

Grammar considered for calculator is

$$E \rightarrow E + T \mid E - T \mid T$$
$$T \rightarrow T * F \mid T / F \mid F$$
$$F \rightarrow (E) \mid \text{INT}$$

Consider Two Functions:

nodeInt(INT): Node consists only of leaf nodes, i.e. Integers.

nodeOp(Op, L, R): Node consists of the operation that is to performed(Op), expression on the Left side of the operator(L) and expression on the right side of the operator(R).

$$E \rightarrow E + T \{E.value = \text{nodeOp}(+, E.value, T.value)\}$$
$$E \rightarrow E - T \{E.value = \text{nodeOp}(-, E.value, T.value)\}$$
$$E \rightarrow T \quad \{E.value = T.value\}$$
$$T \rightarrow T * F \{T.value = \text{nodeOp}(*, T.value, F.value)\}$$
$$T \rightarrow T / F \{T.value = \text{nodeOp}(/, T.value, F.value)\}$$
$$T \rightarrow F \quad \{T.value = F.value\}$$
$$F \rightarrow (E) \{F.value = E.value\}$$
$$F \rightarrow \text{INT} \{F.value = \text{nodeInt}(\text{INT})\}$$

This is a Syntax Attributed Grammar (SAG). We compute the attributes in a bottom up fashion. So we use this along with LR Parsing.

As the leaf nodes must be integers and we evaluate them in a Bottom up parsing. If we encounter an Integer we push them into a separate stack which consists only of values. The values from this stack are used for computation.