

Q → Given an array with daily profit/loss from a particular stock. Calculate the total profit/loss over a given range of days.

The function should be able to handle multiple queries for different ranges.

$A = [-5, 10, 20, 40, 50, -10, 8]$

Queries

start      End

1      4      → 120

2      5      → 100

0      0      → -5

Given an integer array with N elements & Q queries, for every find sum of elements from index L to R.

$A = [-5, 10, 20, 40, 50, -10, 8]$

Queries

L      R

1      4      → 120

2      5      → 100

0      0      → -5

Range Sum Queries

Bruteforce → V Queries, iterate from index L to R.

TC =  $O(N * Q)$

SC =  $O(1)$

for  $i \rightarrow 0$  to  $(Q-1)$  {  
    // L, R

    for  $i \rightarrow L$  to  $R$  {

## Cricket

}  
sum += A[i]  
}

Over → 0 1 2 3 4 5 6 7 8 9 10  
Score → 2 8 14 29 31 49 65 79 88 97

Runs scored in 7<sup>th</sup> over →  $65 - 49 = 16$

Runs scored from 6<sup>th</sup> to 10<sup>th</sup> over →  $97 - 31 = 66$

Runs scored in 10<sup>th</sup> over →  $97 - 88 = 9$

Runs scored from 3<sup>rd</sup> to 6<sup>th</sup> over →  $49 - 8 = 41$

Runs scored from 4<sup>th</sup> to 9<sup>th</sup> over →  $88 - 14 = 74$

Prefix Sum →  $P[i] = A[0] + A[1] + \dots + A[i]$

$$P[2] = A[0] + A[1] + A[2]$$

$$P[3] = A[0] + A[1] + A[2] + A[3]$$
$$= P[2] + A[3]$$

$$P[i] = P[i-1] + A[i]$$

$$P[0] = A[0]$$

$$P[0] = A[0]$$

for  $i \rightarrow 1$  to  $(N-1)$  {

$$P[i] = P[i-1] + A[i]$$

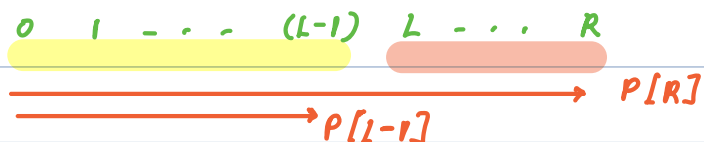
}

$$TC = O(N)$$

A = [10 32 6 12 20 1]  
✓ P → [10 42 48 60 80 81]

sum (L to R)

$$P[R] - P[L-1]$$



sum (0 — 3)  $\rightarrow$   $P[3] - P[0-1]$

index out of bound error

for  $i \rightarrow 0$  to  $(Q-1)$  {

    // L, R

    if ( $L == 0$ ) print ( $P[R]$ )

    else print ( $P[R] - P[L-1]$ )

}

$TC = O(Q)$

$TC = O(N + Q)$

$SC = O(N)$

$O(1)$   $\rightarrow$  Use  $A[]$  to store prefix sum.

~~$A[0] = A[0]$~~

for  $i \rightarrow 1$  to  $(N-1)$  {

$A[i] = A[i-1] + A[i]$

}

$A = [ \overset{0}{10} \quad \overset{1}{\cancel{32}} \quad \overset{2}{\cancel{6}} \quad \overset{3}{\cancel{12}} \quad \overset{4}{\cancel{20}} \quad \overset{5}{\cancel{1}} ]$   
          42    48    60    80    81

$A[i] = P[i] - P[i-1]$

$Q \rightarrow$  Given an integer array &  $Q$  queries ( $L, R$ )  
Find the sum of all even indexed elements.

