

Polynomial-Regression

January 14, 2025

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[ ]: '''  
    Polynomial Regression -->  
  
    Polynomial regression is a form of regression analysis that models the  
    ↪ relationship between the independent variable  
    x and the dependent variable y. y as an n-th degree polynomial. It is  
    ↪ useful when data shows a curvilinear relationship  
    rather than a straight line, as linear regression does.  
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[ ]: '''  
    Polynomial Regression -->  
  
     $y = 0 + 1x + 2x^2 + 3x^3 + \dots + nx^n +$   
  
    Where -->  
  
    y is the dependent variable (target)  
    x is the independent variable (input)  
    0, 1, ..., n are the coefficients to be learned  
    n is the degree of the polynomial  
    is the error term  
    '''
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[21]: # Importing Libraries -->  
  
import pandas as pd  
import numpy as np  
import matplotlib.pyplot as plt  
from sklearn.linear_model import LinearRegression  
from sklearn.preprocessing import PolynomialFeatures
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[22]: # Importing Dataset -->  
  
data = pd.read_csv('Data/Position_Salaries.csv')  
data
```

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[22]:
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	Position	Level	Salary
0	Business Analyst	1	45000
1	Junior Consultant	2	50000
2	Senior Consultant	3	60000
3	Manager	4	80000
4	Country Manager	5	110000
5	Region Manager	6	150000
6	Partner	7	200000
7	Senior Partner	8	300000
8	C-level	9	500000
9	CEO	10	1000000

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[23]: x_data = data.iloc[:, 1: -1].values
      y_data = data.iloc[:, -1].values
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[24]: # Building Linear Model -->

linear_model = LinearRegression()
linear_model.fit(x_data, y_data)
```

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[24]: LinearRegression()
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[34]: # Applying Polynomial Features To Data -->

polynomial_model = PolynomialFeatures(degree = 4)
x_poly = polynomial_model.fit_transform(x_data)
x_poly
```

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[34]: array([[1.000e+00, 1.000e+00, 1.000e+00, 1.000e+00, 1.000e+00],
      [1.000e+00, 2.000e+00, 4.000e+00, 8.000e+00, 1.600e+01],
      [1.000e+00, 3.000e+00, 9.000e+00, 2.700e+01, 8.100e+01],
      [1.000e+00, 4.000e+00, 1.600e+01, 6.400e+01, 2.560e+02],
      [1.000e+00, 5.000e+00, 2.500e+01, 1.250e+02, 6.250e+02],
      [1.000e+00, 6.000e+00, 3.600e+01, 2.160e+02, 1.296e+03],
      [1.000e+00, 7.000e+00, 4.900e+01, 3.430e+02, 2.401e+03],
      [1.000e+00, 8.000e+00, 6.400e+01, 5.120e+02, 4.096e+03],
      [1.000e+00, 9.000e+00, 8.100e+01, 7.290e+02, 6.561e+03],
      [1.000e+00, 1.000e+01, 1.000e+02, 1.000e+03, 1.000e+04]])
```

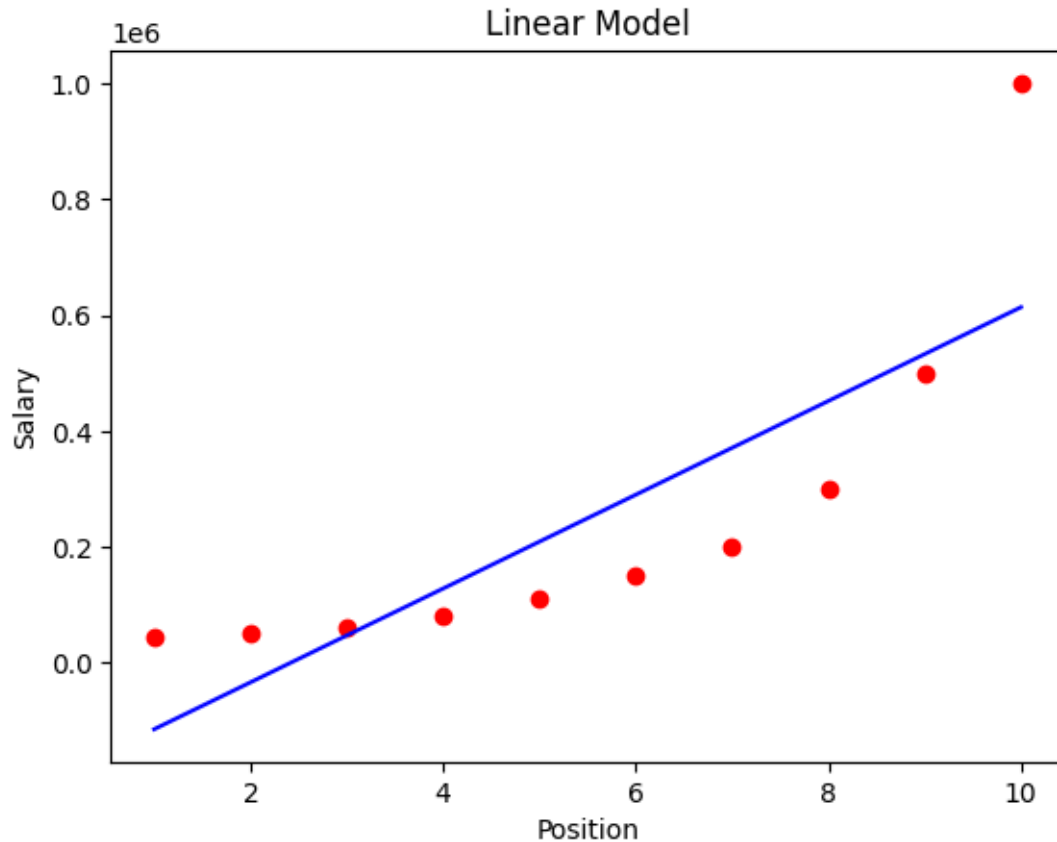
```
[35]: # Building Polynomial Model -->

model = LinearRegression()
model.fit(x_poly, y_data)
```

