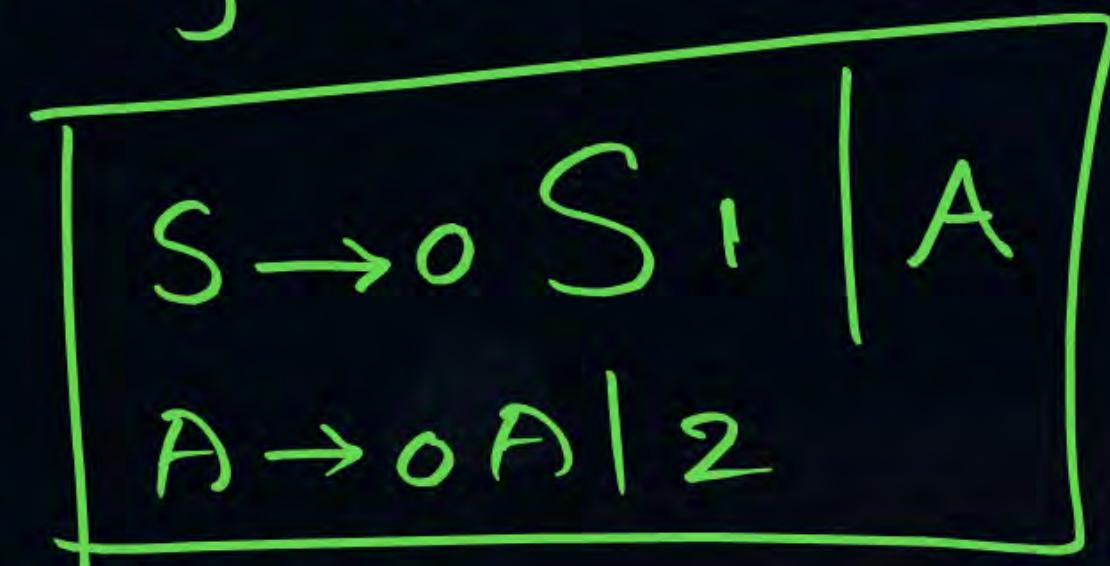
CFG for L(G).

C

Both (a) and (b)

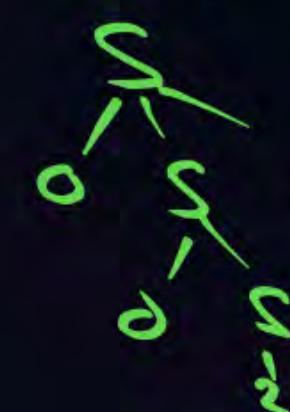
D

None of these.



$$A = 0^* 2$$

$$S = 0^* 0^* 2^* 1^*$$



CFG is Ambiguous

iff

$\exists w, > 1 \text{ PT}$

$L$  is Inherently Ambiguous

iff

Every CFG that generates  $L$   
is Amb

$S \rightarrow SS \mid a$ 

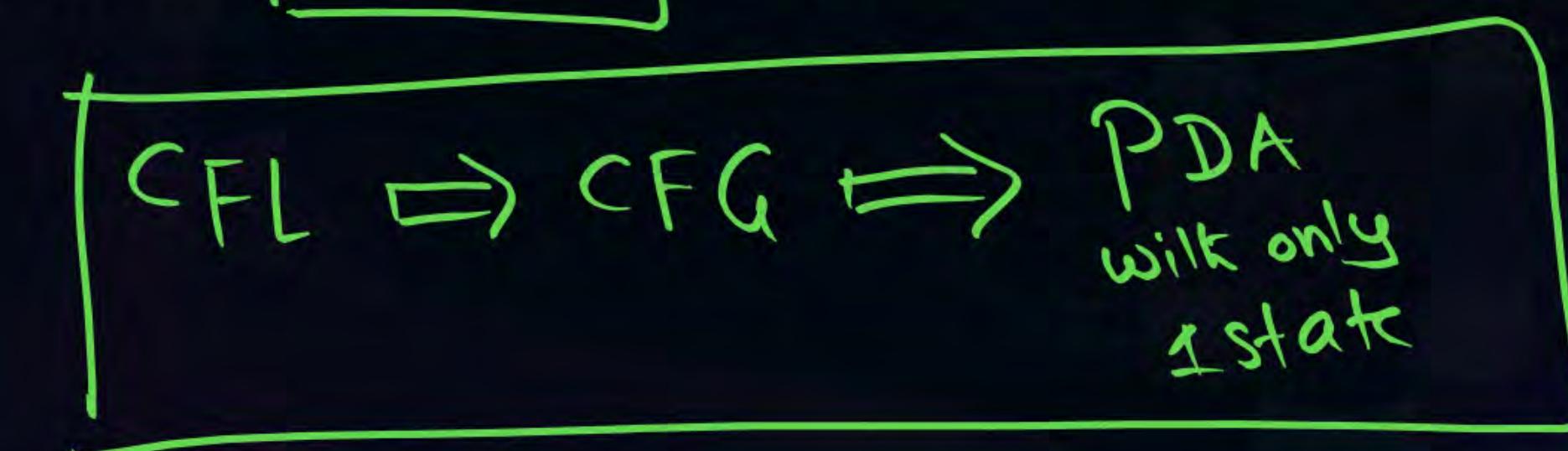
#Q95. Consider the following statements:

S<sub>1</sub>: only unambiguous context free grammar can be converted into Chomsky normal form. ~~False~~

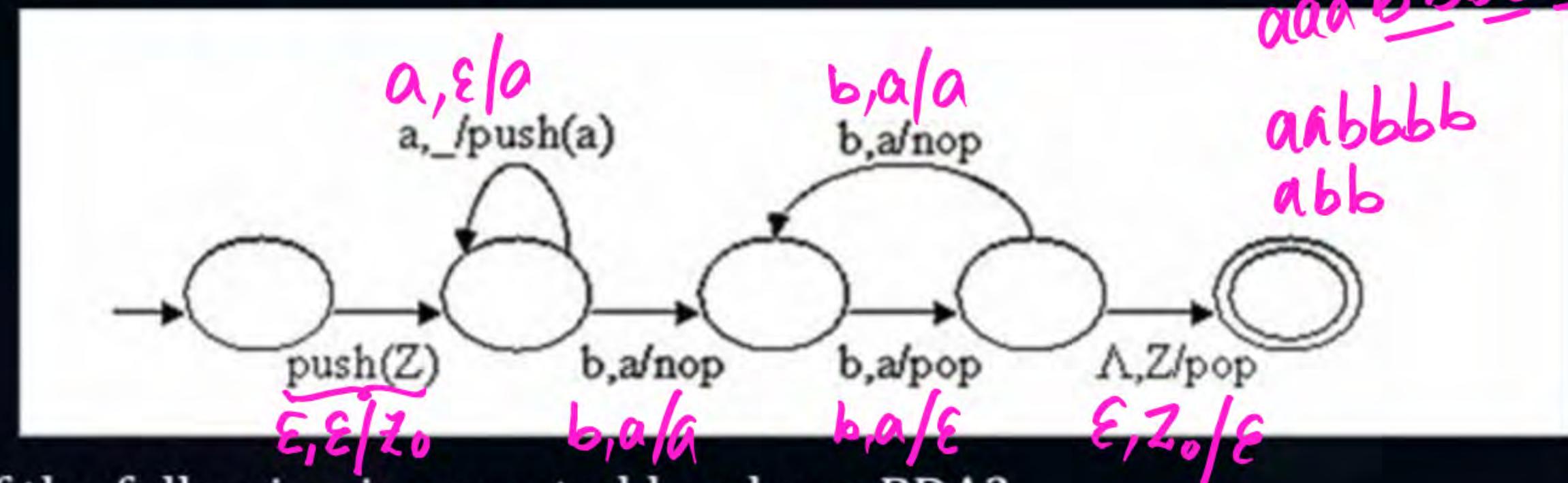
S<sub>2</sub>: A context free grammar can generate many languages but vice-versa is not true. ~~False~~

\*\*\* S<sub>3</sub>: For every CFL, there exist a PDA with one state. ~~True~~

How many statements are INCORRECT? = 2



#Q96. Assume stack is empty initially.



Which of the following is accepted by above PDA?

A

$$\{a^n b^n \mid n > 0\}$$

C

$$\{a^{2n} b^n \mid n > 0\}$$

B

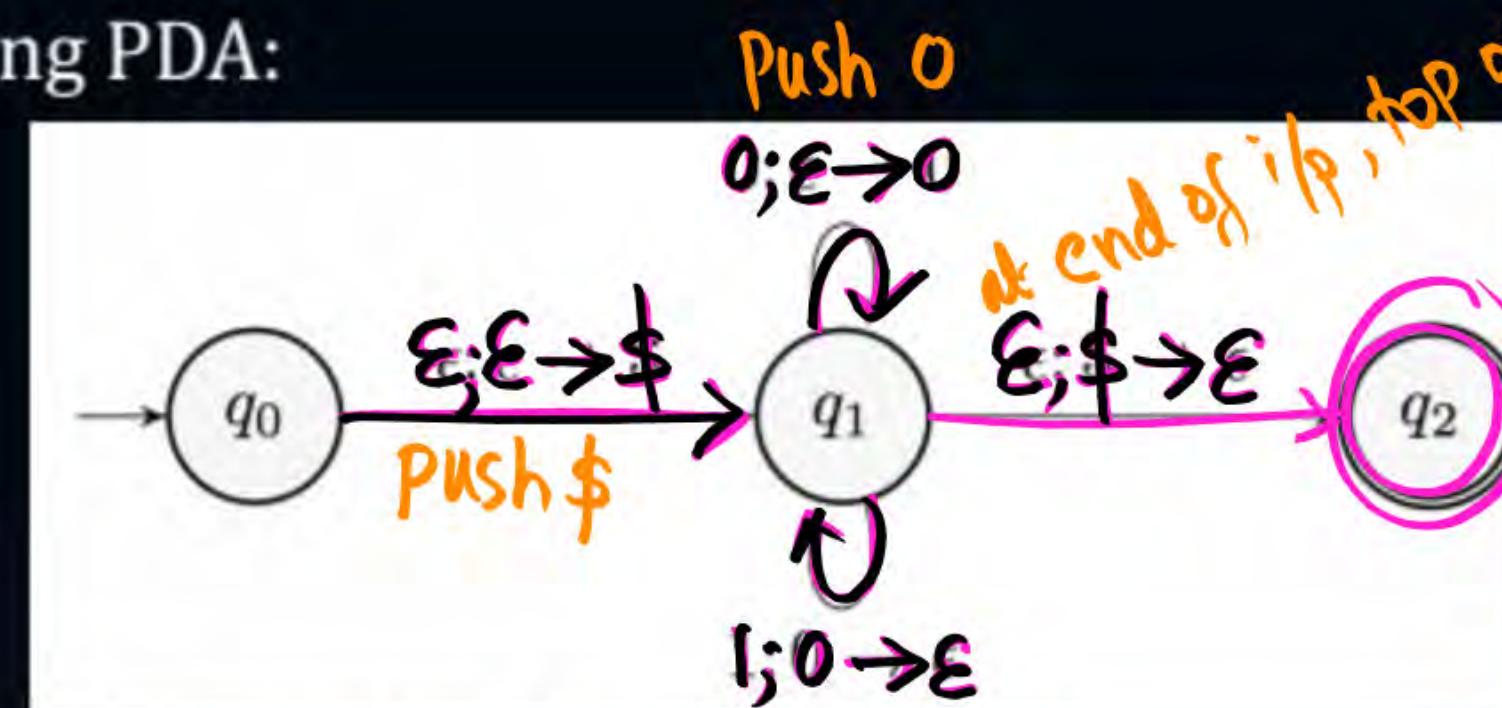
$$\{a^n b^{2n} \mid n > 0\}$$

D

None of these

#Q97. Consider the following PDA:

$\epsilon \checkmark$   
 $0 \times$   
 $1 \times$   
 $00 \times$   
 $01 \checkmark$



Which of the following is accepted by above PDA?

Pop 0 for 1

A

{ $w | w \in \{0,1\}^*, n_0(w) \geq n_1(w)$ }

C

{ $w | w \in \{0,1\}^*, n_0(w) = n_1(w)$ }

B

{ $w | w \in \{0,1\}^*, n_1(w) \geq n_0(w)$ }

D

None of these

$\{w | w \in \{0,1\}^*, n_0(w) = n_1(w)\}$ ,  
 $n_0(w) = n_1(w)$ ,  
every prefix of  $(w)$

must contain  
 $n_0 \geq n_1$

[MCQ]

P  
W

Initially stack is empty.

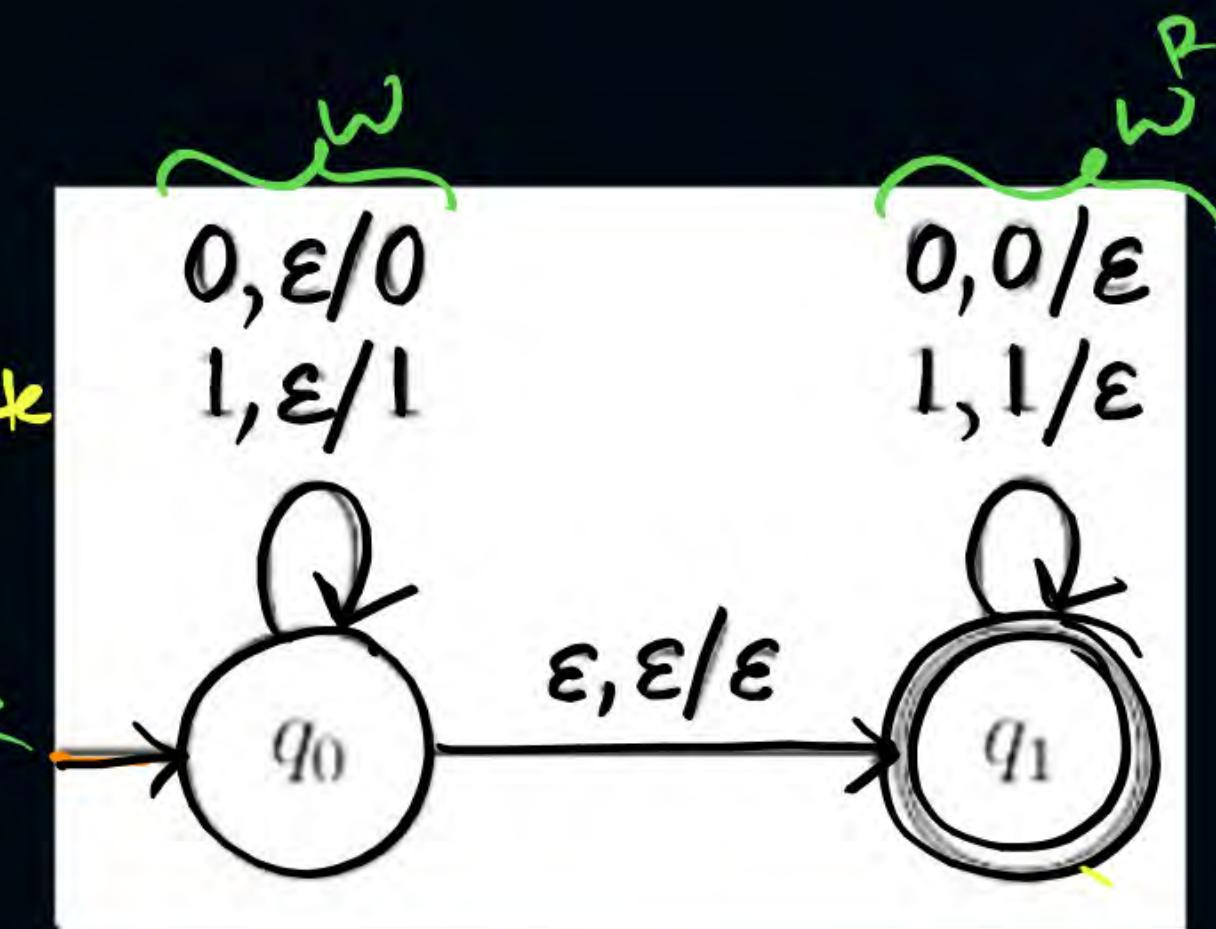
#Q98. Consider the following PDA:

Method I: If PDA uses Final state

then  $L = (0+1)^*$

Method II: If PDA uses Empty stack

then  $L = \omega\omega^R$



Which of the following is accepted by above PDA?

A

$$\{ww \mid w \in \{0,1\}^*\}$$

C

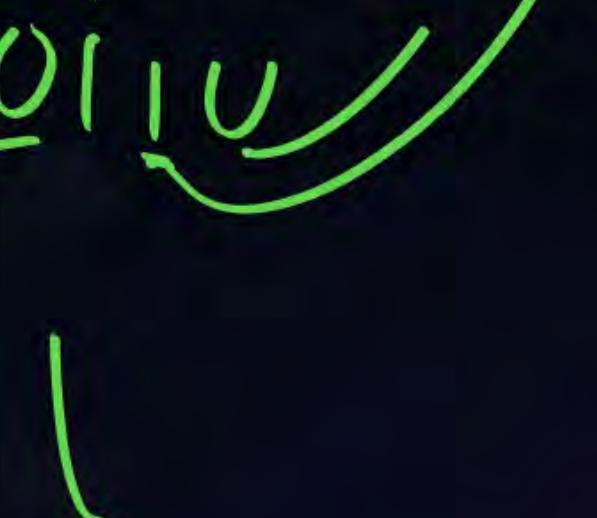
$$\{ww^R \mid w \in \{0,1\}^*\}$$

B

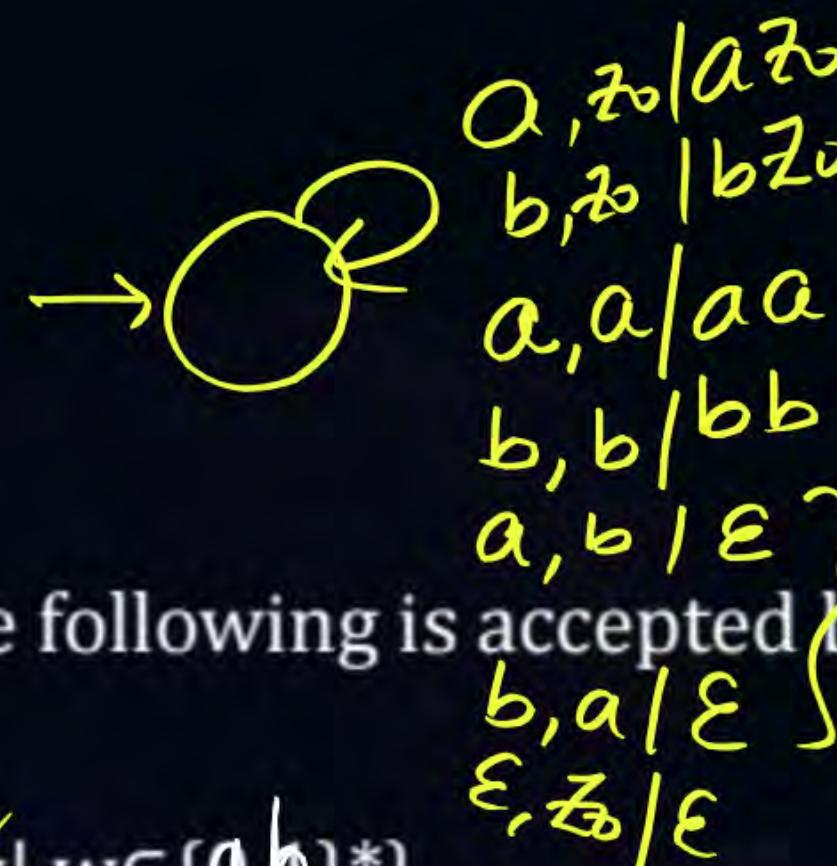
$$\{w \mid w \in \{0,1\}^*\}$$

D

None of these



#Q99. Consider the following PDA:



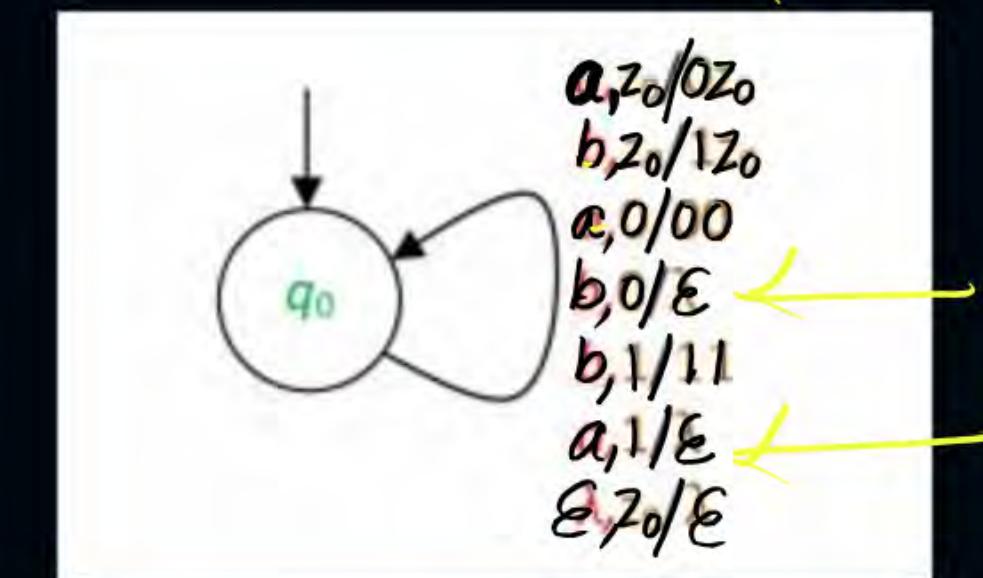
Which of the following is accepted by above PDA if it uses empty stack mechanism?

