LU ICPC kladīte;)

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C++ programming language

1.1. Input/Output disable sync

```
ios base::sync with stdio(false);
cin.tie(NULL); cout.tie(NULL);
```

1.2. Optimization pragmas

```
// change to 03 to disable fast-math for geometry problems
#pragma GCC optimize("Ofast,unroll-loops")
#pragma GCC target("avx2,bmi,bmi2,lzcnt,popcnt,tune=native")
```

1.3. Printing structs

```
ostream& operator<<(ostream& os, const pair<int, int>& p) {
    return os << "(" << p.first << ", " << p.second << ")";</pre>
}
```

1.4. Lambda func for sorting

```
using ii = pair<int,int>;
vector<ii> fracs = \{\{1, 2\}, \{3, 4\}, \{1, 3\}\}\};
// sort positive rational numbers
sort(fracs.begin(), fracs.end(),
    [](const ii& a, const ii& b) {
    return a.fi*b.se < b.fi*a.se;</pre>
});
```

Algebra

2.1. Binary exponentiation

```
ll m_pow(ll base, ll exp, ll mod) {
    base %= mod;
    ll result = 1;
    while (exp > 0) {
        if (exp & 1) result = ((ll)result * base) % mod;
        base = ((ll)base * base) % mod;
        exp >>= 1;
   }
    return result;
}
```

2.2. Extended euclidean

```
a \cdot x + b \cdot y = \gcd(a, b)
int gcd_ext(int a, int b, int& x, int& y) {
    if (b == 0) {
        x = 1; y = 0;
        return a;
    int x1, y1;
    int d = gcd(b, a % b, x1, y1);
    x = y1;
    y = x1 - y1 * (a / b);
    return d;
}
```

2.3. Modular inversion & division

gcd ext defined in Section 2.2.

```
\exists x (a \cdot x \equiv 1 \pmod{m}) \Leftrightarrow \gcd(a, m) = 1
int mod_inv(int b, int m) {
    int x, y;
    int g = gcd_ext(b, m, &x, &y);
    if (g != 1) return -1;
     return (x%m + m) % m:
int m divide(ll a, ll b, ll m) {
    int inv = mod inv(b, m);
    assert(inv != -1);
     return (inv * (a % m)) % m;
}
```

2.4. Linear Diophantine equation

gcd ext defined in Section 2.2.

```
\left\{x = x_0 + k \cdot \frac{b}{g}; y = y_0 - k \cdot \frac{a}{g}\right\}
```

 $a \cdot x + b \cdot y = c$

```
bool find_x0_y0(int a, int b, int c, int &x0, int &y0, int &g) {
    g = gcd_ext(abs(a), abs(b), x0, y0);
    if (c % g) return false;
    x0 *= c / g;
    y0 *= c / g;
    if (a < 0) x0 = -x0;
    if (b < 0) y0 = -y0;
    return true;</pre>
```

2.5. Linear sieve

}

```
const int N = 10000000;
vector<int> lp(N+1);
vector<int> pr;

for (int i=2; i <= N; ++i) {
    if (lp[i] == 0) {
        lp[i] = i;
        pr.push_back(i);
    }
    for (int j = 0; i * pr[j] <= N; ++j) {
        lp[i * pr[j]] = pr[j];
        if (pr[j] == lp[i]) break;
    }
}</pre>
```

2.6. Matrix multiplication

2.7. FFT

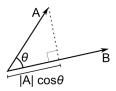
```
using ld = long double;
const int N = 1 << 18;
const ld PI = acos(-1.0);
struct T {
 ld x, y;
 T() : x(0), y(0) \{ \}
 T(ld a, ld b=0) : x(a), y(b) {}
 T operator/=(ld k) { x/=k; y/=k; return (*this); }
 T operator*(T a) const { return T(x*a.x - y*a.y, x*a.y + y*a.x); }
 T operator+(T a) const { return T(x+a.x, y+a.y); }
 T operator-(T a) const { return T(x-a.x, y-a.y); }
};
void fft(T* a, int n, int s) {
 for (int i=0, j=0; i<n; i++) {
   if (i>j) swap(a[i], a[j]);
   for (int l=n/2; (j^=l) < l; l>>=1);
 }
  for(int i = 1; (1<<ii) <= n; i++){
   int M = 1 << i:
   int K = M \gg 1:
   T wn = T(\cos(s*2*PI/M), \sin(s*2*PI/M));
   for(int j = 0; j < n; j += M) {
     T w = T(1, 0);
      for(int l = j; l < K + j; ++l){}
       T t = w*a[l + K];
        a[l + K] = a[l]-t:
        a[l] = a[l] + t;
        w = wn*w:
}
void multiply(T* a, T* b, int n) {
   while (n&(n-1)) n++; // ensure n is a power of two
   fft(a,n,1);
   fft(b,n,1);
    for (int i = 0; i < n; i++) a[i] = a[i]*b[i];
   fft(a,n,-1);
    for (int i = 0; i < n; i++) a[i] /= n;
}
int main() {
 // Example polynomials: (2 + 3x) and (1 - x)
 T a[10] = \{T(2), T(3)\};
 T b[10] = \{T(1), T(-1)\};
 multiply(a, b, 4);
 for (int i = 0; i < 10; i++)
   std::cout << int(a[i].x) << " ";
```

Geometry

3.1. Dot product

$$a \cdot b = |a| |b| \cos(\theta)$$
$$a \cdot b = a_x b_x + a_y b_y$$

$$\theta = \arccos\left(\frac{a_x b_x + a_y b_y}{|a| |b|}\right)$$



Projection of a onto b:

$$\frac{a\cdot b}{|b|}$$

3.2. Cross product

$$a \times b = |a| |b| \sin(\theta)$$

$$a \times b = a_x b_y - a_y b_x$$

 θ is positive if a is clockwise from b

3.3. Line-point distance

Line given by ax + by + c = 0 and point (x_0, y_0) .

$$distance = \frac{|ax_0 + by_0 + c|}{\sqrt{a^2 + b^2}}$$

The coordinates of this point are:

$$x = \frac{b(bx_0 - ay_0) - ac}{a^2 + b^2}$$

$$y = \frac{a(-bx_0 + ay_0) - bc}{a^2 + b^2}$$

3.4. Shoelace formula

$$2A = \sum_{i=1}^{n} \begin{vmatrix} x_i & y_i \\ x_{i+1} & y_{i+1} \end{vmatrix}$$

