

Recursion + Sub Sequence [Day 9]

11 September 2024 19:37

Recursion + Sub-Sequence + Bit Manipulation [Day 9]

Problem Statement

Problem: Multiply two integers using recursion.

Given two integers `a` and `b`, multiply them using recursion. The solution should not use the multiplication operator `*`.

Example

Example 1:

- Input:

- `a = 3`
 - `b = 4`

- Output:

- `12`

$b = -5$

Example 2:

- Input:

- `a = 7`
 - `b = 5`

- Output:

- `35`

$$a = 4$$

$$b = 5$$

Multiply(a,b)

Multiply(a,-b)

$$a * b = a + (a * b - 1).$$

$$4 * 5 = 4 + (4 * 4) = 4 + 16 = 20$$

$$a * b - 1 = a + (a * (b - 2)) =$$

$$4 * 4 = 4 + (4 * 3) = 4 + 12 = 16$$

if $b == 0$

return 0

$b > 0$

multiply(a, b-1)

mul(a,b)

$b < 0$

-multiply(a, -b)

mul(4,5)

mul(a,-(-5))

-mul(a,b) = mul(4,5)

$$-\text{mul}(a,b) = \text{mul}(4,5)$$

```
import java.util.Scanner;
public class RecursionMultiplication {
    public static int multiply(int a , int b){
        if(b == 0){
            return 0;
        }
        if(b > 0){
            return a + multiply(a, b-1);
        }
        return - multiply(a , -b);
    }
    public static void main(String[] args) {
        Scanner scn = new Scanner(System.in);
        System.out.println("Enter the first number(a): " );
        int a = scn.nextInt();
        System.out.println("Enter the Second number(b): " );
        int b = scn.nextInt();

        int result = multiply(a,b);
        System.out.println("Result of " + a + " * " + b + " = "
+ result);
    }
}
```

Problem Statement

Problem: The Josephus Problem

Given `n` people standing in a circle, where every `k`-th person is eliminated, find the position of the last person remaining (the safe position).

Example

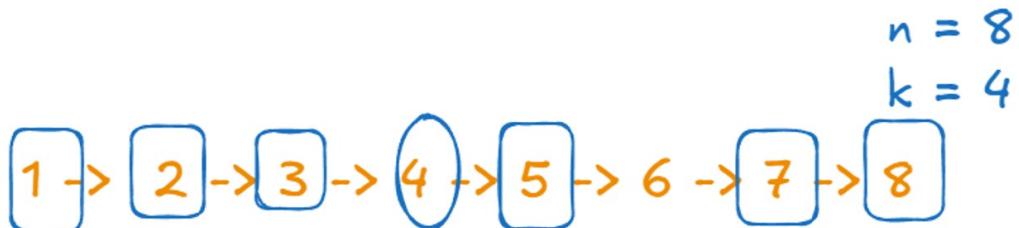
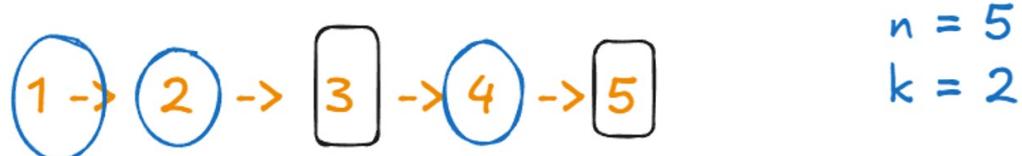
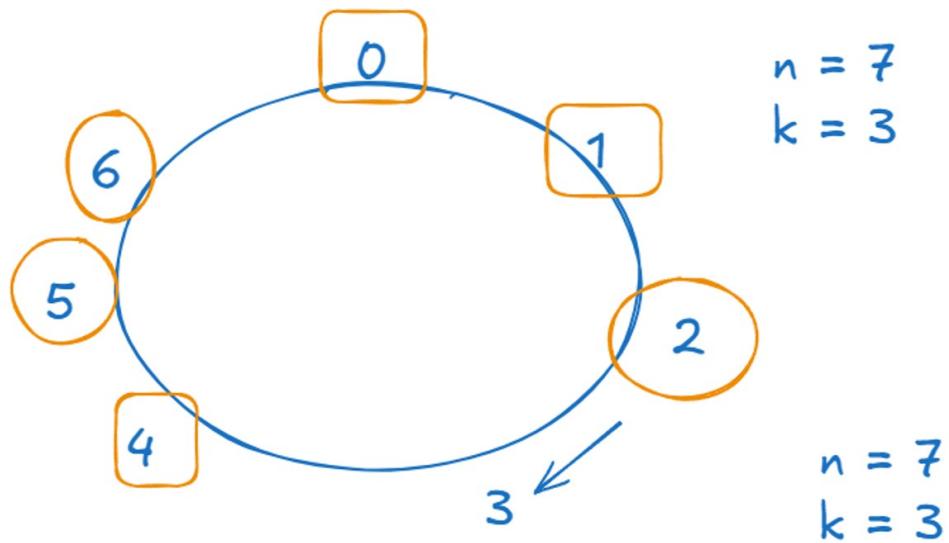
Example 1:

