MIT WORLD PEACE UNIVERSITY

Advanced Data Structures Second Year B. Tech, Semester 4

LINEAR PROBING WITH AND WITHOUT REPLACEMENT FOR HASHING

ASSIGNMENT NO. 8

Prepared By

Krishnaraj Thadesar Cyber Security and Forensics Batch A1, PA 20

April 12, 2023

Contents

1	Objectives	1
2	Problem Statement	1
3	Theory 3.1 What is Hashing? 3.1.1 Hashing in Comparison with other Searching Techniques 3.2 Hash Functions. 3.2.1 Hash Function 3.3 Collision Resolution Techniques 3.3.1 Without Replacement 3.3.2 With Replacement	$1\\2\\2\\2$
4	Platform	4
5	Test Conditions	4
6	Input and Output	4
7	Pseudo Code7.1 Linear Probing with Replacement	
8	Time Complexity 8.1 Linear Probing	5
9	Code 9.1 Program	5
10	Conclusion	13
11	FAQ	14

1 Objectives

- 1. To study hashing techniques
- 2. To implement different hashing techniques
- 3. To study and implement linear probing with and without replacement
- 4. To study how hashing can be used to model real world problems

2 Problem Statement

Implement Direct access file using hashing (linear probing with and without replacement) perform following operations on it:

- 1. Create Database
- 2. Display Database
- 3. Add a record
- 4. Search a record
- 5. Modify a record

3 Theory

3.1 What is Hashing?

Hashing is a technique to convert a range of key values into a range of indexes of an array. The idea is to use the key itself as an index into an array that is why it is also called as direct access table.

3.1.1 Hashing in Comparison with other Searching Techniques

• Sequential Search:

- The worst case time complexity of the sequential search is O(n)
- The worst case time complexity of the hashing is O(1)
- The sequential search is not suitable for large data sets
- The hashing is suitable for large data sets

• Binary Search:

- The worst case time complexity of the binary search is O(log n)
- The worst case time complexity of the hashing is O(1)
- The binary search is only suitable for sorted data sets
- The hashing is suitable for unsorted data sets

• Binary Tree:

- The worst case time complexity of the binary tree search is O(log n)
- The worst case time complexity of the hashing is O(1)
- The binary tree search is only suitable for sorted data sets
- The hashing is suitable for unsorted data sets

3.2 Hash Functions

3.2.1 Hash Function

A hash function is a function that maps a given key to a location in the hash table. The hash function is used to calculate the index of the array where the data is to be stored or retrieved from.

Different types of Hash functions are:

1. Division Method

The division method is one of the simplest hashing methods. It works by computing the remainder of the key when divided by the table size, using a hash function of the form $h(key) = key \mod table_size$. The result is the index of the slot in the hash table where the key-value pair should be stored.

2. Multiplication Method

The multiplication method is another common hashing method. It works by multiplying the key by a constant A in the range (0,1) and then extracting the fractional part of the product. The result is then multiplied by the table size and rounded down to obtain the index of the slot in the hash table where the key-value pair should be stored. The hash function has the form $h(key) = \lfloor table_s ize * (key * A \mod 1) \rfloor$.

3. Universal Hashing

Universal hashing is a family of hashing methods that use a randomly chosen hash function from a set of functions to minimize collisions. The set of functions is chosen to be large enough that the probability of two different keys having the same hash value is small, and the function is chosen randomly each time a new hash table is created. The hash function has the form $h(key) = ((a*key+b) \mod p) \mod table_size$, where a and b are randomly chosen integers and b is a large prime number.

4. Perfect Hashing

Perfect hashing is a technique that is used when the keys are known in advance and fixed. It works by creating a hash function that maps each key to a unique index in the hash table, without any collisions. This is achieved by using two levels of hashing: the first level maps the keys to a set of buckets, and the second level uses a different hash function to map each key within a bucket to a unique index in the hash table. This approach guarantees that there are no collisions, but requires more memory and computation than other hashing methods.

3.3 Collision Resolution Techniques

The main types of Collision Resolution techniques are:

• Open Addressing:

Open addressing is a family of hashing methods that use the hash table itself to resolve collisions, by storing each key-value pair in the next available slot in the table. There are several methods of open addressing, including:

- Linear Probing

Linear probing is an open addressing method where, when a collision occurs, the algorithm searches for the next available slot in the table, by linearly checking each slot in the table until an empty slot is found. The hash function has the form $h(key, i) = (h'(key) + i) \mod table_size$, where h'(key) is the primary hash function and i is the number of the probe.