3.5. Segment to line

$$\begin{split} \left(\left(P_x,P_y\right),\left(Q_x,Q_y\right)\right) \to Ax + By + C &= 0 \\ A &= P_y - Q_y \\ B &= Q_x - P_x \\ C &= -AP_x - BP_y \end{split}$$

Rationing the obtained line equation:

- 1. divide A,B,C by their GCD
- 2. if A < 0 or $A = 0 \land B < 0$ then multiply all by -1

3.6. Three point orientation

3.7. Line-line intersection

From system of linear equations derived Cramer's rule:

$$x = -\frac{c_1b_2 - c_2b_1}{a_1b_2 - a_2b_1}$$
$$y = -\frac{a_1c_2 - a_2c_1}{a_1b_2 - a_2b_1}$$

If the denominator equals zero, the lines are parallel or coincident.

3.8. Check if two segments intersect

```
bool on segment(Point p, Point q, Point r)
   if (q.x \ll max(p.x, r.x)) \& q.x \gg min(p.x, r.x) \& \&
       q.y \le \max(p.y, r.y) \&\& q.y >= \min(p.y, r.y))
       return true:
    return false;
bool do intersect(Point p1, Point q1, Point p2, Point q2)
   // Find the four orientations needed for general and
   // special cases
   int o1 = orientation(p1, q1, p2);
   int o2 = orientation(p1, q1, q2);
   int o3 = orientation(p2, q2, p1);
   int o4 = orientation(p2, q2, q1);
   if (o1 != o2 && o3 != o4)
        return true;
   if (o1 == 0 && on_segment(p1, p2, q1)) return true;
   if (o2 == 0 && on segment(p1, q2, q1)) return true;
   if (o3 == 0 && on segment(p2, p1, q2)) return true;
   if (04 == 0 \&\& on segment(p2, g1, g2)) return true:
```

3.9. Heron's formula

Let a, b, c - sides of a triangle. Then the area A is:

$$A = \frac{1}{4} \sqrt{(a+b+c)(-a+b+c)(a-b+c)(a+b-c)} = \\ \frac{1}{4} \sqrt{4a^2b^2 - (a^2+b^2-c^2)^2}$$

Numerically stable version:

$$a \geq b \geq c, A = \frac{1}{4} \sqrt{(a + (b + c))(c - (a - b))(c + (a - b))(a + (b - c))}$$

3.10. Graham's scan

```
struct pt {double x, y;};
int orientation(pt a, pt b, pt c) {
    double v = a.x*(b.y-c.y)+b.x*(c.y-a.y)+c.x*(a.y-b.y);
    if (v < 0) return -1: // clockwise
    if (v > 0) return +1: // counter-clockwise
    return 0;
}
bool cw(pt a, pt b, pt c, bool include_collinear) {
    int o = orientation(a, b, c);
    return o < 0 || (include_collinear && o == 0);</pre>
bool collinear(pt a, pt b, pt c) { return orientation(a, b, c) ==
0; }
void convex hull(vector<pt>& a, bool include_collinear = false) {
    pt p\theta = *min element(a.begin(), a.end(), [](pt a, pt b) {
        return make pair(a.y, a.x) < make pair(b.y, b.x);</pre>
    sort(a.begin(), a.end(), [&p0](const pt& a, const pt& b) {
        int o = orientation(p0, a, b);
        if (o == 0)
            return (p0.x-a.x)*(p0.x-a.x) + (p0.v-a.v)*(p0.v-a.v)
                < (p0.x-b.x)*(p0.x-b.x) + (p0.y-b.y)*(p0.y-b.y);
        return o < 0:
    });
    if (include collinear) {
        int i = (int)a.size()-1;
        while (i \ge 0 \&\& collinear(p0, a[i], a,back())) i--:
        reverse(a.begin()+i+1, a.end());
    vector<pt> st:
    for (int i = 0; i < (int)a.size(); i++) {</pre>
         while (st.size() > 1 \&\& !cw(st[st.size()-2], st.back(),
a[i], include collinear))
            st.pop_back();
        st.push_back(a[i]);
    }
    a = st;
}
```

3.11. Circumradius

Let $a,\,b,\,c$ - sides of a triangle. A - area of the triangle. Then the circumradius is:

$$R = \frac{abc}{4A}$$

3.12. Closest pair of points

```
double mindist:
pair<int, int> best pair;
void upd ans(const pt & a, const pt & b) {
    double dist = sqrt((a.x - b.x)*(a.x - b.x) + (a.y - b.y)*(a.y)
- b.y));
    if (dist < mindist) {</pre>
        mindist = dist;
        best_pair = {a.id, b.id};
   }
}
vector<pt> t;
void rec(int l, int r) {
    if (r - l \le 3) {
        for (int i = l; i < r; ++i) {
            for (int j = i + 1; j < r; ++j) {
                upd_ans(a[i], a[j]);
            }
       }
        sort(a.begin() + l, a.begin() + r, cmp y());
        return:
    int m = (l + r) >> 1:
    int midx = a[m].x;
    rec(l, m);
    rec(m, r);
    merge(a.begin() + l, a.begin() + m, a.begin() + m, a.begin()
+ r, t.begin(), cmp y());
    copy(t.begin(), t.begin() + r - l, a.begin() + l);
    int tsz = 0;
    for (int i = l; i < r; ++i) {
        if (abs(a[i].x - midx) < mindist) {</pre>
              for (int j = tsz - 1; j >= 0 && a[i].y - t[j].y <
mindist; -- j)
                upd_ans(a[i], t[j]);
            t[tsz++] = a[i];
       }
   }
}
```

