

# Recursion [Day 8]

10 September 2024 19:03

## Recursion - [Day 8]

Generate n-th Fibonacci Number using Recursion.

0 1 1 2 3 5 8 13 21 34

$$\text{Fib}(0) = 0, \text{Fib}(1) = 1$$

$$\text{Fib}(n) = \text{Fib}(n-1) + \text{Fib}(n-2)$$

$$\text{Fib}(9) = \text{Fib}(8) + \text{Fib}(7) = 21 + 13 = 34$$

$$\text{Fib}(8) = \text{Fib}(7) + \text{Fib}(6) = 13 + 8 = 21$$

$$\text{Fib}(7) = \text{Fib}(6) + \text{Fib}(5) = 8 + 5 = 13$$

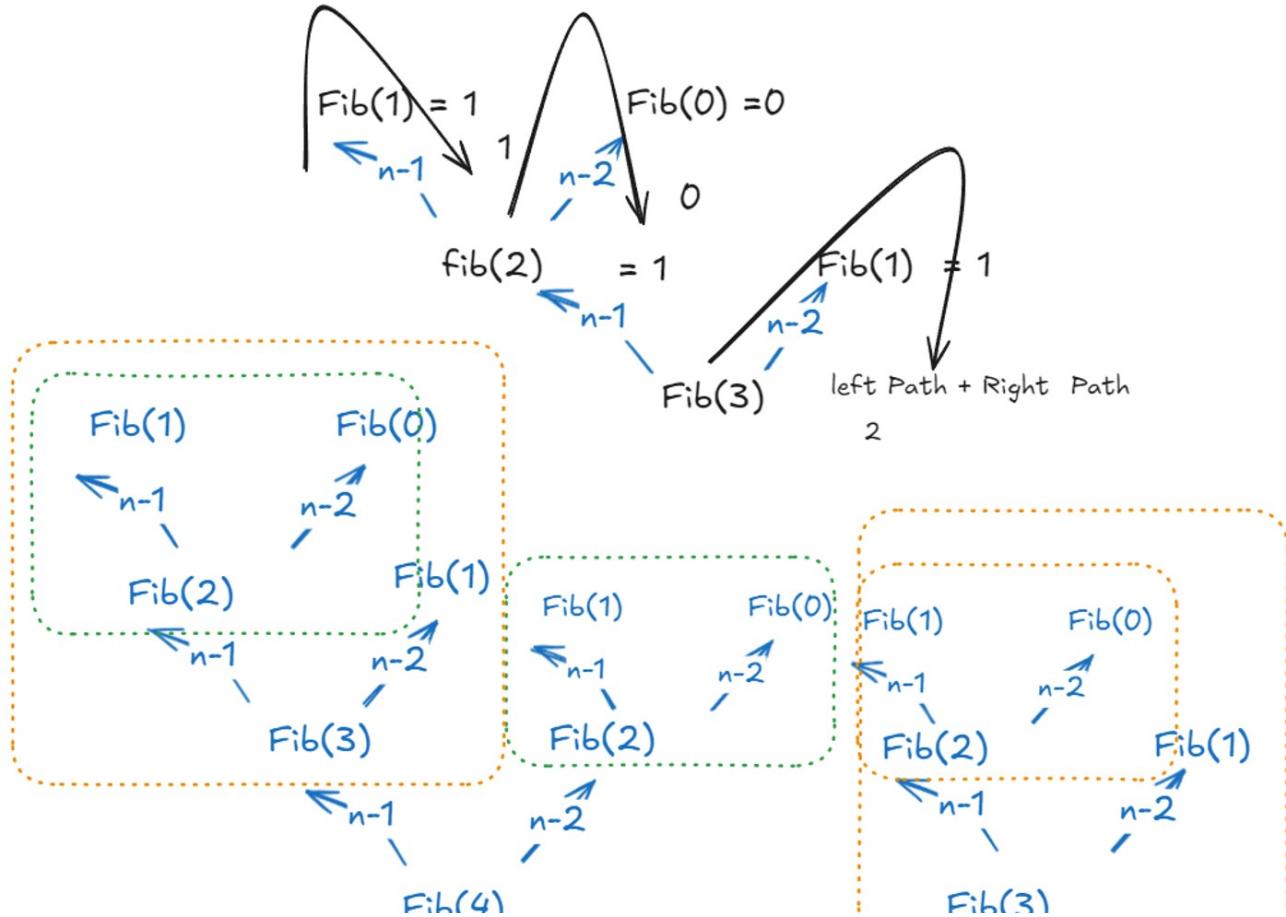
$$\text{Fib}(6) = \text{Fib}(5) + \text{Fib}(4) = 5 + 3 = 8$$

