

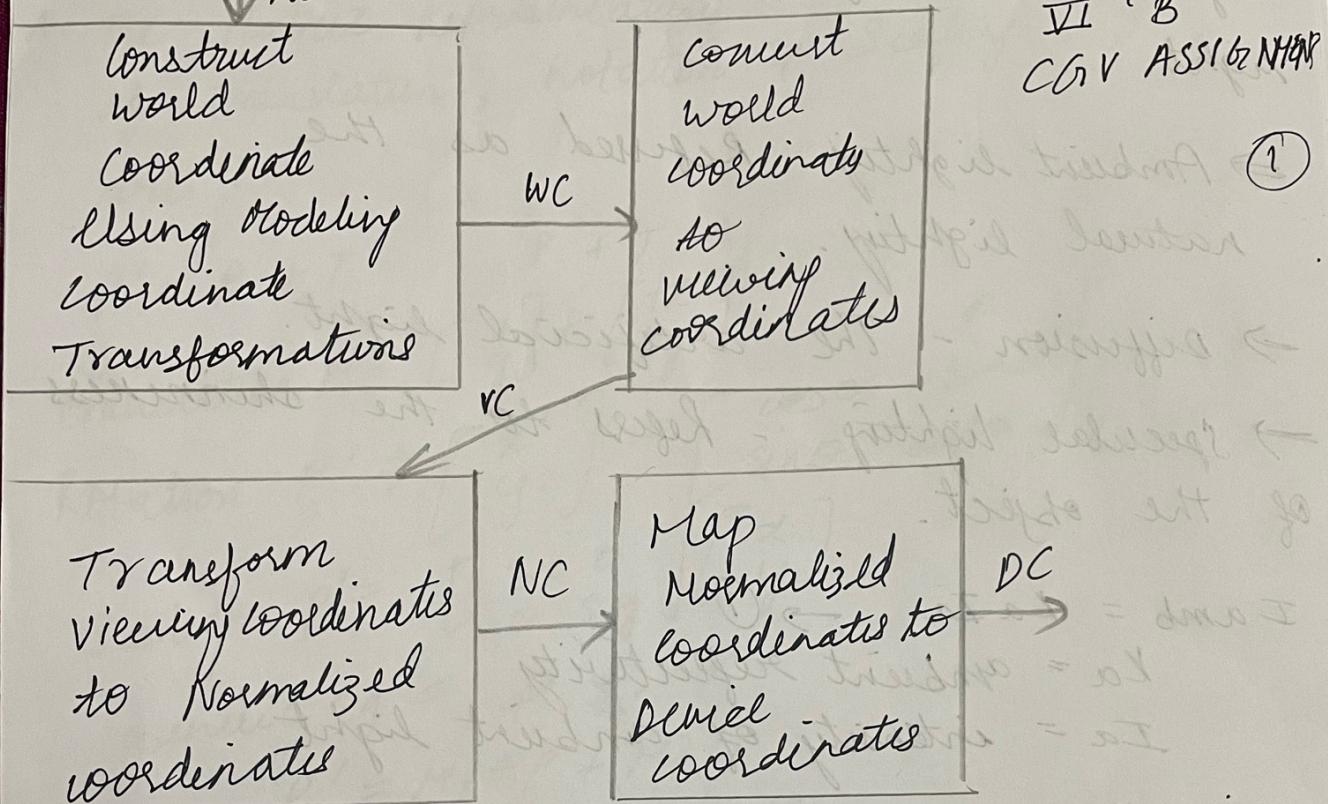
# ① 2D Pipeline

KRISHA · M

KRISHA · H

IBY20CS089

VI 'B'  
CIV ASSIGNMENT



- We could set up a separate 2-d, viewing coordinate reference frame for specifying clipping window.
- Systems use normalized coordinates in the range from 0 to 1, others used a normalized range from -1 to 1.
- Clipping is usually performed in the normalized coordinates.

② Build Phong lighting Model with Equations  
light consists of 3 different types of light.

- y → Ambient lighting - Refers as the natural lighting.
- Diffusion - The artificial light.
- Specular lighting - Refers to the shininess of the object.

$$I_{amb} = k_a I_a \rightarrow ①$$

$k_a$  = ambient reflectivity

$I_a$  = intensity of ambient light

Similarly

$$I_{diff} = k_d I_p \cos(\theta) \rightarrow ②$$

$$= k_d I_p (N.L)$$

$$I_{spec} = k_s I_l \cos^n \phi$$

∴ The Phong model gives us the equation of all combined

∴ Total intensity  $I = k_a I_a + k_d I_p \cos \theta + k_s I_l \cos^n \phi$

Apply homogeneous coordinates for translation, rotation and scaling via matrix representation. (2)

