

Arrays LL Stacks Queues - linear

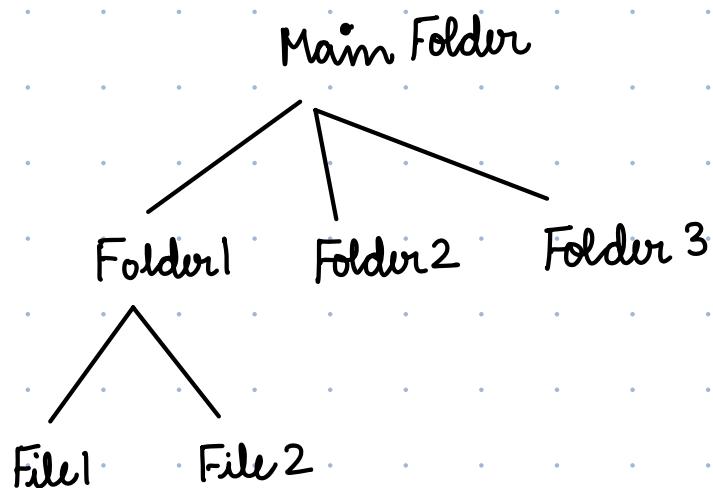
Trees

- Non Linear

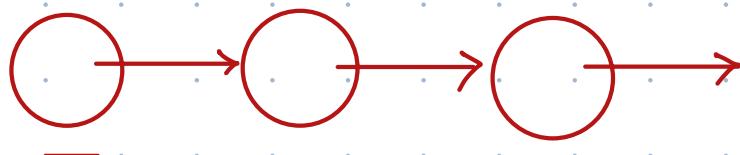
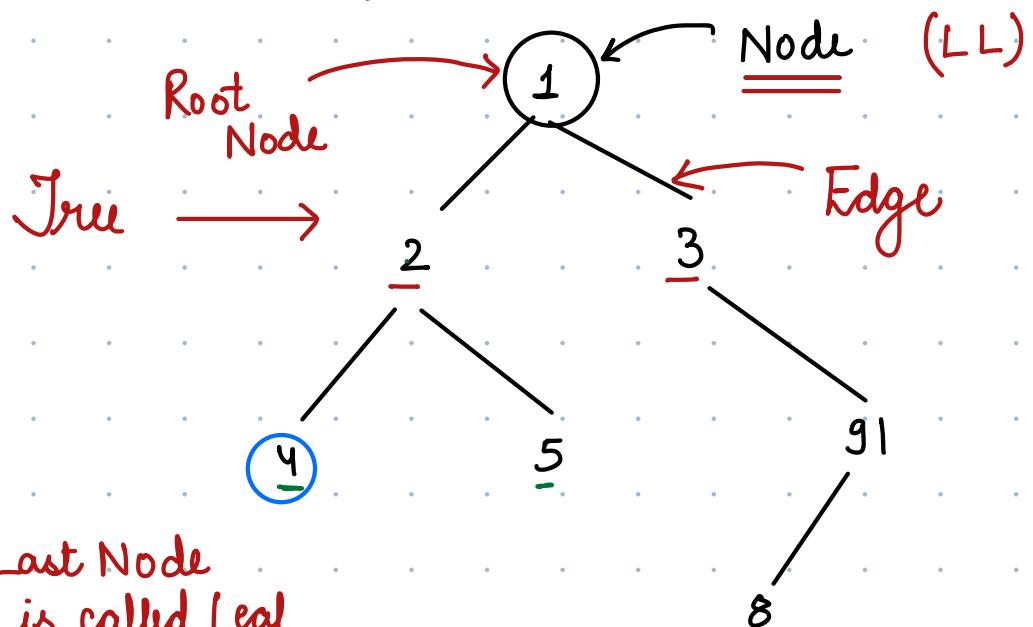


