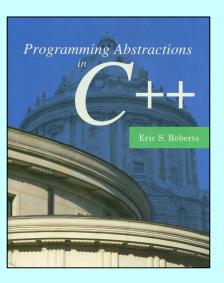
#### CHAPTER 15

#### Maps

A map was a fine thing to study when you were disposed to think of something else . . . .

-George Eliot, Middlemarch, 1874



- 15.1 Implementing maps using vectors
- 15.2 Lookup tables
- 15.3 Hashing
- 15.4 Implementing the HashMap class



### The Map<type, type> Class

- A *map* is conceptually similar to a dictionary in real life (and in Python), which allows you to look up a word to find its meaning.
- The Map class is a generalization of this idea that provides an association between an identifying tag called a *key* (e.g., the word in a dictionary) and an associated *value* (e.g., the definition of the word in the dictionary), which may be a much larger and more complicated structure.
- Map declaration: Map<key type, value type> map;
- The type for the keys stored in a Map must define a natural ordering, usually through a less function and/or < operator so that the keys can be compared and ordered.
- E.g., two most commonly used maps:

```
Map<string, string> dictionary;
Map<string, double> symbolTable;
```



## Methods in the Map Classes

• A *map* associates *keys* and *values*. The Stanford library offers two flavors of maps, Map and HashMap (more about hash later), both of which implement the following methods:

#### map.size()

Returns the number of key/value pairs in the map.

#### map.isEmpty()

Returns **true** if the map is empty.

#### map.put(key, value)

or

map[key] = value;

Makes an association between key and value, discarding any existing one.

#### map.get(key)

OY

map[key]

Returns the most recent value associated with key.

#### map.containsKey(key)

Returns true if there is a value associated with key.

#### map.remove(key)

Removes key from the map along with its associated value, if any.

#### map.clear()

Removes all key/value pairs from the map.

## Simplifying the Map Abstraction

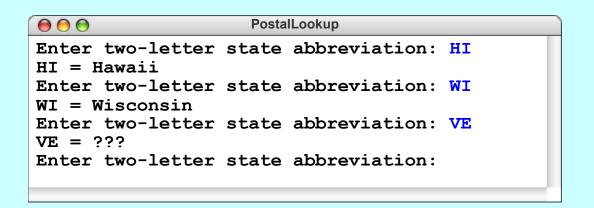
- Although templates offer considerable flexibility when you are designing a collection class, they also complicate both the interface and the implementation, making them harder to follow.
- To make sure that you understand the details of the various strategies for implementing maps, this chapter simplifies the interface so that both the keys and values are always strings (e.g., a dictionary). The resulting class is called **StringMap**.
- Although the previous slide included a more expansive set of methods, this lecture looks only at put, get, and a private method findkey.
- Once you understand how to implement the StringMap class using each of the possible representations, you can add the remaining methods and use the C++ template mechanism to generalize the key and value types, just like the extension from CharStack to Stack.

### An Illustrative Mapping Application

- Suppose that you want to write a program that displays the name of a US state given its two-letter postal abbreviation.
- This program is an ideal application for the StringMap class because what you need is a map between two-letter codes and state names. Each two-letter code uniquely identifies a particular state and therefore serves as a key for the StringMap; the state names are the corresponding values.
- To implement this program in C++, you need to perform the following steps, which are illustrated on the following slide:
  - 1. Create a StringMap containing the key/value pairs.
  - 2. Read in the two-letter abbreviation to translate.
  - 3. Call get on the StringMap to find the state name.
  - 4. Print out the name of the state.

### The PostalLookup Program

```
int main() {
   StringMap stateMap;
   initStateMap(stateMap);
   while (true) {
      cout << "Enter two-letter state abbreviation: ";
      string code = getLine();
      if (code == "") break;
      if (stateMap.containsKey(code)) {
           cout << code << " = " << stateMap.get(code) << endl;
      } else {
           cout << code << " = ???" << endl;
      }
    }
}</pre>
```



AL=Alabama
AK=Alaska
AZ=Arizona
...
FL=Florida
GA=Georgia
HI=Hawaii
...
WI=Wisconsin
WY=Wyoming

## Methods in the Vector<type> Class

#### vec.size()

Returns the number of elements in the vector.

