Pairings map elliptic curve problems to finite field problems

Elliptic curve arithmetic is slow

Finite field arithmetic is (very) fast