

**Speeding-up  
general pairings**

### pairing crypto

Choose a “nice” curve  $E$ ,  
Choose a “nice” prime  $p$ ,  
to do **pairings** with

Computing  $e(P, Q)$   
is quite **fast**!



### isogeny crypto

Choose a “nice” curve  $E$ ,  
Choose a “nice” prime  $p$ ,  
to do **isogenies** with

These are mediocre curves,  
and definitely bad primes,  
to do **pairings** with

Computing  $e(P, Q)$   
seems way too **slow**!



### core idea

For  $P \in E(\mathbb{F}_p)$  and  $Q \in E'(\mathbb{F}_p)$ ,  
don't use curve arithmetic  
but pairing  $e(P, Q)$  to get  
overlap in orders!

### MAIN RESULTS

1

make pairings  
great again

2

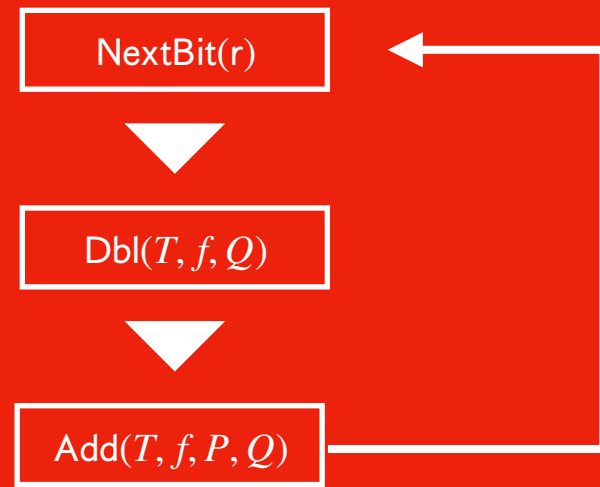
apply core idea

3

faster isogeny  
algorithms!

first  
this

then  
this



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### general notice

Computing pairings fast is quite technical.  
Better suited for papers than slides



### core idea

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don't use curve arithmetic  
but pairing  $e(P, Q)$  to get  
overlap in orders!



### general approach

Instead I describe the general approach,  
and leave all details out