Family tree
Company hierarchy

File System



Hierarchy with the help of Number



Subarray of an array
substring of a string
subtree of a tree

— part of tree with some nodes

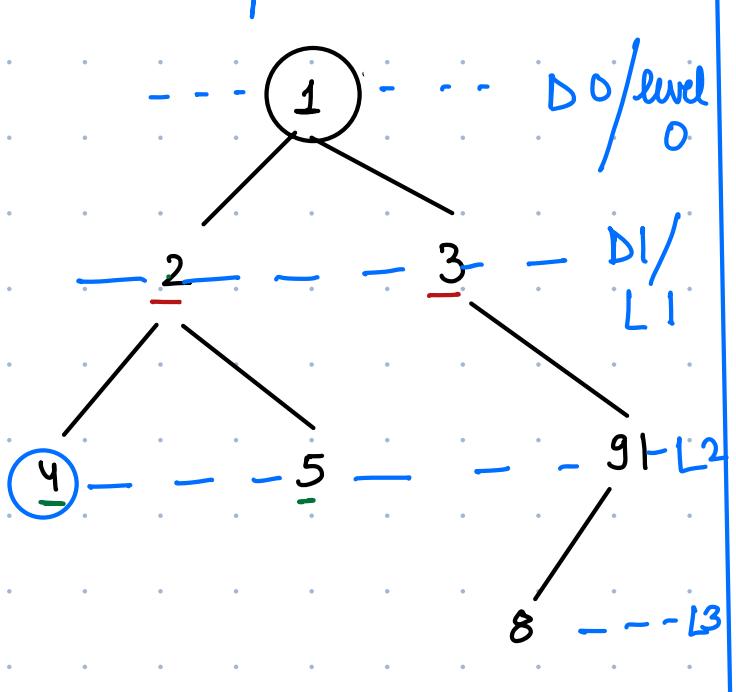
If 2 nodes have same parent, they are called siblings

2 & 3.

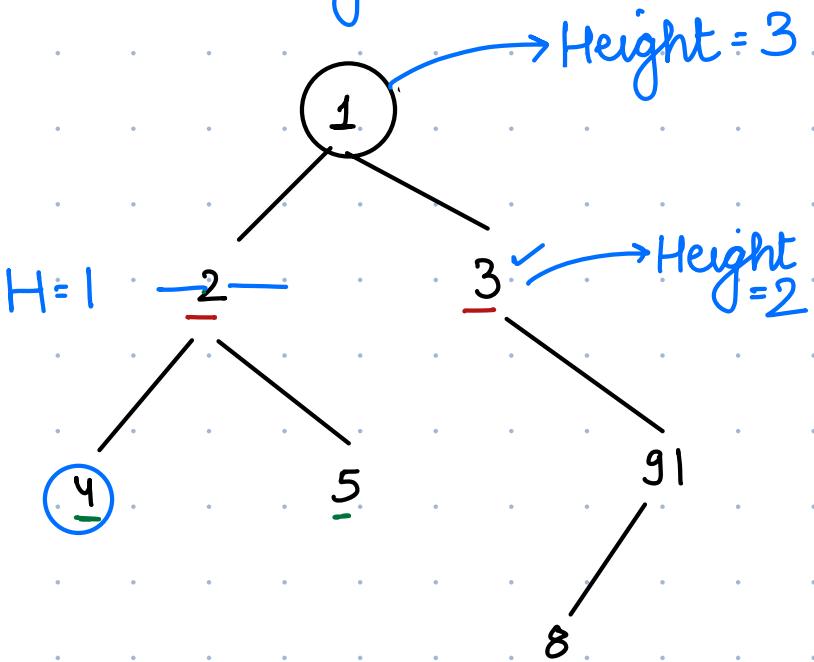
Anccestor — Root to Node path — All nodes inside it.

Descendant — Node to leaf part — All nodes inside it.

Depth



height



Depth is measured from root node

Height is measured from leaf node.

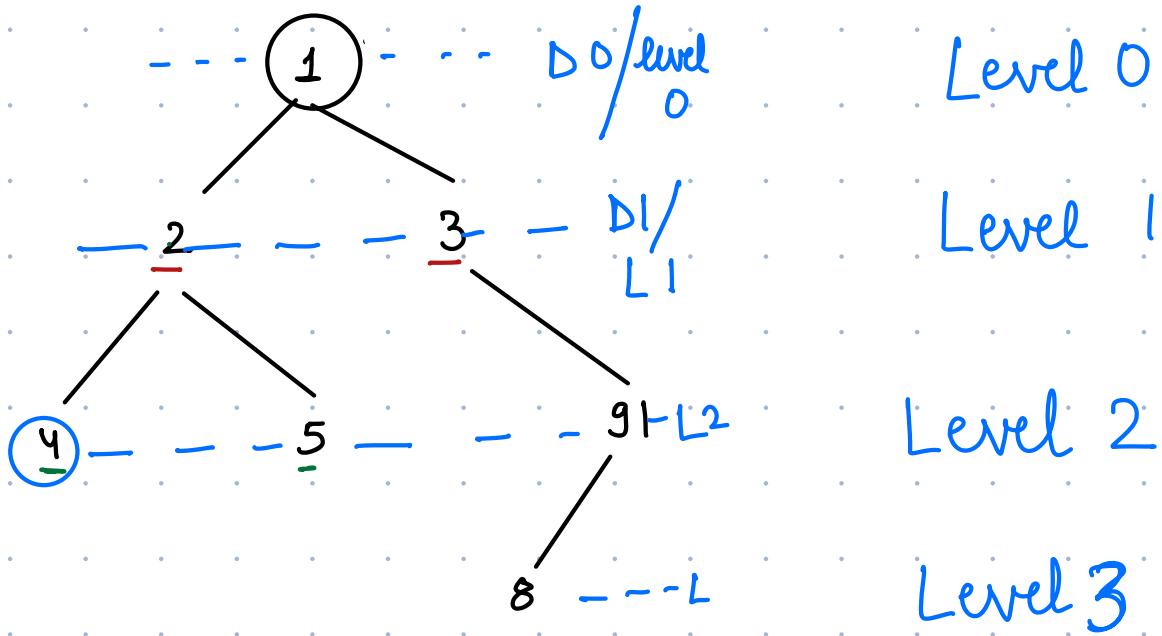
→ Can leaf Node be a subtree?

