```
1: (* $Id: lazythunk.ml, v 361.1 2006-03-02 18:48:23-08 - - $ *)
 2:
 3: open Printf
 4:
 5: (* re-implementation of module Lazy *)
 6:
7: type 'a promise =
       | Value of 'a
8:
9:
        | Excep of exn
10:
        | Delay of (unit -> 'a)
11:
12: type 'a thunk = 'a promise ref
13:
14: let force thunk = match !thunk with
15:
        | Value value -> value
        | Excep excep -> raise excep
17:
        | Delay delay -> (try let value = delay ()
18:
                                in (thunk := Value value; value)
19:
                           with excep -> (thunk := Excep excep;
20:
                                          raise excep))
21:
22: let (!!) = force
24: (* stream and lazy stuff *)
26: type 'a stream = End | Stream of 'a * 'a stream thunk
27:
28: exception End_stream
29:
30: let (@::) car cdr = Stream (car, cdr)
32: let head stream = match stream with
33:
        | End -> raise End_stream
34:
        | Stream (car, _) -> car
35:
36: let tail stream = match stream with
        | End -> raise End_stream
37:
38:
        | Stream (_, cdr) -> !!cdr
39:
40: let rec take n stream = match n, stream with
41:
        | _, End -> End
42:
        \mid n, \_ when n <= 0 -> End
        | _, Stream (car, cdr) ->
43:
44:
              Stream (car, ref (Delay (fun () -> take (n - 1) !!cdr)))
45:
46: let rec list_of_stream stream = match stream with
47:
        | End -> []
        | Stream (car, cdr) -> car :: list_of_stream !!cdr
48:
49:
50: let rec drop n stream = match n, stream with
51:
        | _, End -> End
52:
        \mid n, \_ when n <= 0 -> stream
53:
        | _, Stream (car, cdr) -> drop (n - 1) !!cdr
54:
55: let rec iter fn stream = match stream with
        | End -> ()
        | Stream (car, cdr) -> (fn car; iter fn !!cdr)
57:
58:
```

```
59: let rec iter2 fn stream1 stream2 = match stream1, stream2 with
         | End, _ -> ()
 60:
         | _, End -> ()
 61:
         | Stream (car1, cdr1), Stream (car2, cdr2)
 62:
               -> (fn car1 car2; iter2 fn !!cdr1 !!cdr2)
 63:
 64:
 65: let rec iter3 fn stream1 stream2 stream3 =
         match stream1, stream2, stream3 with
 66:
         | End, _, _ -> ()
 67:
         | _, End, _ -> ()
 68:
 69:
         | _, _, End -> ()
 70:
         | Stream (car1, cdr1), Stream (car2, cdr2), Stream (car3, cdr3)
 71:
               -> (fn car1 car2 car3; iter3 fn !!cdr1 !!cdr2 !!cdr3)
 72:
 73: let rec map2 fn stream1 stream2 = match stream1, stream2 with
         | End, _ -> End
 75:
         | _, End -> End
 76:
         | Stream (car1, cdr1), Stream (car2, cdr2)
 77:
               -> Stream (fn car1 car2,
                           ref (Delay (fun () -> map2 fn !!cdr1 !!cdr2)))
 78:
 79:
 80: (* stuff that uses streams and Nums *)
 82: let rec range head limit =
 83:
         if head > limit
         then End
 84:
         else let next = head + 1
              in Stream (head, ref (Delay (fun () -> range next limit)))
 86:
 87:
 88: let naturals = range 0 max_int
 89:
 90: let fac n =
 91:
         let rec fac' n m = match n with
 92:
             \mid 0 \rightarrow m
 93:
             | n -> fac' (n - 1) (n * m)
 94:
         in if n < 0 then invalid_arg "fac"</pre>
 95:
                      else fac' n 1
 96:
 97: let printfac n = printf "2d! = 10d\n" n (fac n)
 99: let printfacs n = iter printfac (take n naturals)
100:
101: (* lazy let fib = 0 : 1 : map2 (+) fib (tail fib) *)
102:
103: let fibstream =
104:
         let rec stream0 = Stream (0, stream1)
             and stream1 = ref (Delay (fun () -> Stream (1, stream2)))
105:
             and stream2 = ref (Delay (fun () -> map2 (+) stream0 !!stream1))
106:
107:
         in stream0
108:
109: let printfib n nfib nfib' =
        printf "fib(%3d) = %11d, %20.15f\n"
111:
                n nfib (float_of_int nfib /. float_of_int nfib')
112:
113: let printfibs n = iter3 printfib naturals
114:
                                       (take n fibstream)
115:
                                       (take n (drop 1 fibstream))
116:
```

```
1: type 'a promise = Value of 'a | Excep of exn | Delay of (unit -> 'a)
 2: type 'a thunk = 'a promise ref
 3: val force : 'a promise ref -> 'a
 4: val ( !! ) : 'a promise ref -> 'a
 5: type 'a stream = End | Stream of 'a * 'a stream thunk
 6: exception End_stream
7: val ( @:: ) : 'a -> 'a stream thunk -> 'a stream
8: val head : 'a stream -> 'a
9: val tail : 'a stream -> 'a stream
10: val take : int -> 'a stream -> 'a stream
11: val list_of_stream : 'a stream -> 'a list
12: val drop : int -> 'a stream -> 'a stream
13: val iter : ('a -> 'b) -> 'a stream -> unit
14: val iter2 : ('a \rightarrow 'b \rightarrow 'c) \rightarrow 'a stream \rightarrow 'b stream \rightarrow unit
15: val iter3:
      ('a -> 'b -> 'c -> 'd) -> 'a stream -> 'b stream -> 'c stream -> unit
17: val map2 : ('a -> 'b -> 'c) -> 'a stream -> 'b stream -> 'c stream
18: val range : int -> int -> int stream
19: val naturals : int stream
20: val fac : int -> int
21: val printfac : int -> unit
22: val printfacs : int -> unit
23: val fibstream : int stream
24: val printfib : int -> int -> int -> unit
25: val printfibs : int -> unit
```