#### vec.isEmpty()

Returns **true** if the vector is empty.

#### vec.get(i)

or

vec[i]

Returns the i<sup>th</sup> element of the vector.

#### vec.set(i, value)

or

vec[i] = value;

Sets the i<sup>th</sup> element of the vector to value.

#### vec.add(value)

or

vec += value;

Adds a new element to the end of the vector.

#### vec.insertAt(index, value)

Inserts the value before the specified index position.

#### vec.removeAt(index)

Removes the element at the specified index.

#### vec.clear()

Removes all elements from the vector.

### The Vector-Based stringmap Interface

```
/*
 * File: stringmap.h
 * This interface exports the StringMap class, which maintains a collection
 * of key/value pairs, both of which are of type string.
 */
#ifndef stringmap h
#define stringmap h
#include <string>
#include "vector.h"
class StringMap {
public:
/*
 * Constructor: StringMap
 * Usage: StringMap map;
 * Initializes a new empty StringMap.
 */
   StringMap();
```

### The Vector-Based stringmap Interface

```
/*
 * Destructor: ~StringMap
* Frees any heap storage associated with this map.
*/
  ~StringMap();
/*
 * Method: get
 * Usage: string value = map.get(key);
 * Returns the value for key or the empty string, if key is unbound.
 */
  std::string get(const std::string & key) const;
/*
 * Method: put
 * Usage: map.put(key, value);
 * Associates key with value in this map.
 */
  void put(const std::string & key, const std::string & value);
```

## he Vector-Based stringmap Interface

```
/* Private section */
private:
/*
 * Type: KeyValuePair
 * This type combines a key and a value into a single structure.
   struct KeyValuePair {
      std::string key;
      std::string value;
   };
/* Instance variables */
   Vector<KeyValuePair> bindings;
/* Private function prototypes */
   int findKey(const std::string & key) const;
};
#endif
```

#### Vector-Based Code for StringMap

```
/*
 * File: stringmap.cpp
 * This interface exports the StringMap class using a Vector.
 */
#include <string>
#include "stringmap.h"
using namespace std;
/*
 * Implementation notes: StringMap constructor and destructor
 * All dynamic allocation is handled by the Vector class.
 */
StringMap::StringMap() { }
StringMap::~StringMap() { }
```

### Vector-Based Code for StringMap

```
/*
 * Implementation notes: put, get
 * These methods use findKey to search for the specified key.
 */
string StringMap::get(const string & key) const {
   int index = findKey(key);
   return (index == -1) ? "" : bindings.get(index).value;
void StringMap::put(const string & key, const string & value) {
   int index = findKey(key);
   if (index == -1) {
      KeyValuePair entry;
      entry.key = key;
      index = bindings.size();
     bindings.add(entry);
   bindings[index].value = value;
```

#### Vector-Based Code for StringMap

```
/*
 * Private method: findKey
 * Returns the index at which the key appears, or -1 if the key is not found.
 */
int StringMap::findKey(const string & key) const {
   for (int i = 0; i < bindings.size(); i++) {
      if (bindings.get(i).key == key) return i;
   return -1;
```



## Implementation Strategies for Maps

- There are several strategies you might choose to implement the map operations get and put. Those strategies include:
  - 1. **Linear search**. Keep track of all the key/value pairs in a vector. In this model, both the **get** and **put** operations run in O(N) time.
  - 2. **Binary search**. If you keep the vector sorted by the key, you can use binary search to find the key. Using this strategy improves the performance of **get** to...?
    - $O(\log N)$ . But to keep the vector sorted, **put** runs in...? O(N). Why?
  - 3. **Table lookup in a grid**. In this specific example, you can store the state names (two-character code) in a 26 × 26 **Grid<string>** in which the first and second indices correspond to the two letters in the code. Because you can now find any code in a single step, this strategy is *O*(1), although this performance comes at a cost in memory space (only 50/676 occupied).