Yes

→ Do all nodes have a parent node?

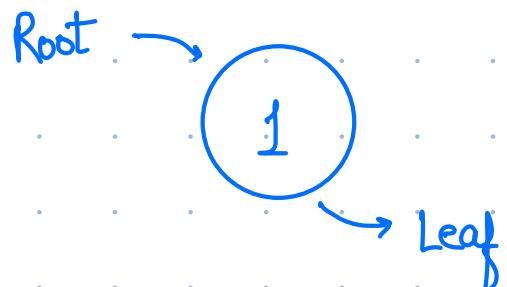
No → Root node

- Depth = Level



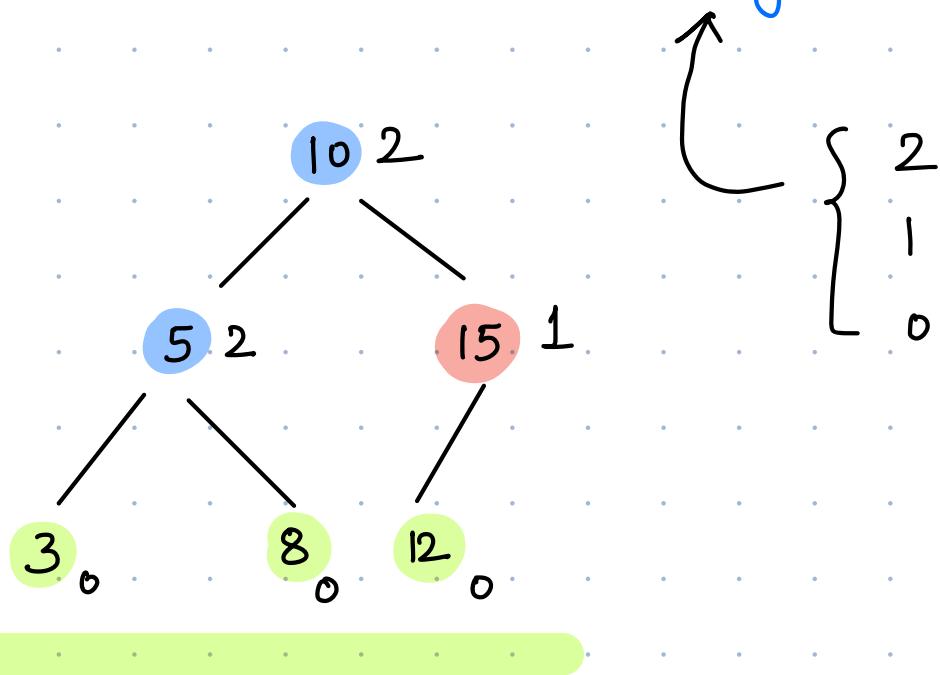
- Q. • Height = Leaf
- ↳ Height of leaf node = 0

Can 1 node be a tree



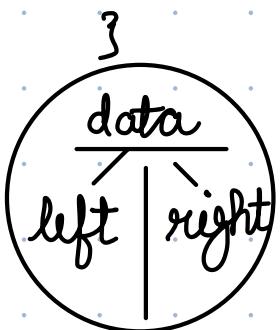
Yes!