Data structures

4.1. Treap

```
// Implicit segment tree implementation
struct Node{
   int value, cnt, priority;
   Node *left, *right:
   Node(int p) : value(p), cnt(1), priority(gen()), left(NULL),
right(NULL) {};
};
typedef Node* pnode;
int get(pnode g){
   if(!q) return 0;
    return q->cnt;
}
void update_cnt(pnode &q){
   if(!q) return:
   q - cnt = get(q - left) + get(q - right) + 1;
}
void merge(pnode &T, pnode lef, pnode rig){
   if(!lef) {T=ria:return:}
   if(!rig){T=lef;return;}
   if(lef->priority > rig->priority){
        merge(lef->right, lef->right, rig);
        T = lef:
   }
   else{
        merge(rig->left, lef, rig->left);
       T = ria:
   }
   update cnt(T);
}
void split(pnode cur, pnode &lef, pnode &rig, int key){
   if(!cur){
        lef = rig = NULL;
        return;
   }
   int id = get(cur->left) + 1;
   if(id <= key){</pre>
        split(cur->right, cur->right, rig, key - id);
        lef = cur;
   }
   else{
        split(cur->left, lef, cur->left, key);
        rig = cur;
   }
   update cnt(cur);
}
```

```
4.2. Lazy segment tree
```

```
struct SumSeamentTree{
    vector<ll> S, 0, L;
    void build(ll ti, ll tl, ll tr){
        if(tl==tr){S[ti]=0[tl]; return;}
        build(ti*2, tl, (tl+tr)/2);
        build((ti*2)+1, ((tl+tr)/2)+1, tr);
        S[ti]=S[ti*2]+S[(ti*2)+1];
    void push(ll ti, ll tl, ll tr){
        S[ti] += L[ti]*(tr-tl+1);
        if(tl==tr){L[ti]=0; return;}
        L[ti+ti] \leftarrow L[ti], L[ti+ti+1] \leftarrow L[ti];
        L[ti] = 0;
   }
    ll query(ll ti, ll tl, ll tr, ll i, ll j){
        push(ti, tl, tr);
        if(i<=tl&&tr<=j) return S[ti];</pre>
        if(tr<i||tl>j) return 0;
        ll a = query(ti*2, tl, (tl+tr)/2, i, j);
        ll b = query((ti*2)+1, ((tl+tr)/2)+1, tr, i, j);
        return a+b;
    void update(ll ti, ll tl, ll tr, ll i, ll i, ll v){
        if(i<=tl&&tr<=j){L[ti]+=v;return;}</pre>
        if(tr<i||tl>j) return;
        S[ti] += v*(i-j+1);
        update(ti*2, tl, (tl+tr)/2, i, j, v);
        update((ti*2)+1, ((tl+tr)/2)+1, tr, i, j, v);
   }:
    ST(vector<ll> &V){
        0 = V:
        S.resize(0.size()*4, 0):
        L.resize(0.size()*4, 0):
        build(1, 0, 0.size()-1);
   }
};
4.3. Sparse table
const int N;
const int M; //log2(N)
int sparse[N][M];
void build() {
  for(int i = 0; i < n; i++)
    sparse[i][0] = v[i];
  for(int j = 1; j < M; j++)
    for(int i = 0; i < n; i++)
      sparse[i][i] =
        i + (1 << j - 1) < n
        ? min(sparse[i][j - 1], sparse[i + (1 << j - 1)][j - 1])</pre>
        : sparse[i][j - 1];
}
int query(int a, int b){
  int pot = 32 - builtin clz(b - a) - 1;
  return min(sparse[a][pot], sparse[b - (1 << pot) + 1][pot]);</pre>
}
```

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4.4. Fenwick tree

```
struct FenwickTree {
    vector<ll> bit; // binary indexed tree
    int n;
    FenwickTree(int n) {
        this->n = n;
        bit.assign(n, 0);
    ll sum(int r) {
        ll ret = 0;
        for (; r \ge 0; r = (r \& (r + 1)) - 1)
            ret += bit[r];
        return ret;
    }
    ll sum(int l, int r) { // l to r of the og array INCLUSIVE
        return sum(r) - sum(l - 1);
    void add(int idx, ll delta) {
        for (; idx < n; idx = idx \mid (idx + 1))
            bit[idx] += delta:
};
4.5. Trie
const int K = 26;
struct Vertex {
    int next[K]:
    bool output = false;
    Vertex() {fill(begin(next), end(next), -1);}
};
vector<Vertex> t(1); // trie nodes
void add_string(string const& s) {
    int v = 0;
    for (char ch : s) {
        int c = ch - 'a';
        if (t[v].next[c] == -1) {
            t[v].next[c] = t.size();
            t.emplace_back();
        }
        v = t[v].next[c];
    t[v].output = true;
}
```

4.6. Aho-Corasick

```
const int K = 26:
struct Vertex {
   int next[K]:
   bool output = false:
   int p = -1; // parent node
   char pch; // "transition" character from parent to this node
   int link = -1; // fail link
   int qo[K]; // if need more memory can delete this and use "next"
   // additional potentially useful things
   int depth = -1;
   // longest string that has an output from this vertex
   int exitlen = -1;
   Vertex(int p=-1, char ch='$') : p(p), pch(ch) {
        fill(begin(next), end(next), -1);
        fill(begin(go), end(go), -1);
   }
};
vector<Vertex> t(1);
void add string(string const& s) {
   int v = 0:
   for (char ch : s) {
        int c = ch - 'a':
        if (t[v].next[c] == -1) {
           t[v].next[c] = t.size();
           t.emplace back(v, ch); // !!!!! ch not c
        v = t[v].next[c];
   t[v].output = true;
int go(int v, char ch);
int get link(int v) {
   if (t[v].link == -1) {
        if (v == 0 || t[v].p == 0)
           t[v].link = 0;
        else
            t[v].link = go(get_link(t[v].p), t[v].pch);
   return t[v].link;
int go(int v, char ch) {
   int c = ch - 'a';
   if (t[v].go[c] == -1) {
        if (t[v].next[c] != -1)
           t[v].qo[c] = t[v].next[c];
           // !!!!! ch not c
           t[v].go[c] = v == 0 ? 0 : go(get link(v), ch);
   return t[v].go[c];
}
```

```
// int go(int v, char ch) { // go without the go[K] variable
       int c = ch - 'a';
       if (t[v].next[c] == -1) {
//
//
           // !!!!! ch not c
//
           t[v].next[c] = v == 0 ? 0 : go(get_link(v), ch);
//
//
       return t[v].next[c];
// }
// helper function
int get depth(int v){
    if (t[v].depth == -1){
        if (v == 0) {
            t[v].depth = 0;
        } else {
            t[v].depth = get depth(t[v].p)+1;
   }
    return t[v].depth:
// helper function
int get exitlen(int v){
   if (t[v].exitlen == -1){
        if (v == 0){
            t[v].exitlen = 0;
        } else if (t[v].output) {
            t[v].exitlen = get depth(v):
            t[v].exitlen = get_exitlen(get_link(v));
   }
    return t[v].exitlen;
4.7. Disjoint Set Union
struct DSU {
    vector<int> parent, rank;
    DSU(int n) {
        parent.resize(n); rank.resize(n);
        for (int i = 0; i < n; i++)
            parent[i] = i;
   }
    int root(int a) {
        if (parent[a] == a) return a;
        return parent[a] = find(parent[a]);
    void unite(int a, int b) {
        a = find(a), b = find(b);
        if (a == b) return;
        if (rank[a] < rank[b]) {</pre>
            parent[a] = b;
        } else if (rank[a] > rank[b]) {
            parent[b] = a;
        } else {
            parent[b] = a;
            rank[a] = rank[a] + 1;
   }
```

