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$$E_A : y^2 = x^3 + Ax^2 + x, \qquad \text{with } A \in \mathbb{F}_{p^2}.$$

If a point $P = (x_P, y_P) \in E(\mathbb{F}_{p^2})$ has x_P non-square, then P has order divisible by 2^n

Tate
Pairing?

PART 1

The Tate Pairing

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Theorem 3. For an elliptic curve $E : y^2 = (x - r_1)(x - r_2)(x - r_3)$ with $r_i \in \mathbb{F}_{p^2}$, we have

$$P \in [2]E(\mathbb{F}_{p^2}) \qquad \textit{if and only if} \qquad (x_P - r_1),\ (x_P - r_2), \text{ and } (x_P - r_3) \text{ are squares.}$$

Consequently, $P \in E(\mathbb{F}_{p^2}) \setminus [2]E(\mathbb{F}_{p^2})$ if any $(x_P - r_i)$ is a non-square.

Tate Pairing?