LU ICPC kladīte;)

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Algebra

Sum formulas

$$(a+b)^2 = a^2 + 2ab + b^2$$

$$\sum_{k=1}^n k = \frac{n(n+1)}{2}$$

$$\sum_{k=1}^n k^2 = \frac{n(n+1)(2n+1)}{6}$$

$$\sum_{k=1}^n k^3 = \frac{n^2(n+1)^2}{4}$$

$$\sum_{k=1}^n k^4 = \frac{n(n+1)(2n+1)(3n^2 + 3n - 1)}{30}$$

```
FFT
                                                                         }
  // Fast Fourier Transform - O(nlogn)
                                                                       // assert n is a power of two greater of equal product size
                                                                       // n = na + nb; while (n&(n-1)) n++;
 // Use struct instead. Performance will be way better!
                                                                       void multiply(T* a, T* b, int n) {
  typedef complex<ld> T;
                                                                         fft(a,n,1);
  T a[N], b[N];
                                                                         fft(b,n,1);
                                                                         for (int i = 0; i < n; i++) a[i] = a[i]*b[i];
                                                                         fft(a,n,-1);
  struct T {
                                                                         for (int i = 0; i < n; i++) a[i] /= n;
   ld x, y;
   T() : x(0), y(0) \{ \}
   T(ld a, ld b=0) : x(a), y(b) {}
                                                                       // Convert to integers after multiplying:
                                                                       // (int)(a[i].x + 0.5);
    T operator/=(ld k) { x/=k; y/=k; return (*this); }
    T operator*(T a) const { return T(x*a.x - y*a.y, x*a.y + y*a.x); }
                                                                        Geometry
    T operator+(T a) const { return T(x+a.x, y+a.y); }
4 T operator-(T a) const { return T(x-a.x, y-a.y); }
4 } a[N], b[N];
                                                                       Basics
                                                                       #include <bits/stdc++.h>
  // a: vector containing polynomial
  // n: power of two greater or equal product size
                                                                       using namespace std;
  // Use iterative version!
                                                                       #define st first
 void fft recursive(T* a, int n, int s) {
                                                                       #define nd second
   if (n == 1) return;
                                                                       #define pb push back
    T tmp[n];
                                                                       #define cl(x,v) memset((x), (v), sizeof(x))
    for (int i = 0; i < n/2; ++i)
                                                                       \#define \ db(x) \ cerr << \#x << " == " << x << endl
      tmp[i] = a[2*i], tmp[i+n/2] = a[2*i+1];
                                                                       #define dbs(x) cerr << x << endl</pre>
                                                                       #define << ", " <<
    fft recursive(&tmp[0], n/2, s);
    fft recursive(&tmp[n/2], n/2, s);
                                                                       typedef long long ll;
                                                                       typedef long double ld;
    T wn = T(\cos(s*2*PI/n), \sin(s*2*PI/n)), w(1,0);
                                                                       typedef pair<int,int> pii;
    for (int i = 0; i < n/2; i++, w=w*wn)
                                                                       typedef pair<int, pii> piii;
      a[i] = tmp[i] + w*tmp[i+n/2],
                                                                       typedef pair<ll,ll> pll;
      a[i+n/2] = tmp[i] - w*tmp[i+n/2];
                                                                       typedef pair<ll, pll> plll;
                                                                       typedef vector<int> vi;
                                                                       typedef vector <vi> vii;
  void fft(T* a, int n, int s) {
                                                                       const ld EPS = 1e-9, PI = acos(-1.);
    for (int i=0, j=0; i<n; i++) {
                                                                       const ll LINF = 0x3f3f3f3f3f3f3f3f3f;
      if (i>j) swap(a[i], a[j]);
                                                                       const int INF = 0x3f3f3f3f, MOD = 1e9+7;
      for (int l=n/2; (j^=l) < l; l>>=1);
                                                                       const int N = 1e5+5;
                                                                       typedef long double type;
    for(int i = 1; (1<<i) <= n; i++){
                                                                       //for big coordinates change to long long
      int M = 1 << i;
      int K = M \gg 1;
                                                                       bool ge(type x, type y) { return x + EPS > y; }
      T wn = T(\cos(s*2*PI/M), \sin(s*2*PI/M));
                                                                       bool le(type x, type y) { return x - EPS < y; }</pre>
      for(int j = 0; j < n; j += M) {
                                                                       bool eq(type x, type y) { return ge(x, y) and le(x, y); }
        T w = T(1, 0);
                                                                       int sign(type x) { return ge(x, 0) - le(x, 0); }
        for(int l = j; l < K + j; ++l){}
          T t = w*a[l + K];
                                                                       struct point {
          a[l + K] = a[l]-t;
                                                                           type x, y;
          a[l] = a[l] + t;
          w = wn*w:
                                                                           point() : x(0), y(0) {}
                                                                           point(type x, type y) : x(x), y(y) {}
```

```
point operator -() { return point(-x, -y); }
                                                                    p.abs()); }
    point operator +(point p) { return point(x + p.x, y + p.y); }
    point operator -(point p) { return point(x - p.x, y - p.y); }
                                                                                                                                         void closest_pair(int l, int r) {
                                                                                                                                             if (r - l <= 3) {
    point operator *(type k) { return point(x*k, y*k); }
                                                                    int direction(point o, point p, point q) { return p.dir(o, q); }
                                                                                                                                                 for (int i = l; i < r; ++i) {