max. 2 children ← Binary Tree



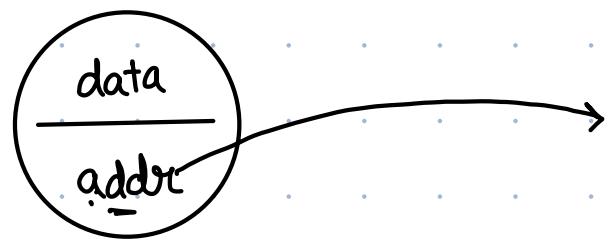
make node of a binary tree

```
class Node {  
    int data  
    Node left  
    Node right
```



node of a LL

```
class Node  
int data  
Node next
```



Binary base 2 {0 1}

Decimal base 10 {0 - 9}

Octal base 8 {0 - 7}

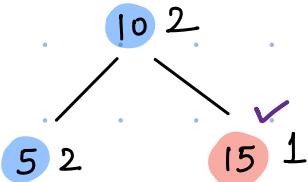
Hexadecimal base 16 {0 - 9,
A,B,C,D,E,F}

Example addresses —

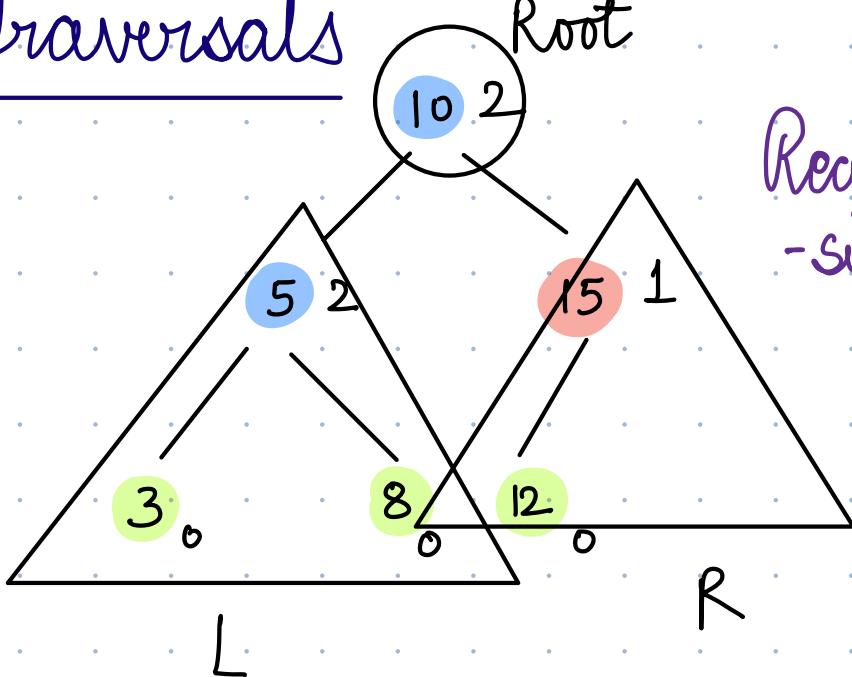
E948
A41

12E
549
90A

root = E948



Traversals



Recursive {

- PreOrder ✓
- PostOrder ✓
- InOrder ✓
- InOrder Iterative

<u>L</u>	Root	<u>R</u>
Sub - tree		Sub - tree

Left Root Right = InOrder

Root Left Right = Pre Order

Left Right Root = Post Order

PreOrder Traversal

void inOrder(Node root) {

 inOrder(root.left)

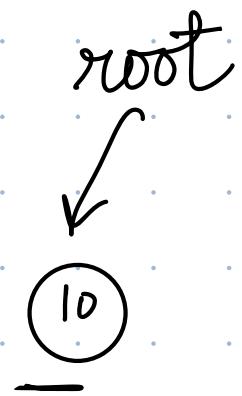
 print(root.data);

 inOrder(root.right)

}

P

= Print nodes of tree rooted at root



SPI = Print nodes of tree rooted at root.left



Print (root.data)



SP2 = Print nodes of tree rooted at root.right

IN ORDER

P = Print nodes of tree rooted at 10

SP1 = Print nodes of tree rooted at 5

SP2 = Print nodes of tree rooted at 15

Print (root.data)

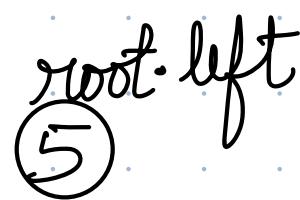
Post ORDER

P = Print nodes of tree rooted at 10



Print (root.data)