};

```
4.8. Merge sort tree
```

```
struct MergeSortTree {
   int size;
   vector<vector<ll>> values:
   void init(int n){
        size = 1;
        while (size < n){
            size *= 2;
        values.resize(size*2, vl(0));
   void build(vl &arr, int x, int lx, int rx){
       if (rx - lx == 1){
            if (lx < arr.size()){</pre>
                values[x].pb(arr[lx]);
           } else {
                values[x].pb(-1);
            }
            return;
        int m = (lx+rx)/2:
        build(arr, 2 * x + 1, lx, m);
       build(arr, 2 * x + 2, m, rx);
        int i = 0:
       int j = 0;
       int asize = values[2*x+1].size();
       while (i < asize && j < asize){
            if (values[2*x+1][i] < values[2*x+2][j]){</pre>
                values[x].pb(values[2*x+1][i]);
                1++:
            } else {
                values[x].pb(values[2*x+2][j]);
                j++;
           }
        while (i < asize) {</pre>
            values[x].pb(values[2*x+1][i]);
       }
        while (j < asize){</pre>
            values[x].pb(values[2*x+2][j]);
            j++;
       }
   void build(vl &arr){
        build(arr, 0, 0, size);
```

```
int calc(int l, int r, int x, int lx, int rx, int k){
    if (lx >= r \mid | rx <= l) return 0;
    // (elements strictly less than k currently)
    if (lx >= l && rx <= r) { // CHANGE HEURISTIC HERE
        int lft = -1;
        int rght = values[x].size();
        while (rght - lft > 1){
            int mid = (lft+rght)/2;
            if (values[x][mid] < k){</pre>
                lft = mid;
            } else {
                rght = mid;
            }
        return lft+1;
    int m = (lx+rx)/2;
    int values1 = calc(l, r, 2*x+1, lx, m, k):
    int values2 = calc(l, r, 2*x+2, m, rx, k);
    return values1 + values2:
int calc(int l, int r, int k){
    return calc(l, r, 0, 0, size, k);
```

Graph algorithms

5.1. Bellman-Ford

};

```
void solve()
{
    vector<int> d(n, INF);
    d[v] = 0;
    for (;;) {
        bool any = false;

        for (Edge e : edges)
            if (d[e.a] < INF)
            if (d[e.b] > d[e.a] + e.cost) {
                 d[e.b] = d[e.a] + e.cost;
                any = true;
            }

        if (!any)
            break;
    }
    // display d, for example, on the screen
}
```

5.2. Dijkstra

```
vector<int> adj[N], adjw[N];
int dist[N];
memset(dist, 63, sizeof(dist));
priority_queue<pri> pq;
```

```
pq.push(mp(0,0));
while (!pq.empty()) {
  int u = pq.top().nd;
  int d = -pq.top().st;
  pq.pop();
  if (d > dist[u]) continue;
  for (int i = 0; i < adj[u].size(); ++i) {</pre>
   int v = adj[u][i];
   int w = adjw[u][i];
   if (dist[u] + w < dist[v])</pre>
     dist[v] = dist[u]+w, pq.push(mp(-dist[v], v));
 }
}
5.3. Floyd-Warshall
int adj[N][N]; // no-edge = INF
for (int k = 0; k < n; ++k)
  for (int i = 0; i < n; ++i)
    for (int j = 0; j < n; ++j)
      adj[i][j] = min(adj[i][j], adj[i][k]+adj[k][j]);
5.4. Bridges & articulations
// Articulation points and Bridges O(V+E)
int par[N], art[N], low[N], num[N], ch[N], cnt;
void articulation(int u) {
  low[u] = num[u] = ++cnt;
  for (int v : adj[u]) {
   if (!num[v]) {
      par[v] = u; ch[u] ++;
     articulation(v);
     if (low[v] >= num[u]) art[u] = 1;
     if (low[v] > num[u]) { /* u-v bridge */ }
     low[u] = min(low[u], low[v]);
    else if (v != par[u]) low[u] = min(low[u], num[v]);
 }
}
for (int i = 0; i < n; ++i) if (!num[i])
  articulation(i), art[i] = ch[i]>1;
5.5. Dinic's max flow / matching
Time complexity:
• generally: O(EV^2)
• small flow: O(F(V+E))
• bipartite graph or unit flow: O(E\sqrt{V})
Usage:
• dinic()
• add_edge(from, to, capacity)
• recover() (optional)
```

```
const ll N=1e5+5, INF=1e9;
struct edge{ll v, c, f;};
ll src=0, snk=N-1, h[N], ptr[N];
vector<edge> edgs;
vector<ll> q[N];
void add edge(ll u, ll v, ll c) {
    edgs.push_back({v,c,0}), edgs.push_back({u,0,0});
    ll k=edgs.size();
    g[u].push_back(k), g[v].push_back(k+1);
}
bool bfs() {
    memset(h, 0, sizeof(h));
    queue<ll> q;
    h[src]=1;
    q.push(src);
    while(!q.emptv()){
        ll u=q.front();q.pop();
        for(ll i:a[u]){
            ll v=edgs[i].v;
            if(!h[v]&&edgs[i].f<edgs[i].c)</pre>
                q.push(v),h[v]=h[u]+1;
        }
    return h[snk]:
}
ll dfs(ll u, ll flow){
    if(!flow or u==snk) return flow;
    for(ll &i=ptr[u];i<g[u].size();i++){</pre>
        edge &dir=edgs[g[u][i]],&rev=edgs[g[u][i]^1];
        if(h[dir.v]!=h[u]+1) continue;
        ll inc=min(flow,dir.c-dir.f);
        inc=dfs(dir.v,inc);
        if(inc){ dir.f+=inc,rev.f-=inc; return inc;}
    return 0;
}
ll dinic(){
    ll flow=0:
    while(bfs()){
        memset(ptr.0.sizeof(ptr));
        while(ll inc=dfs(src,INF)) flow += inc;
    }
    return flow;
}
vector<pair<ii,ll>> recover() {
    vector<pair<ii.ll>> res:
    for(ll i=0;i<edgs.size();i+=2){</pre>
        if(edas[i].f>0){
            ll v=edgs[i].v, u=edgs[i^1].v;
            res.push back({{u,v},edgs[i].f});
        }
    return res;
}
```

