ESC201: Lecture 8

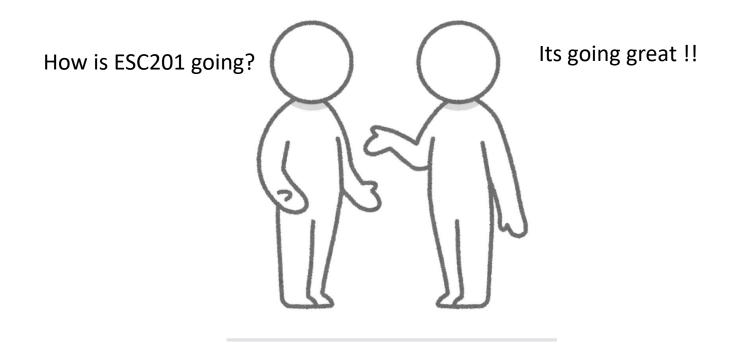


Dr. Imon Mondal

ASSISTANT PROFESSOR, ELECTRICAL ENGINEERING, IIT KANPUR

2024-25 SEM-I | ESC201 INTRODUCTION TO ELECTRONICS

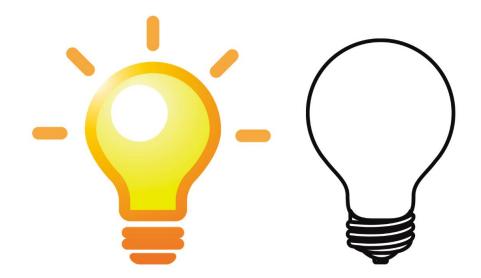
Conversation



After a few days



Storage



Every number system is associated with a base or radix

A positional notation is commonly used to express numbers

$$(a_5 a_4 a_3 a_2 a_1 a_0)_r = a_5 r^5 + a_4 r^4 + a_3 r^3 + a_2 r^2 + a_1 r^1 + a_0 r^0$$

The decimal system has a base of 10 and uses symbols (0,1,2,3,4,5,6,7,8,9) to represent numbers

$$(2009)_{10} = 2 \times 10^3 + 0 \times 10^2 + 0 \times 10^1 + 9 \times 10^0$$

$$(123.24)_{10} = 1 \times 10^2 + 2 \times 10^1 + 3 \times 10^0 + 2 \times 10^{-1} + 4 \times 10^{-2}$$

An octal number system has a base 8 and uses symbols (0,1,2,3,4,5,6,7)

$$(2007)_8 = 2 \times 8^3 + 0 \times 8^2 + 0 \times 8^1 + 7 \times 8^0$$

What decimal number does it represent?

$$(2007)_8 = 2 \times 512 + 0 \times 64 + 0 \times 8^1 + 7 \times 8^0 = 1033$$

A hexadecimal system has a base of 16

Number	Symbol
0	0
1	1
2	2
3	3
4	4
5	5
6	6
7	7
8	8
9	9
10	А
11	В
12	С
13	D
14	E
15	F

$$(2BC9)_{10} = 2 \times 16^3 + B \times 16^2 + C \times 16^1 + 9 \times 16^0$$

How do we convert it into decimal number?

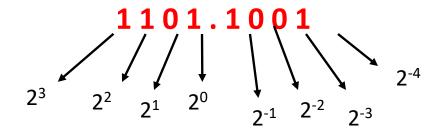
$$(2BC9)_{10} = 2 \times 4096 + 11 \times 256 + 12 \times 16^{1} + 9 \times 16^{0} = 11209$$

A Binary system has a base 2 and uses only two symbols 0, 1 to represent all the numbers

$$(1101)_2 = 1 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0$$

Which decimal number does this correspond to?

$$(1101)_2 = 1 \times 8 + 1 \times 4 + 0 \times 2^1 + 1 \times 2^0 = 13$$



2 ⁰	1	
2 ¹	2	
2 ²	4	
2 ³	8	
24	16	
2 ⁵	32	
2 ⁶	64	
27	128	
2 ⁸	256	
2 ⁹	512	
<mark>2¹⁰</mark>	1024(K)	
<mark>2²⁰</mark>	1048576(M)	