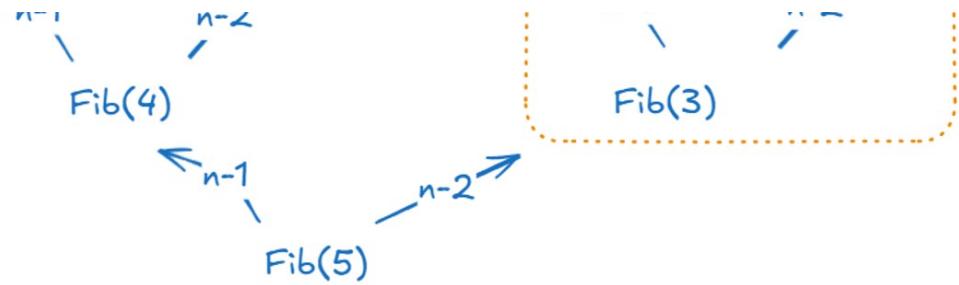
$$\text{Fib}(5) = \text{Fib}(4) + \text{Fib}(3) = 3 + 2 = 5$$

$$\text{Fib}(4) = \text{Fib}(3) + \text{Fib}(2) = 2 + 1 = 3$$

$$\text{Fib}(3) = \text{Fib}(2) + \text{Fib}(1) = 1 + 1 = 2$$

$$\text{Fib}(2) = \text{Fib}(1) + \text{Fib}(0) = 0 + 1 = 1$$





```

import java.util.Scanner;
public class Fibonacci {
    public static int fibonacci(int num){
        if(num == 0){
            return 0;
        }else if(num == 1){
            return 1;
        }else{
            return fibonacci(num - 1) + fibonacci(num - 2);
        }
    }

    public static void main(String[] args) {
        Scanner scn = new Scanner(System.in);
        System.out.println("Enter the non-negative Integers : ");
        int num = scn.nextInt();
        int result = fibonacci(num);
        System.out.println(result);
    }
}

```

### Problem Statement

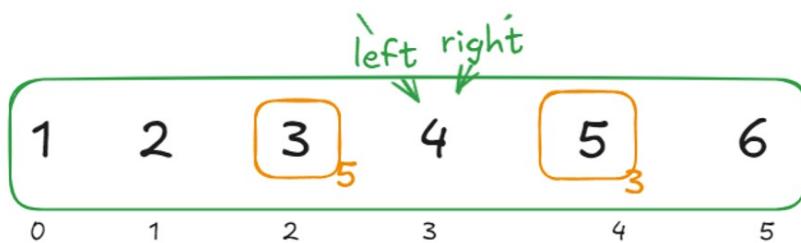
**Problem:** Reverse a Subarray

Given an array and two indices, `left` and `right`, reverse the elements of the array between these indices (inclusive).

### Example

**Example 1:**

- **Input:**
  - Array: `[1, 2, 3, 4, 5, 6]`
  - Left index: `2`
  - Right index: `4`
- **Output:**
  - Array after reversing the subarray from index `2` to `4`: `[1, 2, 5, 4, 3, 6]`



```
while(left >= right){}
```

```
while(left >= right){  
    return;  
}
```