## The Lookup-Table Strategy

	Α	В	С	D	E	F
Α						
В						
С	California					
D					Delaware	
Ε						
F						
G	Georgia					
Н						
I	Iowa			Idaho		
J						
K						
L	Louisiana					
M	Massachusetts			Maryland	Maine	

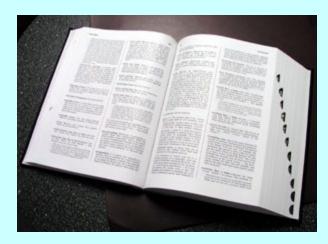
### The Lookup-Table Strategy

• Why is it O(1)?

```
string getStateName(string key, Grid<string> & grid) {
   char row = key[0] - 'A';
   char col = key[1] - 'A';
   if (!grid.inBounds(row, col) || grid[row][col] == "") {
      error("No state name for " + abbr);
   }
   return grid[row][col];
}
```

## The Idea of Hashing

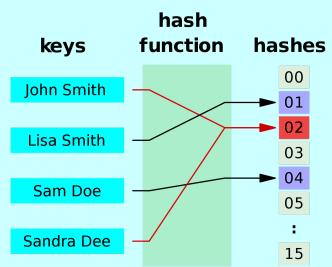
- The lookup-table strategy from the preceding slide shows that one can make the **get** and **put** operations run very quickly, even to the point that the cost of finding a key is independent of the number of keys in the table. This O(1) performance is possible only if you know where to look for a particular key.
- To get a sense of how you might achieve this goal in practice, it helps to think about how you find a word in a dictionary. Most dictionaries have thumb index that indicate where each letter appear. Words starting with A are in the A section, and so on.
- The most common implementations of maps use a strategy called *hashing*, which is conceptually similar to the thumb index in a dictionary. The critical idea is that you can improve performance enormously if you use the key to figure out where to look.





### Hash Maps

- The StringMap class implemented using the hashing strategy is called a *hash map* (sometimes a *hash table*).
- The implementation requires the existence of a free function (called a *hash function*) that transforms a key into a nonnegative integer (called a *hash code*), preferably in constant time. The hash code tells the implementation where it should look for a particular key, thereby reducing the search time dramatically.
- The important things to remember about hash codes are:
  - 1. From a certain hash function, every key has a hash code, and only one hash code.
  - 2. If two keys are different, they ideally should not, but practically could, have the same hash code (called *collision*).

