```
In [1]: | import time
        import datetime
        import pandas as pd
        import matplotlib.pyplot as plt
        import plotly.express as px
        import seaborn as sb
        import numpy as np
        import random
        from statsmodels.tsa.arima.model import ARIMA
        from statsmodels.tsa.holtwinters import SimpleExpSmoothing, ExponentialS
        moothing
        from sklearn.neighbors import KNeighborsRegressor
        from sklearn.model_selection import train_test_split,GridSearchCV
        from sklearn.model selection import KFold
        from sklearn.metrics import mean_squared_error
        from sklearn.model_selection import train_test_split
        from sklearn.preprocessing import StandardScaler, PolynomialFeatures
        from sklearn.linear_model import Lasso
        from sklearn.metrics import mean_squared_error
        from sklearn.pipeline import Pipeline
        from sklearn.model selection import GridSearchCV
        import pickle
        import yfinance as yf
        from sklearn.metrics import mean absolute error, mean squared error
        from sklearn.linear model import LinearRegression, LogisticRegression
        from sklearn.preprocessing import MinMaxScaler
        from tensorflow.keras.models import Sequential
        from tensorflow.keras.layers import Dense, LSTM
        from sklearn.ensemble import RandomForestRegressor
        from sklearn.metrics import r2 score
        from sklearn.model selection import RandomizedSearchCV
        from scipy.stats import randint
        from tensorflow import random
```

/usr/local/lib/python3.8/dist-packages/statsmodels/tsa/base/tsa_model.p y:7: FutureWarning: pandas.Int64Index is deprecated and will be removed from pandas in a future version. Use pandas.Index with the appropriate dtype instead.

from pandas import (to_datetime, Int64Index, DatetimeIndex, Period, /usr/local/lib/python3.8/dist-packages/statsmodels/tsa/base/tsa_model.p y:7: FutureWarning: pandas.Float64Index is deprecated and will be removed from pandas in a future version. Use pandas.Index with the appropriate dtype instead.

from pandas import (to datetime, Int64Index, DatetimeIndex, Period,

```
In [2]: ticker = '^GSPC'
    period1 = int(time.mktime(datetime.datetime(1927, 12, 29, 23, 59).timetu
    ple()))
    period2 = int(time.mktime(datetime.datetime(2023, 1, 16, 23, 59).timetup
    le()))
    interval = 'ld'

    query_string = f'https://query1.finance.yahoo.com/v7/finance/download/{t
    icker}?period1={period1}&period2={period2}&interval={interval}&events=hi
    story&includeAdjustedClose=true'

    df = pd.read_csv(query_string)

    csv_data=df.to_csv('SNP.csv', header=True, index = False)

    snpdf = pd.read_csv("SNP.csv")
    snpdf.head()
```

Out[2]:

	Date	Open	High	Low	Close	Adj Close	Volume
0	1927-12-30	17.660000	17.660000	17.660000	17.660000	17.660000	0
1	1928-01-03	17.760000	17.760000	17.760000	17.760000	17.760000	0
2	1928-01-04	17.719999	17.719999	17.719999	17.719999	17.719999	0
3	1928-01-05	17.549999	17.549999	17.549999	17.549999	17.549999	0
4	1928-01-06	17.660000	17.660000	17.660000	17.660000	17.660000	0

In [3]: snpdf.shape

Out[3]: (23874, 7)

In [4]: snpdf.describe()

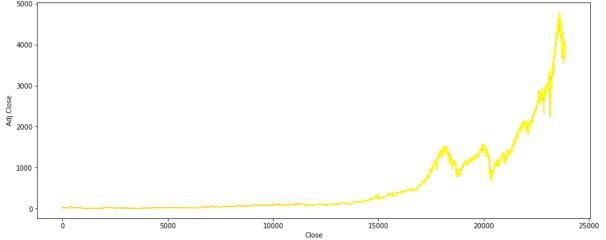
Out[4]:

