

# **EC 415: Homework 4**

Due by Friday 04/09/2021 6:00PM

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**Exercise 4.21**

Suppose that the noise in `improvesnr.m` is replaced with narrowband noise (as discussed in Section 4.1.3). Investigate the improvements in SNR

- a. when the narrowband interference occurs outside the 3000 to 4000 Hz passband,
- b. when the narrowband interference occurs inside the 3000 to 4000 Hz passband.

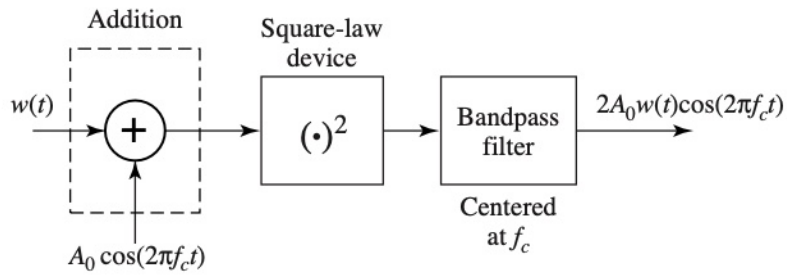
For part (a) use  $n = 0.1 * (\cos(2 * \pi * f_1 * t) + \cos(2 * \pi * f_2 * t))$  to model narrowband noise around the frequencies  $f_1$  and  $f_2$ . Choose  $f_1 = 2000$  Hz and  $f_2 = 5000$  Hz.

For part (b) use  $n = 0.1 * \cos(2 * \pi * f_3 * t)$  to model narrowband noise around the frequency  $f_3$ . Choose  $f_3 = 3500$  Hz.

**Solution**

- a. TODO
- b. TODO

## Exercise 5.9



**Figure 5.8** The square-law mixing transmitter of Exercises 5.9 through 5.11.

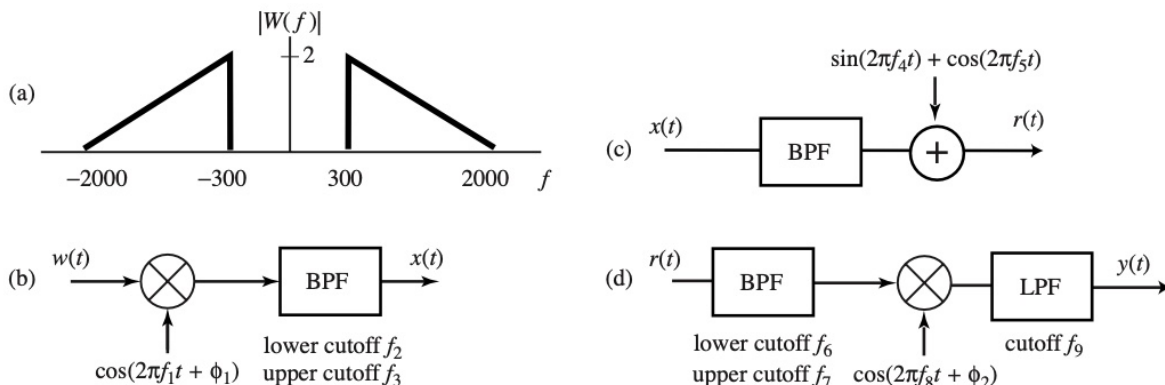
Figure 1: Figure 5.8

Consider the system shown in Figure 5.8. Show that the output of the system is  $2A_0 w(t) \cos(2\pi f_c t)$ , as indicated.

**Solution**

TODO

## Exercise 5.12



**Figure 5.9** The transmission system for Exercise 5.12: (a) the magnitude spectrum of the message, (b) the transmitter, (c) the channel, and (d) the receiver.