5.6. Flow with demands

Finding an arbitrary flow

- Assume a network with [L; R] on edges (some may have L = 0), let's call it old network.
- Create a New Source and New Sink (this will be the src and snk for Dinic).
- Modelling network:
- 1. Every edge from the old network will have cost R-L
- 2. Add an edge from New Source to every vertex \boldsymbol{v} with cost:
 - S(L) for every (u, v). (sum all L that LEAVES v)
- 3. Add an edge from every vertex v to New Sink with cost:
- S(L) for every (v, w). (sum all L that ARRIVES v)
- 4. Add an edge from Old Source to Old Sink with cost INF (circulation problem)
- The Network will be valid if and only if the flow saturates the network (max flow == S(L))

Finding Min Flow

- To find min flow that satisfies just do a binary search in the (Old Sink
 Old Source) edge
- The cost of this edge represents all the flow from old network
- Min flow = S(L) that arrives in Old Sink + flow that leaves (Old Sink -> Old Source)

5.7. Kosaraju's algorithm

const int N = 2e5 + 5;

```
vector<int> adj[N], adjt[N];
int n, ordn, scc_cnt, vis[N], ord[N], scc[N];
//Directed Version
void dfs(int u) {
 vis[u] = 1;
  for (auto v : adj[u]) if (!vis[v]) dfs(v);
 ord[ordn++] = u;
void dfst(int u) {
 scc[u] = scc cnt, vis[u] = 0;
  for (auto v : adjt[u]) if (vis[v]) dfst(v);
// add edge: u -> v
void add edge(int u, int v){
 adi[u].push back(v):
 adjt[v].push back(u);
// run kosaraiu
void kosaraju(){
 for (int i = 1; i <= n; ++i) if (!vis[i]) dfs(i);
 for (int i = ordn - 1; i \ge 0; --i) if (vis[ord[i]]) scc cnt++,
dfst(ord[i]):
}
```

5.8. Lowest Common Ancestor

```
const int N = 1e6. M = 25:
int anc[M][N], h[N], rt;
// TODO: Calculate h[u] and set anc[0][u] = parent of node u for
each u
// build (sparse table)
anc[0][rt] = rt; // set parent of the root to itself
for (int i = 1; i < M; ++i)
 for (int j = 1; j \le n; ++j)
    anc[i][j] = anc[i-1][anc[i-1][j]];
// query
int lca(int u, int v) {
  if (h[u] < h[v]) swap(u, v);
  for (int i = M-1; i \ge 0; --i) if (h[u]-(1 << i) \ge h[v])
   u = anc[i][u];
  if (u == v) return u;
  for (int i = M-1; i \ge 0; --i) if (anc[i][u] != anc[i][v])
   u = anc[i][u], v = anc[i][v];
  return anc[0][u]:
```

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5.9. General matching in a graph

String Processing

vector<int> Blossom(vector<vector<int>> graph){ int n = graph.size(); int timer = -1; vector<int> mate(n, -1), label(n), parent(n), orig(n), aux(n, -1), q; auto $lca = [\&](int x, int y) {$ for (timer++; ; swap(x, y)) { if (x == -1) continue; if (aux[x] == timer) return x; aux[x] = timer;x = (mate[x] == -1 ? -1 : orig[parent[mate[x]]]);}; auto blossom = [&](int v, int w, int a) { while (orig[v] != a) { parent[v] = w; w = mate[v]; if (label[w] == 1) label[w] = 0, q.push_back(w); orig[v] = orig[w] = a; v = parent[w]; } }; auto augment = [&] (int v) { while (v != -1) { int pv = parent[v]. nv = mate[pv]: mate[v] = pv; mate[pv] = v; v = nv; }; auto bfs = [&](int root) { fill(label.begin(), label.end(), -1); iota(orig.begin(), orig.end(), 0); a.clear(): label[root] = 0: q.push back(root): for (int i = 0; $i < (int)q.size(); ++i) {$ int v = q[i];for (auto x : graph[v]) { if (label[x] == -1) { label[x] = 1; parent[x] = v;if (mate[x] == -1)return augment(x), 1; label[mate[x]] = 0; q.push_back(mate[x]); } else if (label[x] == 0 && orig[v] != orig[x]) { int a = lca(orig[v], orig[x]); blossom(x, v, a); blossom(v, x, a); } } return 0; for (int i = 0; i < n; i++) if (mate[i] == -1) bfs(i): return mate:

6.1. Knuth-Morris-Pratt (KMP)

```
// Knuth-Morris-Pratt - String Matching O(n+m)
char s[N], p[N];
int b[N], n, m; // n = strlen(s), m = strlen(p);
void kmppre() {
 b[0] = -1;
  for (int i = 0, j = -1; i < m; b[++i] = ++j)
   while (j \ge 0 \text{ and } p[i] != p[j])
      j = b[j];
}
void kmp() {
  for (int i = 0, j = 0; i < n;) {
   while (j \ge 0 \text{ and } s[i] != p[j]) j=b[j];
   i++, j++;
   if (j == m) {
      // match position i-j
      j = b[j];
   }
 }
}
```

