LU ICPC kladīte;)

Contents

1. C++ programming language	
1.1. Input/Output disable sync	1
1.2. Optimization pragmas	
1.3. Printing structs	
1.4. Lambda func for sorting	1
2. Algebra	1
2.1. Binary exponentiation	1
2.2. Extended euclidean	
2.3. Modular inversion & division	
2.4. Linear Diophantine equation	
2.5. Linear sieve	
2.6. Matrix multiplication	
2.7. FFT	
3. Geometry	
3.1. Dot product	
3.2. Cross product	
3.3. Line-point distance	
3.4. Shoelace formula	
3.5. Segment to line	
3.6. Three point orientation	
3.7. Line-line intersection	
3.8. Check if two segments intersect	
3.9. Heron's formula	
3.10. Graham's scan	
3.11. Circumradius	
4. Data structures	
4.1. Treap	
4.2. Lazy segment tree	
4.3. Sparse table	
4.4. Fenwick tree	
4.5. Trie	
4.6. Aho-Corasick	
4.7. Disjoint Set Union	
4.8. Merge sort tree	
5. Graph algorithms	
5.1. Bellman-Ford	
5.2. Dijkstra	
5.3. Floyd-Warshall	6
5.4. Bridges & articulations	6
5.5. Dinic's max flow / matching	
5.6. Flow with demands	7
5.7. Kosaraju's algorithm	7
5.8. Lowest Common Ancestor	7
5.9. General matching in a graph	7
6. String Processing	7
6.1. Knuth-Morris-Pratt (KMP)	
• • •	

	6.2. Suffix Array	
	6.3. Longest common prefix with SA	
	6.4. Rabin-Karp	
	6.5. Z-function	
	6.6. Manacher's	
7. Dynamic programming		
	7.1. Convex hull trick	
	7.2. Longest Increasing Subsequence	
	7.3. SOS DP (Sum over Subsets)	
	,	

C++ programming language

1.1. Input/Output disable sync

```
ios_base::sync_with_stdio(false);
cin.tie(NULL); cout.tie(NULL);
```

1.2. Optimization pragmas

```
// change to 03 to disable fast-math for geometry problems
#pragma GCC optimize("Ofast,unroll-loops")
#pragma GCC target("avx2,bmi,bmi2,lzcnt,popcnt,tune=native")
```

1.3. Printing structs

```
ostream& operator<<(ostream& os, const pair<int, int>& p) {
    return os << "(" << p.first << ", " << p.second << ")";
}</pre>
```

1.4. Lambda func for sorting

```
using ii = pair<int,int>;
vector<ii> fracs = {{1, 2}, {3, 4}, {1, 3}};
// sort positive rational numbers
sort(fracs.begin(), fracs.end(),
   [](const ii& a, const ii& b) {
   return a.fi*b.se < b.fi*a.se;
});</pre>
```

Algebra

2.1. Binary exponentiation

```
ll m_pow(ll base, ll exp, ll mod) {
   base %= mod;
   ll result = 1;
   while (exp > 0) {
      if (exp & 1) result = ((ll)result * base) % mod;
      base = ((ll)base * base) % mod;
      exp >>= 1;
   }
   return result;
}
```

2.2. Extended euclidean

2.3. Modular inversion & division

gcd_ext defined in Section 2.2.

```
 \exists x(a \cdot x \equiv 1 \pmod{m}) \Leftrightarrow \gcd(a,m) = 1  int mod_inv(int b, int m) {    int x, y;    int g = gcd_ext(b, m, &x, &y);    if (g != 1) return -1;    return (x%m + m) % m; } int m_divide(ll a, ll b, ll m) {    int inv = mod_inv(b, m);    assert(inv != -1);    return (inv * (a % m)) % m; }
```

2.4. Linear Diophantine equation

gcd ext defined in Section 2.2.

```
\left\{x = x_0 + k \cdot \frac{b}{g}; y = y_0 - k \cdot \frac{a}{g}\right\}
```

 $a \cdot x + b \cdot y = c$

```
bool find_x0_y0(int a, int b, int c, int &x0, int &y0, int &g) {
    g = gcd_ext(abs(a), abs(b), x0, y0);
    if (c % g) return false;
    x0 *= c / g;
    y0 *= c / g;
    if (a < 0) x0 = -x0;
    if (b < 0) y0 = -y0;
    return true;
}</pre>
```

2.5. Linear sieve const int N = 10000000:

```
vector<int> lp(N+1);
vector<int> pr;
for (int i=2; i <= N; ++i) {
    if (lp[i] == 0) {
        lp[i] = i;
        pr.push back(i);
    for (int j = 0; i * pr[j] <= N; ++j) {
        lp[i * pr[j]] = pr[j];
        if (pr[j] == lp[i]) break;
}
2.6. Matrix multiplication
struct Matrix:vector<vector<int>>
{
    // "inherit" vector's constructor
    using vector::vector;
    Matrix operator *(Matrix other)
        int rows = size();
        int cols = other[0].size();
        Matrix res(rows, vector<int>(cols));
        for(int i=0;i<rows;i++)</pre>
            for(int j=0;j<other.size();j++)</pre>
                for(int k=0:k<cols:k++)</pre>
                     res[i][k]+=at(i).at(j)*other[j][k];
        return res:
};
```