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[35]: LinearRegression()
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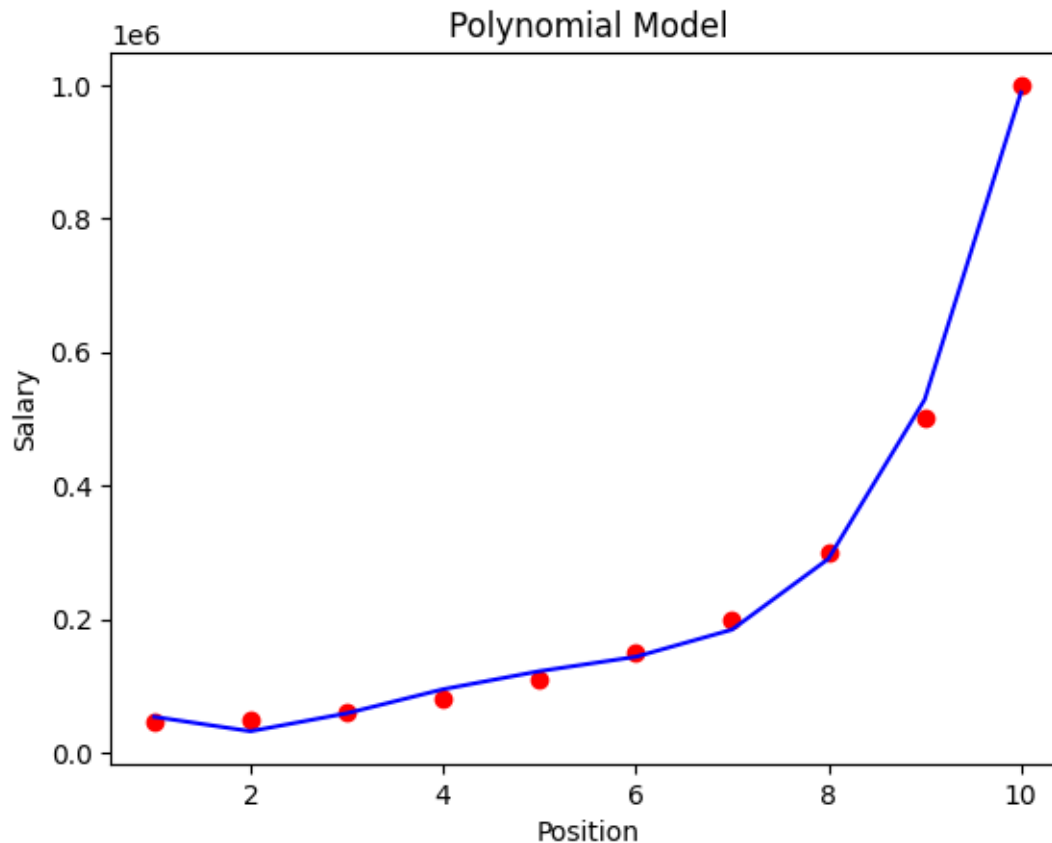
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[36]: # Visualizing Linear Model -->
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plt.scatter(x_data, y_data, color = 'red')
plt.plot(x_data, linear_model.predict(x_data), color = 'blue')
plt.title("Linear Model")
plt.xlabel("Position")
plt.ylabel("Salary")
plt.show()
```



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[37]: # Visualizing Polynomial Model -->
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```
plt.scatter(x_data, y_data, color = 'red')
plt.plot(x_data, model.predict(x_poly), color = 'blue')
plt.title("Polynomial Model")
plt.xlabel("Position")
plt.ylabel("Salary")
plt.show()
```



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[ ]: # Predicting Salary with Linear Model -->
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linear_model.predict([[6.5]])
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[ ]: array([330378.78787879])
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[41]: # Linear Model has very high Error Lets check with Polynomial Model -->
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model.predict(polynomial_model.fit_transform([[6.5]]))
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[41]: array([158862.45265155])
```

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[ ]: '''
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Summary -->

*Polynomial regression is linear because it is linear in the coefficients, □
 ↳ even though it involves polynomial features*

*Degree 4 is chosen when the data shows more complex relationships than can □
 ↳ be captured by a lower degree*

(like degree 2 or 3), but care should be taken to avoid overfitting

*Data transformation (e.g., creating polynomial features like x^2 , x^3)
↳ allowing a linear regression model
to handle more complex patterns in the data*