SPI = Print nodes of tree rooted at 5

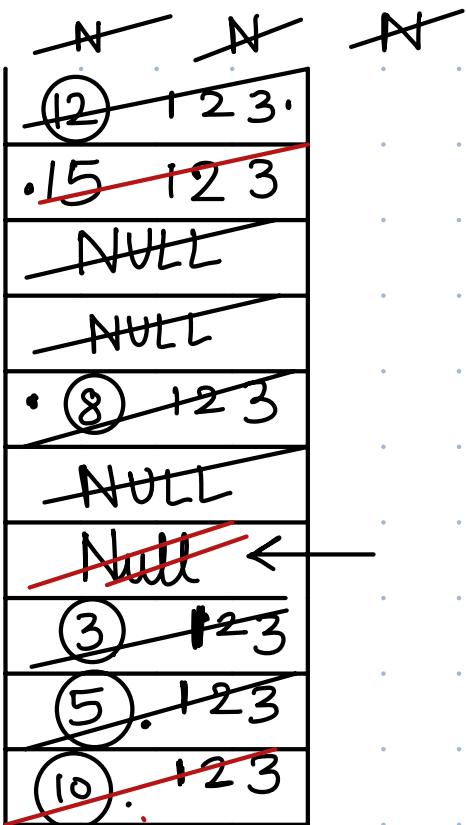


SP2 = Print nodes of tree rooted at 15



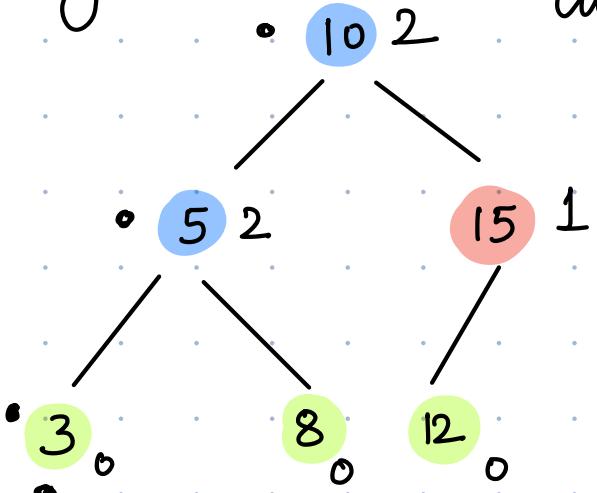
PRE ORDER

```
void inOrder(Node root)  
{  
    if (root == null) { return; }  
    inOrder(root.left);  
    print (root.data);  
    inOrder(root.right);  
}
```



Dry Run

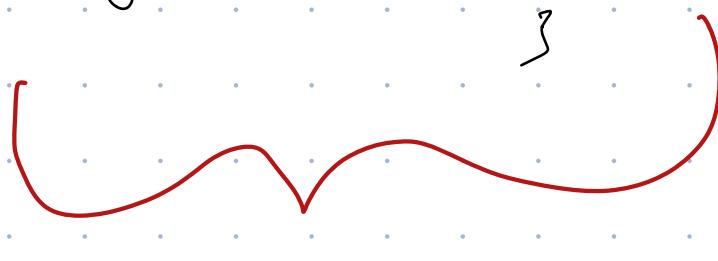
→ Base Case



3 5 8 10 12 15

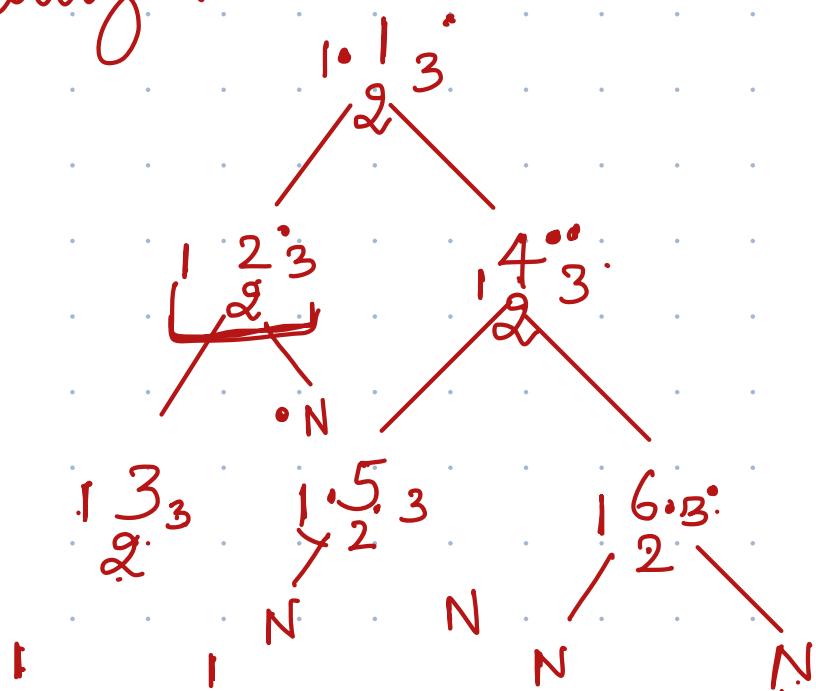
```
void preOrder(Node root)  
if (root == null) { return; }  
print (root.data);  
preOrder(root.left);  
preOrder(root.right)
```

```
void postOrder(Node root)  
if (root == null) { return; }  
postOrder(root.left);  
postOrder(root.right);  
print (root.data);
```