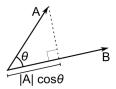
2.7. FFT

```
using ld = long double;
const int N = 1 << 18;
const ld PI = acos(-1.0);
struct T {
 ld x, y;
 T() : x(0), y(0) \{ \}
 T(ld a, ld b=0) : x(a), y(b) {}
 T operator/=(ld k) { x/=k; y/=k; return (*this); }
 T operator*(T a) const { return T(x*a.x - y*a.y, x*a.y + y*a.x); }
 T operator+(T a) const { return T(x+a.x, y+a.y); }
 T operator-(T a) const { return T(x-a.x, y-a.y); }
};
void fft(T* a, int n, int s) {
 for (int i=0, j=0; i<n; i++) {
   if (i>j) swap(a[i], a[j]);
   for (int l=n/2; (j^=l) < l; l>>=1);
  for(int i = 1; (1<<ii) <= n; i++){
   int M = 1 << i:
   int K = M \gg 1:
   T wn = T(\cos(s*2*PI/M), \sin(s*2*PI/M));
   for(int j = 0; j < n; j += M) {
     T w = T(1, 0);
      for(int l = j; l < K + j; ++l){}
       T t = w*a[l + K];
        a[l + K] = a[l]-t:
        a[l] = a[l] + t;
        w = wn*w:
}
void multiply(T* a, T* b, int n) {
   while (n&(n-1)) n++; // ensure n is a power of two
   fft(a,n,1);
   fft(b,n,1);
   for (int i = 0; i < n; i++) a[i] = a[i]*b[i];</pre>
   fft(a,n,-1);
    for (int i = 0; i < n; i++) a[i] /= n;
}
int main() {
 // Example polynomials: (2 + 3x) and (1 - x)
 T a[10] = \{T(2), T(3)\};
 T b[10] = \{T(1), T(-1)\};
 multiply(a, b, 4);
 for (int i = 0; i < 10; i++)
   std::cout << int(a[i].x) << " ";
```

Geometry

3.1. Dot product

$$\begin{aligned} a \cdot b &= |a| \; |b| \cos(\theta) \\ a \cdot b &= a_x b_x + a_y b_y \\ \theta &= \arccos\bigg(\frac{a_x b_x + a_y l}{|a| \; |b|} \end{aligned}$$



Projection of a onto b:

$$\frac{a\cdot b}{|b|}$$

3.2. Cross product

$$a \times b = |a| |b| \sin(\theta)$$
$$a \times b = a_x b_y - a_y b_x$$

 θ is positive if a is clockwise from b

3.3. Line-point distance

Line given by ax + by + c = 0 and point (x_0, y_0) .

$$distance = \frac{|ax_0 + by_0 + c|}{\sqrt{a^2 + b^2}}$$

The coordinates of this point are:

$$x = \frac{b(bx_0 - ay_0) - ac}{a^2 + b^2}$$

$$y = \frac{a(-bx_0 + ay_0) - bc}{a^2 + b^2}$$

3.4. Shoelace formula

$$2A = \sum_{i=1}^{n} \begin{vmatrix} x_i & y_i \\ x_{i+1} & y_{i+1} \end{vmatrix}$$

3.5. Segment to line

$$\begin{split} \left(\left(P_x,P_y\right),\left(Q_x,Q_y\right)\right) \to Ax + By + C &= 0 \\ A &= P_y - Q_y \\ B &= Q_x - P_x \\ C &= -AP_x - BP_y \end{split}$$

Rationing the obtained line equation:

- 1. divide A,B,C by their GCD
- 2. if A < 0 or $A = 0 \wedge B < 0$ then multiply all by -1

3.6. Three point orientation

3.7. Line-line intersection

From system of linear equations derived Cramer's rule:

$$x = -\frac{c_1b_2 - c_2b_1}{a_1b_2 - a_2b_1}$$
$$y = -\frac{a_1c_2 - a_2c_1}{a_1b_2 - a_2b_1}$$

If the denominator equals zero, the lines are parallel or coincident.

