PART 2 The Tate Profile

Definition 4. Assume $E[m] \subseteq E(\mathbb{F}_q)$ and let (P_1, P_2) be a basis for E[m]. Then, the m-Tate profile is the map $t_{[m]} : E(\mathbb{F}_q) \to \mu_{m'}^2 \qquad Q \ \mapsto \ \left(\ t_2(P_1, Q), \ t_2(P_2, Q) \ \right).$

For $Q \in E(\mathbb{F}_q)$, we say that $t_{[m]}(Q)$ is the *m-profile* of Q. When $t_{[m]}(Q) = (1,1)$, we say the profile is *trivial*.



La Siesta (1982)

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If the Tate pairing t_m is bilinear, then the Tate profile $t_{\lceil m \rceil}$ is linear.



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