Base Condition.

```
Swap the value ;  
reverseSubarray(arr , left++ , right--);
```

```
Main(){  
    reverseSubarray(arr , left , right)  
}
```

```
import java.util.Arrays;  
import java.util.Scanner;  
public class ReverseSubarray {  
    public static void reverseSubarray(int[] arr, int left , int right){  
        if(left >= right){  
            return;  
        }  
        int temp = arr[left];  
        arr[left] = arr[right];  
        arr[right] = temp;  
  
        reverseSubarray(arr, left + 1, right - 1);  
    }  
    public static void main(String[] args) {  
        Scanner scn = new Scanner(System.in);  
        System.out.println("Enter the size of an array");  
        int n = scn.nextInt();  
  
        int[] arr = new int[n];  
        System.out.println("Enter the elements of the array");  
        for(int i =0 ; i<n; i++){  
            arr[i] = scn.nextInt();  
        }  
        System.out.println("Enter the Left Index : ");  
        int left = scn.nextInt();  
        System.out.println("Enter the Right Index : ");  
        int right = scn.nextInt();  
  
        if(left < 0 || right >=n || left > right){  
            System.out.println("Invalid Indices");  
        }else{  
            reverseSubarray(arr , left , right);  
            System.out.println("After Reversing the subarray");  
            System.out.println(Arrays.toString(arr));  
        }  
    }  
}
```

```
Enter the size of an array  
6  
Enter the elements of the array  
1  
2  
3
```

```

Enter the elements of the array
1
2
3
4
5
6
Enter the Left Index :
2
Enter the Right Index :
4
After Reversing the subarray
[1, 2, 5, 4, 3, 6]

```

## Problem Statement

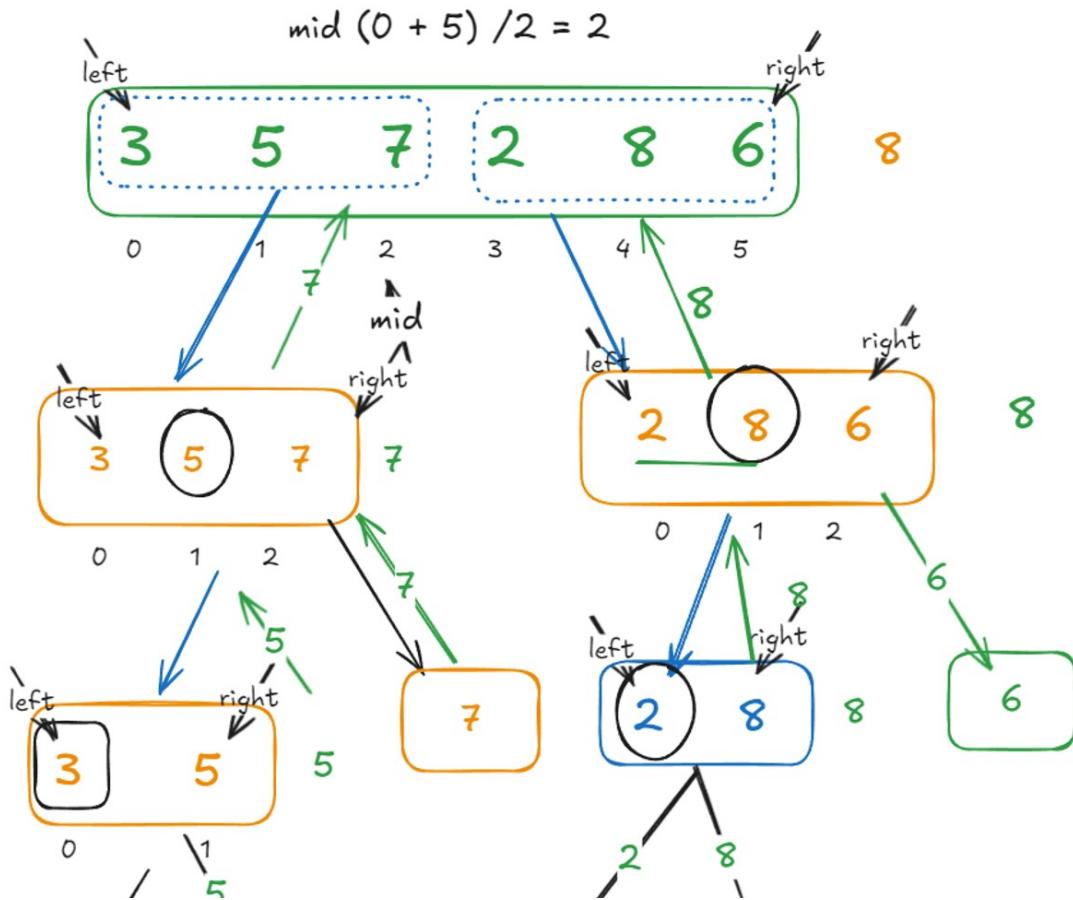
**Problem:** Find the Maximum Element in an Array

Given an array of integers, find the maximum element in the array using recursion.