   point operator /(type k) { return point(x/k, y/k); }
                                                                                                                                                     for (int j = i + 1; j < r; ++j) {
                                                                    point rotate ccw90(point p) { return point(-p.y,p.x); }
                                                                                                                                                         upd_ans(pts[i], pts[j]);
   //inner product
                                                                    point rotate_cw90(point p) { return point(p.y,-p.x); }
                                                                                                                                                     }
    type operator *(point p) { return x*p.x + y*p.y; }
   //cross product
                                                                    //for reading purposes avoid using * and % operators, use the
                                                                                                                                                 sort(pts.begin() + l, pts.begin() + r, cmp_y());
    type operator %(point p) { return x*p.y - y*p.x; }
                                                                    functions below:
                                                                                                                                                 return;
                                                                    type dot(point p, point q)
                                                                                                                                             }
                                                                                                   { return p.x*q.x + p.y*q.y; }
    bool operator ==(const point &p) const{ return x == p.x and y type cross(point p, point q) { return p.x*q.y - p.y*q.x; }
== p.y; }
                                                                                                                                             int m = (l + r) >> 1;
   bool operator !=(const point &p) const{ return x != p.x or y ! //double area
                                                                                                                                             type midx = pts[m].x:
                                                                    type area 2(point a, point b, point c) { return cross(a,b) +
                                                                                                                                             closest pair(l, m);
    bool operator < (const point &p) const { return (x < p.x) or (x cross(b,c) + cross(c,a); }
                                                                                                                                             closest pair(m, r);
== p.x and y < p.y); }
                                                                    //angle between (a1 and b1) vs angle between (a2 and b2)
                                                                                                                                               merge(pts.begin() + l, pts.begin() + m, pts.begin() + m,
    // 0 => same direction
                                                                    //1 : bigger
                                                                                                                                         pts.begin() + r. stripe.begin(), cmp v());
   // 1 => p is on the left
                                                                    //-1 : smaller
                                                                                                                                             copy(stripe.begin(), stripe.begin() + r - l, pts.begin() + l);
    //-1 \Rightarrow p is on the right
   int dir(point o, point p) {
                                                                    int angle less(const point& al, const point& bl, const point& a2,
                                                                                                                                             int stripe sz = 0;
       type x = (*this - o) % (p - o);
                                                                    const point& b2) {
                                                                                                                                             for (int i = l; i < r; ++i) {
        return ge(x,0) - le(x,0);
                                                                        point p1(dot( a1, b1), abs(cross( a1, b1)));
                                                                                                                                                 if (abs(pts[i].x - midx) < min dist) {</pre>
                                                                        point p2(dot( a2, b2), abs(cross( a2, b2)));
                                                                                                                                                        for (int j = stripe sz - 1; j >= 0 \& \text{pts[i].y} -
                                                                        if(cross(p1, p2) < 0) return 1;</pre>
                                                                                                                                         stripe[j].y < min dist; --j)</pre>
   bool on seg(point p, point q) {
                                                                        if(cross(p1, p2) > 0) return -1;
                                                                                                                                                         upd ans(pts[i], stripe[j]);
       if (this->dir(p, q)) return 0;
                                                                        return 0;
                                                                                                                                                     stripe[stripe_sz++] = pts[i];
         return ge(x, min(p.x, q.x)) and le(x, max(p.x, q.x)) and }
                                                                                                                                                 }
ge(y, min(p.y, q.y)) and le(y, max(p.y, q.y));
                                                                                                                                             }
                                                                    ostream &operator<<(ostream &os, const point &p) {
                                                                                                                                         }
                                                                        os << "(" << p.x << "," << p.y << ")";
   ld abs() { return sqrt(x*x + y*y); }
                                                                        return os;