A

$\{w \mid w \in \{a, b\}^*\}$

C

$\{w \mid w \in \{a, b\}^*, n_a(w) \neq n_b(w)\}$



$$\lambda = \epsilon$$

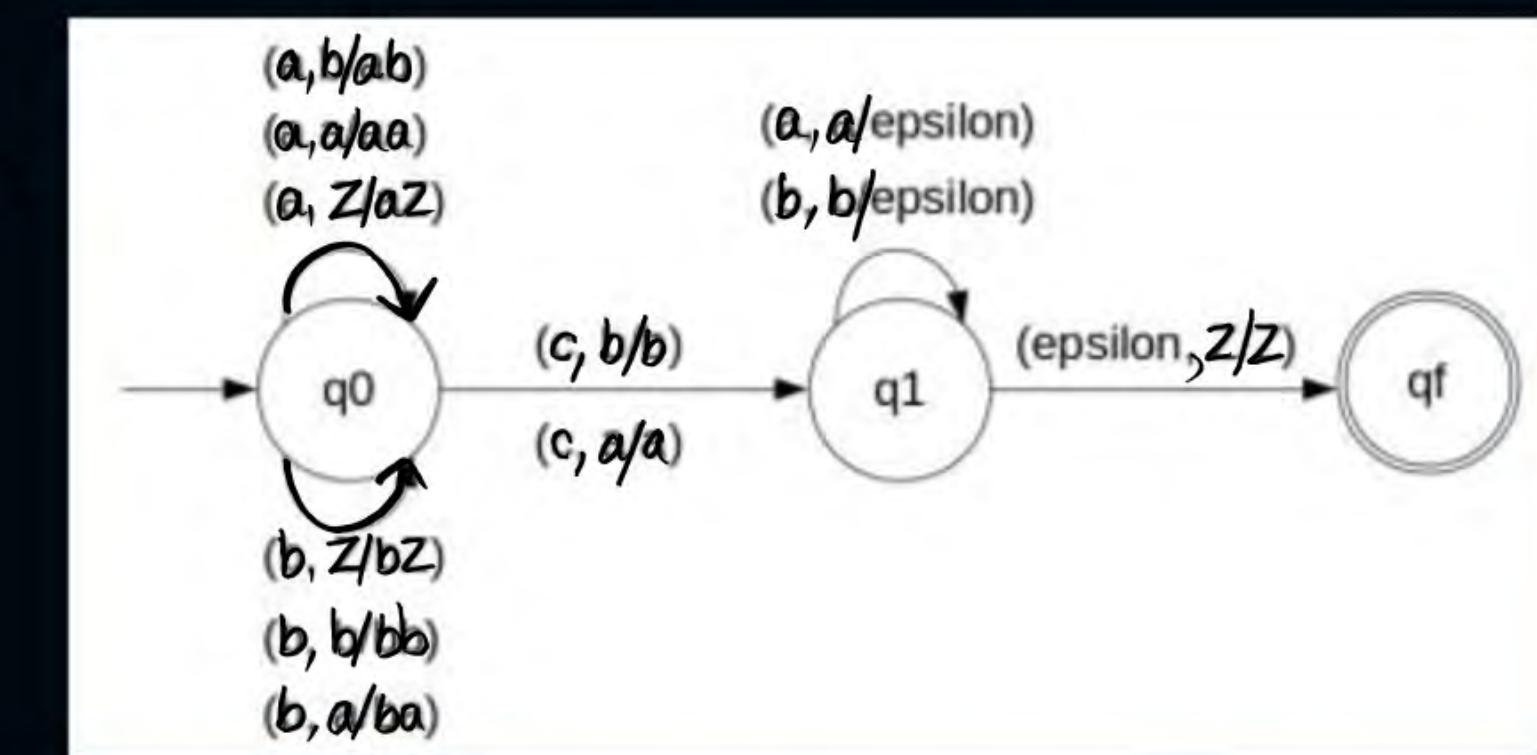
B

$\{w \mid w \in \{a, b\}^*, n_a(w) = n_b(w)\}$

D

None of these

#Q100. Consider the following PDA:



Which of the following is accepted by above PDA if it uses empty stack mechanism?

A

$$\{wcw \mid w \in \{a,b\}^*\}$$

C

$$\{ww^R \mid w \in \{a,b,c\}^*\}$$

B

$$\{wcw^R \mid w \in \{a,b\}^*\}$$

D

None of these

#Q101. Consider the following CFG:

$$\begin{aligned}S &\rightarrow S_1 | S_2 \\S_1 &\rightarrow X | XXS_1 \\S_2 &\rightarrow T_a T_b | T_b T_a \\T_a &\rightarrow X T_a X | a \\T_b &\rightarrow X T_b X | b \\X &\rightarrow a | b\end{aligned}$$

Which of the following is represented by above CFG?

**A**

Complement of  $\{ww \mid w \in \{a,b\}^*\}$

**B**

Complement of  $\{ww^R \mid w \in \{a,b\}^*\}$

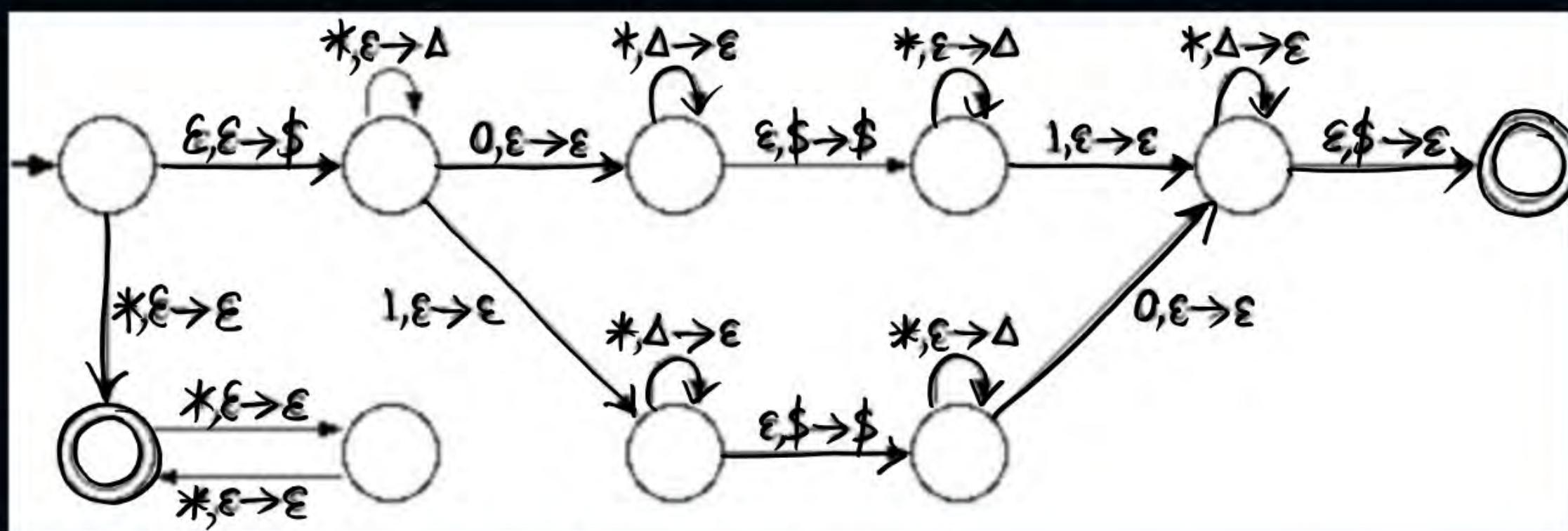
**C**

$\{ww^R \mid w \in \{a,b,c\}^*\}$

**D**

None of these

#Q102. Consider the following CFG: \$ is bottom of stack symbol. \* is either 0 or 1.



Which of the following is represented by above CFG?

**A**

Complement of  $\{ww \mid w \in \{a,b\}^*\}$

**B**

Complement of  $\{ww^R \mid w \in \{a,b\}^*\}$

**C**

$\{ww^R \mid w \in \{a,b,c\}^*\}$

**D**

None of these

#Q103. Consider the following CFG..

$$S \rightarrow 0S1S1S \mid 1S0S1S \mid 1S1S0S \mid \epsilon$$

Which of the following strings are generated by above CFG?

- A** Binary strings with twice as many 1's as 0's.
- B** Binary strings with twice as many 11's as 00's.
- C** Binary strings with twice as many 0's as 1's.
- D** None of these

#Q104. Consider the following CFG..

$$S \rightarrow AB \mid BA$$

$$A \rightarrow CAC \mid a$$

$$B \rightarrow CBC \mid b$$

$$C \rightarrow a \mid b$$

Which of the following strings are generated by above CFG?

**A**

$$\{xy \mid x,y \in \{0,1\}^*, |x|=|y|, x \neq y\}.$$

**B**

$$\{xy \mid x,y \in \{0,1\}^*, |x|=|y|\}.$$

**C**

$$\{xy \mid x,y \in \{0,1\}^*, x=y\}.$$

**D**

$$\{xy \mid x,y \in \{0,1\}^*, |x|=|y|, x=y\}.$$

#Q105. Consider the following CFG..

$$S \rightarrow 0A \mid 1B$$

$$A \rightarrow 0AA \mid 1S \mid 1$$

$$B \rightarrow 1BB \mid 0S \mid 0$$

Which of the following language is generated by above CFG?

**A**

$$\{w \mid w \in \{0,1\}^*, n_0(w) = n_1(w)\}.$$

**B**

$$\{w \mid w \in \{0,1\}^*, n_0(w) \neq n_1(w)\}.$$

**C**

$$\{w \mid w \in \{0,1\}^*, n_0(w) < n_1(w)\}.$$

**D**

$$\{w \mid w \in \{0,1\}^*, n_0(w) > n_1(w)\}.$$



THANK - YOU

# CS & IT ENGINEERING

## Theory of Computation

Lecture No.- 08

Mallesham Devasane Sir



# Recap of Previous Lecture



**Topic**

Regular Languages

**Topic**

Context Free Languages

# Topics to be Covered



Topic

Regular Languages

Topic

Context Free Languages

Topic

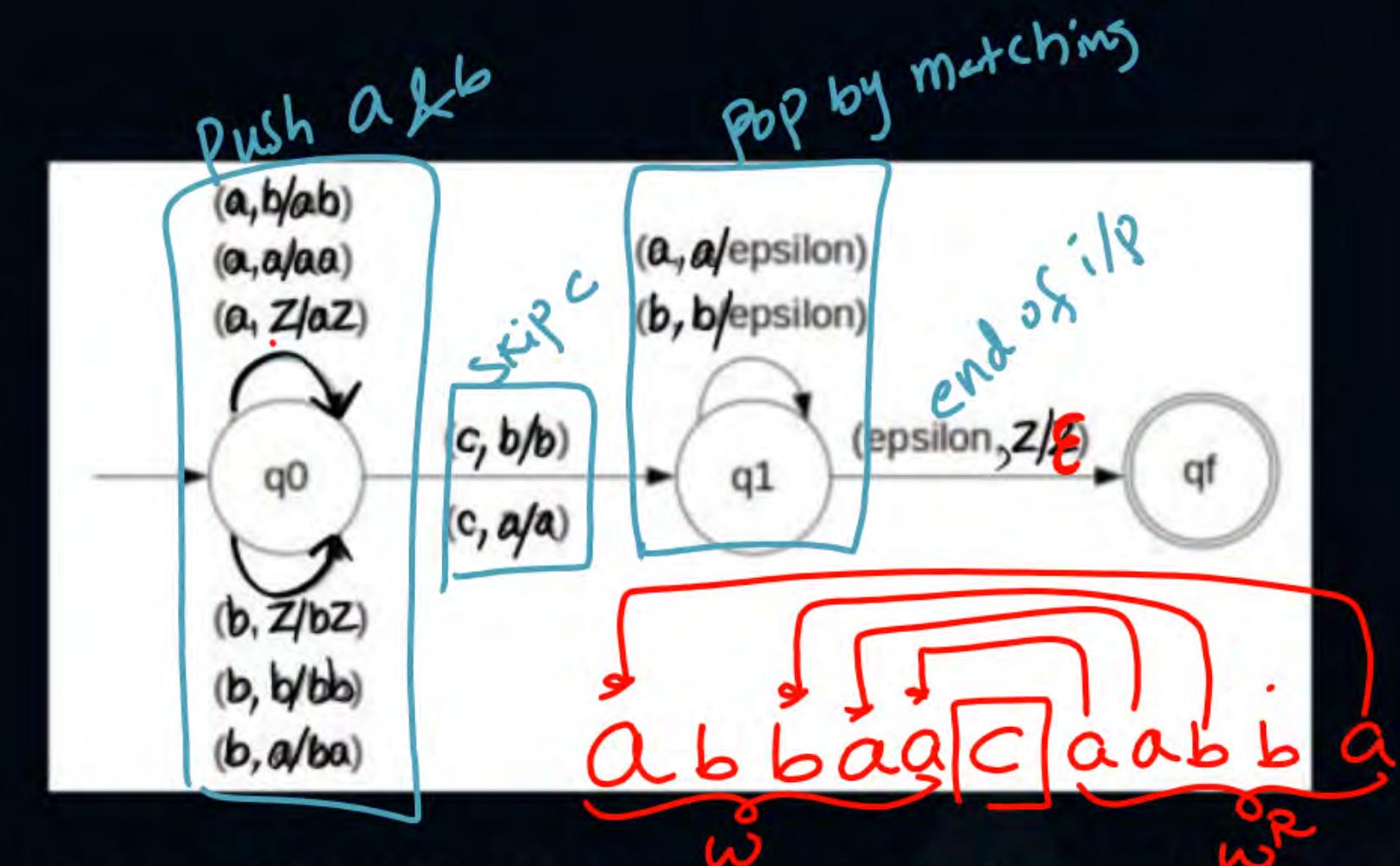
Turing Machine

Topic

Undecidability Concepts

#Q100. Consider the following PDA:

Initially  $z$  is on stack.



Which of the following is accepted by above PDA if it uses empty stack mechanism?

**A**

$\{wcw \mid w \in \{a,b\}^*\}$  *not F*

**C**

$\{ww^R \mid w \in \{a,b,c\}^*\}$

**B**

$\{wcw^R \mid w \in \{a,b\}^+\}$

**D**

None of these

#Q101. Consider the following CFG:

$S_2$  guarantees  
 ↳ generates even length  
 ↳ not  $ww$  form

$$\begin{aligned} S &\rightarrow S_1 | S_2 \\ S_1 &\rightarrow X | XXS_1 \\ S_2 &\rightarrow T_aT_b | T_bT_a \\ T_a &\rightarrow XT_aX | a \\ T_b &\rightarrow XT_bX | b \\ X &\rightarrow a | b \end{aligned}$$

$S_1 \Rightarrow$  odd length strings

$$S_2 \Rightarrow \left\{ w_1w_2 \mid w_1, w_2 \in \{a, b\}^*, |w_1| = |w_2|, w_1 \neq w_2 \right\}$$

Which of the following is represented by above CFG?

A

Complement of  $\{ww \mid w \in \{a, b\}^*\}$

C

$\{ww^R \mid w \in \{a, b, c\}^*\}$

B

Complement of  $\{ww^R \mid w \in \{a, b\}^*\}$

D

None of these

$L = \{ww \mid w \in \{a,b\}^*\}$   $\Rightarrow$  not CFL

$\overline{L} = \{\omega\omega \mid \omega \in \{a,b\}^*\} \Rightarrow$  CFL

$$L = \{ww \mid w \in \{a,b\}^*\} = \{\epsilon, aa, bb, aaaa, abab, baba, bbbb, \dots\}$$

$\cup$

= Set of all even length strings in  $ww$  form

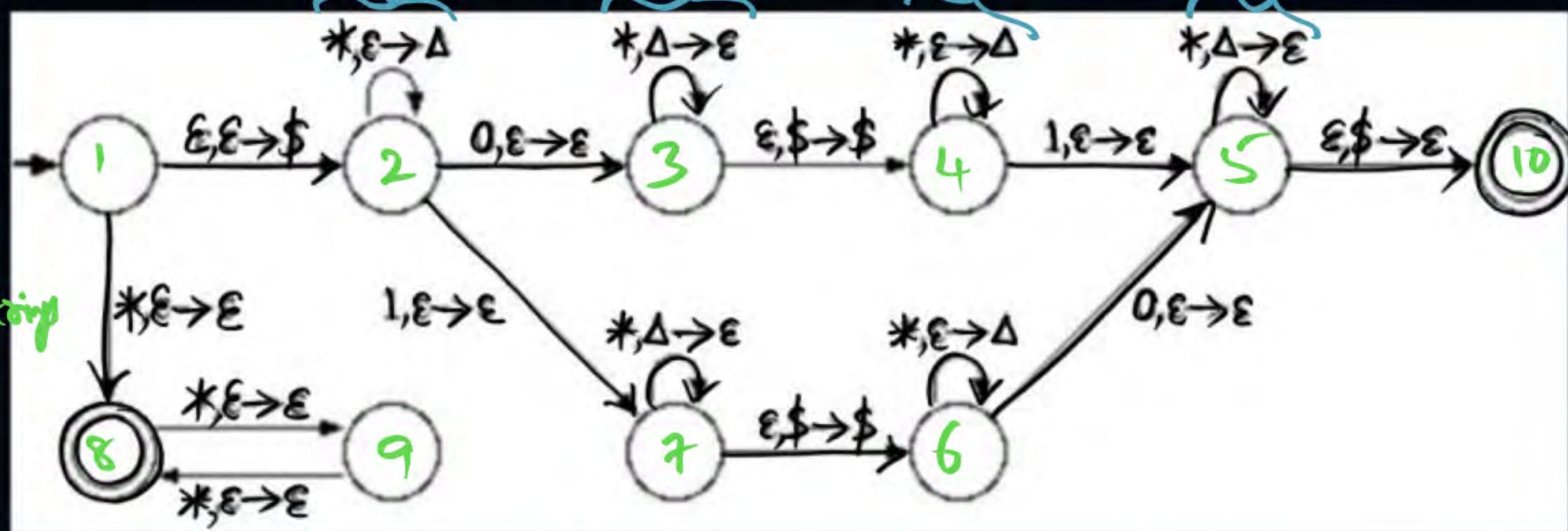
$$\bar{L} = \Sigma^* - L = (a+b)^* - L$$

= Set of all odd length strings  $\cup$  Set of all even lengths  
not in  $ww$  form

[NAT]

#Q102. Consider the following CFG. \$ is bottom of stack symbol. \* is either 0 or 1.

