

Hypothesis testing in Machine learning using Python



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Well probably all who are beginner in machine learning or in intermediate level or statistic student heard about this buzz word hypothesis testing.

Today i will give a brief introduction over this topic which created headache for me when i was learning this. I put all those concept together and examples using python.

some question in mind before i will go for broader things -

What is hypothesis testing ? why do we use it ? what are basic of hypothesis ? which are important parameter of hypothesis testing ?

Let's start one by one :

1. What is hypothesis testing ?

Hypothesis testing is a statistical method that is used in making statistical decisions using experimental data. Hypothesis Testing is basically an assumption that we make about the population parameter.

Ex : you say avg student in class is 40 or a boy is taller than girls.

all those example we assume need some statistic way to prove those. we need some mathematical conclusion what ever we are assuming is true.

2. why do we use it ?

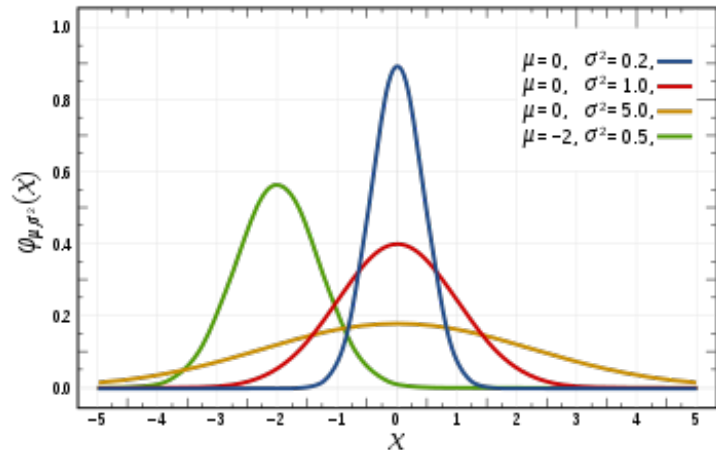
Hypothesis testing is an essential procedure in statistics. A **hypothesis test** evaluates two mutually exclusive statements about a population to determine which statement is best supported by the

sample data. When **we** say that a finding is statistically significant, it's thanks to a **hypothesis test**.

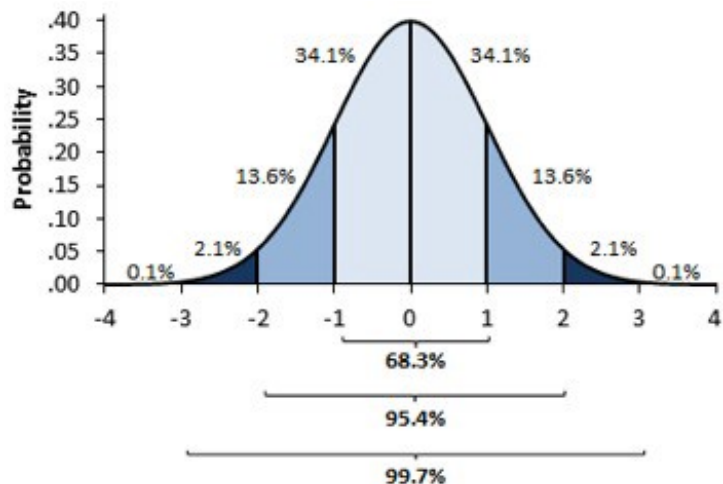
3. what are basic of hypothesis ?

Normal Curve images with different mean and variance

The basic of hypothesis is normalisation and standard normalisation. all our hypothesis is revolve around basic of these 2 terms. let's see these.



Standardised Normal curve image and separation on data in percentage in each section.



You must be wondering what's difference between these two image, one might say i don't find, while other will see some flatter graph compare to steep.

well buddy this is not what i want to represent , in 1st first you can see there are different normal curve all those normal curve can have different mean's and variances where as in 2nd image if you notice the graph is properly distributed and **mean =0 and variance =1 always**. concept of z-score comes in picture when we use **standardised normal data**.