- Quadratic Probing

Quadratic probing is similar to linear probing, but uses a quadratic function to search for the next available slot. The hash function has the form $h(key, i) = (h'(key) + c_1 \cdot i + c_2 \cdot i^2)$ mod $table_size$, where c_1 and c_2 are constants that depend on the hash table size.

- Double Hashing

Double hashing is another open addressing method that uses two hash functions to determine the next available slot in the table. The hash function has the form $h(key, i) = (h_1(key) + i \cdot h_2(key)) \mod table_size$, where h_1 and h_2 are two different hash functions.

• Separate Chaining

Separate chaining is a hashing method that uses linked lists to store the key-value pairs that hash to the same slot in the table. When a collision occurs, the key-value pair is added to the linked list at the appropriate slot. The hash function has the form $h(key) = key \mod table_size$.

• Double Hashing

Double hashing is both an open addressing method and a separate chaining method. It uses two hash functions to determine the slot in the table, and if there is a collision, it uses a linked list to store the key-value pairs that hash to the same slot. The hash function has the form $h(key,i) = (h_1(key) + i \cdot h_2(key)) \mod table_size$, where h_1 and h_2 are two different hash functions.

Most of these techniques can be implemented in 2 ways

3.3.1 Without Replacement

[Without Replacement] In this technique, when a collision occurs, the new element is simply discarded.

3.3.2 With Replacement

[With Replacement] In this technique, when a collision occurs, the old element is replaced by the new element.

4 Platform

Operating System: Arch Linux x86-64

IDEs or Text Editors Used: Visual Studio Code

Compilers: g++ and gcc on linux for C++

5 Test Conditions

- 1. Input at least 10 nodes.
- 2. Display collision with replacement and without replacement.

6 Input and Output

1. The minimum cost of the spanning tree.

7 Pseudo Code

7.1 Linear Probing with Replacement

```
void HashTable::insert_without_replacement(int key)
      int index = hash(key);
3
      if (table[index] == -1)
          table[index] = key;
5
      else
6
7
      {
          int i = 1;
          while (table[(index + i) % SIZE] != -1)
10
          table[(index + i) % SIZE] = key;
11
      }
12
13 }
```

7.2 Linear Probing without Replacement

```
void HashTable::insert_with_replacement(int key)
     {
2
          int index = hash(key);
3
          // there is no value there.
          if (table[index] == -1)
              table[index] = key;
          // the value that is already there, belongs there, then check, and then
     find another empty slot and insert there.
          else if (hash(table[index]) == index)
10
11
              int i = 1;
              while (table[(index + i) % SIZE] != -1)
13
              table[(index + i) % SIZE] = key;
```

```
}
15
          // the value that is already there, does not belong there, then replace it
16
       with the new value, and push the existing value down.
17
          {
18
               // find empty slot
19
               int i = 1;
20
               while (table[(index + i) % SIZE] != -1)
24
               int temp = table[index]; // current value that doesnt belong there.
25
               table[index] = key;
               table[(index + i) % SIZE] = temp;
26
          }
27
```

8 Time Complexity

8.1 Linear Probing

• Time Complexity:

O(n)

It would be 1 if the it was the best case, and n for worst case, where all the slots would be filled, and we would have to keep probing over all the elements.

• Space Complexity:

O(n)

For storing the Table, as there is no additional array or table required to store and hash.