- Input:
 - `n = 7` (total people)
 - `k = 3` (every 3rd person is eliminated)
- Output:
 - `4` (the safe position)

Example 2:

- Input:
 - `n = 5`
 - `k = 2`

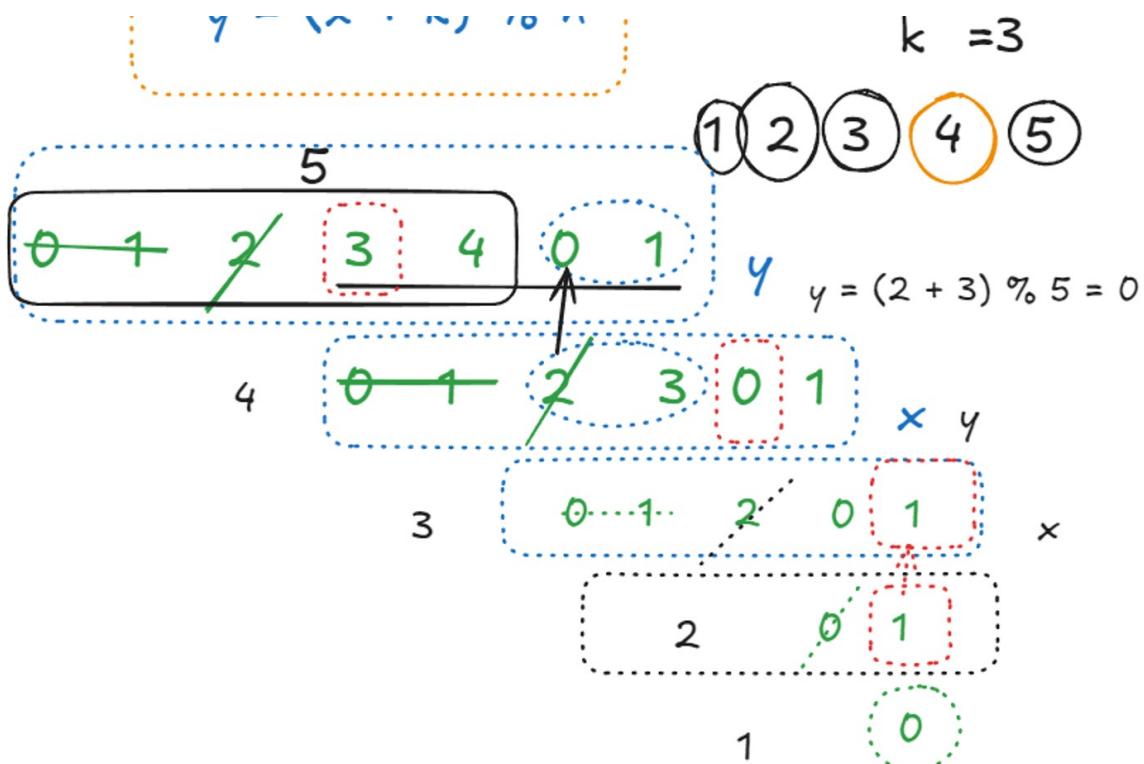
- `n = 5`
- `k = 2`
- Output:
- `3`



$$y = (x + k) \% n$$

$n = 5$
 $k = 3$





```

import java.util.Scanner;
public class JosephusProblem {
    public static int josephus(int n , int k){
        if(n == 1){
            return 0;
        }
        return (josephus(n-1, k) + k ) % n;
    }
    public static void main(String[] args) {
        Scanner scn = new Scanner(System.in);

        System.out.println("Enter the number of people(n) :");
        int n = scn.nextInt();
        System.out.println("Enter the step count (k) :");
        int k = scn.nextInt();

        int safePosition = josephus(n , k) + 1;
        System.out.println("The safe position is : " + safePosition);
    }
}

```

Enter the number of people(n) :
5

```

Enter the number of people(n) :
5
Enter the step count (k) :
2
The safe position is : 3