Normal Distribution -

A variable is said to be normally distributed or have a **normal distribution** if **its distribution** has the shape of a **normal curve**—a special bell-shaped **curve**. ... The graph of a **normal distribution** is called the **normal curve**, which has all of the following **properties**: 1. The mean, median, and mode are equal.

$$x_{new} = \frac{x - x_{min}}{x_{max} - x_{min}}$$

Normal distribution formula

Standardised Normal Distribution —

A standard normal distribution is a normal distribution with mean 0 and standard deviation 1

Standard Normal Distribution

Which are important parameter of hypothesis testing ?

$$x_{new} = \frac{x - \mu}{\sigma}$$

Null hypothesis :- In inferential statistics, the null hypothesis is a general statement or default position that there is no relationship between two measured phenomena, or no association among groups

In other words it is a basic assumption or made based on domain or problem knowledge.

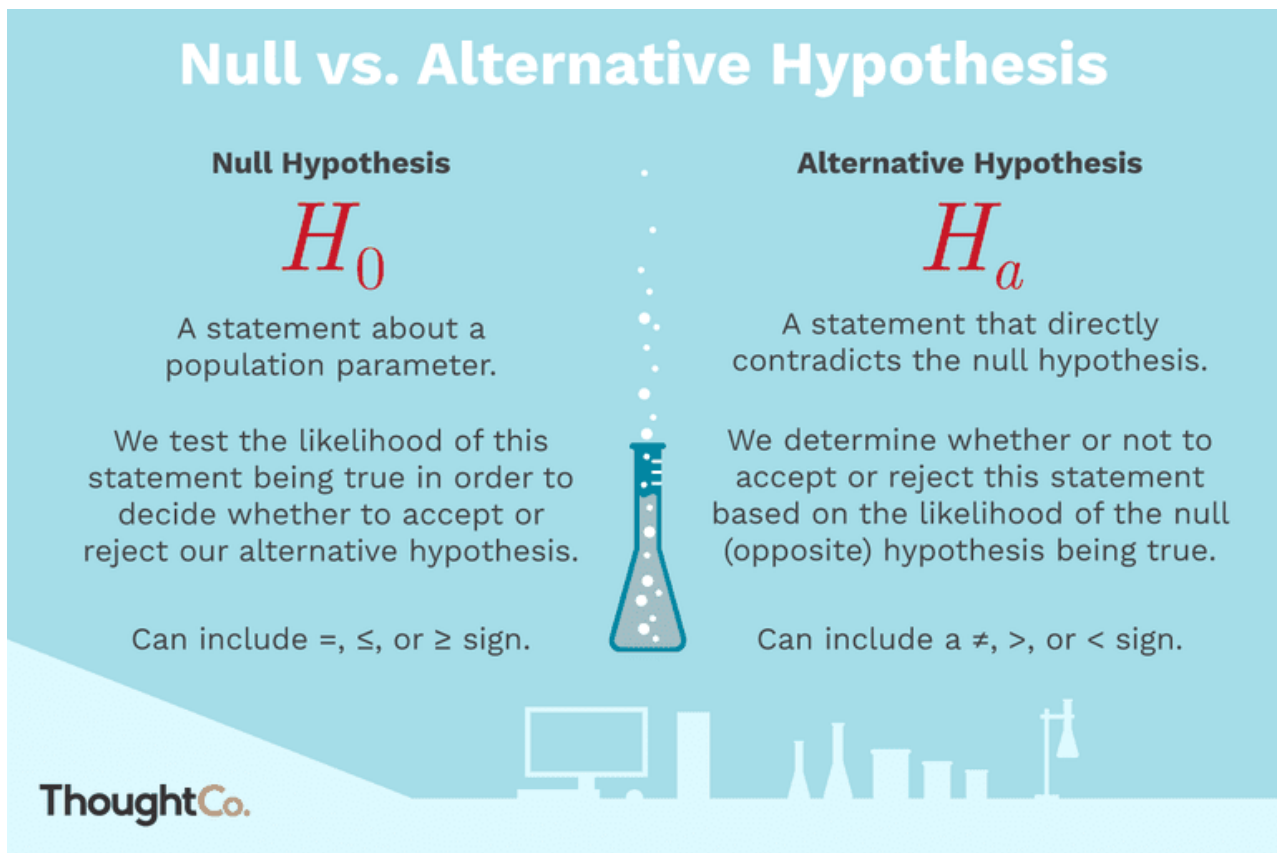
Example : a company production is = 50 unit/per day etc.

