

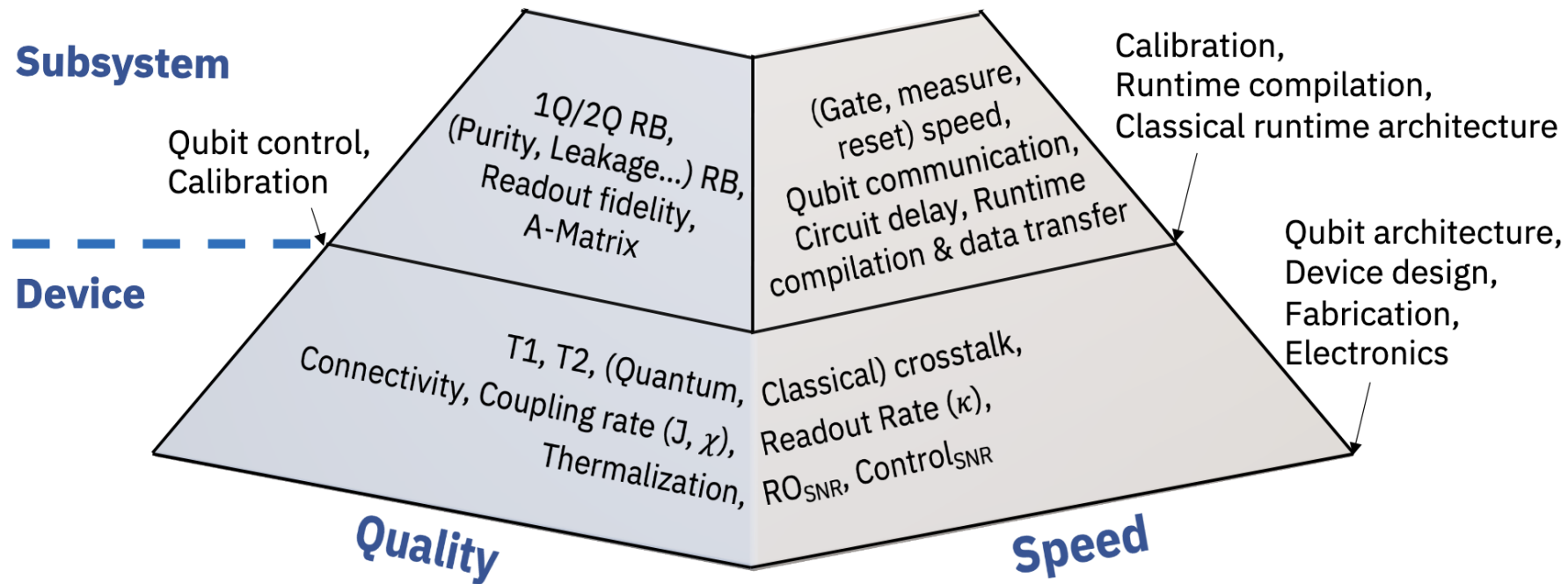
# Quantum Benchmarking II

**Majo Lozano**

*Quantum Hardware Engineer*

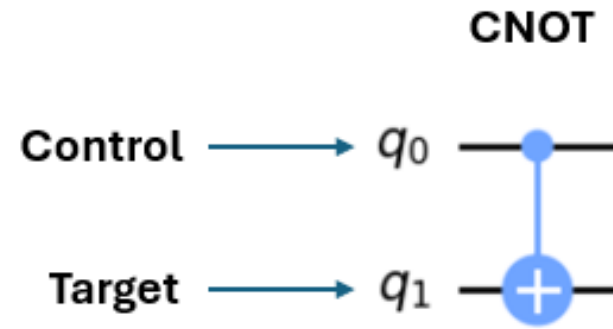
IBM Quantum

# What have we covered so far?



# Hellinger Fidelity of a Bell State

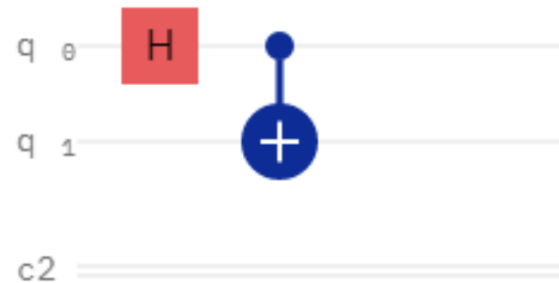
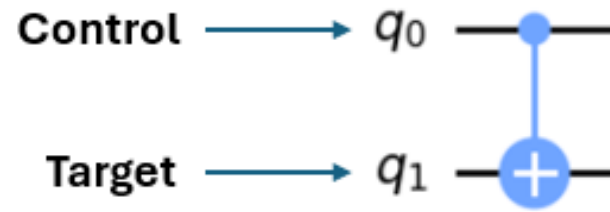
- Benchmarks a 2Q entangling gate
- CNOT



# Hellinger Fidelity of a Bell State

- Generates a bell state using an odd number of CNOTS
- 4 distinct bell states (maximally entangled states)
- Compares with ideal results

CNOT



$$|\Phi^+\rangle = \frac{|00\rangle + |11\rangle}{\sqrt{2}}$$

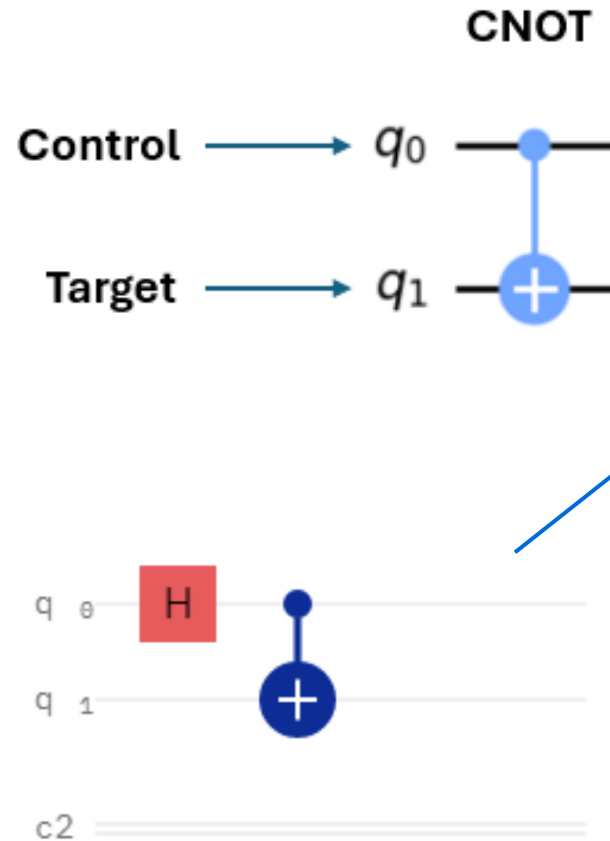
$$|\Phi^-\rangle = \frac{|00\rangle - |11\rangle}{\sqrt{2}}$$

$$|\Psi^+\rangle = \frac{|01\rangle + |10\rangle}{\sqrt{2}}$$

$$|\Psi^-\rangle = \frac{|01\rangle - |10\rangle}{\sqrt{2}}$$

# Hellinger Fidelity of a Bell State

- Hellinger Fidelity given as  $(1-H^2)^2$  where  $H$  is the Hellinger distance
- Distance between 2 count distributions (ideal case and experimental case)
- Sensitive to qubit initialization, 1Q and 2Q errors, and readout errors