A. The Matrix Representations of Translation, Rotation & Scaling are

$$P' = P + T \quad \begin{bmatrix} P \\ 1 \end{bmatrix} + \begin{bmatrix} tx \\ ty \end{bmatrix}$$

$$\text{Translation } P' = \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} + \begin{bmatrix} tx \\ ty \\ 1 \end{bmatrix}$$

$$\text{Rotation } P' = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

$$\text{Scaling } P' = \begin{bmatrix} sx & 0 \\ 0 & sy \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

$$\text{generic eq} = P \cdot S \cdot R \cdot P'$$

$$P' = M_1 \cdot P + M_2$$

$$\text{But } x = \frac{xh}{n}, y = \frac{yh}{n}$$

$$h=1 \therefore \text{consider } (h+x, h+y, 1)$$

$$\text{Translation } \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & tx \\ 0 & 1 & ty \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

$$\text{Rotation } \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} sx & 0 & 0 \\ 0 & sy & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

$$\text{Scaling } \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} \cos\theta & -\sin\theta & 0 \\ \sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

(7.) Differences between Raster and Random scan displays.

Raster Scan	Random Scan
<ul style="list-style-type: none"><li>• Produces jagged lines that are plotted as a discrete point sets.</li><li>• less expensive</li><li>• modification difficult</li><li>• Resolution low</li><li>• solid pattern is easy to fill.</li></ul>	<p>Random system produces smooth lines drawing.</p> <ul style="list-style-type: none"><li>• More expensive</li><li>• modification easy</li><li>• Resolution high</li><li>• Solid pattern is difficult to fill.</li></ul>

(5) Demonstrate general functions for window management using GLUT.

- glutCreateWindow - used to create a new window.
- glutCreateSubWindow - used to create another window within same window.
- glutSetWindow - used to set a particular id for the window.

glutGetWindow - used to get the window ID. (3)

- glutDestroyWindow - To delete the window that was created.
- glutPostRedisplay - To display the window again & again, continuously until forcibly closed.
- glutReshapeWindow - Used for transformation of world coordinates to view coordinates and displaying it.
- glutFullscreen - To represent window in full screen mode.
- glutPopWindow / glutPushWindow - Works just like a matrix on window.
- glutHideWindow - To hide the window from being displayed on screen.
- glutDisplayFunc - To display
- glutMainLoop
- init()

## 6. OpenGL visibility Detection Functions

(a) OpenGL polygon culling Functions  
Remove backface, front face of an object.

glCullFace(mode);

glEnable(GL\_CULL\_FACE);

glDisable(GL\_CULL\_FACE);

(b) Depth-Buffer Functions

glutInitDisplayMode(GLUT\_SINGLE)

(GLUT\_RGB | GLUT\_DEPTH)

glClear(GL\_DEPTH\_BUFFER\_BIT)

This works as initialization function for depth buffer and refresh buffer.

glDepthRange(farNornalDepth, nearNormalDepth)

glClear(GL\_DEPTH\_BUFFER\_BIT)

glClearDepth(farDepth)

glEnable(GL\_DEPTH\_TEST)

glDisable(GL\_DEPTH\_TEST)

(c) OpenGL Wireframe surface visibility Methods

glPolygonMode(GL\_FRONT\_AND\_BACK,

GL\_LINE), - visible & hidden edges displayed.

(d) OpenGL depth using Fns

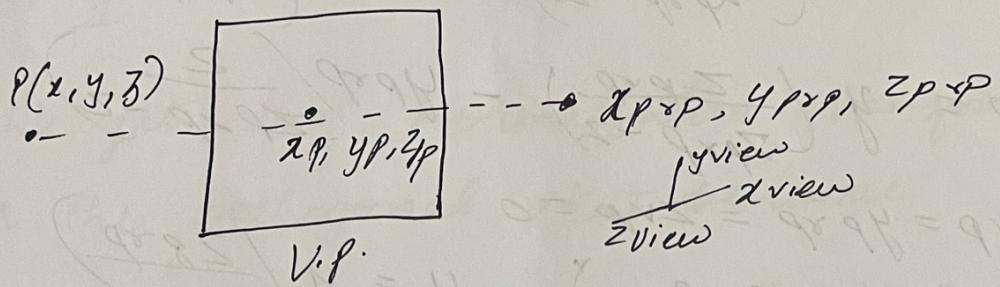
glFogi(GL\_FOG\_MODE, GL\_UNEAK)

glEnable(GL\_FOG)

To increase or decrease the brightness.

③ Write special cases discussed with Perspective Projections.

(4)



Consider

$$x' = x - (x - x_{\text{proj}})u$$

$$y' = y - (y - y_{\text{proj}})u$$

$$z' = z - (z - z_{\text{proj}})u$$

$$u = \frac{z_{\text{view}} - z}{z_{\text{proj}} - z}$$

$$x_{\text{proj}} = x \left( \frac{z_{\text{proj}} - z_{\text{view}}}{z_{\text{proj}} - z} \right) + x_{\text{view}} \left( \frac{z_{\text{view}} - z}{z_{\text{proj}} - z} \right)$$

$$y_{\text{proj}} = y \left( \frac{z_{\text{proj}} - z_{\text{view}}}{z_{\text{proj}} - z} \right) + y_{\text{view}} \left( \frac{z_{\text{view}} - z}{z_{\text{proj}} - z} \right)$$