Alternative hypothesis :-

The alternative hypothesis is the hypothesis used in **hypothesis testing** that is contrary to the null hypothesis. It is usually taken to be that the observations are the result of a real effect (with some

amount of chance variation superposed)

Example : a company production is $\neq 50$ unit/per day etc.



Null and Alternate hypothesis.

Level of significance: Refers to the degree of significance in which we accept or reject the null-hypothesis. 100% accuracy is not possible for accepting or rejecting a hypothesis, so we therefore select a level of significance that is usually 5%.

This is normally denoted with alpha(maths symbol α) and generally it is 0.05 or 5% , which means your output should be 95% confident to give similar kind of result in each sample.

Type I error: When we reject the null hypothesis, although that hypothesis was true. Type I error is denoted by alpha. In hypothesis testing, the normal curve that shows the critical region is called the alpha region

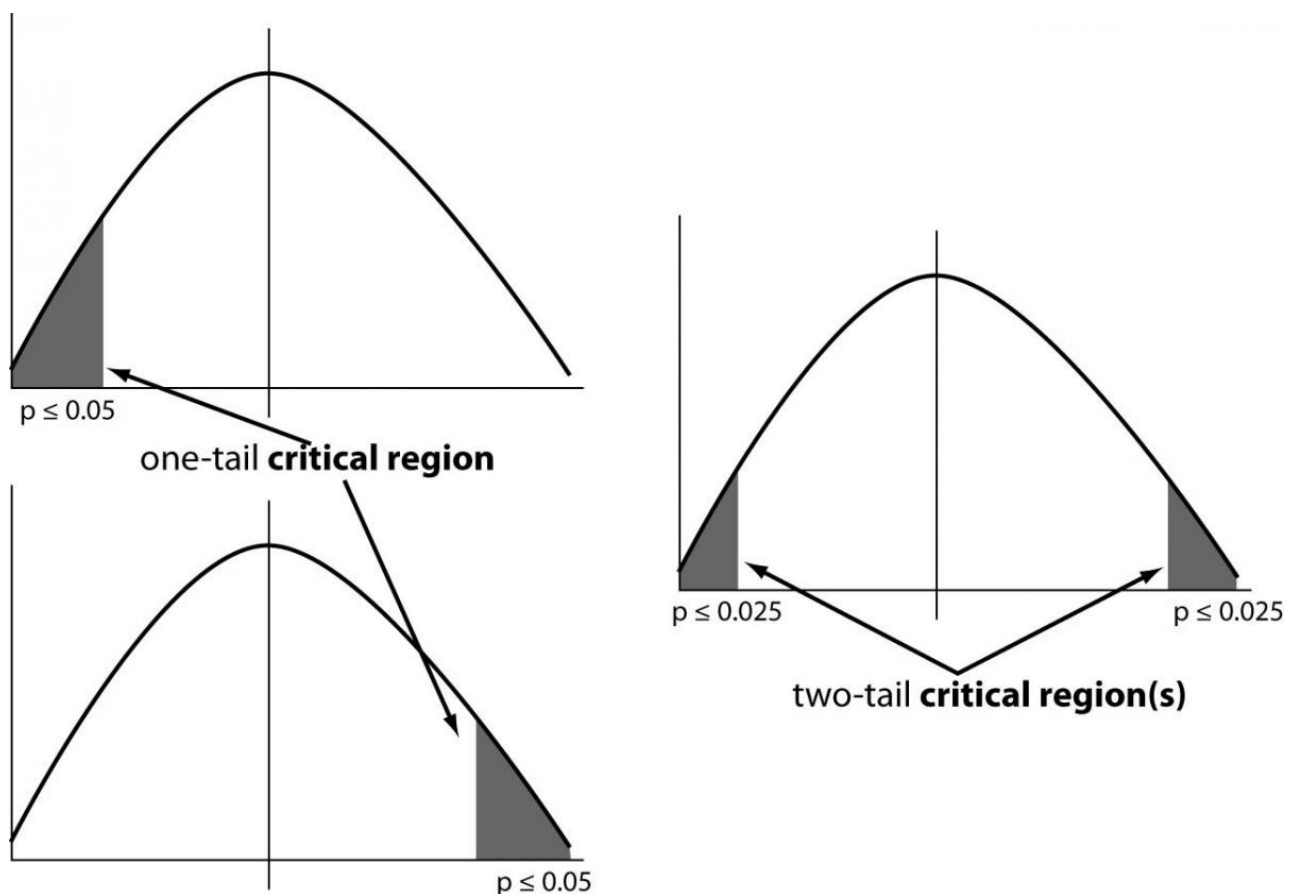
Type II errors: When we accept the null hypothesis but it is false. Type II errors are denoted by beta. In Hypothesis testing, the normal curve that shows the acceptance region is called the beta region.