P  
W



Which of the following is represented by above CFG?

A

Complement of  $\{ww \mid w \in \{a,b\}^*\}$

B

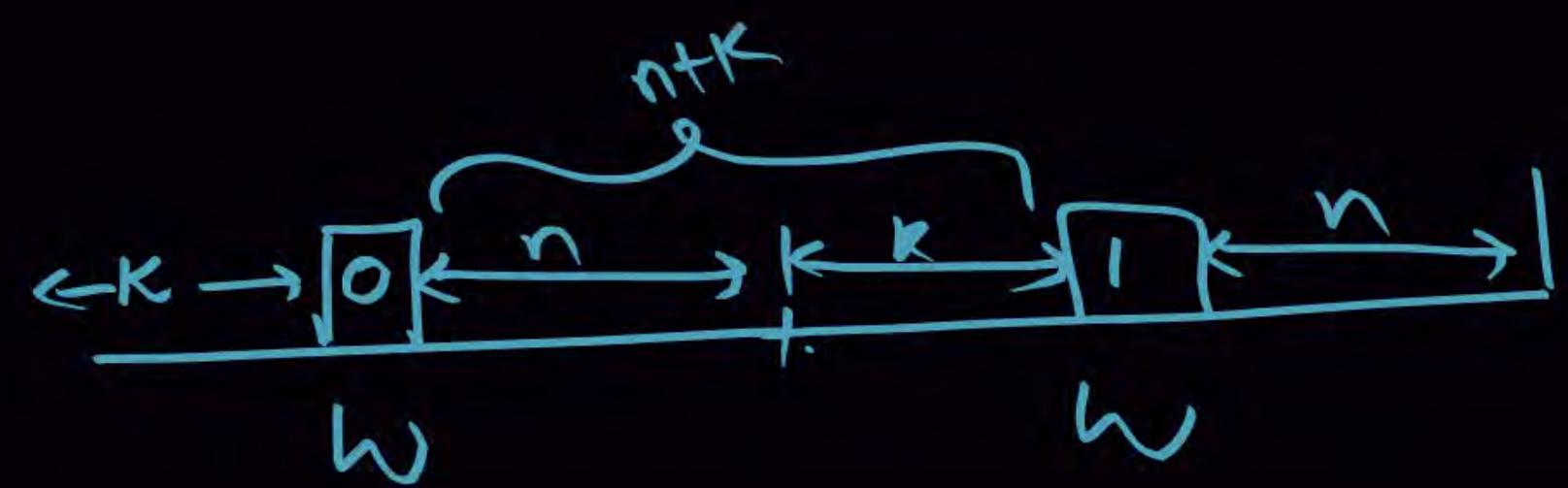
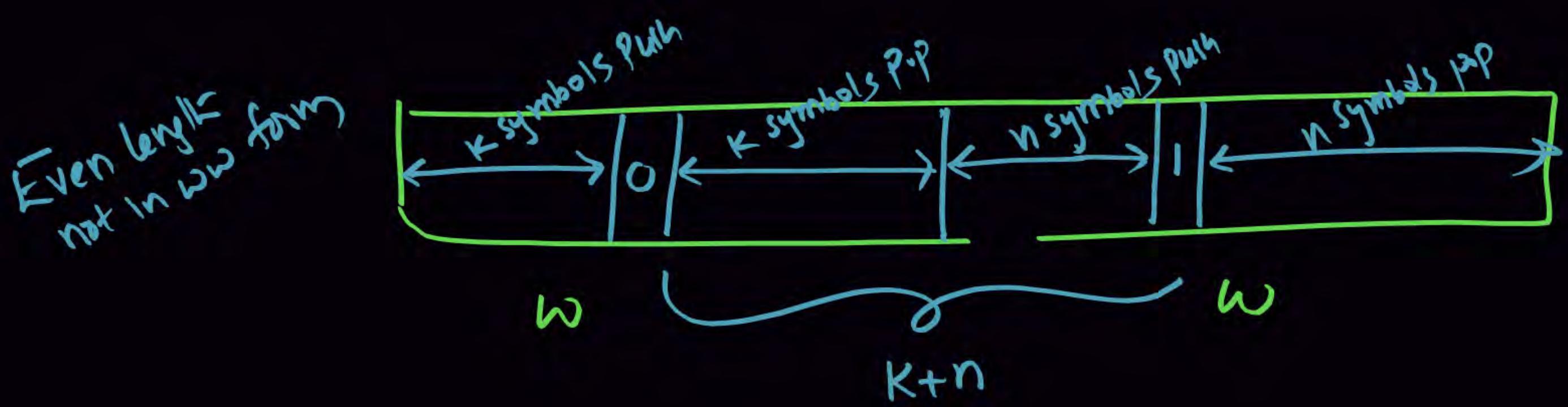
Complement of  $\{ww^R \mid w \in \{a,b\}^*\}$

C

$\{ww^R \mid w \in \{a,b,\$ \}^*\}$

D

None of these



$w \epsilon \{0,1\}^*$

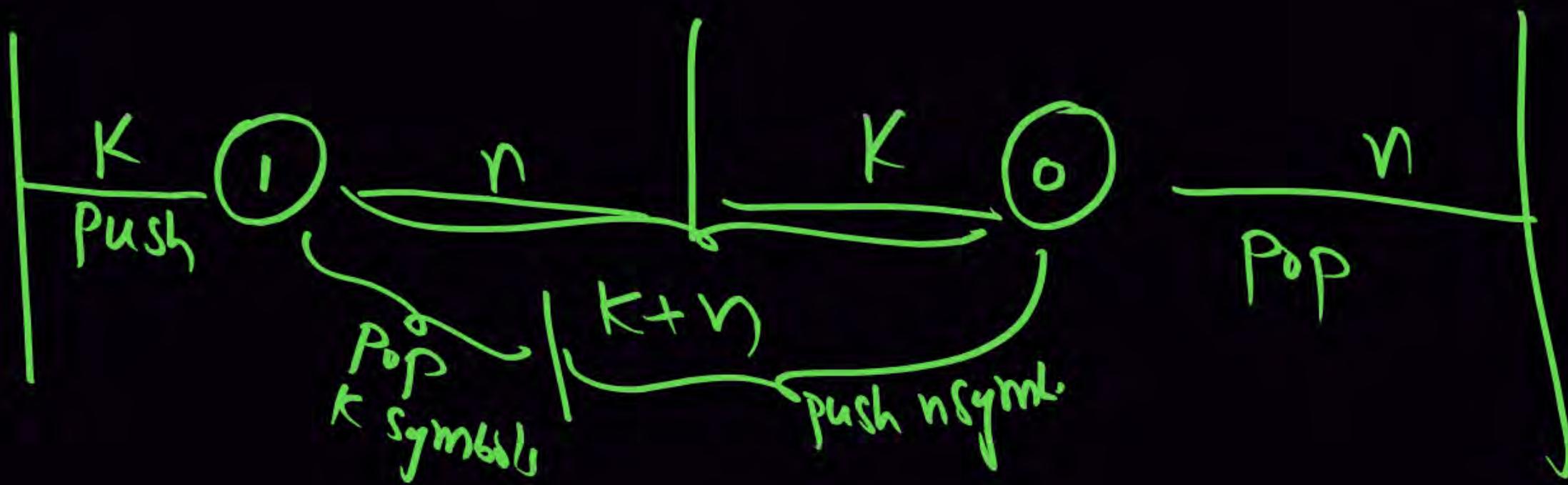
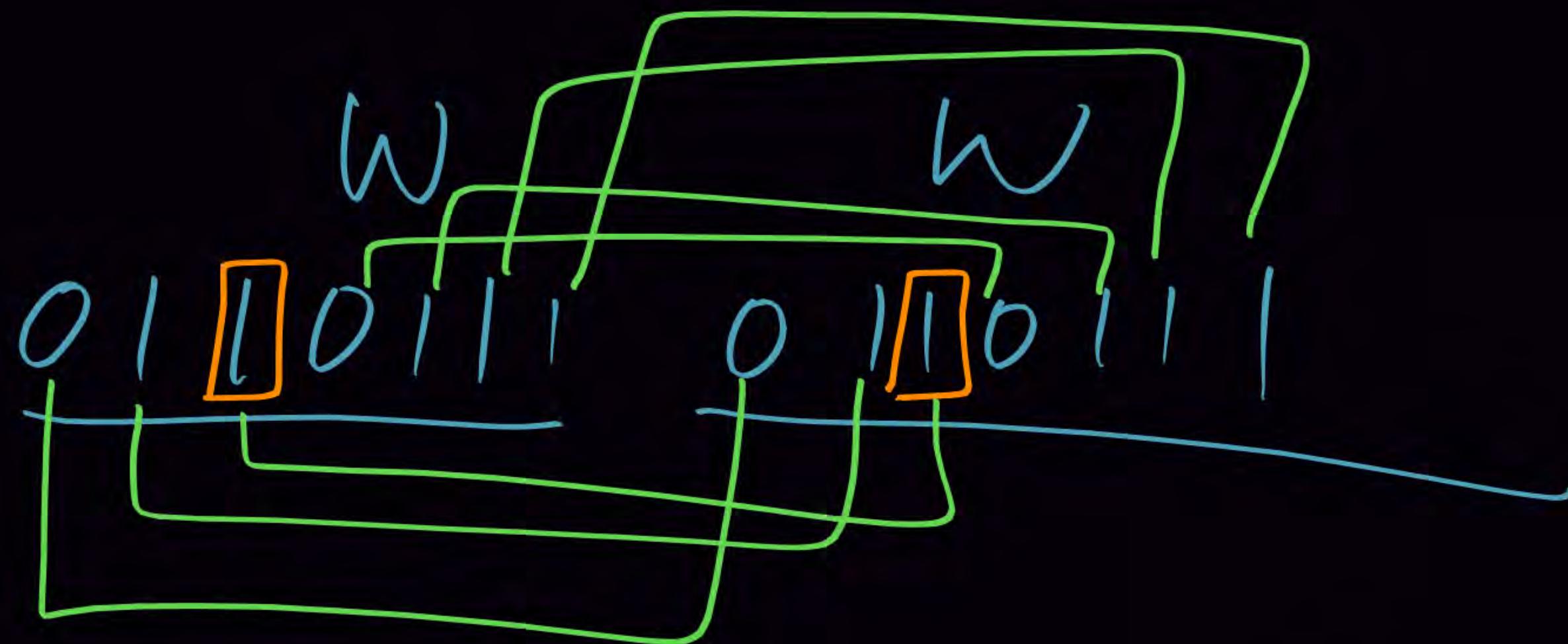
WW

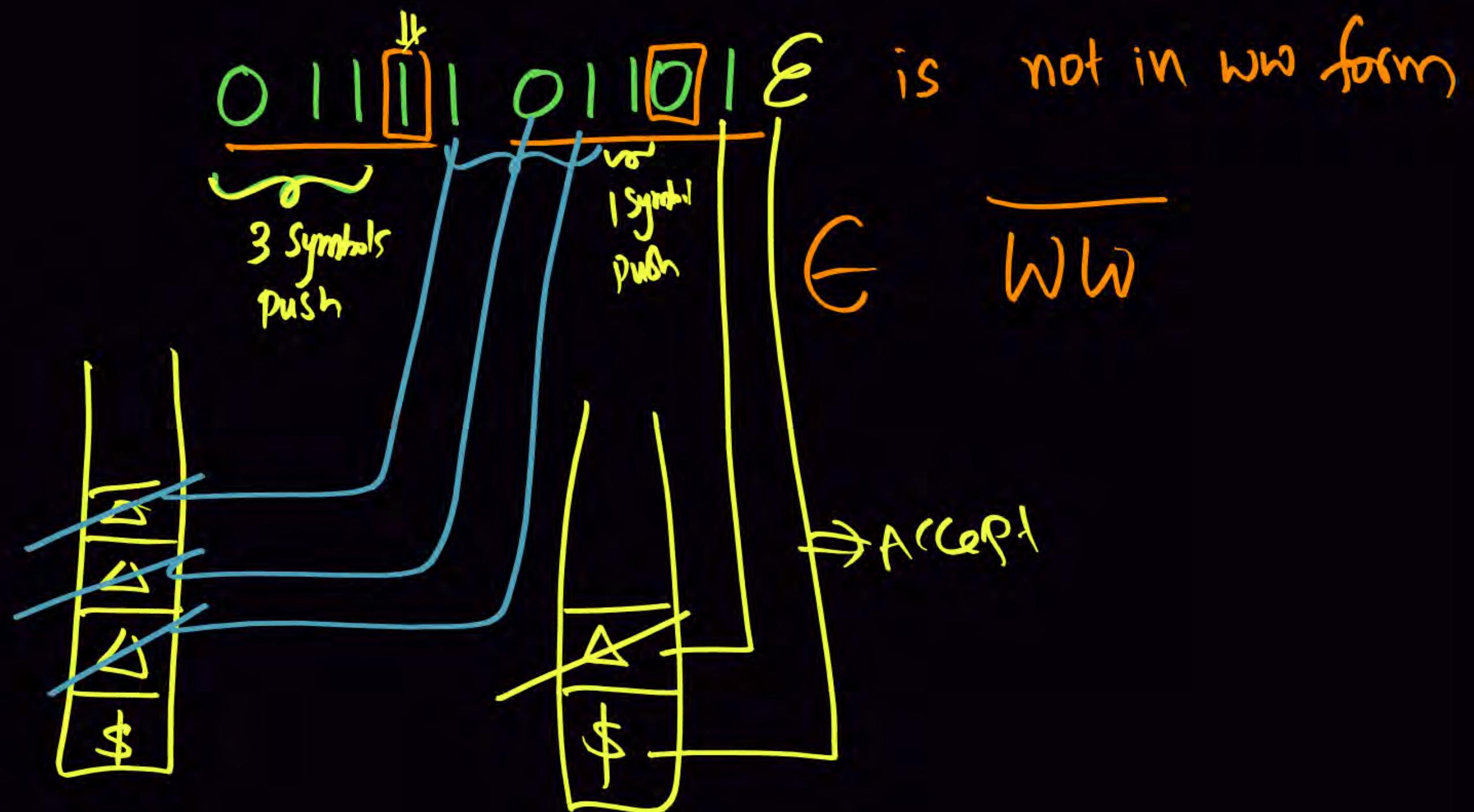


All odd length strings

All even length strings not in WW form

WW





#Q103. Consider the following CFG..

$$S \rightarrow 0S1S1S \mid 1S0S1S \mid 1S1S0S \mid \epsilon$$

$\epsilon \checkmark$   
 $011 /$   
 $101 /$   
 $110 /$

Which of the following strings are generated by above CFG?

~~A~~  $n_1(\omega) = 2 n_0(\omega)$

Binary strings with twice as many 1's as 0's.

C Binary strings with twice as many 0's as 1's.

B

Binary strings with twice as many 11's as 00's.

D

None of these

$n_0(\omega) = \frac{1}{2} n_1(\omega)$

#Q104. Consider the following CFG..

$$S \rightarrow AB \mid BA$$

$$A \rightarrow CAC \mid a$$

$$B \rightarrow CBC \mid b$$

$$C \rightarrow a \mid b$$

Which of the following strings are generated by above CFG?

**A**

$$\{xy \mid x,y \in \{0,1\}^*, |x|=|y|, x \neq y\}.$$

**C**

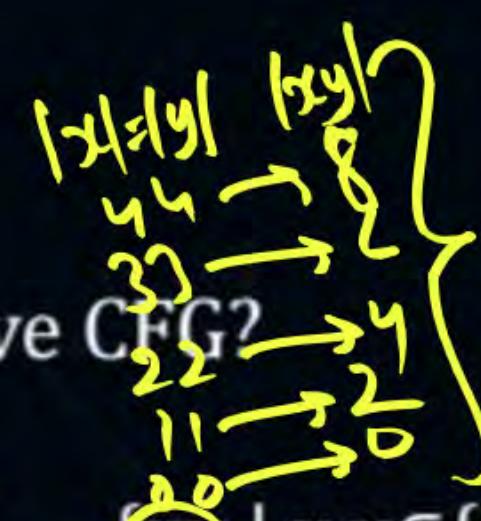
$$\{xy \mid x,y \in \{0,1\}^*, x=y\}.$$

**B**

$$\{xy \mid x,y \in \{0,1\}^*, |x|=|y|\}.$$

**D**

$$\{xy \mid x,y \in \{0,1\}^*, |x|=|y|, x=y\}.$$



$$\left( \left( 0^k \right)^2 \right)^*$$

"Set of all even length strings"

#Q105. Consider the following CFG..

$$S \rightarrow 0A \mid 1B$$

$$A \rightarrow 0AA \mid 1S \mid 1$$

$$B \rightarrow 1BB \mid 0S \mid 0$$

$$L = \{0^l, 1^0, 00^{ll}, 1100, 0101, 0110, \dots\}$$

Which of the following language is generated by above CFG?



**A** { $w \mid w \in \{0,1\}^*, n_0(w) = n_1(w)$ }.



**C** { $w \mid w \in \{0,1\}^*, n_0(w) < n_1(w)$ }.



**B** { $w \mid w \in \{0,1\}^*, n_0(w) \neq n_1(w)$ }.



**D** { $w \mid w \in \{0,1\}^*, n_0(w) > n_1(w)$ }.

#Q106. Suppose L1 and L2 are Turing Recognizable Languages.

Which of the following is Turing Recognizable?

