

TMC-104_ Unit-1
Assignment-1

1. Show that “less than and equal to” is a partial ordering relation on the set of integers.
2. If $f: \mathbb{R}^+ \rightarrow \mathbb{R}^+$ and $g: \mathbb{R}^+ \rightarrow \mathbb{R}^+$ be functions defined by $f(x) = \sqrt{x}$ and $g(x) = 3x + 1 \ \forall x \in \mathbb{R}^+$. Find gof and fog .
3. If $(x) = x^2$, $g(x) = x + 1$ and $h(x) = x - 1$ are the functions, then find $gofoh$ and $fogoh$.
4. Show that if R is an equivalence relation on set A , then R^{-1} is also an equivalence relation on set A .
5. If A & B are any two sets then $A-B = A \Leftrightarrow A \cap B = \emptyset$.
6. Out of 450 students in a school, 193 students read science, 200 student read Commerce, 80 students read neither. Find out how many read both.
7. Let $A = \{1,2,3,4\}$ & $R = \{(1,1), (1,2), (2,1), (2,2), (2,3), (2,4), (3,4), (4,1), (4,3)\}$ then construct diagraph and matrix of the relation. Find its transitive closure by using Warshall's Algorithm.
8. Let $A = \{2,3,4,6,12,36,48\}$ be a nonempty set and R bet the Poset of divisibility defined on A that is if $a, b \in A$ then a divides b . Draw Hasse diagram.
9. Let $f: \mathbb{R} \rightarrow \mathbb{R}$ and $g: \mathbb{R} \rightarrow \mathbb{R}$ where \mathbb{R} is the set of real no. find fog and gof , where $f(x) = x^2$ and $g(x) = x + 4$ state wheather these functions are injective, surjective and bijective.
10. Show that the function $f: \mathbb{Q} \rightarrow \mathbb{Q}$ s.t. $f(x) = 3x + 4$ is invertible and find its inverse.
11. Show that the $f(x,y) = x^y$ is a primitive recursive function
12. Construct the divides relation on each of the sets $S = \{1,2,3,4,6,9\}$ and draw Hasse diagram for each relation and find (a) All maximal and minimal elements (b) Greatest and least elements.
13. If a mapping $f: A \rightarrow B$ is one-one and onto then f^{-1} is also one-one and onto.
14. Prove that $[0,1]$ is not countable.
15. If R be a relation in the set of integers \mathbb{Z} defined by
 $R = \{(x, y): x \in \mathbb{Z}, y \in \mathbb{Z}, x - y \text{ is divisible by } 3\}$.
Then prove that R is an equivalence relation