One tailed test :- A test of a statistical hypothesis , where the region of rejection is on only **one** side of the sampling distribution , is called a **one-tailed test**.

Example :- a college has ≥ 4000 student or data science $\leq 80\%$ org adopted.

Two-tailed test :- A **two-tailed test** is a statistical **test** in which the critical area of a distribution is **two-sided** and tests whether a sample is greater than or less than a certain range of values. If the sample being tested falls into either of the critical areas, the alternative hypothesis is accepted instead of the null hypothesis.

Example : a college $\neq 4000$ student or data science $\neq 80\%$ org adopted



one and two-tailed images

P-value :- The **P value**, or calculated probability, is the probability of finding the observed, or more extreme, results when the null hypothesis (H_0) of a study question is true—the **definition** of ‘extreme’ depends on how the hypothesis is being tested.

If your P value is less than the chosen significance level then you reject the null hypothesis i.e. accept that your sample gives reasonable evidence to support the alternative hypothesis. It does NOT imply a “meaningful” or “important” difference; that is for you to decide when considering the real-world relevance of your result.

Example : you have a coin and you don’t know whether that is fair or tricky so let’s decide **null** and **alternate hypothesis**

H0 : a coin is a fair coin.

H1 : a coin is a tricky coin. and **alpha** = **5% or 0.05**

Now let’s toss the coin and calculate **p- value** (probability value).

Toss a coin 1st time and result is **tail**- P-value = 50% (as head and tail have equal probability)

Toss a coin 2nd time and result is **tail**, now **p-value** = $50/2 = 25\%$

and similarly we Toss 6 consecutive time and got result as P-value = **1.5%** but we set our significance level as 95% means 5% error rate we allow and here we see we are beyond that level i.e. our null-hypothesis does not hold good so we need to reject and propose that this coin is a tricky coin which is actually.

Degree of freedom :- Now imagine you’re not into hats. You’re into data analysis. You have a data set with 10 values. If you’re not estimating anything, each value can take on any number, right? Each value is completely free to vary. But suppose you want to test the population mean with a sample of 10 values, using a 1-sample t test. You now have a constraint—the estimation of the mean. What is that

constraint, exactly? By definition of the mean, the following relationship must hold: The sum of all values in the data must equal $n \times \text{mean}$, where n is the number of values in the data set.

So if a data set has 10 values, the sum of the 10 values *must* equal the mean $\times 10$. If the mean of the 10 values is 3.5 (you could pick any number), this constraint requires that the sum of the 10 values must equal $10 \times 3.5 = 35$.