	Open	High	Low	Close	Adj Close	Volume
count	23874.000000	23874.000000	23874.000000	23874.000000	23874.000000	2.387400e+04
mean	551.068917	574.621012	567.544959	571.304355	571.304355	8.563583e+08
std	916.289815	910.203806	899.249453	905.060532	905.060532	1.579850e+09
min	0.000000	4.400000	4.400000	4.400000	4.400000	0.000000e+00
25%	9.480000	24.350000	24.350000	24.350000	24.350000	1.420000e+06
50%	39.459999	101.910000	100.349998	101.079998	101.079998	1.887000e+07
75%	942.289978	950.774994	932.690002	942.297485	942.297485	7.614500e+08
max	4804.509766	4818.620117	4780.040039	4796.560059	4796.560059	1.145623e+10

```
In [5]: snpdf.info()
        <class 'pandas.core.frame.DataFrame'>
        RangeIndex: 23874 entries, 0 to 23873
        Data columns (total 7 columns):
                        Non-Null Count Dtype
             Column
                                         object
         0
             Date
                        23874 non-null
         1
             Open
                        23874 non-null
                                        float64
         2
                        23874 non-null
                                         float64
             High
         3
             Low
                        23874 non-null
                                        float64
         4
             Close
                        23874 non-null
                                        float64
             Adj Close 23874 non-null float64
             Volume
                        23874 non-null
                                         int64
        dtypes: float64(5), int64(1), object(1)
        memory usage: 1.3+ MB
```

There are no null values in the data set.

```
In [7]: plt.figure(figsize=(15,6))
   plt.plot(snpdf['Close'],'red')
   plt.plot(snpdf['Adj Close'],'yellow')
   plt.xlabel('Close')
   plt.ylabel('Adj Close')
   plt.show()
```



```
In [8]: snpdf['Close'].equals(snpdf['Adj Close'])
Out[8]: True
```

From both of the tests above, we can see that values of Close and Adj Close are same and hence we can drop one of the columns.

```
In [9]: del snpdf['Adj Close']
         snpdf.head()
Out[9]:
                 Date
                         Open
                                   High
                                            Low
                                                    Close Volume
         0 1927-12-30 17.660000 17.660000 17.660000
                                                              0
         1 1928-01-03 17.760000 17.760000 17.760000 17.760000
         2 1928-01-04 17.719999 17.719999 17.719999
                                                              0
         3 1928-01-05 17.549999 17.549999
                                                              0
                                       17.549999 17.549999
         4 1928-01-06 17.660000 17.660000 17.660000
                                                              0
```

snpdf['Date']=pd.to_datetime(snpdf['Date'])

In [10]:

Closing Price of S&P500 over years



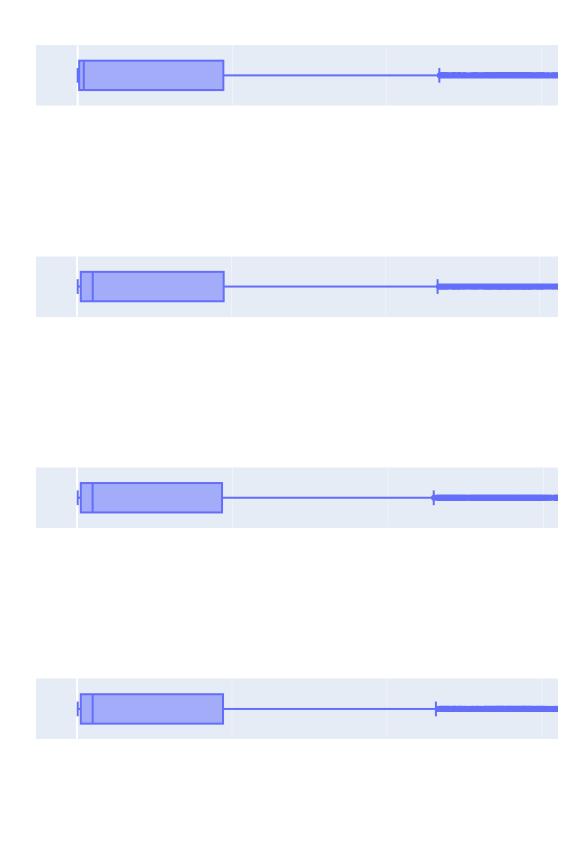
Reason behind dip or growth in S&P 500 throughout years