3.8. Check if two segments intersect

```
bool on segment(Point p, Point q, Point r)
   if (q.x \le max(p.x, r.x)) \& q.x \ge min(p.x, r.x) \& \&
       q.y \le \max(p.y, r.y) \&\& q.y >= \min(p.y, r.y))
       return true:
    return false;
bool do intersect(Point p1, Point q1, Point p2, Point q2)
   // Find the four orientations needed for general and
   // special cases
   int o1 = orientation(p1, q1, p2);
   int o2 = orientation(p1, q1, q2);
   int o3 = orientation(p2, q2, p1);
   int o4 = orientation(p2, q2, q1);
   if (o1 != o2 && o3 != o4)
        return true;
   if (o1 == 0 && on_segment(p1, p2, q1)) return true;
   if (o2 == 0 && on segment(p1, q2, q1)) return true;
   if (o3 == 0 && on segment(p2, p1, q2)) return true;
   if (04 == 0 \&\& on segment(p2, g1, g2)) return true:
```

3.9. Heron's formula

Let a, b, c - sides of a triangle. Then the area A is:

$$A = \frac{1}{4}\sqrt{(a+b+c)(-a+b+c)(a-b+c)(a+b-c)} = \frac{1}{4}\sqrt{4a^2b^2 - (a^2+b^2-c^2)^2}$$

Numerically stable version:

$$a \geq b \geq c, A = \frac{1}{4} \sqrt{(a + (b + c))(c - (a - b))(c + (a - b))(a + (b - c))}$$

3.10. Graham's scan

```
struct pt {double x, y;};
int orientation(pt a, pt b, pt c) {
    double v = a.x*(b.y-c.y)+b.x*(c.y-a.y)+c.x*(a.y-b.y);
    if (v < 0) return -1: // clockwise
    if (v > 0) return +1: // counter-clockwise
    return 0;
}
bool cw(pt a, pt b, pt c, bool include_collinear) {
    int o = orientation(a, b, c);
    return o < 0 || (include_collinear && o == 0);</pre>
bool collinear(pt a, pt b, pt c) { return orientation(a, b, c) ==
0; }
void convex hull(vector<pt>& a, bool include_collinear = false) {
    pt p\theta = *min element(a.begin(), a.end(), [](pt a, pt b) {
        return make pair(a.y, a.x) < make pair(b.y, b.x);</pre>
    sort(a.begin(), a.end(), [&p0](const pt& a, const pt& b) {
        int o = orientation(p0, a, b);
        if (o == 0)
            return (p0.x-a.x)*(p0.x-a.x) + (p0.v-a.v)*(p0.v-a.v)
                < (p0.x-b.x)*(p0.x-b.x) + (p0.y-b.y)*(p0.y-b.y);
        return o < 0:
    });
    if (include collinear) {
        int i = (int)a.size()-1;
        while (i \ge 0 \&\& collinear(p0, a[i], a,back())) i--:
        reverse(a.begin()+i+1, a.end());
    vector<pt> st:
    for (int i = 0; i < (int)a.size(); i++) {</pre>
         while (st.size() > 1 \&\& !cw(st[st.size()-2], st.back(),
a[i], include collinear))
            st.pop_back();
        st.push_back(a[i]);
    }
    a = st;
}
```

3.11. Circumradius

Let $a,\,b,\,c$ - sides of a triangle. A - area of the triangle. Then the circumradius is:

$$R = \frac{abc}{4A}$$

Data structures

4.1. Treap

```
// Implicit segment tree implementation
struct Node{
    int value. cnt. priority:
    Node *left, *right:
    Node(int p) : value(p), cnt(1), priority(gen()), left(NULL),
right(NULL) {};
};
typedef Node* pnode;
int get(pnode g){
    if(!q) return 0;
    return q->cnt;
}
void update cnt(pnode &q){
    if(!q) return;
    q - cnt = get(q - left) + get(q - right) + 1;
}
void merge(pnode &T, pnode lef, pnode rig){
    if(!lef) {T=rig:return:}
    if(!rig){T=lef;return;}
    if(lef->priority > rig->priority){
        merge(lef->right, lef->right, rig);
        T = lef:
    else{
        merge(ria->left, lef, ria->left);
        T = ria:
    update cnt(T);
}
void split(pnode cur, pnode &lef, pnode &rig, int key){
    if(!cur){
        lef = rig = NULL;
        return;
    int id = get(cur->left) + 1;
    if(id <= key){</pre>
        split(cur->right, cur->right, rig, key - id);
        lef = cur;
    }
        split(cur->left, lef, cur->left, key);
        riq = cur;
    }
    update cnt(cur);
}
```