With that constraint, the first value in the data set is free to vary. Whatever value it is, it's still possible for the sum of all 10 numbers to have a value of 35. The second value is also free to vary, because whatever value you choose, it still allows for the possibility that the sum of all the values is 35.

Now Let's see some of widely used hypothesis testing type :-

1. T Test (Student T test)
2. Z Test
3. ANOVA Test
4. Chi-Square Test

T- Test :- A t-test is a type of inferential statistic which is used to determine if there is a significant difference between the means of two groups which may be related in certain features. It is mostly used when the data sets, like the set of data recorded as outcome from flipping a coin a 100 times, would follow a normal distribution and may have unknown variances. T test is used as a hypothesis testing tool, which allows testing of an assumption applicable to a population.

T-test has 2 types : 1. one sampled t-test 2. two-sampled t-test.

One sample t-test : The One Sample t Test determines whether the sample mean is statistically different from a known or hypothesised population mean. The One Sample t Test is a parametric test.

Example :- you have 10 ages and you are checking whether avg age is 30 or not. (check code below for that using python)

```

from scipy.stats import ttest_1samp
import numpy as np

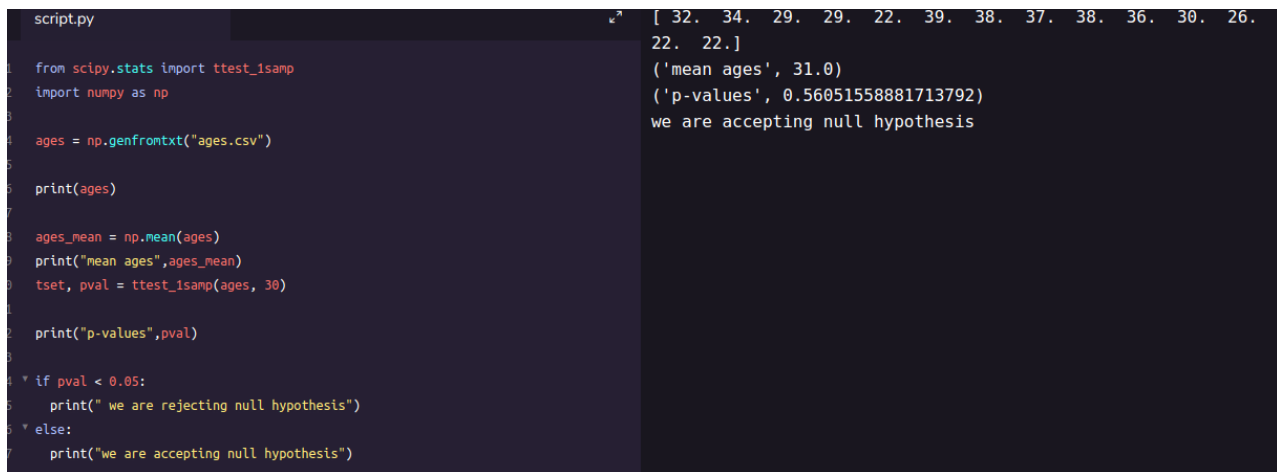
ages = np.genfromtxt("ages.csv")

ages_mean = np.mean(ages)
print(ages_mean)
tset, pval = ttest_1samp(ages, 30)

if pval < 0.05: # alpha value is 0.05 or 5%
    print(" we are rejecting null hypothesis")
else:
    print("we are accepting null hypothesis")

```

Output for above code is :



```

script.py
[ 32.  34.  29.  29.  22.  39.  38.  37.  38.  36.  30.  26.
 22.  22.]
('mean ages', 31.0)
('p-values', 0.56051558881713792)
we are accepting null hypothesis

from scipy.stats import ttest_1samp
import numpy as np

ages = np.genfromtxt("ages.csv")

print(ages)

ages_mean = np.mean(ages)
print("mean ages",ages_mean)
tset, pval = ttest_1samp(ages, 30)

print("p-values",pval)

if pval < 0.05:
    print(" we are rejecting null hypothesis")
else:
    print("we are accepting null hypothesis")

```

one-sample t-test output

Two sampled T-test :-The Independent **Samples t Test** or 2-sample t-test compares the means of two independent groups in order to determine whether there is statistical evidence that the associated population means are significantly different. The Independent **Samples t Test** is a parametric **test**. This **test** is also known as: Independent **t Test**.