A

$$L_1 \cup L_2 = \text{REL}, \cup \text{REL}_2 \Rightarrow \text{REL}$$

C

$$L_1 - L_2 = \text{REL}_1 - \text{REL}_2 \Rightarrow \text{Need not be REL}$$

$$L_1 - L_2 = L_1 \cap \overline{L_2}$$

- X

B

$$L_1 \cap L_2$$

D

$$L_1 L_2$$

$$\text{REL}_1 \cdot \text{REL}_2 \Rightarrow \text{REL}$$

CDSFI

RELs



Complement

Difference

Not closed

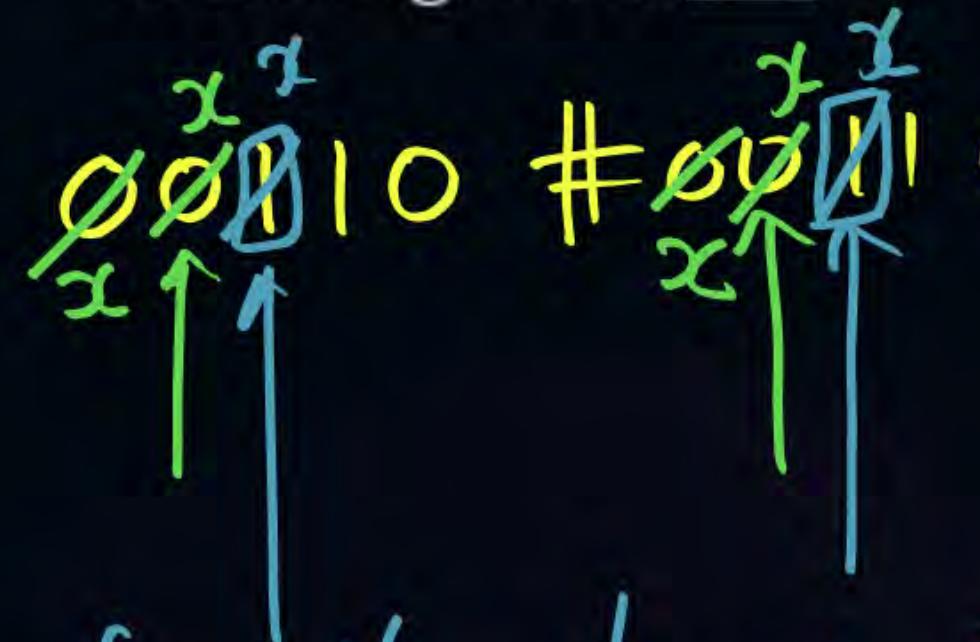
Subset

Inf . . .

Finite Difference

[MCQ]

#Q107. Language accepted by following TM is —



$$\{w\#w \mid w \in \{0,1\}^*\}$$

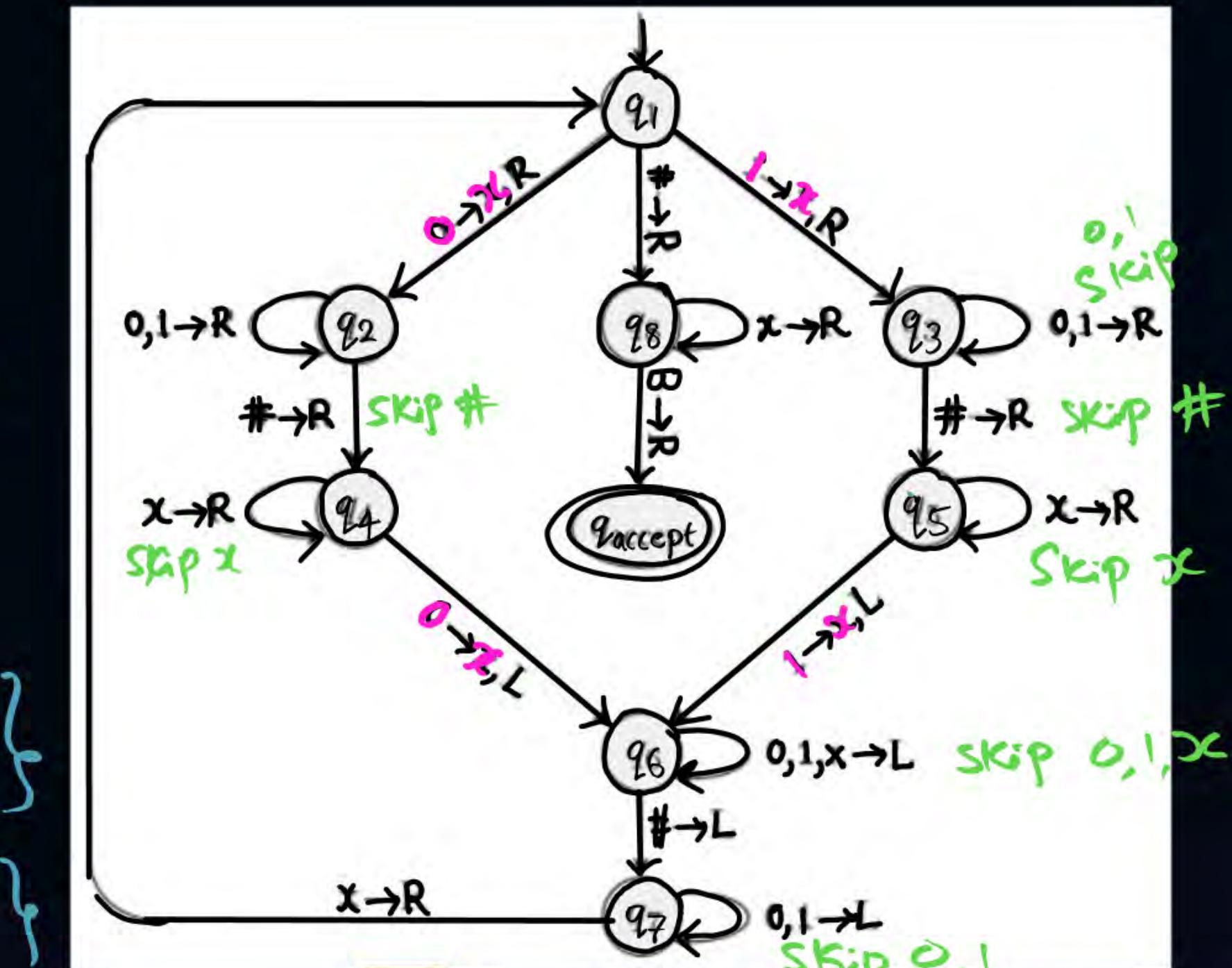
$$= \{\#, 0\#0, 1\#1, \dots\}$$

A

$$\{ww \mid w \in \{a,b\}^*\}$$

C

$$\{ww^R \mid w \in \{a,b,c\}^*\}$$



B

$$\text{Complement of } \{ww^R \mid w \in \{a,b\}^*\}$$

D

None of these

#Q108. How many of the following statements are equivalent to TM?

- 1. Multi-tape Turing machines
- 2. Turing machines with Bi-infinite Tape
- 3. Nondeterministic Turing machines
- 4. Postmachines or Queue automaton
- 5. PDAs with two stacks
- 6. Counter machines

✓ 6

Equivalent  
to TM

DTM

NTM

UTM

2 stack PDA

one way infinite tape TM  
2-way " " TM

Single head TM

multi head TM

1-D tape TM

2-D tape TM

:

#Q109. Which of the following does by Turing Machine?



Sorting a list



Graph Search



String Matching



Searching a list

Program

$\cong$

TM

$\cong$

Computer

Algorithm

$\cong$

Halting program

$\cong$

HIM

#Q110. Which of the following is countable?

A

Set of binary strings  $= \sum^* = (0+1)^*$

C

Set of RELs

$L = \{ \text{REL}_1, \text{REL}_2, \text{REL}_3, \dots \}$

→ It is also REL  
TM exist

B

$L = \{ R_1, R_2, R_3, \dots \}$

Set of regular languages

D

None of these

all countable sets

all RELs

- $\Sigma^*$
- set of all regulars
- set of all RELs

#Q111. Which of the following is TRUE?

1. If both L and complement of L are RE ,then L is recursive.
2. If L is recursive then so is the complement of L.

**A**

Only 1

**C**

Both 1 and 2

**B**

Only 2

**D**

None of these

#Q112. Which of the following L is Recursively Enumerable Language?

**A**

L is Regular

**C**

L is Enumerable

**B**

L is Decidable

**D**

L is Undecidable

#Q113. If L is recursive language, then complement of L is \_\_



Recursive



RE



Undecidable



CFL

#Q114. Consider the following statements.

- I. Every decidable set is countable
- II. Every RE set is countable
- III. Every countable set is RE

How many of the above statements is/are true?

**A**

0

**C**

2

**B**

1

**D**

3

#Q115. Complement of not REL is \_\_\_\_\_



A Recursive



REL



B Undecidable



D None of these

$X$  is countable set

iff

$f: X \rightarrow Y$  is Bijective  
where  $Y$  is known countable.



THANK - YOU

# CS & IT ENGINEERING

## Theory of Computation

Lecture No.- 09

Mallesham Devasane Sir



# Recap of Previous Lecture



Topic

Regular Languages

Topic

Context Free Languages

Topic

Turing Machine

Topic

Undecidability Concepts

# Topics to be Covered



Topic

Regular Languages

Topic

Context Free Languages

Topic

Turing Machine

Topic

Undecidability Concepts

#Q111. Which of the following is TRUE?

1. If both L and complement of L are RE ,then L is recursive. T
2. If L is recursive then so is the complement of L. T



Only 1



Both 1 and 2



Only 2



None of these

#Q112. Which of the following L is Recursively Enumerable Language?

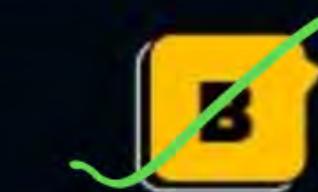
Dec ✓  
Reg ✓  
Enu ✓  
Unde ✗



L is Regular



L is Enumerable

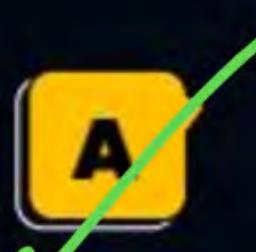


L is Decidable



L is Undecidable

#Q113. If L is recursive language, then complement of L is Recursive  
REL



Recursive



RE



Undecidable



CFL

#Q114. Consider the following statements.

- I. Every decidable set is countable **T**
- II. Every RE set is countable **T**
- III. Every countable set is RE **False**

How many of the above statements is/are true?

**A**

0

**B**

1

**C**

2

**D**

3

#Q115. Complement of not REL is \_\_\_\_\_

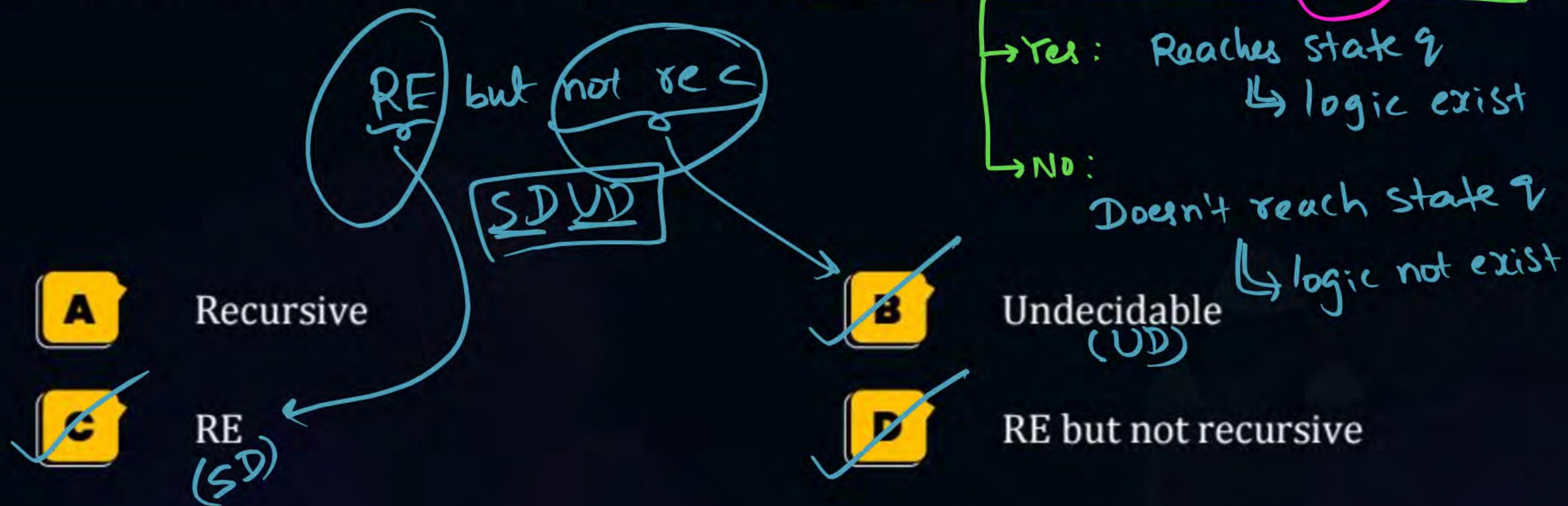
Not REL  $\Rightarrow$  RE but not rec  
OR  
Not REL } = Never dec  
} = UD  
} = Not rec

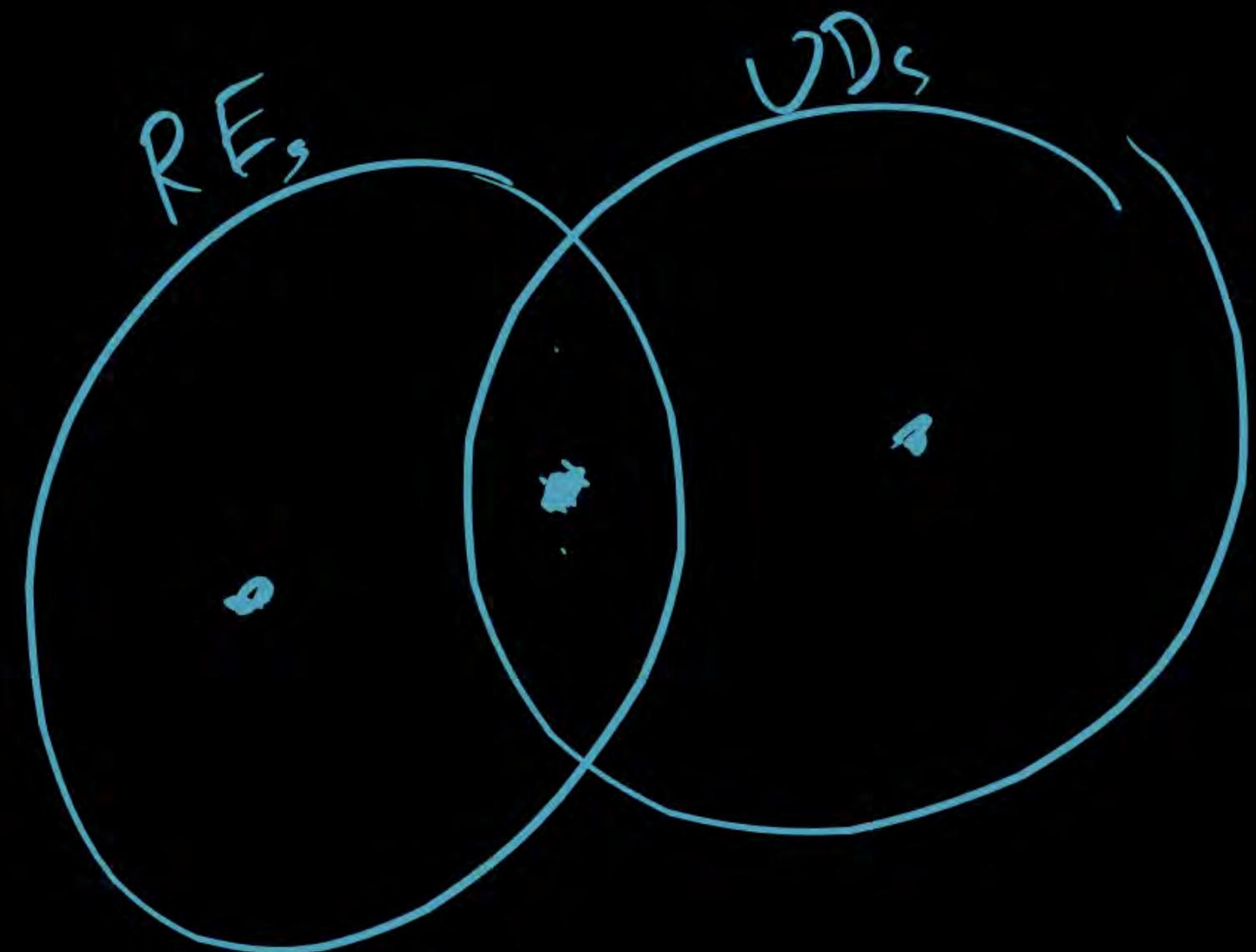
- A Recursive
- B Undecidable
- C REL
- D None of these

## State Entry Problem

#Q116. Given a TM 'M' and a state 'q' of M, does M ever enter state q on some input?

Particular





→ TM

#Q117. Does 'M' ever enter state 'q' on **input 'abb'**?

RE but not rec  
(SDUD)



Recursive



RE

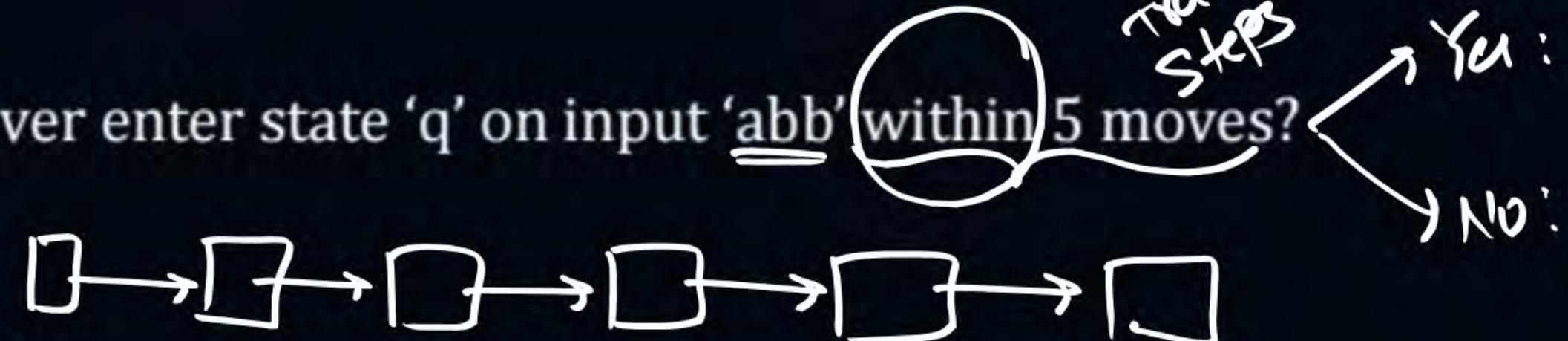


Undecidable



None of these

#Q118. Does 'M' ever enter state 'q' on input 'abb' within 5 moves?



- A Recursive
- C REL

- B Undecidable
- D ~~No of the~~  
RE but not Rec

#Q119. "TM accepts epsilon" is \_

IS  $\epsilon \in L(TM)$  ?

IS TM accepts  $\epsilon$  ?  
(membership)

Yes:  $\epsilon$  accepted by TM logic ✓

No:  $\epsilon$  not accepted by TM logic ✗

A

Recursive

C

RE

B

Undecidable

D

None of these  
RE but not recursive

#Q120. "TM accepts only epsilon" is \_\_

IS  $L(TM) = \{\epsilon\}$  ?

