

Alternative Sol to

1 to n .

// initialize k=1

```
void fun (int n, int k)
```

```
{
```

```
    if (n == 0)
```

```
        return
```

```
        S.o.pln(k)
```

```
        fun (n-1, k+1);
```

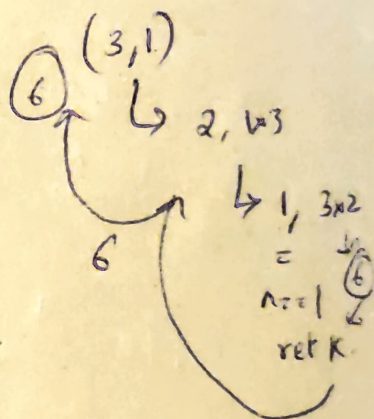
```
}
```

```
int fact (int n, int k) // k=1
```

```
if (n == 0 || n == 1)
```

```
    return k.
```

```
    return fact (n-1, k*n).
```



Tail Recursion

Solved faster by modern day

Compilers - //

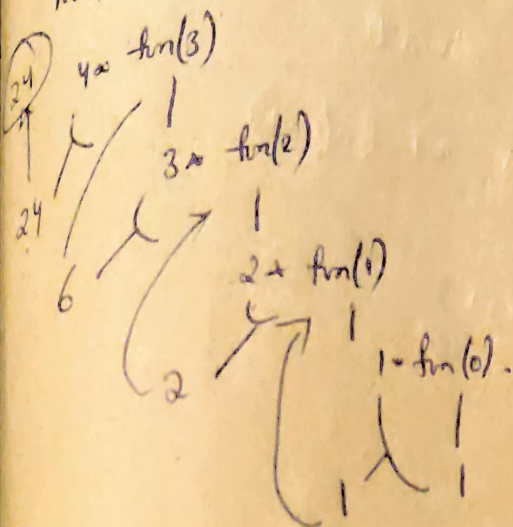
factorial n where $n \geq 0$

$n = 4$

o/p: 24.

```
int fun (int n)
    if  $n == 0$ 
        return 1;
    return  $n * \text{fun}(n-1)$ 
```

$n = 4$



Fibonacci number $n \geq 0$.

```
int fib (int n)
```

```
    if ( $n == 0$ )
        return 0;
    if ( $n == 1$ )
        return 1;
```

```
    return  $\text{fib}(n-1) + \text{fib}(n-2)$ ;
```

```
    if ( $n <= 1$ )
        return  $n$ ;
```


Sum of 1st n natural no

$n = 2$

o/p: 5

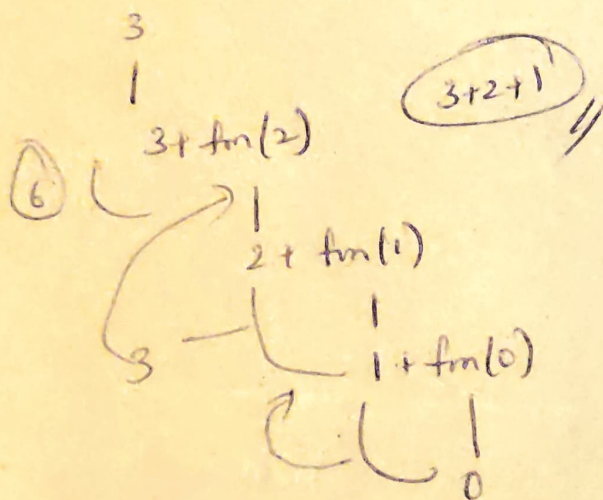
① ②

int fun(int n)

if (n == 0)

return 0;

return n + fun(n-1);



Palindrome

// initially

Start = 0;

End = n-1;

boolean Palindrome (String str,

int Start,

int End)

if Start >= End

return true;

return (str.charAt(start)

= str.charAt(end)) ;

Palindrome(str, start+1, end-1);

Pal("acbcq")

└ Pal("cbc")

└ Pal("b")

"atla"

└ "bb"

" "

Recursion happens only if $str[start] \neq str[end]$ ← "Short circuit"
char equals

Optimize
 $n \leq 9$
return n;

$n = 253$

int Sum(int n)

return Sum(n/10) + (n%10);
if (n == 0)
return 0;

3

d+1 - Recr calls
 $O(d)$

d+1 - for call stack
 $O(d)$ + Space.

253

└ Sum(253/10) + 3

└ n = (25)

└ Sum(25/10) + 25%10

└ Sum(2/10) + 2%10

└ Sum(0)

0