### Example

**Example 1:**

- **Input:**
  - Array: `[3, 5, 7, 2, 8, 6]`
- **Output:**
  - Maximum Element: `8`





```

import java.util.Scanner;
public class MaxElementRecursion {

    public static int FindMax(int[] arr , int left , int right){
        if(left == right){
            return arr[left]; // or arr[right] both are pointing to same value.
        }
        int mid = (left + right) /2;
        int leftMax = FindMax(arr, left , mid);
        int rightMax = FindMax(arr, mid + 1, right);
        return Math.max(leftMax, rightMax);
    }

    public static void main(String[] args) {
        Scanner scn = new Scanner(System.in);
        System.out.println("Enter the size of an array : ");
        int n = scn.nextInt();

        int[] arr = new int[n];
        System.out.println("Enter the elements of an array:");
        for(int i = 0 ; i< n; i++){
            arr[i] = scn.nextInt();
        }

        int max = FindMax(arr , 0 , n -1);
        System.out.println("The maximum element of an array is : " + max);
    }
}

```

```

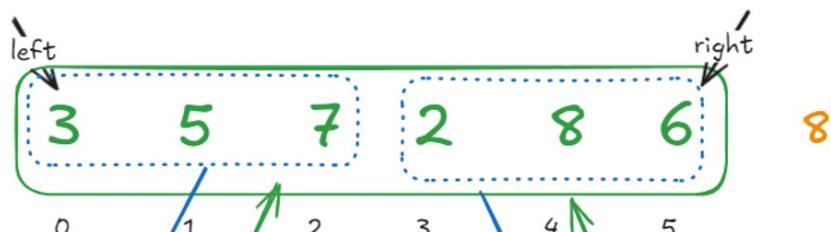
MAXELEMENTRECURSION
Enter the size of an array :
6
Enter the elements of an array:
4
5
7
1
9
3
The maximum element of an array is : 9
PS C:\Users\Nishant\VSCode\Java\DSA>

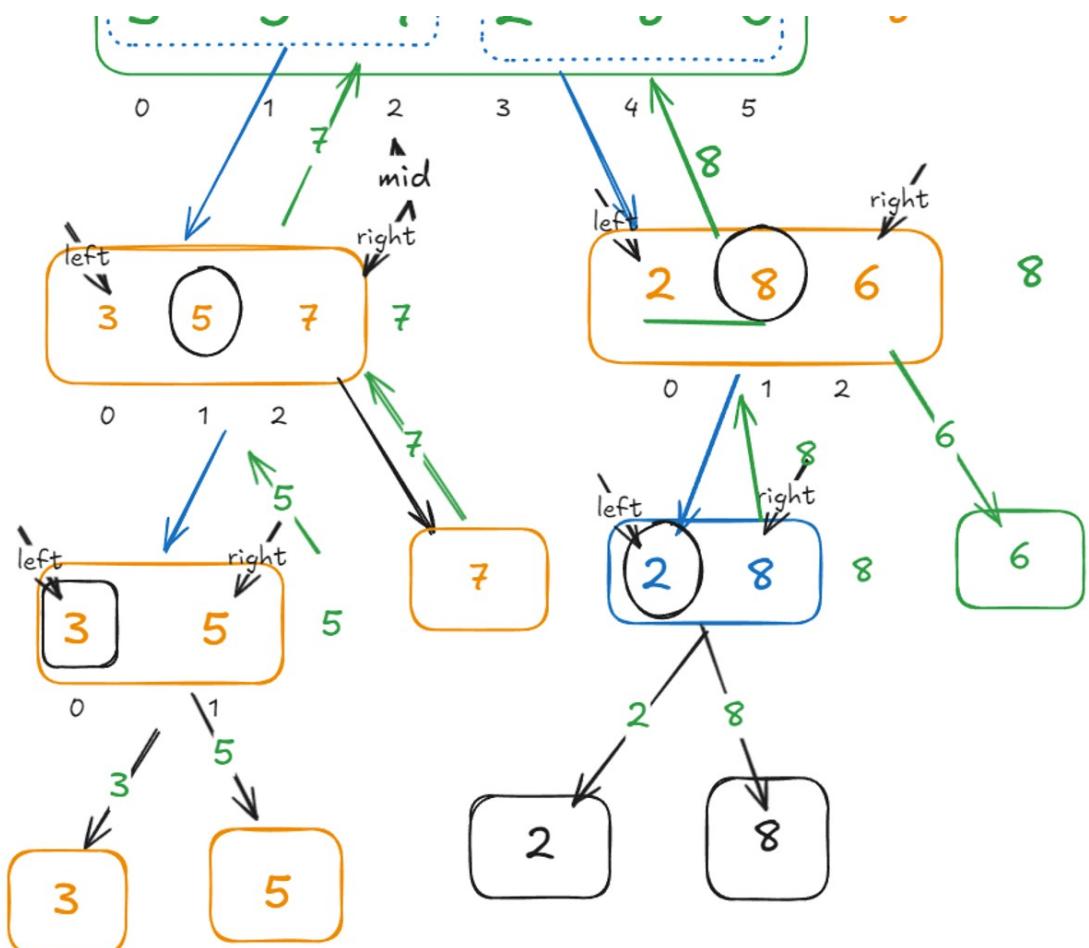
```

```

if(left == right){
    return arr[left]; // or arr[right] both are
}
int mid = (left + right) /2;
int leftMax = FindMax(arr, left , mid);
int rightMax = FindMax(arr, mid + 1, right);
return Math.max(leftMax, rightMax);