Example : is there any association between week1 and week2 (code is given below in python)

```

from scipy.stats import ttest_ind
import numpy as np

week1 = np.genfromtxt("week1.csv", delimiter=",")
week2 = np.genfromtxt("week2.csv", delimiter=",")

```



```

week1_std = np.std(week1)
week2_std = np.std(week2)

ttest,pval = ttest_ind(week1,week2)
print("p-value",pval)

```

```

script.py
from scipy.stats import ttest_ind
import numpy as np

week1 = np.genfromtxt("week1.csv", delimiter=",")
week2 = np.genfromtxt("week2.csv", delimiter=",")

print(week1)
print("week2 data :-\n")
print(week2)
week1_mean = np.mean(week1)
week2_mean = np.mean(week2)

print("week1 mean value:",week1_mean)
print("week2 mean value:",week2_mean)

week1_std = np.std(week1)
week2_std = np.std(week2)

print("week1 std value:",week1_std)
print("week2 std value:",week2_std)

ttest,pval = ttest_ind(week1,week2)
print("p-value",pval)

* if pval < 0.05:
    print("we reject null hypothesis")
* else:
    print("we accept null hypothesis")

```

20.83415999	23.79367158	19.7556718	29.54421084
20.1433138			
week2 data :-			
[18.63431907	31.28788036	34.96797943	21.81678117
28.21619974			
39.39313736	35.52223207	27.54222109	33.64395433
25.31673581			
28.81392191	30.7358016	26.37241881	26.0945555
26.34073477			
19.42196017	32.58797652	24.84001926	28.93348335
20.43667584			
22.72495967	32.31728012	35.384306	29.66709637
24.53512973			
30.91406007	19.56117513	24.90816833	30.13163726
31.47466199			
27.77683598	16.51307462	35.0770162	31.74818107
36.36053496			
27.70500593	29.49869936	27.65575346	37.18504075
25.16055104			
29.26553553	38.22163057	28.92102091	24.8215439
38.30155495			
34.76020645	22.26869162	28.82593733	32.00975127
36.46437665]			
('week1 mean value:', 25.448059395144654)			
('week2 mean value:', 29.021568107746155)			
('week1 std value:', 4.5316933870843146)			
('week2 std value:', 5.4979667086536512)			
('p-value', 0.00067676769000677567)			
we reject null hypothesis			

2-sampled t-test output

Paired sampled t-test :- The paired sample t-test is also called dependent sample t-test. It's an uni variate test that tests for a significant difference between 2 related variables. An example of this is if you where to collect the blood pressure for an individual before and after some treatment, condition, or time point.

H0 :- means difference between two sample is 0

H1:- mean difference between two sample is not 0

check the code below for same

```

import pandas as pd
from scipy import stats
df = pd.read_csv("blood_pressure.csv")

df[['bp_before','bp_after']].describe()

```

```
ttest,pval = stats.ttest_rel(df['bp_before'], df['bp_after'])
print(pval)
```

When you can run a Z Test.

Several different types of tests are used in statistics (i.e. f test, chi square test, t test). You would use a Z test if:

- Your sample size is greater than 30. Otherwise, use a t test.
- Data points should be independent from each other. In other words, one data point isn't related or doesn't affect another data point.
- Your data should be normally distributed. However, for large sample sizes (over 30) this doesn't always matter.
- Your data should be randomly selected from a population, where each item has an equal chance of being selected.
- Sample sizes should be equal if at all possible.