Special cases :

$$\textcircled{1} \quad x_{\text{view}}, y_{\text{view}} = 0$$

$$x_{\text{proj}} = x \left( \frac{z_{\text{proj}} - z_{\text{view}}}{z_{\text{proj}} - z} \right)$$

$$y_{\text{proj}} = y \left( \frac{z_{\text{proj}} - z_{\text{view}}}{z_{\text{proj}} - z} \right)$$

$$\textcircled{2} \quad x_{\text{proj}}, y_{\text{proj}}, z_{\text{proj}} = (0, 0, 0); \text{ view depth } z_{\text{view}} = 0$$

$$x_{\text{proj}} = x \left( \frac{z_{\text{view}}}{z} \right)$$

$$y_{\text{proj}} = y \left( \frac{z_{\text{view}}}{z} \right)$$

$$3) z_{VP} = 0$$

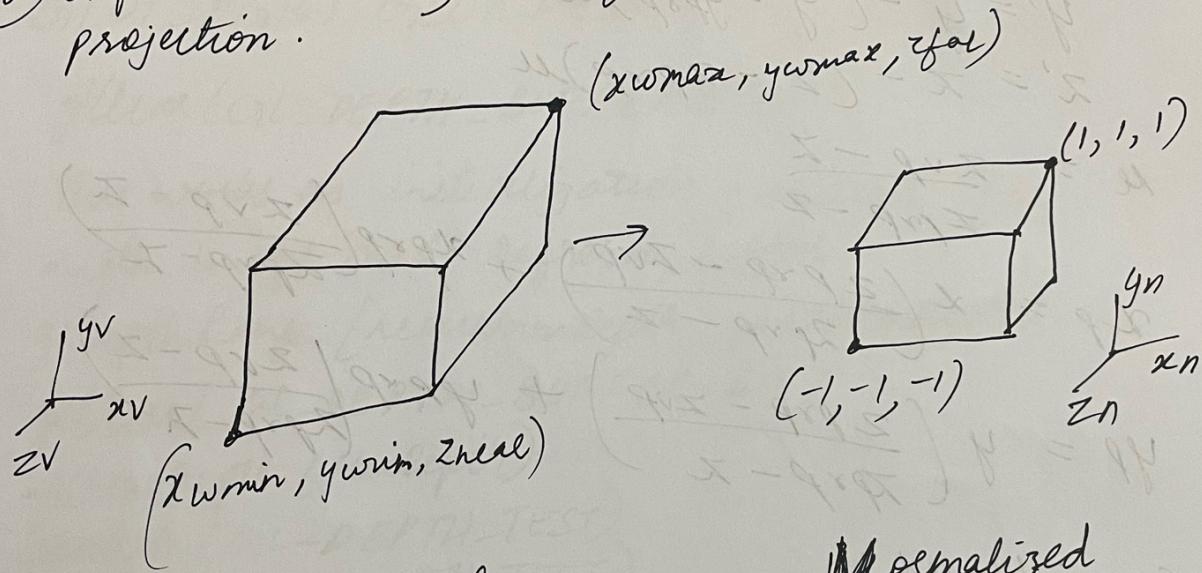
$$x_P = x \left( \frac{z_{PVP}}{z_{PVP} - z} \right) - x_{PVP} \left( \frac{z}{z_{PVP} - z} \right)$$

$$y_P = y \left( \frac{z_{PVP}}{z_{PVP} - z} \right) - y_{PVP} \left( \frac{z}{z_{PVP} - z} \right)$$

$$4) x_{PVP} = y_{PVP} = z_{VP} = 0$$

$$x_P = x \left( \frac{z_{PVP}}{z_{PVP} - z} \right), y_P = y \left( \frac{z_{PVP}}{z_{PVP} - z} \right)$$

⑧ Explain normalization for an orthogonal projection.



Orthogonal  
Projection  
View Volume

Normalized  
View  
Volume

We consider a unit cube for this normalized view volume with each  $x, y, z$  coordinates normalized in the range 0 to 1

• Another normalization transformation approach is to use symmetric cube with coordinates  $-1$  to  $1$  (9)

$\therefore$  We get the normalization transformation for the orthogonal view volume

$$M_{\text{ortho, norm}} = \begin{bmatrix} 2 & 0 & 0 \\ \frac{x_wmax - x_wmin}{x_wmax + x_wmin} & \frac{2}{x_wmax - x_wmin} & 0 \\ 0 & 0 & \frac{-2}{z_{near} - z_{far}} \\ 0 & 0 & 0 \end{bmatrix}$$

-  $\frac{x_wmax + x_wmin}{x_wmax - x_wmin}$   
 -  $\frac{y_wmax + y_wmin}{y_wmax - y_wmin}$   
 -  $\frac{z_{near} + z_{far}}{z_{near} - z_{far}}$

(9) Explain Bezier Curve and its properties with equations.

Bezier curves are parametric curves that are generated with the help of control points. It is widely used in graphics and other related industry.