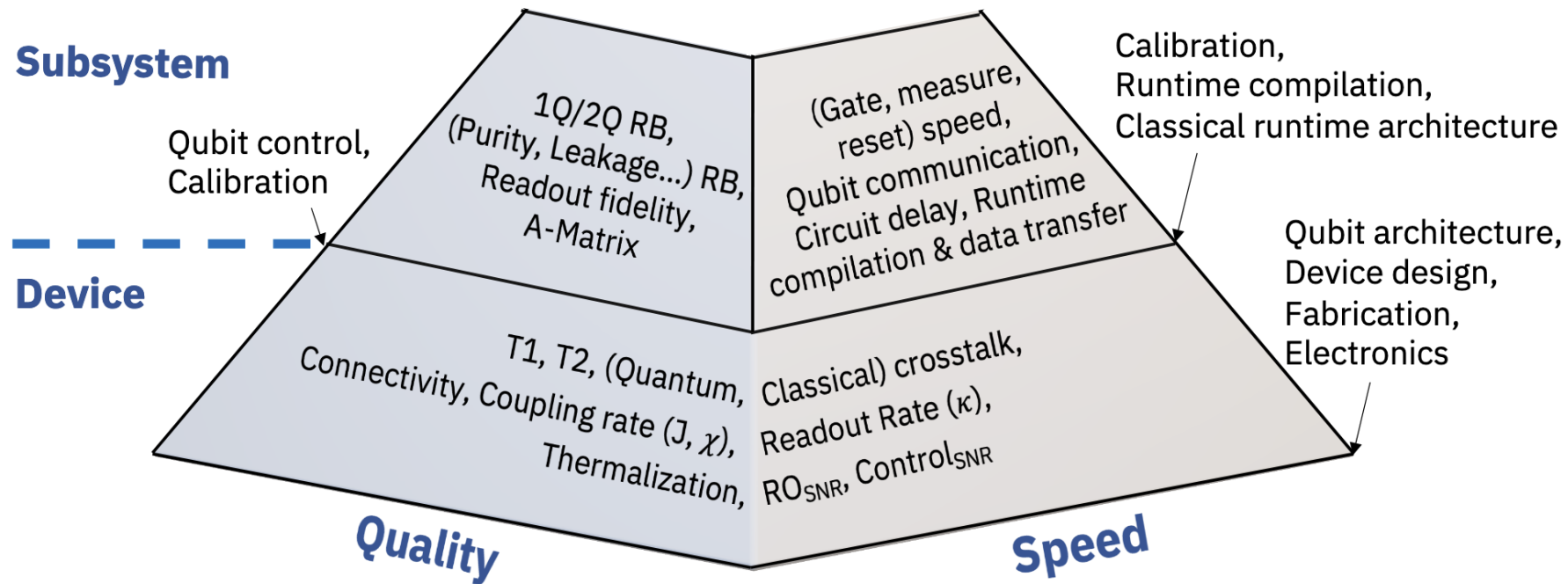
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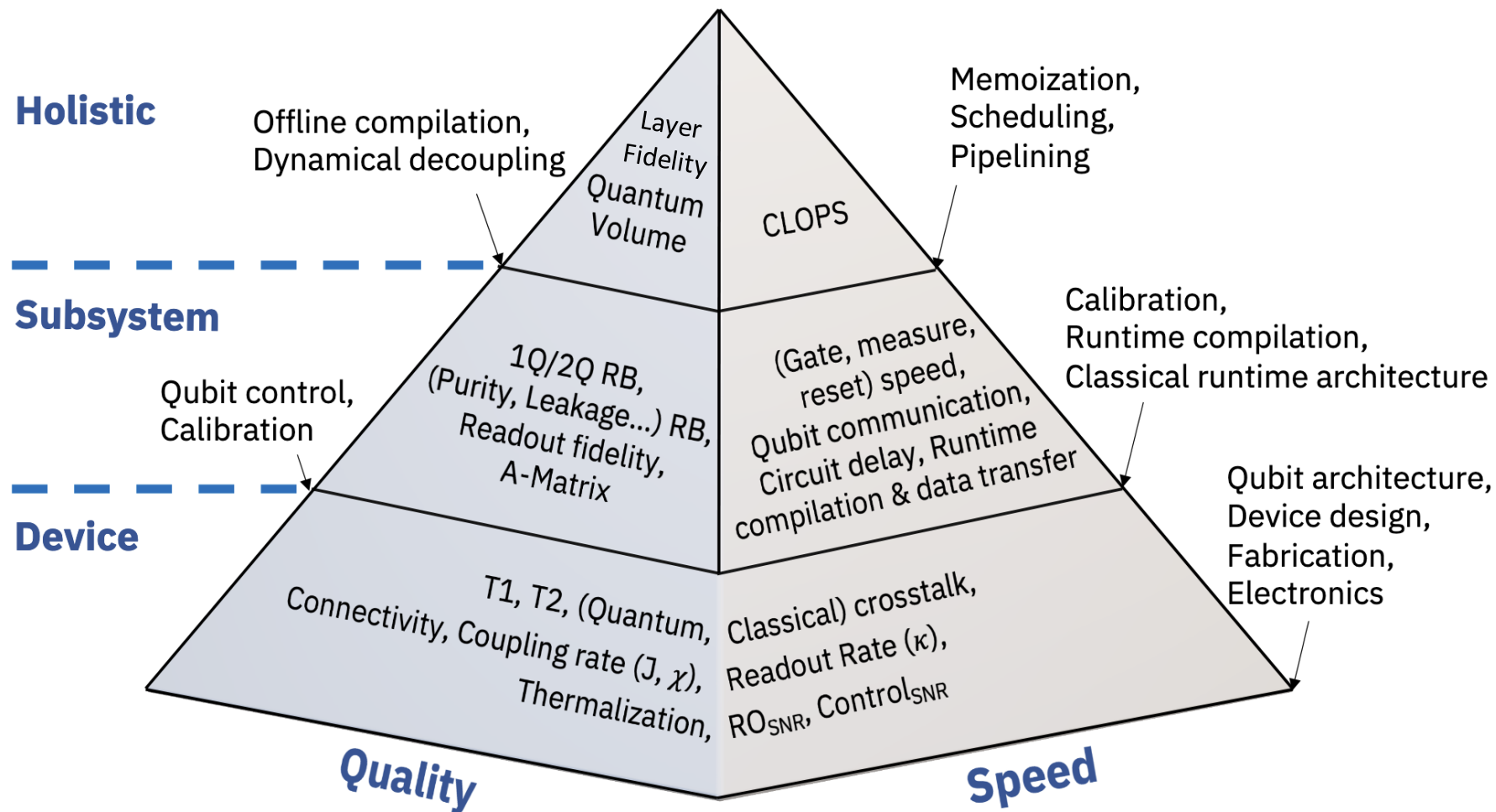
$$|\Psi^+\rangle = \frac{|01\rangle + |10\rangle}{\sqrt{2}}$$

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# What have we covered so far?

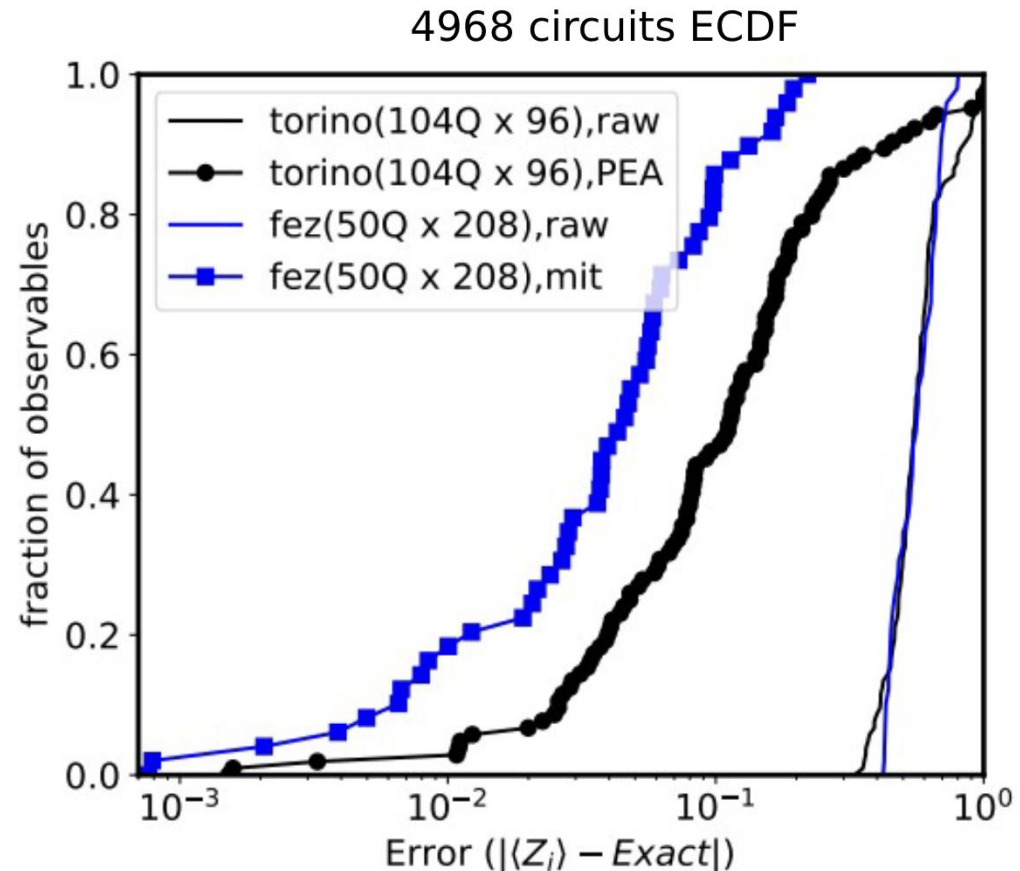


# What have we covered so far?



# Mirror Circuit (MC)

- Primitive quality benchmark
- Indicates the ability to deliver accurate observables for utility-scale circuits (5K gates)
- **Idea:** Apply a utility-scale circuit followed by its inverse. Useful for testing error mitigation (we require estimation tasks with easy-to-compute ideal answers)

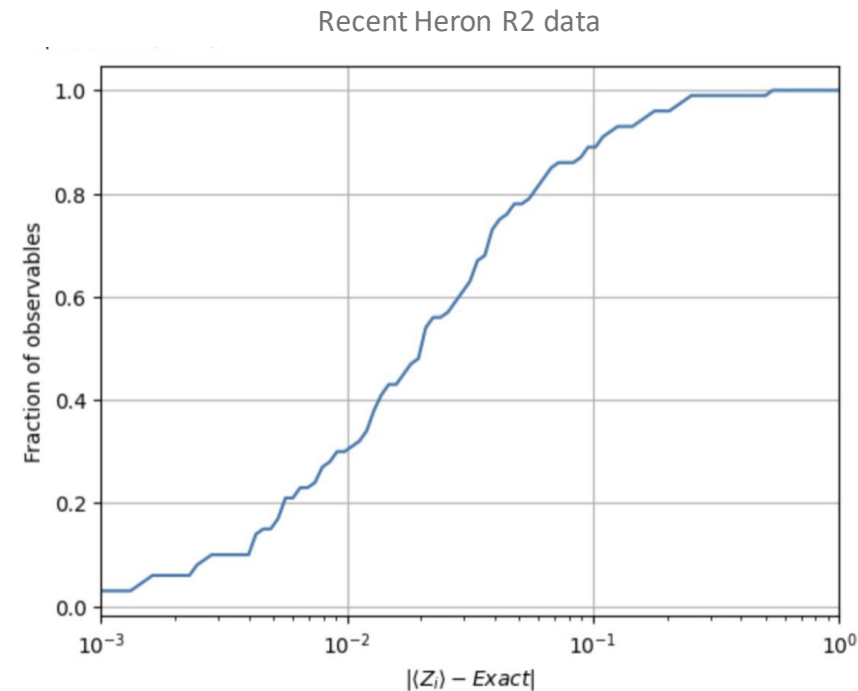
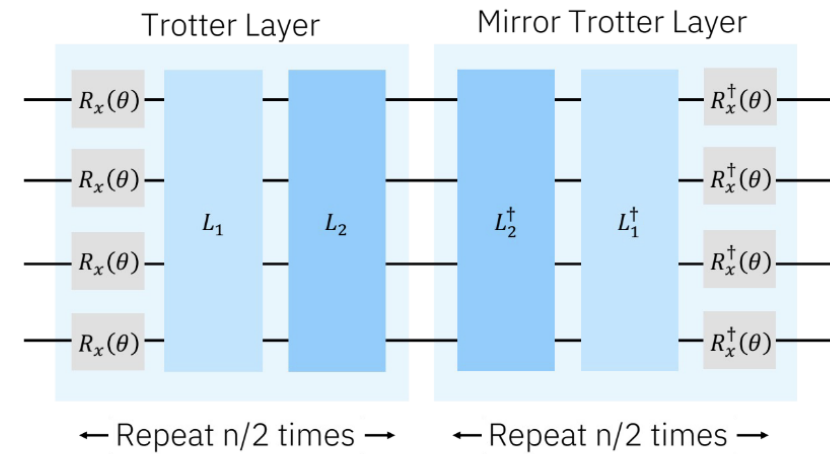


More than 40% of 1Q observables within 10% of ideal value at 5k scale.