6.2. Suffix Array

```
// s.push('$'):
vector<int> suffix array(string &s){
  int n = s.size(), alph = 256;
  vector<int> cnt(max(n, alph)), p(n), c(n);
  for(auto c : s) cnt[c]++;
  for(int i = 1; i < alph; i++) cnt[i] += cnt[i - 1];
  for(int i = 0; i < n; i++) p[--cnt[s[i]]] = i;
  for(int i = 1; i < n; i++)
   c[p[i]] = c[p[i - 1]] + (s[p[i]] != s[p[i - 1]]);
  vector<int> c2(n), p2(n);
  for(int k = 0; (1 << k) < n; k++){
   int classes = c[p[n - 1]] + 1;
   fill(cnt.begin(), cnt.begin() + classes, 0);
    for(int i = 0; i < n; i++) p2[i] = (p[i] - (1 << k) + n)%n;
    for(int i = 0; i < n; i++) cnt[c[i]]++;
    for(int i = 1; i < classes; i++) cnt[i] += cnt[i - 1];</pre>
    for(int i = n - 1; i \ge 0; i - - p[--cnt[c[p2[i]]]] = p2[i];
    c2[p[0]] = 0:
    for(int i = 1; i < n; i++){
     pair<int, int> b1 = {c[p[i]], c[(p[i] + (1 << k))%n]};
     pair<int, int> b2 = {c[p[i - 1]], c[(p[i - 1] + (1 << k))%n]};
     c2[p[i]] = c2[p[i - 1]] + (b1 != b2);
    c.swap(c2);
 }
  return p;
6.3. Longest common prefix with SA
vector<int> lcp(string &s, vector<int> &p){
 int n = s.size();
  vector<int> ans(n - 1), pi(n);
  for(int i = 0; i < n; i++) pi[p[i]] = i;
  int lst = 0;
  for(int i = 0; i < n - 1; i++){
   if(pi[i] == n - 1) continue;
   while(s[i + lst] == s[p[pi[i] + 1] + lst]) lst++;
   ans[pi[i]] = lst;
   lst = max(0, lst - 1);
 }
  return ans;
```

6.4. Rabin-Karp

```
// Rabin-Karp - String Matching + Hashing O(n+m)
const int B = 31:
char s[N], p[N];
int n, m; // n = strlen(s), m = strlen(p)
void rabin() {
 if (n<m) return;</pre>
  ull hp = 0, hs = 0, E = 1;
  for (int i = 0; i < m; ++i)
    hp = ((hp*B)%MOD + p[i])%MOD,
    hs = ((hs*B)*MOD + s[i])*MOD,
    E = (E*B)%MOD;
  if (hs == hp) { /* matching position 0 */ }
  for (int i = m; i < n; ++i) {
    hs = ((hs*B)*MOD + s[i])*MOD;
    hhs = (hs - s[i-m]*E%MOD + MOD)%MOD;
    if (hs == hp) { /* matching position i-m+1 */ }
}
```

6.5. Z-function

The Z-function of a string s is an array z where z_i is the length of the longest substring starting from s_i which is also a prefix of s.

Examples:

```
• "aaaaa": [0,4,3,2,1]
• "aaabaab": [0,2,1,0,2,1,0]
• "abacaba": [0,0,1,0,3,0,1]

vector<int> z function(const string& s){
    vector<int> z (s.size());
    for (int i = 1, l = 0, r = 0, n = s.size(); i < n; i++){
        if (i <= r) z[i] = min(z[i-l], r - i + 1);
        while (i + z[i] < n and s[z[i]] == s[z[i] + i]) z[i]++;
        if (i + z[i] - 1 > r) l = i, r = i + z[i] - 1;
    }
    return z;
}
```

6.6. Manacher's

```
// Manacher (Longest Palindromic String) - O(n)
int lps[2*N+5];
char s[N];
int manacher() {
 int n = strlen(s);
 string p (2*n+3, '#');
 p[0] = '^';
 for (int i = 0; i < n; i++) p[2*(i+1)] = s[i];
 p[2*n+2] = '$';
 int k = 0, r = 0, m = 0;
 int l = p.length();
 for (int i = 1; i < l; i++) {
   int o = 2*k - i;
   lps[i] = (r > i) ? min(r-i, lps[o]) : 0;
   while (p[i + 1 + lps[i]] == p[i - 1 - lps[i]]) lps[i]++;
   if (i + lps[i] > r) k = i, r = i + lps[i];
   m = max(m, lps[i]);
 return m;
```

Dynamic programming

7.1. Convex hull trick

```
// Convex Hull Trick
// ATTENTION: This is the maximum convex hull. If you need the
minimum
// CHT use {-b. -m} and modify the query function.
// In case of floating point parameters swap long long with long
double
typedef long long type;
struct line { type b, m; };
line v[N]: // lines from input
int n; // number of lines
// Sort slopes in ascending order (in main):
sort(v, v+n, [](line s, line t){
     return (s.m == t.m) ? (s.b < t.b) : (s.m < t.m); });
// nh: number of lines on convex hull
// pos: position for linear time search
// hull: lines in the convex hull
int nh, pos;
line hull[N];
bool check(line s, line t, line u) {
 // verify if it can overflow. If it can just divide using long
double
  return (s.b - t.b)*(u.m - s.m) < (s.b - u.b)*(t.m - s.m);
}
```

```
// Add new line to convex hull, if possible
// Must receive lines in the correct order, otherwise it won't work
void update(line s) {
 // 1. if first lines have the same b, get the one with bigger m
 // 2. if line is parallel to the one at the top, ignore
 // 3. pop lines that are worse
 // 3.1 if you can do a linear time search, use
  // 4. add new line
  if (nh == 1 and hull[nh-1].b == s.b) nh--;
  if (nh > 0 and hull[nh-1].m >= s.m) return;
  while (nh >= 2 and !check(hull[nh-2], hull[nh-1], s)) nh--;
  pos = min(pos, nh);
 hull[nh++] = s;
type eval(int id, type x) { return hull[id].b + hull[id].m * x; }
// Linear search query - O(n) for all queries
// Only possible if the queries always move to the right
type query(type x) {
 while (pos+1 < nh \text{ and } eval(pos, x) < eval(pos+1, x)) pos++;
  return eval(pos, x);
  // return -eval(pos, x); ATTENTION: Uncomment for minimum CHT
```