4.2. Lazy segment tree

```
struct SumSeamentTree{
    vector<ll> S. O. L:
    void build(ll ti, ll tl, ll tr){
        if(tl==tr){S[ti]=0[tl]; return;}
        build(ti*2, tl, (tl+tr)/2);
        build((ti*2)+1, ((tl+tr)/2)+1, tr);
        S[ti]=S[ti*2]+S[(ti*2)+1];
    void push(ll ti, ll tl, ll tr){
        S[ti] += L[ti]*(tr-tl+1);
        if(tl==tr){L[ti]=0;return;}
        L[ti+ti] \leftarrow L[ti], L[ti+ti+1] \leftarrow L[ti];
        L[ti] = 0;
   ll query(ll ti, ll tl, ll tr, ll i, ll j){
        push(ti, tl, tr);
        if(i<=tl&&tr<=j) return S[ti];</pre>
        if(tr<i||tl>j) return 0;
        ll a = query(ti*2, tl, (tl+tr)/2, i, j);
        ll b = query((ti*2)+1, ((tl+tr)/2)+1,tr, i, j);
        return a+b;
    void update(ll ti, ll tl, ll tr, ll i, ll j, ll v){
        if(i<=tl&&tr<=j){L[ti]+=v;return;}</pre>
        if(tr<i||tl>j) return;
        S[ti]+=v*(i-j+1);
        update(ti*2, tl, (tl+tr)/2, i, j, v);
        update((ti*2)+1, ((tl+tr)/2)+1, tr, i, j, v);
   }:
   ST(vector<ll> &V){
        0 = V:
        S.resize(0.size()*4, 0):
       L.resize(0.size()*4, 0):
        build(1, 0, 0.size()-1);
   }
};
4.3. Sparse table
const int N;
const int M; //log2(N)
int sparse[N][M];
void build() {
  for(int i = 0; i < n; i++)
    sparse[i][0] = v[i];
  for(int j = 1; j < M; j++)
    for(int i = 0; i < n; i++)
      sparse[i][i] =
       i + (1 << j - 1) < n
        ? min(sparse[i][j-1], sparse[i+(1 << j-1)][j-1])
        : sparse[i][j - 1];
}
int query(int a, int b){
 int pot = 32 - builtin clz(b - a) - 1;
  return min(sparse[a][pot], sparse[b - (1 << pot) + 1][pot]);</pre>
```

4.4. Fenwick tree

```
struct FenwickTree {
    vector<ll> bit; // binary indexed tree
    int n;
    FenwickTree(int n) {
        this->n = n;
        bit.assign(n, 0);
   }
   ll sum(int r) {
        ll ret = 0;
        for (; r \ge 0; r = (r \& (r + 1)) - 1)
            ret += bit[r];
        return ret;
   }
   ll sum(int l, int r) { // l to r of the og array INCLUSIVE
        return sum(r) - sum(l - 1);
    void add(int idx, ll delta) {
        for (; idx < n; idx = idx | (idx + 1))
           bit[idx] += delta:
   }
};
4.5. Trie
const int K = 26;
struct Vertex {
    int next[K]:
   bool output = false;
    Vertex() {fill(begin(next), end(next), -1);}
};
vector<Vertex> t(1); // trie nodes
void add_string(string const& s) {
   int v = 0;
    for (char ch : s) {
        int c = ch - 'a';
        if (t[v].next[c] == -1) {
            t[v].next[c] = t.size();
            t.emplace_back();
        v = t[v].next[c];
    t[v].output = true;
```

University of Latvia 5/9

4.6. Aho-Corasick

```
const int K = 26:
struct Vertex {
    int next[K]:
    bool output = false:
    int p = -1; // parent node
    char pch; // "transition" character from parent to this node
    int link = -1; // fail link
   int qo[K]; // if need more memory can delete this and use "next"
    // additional potentially useful things
    int depth = -1;
    // longest string that has an output from this vertex
    int exitlen = -1;
    Vertex(int p=-1, char ch='$') : p(p), pch(ch) {
        fill(begin(next), end(next), -1);
        fill(begin(go), end(go), -1);
    }
};
vector<Vertex> t(1);
void add string(string const& s) {
    int v = 0:
    for (char ch : s) {
        int c = ch - 'a':
        if (t[v].next[c] == -1) {
            t[v].next[c] = t.size();
            t.emplace back(v, ch); // !!!!! ch not c
        }
        v = t[v].next[c];
    t[v].output = true;
int go(int v, char ch);
int get link(int v) {
    if (t[v].link == -1) {
        if (v == 0 || t[v].p == 0)
            t[v].link = 0;
        else
            t[v].link = go(get_link(t[v].p), t[v].pch);
    return t[v].link;
}
int go(int v, char ch) {
    int c = ch - 'a';
    if (t[v].go[c] == -1) {
        if (t[v].next[c] != -1)
            t[v].go[c] = t[v].next[c];
            // !!!!! ch not c
            t[v].go[c] = v == 0 ? 0 : go(get link(v), ch);
    return t[v].go[c];
```

```
// int go(int v, char ch) { // go without the go[K] variable
      int c = ch - 'a';
      if (t[v].next[c] == -1) {
//
//
          // !!!!! ch not c
//
           t[v].next[c] = v == 0 ? 0 : qo(qet link(v), ch);
//
//
      return t[v].next[c];
// }
// helper function
int get depth(int v){
   if (t[v].depth == -1){
       if (v == 0) {
           t[v].depth = 0;
        } else {
           t[v].depth = get depth(t[v].p)+1;
   }
    return t[v].depth:
// helper function
int get exitlen(int v){
   if (t[v].exitlen == -1){
       if (v == 0){
            t[v].exitlen = 0;
       } else if (t[v].output) {
            t[v].exitlen = get depth(v);
            t[v].exitlen = get_exitlen(get_link(v));
   }
    return t[v].exitlen;
4.7. Disjoint Set Union
struct DSU {
   vector<int> parent, rank;
   DSU(int n) {
        parent.resize(n); rank.resize(n);
        for (int i = 0; i < n; i++)
           parent[i] = i;
   }
   int root(int a) {
        if (parent[a] == a) return a;
        return parent[a] = find(parent[a]);
   void unite(int a, int b) {
       a = find(a), b = find(b);
       if (a == b) return;
       if (rank[a] < rank[b]) {</pre>
           parent[a] = b;
       } else if (rank[a] > rank[b]) {
           parent[b] = a;
        } else {
           parent[b] = a;
            rank[a] = rank[a] + 1;
   }
};
```