# Mirror Circuit (MC)

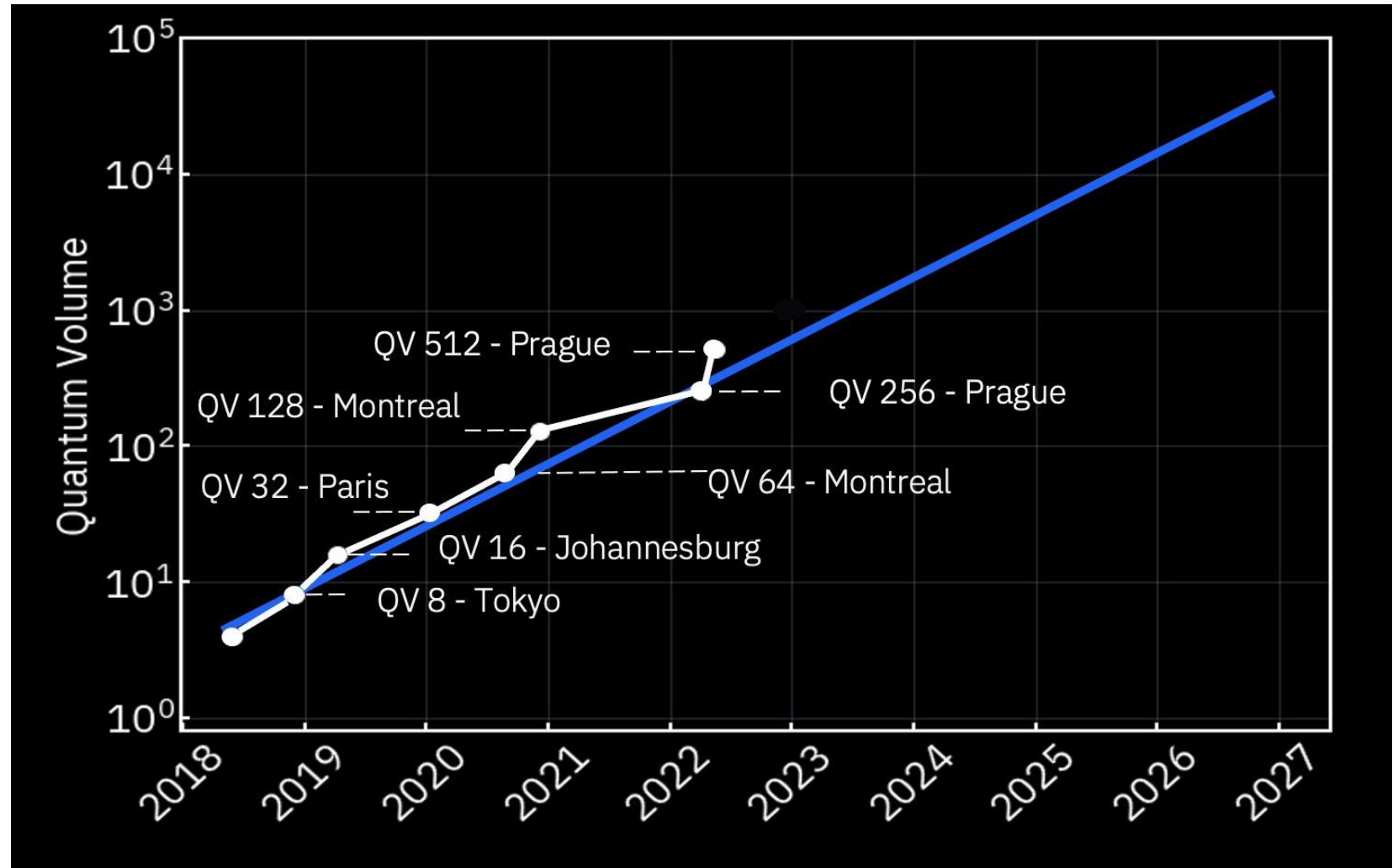
- **Utility-scale circuit:**  
evolution of a 1D Ising chain (trotterized time) followed by its inverse
- Effective action is equivalent to the **identity**
- Easy to detect whether the returned observables are accurate
- Plot: distribution (observables - exact case). We care about observables within 10% of the ideal solution

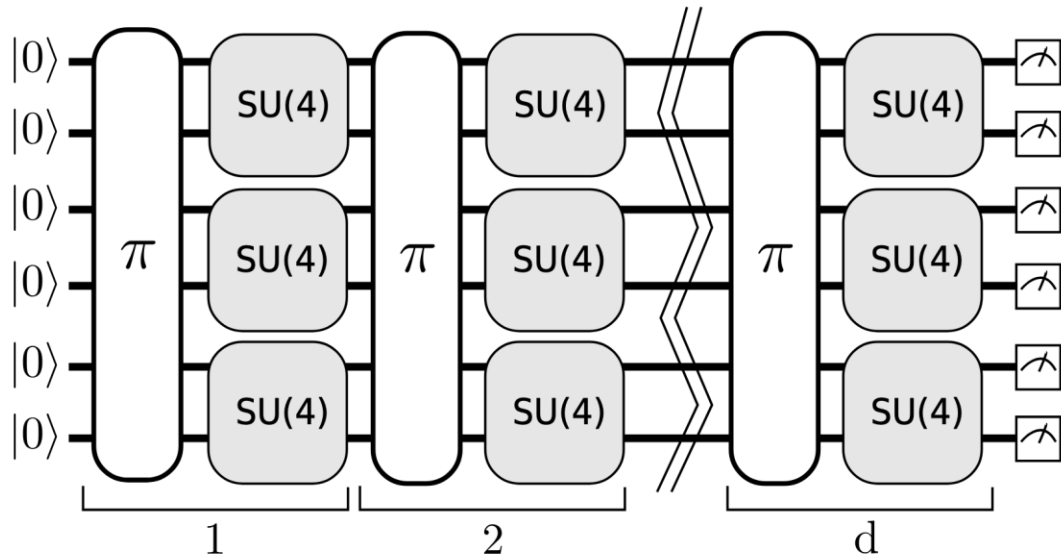


More than 85% of observables within 10% of ideal value at 5k scale

# Quantum Volume (QV)

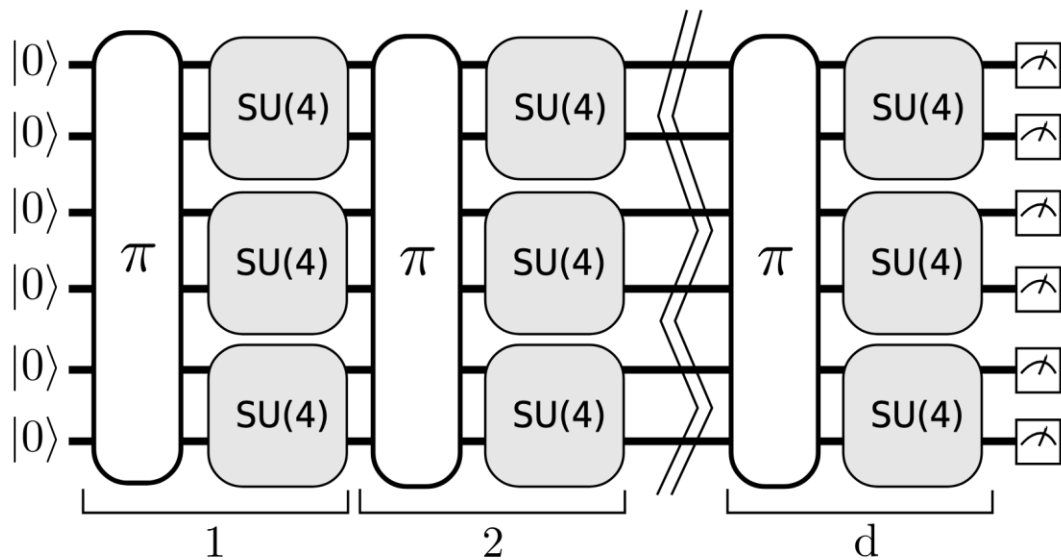
- Holistic metric (quality)
- Indicates how faithfully a “square” quantum circuit of depth  $d$  can be implemented
- Sensitive to coherence, gate fidelity, and measurement fidelity





1)

Define a QV circuit consisting of  $d$  layers (random permutations of the qubit labels followed by 2Q gates)