7.2. Online Convex Hull Trick

```
// Source: KTH notebook
struct Line {
  mutable ll k, m, p;
  bool operator<(const Line& o) const { return k < o.k; }</pre>
  bool operator<(ll x) const { return p < x; }</pre>
};
struct LineContainer : multiset<Line, less<>>> {
  // (for doubles, use inf = 1/.0, div(a,b) = a/b)
  static const ll inf = LLONG MAX;
  ll div(ll a, ll b) { // floored division
   return a / b - ((a ^ b) < 0 && a % b); }
  bool isect(iterator x, iterator y) {
   if (y == end()) return x -> p = inf, 0;
    if (x->k == y->k) x->p = x->m > y->m ? inf : -inf;
    else x -> p = div(y -> m - x -> m, x -> k - y -> k);
    return x->p >= v->p:
  void add(ll k, ll m) {
    auto z = insert(\{k, m, 0\}), y = z++, x = y;
    while (isect(y, z)) z = erase(z);
    if (x != begin() \&\& isect(--x, y)) isect(x, y = erase(y));
    while ((y = x) != begin() \&\& (--x)->p >= y->p)
      isect(x. erase(v)):
  ll query(ll x) {
    assert(!empty());
    auto l = *lower bound(x):
    return l.k * x + l.m;
 }
};
```

7.3. Longest Increasing Subsequence

```
memset(dp, 63, sizeof dp);
for (int i = 0; i < n; ++i) {
  // increasing: lower bound
  // non-decreasing: upper bound
  int j = lower_bound(dp, dp + lis, v[i]) - dp;
  dp[j] = min(dp[j], v[i]);
  lis = max(lis, j + 1);
7.4. SOS DP (Sum over Subsets)
// 0(bits*(2^bits))
const int bits = 20;
vector<int> a(1<<bits); // initial value of each subset</pre>
vector<int> f(1<<bits); // sum over all subsets</pre>
// (at f[011] = a[011]+a[001]+a[010]+a[000])
for (int i = 0; i<(1<<bits); i++){</pre>
    f[i] = a[i];
}
for (int i = 0; i < bits; i++) {</pre>
  for(int mask = 0; mask < (1<<bits); mask++){</pre>
    if(mask & (1<<i)){</pre>
        f[mask] += f[mask^(1<<i)];
  }
}
```

General

8.1. Simulated annealing

```
const ld T = (ld)2000;
const ld alpha = 0.999999;
// (new score - old score) / (temperature final) ~ 10 works well
const ld L = (ld)1e6;
ld small rand(){
  return ((ld)gen(L))/L;
ld P(ld old, ld nw, ld temp){
  if(nw > old)
    return 1.0;
  return exp((nw-old)/temp);
}
{
  auto start = chrono::steady_clock::now();
  ld time_limit = 2000;
  ld temperature = T;
  ld max_score = -1;
  while(elapsed_time < time_limit){</pre>
    auto cur = chrono::steady_clock::now();
```

```
elapsed_time = chrono::duration_cast<chrono::milliseconds>(cur
- start).count();
  temperature *= alpha;

  // try a neighboring state
  // ....
  // ....

  old_score = score(old_state);
  new_score = score(new_state);
  if(P(old_score, new_score, temperature) >= small_rand()){
    old_state = new_state;
    old_score = new_score;
}

if(old_score > max_score){
    max_score = old_score;
    max_state = old_state;
}
}
}
```

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8.2. Eulerian Path

A Eulerian path is a path in a graph that passes through all of its edges exactly once. A Eulerian cycle is a Eulerian path that is a cycle.

The problem is to find the Eulerian path in an undirected multigraph with loops

Algorithm

First we can check if there is an Eulerian path. We can use the following theorem. An Eulerian cycle exists if and only if the degrees of all vertices are even. And an Eulerian path exists if and only if the number of vertices with odd degrees is two (or zero, in the case of the existence of a Eulerian cycle). In addition, of course, the graph must be sufficiently connected (i.e., if you remove all isolated vertices from it, you should get a connected graph).

To find the Eulerian path / Eulerian cycle we can use the following strategy: We find all simple cycles and combine them into one this will be the Eulerian cycle. If the graph is such that the Eulerian path is not a cycle, then add the missing edge, find the Eulerian cycle, then remove the extra edge.

Looking for all cycles and combining them can be done with a simple recursive procedure:

```
procedure FindEulerPath(V)
1. iterate through all the edges outgoing from vertex V;
    remove this edge from the graph,
    and call FindEulerPath from the second end of this edge;
2. add vertex V to the answer.
```

The complexity of this algorithm is obviously linear with respect to the number of edges.

But we can write the same algorithm in the non-recursive version:

```
stack St;
put start vertex in St;
until St is empty
let V be the value at the top of St;
if degree(V) = 0, then
   add V to the answer;
   remove V from the top of St;
otherwise
find any edge coming out of V;
   remove it from the graph;
   put the second end of this edge in St;
```

It is easy to check the equivalence of these two forms of the algorithm. However, the second form is obviously faster, and the code will be much more efficient.

8.3. Flows with demands

Finding an arbitrary flow

We make the following changes in the network. We add a new source s' and a new sink t', a new edge from the source s' to every other vertex, a new edge for every vertex to the sink t', and one edge from t to s. Additionally we define the new capacity function c' as:

- $c'((s',v)) = \sum_{u \in V} d((u,v))$ for each edge (s',v).
- $c'((v,t')) = \sum_{w \in V} d((v,w))$ for each edge (v,t').
- c'((u,v)) = c((u,v)) d((u,v)) for each edge (u,v) in the old network.
- $c'((t,s)) = \infty$

If the new network has a saturating flow (a flow where each edge outgoing from s' is completely filled, which is equivalent to every edge incoming to t' is completely filled), then the network with demands has a valid flow, and the actual flow can be easily reconstructed from the new network. Otherwise there doesn't exist a flow that satisfies all conditions. Since a saturating flow has to be a maximum flow, it can be found by any maximum flow algorithm, like the Edmonds-Karp algorithm or the Push-relabel algorithm.