- Rise in 1999: Investors invested a lot of money into interent based startups known as dot-com bubble
- Drop in 2002: Fallout from frenzied investments in internet tech companies and implosion of dot-com bubble
- Drop in 2008: Widespread debt defaults created distrust in stock investment along with Great Recession
- Drop in 2020: The COVID-19 pandemic affected stock market sending the world into recession
- Rise in 2021: Continued federal support, low interest rates, a healthy job market, and massive growth in the largest sector of the U.S. economy technology

```
In [12]: features = ['Open', 'High', 'Low', 'Close', 'Volume']

for i, col in enumerate(features):

    duration_box = px.box(
        snpdf,
        x=snpdf[col],
        height=200
    )
    duration_box.show()
```





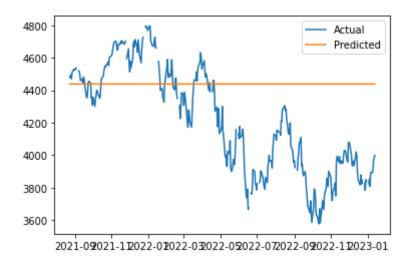
From above boxplots, we can see that only Volume column has outliers values. The rest of the columns doesn't have significant number of outliers.

ARIMA

```
In [13]: arpdf = snpdf.copy()
    arpdf['Date'] = pd.to_datetime(arpdf['Date'])
    arpdf.set_index('Date', inplace=True)
    arpdf = arpdf.asfreq('B')
    train = arpdf.iloc[:-365]
    test = arpdf.iloc[-365:]
    arimamodel = ARIMA(train['Close'], order=(1,1,1))
    model_fit = arimamodel.fit()
    predictions = model_fit.predict(start=len(train), end=len(train)+len(test)-1, typ='levels')
    plt.plot(test['Close'], label='Actual')
    plt.plot(predictions, label='Predicted')
    plt.legend()
    plt.show()
```

/usr/local/lib/python3.8/dist-packages/statsmodels/tsa/base/tsa_model.p y:574: FutureWarning:

is_monotonic is deprecated and will be removed in a future version. Use is_monotonic_increasing instead.



Linear Regression

```
In [15]: lrmodel = LinearRegression()
lrmodel.fit(X_train_lr, y_train_lr)

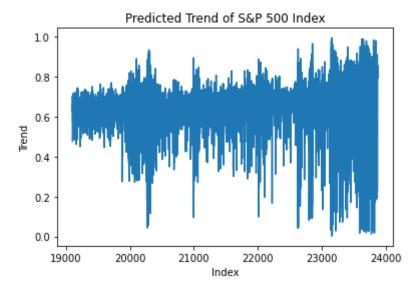
Out[15]: LinearRegression()

In [16]: y_pred_lr = lrmodel.predict(X_test_lr)
    y_pred_lr = np.exp(y_pred_lr) / (1 + np.exp(y_pred_lr)) #Transforming pr
    edicted value between 0 and 1
    MSE = mean_squared_error(y_test_lr, y_pred_lr)
    print("Mean Square Error:", MSE)

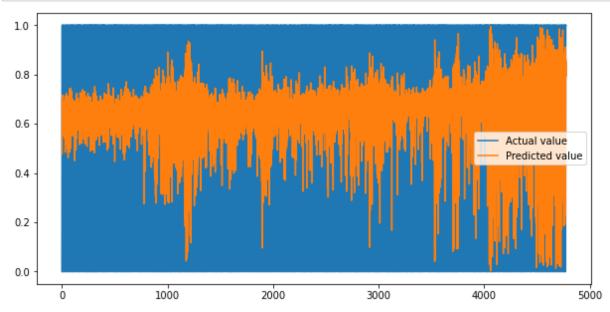
Mean Square Error: 0.19593024156229216
```

```
In [17]: dates = X_test_lr.index
    pred_lrdf = pd.DataFrame({"Date": dates, "Trend": y_pred_lr})

# Plot the predicted trend values
    plt.plot(pred_lrdf["Date"], pred_lrdf["Trend"])
    plt.title("Predicted Trend of S&P 500 Index")
    plt.xlabel("Index")
    plt.ylabel("Trend")
    plt.show()
```



```
In [18]: plt.figure(figsize=(10,5))
    plt.plot(y_test_lr.values, label="Actual value")
    plt.plot(y_pred_lr, label="Predicted value")
    plt.legend()
    plt.show()
```