```

1. Print All Subsequences of a String

Problem Statement

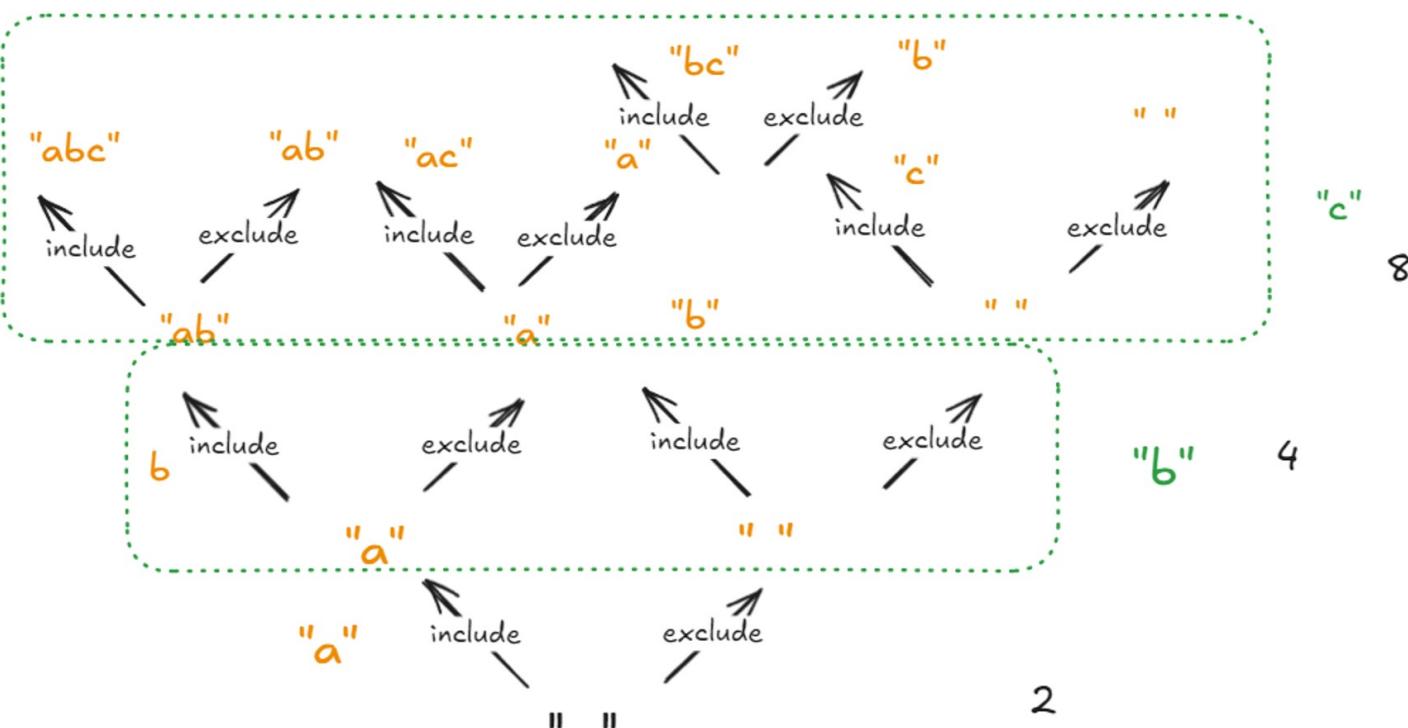
Given a string s , print all possible subsequences of the string. A subsequence is a sequence that can be derived from another sequence by deleting some or no elements without changing the order of the remaining elements.

Examples

- Input: $s = "abc"$
- Output: $["", "a", "b", "c", "ab", "ac", "bc", "abc"]$



$$\frac{2}{a} \quad \frac{2}{b} \quad \frac{2}{c} = 8$$



```
public class SubSequence {
```

```

    public static void printSubsequence(String str , int index , String current){
        if(index == str.length()){
            System.out.println(current);
            return;
        }
    }
}
```