Dry Run = Exercise

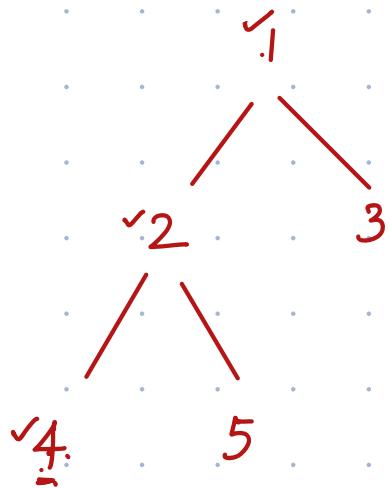
Quiz:



Inorder

3 2 1 5 4 6

Iterative InOrder :



4
2
5
1
3

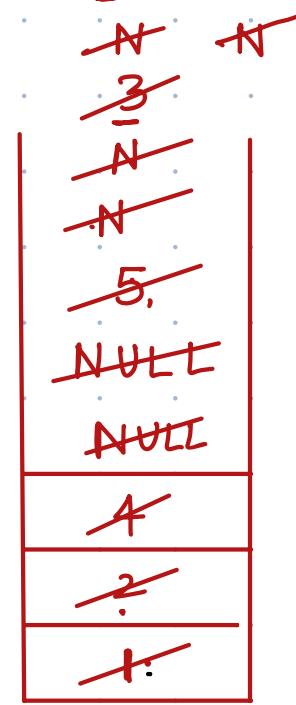
Push Element →

Push its left

Pop Element, Print element

→ Push its right

Start with !



curr = root

while ($\text{curr} \neq \text{NULL}$ || st.isEmpty() == false) {

if ($\text{curr} \neq \text{NULL}$) {

st.push(curr)

curr = curr.left

} else {

curr = st.pop()

print (curr.data)

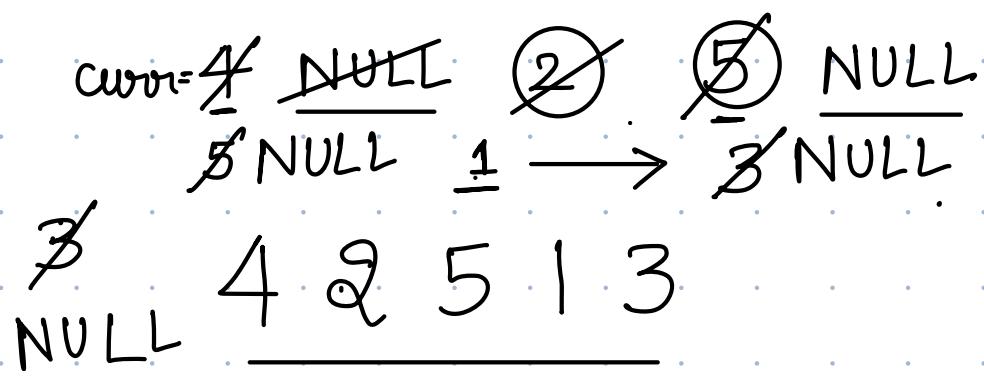
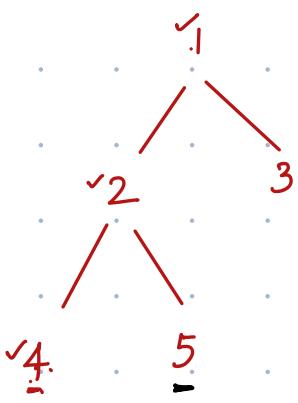
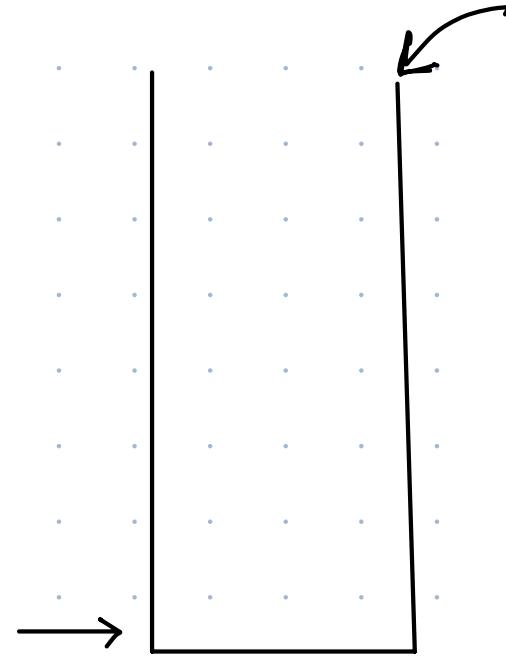
curr = curr.right