kNN

```
In [19]: X_train, X_test, y_train, y_test = train_test_split(snpdf[['Open', 'Lo
    w', 'High', 'Volume']], snpdf['Close'], test_size=0.2, random_state=10,
    shuffle=False)

# Initialize the regressor and set the number of neighbors (k)
    k = 5
    knn = KNeighborsRegressor(n_neighbors=k)

knn.fit(X_train, y_train)

y_pred = knn.predict(X_test)

mse_knn1 = mean_squared_error(y_test, y_pred)
    print("Mean Squared Error: ", mse_knn1)
```

Mean Squared Error: 2348137.4819751726

```
In [20]: X_train, X_test, y_train, y_test = train_test_split(snpdf[['Open', 'Lo
    w', 'High', 'Volume']], snpdf['Close'], test_size=0.2, random_state=10,
    shuffle=False)

scaler = StandardScaler()
scaler.fit(X_train)

X_train_scaled = scaler.transform(X_train)
X_test_scaled = scaler.transform(X_test)

k = 5
knn = KNeighborsRegressor(n_neighbors=k)

knn.fit(X_train_scaled, y_train)

y_pred = knn.predict(X_test_scaled)

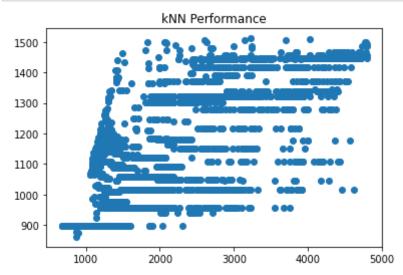
mse_knn2 = mean_squared_error(y_test, y_pred)
print("Mean Squared Error: ", mse_knn2)
```

Mean Squared Error: 1546639.2560510621

```
In [21]: X train, X test, y train, y test = train test split(snpdf[['Open', 'Lo
         w', 'High', 'Volume']], snpdf['Close'], test_size=0.2, random_state=10,
         shuffle=False)
         scaler = StandardScaler()
         scaler.fit(X_train)
         X_train_scaled = scaler.transform(X_train)
         X test scaled = scaler.transform(X test)
         param_grid = {
             "n_neighbors": [3, 5, 7, 9],
             "weights": ["uniform", "distance"],
             "p": [1, 2]
         }
         knn = KNeighborsRegressor()
         grid_search = GridSearchCV(knn, param_grid, cv=5)
         grid_search.fit(X_train_scaled, y_train)
         print("Best hyperparameters for kNN:", grid search.best params_)
         # Use the best hyperparameters to initialize a new KNN regressor and fit
         it on the scaled training data
         best knn = KNeighborsRegressor(**grid search.best params )
         best_knn.fit(X_train_scaled, y_train)
         y pred = best knn.predict(X test scaled)
         mse knn3 = mean squared error(y test, y pred)
         print("Mean Squared Error: ", mse_knn3)
         Best hyperparameters for kNN: {'n neighbors': 9, 'p': 2, 'weights': 'un
         iform'}
```

Mean Squared Error: 1565827.4598722989

```
In [22]: plt.scatter(y_test, y_pred)
   plt.title('kNN Performance')
   plt.show()
```



