



Applying pairings in isogeny crypto



fast pairings

Optimized pairing
computation for the specific
scenario $P \in E(\mathbb{F}_p)$, $Q \in E'(\mathbb{F}_p)$

&



core idea

For $P \in E(\mathbb{F}_p)$ and $Q \in E'(\mathbb{F}_p)$,
don't use curve arithmetic
but pairing $e(P, Q)$ to get
overlap in orders!

Faster isogeny subroutines



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verify full torsion P

In some CSIDH variants, we are given $P \in E(\mathbb{F}_p)$ and $Q \in E'(\mathbb{F}_p)$.

Q: verify that both P and Q have order $p + 1$, e.g. full torsion points