}

}

Dry Run :

```
curr = root ✓  
while (curr!=NULL || st.isEmpty() == false){  
    if (curr!=NULL) {  
        st.push(curr)  
        curr = curr.left  
    } else {  
        curr = st.pop()  
        print (curr.data)  
        curr = curr.right  
    }  
}
```



Equal Tree Partition

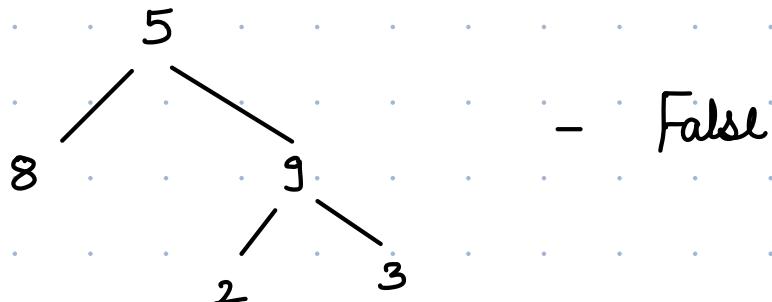
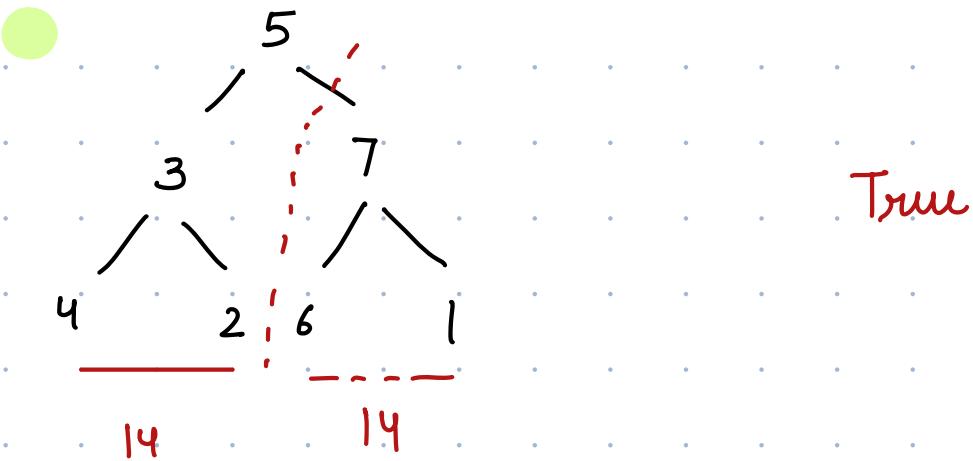
Recursion