Yes:

TM should accept  $\epsilon$  and TM should not accept any other string

No:

TM may accept nothing  
OR

TM should accept some string other than  $\epsilon$

Undecidable

logic X

than  $\epsilon$

Not RE

A

Recursive

C

REL

B

D

None of these

#Q121. Which of the following problem is Decidable for TM?



- A** Membership
- B** Halting
- C** Equivalence
- D** None of these

#Q122. Which of the following problem is RE but not recursive for TM?

A

Membership  
Yes  $\Rightarrow$  logic ✓  
No  $\Rightarrow$  logic ✗

C

Finiteness  
Yes  $\Rightarrow$  logic ✗  
No  $\Rightarrow$  logic ✗

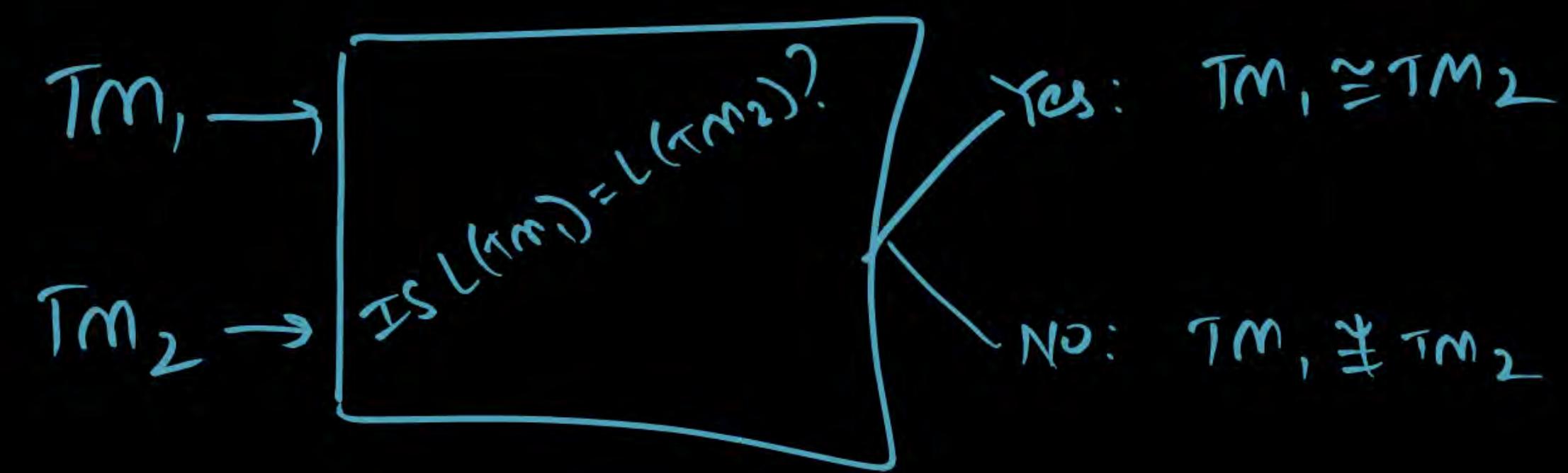
B

Halting  
Yes  $\Rightarrow$  logic ✓  
No  $\Rightarrow$  logic ✗

D

None of these  
Equivalent

# Äquivalenz für TM



**[MCQ]**

#Q123. {M | L(M) is regular language}

Whether M accepts regular  
↓  
Not P.C

$$L = \{M_1, M_2, \dots\}$$

$$\overline{L} = \{M'_1, M'_2, \dots\}$$

**A**

Recursive

**C**

Regular

**B**

REL

**D**

None of these

IS TM accepts regular language?

IS " " finite " ?  $\Rightarrow$  Not RE

IS " " CFL ?

IS " " CSL ?

IS " " Recursive ?

Trivial IS " " REL ?  $\Rightarrow$  decidable

#Q124. {M | M halts on all inputs within 100 steps}

Yes: upto 100 lengths, all halts  
within 100 moves

No: atleast one string within 100 length  
strings takes  $10^{16}$  move.

$$\Sigma^* = \{ \epsilon, a, b, aa, ab, ba, bb, \dots \}$$

3 length,  
4 length,  
5 length,  
100 length,

Recursive



REL



REL but not recursive  
None of these

#Q125. {M | M halts on all inputs after 100 steps}  $\Rightarrow$  Check upto 100 length strings

M should not halt within 100 steps

for every input

Verify each string should take  
101<sup>st</sup> more

I will write GATE exam after <sup>next</sup> year

I may write GATE after 2025  
OR  
I may not write



Recursive



Regular



REL



None of these

I will check upto 2 years



THANK - YOU

# CS & IT ENGINEERING

## Theory of Computation

Lecture No.- 10

Mallesham Devasane Sir



# Recap of Previous Lecture



Topic

Regular Languages

Topic

Context Free Languages

Topic

Turing Machine

Topic

Undecidability Concepts



# Topics to be Covered



Topic

Regular Languages

Topic

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Topic

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Topic

Undecidability Concepts

#Q126. Which of the following is TRUE?

*Myhill-Nerode Theorem*

1. L is regular if and only if  $\equiv_L$  has a finite number of equivalences classes.
2. L is not regular if and only if  $\equiv_L$  has an infinite number of equivalences classes.

A

Only 1

C

Both 1 and 2

B

Only 2

D

None of these

#Q127 . Which of the following is countable?

- A** Set of finite languages  $\{L \mid L \text{ is finite}\}$
- C** Set of regular languages  $\{L \mid L \text{ is Regular}\}$
- B** Set of languages  $= \mathcal{Q} = P(\Sigma^*)$
- D** Set of strings  $= \Sigma^*$
- Handwritten annotations:
- A is crossed out with a yellow marker.
  - C has a yellow checkmark.
  - B is crossed out with a yellow marker.
  - D is crossed out with a yellow marker.
  - The set of finite languages is labeled  $\{L \mid L \text{ is finite}\}$  in yellow above A.
  - The set of regular languages is labeled  $\{L \mid L \text{ is Regular}\}$  in yellow below C.
  - The set of languages is labeled  $\mathcal{Q} = P(\Sigma^*)$  in yellow next to B.
  - The set of strings is labeled  $\Sigma^*$  in yellow next to D.
  - An arrow points from the handwritten "uncountable" label to the set of languages B.

Set of languages :

$$\{ \{ \} ; \{ s \} , \{ a \} , \{ b \} , \{ aa \} , \{ ab \} , \dots ; \{ \epsilon, a \} , \{ \epsilon, b \} , \{ a, b \} , \{ \epsilon, aa \} , \dots ; \{ \epsilon, a, b \} , \{ \epsilon, a, aa \} , \dots ; \}$$

Set of strings over  $\Sigma$

$$=\Sigma^*$$

$$=\{ \underset{1}{\varepsilon}, \underset{2}{a}, \underset{3}{b}, \underset{4}{aa}, \underset{5}{ab}, \underset{6}{ba}, \underset{7}{bb}, \dots \}$$

N:    |    2    3    4    5    6    7

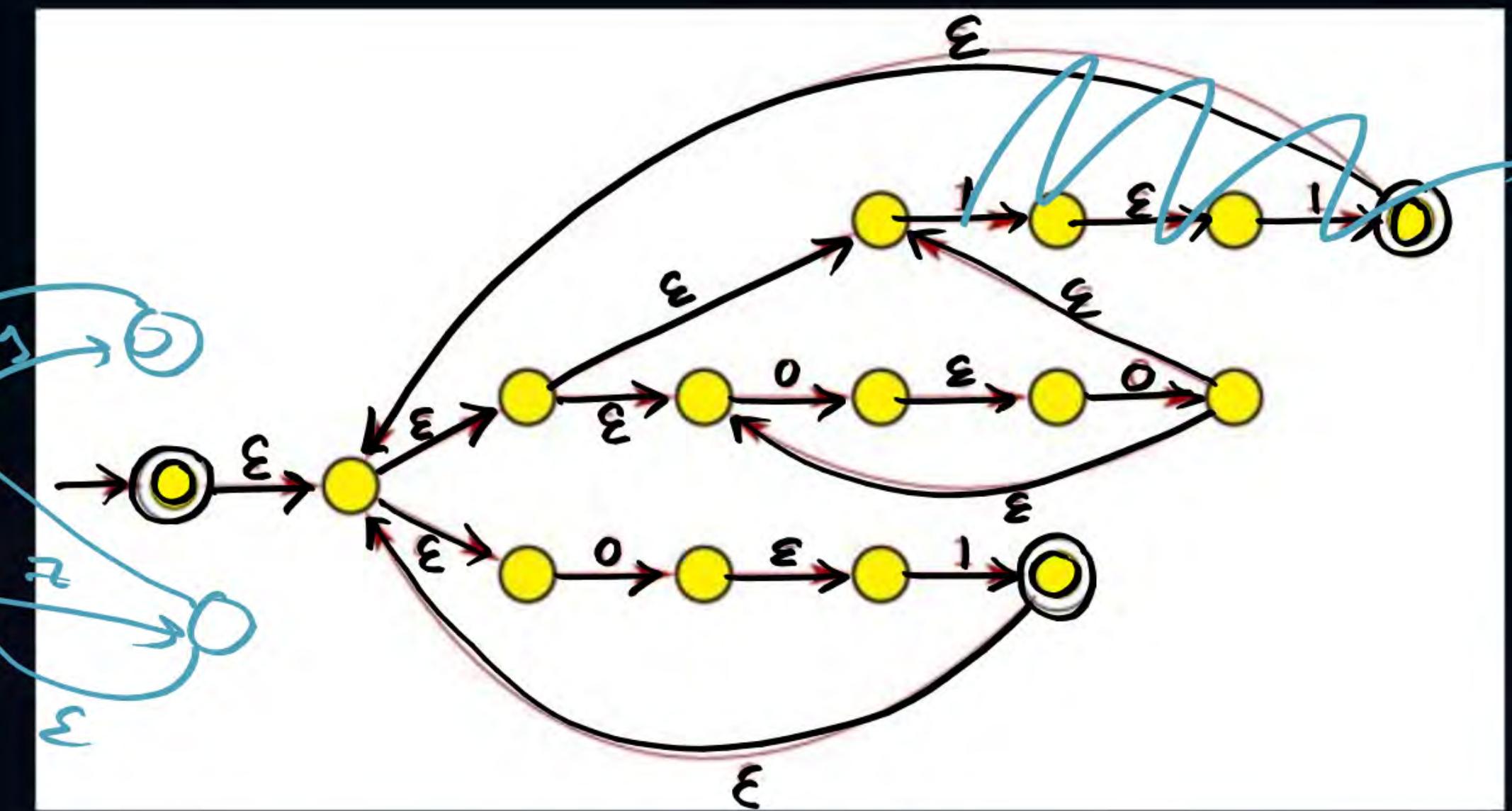
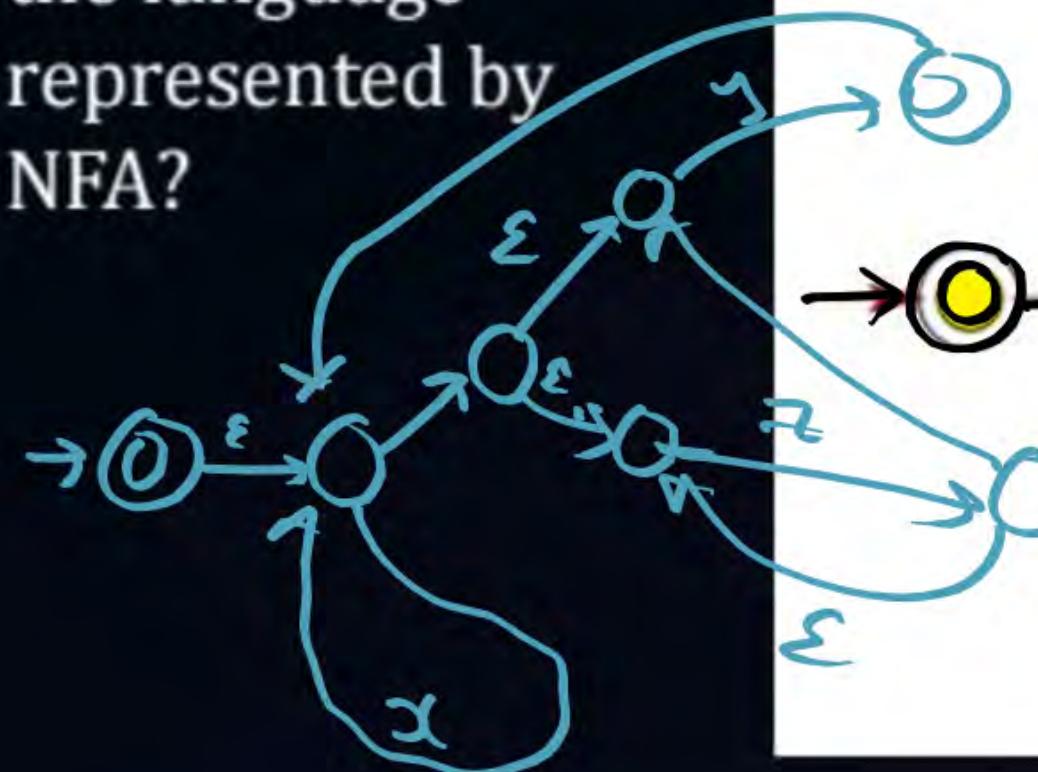
f:  $\Sigma^* \rightarrow N$  is Bijective

$X$  is countable

iff

$f: X \rightarrow$  known countable set is Bijective

#Q128. What is the language represented by NFA?



A

$$((00)^* + 11 + 01)^*$$

C

$$((00)^*(11+01))^*$$

B

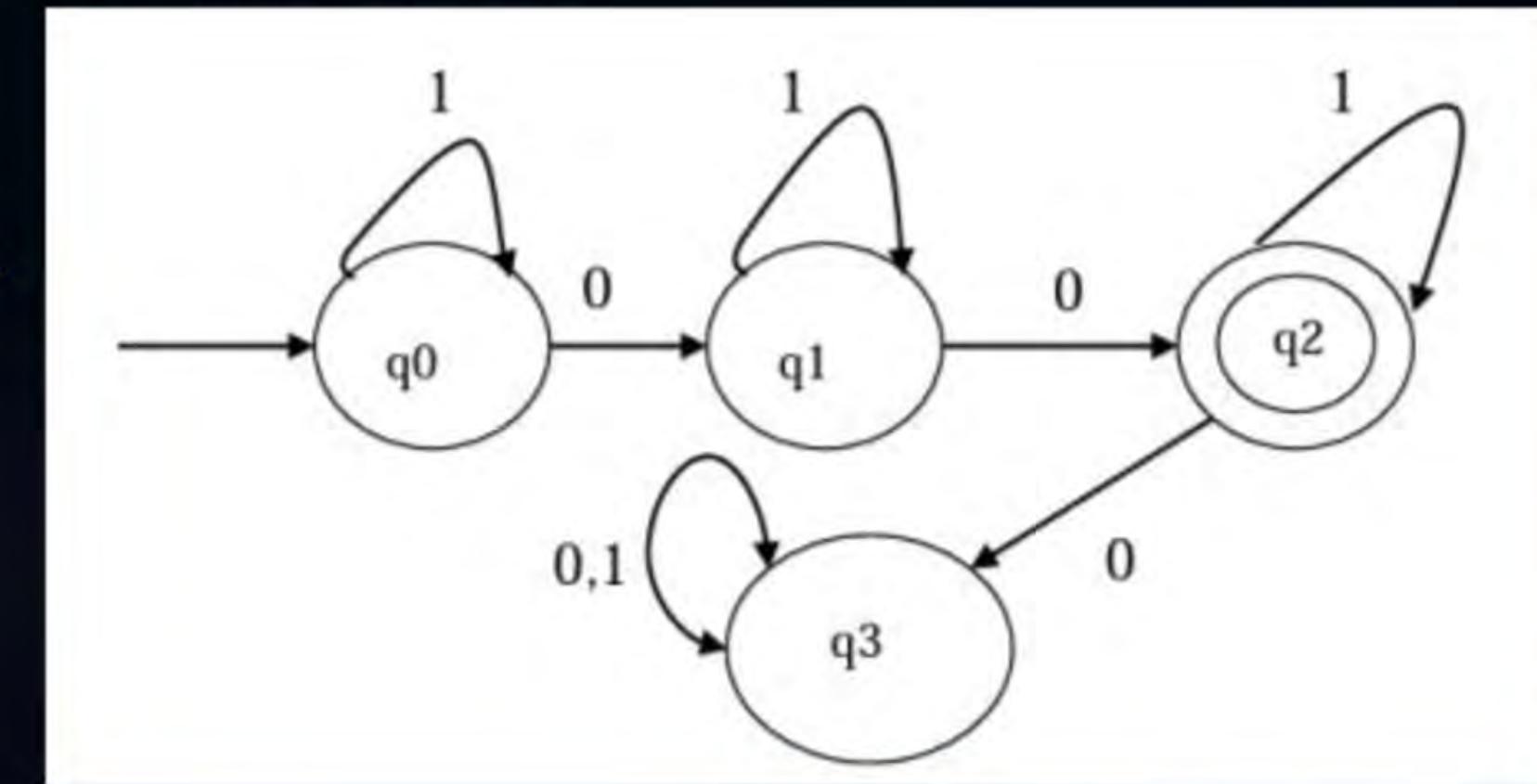
$$((00)^*(11) + 01)^* \\ (z^*y + z)^*$$

D

$$((00)^*(01) + 11)^*$$

#Q129. What is the language accepted by FA?

