${\bf DEMFEMVolume Coupling Application}$

Implementation and Usage Guide

Overview

This document describes the implementation and usage of the **DEMFEMVolumeCouplingApplication** in Kratos Multiphysics. It provides the information needed to compile, run, and extend the volume-coupled DEM-FEM solver. A complete, runnable example is available in the applications/DEMFEMVolumeCouplingApplication/tests folder.

The coupling strategy is based on the *volume-coupling* approach and is implemented entirely within Kratos as a new application. It builds on existing Kratos modules: **StructuralMechanicsApplication** (FEM), **DEMApplication** (DEM), **MappingApplication**, **ConstitutiveLawsApplication**, and the solver-agnostic **CoSimulationApplication**.

1 Source Tree and Build Integration

Source Locations

New functionality is implemented in three main locations:

applications/DEMFEMVolumeCouplingApplication Contains all FEM/DEM extensions:

- Top level: CMakeLists.txt, DEMFEM_volume_coupling_application.{cpp,h,py}
- custom_elements: volume_coupling_element.{cpp,h}, volume_coupling_particle. {cpp,h}
- custom_python: add_custom_utilities_to_python.{cpp,h}, DEMFEM_volume_coupling_python_application.cpp
- custom_utilities: utility_functions.h

applications/CoSimulationApplication Thin integration layer:

- python_scripts/coupled_solvers/volume_coupling.py: orchestrates DEM and FEM time stepping, executes coupling operations, manages data exchange
- python_scripts/coupling_operations/compute_dem_fem_volume_coupling_force. py: computes FEM nodal coupling forces

- python_scripts/coupling_operations/compute_dem_momentum.py: evaluates DEM momentum and contact forces
- python_scripts/solver_wrappers/kratos/volume_coupling_structural_wrapper. py: toggles ACTIVATION_LEVEL for weighted post-processing

applications/DEMApplication Minimal patch in python_scripts/DEM_procedures.py to register new variables:

```
import\ Kratos Multiphysics. DEMFEMVolume Coupling Application\ as\ VCA\\ model\_part. AddNodalSolution Step Variable (VCA. PARTICLE\_COUPLING\_WEIGHT)\\ model\_part. AddNodalSolution Step Variable (VCA. DISPLACEMENT\_MULTIPLIED\_MASS)\\ model\_part. AddNodalSolution Step Variable (VCA. VELOCITY\_MULTIPLIED\_MASS)\\ model\_part. AddNodalSolution Step Variable (VCA. DEMFEM\_VOLUME\_COUPLING\_FORCE)
```

No other DEM core changes are required.

Build Instructions

The root CMakeLists.txt integrates the application into the Kratos super-build. Enable at configure time:

-DENABLE DEMFEM_VOLUME_COUPLING=ON

Recompile Kratos to include the new application.

2 Coupling Utilities

All helper routines are in custom_utilities/utility_functions.h. They operate exclusively on Kratos-native data structures and MPI communicators, ensuring thread safety and scalability.

Available Operations

- AssignPointLoads applies frictional wall loads on selected FEM boundaries (optional)
- SetNodalCouplingWeightsOnFEMLinearly assigns hybrid weights by linear interpolation between two horizontal planes
- SetNodalCouplingWeightsFromLayers assigns hybrid weights from user-defined SubModelParts
- CalculateDisplacementDifference accumulates DEM-FEM velocity mismatch over time
- ullet CalculateNodalCouplingForces converts the mismatch into FEM nodal forces using a penalty parameter ϵ
- CalculateNodalDEMCouplingForces rescales FEM penalty forces with DEM lumped mass before mapping back
- ullet CalculateMomentum stores $m\, {f u}$ and $m\, {f v}$ in nodal variables for export
- CalculateDEMForces multiplies external forces by nodal mass where $\varpi \neq 0$

Hybrid Region Weighting

Two strategies assign weights $\omega \in [0, 1]$:

- 1. Linear interpolation between planes at y_{FEM} and y_{DEM}
- 2. Layer-based: user supplies a dictionary mapping SubModelPart names to weights

The second method supports arbitrary geometry and dynamic hybrid zones.

Penalty Enforcement

Coupling uses a velocity-based penalty:

- 1. Integrate mismatch: $\Delta \mathbf{u} += (\mathbf{v}_{\text{DEM}} \mathbf{v}_{\text{FEM}}) \Delta t$
- 2. Multiply by penalty ϵ to compute FEM nodal forces
- 3. Rescale forces with DEM lumped mass and map back to particles

3 FEM Side – VolumeCouplingElement

VolumeCouplingElement derives from SmallDisplacementElement. Modifications:

- Override GetIntegrationWeight: scale Gauss weight W_0 by $(1 \bar{\omega})$ where $\bar{\omega}$ is the weighted sum of nodal ω_i
- Override CalculateOnIntegrationPoints: optionally weight output stresses by $(1-\bar{\omega})$ only when ACTIVATION_LEVEL = 1

Stress weighting is used for post-processing to form hybrid stresses; can be disabled.

4 DEM Side – VolumeCouplingParticle

VolumeCouplingParticle derives from SphericParticle. Changes:

- 1. Initialize: set $\varpi = 1$
- 2. GetMass: return $m^* = \varpi m$
- 3. EvaluateBallToBallForcesForPositiveIndentations: apply symmetric weight $\varpi_{12} = \frac{\varpi_1 a_2 + \varpi_2 a_1}{a_1 + a_2}$
- 4. EvaluateBallToRigidFaceForcesForPositiveIndentations: rescale ball-wall forces similarly

5 CoSimulation Workflow

A custom coupled solver DemFemVolumeCoupledSolver in volume_coupling.py runs the following per step:

- 1. Compute DEM momentum and velocity
- 2. Map DEM data \rightarrow FEM
- 3. Assemble FEM penalty forces
- 4. Map FEM forces \rightarrow DEM
- 5. Finalize coupling (mass scaling, extra loads)
- 6. Advance both DEM and FEM solvers

Lightweight Python modules implement each stage:

- compute_dem_momentum.py gather DEM momentum and scale forces
- compute_dem_fem_volume_coupling_force.py assemble and map FEM penalty forces
- volume_coupling.py orchestrates the full sequence

6 Case Setup

```
A typical folder layout is: (Please check the .json files for the exact folder-file layout)

case/

CoSimulationParameters.json
dem/

ProjectParametersDEM.json
Materials.json
particles.mdpa
boundaries.mdpa
fem/
ProjectParametersFEM.json
StructuralMaterials.json
model.mdpa
```

Check the exact folder structure and names in the JSON files in the tests folder.

DEM Inputs

- ProjectParametersDEM.json solver settings, time stepping, processes
- Materials.json particle and wall material data
- .mdpa particle and boundary geometries

FEM Inputs

- ProjectParametersFEM.json solver settings, BCs, output
- StructuralMaterials.json FEM material properties
- model.mdpa mesh and SubModelParts

CoSimulation Inputs

• CoSimulationParameters.json – participants, coupling sequence, mapping settings, scheme, time control

Practical Notes

- Maintain consistent units between DEM and FEM
- Use SubModelParts for BCs, loads, mapping interfaces
- ullet Example cases are in applications/DEMFEMVolumeCouplingApplication/tests

7 Quick Start

- 1. Build Kratos with:
 - -DENABLE DEMFEM VOLUME COUPLING=ON
- 2. Prepare DEM, FEM, and CoSimulation parameter files (see tests)
- 3. Run with:

python3 co_simulation_run.py —cosp-file CoSimulationParameters.json

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