The correctness of these transformations is more difficult to understand. We can think of it in the following way: Each edge e=(u,v) with d(e)>0 is originally replaced by two edges: one with the capacity d(i), and the other with c(i)-d(i). We want to find a flow that saturates the first edge (i.e. the flow along this edge must be equal to its capacity). The second edge is less important - the flow along it can be anything, assuming that it doesn't exceed its capacity. Consider each edge that has to be saturated, and we perform the following operation: we draw the edge from the new source s' to its end v, draw the edge from its start u to the new sink t', remove the edge itself, and from the old sink t to the old source s we draw an edge of infinite capacity. By these actions we simulate the fact that this edge is saturated - from s0 there will be an additionally s0 flow outgoing (we simulate it with a new source that feeds the right amount of flow to s0, and s0 will also push s0 additional flow (but instead along the old edge, this flow will go directly to the new sink s1. A flow with the value s2, that originally flowed along the path s3 and s4 flow will go directly to the new sink s5. A flow with the value s6, that originally flowed along the path s6 and s7 flow in the definition of the new network, is that if procedure created multiple edges between the same pair of vertices, then they are combined to one single edge with the summed capacity.

Minimal flow

Note that along the edge (t,s) (from the old sink to the old source) with the capacity ∞ flows the entire flow of the corresponding old network. I.e. the capacity of this edge effects the flow value of the old network. By giving this edge a sufficient large capacity (i.e. ∞), the flow of the old network is unlimited. By limiting this edge by smaller capacities, the flow value will decrease. However if we limit this edge by a too small value, than the network will not have a saturated solution, e.g. the corresponding solution for the original network will not satisfy the demand of the edges. Obviously here can use a binary search to find the lowest value with which all constraints are still satisfied. This gives the minimal flow of the original network.

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8.4. Point in convex polygon $O(\log n)$

Algorithm

Let's pick the point with the smallest x-coordinate. If there are several of them, we pick the one with the smallest y-coordinate. Let's denote it as p_0 . Now all other points p_1, \ldots, p_n of the polygon are ordered by their polar angle from the chosen point (because the polygon is ordered counter-clockwise).

If the point belongs to the polygon, it belongs to some triangle p_0, p_i, p_{i+1} (maybe more than one if it lies on the boundary of triangles). Consider the triangle p_0, p_i, p_{i+1} such that p belongs to this triangle and i is maximum among all such triangles.

There is one special case. p lies on the segment (p_0, p_n) . This case we will check separately. Otherwise all points p_j with $j \le i$ are counter-clockwise from p with respect to p_0 , and all other points are not counter-clockwise from p. This means that we can apply binary search for the point p_i , such that p_i is not counter-clockwise from p with respect to p_0 , and i is maximum among all such points. And afterwards we check if the points is actually in the determined triangle.

The sign of $(a-c)\times(b-c)$ will tell us, if the point a is clockwise or counter-clockwise from the point b with respect to the point c. If $(a-c)\times(b-c)>0$, then the point a is to the right of the vector going from c to b, which means clockwise from b with respect to c. And if $(a-c)\times(b-c)<0$, then the point is to the left, or counter clockwise. And it is exactly on the line between the points b and c.

Back to the algorithm: Consider a query point p. Firstly, we must check if the point lies between p_1 and p_n . Otherwise we already know that it cannot be part of the polygon. This can be done by checking if the cross product $(p_1-p_0)\times(p-p_0)$ is zero or has the same sign with $(p_1-p_0)\times(p_n-p_0)$, and $(p_n-p_0)\times(p-p_0)$ is zero or has the same sign with $(p_n-p_0)\times(p_1-p_0)$. Then we handle the special case in which p is part of the line (p_0,p_1) . And then we can binary search the last point from $p_1,\dots p_n$ which is not counter-clockwise from p with respect to p_0 . For a single point p_i this condition can be checked by checking that $(p_i-p_0)\times(p-p_0)\leq 0$. After we found such a point p_i , we must test if p lies inside the triangle p_0,p_i,p_{i+1} . To test if it belongs to the triangle, we may simply check that

 $|(p_i-p_0)\times(p_{i+1}-p_0)|=|(p_0-p)\times(p_i-p)|+|(p_i-p)\times(p_{i+1}-p)|+|(p_{i+1}-p)\times(p_0-p)|$. This checks if the area of the triangle p_0,p_i,p_{i+1} has to exact same size as the sum of the sizes of the triangle p_0,p_i,p_i , p_i , the triangle p_0,p_i,p_{i+1} and the triangle p_0,p_i,p_{i+1} , p_i . If p_i is outside, then the sum of those three triangle will be bigger than the size of the triangle. If it is inside, then it will be equal.

```
bool pointInTriangle(pt a, pt b, pt c, pt point) {
    long long s1 = abs(a.cross(b, c));
    long long s2 = abs(point.cross(a, b)) + abs(point.cross(b, c)) + abs(point.cross(c, a));
    return s1 == s2;
}
void prepare(vector<pt> &points) {
    n = points.size();
    int pos = 0;
    for (int i = 1; i < n; i++) {
        if (lexComp(points[i], points[pos]))
            pos = i;
    rotate(points.begin(), points.begin() + pos, points.end());
    n--;
    seq.resize(n);
    for (int i = 0; i < n; i++)
        seq[i] = points[i + 1] - points[0];
    translation = points[0];
}
```

```
bool pointInConvexPolygon(pt point) {
    point = point - translation;
    if (seq[0].cross(point) != 0 &&
            sgn(seq[0].cross(point)) != sgn(seq[0].cross(seq[n - 1])))
        return false:
    if (seq[n - 1].cross(point) != 0 &&
            sgn(seg[n - 1].cross(point)) != sgn(seg[n - 1].cross(seg[0])))
        return false;
    if (seq[0].cross(point) == 0)
        return seq[0].sqrLen() >= point.sqrLen();
    int l = 0, r = n - 1;
    while (r - l > 1) {
        int mid = (l + r) / 2;
        int pos = mid;
        if (seq[pos].cross(point) >= 0)
           l = mid;
        else
            r = mid:
    }
    int pos = l:
    return pointInTriangle(seq[pos], seq[pos + 1], pt(0, 0), point);
```