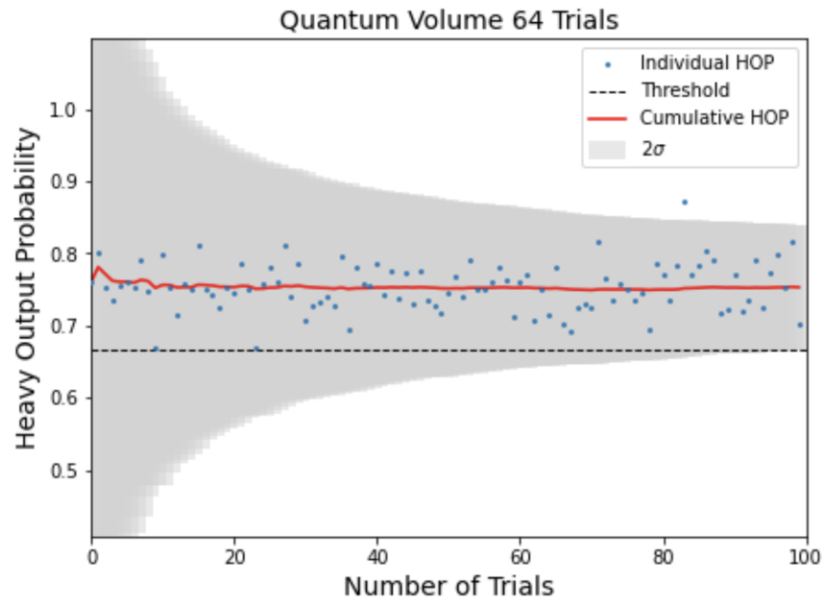
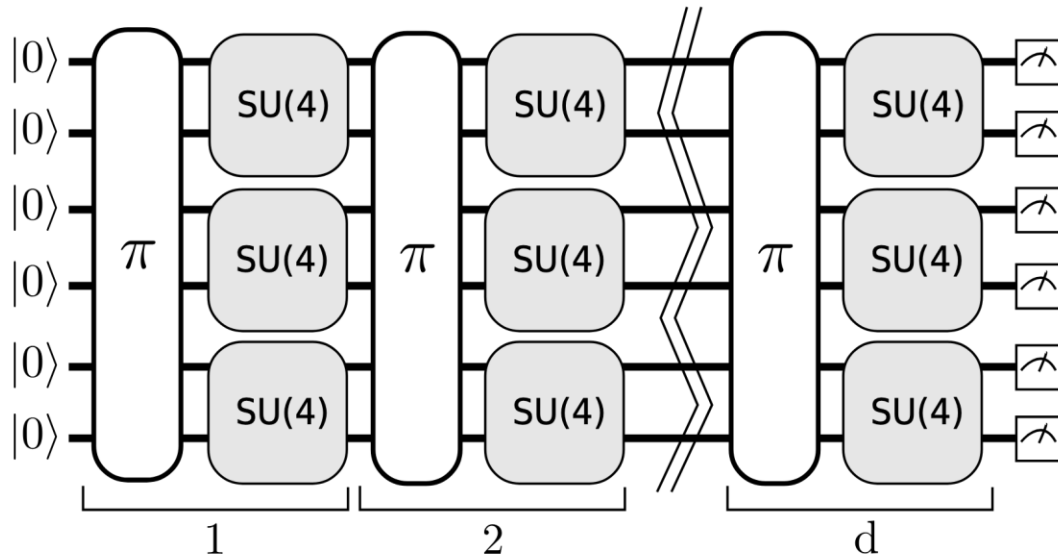


1)

Define a QV circuit consisting of  $d$  layers (random permutations of the qubit labels followed by 2Q gates)

2)

Simulate ideal circuit results



1)

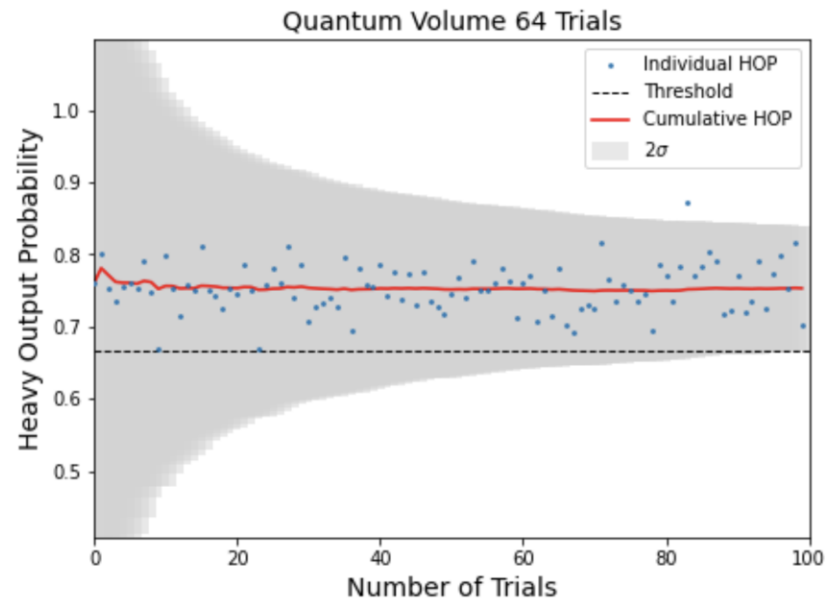
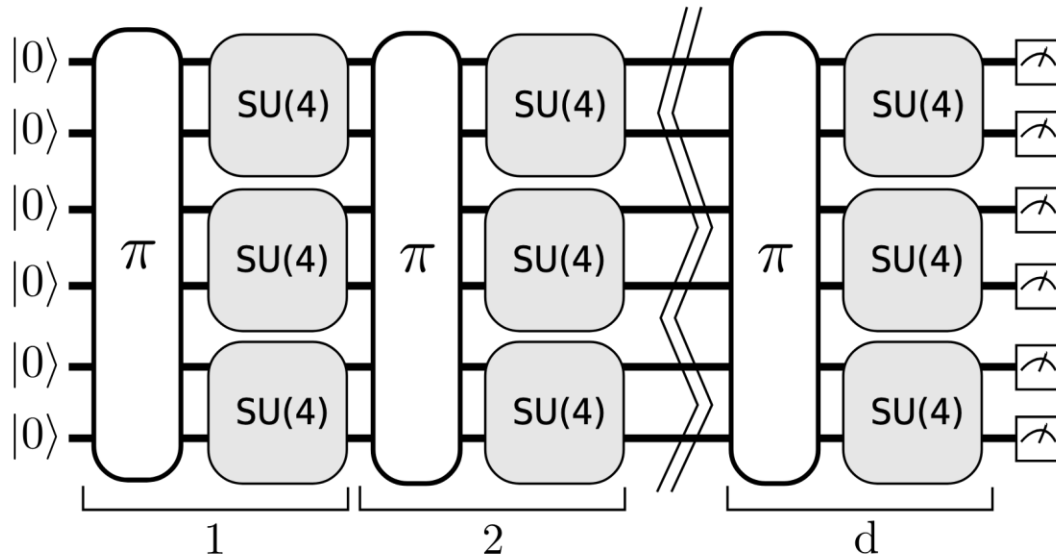
Define a QV circuit consisting of  $d$  layers (random permutations of the qubit labels followed by 2Q gates)

2)

Simulate ideal circuit results

3)

Run the QV circuit and compare the heavy output states with the ideal simulation results



1)

Define a QV circuit consisting of  $d$  layers (random permutations of the qubit labels followed by 2Q gates)

2)

Simulate ideal circuit results

3)

Run the QV circuit and compare the heavy output states with the ideal simulation results

4)

The largest QV circuit of depth  $d$  that produces more than  $2/3$  of heavy outputs determines the QV on a system  $\rightarrow 2^d$

# Some points to consider regarding QV

(stay tuned for Layer Fidelity, another holistic benchmark that addresses these points)

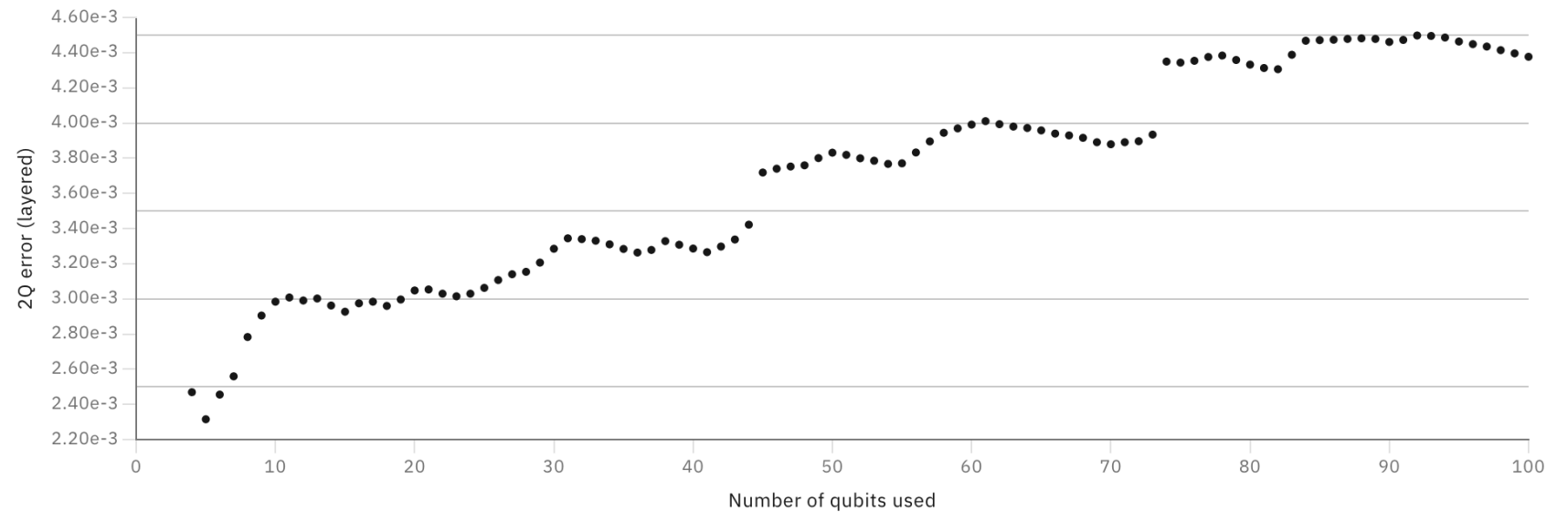
- Is a discrete pass / fail test
- 

- Does not provide individual gate information
- 

- For devices with more qubits than  $\log_2(QV)$ , QV is not the best representative number of overall quality