$1^* 0 1^* 0 1^*$   
          



A

{ $w \mid w$  is binary,  $n_0(w) = 2$ }

C

{ $w \mid w$  is binary,  $n_1(w) = 2$ }

B

{ $w \mid w$  is binary,  $n_0(w) > 2$ }

D

{ $w \mid w$  is binary,  $n_1(w) > 2$ }

#Q130. Find the language generated by the following CFG.

$$\left. \begin{array}{l} S \rightarrow AB \\ A \rightarrow 0A|0 \\ B \rightarrow 1B|\epsilon \end{array} \right\} \quad \left. \begin{array}{l} A = 0^+ \\ B = 1^* \end{array} \right\} \quad L = S = AB = 0^+ 1^*$$

**A**  $0^* 1^* 1 = 0^* 1^*$

~~B~~  $00^* 1^* = 0^* 1^*$

**C**  $0^* 11^* = 0^* 1^*$

~~D~~  $0^* 01^* = 0^* 1^*$

#Q131. Find the language generated by the following CFG.

$$S \rightarrow AC \mid CB$$

$$C \rightarrow aCb \mid \epsilon$$

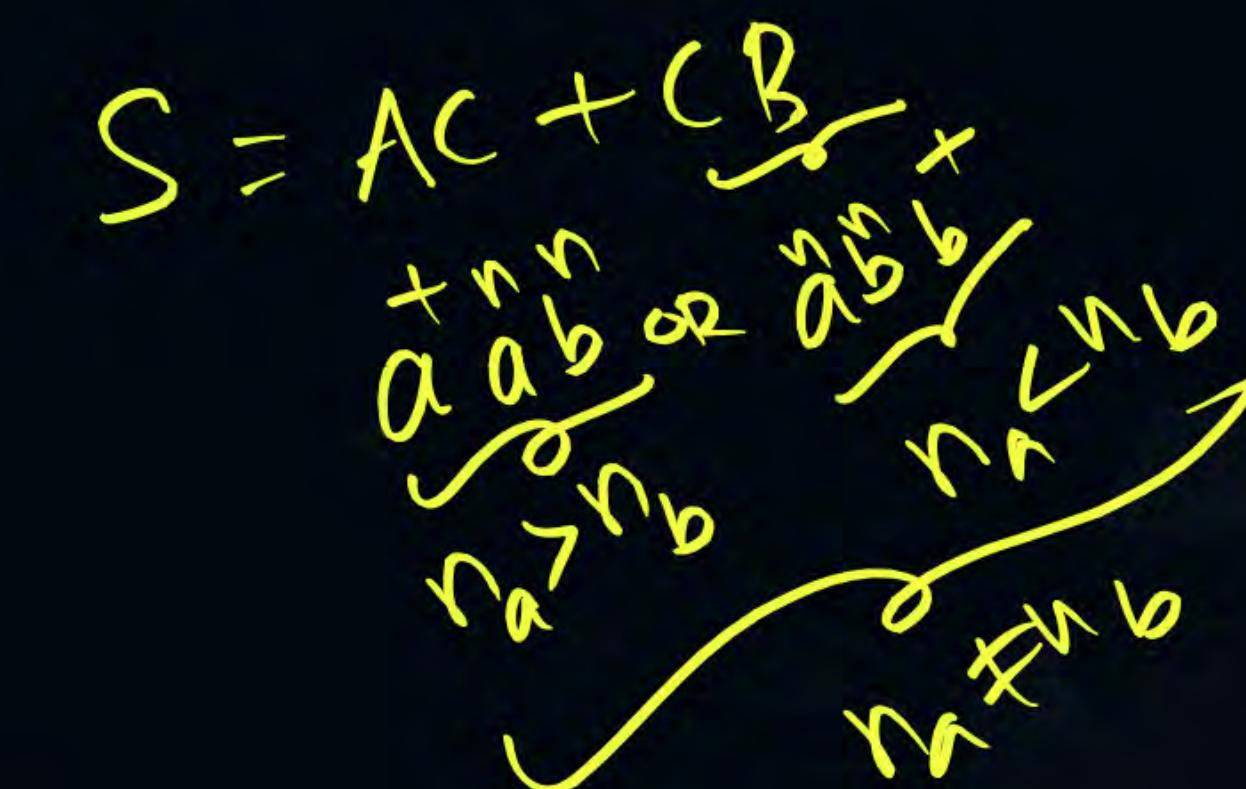
$$A \rightarrow aA \mid a$$

$$B \rightarrow bB \mid b$$

$$C = a^n b^n$$

$$A = a^+$$

$$B = b^+$$



A

$$\{a^m b^n \mid m=n\}$$

C

$$\{a^m b^n \mid m \leq n\}$$

B

$$\{a^m b^n \mid m \geq n\}$$

D

$$\{a^m b^n \mid m \neq n\}$$

#Q132. How many of the following statements are **TRUE?**

I. Complement of L is same as L **FALSE**

II. Kleene star of L is same as L **FALSE**

**✓** III. Complement of Complement of L is same as L

IV. Kleene star of Kleene star of L is same as L **FALSE**

$$\overline{\overline{L}} = L$$

$$\overline{L} = \Sigma^* - L$$

$$L \neq \overline{L}$$

$$L = \{a\}^*$$

$$L^* = a^*$$

$$L \neq L^*$$

$$L = \{a\}^*$$

$$L^* = a^*$$

$$L \neq L^*$$

$$L = \{a\}^*$$

$$(L^*)^* = \Sigma^* = \{a\}^*$$

$$L = L^*$$

Note:

$$\overset{*}{L} = (\overset{*}{L})^\dagger$$

$$\begin{matrix} \overset{\circ}{\text{j}} \\ \overset{'}{\text{j}} \\ \overset{\circ}{\text{j}} \\ \overset{'}{\text{j}} \end{matrix}$$

#Q133. Which of the following is correct?

A

$$(r + s)^* = r^* + s^*$$



C

$$(r + s)^* = r^*s^*$$



B

$$(r + s)^* = (r^* + s^*)^*$$

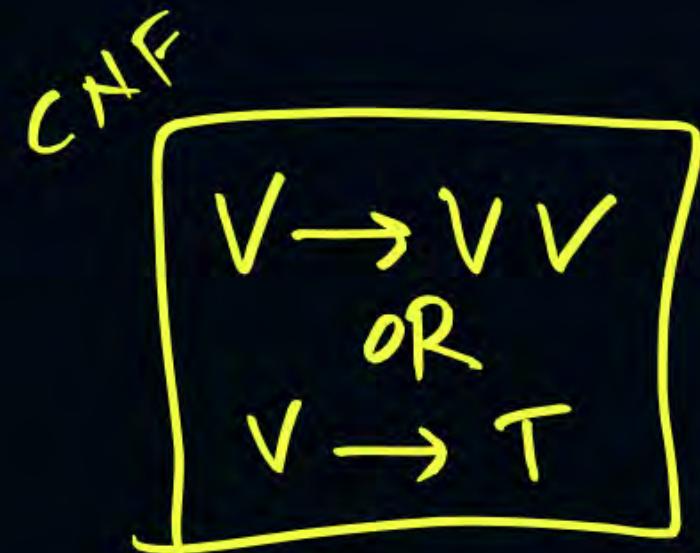


D

$$(r + s)^* = (r^*s^*)^*$$



#Q134. Which of the following CFGs are in CNF?



$$S \rightarrow \underline{aa} \mid \underline{SS}$$



$$S \rightarrow \underline{abc} \mid \underline{SS}$$



$$S \rightarrow \underline{a} \mid \underline{SS}$$



$$S \rightarrow \underline{a} \mid \underline{\underline{SS}}$$

#Q135. Which of the following CFGs are in GNF?

$$V \rightarrow T V^*$$



$$S \rightarrow \underline{a} \mid \underline{aSS}$$



$$S \rightarrow \underline{\underline{abc}} \mid \underline{aSS}$$



$$S \rightarrow \underline{a} \mid \underline{bSS}$$



$$S \rightarrow \underline{a} \mid \underline{SSS}$$

#Q136. Union, Intersection, and Complement operations are closed for \_\_

 ✓  
 $\cup, \cap, \bar{L}$

Regular languages

 ✓  
 $\cup, \cap, \bar{L}$   
✓  
✓  
✓

Decidable languages

 ✓  
 $\cup, \cap, \bar{L}$

CFLs

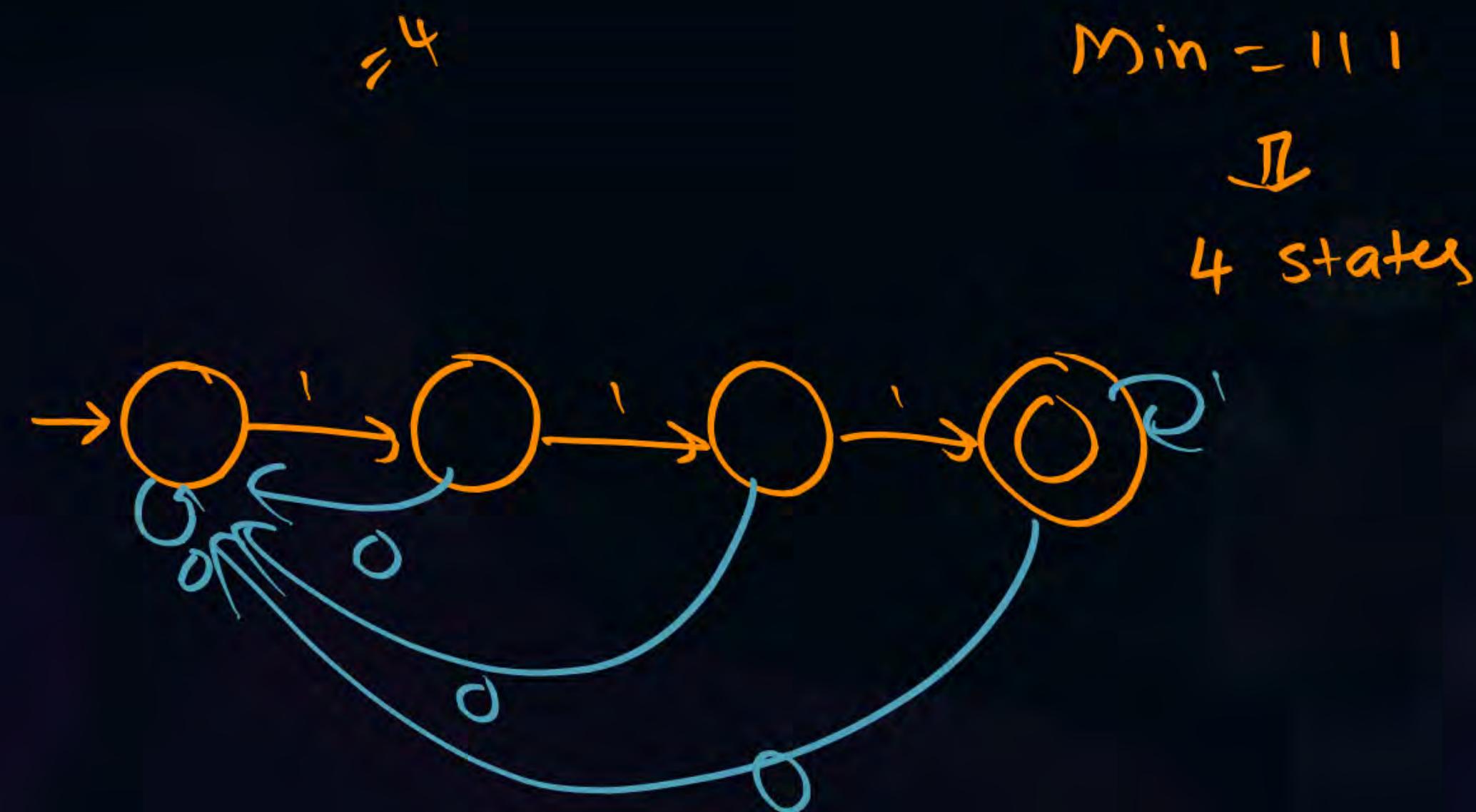
 ✓  
 $\cup, \cap, \bar{L}$

RELS

$\cup, \cap, \bar{L}$   
✓  
✗

	$\cup$	$\cap$	Complement*
Finites	✓	✓	✗
Infinites	✓	✗	✗
Regulars	✓	✓	✓
DCLFs	✗	✗	✓
CFLs	✓	✗	✗
CSLs	✓	✓	✓
Recursive	✓	✓	✓
REls	✓	✓	✗

#Q137. Number of states in Min DFA that accepts all binary strings ending with 111.



#Q138. Which of the following are CFLs but not regular?

A

$\{w \mid w \text{ is binary, } n_0(w) = n_1(w)\}$

CFLs  
not reg

B

$\{w \mid w \text{ is binary, } n_0(w) > n_1(w)\}$

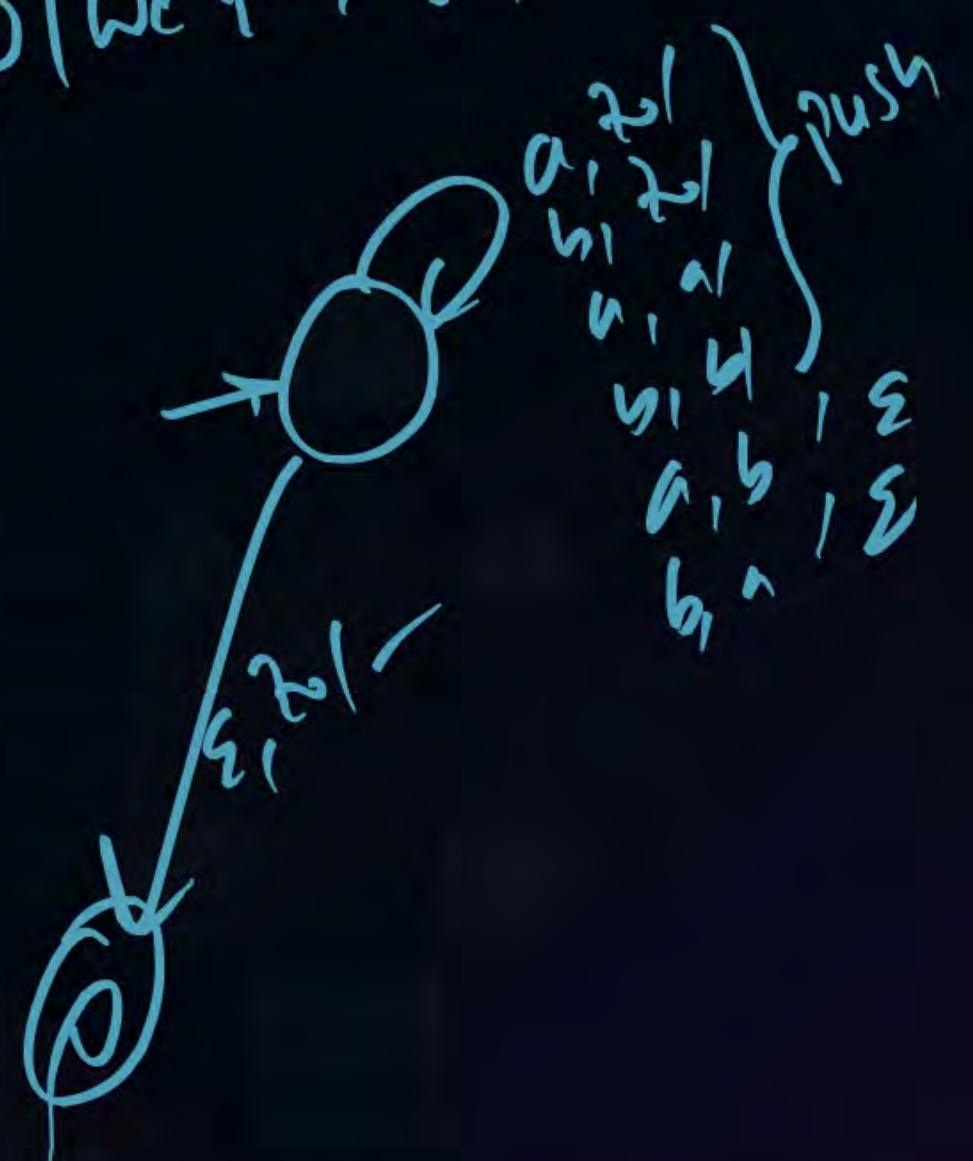
C

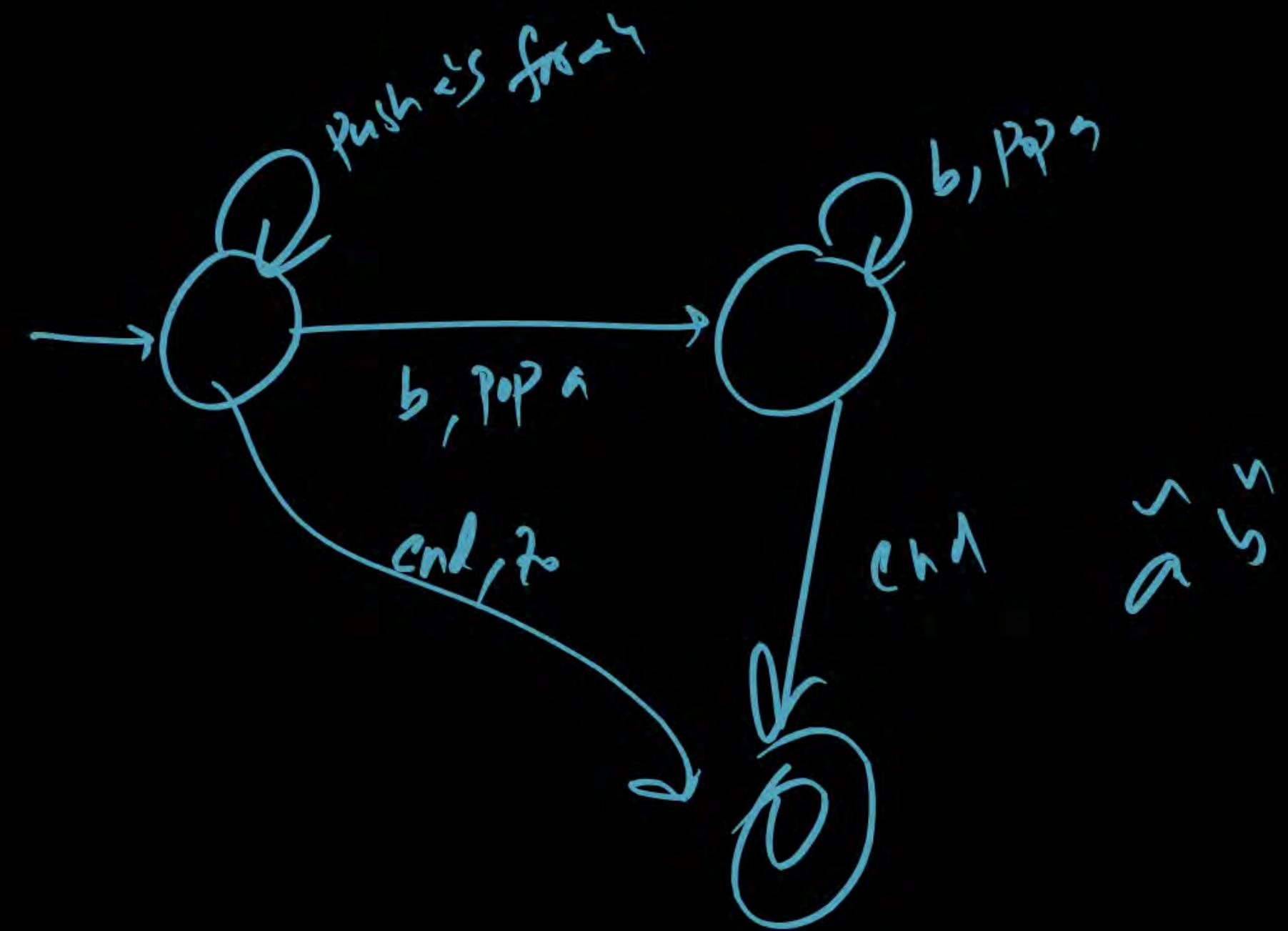
$\{w \mid w \text{ is binary, } n_0(w) < n_1(w)\}$

D

None of these

$\{w \mid w \in \{a, b\}^*, n_a(w) - n_b(w) \leq k\}$





#Q139. Which of the following is CFL?