4.8. Merge sort tree

```
struct MergeSortTree {
    int size:
    vector<vector<ll>> values:
    void init(int n){
        size = 1;
        while (size < n){</pre>
            size *= 2;
        values.resize(size*2, vl(0));
    void build(vl &arr, int x, int lx, int rx){
        if (rx - lx == 1){
            if (lx < arr.size()){</pre>
                values[x].pb(arr[lx]);
            } else {
                values[x].pb(-1);
            }
            return;
        int m = (lx+rx)/2:
        build(arr, 2 * x + 1, lx, m);
        build(arr, 2 * x + 2, m, rx):
        int i = 0:
        int j = 0;
        int asize = values[2*x+1].size();
        while (i < asize && i < asize){
            if (values[2*x+1][i] < values[2*x+2][j]){</pre>
                values[x].pb(values[2*x+1][i]);
                1++:
            } else {
                values[x].pb(values[2*x+2][j]);
                1++;
            }
        while (i < asize) {</pre>
            values[x].pb(values[2*x+1][i]);
        while (j < asize){</pre>
            values[x].pb(values[2*x+2][j]);
            j++;
        }
    void build(vl &arr){
        build(arr, 0, 0, size);
```

```
int calc(int l, int r, int x, int lx, int rx, int k){
   if (lx >= r || rx <= l) return 0;
    // (elements strictly less than k currently)
   if (lx >= l \& rx <= r)  { // CHANGE HEURISTIC HERE
        int lft = -1;
        int rght = values[x].size();
        while (rght - lft > 1){
            int mid = (lft+rght)/2;
            if (values[x][mid] < k){</pre>
                lft = mid;
            } else {
                rght = mid;
            }
        }
        return lft+1;
    int m = (lx+rx)/2:
    int values1 = calc(l, r, 2*x+1, lx, m, k):
    int values2 = calc(l, r, 2*x+2, m, rx, k):
    return values1 + values2:
int calc(int l, int r, int k){
    return calc(l, r, 0, 0, size, k);
```

Graph algorithms

5.1. Bellman-Ford

};

```
void solve()
    vector<int> d(n, INF);
    d[v] = 0;
    for (::) {
        bool any = false;
        for (Edge e : edges)
            if (d[e.a] < INF)
                if (d[e.b] > d[e.a] + e.cost) {
                    d[e.b] = d[e.a] + e.cost;
                    any = true;
        if (!any)
            break;
    // display d, for example, on the screen
}
```

5.2. Dijkstra

```
vector<int> adj[N], adjw[N];
int dist[N];
memset(dist, 63, sizeof(dist));
priority_queue<pii> pq;
```

```
pq.push(mp(0,0));
while (!pq.empty()) {
 int u = pq.top().nd;
 int d = -pq.top().st;
 pq.pop();
  if (d > dist[u]) continue;
  for (int i = 0; i < adj[u].size(); ++i) {</pre>
   int v = adj[u][i];
   int w = adjw[u][i];
   if (dist[u] + w < dist[v])</pre>
      dist[v] = dist[u]+w, pq.push(mp(-dist[v], v));
 }
}
5.3. Floyd-Warshall
int adj[N][N]; // no-edge = INF
for (int k = 0; k < n; ++k)
 for (int i = 0; i < n; ++i)
   for (int j = 0; j < n; ++j)
      adj[i][j] = min(adj[i][j], adj[i][k]+adj[k][j]);
5.4. Bridges & articulations
// Articulation points and Bridges O(V+E)
int par[N], art[N], low[N], num[N], ch[N], cnt;
void articulation(int u) {
 low[u] = num[u] = ++cnt;
  for (int v : adj[u]) {
   if (!num[v]) {
      par[v] = u; ch[u]++;
      articulation(v);
      if (low[v] >= num[u]) art[u] = 1;
      if (low[v] > num[u]) { /* u-v bridge */ }
      low[u] = min(low[u], low[v]);
   else if (v != par[u]) low[u] = min(low[u], num[v]);
}
for (int i = 0; i < n; ++i) if (!num[i])
 articulation(i), art[i] = ch[i]>1;
5.5. Dinic's max flow / matching
Time complexity:
• generally: O(EV^2)
• small flow: O(F(V+E))
• bipartite graph or unit flow: O(E\sqrt{V})
Usage:
• dinic()

    add_edge(from, to, capacity)
```