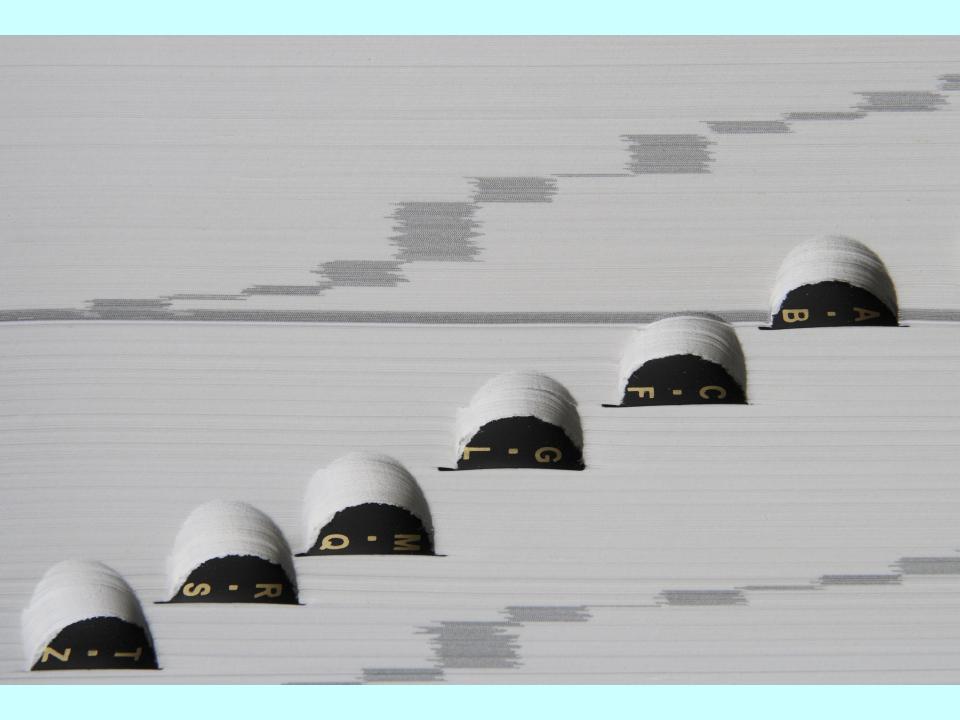


#### **Hash Functions**

- One extreme example for a hash function is the function that transforms anything to 0. In that case, the hash map turns back into a regular map.
- The other extreme example is the function that transforms the N different keys exactly to 0, 1, ..., N-1 (mapping keys to indices) in O(1) time. But imaging how difficult it would be for you to find such a function (see <u>perfect hash function</u>).
- A simple hash function that simulates the idea of the thumb index in a dictionary:

```
int page = thumbIndexVector[key[0]-'A'];
```

• Is this hash function good? Why?





#### Hash Functions

- To achieve the high level of efficiency that hashing offers, a hash function must have the following two properties:
  - 1. The function must be inexpensive to compute.
  - 2. The function should distribute keys as uniformly as possible across the integer range, to minimize *collisions*.
- Hash functions are extremely subtle and often depend on sophisticated mathematics. Most implementations use techniques similar to those for generating pseudorandom numbers, to ensure that the results are hard to predict, hence are unlikely to exhibit any higher level of collision than one would expect by chance (e.g., thumb index collisions are not by chance).
- Fortunately, the correctness of the algorithm is not affected by the collision rate. Implementations that use poorly designed hash functions run more slowly but nonetheless continue to give correct results.

### The hashCode Function for Strings

```
const int HASH SEED = 5381; /* Starting point for first cycle */
const int HASH MULTIPLIER = 33; /* Multiplier for each cycle */
const int HASH MASK = unsigned(-1) >> 1; /* Largest positive integer */
/*
 * Function: hashCode
 * Usage: int code = hashCode(key);
 * This function takes a string key and uses it to derive a hash code,
 * which is nonnegative integer related to the key by a deterministic
 * function that distributes keys well across the space of integers.
 * The specific algorithm used here is called djb2 after the initials
 * of its inventor, Daniel J. Bernstein, Professor of Mathematics at
 * the University of Illinois at Chicago.
 */
int hashCode(const string & str) {
   unsigned hash = HASH SEED;
   int nchars = str.length();
   for (int i = 0; i < nchars; i++) {
                                                    Things that you only need
      hash = HASH MULTIPLIER * hash + str[i];
                                                    to know that you don't
   return (hash & HASH MASK);
                                                    know. I don't need you to
                                                    memorize it for the exam.
```