Example again we are using z-test for blood pressure with some mean like 156 (python code is below for same) **one-sample Z test.**

```
import pandas as pd
from scipy import stats
from statsmodels.stats import weightstats as stests

ztest ,pval = stests.ztest(df['bp_before'], x2=None, value=156)
print(float(pval))
```

Two-sample Z test- In two sample z-test , similar to t-test here we are checking two independent data groups and deciding whether sample mean of two group is equal or not.

H0 : mean of two group is 0

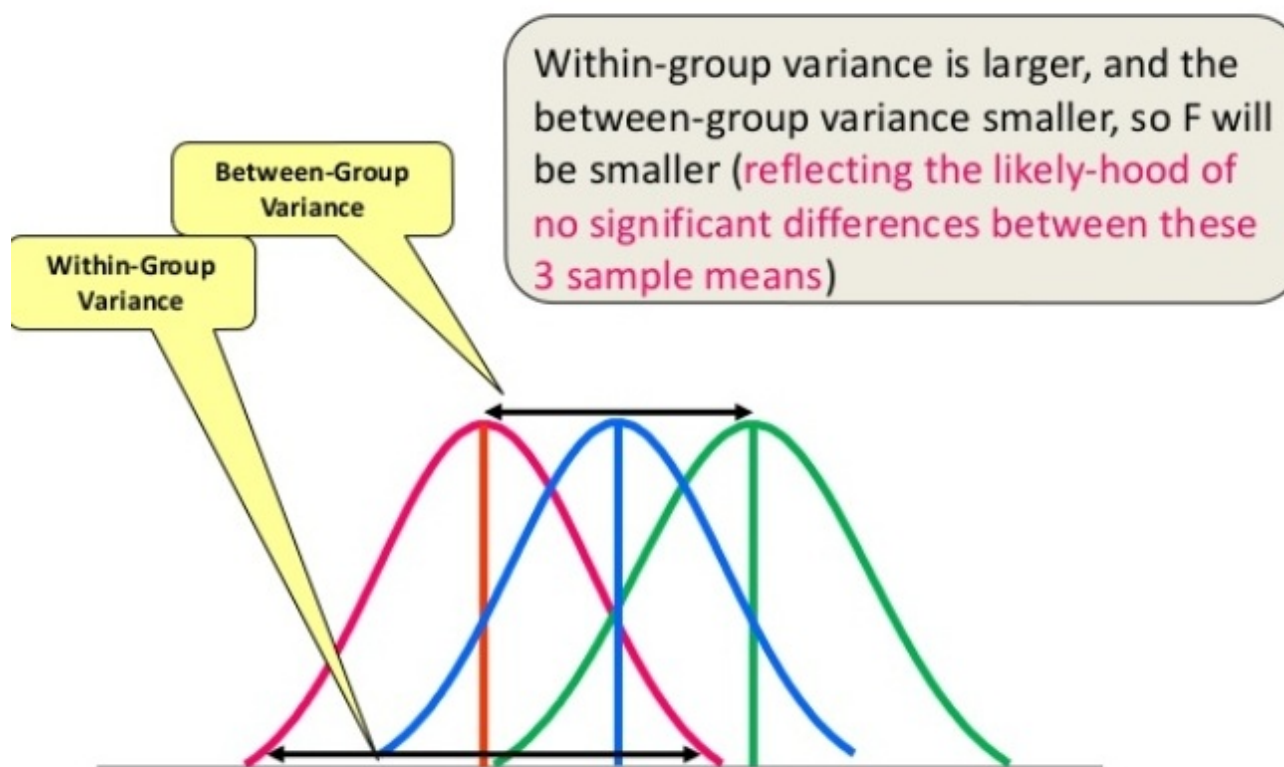
H1 : mean of two group is not 0

Example : we are checking in blood data after blood and before blood data.(code in python below)

```
ztest ,pval1 = stests.ztest(df['bp_before'], x2=df['bp_after'],
value=0,alternative='two-sided')
print(float(pval1))
```

ANOVA (F-TEST) :- The t-test works well when dealing with two groups, but sometimes we want to compare more than two groups at the same time. For example, if we wanted to test whether voter age differs based on some categorical variable like race, we have to compare the means of each level or group the variable. We could carry out a separate t-test for each pair of groups, but when you conduct many tests you increase the chances of false positives. The analysis of variance or ANOVA is a statistical inference test that lets you compare multiple groups at the same time.

