

*This registration is subject to approval(s) from faculty advisor/Course Instructor/Academic office.

Year/Semester: 2024-25/Autumn

Course Code	Course Name	Tag	Credits	Grade	Credit/Audit
AE 616	Gas Dynamics	Additional Learning	6.0		C
GC 101	Gender in the workplace	Core course	0.0		N
ME 601	Stress Analysis	Department elective	6.0		C

Year/Semester: 2024-25/Project

Course Code	Course Name	Tag	Credits	Grade	Credit/Audit
AE 796	I Stage Project	Core course	42.0		C

Year/Semester: 2023-24/Spring

Course Code	Course Name	Tag	Credits	Grade	Credit/Audit
AE 673	Fiber Reinforced Composites	Core course	6.0	AB	C
AE 678	Aeroelasticity	Core course	6.0	BB	C
AE 694	Seminar	Core course	4.0	AB	C
AE 714	Aircraft Design	Department elective	6.0	BB	C
AE 899	Communication Skills	Core course	6.0	PP	N
GC 101	Gender in the workplace	Core course	0.0	NP	N
TD 626	Technology, Society and Development	Institute elective	6.0	BB	C

Year/Semester: 2023-24/Autumn

Course Code	Course Name	Tag	Credits	Grade	Credit/Audit
AE 649	Finite Element Method	Core course	6.0	BC	C
AE 705	Introduction to Flight	Core course	6.0	BB	C
AE 709	Aerospace Structures	Core course	6.0	BB	C
AE 715	Structural Dynamics	Core course	6.0	BC	C
AE 727	Aircraft Structural Mechanics Lab.	Core course	4.0	BB	C
GC 101	Gender in the workplace	Core course	0.0	NP	N
TA 101	Teaching Assistant Skill Enhancement & Training (TASET)	Core course	0.0	PP	N

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M.Tech., Aerospace Engineering

Finite Element Analysis

Project report (AE-649)

Master in Technology

in

Aerospace Engineering

By

Yarranagula Krishna Teja

(23M0036)

Under the Guidance of

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```
%% Rayliegh Ritz Method %%
```

```
clear all
```

```
syms x w1 w2
```

```
syms C1 C2
```

```
L=1
```

```
x_=[0:L]
```

```
u__x= C1*x*(1-x) + C2*x*x*(1-x)
```

```
du__dx= diff(u__x)
```

```
du___dx=diff(du__dx)
```

```
%% rayleigh ritz
```

```
disp('rayleigh ritz METHOD');
```

```
R__x= -(du___dx)-u__x+x^2
```

```
w1=x*(1-x)
```

```
w2=x*x*(1-x)
```

```
G_K_1 = (R__x)*(w1)
```

```
G_K_2 = (R__x)*(w2)
```

```
expand(G_K_1)
```

```
expand(G_K_2)
```

```
G_K_1 = int(G_K_1, x, 0, L)
```

```
G_K_2 = int(G_K_2, x, 0, L)
```

```
[c1,c2] = solve(G_K_1,G_K_2)
```

```
%Clear all
```

```
% defining variable as symbols
```

```
% Variable for trail polynomial soln
```

```
%Trial soln
```

```
%Residue EQN **
```

```
%integrating over domain
```

```
% Tapered beam
```

```
%2 elements
```

```
B=[1 0 0 0; 0 1 1 0;0 0 0 1]
```

```
A=B.'
```

```
k1=(2.5*10*200000/(100/2))
```

```
k2=(1.5*10*200000/(100/2))
```

```
Ke=[k1 -k1 0 0;-k1 k1 0 0;0 0 k2 -k2;0 0 -k2 k2]
```

```
K=B*Ke*A
```

```
error = (100*(-0.00267+0.00275))/0.00275
```

```
%3 elements
```

```
B_=[1 0 0 0 0 0; 0 1 1 0 0 0;0 0 0 1 1 0;0 0 0 0 0 1]
```

```
A_=B_.'
```

```
k_1=(2.67*10*200000/(100/3))
```

```
k_2=(2*10*200000/(100/3))
```

```
k_3=(1.33*10*200000/(100/3))
```

```
Ke=[k_1 -k_1 0 0 0 0;-k_1 k_1 0 0 0 0;0 0 k_2 -k_2 0 0;0 0 -k_2 k_2 0 0;0 0 0 0 k_3 -k_3;0 0 0 0 -k_3 k_3] ✓
```