# Layer Fidelity (LF)

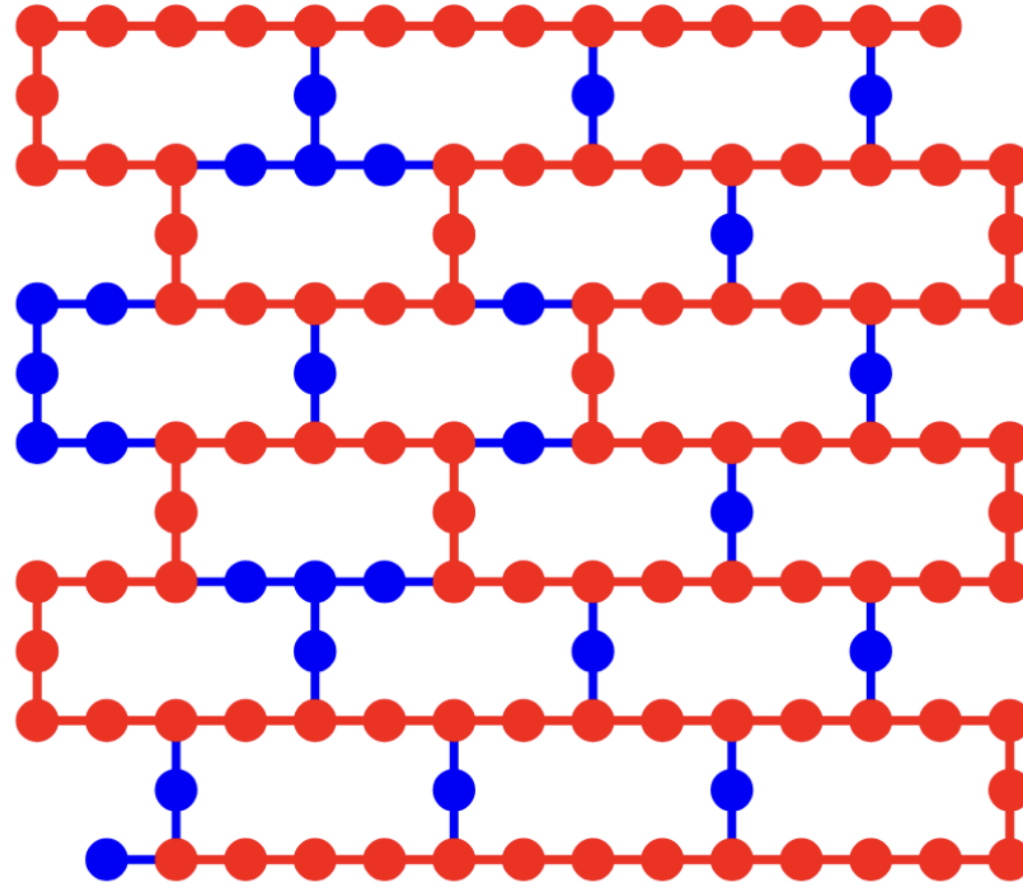
- Holistic metric (quality)
- Great complement to QV
- Captures fidelity of **N fully-connected qubits over M layers**
- Insensitive to state preparation and measurement errors





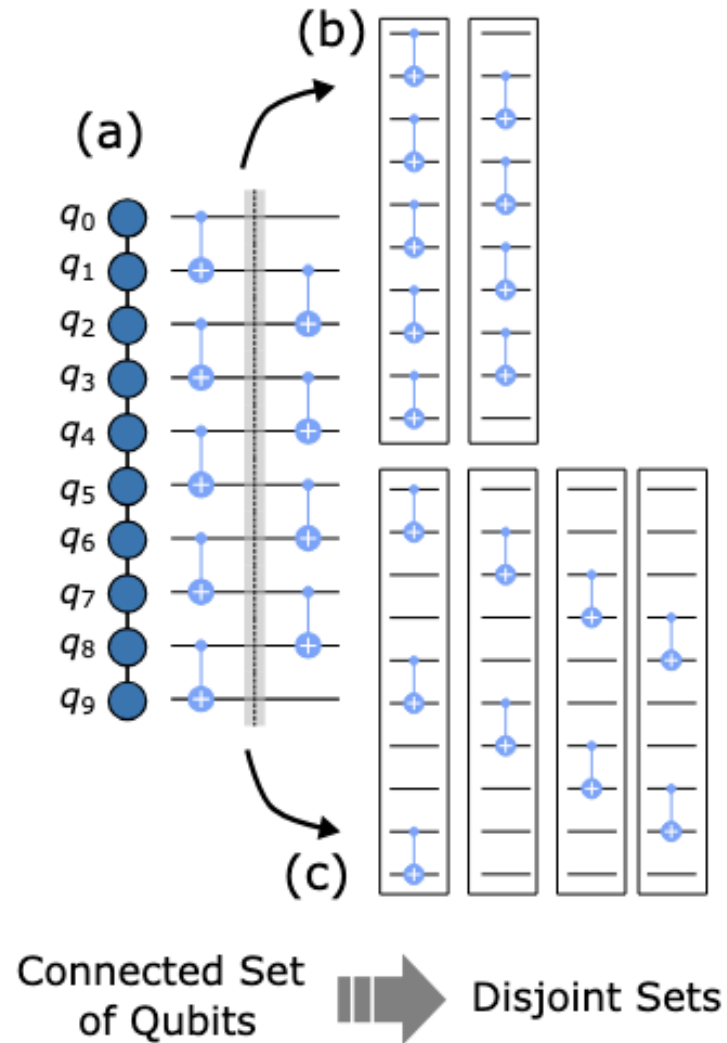
# Layer Fidelity (LF)

- Size of N is flexible
- N can be closer to the device size → captures device wide performance



# Layer Fidelity (LF)

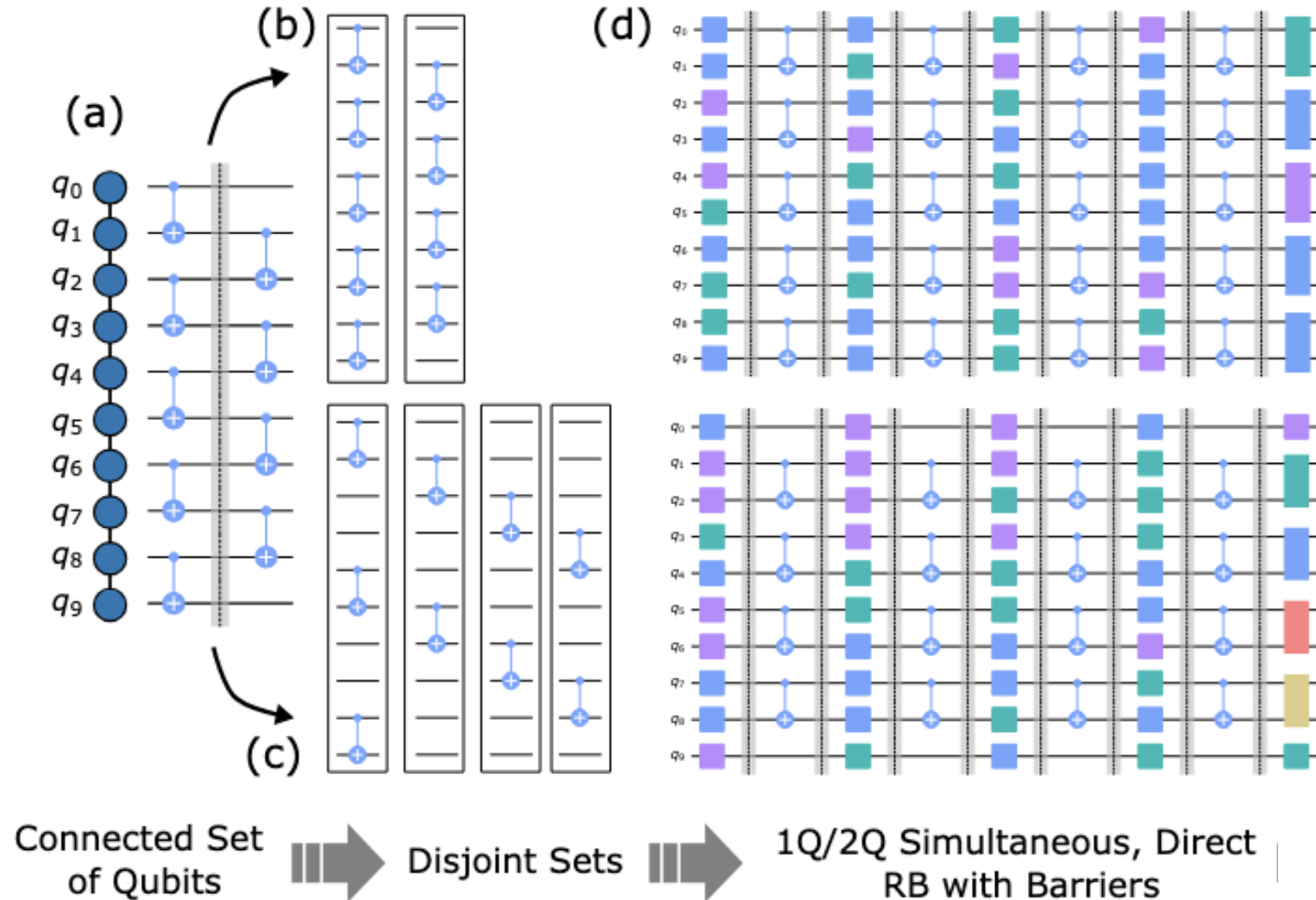
- Partition a set of qubits into  $M$  disjoint layers ( $M=2$  for a linear chain)