F = Between group variability / Within group variability



F-Test or Anova concept image

Unlike the z and t-distributions, the F-distribution does not have any negative values because between and within-group variability are always positive due to squaring each deviation.

One Way F-test(Anova) :- It tell whether two or more groups are

similar or not based on their mean similarity and f-score.

Example : there are 3 different category of plant and their weight and need to check whether all 3 group are similar or not (code in python below)

```
df_anova = pd.read_csv('PlantGrowth.csv')
df_anova = df_anova[['weight','group']]

grps = pd.unique(df_anova.group.values)
d_data = {grp:df_anova['weight'][df_anova.group == grp] for grp in grps}

F, p = stats.f_oneway(d_data['ctrl'], d_data['trt1'], d_data['trt2'])
```

Two Way F-test :- Two way F-test is extension of 1-way f-test, it is used when we have 2 independent variable and 2+ groups. 2-way F-test does not tell which variable is dominant. if we need to check individual significance then **Post-hoc** testing need to be performed.

Now let's take a look at the Grand mean crop yield (the mean crop yield not by any sub-group), as well the mean crop yield by each factor, as well as by the factors grouped together

```
import statsmodels.api as sm
from statsmodels.formula.api import ols

df_anova2 =
pd.read_csv("https://raw.githubusercontent.com/Opensourcefordatascience/Data-sets/master/crop\_yield.csv")

model = ols('Yield ~ C(Fert)*C(Water)', df_anova2).fit()
print(f"Overall model F({model.df_model: .0f},{model.df_resid: .0f}) = {model.fvalue: .3f}, p = {model.f_pvalue: .4f}")

res = sm.stats.anova_lm(model, typ= 2)
res
```

Chi-Square Test- The test is applied when you have two categorical variables from a single population. It is used to determine whether there is a significant association between the two variables.

For example, in an election survey, voters might be classified by gender (male or female) and voting preference (Democrat, Republican, or Independent). We could use a chi-square test for independence to determine whether gender is related to voting preference

check example in python below

```
df_chi = pd.read_csv('chi-test.csv')
contingency_table=pd.crosstab(df_chi["Gender"],df_chi["Shopping?"])
print('contingency_table :-\n',contingency_table)

#Observed Values
Observed_Values = contingency_table.values
print("Observed Values :-\n",Observed_Values)

b=stats.chi2_contingency(contingency_table)
Expected_Values = b[3]
print("Expected Values :-\n",Expected_Values)

no_of_rows=len(contingency_table.iloc[0:2,0])
no_of_columns=len(contingency_table.iloc[0,0:2])
ddof=(no_of_rows-1)*(no_of_columns-1)
print("Degree of Freedom:-",ddof)
alpha = 0.05

from scipy.stats import chi2
chi_square=sum([(o-e)**2./e for o,e in zip(Observed_Values,Expected_Values)])
chi_square_statistic=chi_square[0]+chi_square[1]
print("chi-square statistic:-",chi_square_statistic)

critical_value=chi2.ppf(q=1-alpha,df=ddof)
print('critical_value:',critical_value)

#p-value
p_value=1-chi2.cdf(x=chi_square_statistic,df=ddof)
print('p-value:',p_value)
```

```
if chi_square_statistic >= critical_value:
    print("Reject H0, There is a relationship between 2 categorical variables")
else:
    print("Retain H0, There is no relationship between 2 categorical variables")

if p_value <= alpha:
    print("Reject H0, There is a relationship between 2 categorical variables")
else:
    print("Retain H0, There is no relationship between 2 categorical variables")
```

You can get all code in my [git](#) repository.

ah, finally we came to end of this article. I hope this article would have helped. any feedback is always appreciated.

For more update check my [git](#) and follow we on medium.