2-1	2-2	2-3	2-4	2 ⁻⁵	2 ⁻⁶
0.5	0.25	0.125	0.0625	0.03125	0.015625

Developing Fluency with Binary Numbers

Convert 45 to binary number

$$(45)_{10} = b_n b_{n-1} \dots b_0$$

$$45 = b_n 2^n + b_{n-1} 2^{n-1} \dots b_1 2^1 + b_0$$

Divide both sides by 2

$$\frac{45}{2} = 22.5 = b_n 2^{n-1} + b_{n-1} 2^{n-2} \dots b_1 2^0 + b_0 \times 0.5$$

$$22 + 0.5 = b_n 2^{n-1} + b_{n-1} 2^{n-2} \dots + b_1 2^0 + b_0 \times 0.5$$

$$\Rightarrow b_0 = 1$$

$$22 + 0.5 = b_n 2^{n-1} + b_{n-1} 2^{n-2} + \cdots + b_1 2^0 + b_0 \times 0.5$$
 $\Rightarrow b_0 = 1$

$$22 = b_n 2^{n-1} + b_{n-1} 2^{n-2} \dots b_2 2^1 + b_1 2^0$$

Divide both sides by 2

$$\frac{22}{2} = 11 = b_n 2^{n-2} + b_{n-1} 2^{n-3} \dots b_2 2^0 + b_1 \times 0.5 \implies b_1 = 0$$

$$11 = b_n 2^{n-2} + b_{n-1} 2^{n-3} \dots + b_3 2^1 + b_2 2^0$$

$$5.5 = b_n 2^{n-3} + b_{n-1} 2^{n-4} + b_3 2^0 + 0.5b_2 \implies b_2 = 1$$

$$5 = b_n 2^{n-3} + b_{n-1} 2^{n-4} \dots b_4 2^1 + b_3 2^0$$

$$5 = b_n 2^{n-3} + b_{n-1} 2^{n-4} \dots b_4 2^1 + b_3 2^0$$

$$2.5 = b_n 2^{n-4} + b_{n-1} 2^{n-5} \dots b_4 2^0 + 0.5b_3 \implies b_3 = 1$$

$$2 = b_n 2^{n-4} + b_{n-1} 2^{n-5} \dots b_5 2^1 + b_4 2^0$$

$$1 = b_n 2^{n-5} + b_{n-1} 2^{n-6} \dots b_5 2^0 + 0.5b_4 \implies b_4 = 0$$

$$\implies b_5 = 1$$

$$(45)_{10} = b_5 b_4 b_3 b_2 b_1 b_0 = 101101$$

Method of successive division by 2

45	remainder	
22	1	
11	0	
5	1	
2	1	45 = 101101
1	0	
0	1	

Convert (153)₁₀ to octal number system

$$(153)_{10} = (b_n b_{n-1} \dots b_0)_8$$

$$(153)_{10} = b_n 8^n + b_{n-1} 8^{n-1} \dots b_1 8^1 + b_0$$

Divide both sides by 8

$$\frac{153}{8} = 19.125 = b_n 8^{n-1} + b_{n-1} 8^{n-2} \dots b_1 8^0 + \frac{b_0}{8} \implies \frac{b_0}{8} = 0.125 \implies b_0 = 1$$

153	remainder			
19	1	-		
2	3			(004)
0	2	153	=	(231) ₈

Convert $(0.35)_{10}$ to binary number

$$(0.35)_{10} = 0.b_{-1}b_{-2}b_{-3}.....b_{-n}$$

$$0.35 = 0 + b_{-1}2^{-1} + b_{-2}2^{-2} + \dots b_{-n}2^{-n}$$

How do we find the b_{-1} b_{-2} ... coefficients?