# Layer Fidelity (LF)

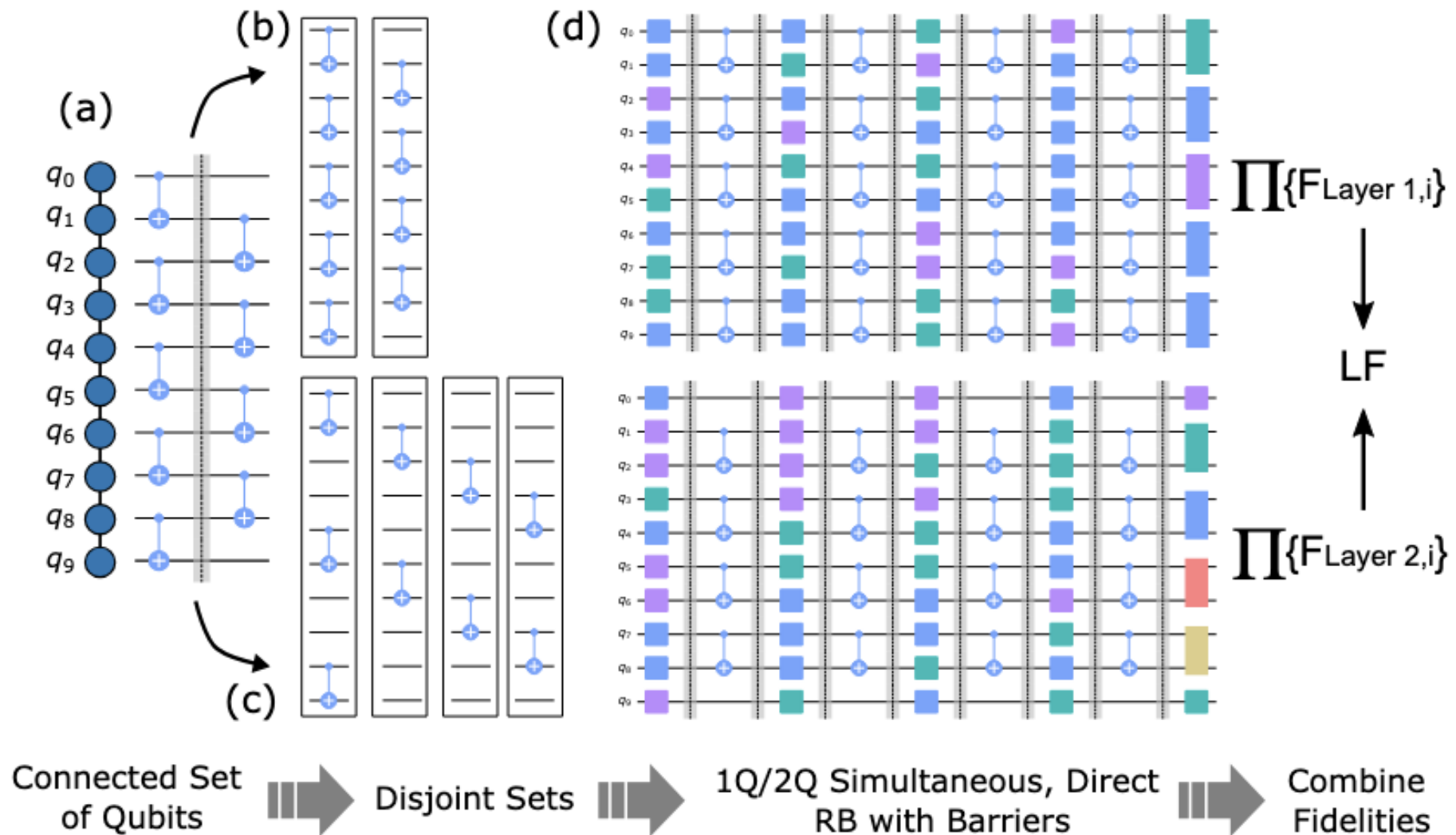
On the disjoint layers:

- Run layers of simultaneous direct RB (imposing a timing barrier between 2Q operations, and twirling through random 1Q Clifford layers)
- Captures crosstalk



# Layer Fidelity (LF)

- Get individual process fidelities and multiply them to get the overall layer fidelity