$A = [ \overset{0}{2} \quad \overset{1}{3} \quad \overset{2}{1} \quad \overset{3}{6} \quad \overset{4}{4} \quad \overset{5}{5} ]$

Queries

1    3     $\rightarrow$  1

2    5     $\rightarrow$  5

3    3     $\rightarrow$  0

Brute force  $\rightarrow TC = O(N * Q)$

$SC = O(1)$

$$P[i] \rightarrow A[0] + A[2] + A[4] \dots$$

	0	1	2	3	4	5		0	1	2	3	4		
A =	[	2	3	1	6	4	5]	A =	[	2	4	3	1	5]
P →	2	2	3	3	7	7	P →	2	2	5	5	10		

$$P[0] = A[0]$$

```

for i → 1 to (N-1) {
    if (i % 2 == 0)    P[i] = P[i-1] + A[i]
    else                P[i] = P[i-1]
}

```

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for i → 0 to (Q-1) { // Queries → L = query[i][0]
    // L, R                R = query[i][1]
    if (L == 0)    print (P[R])
    else    print (P[R] - P[L-1])
}

```

$$TC = \underline{O(N+Q)} \quad SC = \underline{O(N)} \rightarrow \underline{O(1)}$$

Find the sum of all **odd indexed** elements.

```

P[0] = 0
for i → 1 to (N-1) {
    if (i % 2 == 1)    P[i] = P[i-1] + A[i]
    else                P[i] = P[i-1]
}

```

Q → Given an integer array, count the no. of special index i.e. index after removing which sum of all even indexed elements = sum of all odd indexed elements.

<u>i</u>	A = [	<sup>0</sup> 3	<sup>1</sup> 2	<sup>2</sup> 7	<sup>3</sup> 6	<sup>4</sup> -2]	<u>Seven</u>	<u>Sodd</u>
0	→	2	7	6	-2		8	≠ 5
1	→	3	7	6	-2		9	≠ 5
2	→	3	2	6	-2		9	≠ 0
3	→	3	2	7	-2		10	≠ 0
4	→	3	2	7	6		10	≠ 8

Ans = 0

A = [ <sup>0</sup>4 <sup>1</sup>1 <sup>2</sup>~~3~~ <sup>3</sup>7 <sup>4</sup>10 ]

7 10 odd sum = 1 + 10 = 11

A = [ <sup>0</sup>2 <sup>1</sup>3 <sup>2</sup>1 <sup>3</sup>~~4~~ <sup>4</sup>0 <sup>5</sup>-1 <sup>6</sup>2 <sup>7</sup>-2 <sup>8</sup>10 <sup>9</sup>8 ]

0 -1 2 -2 10 8

odd sum = 3 + 0 + 2 + 10 = 15

∀ elements > i<sup>th</sup> index → odd index move to even  
even index move to odd

A = [ <sup>0</sup>2 <sup>1</sup>3 <sup>2</sup>1 <sup>3</sup>~~4~~ <sup>4</sup>0 <sup>5</sup>-1 <sup>6</sup>2 <sup>7</sup>-2 <sup>8</sup>10 <sup>9</sup>8 ]

0 -1 2 -2 10 8

even sum = 2 + 1 + (-1) + (-2) + 8 = 8

check i<sup>th</sup> index

Seven = S<sub>even</sub> (0 — i-1) + S<sub>odd</sub> (i+1 — N-1)

Sodd = S<sub>odd</sub> (0 — i-1) + S<sub>even</sub> (i+1 — N-1)

$$\text{Sum}_{\text{even}} = \text{evenP}[i-1] + (\text{oddP}[N-1] - \text{oddP}[i])$$

$$\text{Sum}_{\text{odd}} = \text{oddP}[i-1] + (\text{evenP}[N-1] - \text{evenP}[i])$$

// calculate oddP[] & evenP[]

cnt = 0

for  $i \rightarrow 0$  to  $(N-1)$  {

    if ( $i == 0$ ) {

$se = \text{oddP}[N-1] - \text{oddP}[i]$

$so = \text{evenP}[N-1] - \text{evenP}[i]$

    } else {

$se = \text{evenP}[i-1] + (\text{oddP}[N-1] - \text{oddP}[i])$

$so = \text{oddP}[i-1] + (\text{evenP}[N-1] - \text{evenP}[i])$

    }

    if ( $se == so$ ) cnt++

}

return cnt

$TC = \underline{O(N)}$

$SC = \underline{O(N)}$

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