PART 3 New Dimensions

In the words of the HD master

"If we know the value of $\varphi: E \to E'$ on enough nice points, then we know how to efficiently evaluate it everywhere"

- Damien Robert



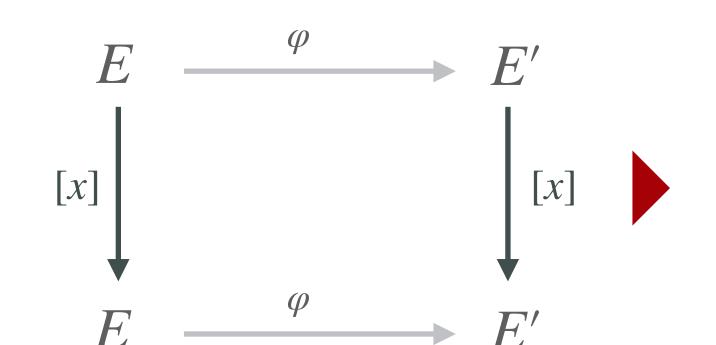
HD representations

instead of describing 1D isogeny $\varphi: E \to E'$ by its kernel $\ker \varphi$, we can also describe it by $E, P_1, ..., P_n, \varphi(P_1), ..., \varphi(P_n)$, for enough points $P_i \in E$

then, with Kani's lemma & improvements, compute $\varphi(Q)$ for any other $Q \in E$

isogeny embedding (rough sketch)

We want to embed the 1-dimensional isogeny $\varphi: E \to E'$ and we assume we know P_1, \ldots, P_n and images $\varphi(P_1), \ldots, \varphi(P_n)$. Assume for the moment that $\deg \varphi = 2^n - x^2$ for some $x \in \mathbb{Z}$



We know and can compute [x] easily! So we can apply Kani's!

$$\Phi: E \times E' \to E \times E'$$

As Φ of degree 2^n , easy to compute and we can use Φ to compute $\varphi(Q)$ for any other point $Q \in E$



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