## Why is it called hash?





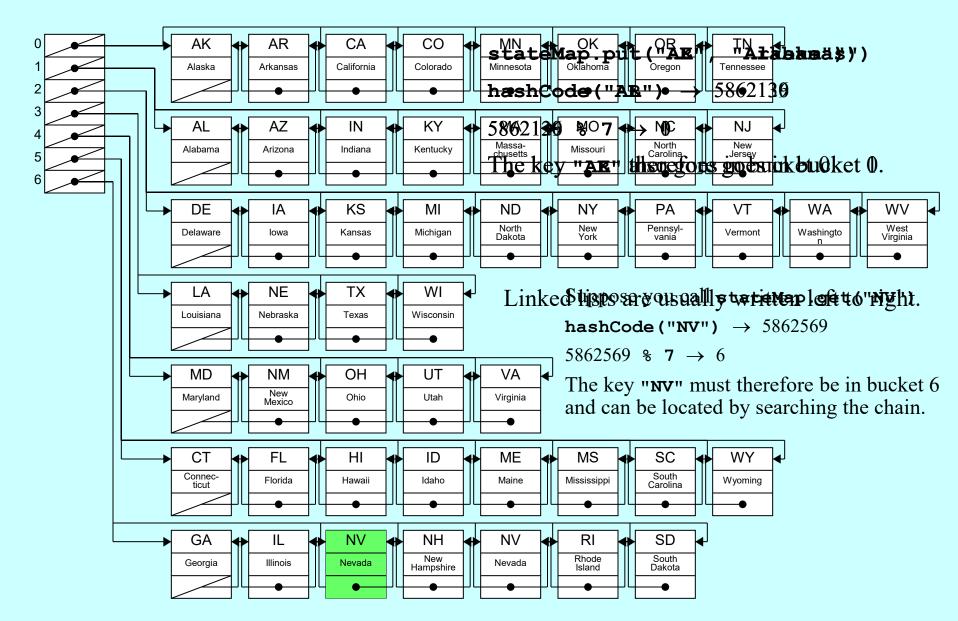
### The Bucket Hashing Strategy

- One common strategy for implementing a map is to use the hash code for each key to select an index into an array that will contain all the keys with that hash code. Each element of that array is conventionally called a *bucket*.
- In practice, the array of buckets is smaller than the number of hash codes, making it necessary to convert the hash code into a bucket index, typically by executing a statement like

```
int index = hashCode(key) % nBuckets;
```

- The value in each element of the bucket array cannot be a single key/value pair given the chance that different keys fall into the same bucket, i.e., *collisions*.
- To take account of the possibility of collisions, each element of the bucket array points to a linked list of key/value pairs whose keys fall into that bucket (called separate chaining) as illustrated on the next slide. Another strategy, called open addressing, uses a single array (Ch.15 Ex.9&10).

### Simulating Bucket Hashing

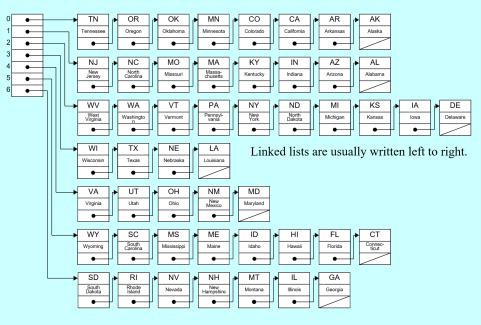


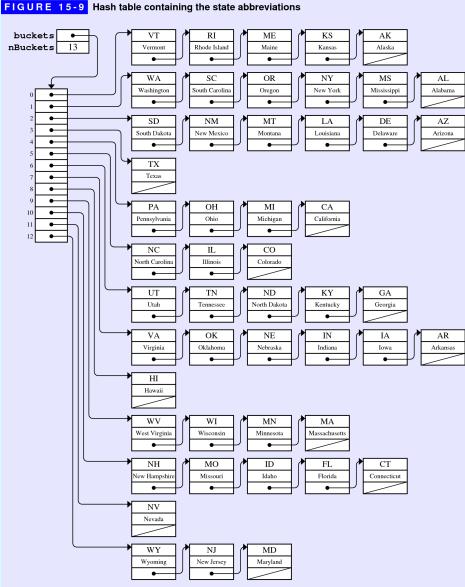
## Achieving O(1) Performance

- The simulation on the previous slide uses only seven buckets to emphasize what happens when collisions occur: the smaller the number of buckets, the more likely collisions become.
- In practice, the implementation of StringMap would use a much larger value for nBuckets to minimize the opportunity for collisions. If the number of buckets is considerably larger than the number of keys, most of the bucket chains will either be empty or contain exactly one key/value pair.
- The ratio of the number of keys to the number of buckets is called the *load factor* of the map. Because a map achieves O(1) performance only if the load factor is small, the library implementation of HashMap increases the number of buckets when the map becomes too full. This process is called *rehashing*.
- O(1) is achieved on average, and the worst case is still O(N).