9 Code

9.1 Program

```
_{1} // Program for linear probing with and without replacement.
  #include <iostream>
5 using namespace std;
7 const int SIZE = 10;
9 class HashTable
10 {
11 public:
      HashTable();
12
      int insert_without_replacement(int key);
13
      int insert_with_replacement(int key);
      void print();
17 private:
     int table[SIZE];
18
      int hash(int key);
20 };
```

```
22 HashTable::HashTable()
      for (int i = 0; i < SIZE; i++)</pre>
          table[i] = -1;
26 }
28 int HashTable::hash(int key)
29 {
      return key % SIZE;
31 }
32
int HashTable::insert_without_replacement(int key)
34 {
      int index = hash(key);
35
      if (table[index] == -1)
           table[index] = key;
37
38
      {
39
          int i = 1;
40
           while (table[(index + i) % SIZE] != -1)
41
               i++;
44
               if (i == SIZE)
45
               {
                   cout << "Table is full. " << endl;</pre>
46
                   return 1;
47
48
          }
49
           table [(index + i) % SIZE] = key;
51
      return 0;
52
53 }
int HashTable::insert_with_replacement(int key)
56 {
57
      int index = hash(key);
58
      // there is no value there.
59
      if (table[index] == -1)
60
          table[index] = key;
61
      // the value that is already there, belongs there, then check, and then find
      another empty slot and insert there.
      else if (hash(table[index]) == index)
63
64
           int i = 1;
65
           while (table[(index + i) % SIZE] != -1)
66
67
               i++;
               if (i == SIZE)
69
70
                   cout << "Table is full. " << endl;</pre>
71
                   return 1;
73
           }
74
           table [(index + i) % SIZE] = key;
75
76
      // the value that is already there, does not belong there, then replace it
      with the new value, and push the existing value down.
```

```
else
78
       {
79
            // find empty slot
81
            int i = 1;
            while (table[(index + i) % SIZE] != -1)
82
            {
83
                 i++:
84
                if (i == SIZE)
                      cout << "Table is full. " << endl;</pre>
88
                     return 1;
                 }
89
            }
90
91
            int temp = table[index]; // current value that doesnt belong there.
92
            table[index] = key;
            table [(index + i) % SIZE] = temp;
95
       return 0;
96
97 }
  void HashTable::print()
99
101
       for (int i = 0; i < SIZE; i++)</pre>
            cout << i << ":" << table[i] << " " << endl;</pre>
102
       cout << endl;</pre>
103
104 }
105
106 int main()
107
       HashTable table;
108
       int key;
109
       cout << "Welcome to ADS Assignment 8, hashign with linear probing." << endl;</pre>
111
       cout << "What do you want to do? " << endl;</pre>
       cout << "1. Insert without replacement. " << endl;</pre>
114
       cout << "2. Insert with replacement. " << endl;</pre>
       cout << "3. Exit. " << endl;</pre>
       int choice;
116
       cin >> choice;
       switch (choice)
118
       {
119
       case 1:
120
            cout << "You chose to insert without replacement. " << endl;</pre>
121
            cout << "Enter the keys to insert. " << endl;</pre>
            while (cin >> key)
123
                 if (table.insert_without_replacement(key) != 1)
127
                      cout << "The table is now: " << endl;</pre>