• recover() (optional)

```
const ll N=1e5+5, INF=1e9;
struct edge{ll v, c, f;};
ll src=0, snk=N-1, h[N], ptr[N];
vector<edge> edgs;
vector<ll> q[N];
void add edge(ll u, ll v, ll c) {
    edgs.push_back(\{v,c,0\}), edgs.push_back(\{u,0,0\});
    ll k=edgs.size();
    g[u].push_back(k), g[v].push_back(k+1);
bool bfs() {
    memset(h, 0, sizeof(h));
    queue<ll> q;
    h[src]=1;
    q.push(src);
    while(!q.emptv()){
        ll u=q.front();q.pop();
        for(ll i:a[u]){
            ll v=edgs[i].v;
            if(!h[v]&&edgs[i].f<edgs[i].c)</pre>
                q.push(v),h[v]=h[u]+1;
        }
    }
    return h[snk];
ll dfs(ll u, ll flow){
    if(!flow or u==snk) return flow;
    for(ll &i=ptr[u];i<g[u].size();i++){</pre>
        edge &dir=edgs[g[u][i]],&rev=edgs[g[u][i]^1];
        if(h[dir.v]!=h[u]+1) continue;
        ll inc=min(flow,dir.c-dir.f);
        inc=dfs(dir.v,inc);
        if(inc){ dir.f+=inc,rev.f-=inc; return inc;}
    }
    return 0;
}
ll dinic(){
    ll flow=0:
    while(bfs()){
        memset(ptr.0.sizeof(ptr));
        while(ll inc=dfs(src,INF)) flow += inc;
    }
    return flow;
vector<pair<ii,ll>> recover() {
    vector<pair<ii.ll>> res:
    for(ll i=0;i<edgs.size();i+=2){</pre>
        if(edgs[i].f>0){
            ll v=edgs[i].v, u=edgs[i^1].v;
            res.push back({{u,v},edgs[i].f});
        }
    }
    return res;
}
```

5.6. Flow with demands

Finding an arbitrary flow

- Assume a network with [L;R] on edges (some may have L=0), let's call it old network.
- Create a New Source and New Sink (this will be the src and snk for Dinic).
- Modelling network:
- 1. Every edge from the old network will have cost R-L
- 2. Add an edge from New Source to every vertex v with cost:
 - S(L) for every (u, v). (sum all L that LEAVES v)
- 3. Add an edge from every vertex v to New Sink with cost:
 - S(L) for every (v, w). (sum all L that ARRIVES v)
- 4. Add an edge from Old Source to Old Sink with cost INF (circulation problem)
- The Network will be valid if and only if the flow saturates the network (max flow == S(L))

Finding Min Flow

- To find min flow that satisfies just do a binary search in the (Old Sink
 Old Source) edge
- The cost of this edge represents all the flow from old network
- Min flow = S(L) that arrives in Old Sink + flow that leaves (Old Sink -> Old Source)

5.7. Kosaraju's algorithm

```
const int N = 2e5 + 5;
vector<int> adj[N], adjt[N];
int n, ordn, scc_cnt, vis[N], ord[N], scc[N];
//Directed Version
void dfs(int u) {
 vis[u] = 1;
 for (auto v : adj[u]) if (!vis[v]) dfs(v);
 ord[ordn++] = u;
void dfst(int u) {
 scc[u] = scc cnt, vis[u] = 0;
 for (auto v : adjt[u]) if (vis[v]) dfst(v);
// add edge: u -> v
void add edge(int u, int v){
 adi[u].push back(v):
 adjt[v].push back(u);
// run kosaraiu
void kosaraju(){
 for (int i = 1; i <= n; ++i) if (!vis[i]) dfs(i);
 for (int i = ordn - 1; i \ge 0; --i) if (vis[ord[i]]) scc cnt++,
dfst(ord[i]):
}
```

5.8. Lowest Common Ancestor

```
const int N = 1e6. M = 25:
int anc[M][N], h[N], rt;
// TODO: Calculate h[u] and set anc[0][u] = parent of node u for
// build (sparse table)
anc[0][rt] = rt; // set parent of the root to itself
for (int i = 1; i < M; ++i)
 for (int j = 1; j \le n; ++j)
   anc[i][j] = anc[i-1][anc[i-1][j]];
// query
int lca(int u, int v) {
 if (h[u] < h[v]) swap(u, v);
 for (int i = M-1; i \ge 0; --i) if (h[u]-(1 << i) \ge h[v])
   u = anc[i][u];
 if (u == v) return u;
  for (int i = M-1; i \ge 0; --i) if (anc[i][u] != anc[i][v])
   u = anc[i][u], v = anc[i][v];
  return anc[0][u]:
```