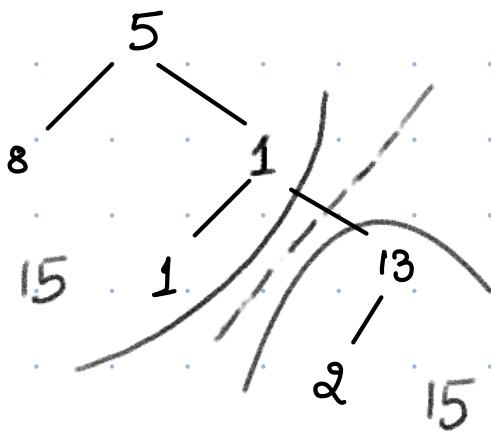
Given

Root of binary tree

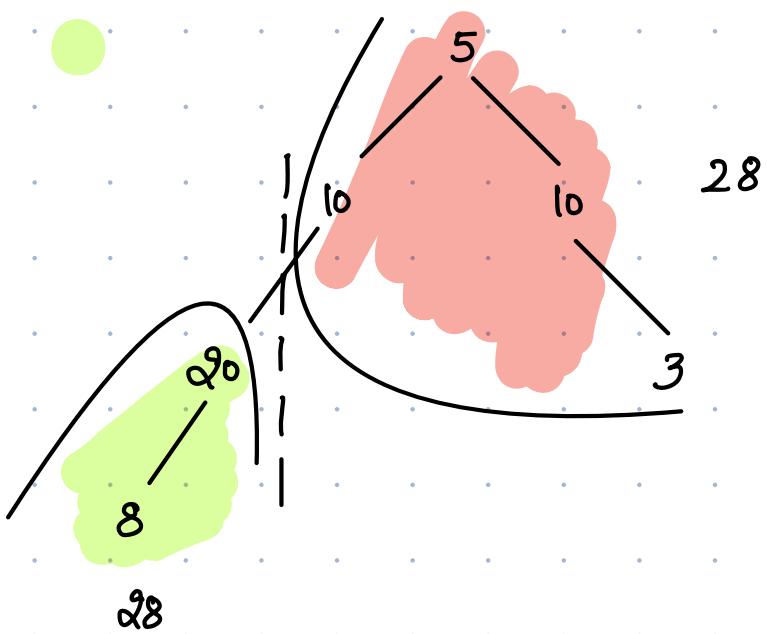
Return true if the tree can be split into 2 non-empty subtrees of equal sums

Otherwise return false.





True



Yes

```

function sum ( Node root )
if (root == null) { return 0; }

int s1 = sum( root.left );
int s2 = sum( root.right );
return s1 + s2 + root.data;
  
```

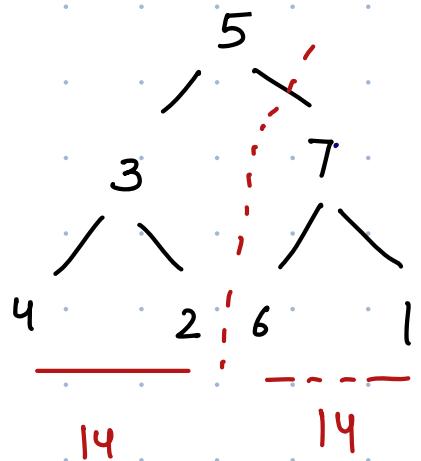
}

boolean
function \rightarrow hasSubtreeWith HalfSum (Node root,
int totalSum){
if (root == null) { return false; }
base case $SL = \text{sum}(\text{root.left})$
for Odd if ($SL == \text{totalSum}/2$) { return true; }

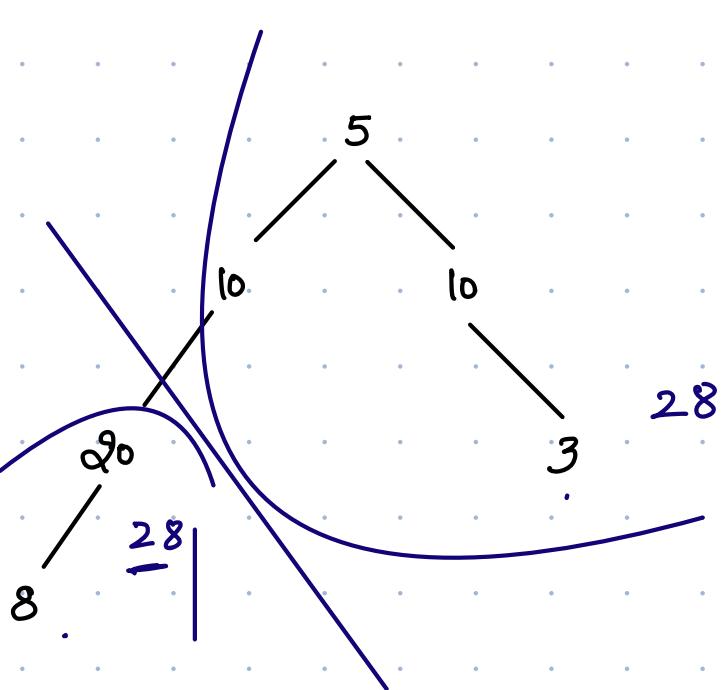
$SR = \text{sum}(\text{root.right})$
if ($SR == \text{totalSum}/2$) { return true; }

ans = hasSubtreeWith HalfSum (root.left, totalSum)
if (ans == true) { return true; }

ans = hasSubtreeWith HalfSum (root.right, totalSum)
if (ans == true) { return true; }
return false;



$$\begin{aligned}
 (3) &= 9 \\
 (7) &= \frac{14}{\text{RS}} = \frac{28}{2}
 \end{aligned}$$



$$\begin{aligned}
 \underline{(5)} & \\
 (10) &= 38 \times \\
 (10) &= 13 \times \\
 (20) &= \underline{28} \text{ true}
 \end{aligned}
 \quad TS = 56$$

