

MAT 3007 Optimization: Tutorial 5

Simplex Tableau

Guxin Du

The Chinese University of Hong Kong, Shenzhen

June 19, 2025

Exercise 1

Use the simplex tableau method to solve the following problem

$$\begin{array}{ll} \max & 3x_1 + 4x_2 \\ \text{s.t.} & x_1 + x_2 \leq 4 \\ & 2x_1 + x_2 \leq 5 \\ & x \geq 0 \end{array} \quad (1)$$

Exercise 2: Two-phased Method

Use the two-phase simplex method to completely solve the linear optimization problem:

$$\begin{array}{ll}
 \min & 2x_1 + 3x_2 + 3x_3 + x_4 - 2x_5 \\
 \text{s.t.} & x_1 + 3x_2 + \quad + 4x_4 + x_5 = 2 \\
 & x_1 + 2x_2 + \quad - 3x_4 + x_5 = 2 \\
 & x_1 + 4x_2 - 3x_3 + \quad + \quad = -1 \\
 & x \geq 0
 \end{array}$$

Exercise 3: Big-M Method

Use the big-M simplex method to completely solve the linear optimization problem:

$$\begin{array}{ll}\min & 4x_1 + x_2 + x_3 \\ \text{s.t.} & 2x_1 + x_2 + 2x_3 = 4 \\ & 3x_1 + 3x_2 + x_3 = 3 \\ & x \geq 0\end{array}$$

Acknowledgements

Acknowledgements: Thank Prof. Zizhuo WANG, Wentao Ding and Yicheng Liu for the original code and content of this tutorial.