Multiply both sides by 2

$$0.7 = b_{-1} + b_{-2} 2^{-1} + \dots b_{-n} 2^{-n+1} \implies b_{-1} = 0$$

$$0.7 = b_{-2}2^{-1} + b_{-3}2^{-2} + \dots b_{-n}2^{-n+1}$$

$$0.7 = b_{-2}2^{-1} + b_{-3}2^{-2} + \dots b_{-n}2^{-n+1}$$

Multiply both sides by 2

$$1.4 = b_{-2} + b_{-3}2^{-1} + \dots b_{-n}2^{-n+2}$$

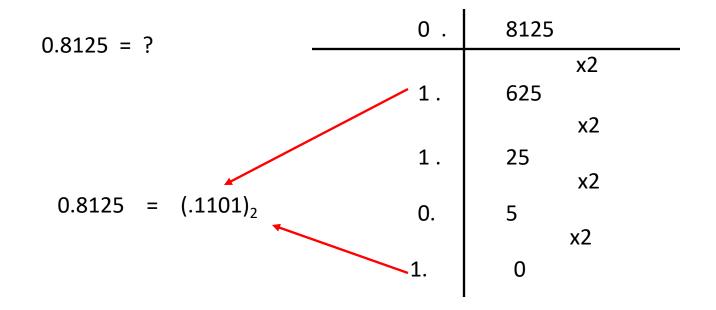
Note that ½+1/4+1/8+.....≤1

$$\Rightarrow b_{-2} = 1$$

$$0.4 = b_{-3}2^{-1} + b_{-4}2^{-2} \dots b_{-n}2^{-n+2}$$

$$0.8 = b_{-3} + b_{-4} 2^{-1} \dots b_{-n} 2^{-n+3} \implies b_{-3} = 0$$

	0.	125	
			x2
	0 .	25	
			x2
_	0.	5	
$0.125 = (.001)_{2}$			x2
(.001)	1.	0	



Binary numbers

Most significant bit or MSB

1011000111

decimal	2bit	3bit	4bit	5bit
0	00	000	0000	00000
1	01	001	0001	00001
2	10	010	0010	00010
3	11	011	0011	00011
4		100	0100	00100
5		101	0101	00101
6		110	0110	00110
7		111	0111	00111
8			1000	01000
9			1001	01001
10			1010	01010
11			1011	01011
12			1100	01100
13			1101	01101
14			1110	01110
15			1111	01111

Least significant bit or LSB

This is a 10 bit number

Binary digit = bit



N-bit binary number can represent numbers from 0 to 2^N -1

Converting Binary to Hex and Hex to Binary

$$(b_{7}b_{6}b_{5}b_{4}b_{3}b_{2}b_{1}b_{0})_{b} = (h_{1}, h_{0})_{Hex}$$

$$b_{7}2^{7} + b_{6}2^{6} + b_{5}2^{5} + b_{4}2^{4} + b_{3}2^{3} + b_{2}2^{2}b_{1}2^{1} + b_{0} = h_{1}16^{1} + h_{0}$$

$$(b_{7}2^{3} + b_{6}2^{2} + b_{5}2^{1} + b_{4})2^{4} + (b_{3}2^{3} + b_{2}2^{2}b_{1}2^{1} + b_{0}) = h_{1}16^{1} + h_{0}$$

$$h_{1} \qquad h_{0}$$

$$(10110011)_{b} = (1011)(0011) = (B3)_{Hex}$$

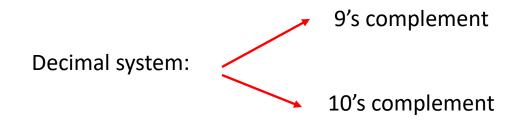
$$(110011)_{b} = (11)(0011) = (33)_{Hex}$$

 $(EC)_{Hox} = (1110)(1100) = (11101100)_{h}$

	Number	Symbol
	0(0000)	0
	1(0001)	1
	2(0010)	2
	3(0011)	3
	4(0100)	4
	5(0101)	5
	6(0110)	6
0	7(0111)	7
	8(1000)	8
	9(1001)	9
	10(1010)	А
	11(1011)	В
	12(1100)	С
	13(1101)	D
	14(1110)	E
	15(1111)	F
_		

Binary Addition/Subtraction

Complement of a number



9's complement of n-digit number x is 10ⁿ -1 -x

10's complement of n-digit number x is 10ⁿ -x

9's complement of 85?

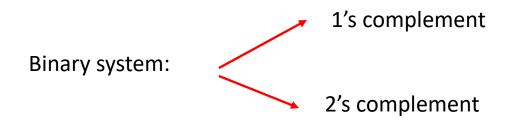
$$10^2 - 1 - 85$$

$$99 - 85 = 14$$

9's complement of 123 = 999 - 123 = 876

10's complement of 123 = 9's complement of 123+1=877

Complement of a binary number



1's complement of n-bit number x is $2^n - 1 - x$

2's complement of n-bit number x is 2^n -x

$$2^4 - 1 - 1011$$

$$1111 - 1011 = 0100$$

1's complement is simply obtained by flipping a bit (changing 1 to 0 and 0 to 1)

1's complement of
$$1001101 = ?$$