5.9. General matching in a graph

```
vector<int> Blossom(vector<vector<int>> graph){
  int n = graph.size();
  int timer = -1;
  vector<int> mate(n, -1), label(n), parent(n),
              orig(n), aux(n, -1), q;
  auto lca = [\&](int x, int y) {
    for (timer++; ; swap(x, y)) {
     if (x == -1) continue;
     if (aux[x] == timer) return x;
      aux[x] = timer;
     x = (mate[x] == -1 ? -1 : orig[parent[mate[x]]]);
  };
  auto blossom = [&](int v, int w, int a) {
    while (orig[v] != a) {
     parent[v] = w; w = mate[v];
     if (label[w] == 1) label[w] = 0, q.push_back(w);
     orig[v] = orig[w] = a; v = parent[w];
  };
  auto augment = [&](int v) {
   while (v != -1) {
     int pv = parent[v]. nv = mate[pv]:
     mate[v] = pv; mate[pv] = v; v = nv;
  };
  auto bfs = [&](int root) {
   fill(label.begin(), label.end(), -1);
   iota(orig.begin(), orig.end(), 0);
   a.clear():
    label[root] = 0; q.push back(root);
    for (int i = 0; i < (int)q.size(); ++i) {
     int v = q[i];
     for (auto x : graph[v]) {
       if (label[x] == -1) {
          label[x] = 1; parent[x] = v;
          if (mate[x] == -1)
            return augment(x), 1;
          label[mate[x]] = 0; q.push_back(mate[x]);
        } else if (label[x] == 0 \&\& \text{ orig}[v] != \text{ orig}[x]) {
          int a = lca(orig[v], orig[x]);
          blossom(x, v, a); blossom(v, x, a);
       }
     }
   }
   return 0;
  };
  for (int i = 0; i < n; i++)
   if (mate[i] == -1)
     bfs(i):
  return mate:
```

String Processing

6.1. Knuth-Morris-Pratt (KMP)

```
// Knuth-Morris-Pratt - String Matching O(n+m)
char s[N], p[N];
int b[N], n, m; // n = strlen(s), m = strlen(p);
void kmppre() {
  b[0] = -1;
  for (int i = 0, j = -1; i < m; b[++i] = ++j)
    while (j \ge 0 \text{ and } p[i] != p[j])
      i = b[i];
}
void kmp() {
  for (int i = 0, j = 0; i < n;) {
    while (j \ge 0 \text{ and } s[i] != p[j]) j=b[j];
    i++, j++;
    if (j == m) {
     // match position i-j
     j = b[j];
  }
}
6.2. Suffix Array
// s.push('$');
vector<int> suffix array(string &s){
  int n = s.size(), alph = 256;
  vector<int> cnt(max(n, alph)), p(n), c(n);
  for(auto c : s) cnt[c]++;
  for(int i = 1; i < alph; i++) cnt[i] += cnt[i - 1];</pre>
  for(int i = 0; i < n; i++) p[--cnt[s[i]]] = i;
  for(int i = 1; i < n; i++)
    c[p[i]] = c[p[i - 1]] + (s[p[i]] != s[p[i - 1]]);
  vector<int> c2(n), p2(n);
  for(int k = 0; (1 << k) < n; k++){
    int classes = c[p[n - 1]] + 1;
    fill(cnt.begin(), cnt.begin() + classes, 0);
    for(int i = 0; i < n; i++) p2[i] = (p[i] - (1 << k) + n)%n;
    for(int i = 0; i < n; i++) cnt[c[i]]++;
    for(int i = 1; i < classes; i++) cnt[i] += cnt[i - 1];</pre>
    for(int i = n - 1; i \ge 0; i - - p[--cnt[c[p2[i]]]] = p2[i];
    c2[p[0]] = 0:
    for(int i = 1; i < n; i++){
      pair<int, int> b1 = {c[p[i]], c[(p[i] + (1 << k))%n]};
     pair<int, int> b2 = {c[p[i - 1]], c[(p[i - 1] + (1 << k))%n]};
      c2[p[i]] = c2[p[i - 1]] + (b1 != b2);
    c.swap(c2):
  }
  return p;
```

```
6.3. Longest common prefix with SA
```

```
vector<int> lcp(string &s, vector<int> &p){
 int n = s.size();
 vector<int> ans(n - 1), pi(n);
 for(int i = 0; i < n; i++) pi[p[i]] = i;
 int lst = 0;
  for(int i = 0; i < n - 1; i++){
   if(pi[i] == n - 1) continue;
   while(s[i + lst] == s[p[pi[i] + 1] + lst]) lst++;
   ans[pi[i]] = lst;
   lst = max(0, lst - 1);
 return ans;
```

6.4. Rabin-Karp

```
// Rabin-Karp - String Matching + Hashing O(n+m)
const int B = 31;
char s[N], p[N];
int n, m; // n = strlen(s), m = strlen(p)
void rabin() {
 if (n<m) return:
  ull hp = 0, hs = 0, E = 1:
  for (int i = 0; i < m; ++i)
   hp = ((hp*B) MOD + p[i]) MOD.
   hs = ((hs*B)*MOD + s[i])*MOD.
   E = (E*B)%MOD:
  if (hs == hp) { /* matching position 0 */ }
  for (int i = m; i < n; ++i) {
   hs = ((hs*B)%MOD + s[i])%MOD;
   hhs = (hs - s[i-m]*E%MOD + MOD)%MOD;
   if (hs == hp) { /* matching position i-m+1 */ }
 }
}
```

6.5. Z-function

The Z-function of a string s is an array z where z_i is the length of the longest substring starting from s_i which is also a prefix of s.