                     table.print();
128
                 }
129
                 else
130
                     break;
131
            }
132
            break;
133
134
            cout << "You chose to insert with replacement. " << endl;</pre>
135
            cout << "Enter the keys to insert. " << endl;</pre>
```

```
while (cin >> key)
137
138
           {
                if (table.insert_with_replacement(key) != 1)
140
                    cout << "The table is now: " << endl;</pre>
141
                    table.print();
142
                }
143
                else
144
                    break;
145
           }
147
           break;
148
       case 3:
           cout << "You chose to exit. " << endl;</pre>
149
           return 0;
150
       default:
151
           cout << "Invalid choice. " << endl;</pre>
153
           return 0;
154
       return 0;
155
156 }
 1 Welcome to ADS Assignment 8, hashign with linear probing.
 2 What do you want to do?
 3 1. Insert without replacement.
 4 2. Insert with replacement.
 5 3. Exit.
 6 1
 7 You chose to insert without replacement.
 8 Enter the keys to insert.
9 1
```

```
39 2:2
40 3:3
41 4:-1
42 5:-1
43 6:-1
44 7:-1
45 8:-1
46 9:-1
48 5
49 The table is now:
50 0:-1
51 1:1
52 2:2
53 3:3
54 4:-1
55 5:5
56 6:-1
57 7:-1
58 8:-1
59 9:-1
61 55
62 The table is now:
63 0:-1
64 1:1
65 2:2
66 3:3
67 4:-1
68 5:5
69 6:55
70 7:-1
71 8:-1
72 9:-1
74 234
75 The table is now:
76 0:-1
77 1:1
78 2:2
79 3:3
80 4:234
81 5:5
82 6:55
83 7:-1
84 8:-1
85 9:-1
86
87 32
88 The table is now:
89 0:-1
90 1:1
91 2:2
92 3:3
93 4:234
94 5:5
95 6:55
96 7:32
97 8:-1
```

```
98 9:-1
99
100 654
101 The table is now:
102 0:-1
103 1:1
104 2:2
105 3:3
106 4:234
107 5:5
108 6:55
109 7:32
110 8:654
111 9:-1
112
113 34
114 The table is now:
115 0:-1
116 1:1
117 2:2
118 3:3
119 4:234
120 5:5
121 6:55
122 7:32
123 8:654
124 9:34
125
126 645
127 The table is now:
128 0:645
129 1:1
130 2:2
131 3:3
132 4:234
133 5:5
134 6:55
135 7:32
136 8:654
137 9:34
140 Welcome to ADS Assignment 8, hashign with linear probing.
141 What do you want to do?
142 1. Insert without replacement.
143 2. Insert with replacement.
144 3. Exit.
145 2
146 You chose to insert with replacement.
147 Enter the keys to insert.
149 The table is now:
150 0:-1
151 1:1
152 2:-1
153 3:-1
154 4:-1
155 5:-1
156 6:-1
```

```
157 7:-1
158 8:-1
159 9: -1
162 The table is now:
163 0:-1
164 1:1
165 2:2
166 3:-1
167 4:-1
168 5:-1
169 6:-1
170 7:-1
171 8:-1
172 9:-1
173
174 3
175 The table is now:
176 0:-1
177 1:1
178 2:2
179 3:3
180 4:-1
181 5:-1
182 6:-1
183 7:-1
184 8:-1
185 9:-1
187 4
188 The table is now:
189 0:-1
190 1:1
191 2:2
192 3:3
193 4:4
194 5:-1
195 6: -1
196 7:-1
197 8:-1
198 9:-1
200 3
201 The table is now:
202 0:-1
203 1:1
204 2:2
205 3:3
206 4:4
207 5:3
208 6:-1
209 7:-1
210 8:-1
211 9:-1
214 The table is now:
215 0:-1
```

```
216 1:1
217 2:2
218 3:3
219 4:4
220 5:3
221 6:-1
222 7:-1
223 8:-1
224 9:9
225
226 99
227 The table is now:
228 0:99
229 1:1
230 2:2
231 3:3
232 4:4
233 5:3
234 6:-1
235 7:-1
236 8:-1
237 9:9
238
239 55
240 The table is now:
241 0:99
242 1:1
243 2:2
244 3:3
245 4:4
246 5:55
247 6:3
248 7:-1
249 8:-1
250 9:9
251
252 66
253 The table is now:
254 0:99
255 1:1
256 2:2
257 3:3
258 4:4
259 5:55
260 6:66
261 7:3
262 8:-1
263 9:9
265 99
266 The table is now:
267 0:99
268 1:1
269 2:2
270 3:3
271 4:4
272 5:55
273 6:66
274 7:3
```

```
275 8:99
276 9:9
277
278 3
279 Table is full.
```

