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## Assignment-6

Roll No. : FWC22036

### Problem Statement:

Find the equations of tangent and normal to the parabola  $y^2 = 4ax$  at point  $(at^2, 2at)$ .

### SOLUTION:

#### Given:

The given equation of parabola  $y^2 = 4ax$  can be written as

$$\mathbf{x}^T \mathbf{V} \mathbf{x} + 2\mathbf{u}^T \mathbf{x} + f = 0 \quad (1)$$

where

$$\mathbf{V} = \begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix}, \quad (2)$$

$$\mathbf{u} = \begin{pmatrix} -2a \\ 0 \end{pmatrix}, \quad (3)$$

$$f = 0 \quad (4)$$

#### To Find

Equation of tangent and normal at point  $(at^2, 2at)$

#### STEP-1

The equation of tangent is given by

$$(\mathbf{V}\mathbf{q} + \mathbf{u})^T \mathbf{x} + \mathbf{u}^T \mathbf{q} + f = 0 \quad (5)$$

where

$$\mathbf{q} = \begin{pmatrix} at^2 \\ 2at \end{pmatrix} \quad (6)$$

substituting  $\mathbf{V}$ ,  $\mathbf{u}$ ,  $\mathbf{q}$  and  $f$  in (5) we get the tangent equation as

$$(-(1/t) \ 1) \mathbf{x} = at \quad (7)$$

#### STEP-2

The equation of normal is given by

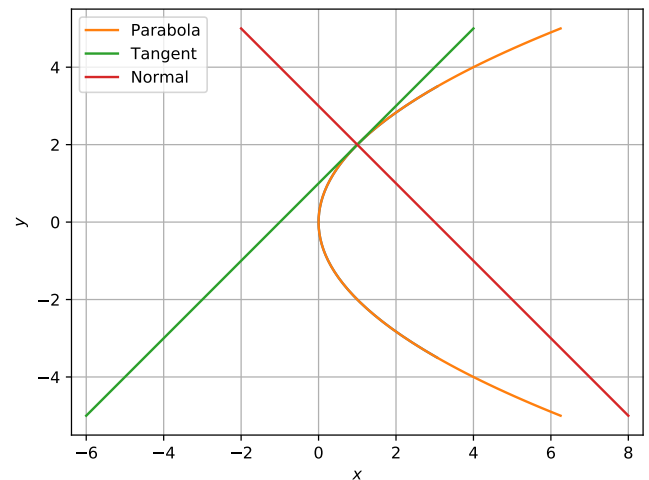
$$\mathbf{m}^T (\mathbf{x} - \mathbf{q}) = 0 \quad (8)$$

where  $\mathbf{m}$  is given by:

$$\mathbf{m} = \begin{pmatrix} 1 \\ 1/t \end{pmatrix} \quad (9)$$

substituting  $\mathbf{m}, \mathbf{q}$  in (8) we get the normal equation as

$$(t \ 1) \mathbf{x} = 2at + at^3 \quad (10)$$



#### Construction

vertex	coordinates
$\mathbf{q}$	$\begin{pmatrix} at^2 \\ 2at \end{pmatrix}$

Download the code

Github link: Assignment-6.