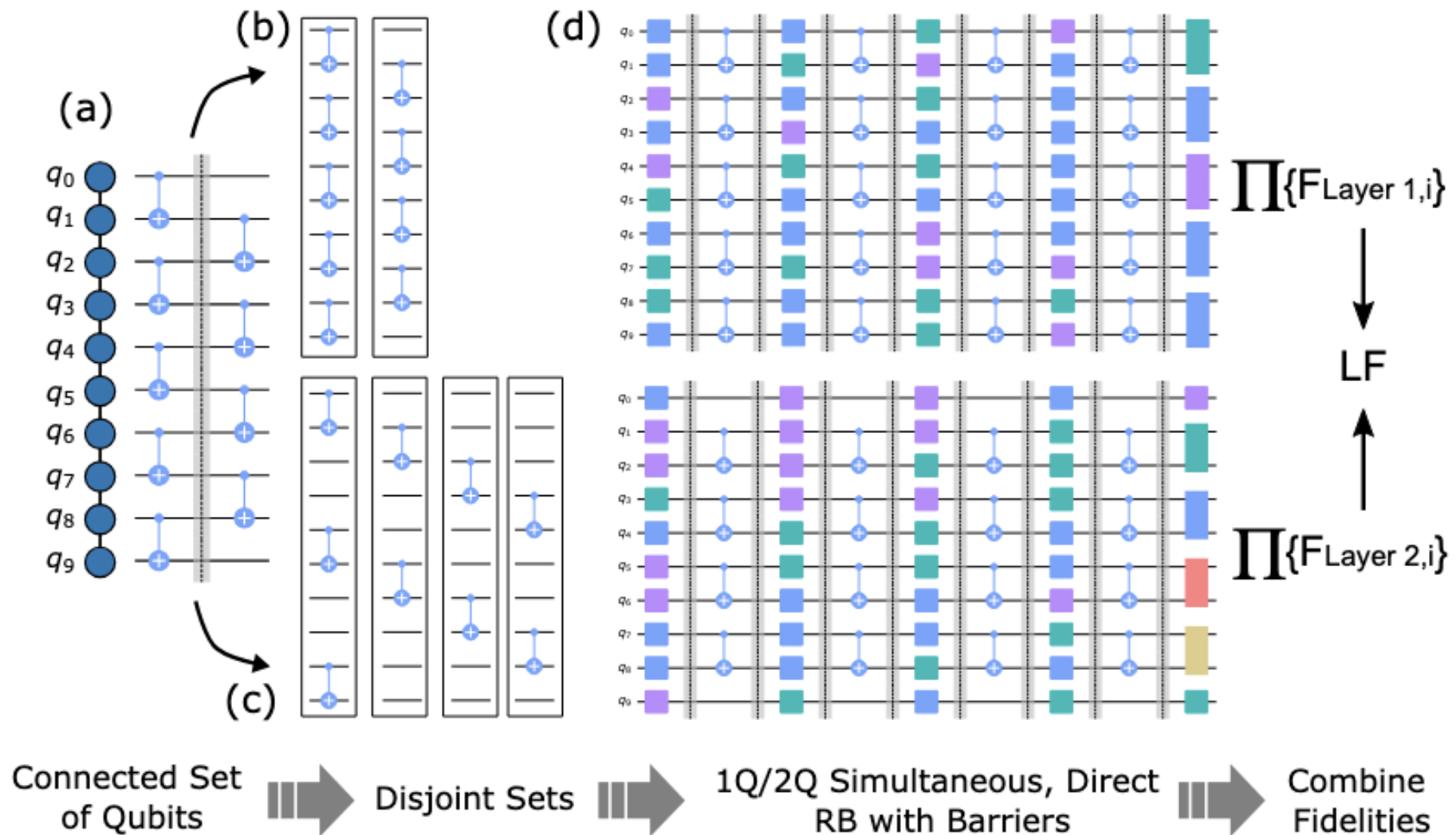


# Layer Fidelity (LF)

$$LF_m = \prod_j F_{j,m},$$

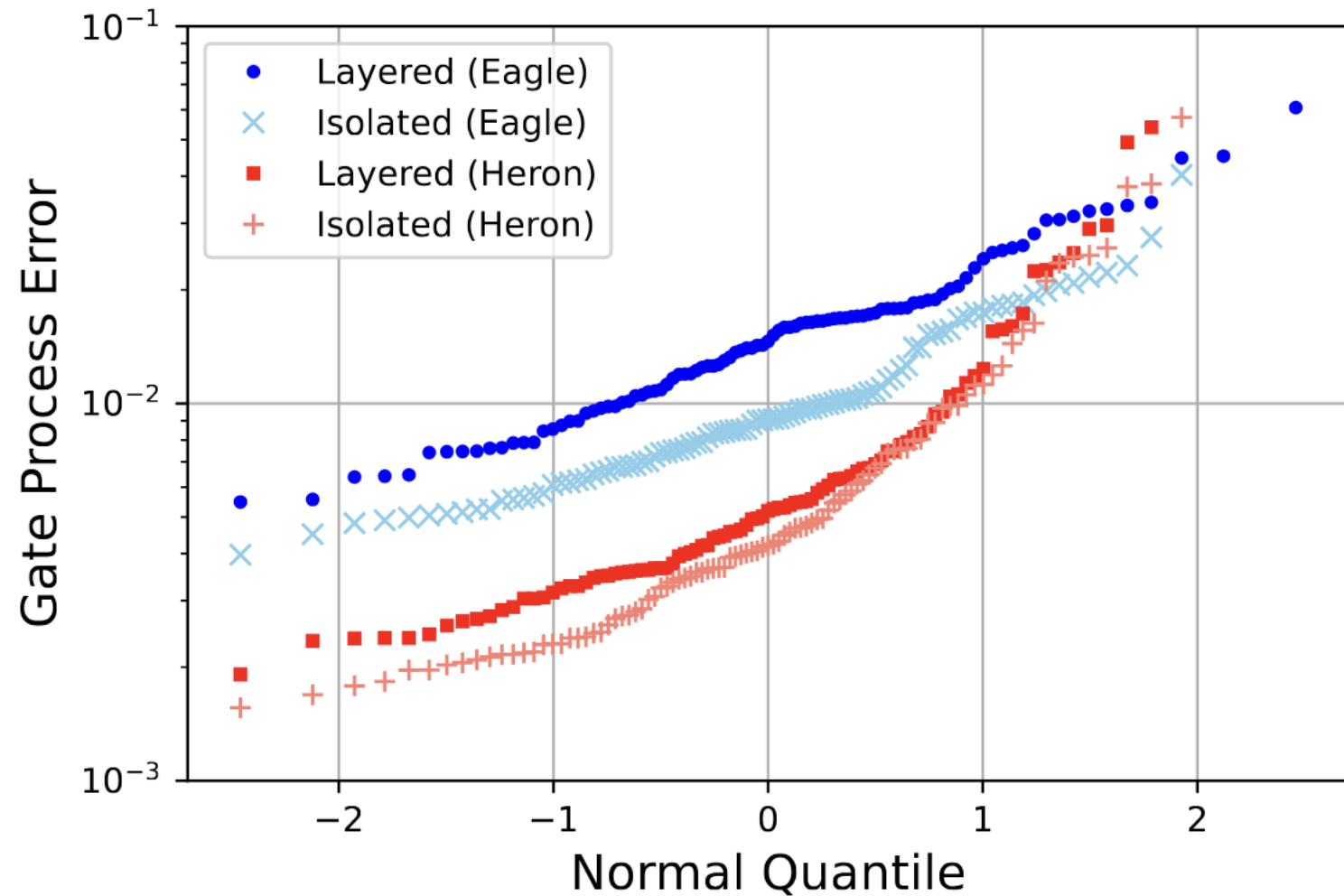
$$LF = \prod_m LF_m.$$

$$\text{EPLG} = 1 - LF^{1/n_{2q}},$$



# Layer Fidelity (LF)

- Error distributions between isolated and layered errors are closer on Herons (virtually eliminates crosstalk)



# Why use Layer Fidelity?

- Is a discrete pass / fail test
  - Introduces a size-independent quantity 'Error per Layered Gate' (EPLG)
- 
-

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  - Provides individual gate errors
-



# Why use Layer Fidelity?

- Is a discrete pass / fail test
  - Introduces a size-independent quantity 'Error per Layered Gate' (EPLG)
- 
- Does not provide individual gate information
  - Provides individual gate errors
- 
- For devices with more qubits than  $\log_2(QV)$ , QV is not the best representative number of overall quality
  - Can span across an entire device via layered circuits

# Layer Fidelity (LF)

- Typical LF for IBM Heron processors

ibm\_marrakesh



QPU status ● Online  
Processor type Heron r2

Qubits	2Q error (best/layered)	CLOPS
156	1.48e-3/4.38e-3	195K

ibm\_fez

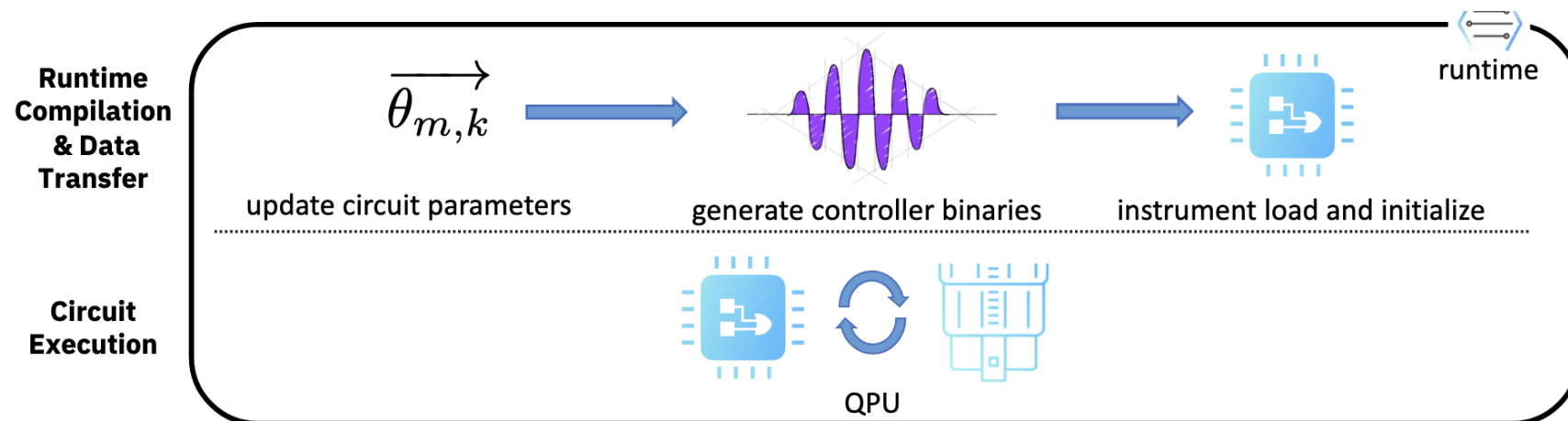


QPU status ● Online  
Processor type Heron r2

Qubits	2Q error (best/layered)	CLOPS
156	2.27e-3/5.25e-3	195K

# Circuit Layer Operations per Second (CLOPS)

- Holistic metric (speed)
- Measures how many layers can be executed per unit of time



# Circuit Layer Operations per Second (CLOPS)

Time break down:

## 1

Time spent  
running the  
circuit: **circuit  
execution**

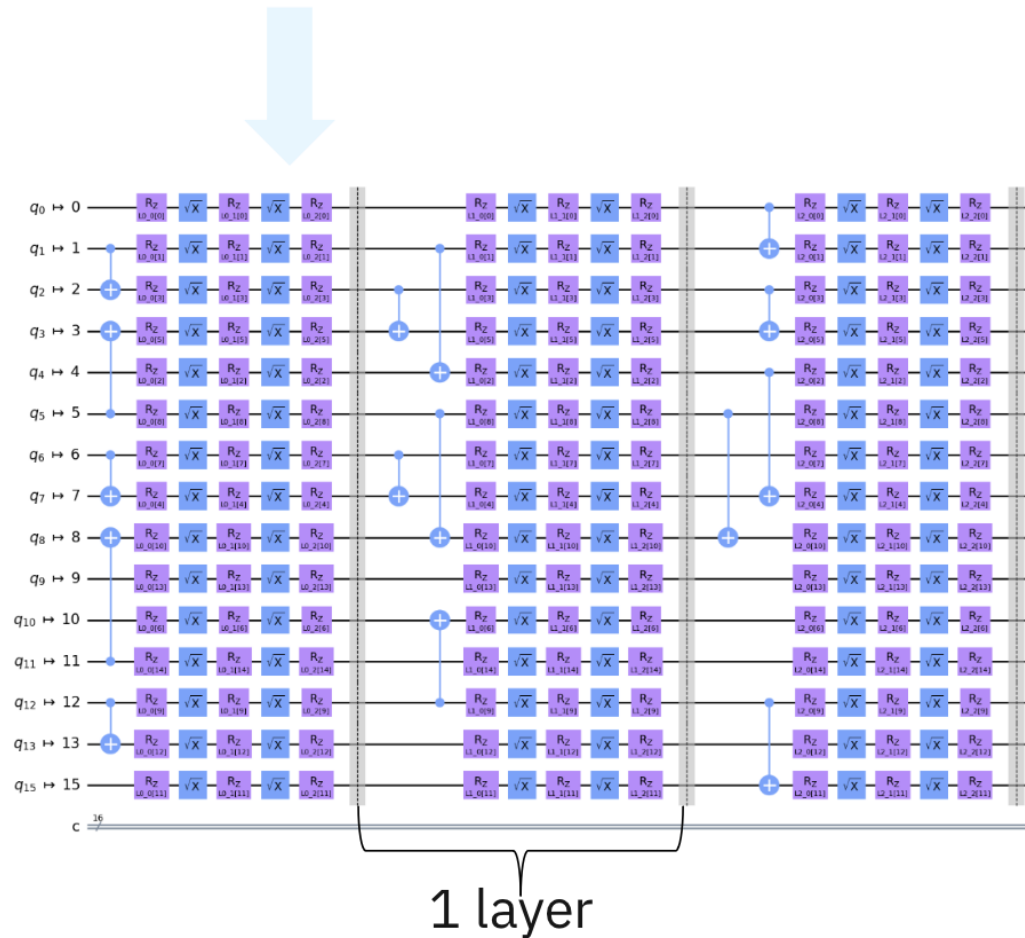
## 2

Delay time  
between each  
shot of each  
circuit: **circuit  
delay**

## 3

Time spent on  
preparing the  
circuits (parameter  
updates, run-time  
compilation,  
waveform  
generation) as well  
as data transfers  
(circuit submission  
to the backend,  
instrument  
initialization,  
instrument load,  
return of results to  
user) : **run-time  
compilation and  
data transfer**