```
K_=B_*Ke*A_
```

```
C=[280200 -120000 0;-120000 199800 -79800;0 -79800 79800]
```

```
D=[0; 0; 100]
```

```
Y=linsolve(C,D)
```

```
error=(100*(-0.0027+0.00275))/0.00275
```

```
## petroGlaerkin_sample.....##
clear all                                     %Clear all
syms x w1                                    % defining variable as symbols
syms C1                                       % Variable for trail polynomial soln
L=1
x_=[0:L]
u__x= 1-x + C1*x*(1-x)                     %Trial soln
du__dx= diff(u__x)
du___dx=diff(du__dx)
%% petrov Galerkin Method
disp('petrov GALERKIN METHOD');
R__x= -2*u__x*du___dx+du__dx*du__dx-4      %Residue EQN **
w1=1
G_K_1 = (R__x)*(w1)
expand(G_K_1)
G_K_1 = int(G_K_1, x, 0, L)                 %integrating over domain
G_K = solve(G_K_1)
C_1= double(G_K)
```

```
## Least Sqaure Method .....###
clear all                                %Clear all
syms x w1                                % defining variable as symbols
syms C1                                  % Variable for trail polynomial soln
L=1
x_=[0:L]
u__x= 1-x + C1*x*(1-x)                  %Trial soln
du__dx= diff(u__x)
du___dx=diff(du__dx)
%% least square method
disp('least square METHOD');
R__x= -2*u__x*du___dx+du__dx*du__dx-4 %Residue EQN **
w1=2*C1+2
G_K_1 = (R__x)*(w1)
expand(G_K_1)
G_K_1 = int(G_K_1, x, 0, L)              %integrating over domain
G_K = solve(G_K_1)
C_1= double(G_K)
```

```
clear all                                %Clear all
syms x w1                                % defining variable as symbols
syms C1                                  % Variable for trail polynomial soln
L=1
x_=[0:L]
u__x= 1-x + C1*x*(1-x)                  %Trial soln
du__dx= diff(u__x)
du___dx=diff(du__dx)
%% Galerkin Method
disp('GALERKIN METHOD');
R__x= -2*u__x*du___dx+du__dx*du__dx-4    %Residue EQN **
w1=x*(1-x)
G_K_1 = (R__x)*(w1)
expand(G_K_1)
G_K_1 = int(G_K_1, x, 0, L)              %integrating over domain
G_K = solve(G_K_1)
C_1= double(G_K)
```

```
%.....  
% MATLAB codes for Finite Element Analysis  
% Discrete_Systems.m  
  
% clear memory  
  
clear all  
  
% elementNodes: connections at elements  
  
elementNodes=[1 2;2 3;2 4];  
  
% numberElements: number of Elements  
  
numberElements=size(elementNodes,1);  
  
% By using the MATLAB function size, that returns the number  
%of lines and columns of a rectangular matrix, we can detect  
%the number of elements by inspecting the number of lines of  
%matrix elementNodes.  
  
% numberNodes: number of nodes  
  
numberNodes=4;  
  
% for structure:  
% displacements: displacement vector  
% force : force vector
```



```
% stiffness: stiffness matrix

% initializing the matrices

displacements=zeros(numberNodes,1);
force=zeros(numberNodes,1);
stiffness=zeros(numberNodes);

% applied load at node 2
force(2)=10.0;

% computation of the system stiffness matrix
% We compute now the stiffness matrix for each element in turn and then assemble
% it in the global stiffness matrix.

for e=1:numberElements;
% elementDof: element degrees of freedom (Dof)
elementDof=elementNodes(e,:) ;

stiffness(elementDof,elementDof)=...
stiffness(elementDof,elementDof)+[1 -1;-1 1];
end

% boundary conditions and solution
% prescribed dofs
prescribedDof=[1;3;4];
% free Dof : activeDof
```

```
activeDof=setdiff([1:numberNodes],[prescribedDof]);
```

```
% solution
```

```
displacements=stiffness(activeDof,activeDof)\force(activeDof);
```

```
% positioning all displacements
```

```
displacements1=zeros(numberNodes,1);
```

```
displacements1(activeDof)=displacements;
```

```
% output displacements/reactions
```

```
outputDisplacementsReactions(displacements1,stiffness,numberNodes,prescribedDof)
```

```
%.....
```

```
function outputDisplacementsReactions(displacements1,stiffness,GDof,prescribedDof)
```

```
% output of displacements and reactions in
```

```
% tabular form
```

```
% GDof: total number of degrees of freedom of
```

```
% the problem
```

```
% displacements
```

```
%displacements=displacements1;
```

```
GDof=4;
```

```
jj=[1:GDof];
```

```
disp('displacements')
```

```
 [ jj.' displacements1]
```

```
% reactions
```

```
F=stiffness*displacements1;
```

```
reactions=F(prescribedDof);
```

```
disp('reactions')
```

```
[prescribedDof reactions]
```

```
end
```

```
%.....
```