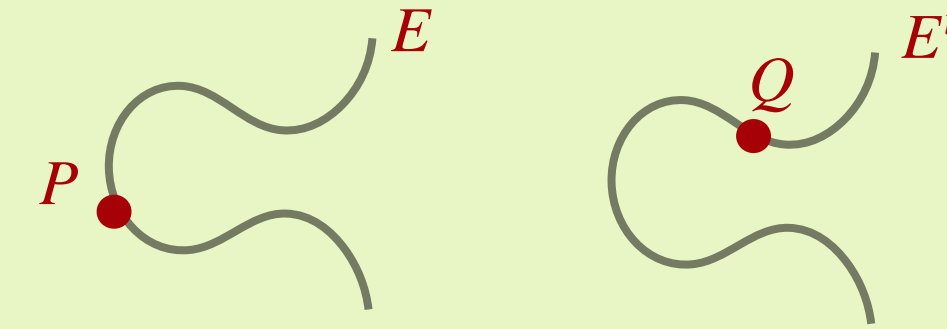


Isogenies & Pairings

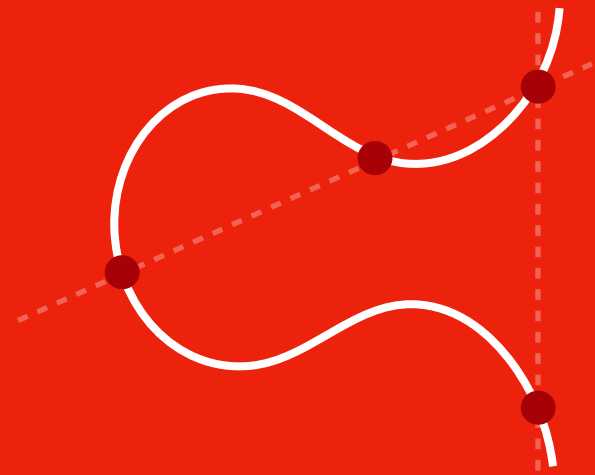
the twist of E

Twist over \mathbb{F}_p of supersingular curve E

- a curve E^t with $p + 1$ points over \mathbb{F}_p
- isomorphic to a specific subset of $E(\mathbb{F}_{p^2})$
- used in CSIDH to “move backwards” in graph
- want $P \in E(\mathbb{F}_p)$ and $Q \in E^t(\mathbb{F}_p)$, both full order



1

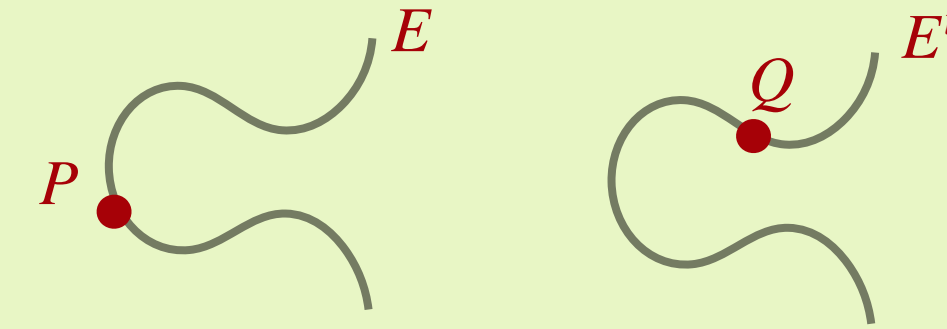


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1

consider P and Q as

$$P = P_0 + P_1 + \dots + P_n$$

$$Q = Q_0 + Q_1 + \dots + Q_n$$

2

let $r = p + 1$

Tate pairing $e_r(P, Q)$ captures
where **both** $P_i, Q_i \neq \mathcal{O}$