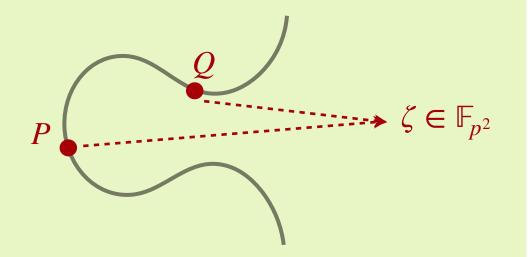
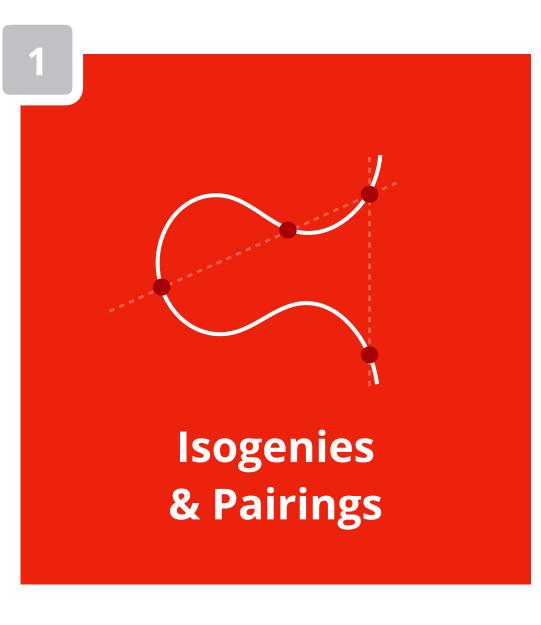


& Pairings

## bilinear pairing from torsion groups to fields

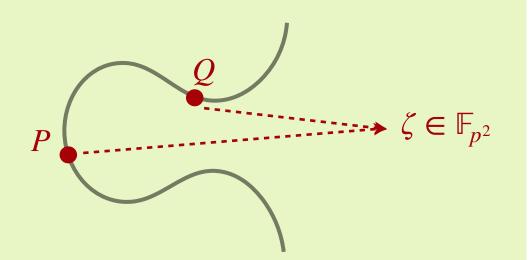
- choose a degree *r*
- take point P of order r on E, that is  $P \in E(\mathbb{F}_{p^2})[r]$
- take point Q on E such that  $Q \in E(\mathbb{F}_{p^2})/rE(\mathbb{F}_{p^2})$
- then  $e_r(P,Q) = \zeta \in \mu_r$





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## in our specific case

Formally, this pairing is abstract. Specifically in our case,  $p+1=4\cdot\ell_1\cdot\ell_2\cdot\ldots\cdot\ell_n$  there is a nice interpretation of this pairing.

Choose r dividing p+1, say  $r=\prod \ell_i=\frac{p+1}{4}$  then for  $P\in E(\mathbb{F}_p)$  we get

$$P = 0 + P_1 + P_2 + \dots + P_n.$$