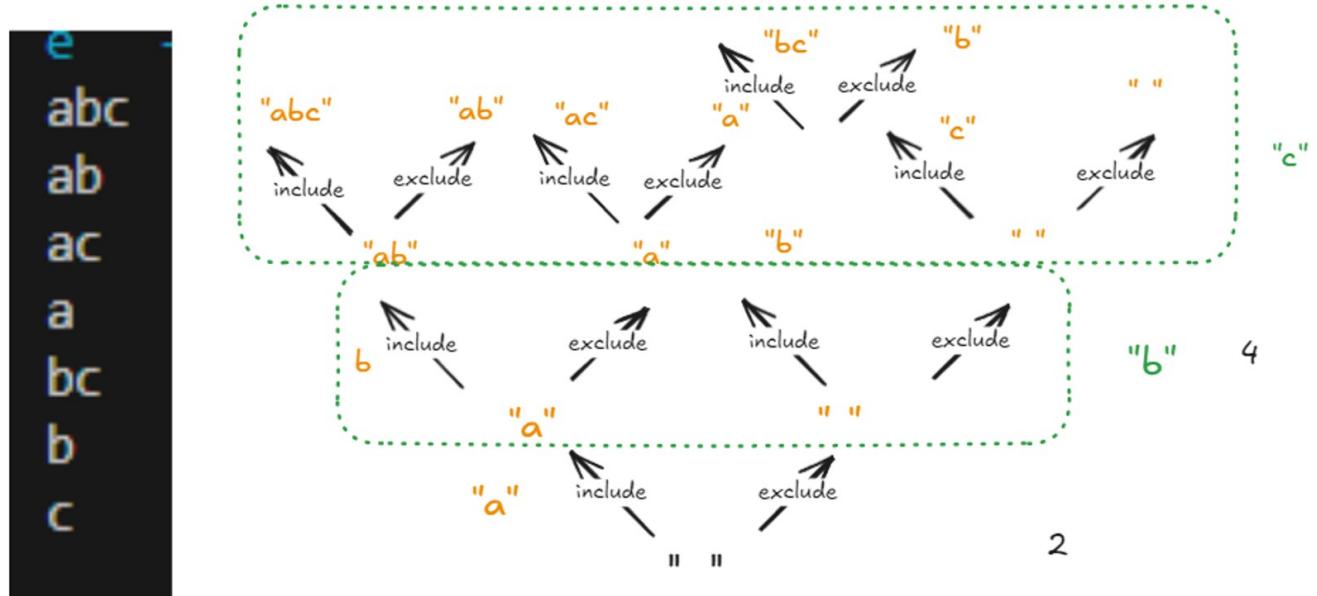
```

        if(index == str.length()){
            System.out.println(current);
            return;
        }

        // Include the character
        printSubsequence(str, index + 1 , current + str.charAt(index));
        // Exclude the character
        printSubsequence(str, index + 1 , current);
    }

    public static void main(String[] args) {
        String str = "abc";
        printSubsequence(str , 0 , "");
    }
}

```



```

        if(index == str.length()){
            System.out.println(current);
            return;
        }

        // Include the character
        printSubsequence(str, index + 1 , current + str.charAt(index));
        // Exclude the character
        printSubsequence(str, index + 1 , current);
    }

    public static void main(String[] args) {
        String str = "abc";
        printSubsequence(str , 0 , "");
    }
}

```

abc, ab, ac, a, bc, b, c, "

P.s("abc", 3, "")
P.s("abc", 2, "")
P.s("abc", 1, "")
P.s("abc", 0, "")

Call Stack

3. Longest Continuous Increasing Subsequence

Problem Statement

Given an unsorted array of integers `nums`, find the length of the longest continuous increasing subsequence (LCIS).

Examples

- Input:** `nums = [1, 3, 5, 4, 7]`
- Output:** `3`
- Explanation:** The longest continuous increasing subsequence is `[1, 3, 5]` with length `3`.

1 3 5 4 7

`max = 3`
`curr = 2`

```
for (1 to <n>){
    if(arr[i] > arr[i-1]){
        curr++;
        max = Math.max(max, curr);
    } else curr = 1;
}
```

```
public class LCIS {
    public static int FindLengthofLCIS(int[] nums){
        if(nums.length == 0){
            return 0;
        }
        int maxLength = 1;
        int currentLength = 1;
        for(int i = 1; i<nums.length; i++){
            if(nums[i] > nums[i-1]){
                currentLength++;
                maxLength = Math.max(maxLength, currentLength);
            }else{
                currentLength = 1;
            }
        }
    }
}
```

```

        }else{
            currentLength = 1;
        }
    }
    return maxLength;
}

public static void main(String[] args) {
    int[] nums = {1 , 3, 5, 4 , 7};
    System.out.println(FindLengthOfLCIS(nums));
}
}

```

Completed

Attendance Code: B1C270B8

Problem Statement

Given an array of positive integers `nums` and a positive integer `target`, find the minimal length of a contiguous subarray of which the sum is greater than or equal to `target`. If no such subarray exists, return `0`.

Examples

- Example 1:
 - Input: `nums = [2, 3, 1, 2, 4, 3]`, `target = 7`
 - Output: `2`
 - Explanation: The subarray `[4, 3]` has the minimal length with a sum equal to `7`.
- Example 2:
 - Input: `nums = [1, 4, 4]`, `target = 4`
 - Output: `1`
 - Explanation: The subarray `[4]` has the minimal length with a sum of `4`.
- Example 3:
 - Input: `nums = [1, 1, 1, 1, 1, 1, 1, 1]`, `target = 11`
 - Output: `0`
 - Explanation: No subarray has a sum greater than or equal to `11`.

$\text{target} = 7$

2 3 1 2 4 3

$\text{minLength} = 3$