```





## Problem Statement

**Problem:** Print the string "ALGOTUTOR" using recursion.

A  
L  
G  
O  
T  
U  
T  
O  
R

```
public class PrintingAlgoTutor {
    public static void printString(String str , int index){
        if(index == str.length()){
            return;
        }
        System.out.println(str.charAt(index));
        printString(str, index + 1);
    }
    public static void main(String[] args) {
        String str = "ALGOTUTOR";
        printString(str , 0);
    }
}
```

```

        printString(str , 0);
    }
}

```

---

**Problem Statement:**

Write a recursive function to calculate the power of a number in a linear manner. Given two integers  $x$  (the base) and  $n$  (the exponent), you need to compute  $x^n$  using recursion.

**Input:**

$x = 2, n = 5$

**Output:**

32

**Explanation:**

$$2^5 = 2 * 2 * 2 * 2 * 2 = 32$$

$$2^5 = 2 * 2^4.$$

$$2^4 = 2 * 2^3.$$

$$2^3 = 2 * 2^2.$$

$$2^2 = 2 * 2^1$$

$$2^1 = 2 * 2^0$$

$[x^n, n == 0 \text{ return } 1]$

```

import java.util.Scanner;
public class PowerLinear {

    public static int power(int x , int n){
        if(n ==0){
            return 1;
        }
        int result = power(x, n-1);
        return x * result;
    }

    public static void main(String[] args) {
        Scanner scn = new Scanner(System.in);
        System.out.println("Enter the base (x) : ");
        int x = scn.nextInt();
        System.out.println("Enter the exponent (n) : ");
        int n = scn.nextInt();

        int result = power(x , n);
        System.out.println( x + " ^ " + n + " = " + result);
    }
}

```

```

C:\Users\Asus>javac PowerLinear.java
C:\Users\Asus>java PowerLinear
Enter the base (x) :
2
Enter the exponent (n) :
5
2 ^ 5 = 32

```

---

**Problem Statement:**

Write a recursive function to calculate the power of a number in a logarithmic manner. Given two integers  $x$  (the base) and  $n$  (the exponent), compute  $x^n$  using recursion, optimizing the solution to have logarithmic time complexity.