## Rehashing





### Private Section of the StringMap Class

```
/* Private section */
private:
/* Type definition for cells in the bucket chain */
  struct Cell {
     std::string key;
     std::string value;
     Cell* link;
  };
/* Instance variables */
  Cell* *buckets; /* Dynamic array of pointers to cells */
  int count; /* The number of entries in the map */
/* Private method prototypes */
  Cell* findCell(int bucket, std::string key);
/* Make copying illegal */
  StringMap (const StringMap & src) { }
  StringMap & operator=(const StringMap & src) { return *this; }
```

```
/*
 * File: stringmap.cpp
 * This file implements the stringmap.h interface using a hash table
 * as the underlying representation.
 */
#include <string>
#include "stringmap.h"
using namespace std;
/*
 * Implementation notes: StringMap constructor and destructor
 * The constructor allocates the array of buckets and initializes each
 * bucket to the empty list. The destructor frees the allocated cells.
 */
StringMap::StringMap() {
   nBuckets = INITIAL BUCKET COUNT;
  buckets = new Cell*[nBuckets];
   for (int i = 0; i < nBuckets; i++) {</pre>
     buckets[i] = NULL;
```

```
StringMap::~StringMap() {
   for (int i = 0; i < nBuckets; i++) {
      Cell *cp = buckets[i];
      while (cp != NULL) {
         Cell *oldCell = cp;
         cp = cp - \lambda ink;
         delete oldCell;
   delete [] buckets;
/*
 * Implementation notes: get
 * This method calls findCell to search the linked list for the matching
 * key. If no key is found, get returns the empty string.
 */
string StringMap::get(const string & key) const {
   Cell *cp = findCell(hashCode(key) % nBuckets, key);
   return (cp == NULL) ? "" : cp->value;
```

```
/*
 * Implementation notes: put
 * The put method calls findCell to search the linked list for the
 * matching key. If a cell already exists, put simply resets the
 * value field. If no matching key is found, put adds a new cell
 * to the beginning of the list for that chain.
 */
void StringMap::put(const string & key, const string & value) {
   int bucket = hashCode(key) % nBuckets;
   Cell *cp = findCell(bucket, key);
   if (cp == NULL) {
      cp = new Cell;
      cp->key = key;
      cp->link = buckets[bucket];
     buckets[bucket] = cp;
   cp->value = value;
```

```
/*
 * Private method: findCell
 * Usage: Cell *cp = findCell(bucket, key);
 * Finds a cell in the chain for the specified bucket that matches key.
 * If a match is found, the return value is a pointer to the cell
 * containing the matching key. If no match is found, findCell
 * returns NULL.
 */
StringMap::Cell *StringMap::findCell(int bucket, const string & key) const {
   Cell *cp = buckets[bucket];
  while (cp != NULL && key != cp->key) {
     return cp;
```



### ementing the HashMap class

nent a more general HashMap (unordered\_map in C++), start from StringMap:

g the missing methods for maps.

- Generalizing the key and value types using templates.
- The algorithm for implementing hash maps imposes several requirements on the type used to represent keys, as follows:
  - The key type must be assignable so that the code can store copies of the keys in the cells.
  - The key type must support the comparison operator == so that the code can tell whether two keys are identical.
  - At the time the template for HashMap is expanded for a specific key type defined by the client, other than the built-in types like string and int, a version of the hashCode function that produces a non-negative integer for every value of the key type must also be provided by the client.