Lasso Regression

```
In [23]: lsdf = snpdf
X_train, X_test, y_train, y_test = train_test_split(lsdf[['Open', 'Clos
e', 'Low', 'High']], lsdf['Volume'], test_size=0.3, random_state=42, shu
ffle=False)
```

```
In [24]: scaler = StandardScaler()
    X_train = scaler.fit_transform(X_train)
    X_test = scaler.transform(X_test)
```

/home/nbgrader/spring22/student-accounts/jkovach2/.local/lib/python3.8/site-packages/sklearn/linear_model/_coordinate_descent.py:647: Converge nceWarning:

Objective did not converge. You might want to increase the number of it erations, check the scale of the features or consider increasing regula risation. Duality gap: 2.330e+18, tolerance: 7.517e+15

```
Out[25]: Lasso(alpha=0.5, max iter=100000)
```

```
In [26]: y_pred = lasso.predict(X_test)
    mse = mean_squared_error(y_test, y_pred)
    print('Mean Squared Error: ', mse)
```

Mean Squared Error: 5.41005210477516e+18

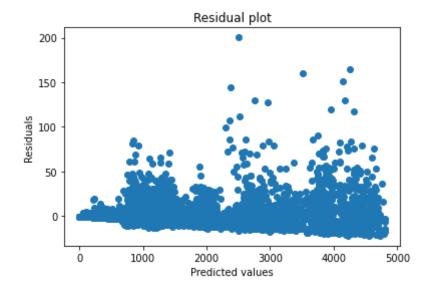
```
In [27]: X train, X test, y train, y test = train test split(lsdf[['Open', 'Low',
         'High', 'Volume']], lsdf['Close'], test size=0.3, random state=42, shuff
         le=False)
In [28]: scaler = StandardScaler()
         X_train = scaler.fit_transform(X_train)
         X test = scaler.transform(X test)
In [29]: lasso2 = Lasso(alpha=0.1, max_iter=10000) # set the regularization param
         eter alpha to 0.1
         lasso2.fit(X_train, y_train)
Out[29]: Lasso(alpha=0.1, max iter=10000)
In [30]: y pred = lasso2.predict(X test)
         mse = mean squared error(y test, y pred)
         print('Mean Squared Error: ', mse)
         Mean Squared Error: 243.26719080932938
In [31]: X = snpdf[['Low', 'High', 'Open', 'Volume']].values
         y = snpdf['Close'].values
         lasso pipe = Pipeline([
             ('scaler', StandardScaler()),
             ('lasso', Lasso())
         ])
         lasso pipe.named steps['lasso'].shuffle = False
         param_grid = {'lasso__alpha': np.logspace(-5, 1, 100)}
         kf = KFold(n splits=5, shuffle=False)
         grid_search = GridSearchCV(lasso_pipe, param_grid, cv=kf, scoring='neg_m
         ean squared error')
         grid_search.fit(X, y)
         print("Best alpha:", grid search.best params ['lasso alpha'])
         print("Mean squared error:", -grid_search.best_score_)
         Best alpha: 1.232846739442066
```

Mean squared error: 51.95472246634172

```
In [32]: y_pred = grid_search.predict(X)
    residuals = y - y_pred

    plt.scatter(y_pred, residuals)
    plt.xlabel('Predicted values')
    plt.ylabel('Residuals')
    plt.title('Residual plot')
```

Out[32]: Text(0.5, 1.0, 'Residual plot')



```
In [33]: X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=0, shuffle = False)

y_pred = np.roll(y_test, 1)

mse_baseline = mean_squared_error(y_test, y_pred)

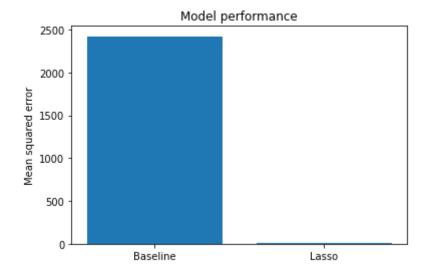
grid_search.fit(X_train, y_train)

y_pred = grid_search.predict(X_test)

mse_lasso = mean_squared_error(y_test, y_pred)

plt.bar(['Baseline', 'Lasso'], [mse_baseline, -grid_search.best_score_])
plt.ylabel('Mean squared error')
plt.title('Model performance')
```