Figure 2: Figure 5.9

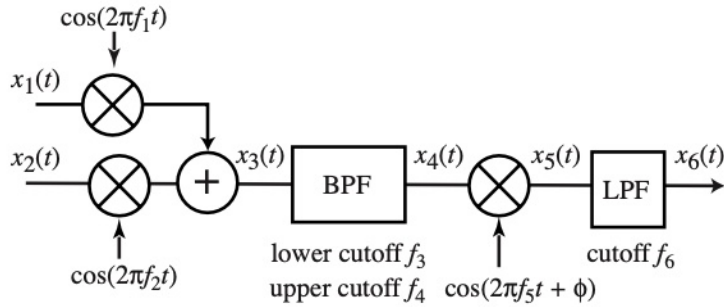
Consider the transmission system of Figure 5.9. The message signal  $w(t)$  has the magnitude spectrum shown in part (a). The transmitter in part (b) produces the transmitted signal  $x(t)$ , which passes through the channel in part (c). The channel scales the signal and adds narrowband interferers to create the received signal  $r(t)$ . The transmitter and channel parameters are  $\phi_1 = 0.3$  radians,  $f_1 = 24.1$  kHz,  $f_2 = 23.9$  kHz,  $f_3 = 27.5$  kHz,  $f_4 = 29.3$  kHz, and  $f_5 = 22.6$  kHz. The receiver processing  $r(t)$  is shown in Figure 5.9(d). All bandpass and lowpass filters are considered ideal, with a gain of unity in the passband and zero in the stopband.

- Sketch  $|R(f)|$  for  $30 \text{ kHz} \leq f \leq 30 \text{ kHz}$ . Clearly indicate the amplitudes and frequencies of key points in the sketch.
- Assume that  $\phi_2$  is chosen to maximize the magnitude of  $y(t)$  and reflects the value of  $\phi_1$  and the delays imposed by the two ideal bandpass filters that form the received signal  $r(t)$ . Select the receiver parameters  $f_6$ ,  $f_7$ ,  $f_8$ , and  $f_9$ , so the receiver output  $y(t)$  is a scaled version of  $w(t)$ .

## Solution

TODO

## Exercise 5.16



**Figure 5.11** The transmission system of Exercise 5.16.

Figure 3: Figure 5.11

Consider the scheme shown in Figure 5.11. The absolute bandwidth of the baseband signal  $x_1$  is 6 MHz and that of the baseband signal  $x_2(t)$  is 4MHz,  $f_1 = 164\text{MHz}$ ,  $f_2 = 154\text{MHz}$ ,  $f_3 = 148\text{MHz}$ ,  $f_4 = 160\text{MHz}$ ,  $f_5 = 80\text{MHz}$ ,  $\phi = \pi/2$ , and  $f_6 = 82\text{MHz}$ .

- What is the absolute bandwidth of  $x_3(t)$ ?
- What is the absolute bandwidth of  $x_5(t)$ ?
- What is the absolute bandwidth of  $x_6(t)$ ?
- What is the maximum frequency in  $x_3(t)$ ?
- What is the maximum frequency in  $x_5(t)$ ?

### Solution

- TODO
- TODO
- TODO
- TODO
- TODO

## Question 5

Consider the last line of AMLarge.m (see Listing 5.1):

$envv = (\pi/2) * filter(b, 1, abs(v));$

Why is the output of the filter multiplied by the constant  $\pi/2$ ? Justify your answer.

**Solution**

TODO

## Question 6

The attached `qam_hw.mat` file is a QAM passband signal that is the sum of two modulated messages  $w_1$  and  $w_2$ . These messages were respectively modulated using cosine and sine functions, with carrier signal  $f = 1000$  Hz. The sampling period is  $T = 1/10000$ s and the total duration of the signal is 0.3s. Note that these parameters are all the same as in the file `AM.m` (listing 5.2 in the textbook). Plot the following:

1. The modulated signal  $v$ .
2. The demodulated signals (before the LPF)  $x_1$  and  $x_2$ .
3. The recovered signals (after the LPF)  $m_1$  and  $m_2$ .

Hints:

1. To load the QAM signal, use the command: `load('qam_hw.mat','v');`
2. Use the same LPF parameters as in `AM.m`.
3. The x-axis should be  $[0, 0.3]$  for all the plots.
4. For the signal  $v$ , the y-axis should be  $[11,11]$ .
5. For the signal  $x_1$  and  $m_1$ , the y-axis should be  $[5,10]$ .
6. For the signals  $x_2$  and  $m_2$ , the y-axis should be  $[10,1]$ .

## Solution

1. TODO
2. TODO
3. TODO