Examples:

```
• "aaaaa": [0, 4, 3, 2, 1]
• "aaabaab": [0, 2, 1, 0, 2, 1, 0]
• "abacaba": [0, 0, 1, 0, 3, 0, 1]
vector<int> zfunction(const string& s){
 vector<int> z (s.size());
  for (int i = 1, l = 0, r = 0, n = s.size(); i < n; i++){
   if (i \le r) z[i] = min(z[i-l], r - i + 1);
   while (i + z[i] < n \text{ and } s[z[i]] == s[z[i] + i]) z[i] ++;
   if (i + z[i] - 1 > r) l = i, r = i + z[i] - 1;
 }
  return z;
```

6.6. Manacher's

```
// Manacher (Longest Palindromic String) - O(n)
int lps[2*N+5];
char s[N];
int manacher() {
 int n = strlen(s);
  string p (2*n+3, '#');
  p[0] = '^';
  for (int i = 0; i < n; i++) p[2*(i+1)] = s[i];
  p[2*n+2] = '$';
  int k = 0, r = 0, m = 0;
  int l = p.length();
  for (int i = 1; i < l; i++) {
   int o = 2*k - i;
   lps[i] = (r > i) ? min(r-i, lps[o]) : 0;
   while (p[i + 1 + lps[i]] == p[i - 1 - lps[i]]) lps[i]++;
   if (i + lps[i] > r) k = i, r = i + lps[i];
    m = max(m, lps[i]);
 }
  return m;
```

Dynamic programming

7.1. Convex hull trick

```
// Convex Hull Trick
// ATTENTION: This is the maximum convex hull. If you need the
minimum
// CHT use {-b, -m} and modify the query function.
// In case of floating point parameters swap long long with long
double
typedef long long type;
struct line { type b, m; };
line v[N]: // lines from input
int n; // number of lines
// Sort slopes in ascending order (in main):
sort(v, v+n, [](line s, line t){
     return (s.m == t.m) ? (s.b < t.b) : (s.m < t.m); });
// nh: number of lines on convex hull
// pos: position for linear time search
// hull: lines in the convex hull
int nh, pos;
line hull[N];
bool check(line s, line t, line u) {
 // verify if it can overflow. If it can just divide using long
  return (s.b - t.b)*(u.m - s.m) < (s.b - u.b)*(t.m - s.m);
}
```

```
// Add new line to convex hull, if possible
// Must receive lines in the correct order, otherwise it won't work
void update(line s) {
 // 1. if first lines have the same b, get the one with bigger m
 // 2. if line is parallel to the one at the top, ignore
 // 3. pop lines that are worse
 // 3.1 if you can do a linear time search, use
 // 4. add new line
 if (nh == 1 and hull[nh-1].b == s.b) nh--;
 if (nh > 0 and hull[nh-1].m >= s.m) return;
 while (nh >= 2 and !check(hull[nh-2], hull[nh-1], s)) nh--;
  pos = min(pos, nh);
 hull[nh++] = s;
type eval(int id, type x) { return hull[id].b + hull[id].m * x; }
// Linear search query - O(n) for all queries
// Only possible if the queries always move to the right
type query(type x) {
 while (pos+1 < nh \text{ and } eval(pos, x) < eval(pos+1, x)) pos++;
 return eval(pos, x);
 // return -eval(pos, x); ATTENTION: Uncomment for minimum CHT
7.2. Longest Increasing Subsequence
memset(dp, 63, sizeof dp);
for (int i = 0; i < n; ++i) {
 // increasing: lower_bound
 // non-decreasing: upper bound
 int j = lower_bound(dp, dp + lis, v[i]) - dp;
 dp[j] = min(dp[j], v[i]);
 lis = \max(lis, j + 1);
7.3. SOS DP (Sum over Subsets)
// 0(bits*(2^bits))
const int bits = 20;
vector<int> a(1<<bits); // initial value of each subset</pre>
vector<int> f(1<<bits); // sum over all subsets</pre>
// (at f[011] = a[011]+a[001]+a[010]+a[000])
for (int i = 0; i<(1<<bits); i++){</pre>
    f[i] = a[i];
for (int i = 0; i < bits; i++) {
 for(int mask = 0; mask < (1<<bits); mask++){</pre>
    if(mask & (1<<i)){</pre>
        f[mask] += f[mask^(1<< i)];
 }
}
```