10 Conclusion

Thus, we have implemented linear probing with and without replacement.

11 FAQ

1. Write different types of hash functions.

There are several types of Hashing Functions. Here are a few:

• **Division Method:** This method is the simplest of all hash functions. It simply divides the key by the table size and uses the remainder as the hash value. The hash function is:

$$h(k) = k \mod m$$

- **Multiplication Method:** In this method, the hash value is obtained by multiplying the key with a constant A and then taking the fractional part.
- **Universal Hashing:** In this method, the hash function is obtained by using a universal hash function.
- **Mid Square Method:** In this method, the key is first squared and the middle digits are then taken as the hash value.
- **Random Number Method:** In this method, a random number is generated and then multiplied with the key to obtain the hash value.
- **Folding Method:** In this method, the key is divided into equal parts and then added to obtain the hash value.
- **Exponential Method:** In this method, the key is multiplied by a constant A and then the fractional part is taken as the hash value.
- **Truncation Method:** In this method, the key is divided into equal parts and then the first part is taken as the hash value.

2. Explain chaining with and without replacement with example.

Chaining is a collision resolution technique used in hash tables to resolve collisions by storing multiple keys in the same slot in the table, with each slot containing a linked list of key-value pairs.

(a) With Replacement: Chaining with replacement involves replacing the old value with the new one when a collision occurs, while chaining without replacement involves inserting the new value into the linked list without replacing the old one.

Here is an example of chaining with replacement:

Suppose we have a hash table of size 5, and the hash function maps keys to slots as follows:

- $key "apple" \rightarrow slot 3$
- key "banana" → slot 1
- key "cherry" $\rightarrow slot 3$
- $key "date" \rightarrow slot 0$

When we try to insert the key "cherry", we find that slot 3 is already occupied by the key "apple". In chaining with replacement, we replace the old value ("apple") with the new one ("cherry"), resulting in the linked list at slot 3 containing only the key-value pair ("cherry", value). Similarly, when we try to insert the key "orange", we find that slot 1 is already occupied by the key "banana". We replace the old value ("banana") with the new one ("orange"), resulting in the linked list at slot 1 containing only the key-value pair ("orange", value). The resulting hash table looks like this:

```
slot 0: ("date", value)slot 1: ("orange", value)
```

• slot 2: empty

• slot 3: ("cherry", value)

(b) Chaining without replacement:

Suppose we have the same hash table and keys as in the previous example.

When we try to insert the key "cherry", we find that slot 3 is already occupied by the key "apple". In chaining without replacement, we add the key-value pair ("cherry", value) to the linked list at slot 3, resulting in the linked list containing both key-value pairs ("apple", value) and ("cherry", value).

Similarly, when we try to insert the key "orange", we find that slot 1 is already occupied by the key "banana". We add the key-value pair ("orange", value) to the linked list at slot 1, resulting in the linked list containing both key-value pairs ("banana", value) and ("orange", value).

The resulting hash table looks like this:

```
• slot 0: ("date", value)
```

• $slot 1: ("banana", value) \rightarrow ("orange", value)$

• *slot 2: empty*

• $slot 3: ("apple", value) \rightarrow ("cherry", value)$

In chaining without replacement, multiple key-value pairs can be stored in the same slot, without replacing any existing values.

3. Explain quadratic probing with example

Quadratic Probing Quadratic probing is a technique used to resolve collisions in hash tables. When a collision occurs, meaning that two or more keys are mapped to the same slot, quadratic probing searches for the next available slot by adding a quadratic sequence of values to the original hash value until an empty slot is found.

To illustrate how quadratic probing works, consider the following example. We have a hash table with 10 slots, and the following keys are inserted using a hash function:

- Slot 0: ("date", value)
- Slot 1: empty
- Slot 2: empty
- Slot 3: ("apple", value)
- Slot 4: empty
- Slot 5: empty
- Slot 6: empty
- Slot 7: ("banana", value)
- Slot 8: empty
- Slot 9: ("cherry", value)

Suppose we want to insert the key "fig" into the hash table. The hash function maps "fig" to slot 9, but we find that slot 9 is already occupied by the key "cherry".

To resolve this collision using quadratic probing, we start at slot 9 and search for the next available slot by adding a quadratic sequence of values to the original hash value.

Here's how we can find the next available slot using quadratic probing:

- (a) Starting from slot 9, we add 1 to get slot 0. But slot 0 is already occupied by "date".
- (b) We add 4 to the original hash value to get slot 13. We need to wrap around to the beginning of the hash table since the hash table only has 10 slots. So slot 13 becomes slot 3. But slot 3 is already occupied by "apple".
- (c) We add 9 to the original hash value to get slot 18. We need to wrap around again to the beginning of the hash table. So slot 18 becomes slot 8. But slot 8 is empty, so we can insert "fig" into slot 8.

We insert the key-value pair ("fig", value) into slot 8, and the resulting hash table looks like this:

- Slot 0: ("date", value)
- Slot 1: empty
- Slot 2: empty
- Slot 3: ("apple", value)
- Slot 4: empty
- Slot 5: empty
- Slot 6: empty
- Slot 7: ("banana", value)
- Slot 8: ("fig", value)
- Slot 9: ("cherry", value)

Here, quadratic probing allowed us to find the next available slot by searching through a quadratic sequence of values until an empty slot was found.