## Parameterized single qubit gates

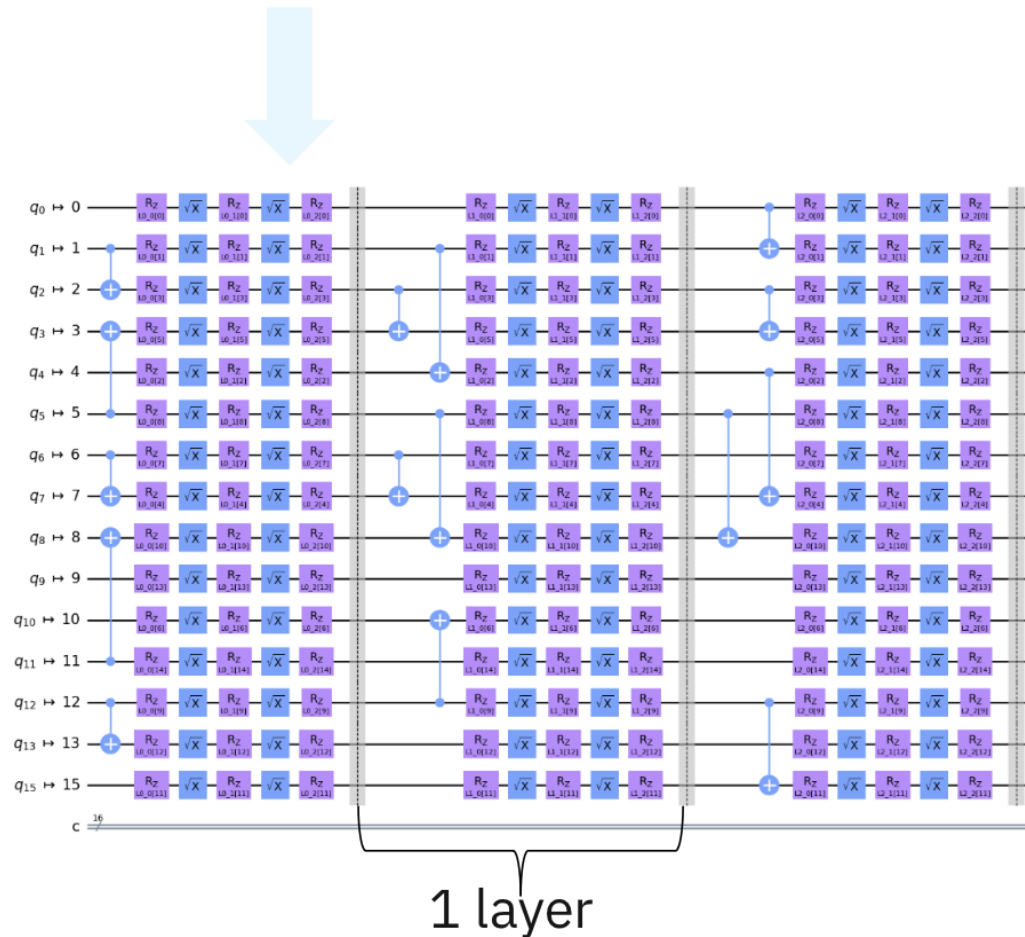


1)

CLOPS measures multiple executions of parametrized layers

The goal is to show that the software and hardware can execute utility scale circuits efficiently

## Parameterized single qubit gates



1)

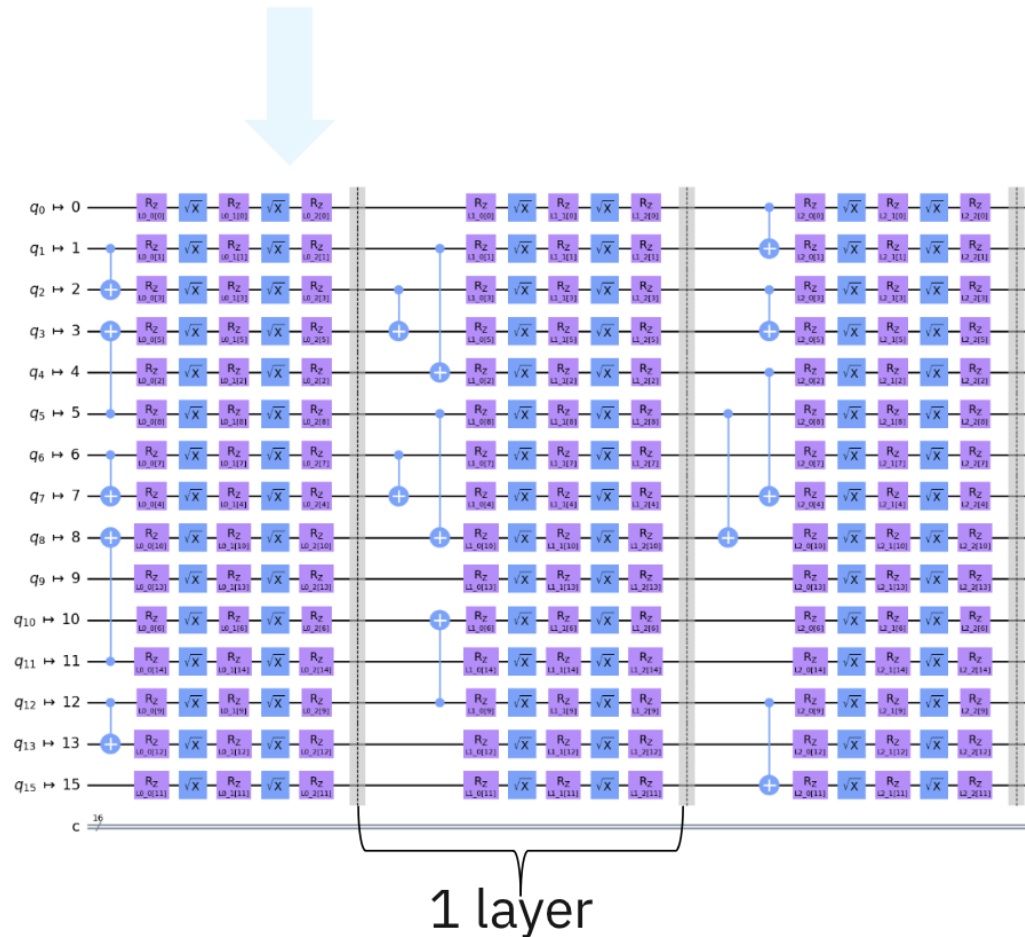
CLOPS measures multiple executions of parametrized layers

The goal is to show that the software and hardware can execute utility scale circuits efficiently

2)

CLOPS can be measured on any circuit size (width/layers). The default is 100x100.

## Parameterized single qubit gates



1)

CLOPS measures multiple executions of parametrized layers

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CLOPS can be measured on any circuit size (width/layers). The default is 100x100.

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Layers consist of 2Q gates that are executed in parallel, and fully parametrized single qubit rotations on all qubits



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CLOPS can be measured on any circuit size (width/layers). The default is 100x100.

Layers consist of 2Q gates that are executed in parallel, and fully parametrized single qubit rotations on all qubits

CLOPS = the number of  
layers executed per second



# Circuit Layer Operations per Second (CLOPS)

- Typical CLOPS for IBM Heron processors

ibm\_**torino**

QPU status ● Online  
Processor type Heron r1



Qubits	2Q error (best/layered)
133	1.63e-3/6.09e-3

CLOPS
210K

ibm\_**fez**

QPU status ● Online  
Processor type Heron r2



Qubits	2Q error (best/layered)
156	2.27e-3/5.25e-3

CLOPS
195K

# Notebooks and resources

- [GitHub repo: qiskit-device-benchmarking](https://github.com/qiskit-community/qiskit-device-benchmarking)  
<https://github.com/qiskit-community/qiskit-device-benchmarking>
- [Layer Fidelity Notebook](https://github.com/qiskit-community/qiskit-device-benchmarking/blob/main/notebooks/layer_fidelity_single_chain.ipynb)  
[https://github.com/qiskit-community/qiskit-device-benchmarking/blob/main/notebooks/layer\\_fidelity\\_single\\_chain.ipynb](https://github.com/qiskit-community/qiskit-device-benchmarking/blob/main/notebooks/layer_fidelity_single_chain.ipynb)
- [CLOPS Notebook](https://github.com/qiskit-community/qiskit-device-benchmarking/tree/main/qiskit_device_benchmarking/clops)  
[https://github.com/qiskit-community/qiskit-device-benchmarking/tree/main/qiskit\\_device\\_benchmarking/clops](https://github.com/qiskit-community/qiskit-device-benchmarking/tree/main/qiskit_device_benchmarking/clops)
- [Mirror Circuit Notebook](https://github.com/qiskit-community/qiskit-device-benchmarking/tree/main/qiskit_device_benchmarking/mirror_test)  
[https://github.com/qiskit-community/qiskit-device-benchmarking/tree/main/qiskit\\_device\\_benchmarking/mirror\\_test](https://github.com/qiskit-community/qiskit-device-benchmarking/tree/main/qiskit_device_benchmarking/mirror_test)
- [Bell State and Identity Tomography](https://github.com/qiskit-community/qiskit-device-benchmarking/blob/main/notebooks/bell_state_tomography.ipynb)  
[https://github.com/qiskit-community/qiskit-device-benchmarking/blob/main/notebooks/bell\\_state\\_tomography.ipynb](https://github.com/qiskit-community/qiskit-device-benchmarking/blob/main/notebooks/bell_state_tomography.ipynb)
- [Quantum Volume Notebook](https://github.com/mjlp123/qiskit-device-benchmarking/blob/majo_qv/notebooks/quantum_volume.ipynb)  
[https://github.com/mjlp123/qiskit-device-benchmarking/blob/majo\\_qv/notebooks/quantum\\_volume.ipynb](https://github.com/mjlp123/qiskit-device-benchmarking/blob/majo_qv/notebooks/quantum_volume.ipynb)

Plot LF and EPLG per chain length

In [14]:

```
lfu.make_lf_eplg_plots(backend=backend,  
exp_data=exp_data,  
chain=qchain,  
machine=machine  
)
```

