Assignment #3

Q_9.2 Perform encryption and decryption using the RSA algorithm, as in Figure 9.6 for the following:

Answer:

$$n = p * q = 3 * 11 = 33$$

$$f(n) = (p-1) * (q-1) = 2 * 10 = 20$$

Now, we need to compute $d = e^{-1} \mod f(n)$ by using backward substitution of GCD algorithm:

According to GCD:

$$20 = 7 * 2 + 6$$

 $7 = 6 * 1 + 1$
 $6 = 1 * 6 + 0$

Therefore, we have:

$$1 = 7 - 6$$

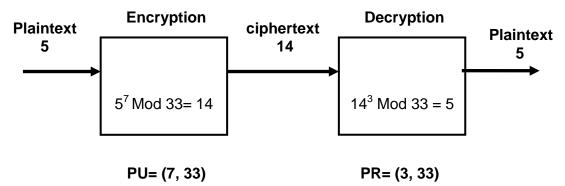
$$= 7 - (20 - 7 * 2)$$

$$= 7 - 20 + 7 * 2$$

$$= -20 + 7 * 3$$

Hence, we get $d = e^{-1} \mod f(n) = e^{-1} \mod 20 = 3 \mod 30 = 3$

So, the public key is {7, 33} and the private key is {3, 33}, RSA encryption and decryption is following:



Answer:

$$n = p * q = 5 * 11 = 55$$

$$f(n) = (p-1) * (q-1) = 4 * 10 = 40$$

Now, we need to compute $d = e^{-1} \mod f(n)$ by using backward substitution of GCD algorithm:

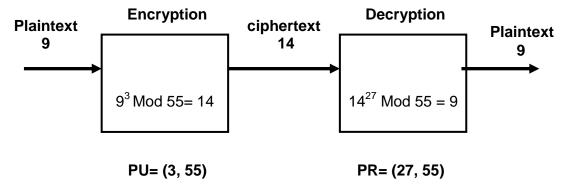
According to GCD:

$$40 = 3 * 13 + 1$$
$$13 = 1 * 13 + 0$$

Therefore, we have:

$$1 = 40 - 3 * 13$$

Hence, we get $d = e^{-1} \mod f(n) = e^{-1} \mod 40 = -13 \mod 40 = (27 - 40) \mod 40 = 27$ So, the public key is $\{3, 55\}$ and the private key is $\{27, 55\}$, RSA encryption and decryption is following:



Answer:

$$n = p * q = 7 * 11 = 77$$

$$f(n) = (p-1) * (q-1) = 6 * 10 = 60$$

Now, we need to compute $d = e^{-1} \mod f(n)$ by using backward substitution of GCD algorithm:

According to GCD:

$$60 = 17 * 3 + 9$$

 $17 = 9 * 1 + 8$
 $9 = 8 * 1 + 1$
 $8 = 1 * 8 + 0$

Therefore, we have:

$$1 = 9 - 8$$

$$= 9 - (17 - 9)$$

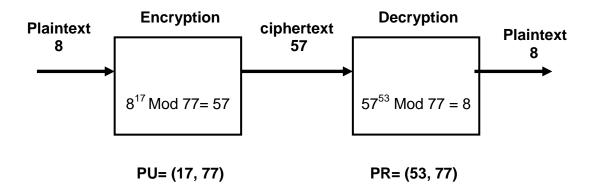
$$= 9 - (17 - (60 - 17 * 3))$$

$$= 60 - 17*3 - (17 - 60 + 17*3)$$

$$= 60 - 17*3 + 60 - 17*4$$

$$= 60*2 - 17*7$$

Hence, we get $d = e^{-1} \mod f(n) = e^{-1} \mod 60 = -7 \mod 60 = (53-60) \mod 60 = 53$ So, the public key is $\{17, 77\}$ and the private key is $\{53, 77\}$, RSA encryption and decryption is following:



Answer:

$$n = p * q = 11 * 13 = 143$$

$$f(n) = (p-1) * (q-1) = 10 * 12 = 120$$

Now, we need to compute $d = e^{-1} \mod f(n)$ by using backward substitution of GCD algorithm:

According to GCD:

$$120 = 11 * 10 + 10$$

 $11 = 10 * 1 + 1$
 $10 = 1 * 10 + 0$

Therefore, we have:

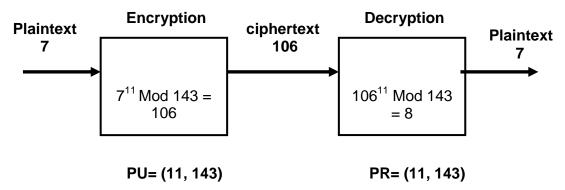
$$1 = 11 - 10$$

$$= 11 - (120 - 11 * 10)$$

$$= 11 - 120 + 11 * 10$$

$$= -120 + 11 * 11$$

Hence, we get $d = e^{-1} \mod f(n) = e^{-1} \mod 120 = 11 \mod 120 = 11$ So, the public key is $\{11, 143\}$ and the private key is $\{11, 143\}$, RSA encryption and decryption is following:



Now, we need to compute $d = e^{-1} \mod f(n)$ by using backward substitution of GCD algorithm:

According to GCD:

$$480 = 7 * 68 + 4$$

 $7 = 4 * 1 + 3$
 $4 = 3 * 1 + 1$
 $3 = 1 * 3 + 0$

Therefore, we have:

$$1 = 4 - 3$$

$$= 4 - (7 - 4)$$

$$= 4 - (7 - (480 - 7*68))$$

$$= 4 - (7 - 480 + 7*68)$$

$$= 480 - 7*68 - 7 + 480 - 7*68$$

$$= 480*2 - 7*137$$

Hence, we get $d = e^{-1} \mod f(n) = e^{-1} \mod 480 = -137 \mod 480 = (343 - 480) \mod 480 = 343$

So, the public key is $\{7, 527\}$ and the private key is $\{343, 527\}$, RSA encryption and decryption is following:

