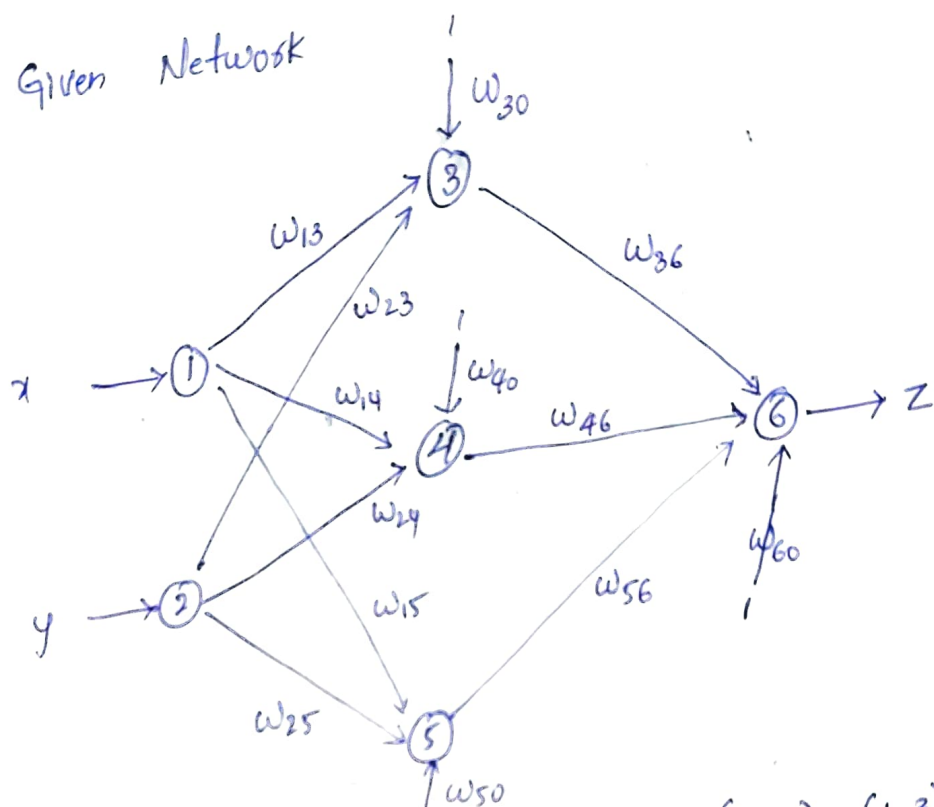


# Group 55 - Assignment 1 - Problem 2

Given Network



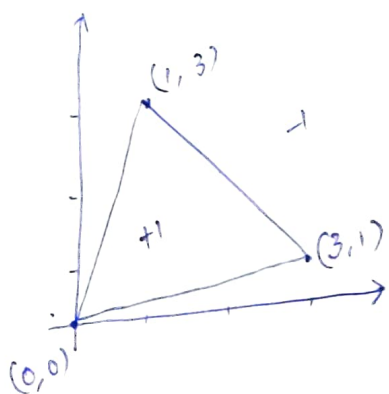
Given Vertices of the triangle  $(0,0)$ ,  $(1,3)$ ,  $(3,1)$

Equations of lines passing through these points

$$(0,0) \text{ \& \; } (3,1) \Rightarrow x - 3y = 0 \rightarrow \textcircled{1}$$

$$(0,0) \text{ \& \; } (1,3) \Rightarrow 3x - y = 0 \rightarrow \textcircled{2}$$

$$(3,1) \text{ \& \; } (1,3) \Rightarrow x + y - 4 = 0 \rightarrow \textcircled{3}$$



Points inside triangle are considered of class 1 and Points on and outside triangle are class -1.

Input for node 3 is

$$w_{13}x + w_{23}y + w_{30}(1) \rightarrow \textcircled{4}$$

$$\text{for node 4} \Rightarrow w_{14}x + w_{24}y + w_{40}(1) \rightarrow \textcircled{5}$$

$$\text{for node 5} \Rightarrow w_{15}x + w_{25}y + w_{50}(1) \rightarrow \textcircled{6}$$

Comparing equations  $\textcircled{1}$   $\textcircled{2}$  &  $\textcircled{3}$  with  $\textcircled{4}$ ,  $\textcircled{5}$  and  $\textcircled{6}$  respectively

$$w_{13} = 3, \quad w_{23} = -1, \quad w_{30} = 0$$

$$w_{14} = 1, \quad w_{24} = -3, \quad w_{40} = 0$$

$$w_{15} = 1, \quad w_{25} = 1, \quad w_{50} = -4$$

If a point lies inside the triangle then the point should lie above the line  $x - 3y = 0$  and below the lines  $x + y - 4 = 0$ ,  $3x - y = 0$ .

We have, a point  $A(x_1, y_1)$  is above a line  $ax + by + c = 0$

if, (i)  $ax_1 + by_1 + c > 0$  and  $b > 0$

(ii)  $ax_1 + by_1 + c < 0$  and  $b < 0$

a point  $A(x_1, y_1)$  is below a line  $ax + by + c = 0$  if,

(i)  $ax_1 + by_1 + c < 0$  and  $b > 0$

(ii)  $ax_1 + by_1 + c > 0$  and  $b < 0$

Hence, for a

Point inside a triangle, it should be ① below

$$3x - y = 0 \Rightarrow \text{output of node 3 should be } > 0$$

$$\text{Since } b < 0$$

$$\textcircled{2} \text{ above } x - 3y = 0 \Rightarrow \text{output of node 4 should be } < 0$$

$$\text{since } b < 0$$

$$\textcircled{3} \text{ below } x + y - 4 = 0 \Rightarrow \text{output of nodes should be } \leq 0$$

$$\text{since } b > 0$$

We considered Sigmoid functions as activation functions at nodes 3, 4, 5 & 6.

Hence we get

$$w_{36} = 1, w_{46} = -1, w_{56} = -1$$

to make outputs of nodes 3, 4, 5 +ve, -ve and -ve respectively.

$$\text{Input to node 6 is } f_3 w_{36} + f_4 w_{46} + f_5 w_{56} + w_{60}$$

This equation is greater than 0 for point inside triangle.

$$f_3 w_{36} + f_4 w_{46} + f_5 w_{56} + w_{60} > 0$$

$$1 \times 1 + (-1)(-1) + (-1)(-1) + w_{60} > 0$$

$$w_{60} > -3$$

Considering  $w_{60}$  to be  $-2$ .

Here are the final weights.

$$w_{13} = 3$$

$$w_{14} = 1$$

$$w_{15} = 1$$

$$w_{36} = 1$$

$$w_{23} = -1$$

$$w_{24} = -3$$

$$w_{25} = 1$$

$$w_{46} = -1$$

$$w_{30} = 0$$

$$w_{40} = 0$$

$$w_{50} = -4$$

$$w_{56} = -1$$

$$w_{60} = -2$$