# Methods in the STL map<type> Class

<u>fx</u> Member functi	ions			_
(constructor)	Construct map (public member functi	Construct map (public member function )		
(destructor)	Map destructor (public member funct	ion )		
operator=	Copy container content (public mem	ber function )		
Iterators:				
begin	Return iterator to beginning (public	member function )		
end	Return iterator to end (public member	Modifiers:		
rbegin	Return reverse iterator to reverse b			
rend	Return reverse iterator to reverse e	insert	Insert elem	ents (public member function )
cbegin 🚥	Return const_iterator to beginning	erase	Erase elem	ents (public member function )
cend 🚥	Return const_iterator to end (public	swap	Swap conte	ent (public member function )
crbegin 🚥	Return const_reverse_iterator to re	clear	Clear conte	ent (public member function )
crend •			Construct a	and insert element (public member function )
crend em Return const_reverse_iterator to re		emplace_hint 🚥	Construct a	and insert element with hint (public member function )
Capacity:				
empty Test whether container is empty (pr		Observers:		
size	Return container size (public membe	key_comp	Return key	comparison object (public member function )
max_size	Return maximum size (public memb	value_comp	Return valu	re comparison object (public member function )
_	,	Operations:		
Element access:		find	Get iterator	r to element (public member function )
operator[]	Access element (public member func	count	Count elem	ents with a specific key (public member function )
at Constant (public member func		lower_bound	Return itera	ator to lower bound (public member function )
		upper_bound	Return itera	ator to upper bound (public member function )
		equal_range	Get range of	of equal elements (public member function )
		Allocator:		

get\_allocator

Get allocator (public member function )

## The STL unordered\_map<type> Class

		Modifiers
fx Member fund	<u>emplace</u>	
(constructor)	Construct unordered_map (public member function)	emplace_hint
(destructor)	Destroy unordered map (public member function)	<u>insert</u>
operator=	Assign content (public member function)	<u>erase</u>
		<u>clear</u>
Capacity		<u>swap</u>
<u>empty</u>	Test whether container is empty (public member fund	
<u>size</u>	Return container size (public member function)	Buckets
max_size	Return maximum size (public member function)	bucket_count
		max_bucket_
Iterators		bucket_size
<u>begin</u>	Return iterator to beginning (public member function)	<u>bucket</u>
<u>end</u>	Return iterator to end (public member function)	,
<u>cbegin</u>	Return const_iterator to beginning (public member)	Hash policy
<u>cend</u>	Return const_iterator to end (public member fur ion)	load_factor
		max_load_fac
Element access		<u>rehash</u>
operator[]	Access element (public member function	reserve
<u>at</u>	Access element (public member fun	
		Observers
Element lookup		hash_function
find	Get iterator to element (mber function)	key_eq
count	Count elements with fic key (public member	get_allocator
<u>equal_range</u>	Get range of elem specific key (public me	
	Hash map in C++	£ Non-me
	Trush map in C	

STL since C++11.

ouniers	
<u>emplace</u>	Construct and insert element (public member function)
emplace_hint	Construct and insert element with hint (public member function)
<u>nsert</u>	Insert elements (public member function)
erase	Erase elements (public member function)
<u>clear</u>	Clear content (public member function)
<u>swap</u>	Swap content (public member function)
ıckets	
oucket_count	Return number of buckets (public member function)
max_bucket_count	Return maximum number of buckets (public member function)
oucket_size	Return bucket size (public member type)
<u>oucket</u>	Locate element's bucket (public member function)
ah nalian	

Hash policy		
	load_factor	Return load factor (public member function)
	max_load_factor	Get or set maximum load factor (public member function)
	<u>rehash</u>	Set number of buckets (public member function)
	<u>reserve</u>	Request a capacity change (public member function)

•	nservers		
	hash_function	Get hash function (public member type)	
	key_eq	Get key equivalence predicate (public member type)	
-	get_allocator	Get allocator (public member function)	
e			

#### ♠ Non-member function overloads

	operators (unordered_map)	Relational operators for unordered_map (function template)
	swap (unordered_map)	Exchanges contents of two unordered_map containers (function temp

The End