\*\*\*

$$n=3 \Rightarrow (a^2 b^3) (a^2 b^3) (a^2 b^3)$$



$$\{ (a^n b^n)^n \mid n \geq 0 \}$$

$$(a^2 b^3)^4$$

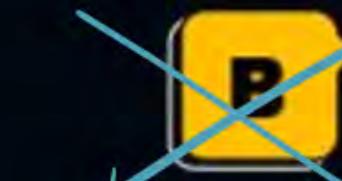


$$\{ (a^m b^n)^k \mid m, n, k \geq 0 \}$$

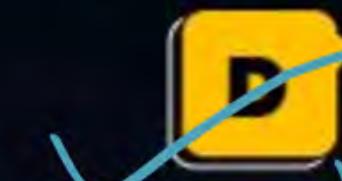
$$m=2 \quad n=3 \quad k=4$$

$$n=2 \quad k=3$$

$$(a^2 b^3)^3 = \underbrace{a^2 b^3}_{\text{t}} \underbrace{a^2 b^3}_{\text{t}} \underbrace{a^2 b^3}_{\text{t}}$$



$$\{ (a^n b^n)^k \mid k, n \geq 0 \}$$



$$\{ (a^* b^*)^n \mid n \geq 0 \}$$

$$n=2 \quad a^* b^* a^* b^*$$

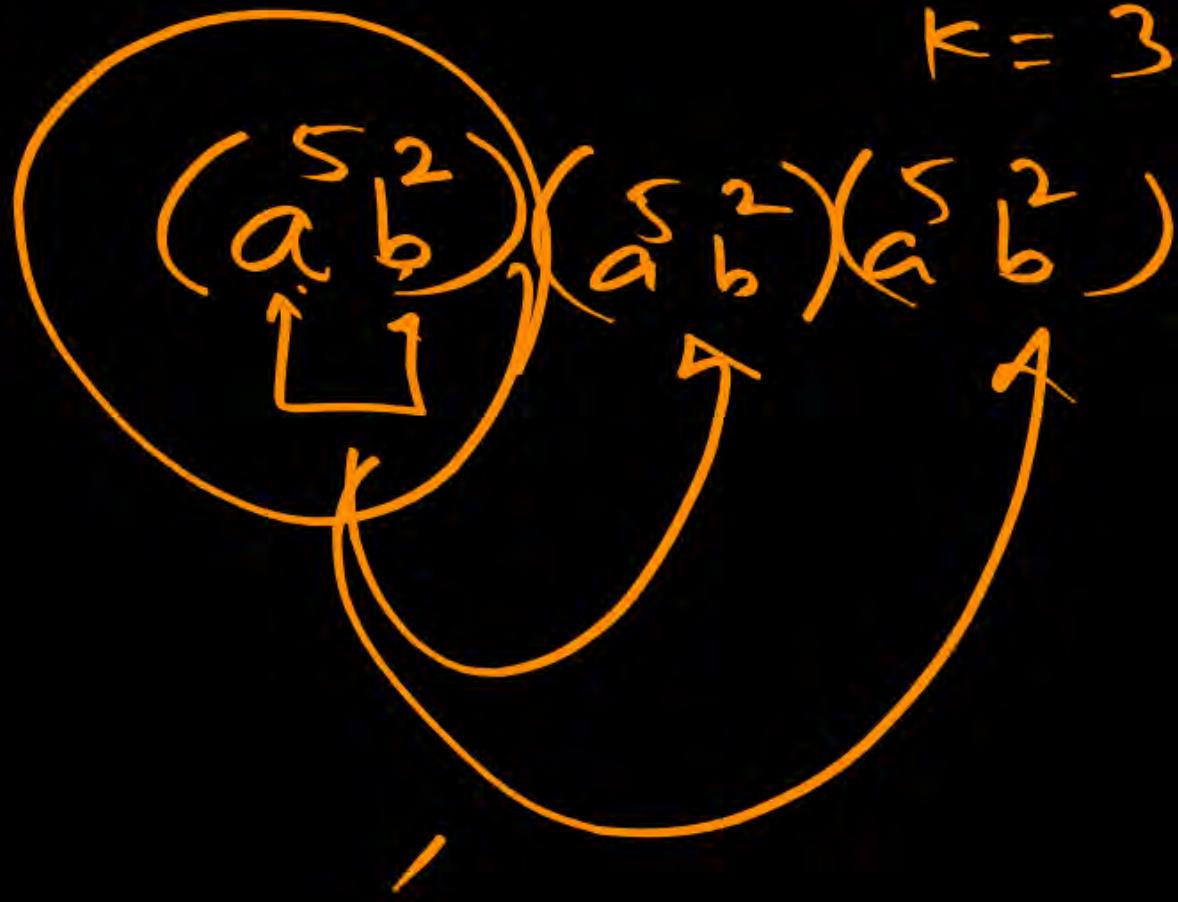
$$= (a^* b^*)^* \\ = (a+b)^*$$

$$\left\{ \left( a^m b^n \right)^k \mid m, n, k \geq 0 \right\}$$

$$m = 5$$

$$n = 2$$

$$k = 3$$



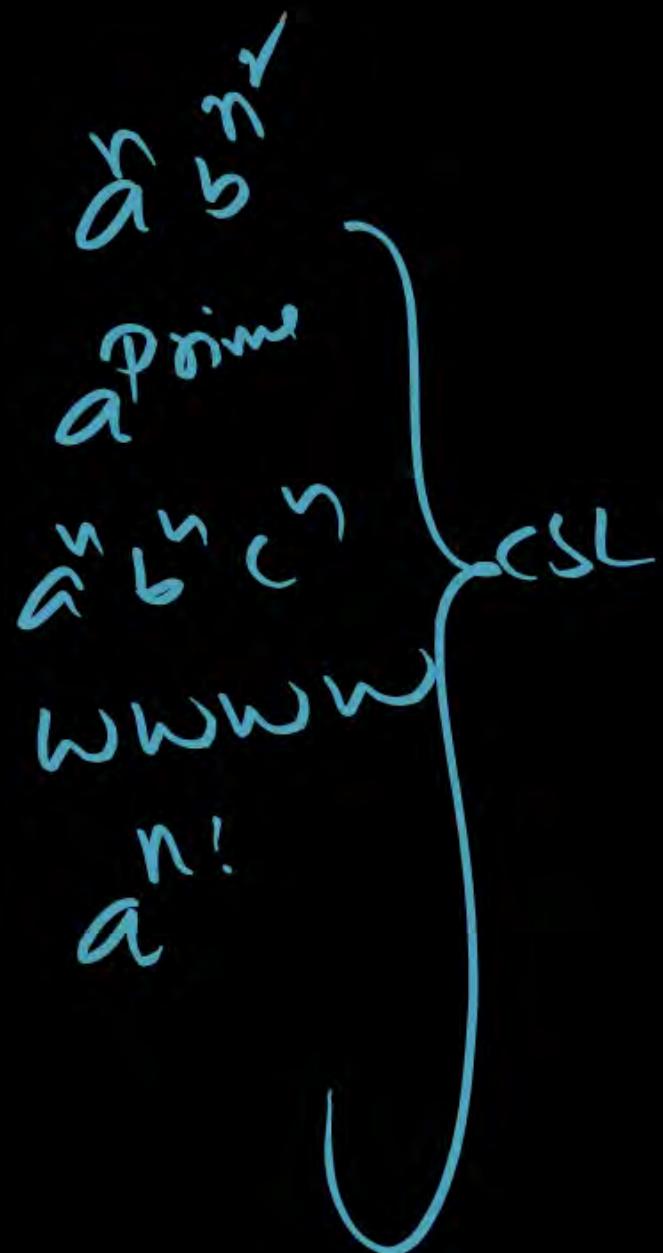
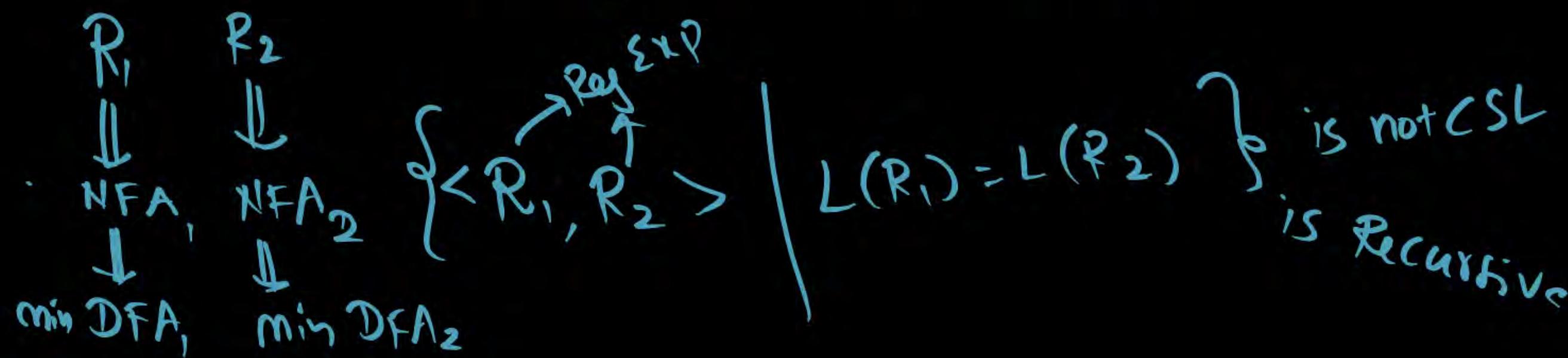
$$\left\{ \left\{ a^m b^n \mid m, n \geq 0 \right\}^k \mid k \geq 0 \right\}$$

$$\left\{ a^m b^n \right\}^2 = \left\{ a^{m_1} b^{n_1} \right\} \left\{ a^{m_2} b^{n_2} \right\}$$

$$\overset{*}{a} \overset{*}{b} \quad \overset{*}{a} \overset{*}{b}$$

# CSL Vs Recursive Set

Every CSL is Recursive



**[MCQ]**P  
W#Q140.  $\{M \mid L(M) \text{ is empty language}\} = \text{Set of machines which accepts empty set}$ 

$$= \{M_1, M_2, M_3, \dots\}$$

Whether given TM accepts empty language

$\hookrightarrow$  Yes :  $L(TM) = \emptyset$  (No logic)

$\hookrightarrow$  No :  $L(TM) \neq \emptyset$

**A**

Recursive

**C**

Regular

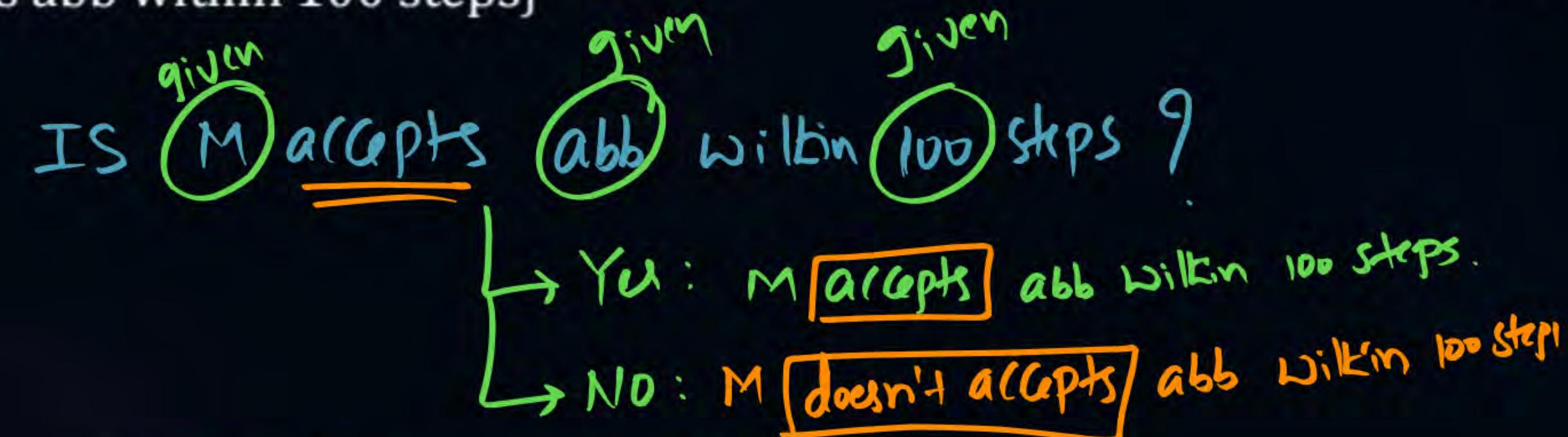
**B**

REL

**D**

None of these

#Q141. {M | M accepts abb within 100 steps}



We will check upto 100 steps

→ Yes: If M halts at final within 100 steps

→ No: If M takes 101<sup>st</sup> step, it is guaranteed M will not accept within 100 steps



Recursive



Regular



REL



None of these

#Q142.  $\{M \mid M \text{ accepts } abb \text{ after } 100 \text{ steps}\}$

M not accepts abb within 100 steps



Recursive



Regular



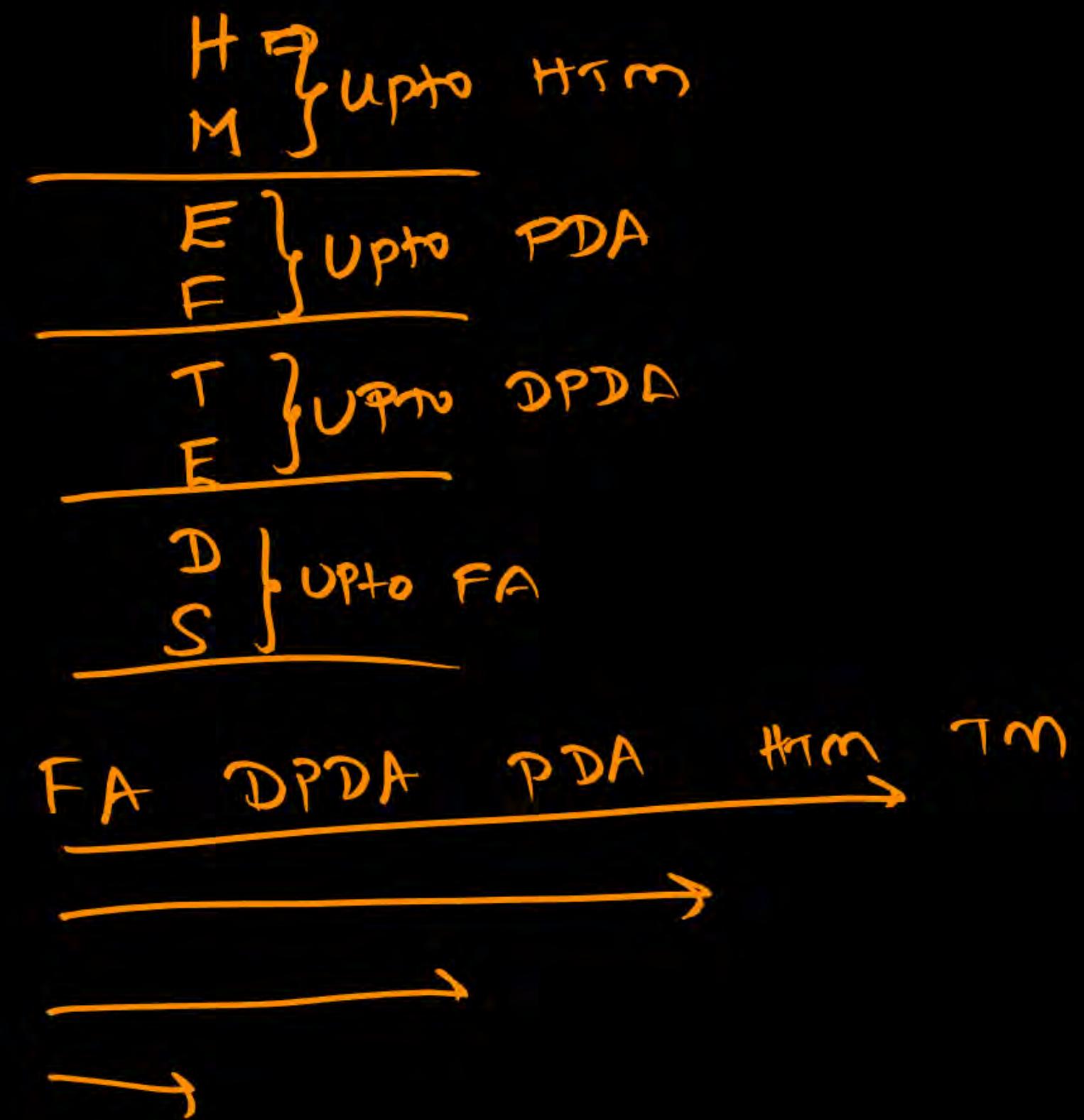
REL



None of these

#Q143. Which of the following is decidable for PDA but not for HTM?

- Decidable for both PDA & HTM*
- A** Membership
- C** Equivalence
- Undecidable for both PDA & HTM*
- B** Emptiness
- D** Finiteness



#Q144. If set L is effectively enumerable by an algorithm A, and X is reducible to L then X is \_\_\_\_\_

(Recursive)  
(Decidable)

Every Recursive is  $\neq$  EL

$X \leq$  Decidable Set  
may or may not be  $\neq$  EL

$X \leq L$   
 $\hookrightarrow$  effectively enumerable



Recursive



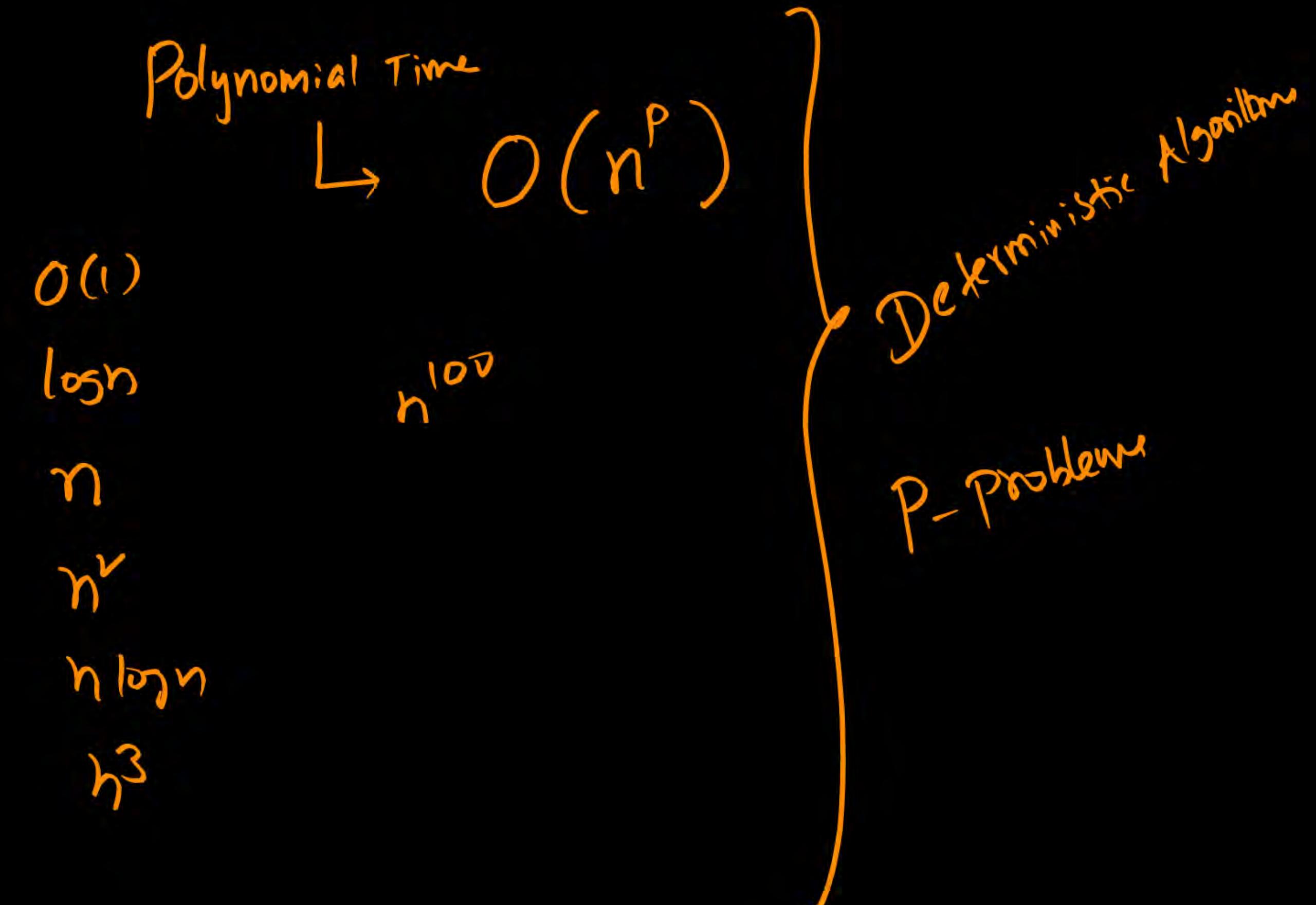
REL



Regular



None of these



P - problem: Solvable in polynomial by DTM

NP - problem: Solvable in " by NTM

(Answer is verifiable in polynomial by DTM)