Out[33]: Text(0.5, 1.0, 'Model performance')



```
In [34]: import joblib
    joblib.dump(grid_search.best_estimator_, 'lasso_model.pkl')
Out[34]: ['lasso_model.pkl']
In [35]: lasso_model = joblib.load('lasso_model.pkl')
```

```
In [36]: sp500 = yf.download('^GSPC', start='2023-01-23', end='2023-03-31')

del sp500['Adj Close']

X_new = sp500.drop(['Close'], axis=1)
y_pred = lasso_model.predict(X_new)

y_true = sp500['Close'].values
mae = mean_absolute_error(y_true, y_pred)
rmse = np.sqrt(mean_squared_error(y_true, y_pred))

print(f"MAE: {mae:.2f}")
print(f"RMSE: {rmse:.2f}")
```

[********* 100%*********** 1 of 1 completed

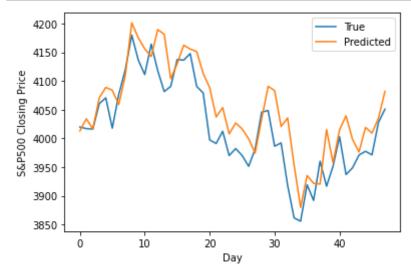
MAE: 38.44 RMSE: 49.04

/home/nbgrader/spring22/student-accounts/jkovach2/.local/lib/python3.8/site-packages/sklearn/base.py:443: UserWarning:

 ${\tt X}$ has feature names, but StandardScaler was fitted without feature name ${\tt s}$

```
In [37]: plt.plot(y_true, label='True')
   plt.plot(y_pred, label='Predicted')

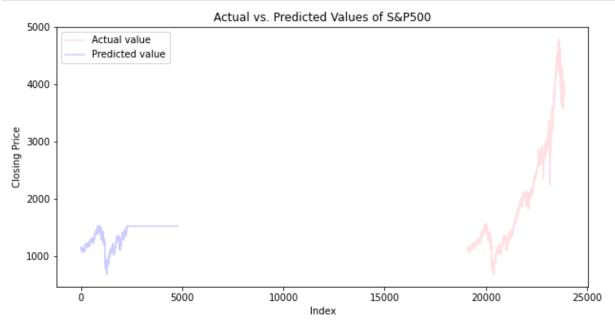
   plt.xlabel('Day')
   plt.ylabel('S&P500 Closing Price')
   plt.legend()
```



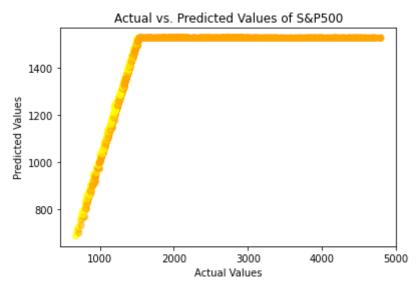
Random forest

```
In [38]: X=snpdf.drop(['Close', 'Date'], axis=1)
         y=snpdf['Close']
         #Splitting into training(80%) and testing data
         X_train_rf, X_test_rf, y_train_rf, y_test_rf = train_test_split(X, y, te
         st_size=0.2, random_state=np.random.seed(40), shuffle=False)
In [39]: #Creating random forest model
         rfmodel = RandomForestRegressor(n_estimators=100, random_state=np.rando
         m.seed(40))
In [40]: #Training the model
         rfmodel.fit(X_train_rf, y_train_rf)
Out[40]: RandomForestRegressor()
In [41]: predictions_rf = rfmodel.predict(X_test_rf)
In [42]: MSE_rf = mean_squared_error(y_test_rf, predictions_rf)
         print('Mean squared error:', MSE_rf)
         Mean squared error: 1194173.6016176166
In [43]: r2_rf = r2_score(y_test_rf, predictions_rf)
         print('R squared:', r2_rf)
         R squared: -0.20686592248754931
```

```
In [44]: plt.figure(figsize=(10,5))
    plt.plot(y_test_rf,color='pink', label='Actual value', alpha=0.5)
    plt.plot(predictions_rf,color='blue', label='Predicted value', alpha=0.
    2)
    plt.xlabel('Index')
    plt.ylabel('Closing Price')
    plt.title('Actual vs. Predicted Values of S&P500')
    plt.legend()
    plt.show()
```