Write a recursive function to calculate the power of a number in a logarithmic manner. Given two integers  $x$  (the base) and  $n$  (the exponent), compute  $x^n$  using recursion, optimizing the solution to have logarithmic time complexity.

**Input:**  
 $x = 2, n = 5$

**Output:**

32

**Explanation:**

$2^5 = 32$

$$x^n = x^{(n-1)} * x^{(n-2)}$$

$$x^n = x^{n/2} * x^{n/2} \text{ - even}$$

$$x^n = (x^{n/2} * x^{n/2}) * x \text{ [odd]}$$

$$2^5 = (2^2 * 2^2) * 2 = 16 * 2 = 32$$

$$2^4 = 2^2 * 2^2 = 4 * 4 = 16$$

```
import java.util.Scanner;
public class PowerLogarithmic {
    public static int power(int x, int n){
        if(n == 0){
            return 1;
        }
        int halfpower = power(x, n/2);
        if(n % 2 == 0){
            return halfpower * halfpower;
        }else{
            return x * halfpower * halfpower;
        }
    }
    public static void main(String[] args){
        Scanner scn = new Scanner(System.in);
        System.out.println("Enter the base (x) : ");
        int x = scn.nextInt();
        System.out.println("Enter the exponent (n) : ");
        int n = scn.nextInt();

        int result = power(x, n);
        System.out.println(x + " ^ " + n + " = " + result);
    }
}
```

```
if(n == 0){
    return 1;
}
int halfpower = power(x, n/2);
if(n % 2 == 0){
    return halfpower * halfpower;
}else{
    return x * halfpower * halfpower;
}
```

$$2^8 = 2^4 * 2^4 = 16 * 16 = 256.$$

$$2^4 = 2^2 * 2^2 = 4 * 4 = 16$$

$$2^2 = 2^1 * 2^1 = 2 * 2 = 4$$

$$\begin{aligned}
 2^4 &= 2^2 * 2^2 = 4 * 4 = 16 \\
 2^2 &= 2^1 * 2^1 = 2 * 2 = 4 \\
 2^1 &= 2 * 2^0 * 2^0 = 2 * 1 * 1 = 2
 \end{aligned}$$

$$2^a * 2^b = 2^{a+b};$$

$$2^4 * 2^3 = 2^{4+3} = 2^7.$$

Completed

Attendance Code: E782F53A

#### Problem Statement:

Write a recursive function that takes an array of integers and prints all its elements, one at a time. The function should print elements starting from the first element to the last element.

**Input:**  
Array = [10, 20, 30, 40, 50]

**Output:**  
10  
20  
30  
40  
50

```

import java.util.Scanner;
public class DisplayArray {

    public static void displayArray(int[] arr , int idx){
        if(idx == arr.length){
            return;
        }

        System.out.println(arr[idx]);
        displayArray(arr, idx+1);
    }

    public static void main(String[] args) {
        Scanner scn = new Scanner(System.in);
        System.out.println("Enter the number of Elements in the array : ");

        int n = scn.nextInt();
        int[] arr = new int[n];
    }
}

```

```

        int n = scn.nextInt();
        int[] arr = new int[n];
        System.out.println("Enter the elements of an array : ");
        for(int i = 0 ; i < n ; i++){
            arr[i] = scn.nextInt();
        }
        System.out.println("Array Elements are : ");
        displayArray(arr, 0);
    }
}

```

**"print the array element in reverse order."**

```

import java.util.Scanner;
public class DisplayArrayReverse {

    public static void displayArrayReverse(int[] arr , int idx){
        if(idx < 0){
            return;
        }

        System.out.println(arr[idx]);
        displayArray(arr, idx - 1);
    }

    public static void main(String[] args) {
        Scanner scn = new Scanner(System.in);
        System.out.println("Enter the number of Elements in the array : ");

        int n = scn.nextInt();
        int[] arr = new int[n];
        System.out.println("Enter the elements of an array : ");
        for(int i = 0 ; i < n ; i++){
            arr[i] = scn.nextInt();
        }
        System.out.println("Array Elements are : ");
        displayArrayReverse(arr , n -1);
    }
}

```