#Q145. How many of the following are Decidable Languages? = 2

- Rice's theorem*
- Turing*
1. { TM | L(TM) is regular language}      " *Whichever given Tm accepts Regular*"
2. { TM | L(TM) is context free language}      " " " "
3. { TM | L(TM) is decidable language}      " " " "
4. { TM | L(TM) is enumerable language}      " " " "
5. { TM | L(TM) is not enumerable language}      " " " "
- RE L  $\Rightarrow$  Yes      not RE L  $\Rightarrow$  NO

4.  $L = \text{Set of all TMs}$

$$\bar{L} = \emptyset$$

5.  $L = \emptyset$

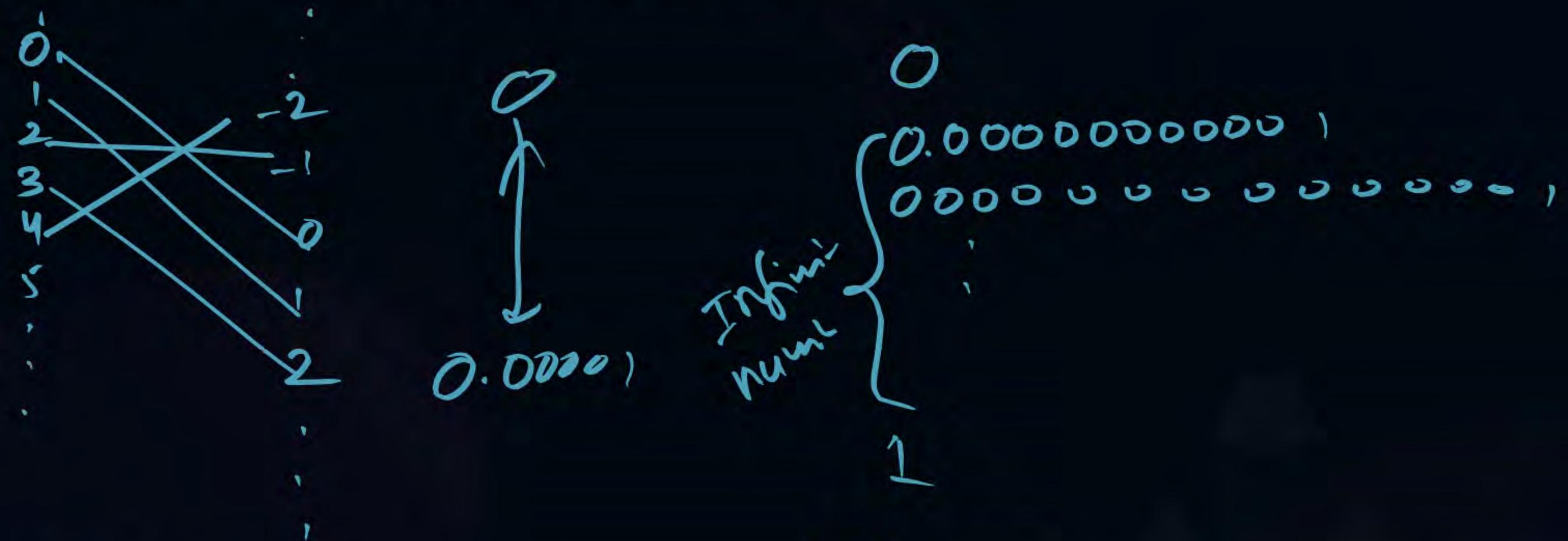
$\bar{L} = \text{Set of all TMs}$

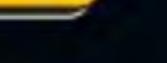
1.  $L = \text{Set of some TMs}$

$\bar{L} = \text{Set of some TMs}$

} non-fin

#Q146. Which of the following is countable set?



- Set of natural numbers
  -  Set of integers
  - Set of rational numbers
  -  Set of real numbers

#Q147. Which of the following is True?

Turing Decidable  
 $\equiv$   
Recursive  
 $\equiv$   
Decidable

- A Every CFL is Turing decidable
- B Every Regular is Turing decidable
- C Every Recursive is Turing decidable
- D Every REL is Turing decidable

Every CFL is Decidable

CFL is Decidable

$\overline{a^b}$  ✓  
 $\overline{a^*}$  ✓

Set of all CFLs is undecidable

$L = \{CFL_1, CFL_2, CFL_3, \dots\}$

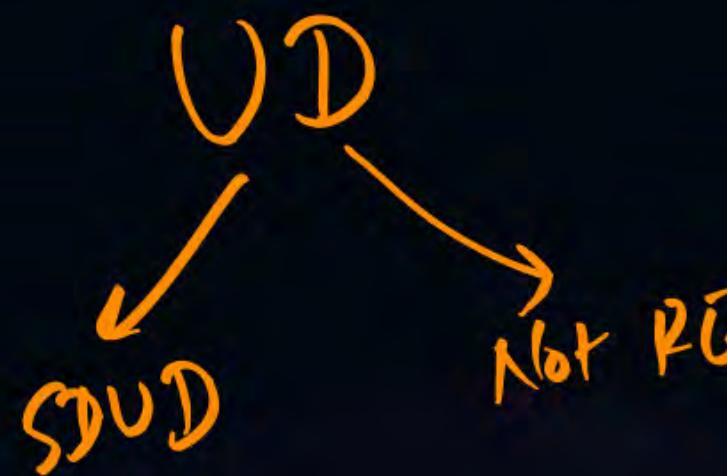
$\bar{L} = \{\text{not } CFL_1, \text{not } CFL_2, \dots\}$

$\xrightarrow{\sim} \text{SDUD}$  } UD  
 $\xrightarrow{\sim} \text{not FL}$

$\overset{n}{\overbrace{ab}} = \{\epsilon, ab, a^2b, \dots\}$  is CFL  
Hence exist

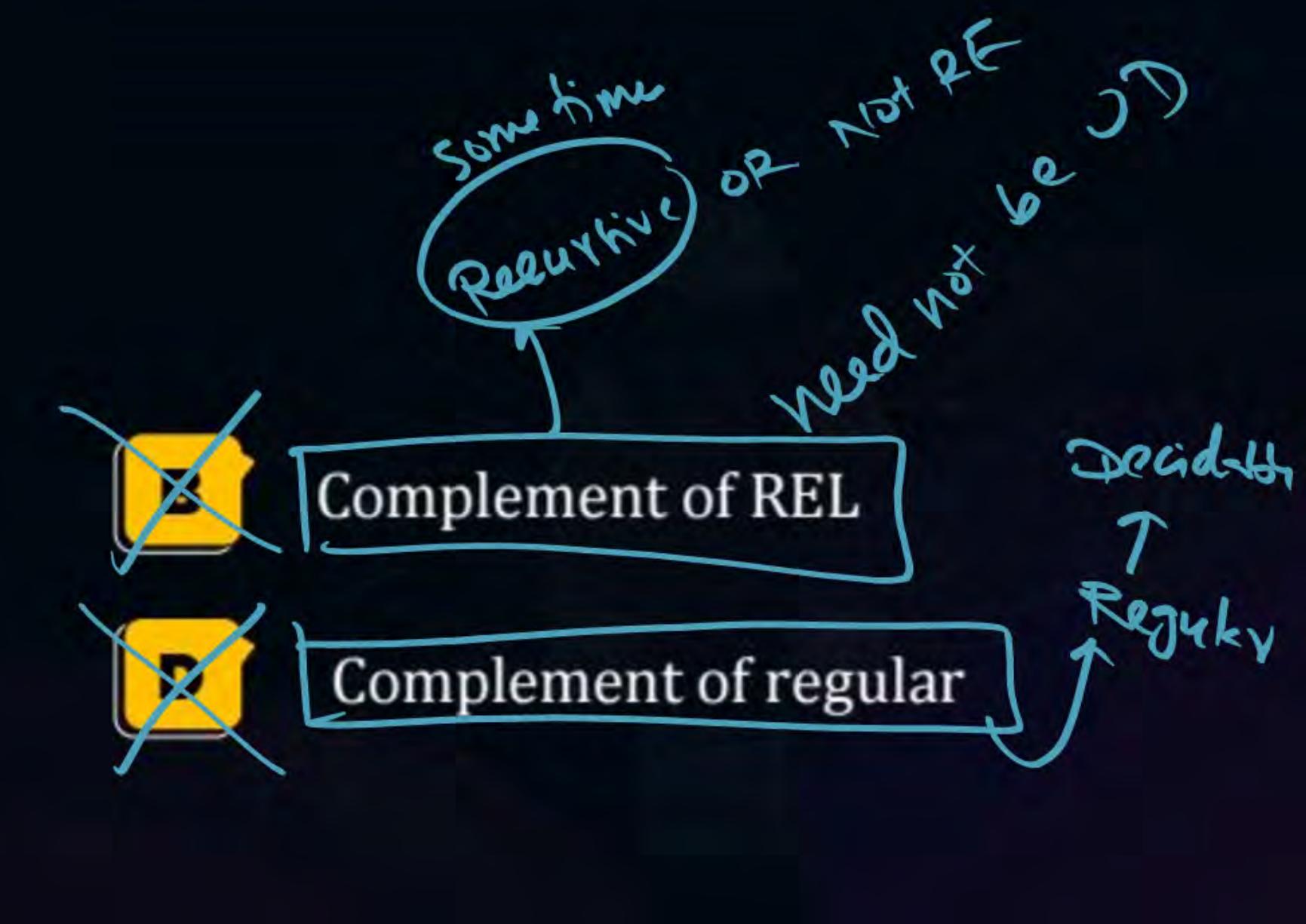
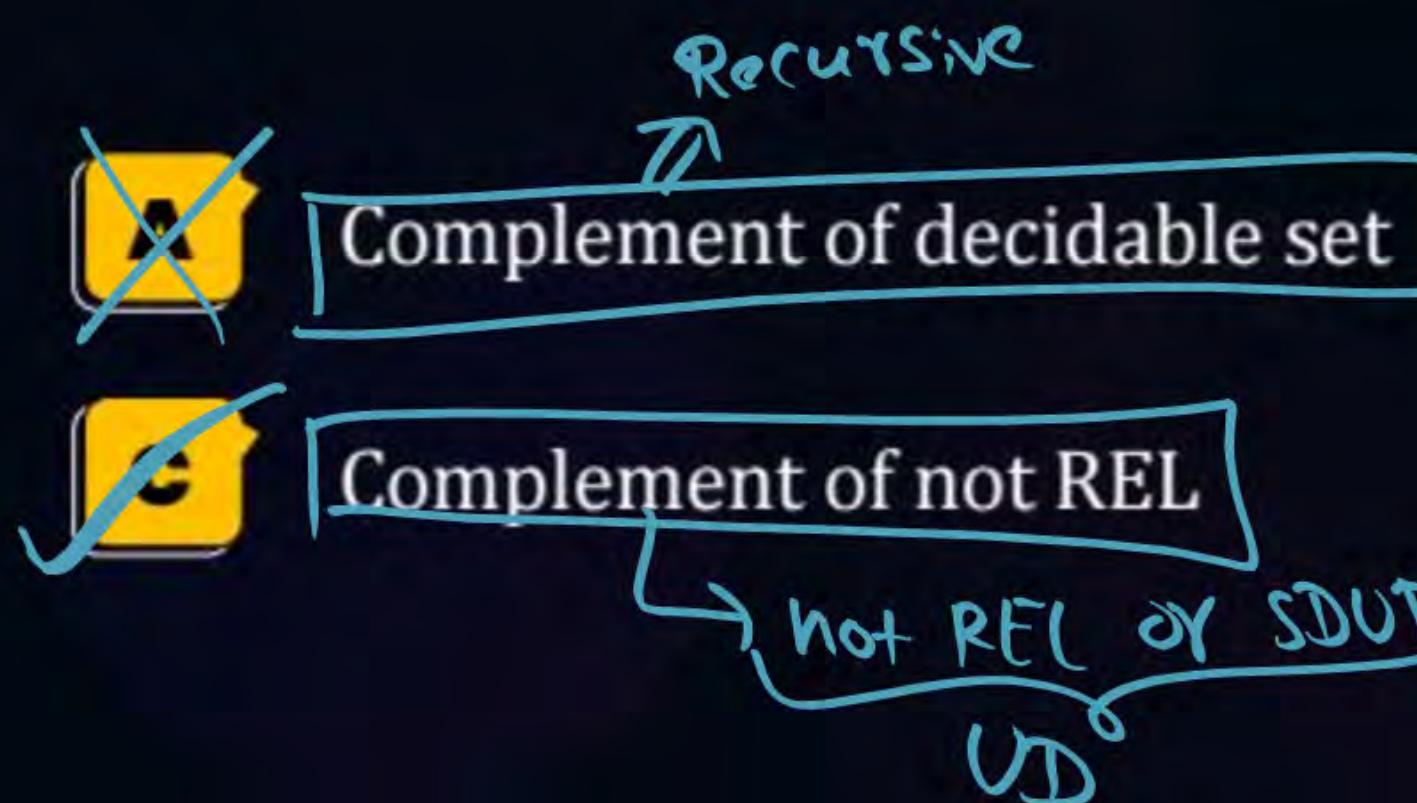
$\left\{ a^*, \phi, b^*, \overset{n}{\overbrace{ab}}, \dots \text{ all CFLs} \right\}$  is set of all CFLs  
Hence not exist  
TM exist

#Q148. Which of the following is not decidable?



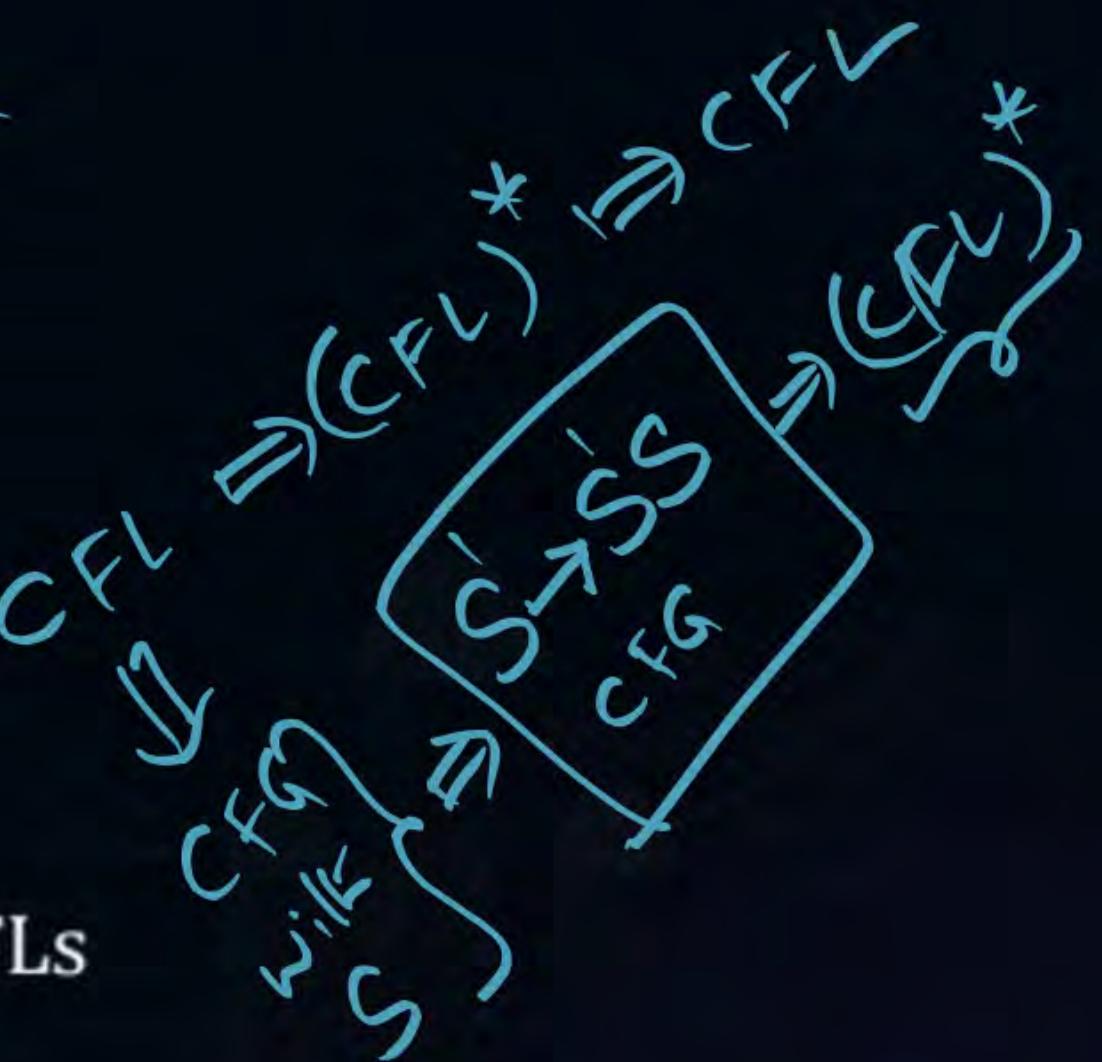
Undecidable

It can not exist



**[MCQ]**P  
W#Q149. Kleene star is not closed for \_\_ $L = \{c a^n b^n\} \cup \{a^k b^{2^k}\}$  is DCFL $L^* = \text{Not DCFL}$ 

Kleene star of DCFL is need not be DCFL



- A DCFLs
- C Decidable languages

- B CFLs
- D RELs

$$L = \{c\overset{n}{\underbrace{ab}}\} \cup \{a^k b^{2k}\}$$

aaaabb

$$L^* = \{ \{c\overset{n}{\underbrace{ab}}\} \cup \{a^k b^{2k}\} \}$$

caan(b)bba

caanbbbbb

q  
{-dc} {dab}

#Q150. Which of the following is TRUE?



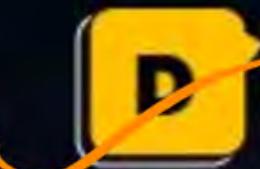
A Some sets are not REL



C Some sets are REL



B Some sets are countable



D Some sets are not countable



THANK - YOU