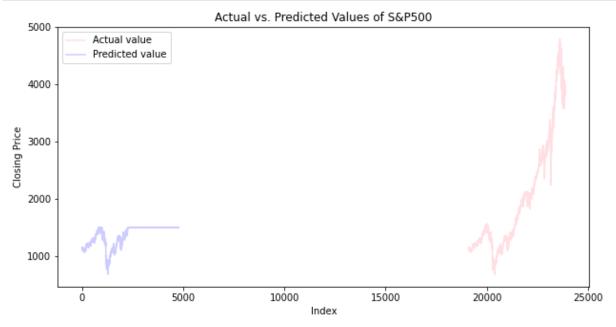


```
In [45]: plt.scatter(y_test_rf,predictions_rf, c=['yellow' if x < y else 'orang
e' for x, y in zip(y_test_rf, predictions_rf)], alpha=0.5 )
#yellow-predicted
plt.xlabel('Actual Values')
plt.ylabel('Predicted Values')
plt.title('Actual vs. Predicted Values of S&P500')
plt.show()</pre>
```

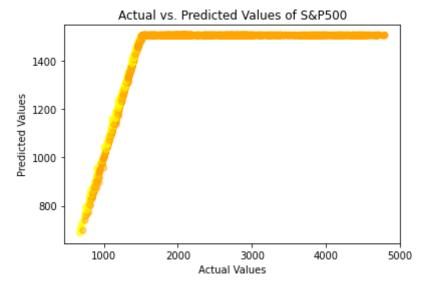


```
In [46]: param_dist = {'n_estimators': randint(50, 500),
                       'max_features': ['auto', 'sqrt', 'log2'],
                       'max depth': [10, 20, 30, 40, None],
                        'min_samples_split': randint(2, 20),
                       'min samples leaf': randint(1, 10)}
         random_search = RandomizedSearchCV(rfmodel, param_distributions=param_di
         st, n iter=50,
                                            n_jobs=-1, cv=5, random_state=np.rand
         om.seed(40))
In [47]: random_search.fit(X_train_rf, y_train_rf)
         print('Best hyperparameters:', random search.best params_)
         Best hyperparameters: {'max_depth': 40, 'max_features': 'log2', 'min_sa
         mples_leaf': 3, 'min_samples_split': 8, 'n_estimators': 107}
In [48]: #Random forest model using best parameters
         #New shuffle
         rfmodel_best = RandomForestRegressor(n_estimators=230, max_features='sqr
         t', max_depth=30,
                                          min samples split=10, min samples leaf=
         2, random_state=np.random.seed(40))
In [49]: rfmodel best.fit(X train rf, y train rf)
Out[49]: RandomForestRegressor(max depth=30, max features='sqrt', min samples le
         af=2,
                               min samples split=10, n estimators=230)
In [50]: predictions rfbest = rfmodel best.predict(X test rf)
In [51]: MSE rfbest = mean squared error(y test rf, predictions rfbest)
         print('Mean squared error:', MSE rfbest)
         r2 rfbest = r2 score(y test rf, predictions rfbest)
         print('R squared:', r2_rfbest)
         Mean squared error: 1220410.749592023
         R squared: -0.23338193301623744
```

```
In [52]: plt.figure(figsize=(10,5))
    plt.plot(y_test_rf,color='pink', label='Actual value', alpha=0.5)
    plt.plot(predictions_rfbest,color='blue', label='Predicted value', alpha
    =0.2)
    plt.xlabel('Index')
    plt.ylabel('Closing Price')
    plt.title('Actual vs. Predicted Values of S&P500')
    plt.legend()
    plt.show()
```



```
In [53]: plt.scatter(y_test_rf,predictions_rfbest, c=['yellow' if x < y else 'or ange' for x, y in zip(y_test_rf, predictions_rfbest)], alpha=0.5 )
#yellow-predicted
plt.xlabel('Actual Values')
plt.ylabel('Predicted Values')
plt.title('Actual vs. Predicted Values of S&P500')
plt.show()</pre>
```



