

Task 1 & 2

Consider function $f(x) = \sin x$ in a period $[a, b]$, then approximate $f(x)$ by piecewise function

Task 1

- Step1: Draw the diagram of $f(x)$
- Step2: Cut $[a, b]$ into a set of N intervals $I_j = [x_j, x_{j+1}]$
 - $x_0 = a, x_N = b$
 - $j = 0, 1, 2, \dots, N$
 - Set $a = -10, b = 10$
- Step3: Plot piecewise functions $\tilde{f}(x)$
 - $\tilde{f}(x) = f(x_{j+\frac{1}{2}})$
 - $x \in [x_j, x_{j+1}]$

- Step4:

$$k \quad N_x \quad e_k = \sum_{j=0}^{n-1} \int_{x_j}^{x_{j+1}} |\tilde{f}(x) - f(x)| \log_2\left(\frac{e_k}{e_{k-1}}\right)$$

1 10

2 20

3 40

4 80

Task 2

- Step1: Draw the diagram of $f(x)$
- Step2: Cut $[a, b]$ into a set of N intervals $I_j = [x_j, x_{j+1}]$
 - $x_0 = a, x_N = b$
 - $j = 0, 1, 2, \dots, N$
 - $\Delta x = \frac{b-a}{N}$
 - Set $a = -10, b = 10$
- Step3: Plot piecewise functions $\bar{f}(x)$
 - $\bar{f}(x) = \frac{1}{\Delta x} \int_{I_j} f(x) dx$
 - $x \in [x_j, x_{j+1}]$

- Step4:

$$k \quad N_x \quad e_k = \sum_{j=0}^{n-1} \int_{x_j}^{x_{j+1}} |\bar{f}(x) - f(x)| \log_2\left(\frac{e_k}{e_{k-1}}\right)$$

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