LSTM-Long Short Term Memory Neural Network Model

```
In [54]: lstmdf = snpdf

lstmdf['Date'] = pd.to_datetime(lstmdf['Date'])

lstmdf['Year'] = lstmdf['Date'].dt.year
    lstmdf['Month'] = lstmdf['Date'].dt.month
    lstmdf['Day'] = lstmdf['Date'].dt.day

lstmdf = lstmdf.drop(columns=['Date'])

lstmdf.head()
```

Out[54]:

	Open	High	Low	Close	Volume	Trend	Year	Month	Day
0	17.660000	17.660000	17.660000	17.660000	0	0	1927	12	30
1	17.760000	17.760000	17.760000	17.760000	0	1	1928	1	3
2	17.719999	17.719999	17.719999	17.719999	0	0	1928	1	4
3	17.549999	17.549999	17.549999	17.549999	0	0	1928	1	5
4	17.660000	17.660000	17.660000	17.660000	0	1	1928	1	6

```
In [55]: #Scaling data
    scaler = MinMaxScaler()
    scaling_data = scaler.fit_transform(lstmdf)
```

```
In [56]: #Splitting into training(80%) and testing data
    train_size = int(len(scaling_data) * 0.8)
    train_data = scaling_data[:train_size, :]
    test_data = scaling_data[train_size:, :]
```

```
In [57]: #Creating sequence

def create_sequence(data, length):
    X = []
    y = []
    for i in range(len(data)-length):
        X.append(data[i:i+length])
        y.append(data[i+length])
    return np.array(X), np.array(Y)

length = 10

X_train, y_train = create_sequence(train_data, length)
    X_test, y_test = create_sequence(test_data,length)
```

```
In [58]: #LSTM model
    random.set_seed(452)
    lstmmodel = Sequential()

    lstmmodel.add(LSTM(50,input_shape=(length, lstmdf.shape[1])))
    lstmmodel.add(Dense(9)) #Dense(8)
    lstmmodel.compile(loss='mean_squared_error', optimizer='adam')
```

In [59]: #Training the model history = lstmmodel.fit(X_train, y_train, epochs=15, batch_size=2, valid ation_split=0.1, verbose=1)

```
Epoch 1/15
6 - val loss: 0.0320
Epoch 2/15
9 - val loss: 0.0317
Epoch 3/15
5 - val_loss: 0.0331
Epoch 4/15
4 - val loss: 0.0352
Epoch 5/15
3 - val loss: 0.0324
Epoch 6/15
1 - val loss: 0.0323
Epoch 7/15
1 - val loss: 0.0340
Epoch 8/15
9 - val loss: 0.0328
Epoch 9/15
9 - val loss: 0.0330
Epoch 10/15
8 - val loss: 0.0336
Epoch 11/15
8 - val loss: 0.0317
Epoch 12/15
7 - val loss: 0.0325
Epoch 13/15
6 - val loss: 0.0320
Epoch 14/15
8590/8590 [=============== ] - 50s 6ms/step - loss: 0.029
4 - val loss: 0.0333
Epoch 15/15
4 - val loss: 0.0327
```

```
In [63]: plt.figure(figsize=(10,5))
    plt.plot(y_test,color='yellow', label='Actual value', alpha=0.5)
    plt.plot(predictions,color='black', label='Predicted value', alpha=0.5)
    plt.xlabel('Year')
    plt.ylabel('S&P500 Index')
    plt.legend()
    plt.show()
```