                                                                                                                                         int main(){
    type abs2() { return x*x + y*y; }
                                                                    }
                                                                                                                                             //read and save in vector pts
   ld dist(point q) { return (*this - q).abs(); }
                                                                                                                                             min_dist = LINF;
                                                                    Closest pair
    type dist2(point q) { return (*this - q).abs2(); }
                                                                                                                                             stripe.resize(n);
                                                                    #include "basics.cpp"
                                                                                                                                             sort(pts.begin(), pts.end());
   ld arg() { return atan2l(y, x); }
                                                                                                                                             closest pair(0, n);
                                                                    //DIVIDE AND CONOUER METHOD
                                                                                                                                         }
                                                                    //Warning: include variable id into the struct point
   // Project point on vector y
   point project(point y) { return y * ((*this * y) / (y * y)); } struct cmp y {
                                                                                                                                         //LINE SWEEP
                                                                        bool operator()(const point & a, const point & b) const {
   // Project point on line generated by points x and y
                                                                                                                                         int n; //amount of points
                                                                            return a.v < b.v;</pre>
  point project(point x, point y) { return x + (*this - x).project(y-
                                                                                                                                         point pnt[N]:
                                                                        }
x): }
                                                                    };
                                                                                                                                         struct cmp y {
   ld dist line(point x, point y) { return dist(project(x, y)); } ld min_dist = LINF;
                                                                                                                                             bool operator()(const point & a, const point & b) const {
                                                                                                                                                 if(a.y == b.y) return a.x < b.x;</pre>
                                                                    pair<int, int> best pair;
   ld dist seg(point x, point y) {
                                                                                                                                                 return a.y < b.y;</pre>
                                                                    vector<point> pts, stripe;
          return project(x, y).on_seg(x, y) ? dist_line(x, y) : int n;
                                                                                                                                             }
min(dist(x), dist(y));
                                                                                                                                         };
                                                                    void upd ans(const point & a, const point & b) {
                                                                                                                                         ld closest pair() {
                                                                         ld \ dist = sqrt((a.x - b.x)*(a.x - b.x) + (a.y - b.y)*(a.y -
   point rotate(ld sin, ld cos) { return point(cos*x - sin*y, sin*x b.y));
                                                                                                                                           sort(pnt, pnt+n);
+ cos*y); }
                                                                                                                                           ld best = numeric limits<double>::infinity();
                                                                        if (dist < min dist) {</pre>
    point rotate(ld a) { return rotate(sin(a), cos(a)); }
                                                                                                                                           set<point, cmp y> box;
                                                                            min dist = dist:
                                                                            // best pair = {a.id, b.id};
   // rotate around the argument of vector p
                                                                                                                                           box.insert(pnt[0]);
                                                                        }
     point rotate(point p) { return rotate(p.y / p.abs(), p.x /
                                                                                                                                           int l = 0;
```

```
for (int i = 1; i < n; i++){
   while(l < i and pnt[i].x - pnt[l].x > best)
     box.erase(pnt[l++]);
     for(auto it = box.lower bound({0, pnt[i].y - best}); it !=
box.end() and pnt[i].y + best >= it->y; it++)
     best = min(best, hypot(pnt[i].x - it->x, pnt[i].y - it->y));
   box.insert(pnt[i]);
 }
 return best;
Data structures
Treap
// Implicit segment tree implementation
struct Node{
   int value:
   int cnt:
   int priority;
   Node *left, *right;
```

```
Node(int p) : value(p), cnt(1), priority(gen()), left(NULL),
right(NULL) {};
};
typedef Node* pnode:
int get(pnode q){
    if(!q) return 0;
    return q->cnt;
}
void update_cnt(pnode &q){
    if(!q) return;
    q \rightarrow cnt = get(q \rightarrow left) + get(q \rightarrow right) + 1;
}
void merge(pnode &T, pnode lef, pnode rig){
    if(!lef) {
        T=rig;
         return;
    if(!rig){
        T=lef;
         return:
    if(lef->priority > rig->priority){
        merge(lef->right, lef->right, rig);
        T = lef:
    else{
        merge(rig->left, lef, rig->left);
        T = rig;
    update_cnt(T);
}
void split(pnode cur. pnode &lef, pnode &rig, int kev){
```

```
if(!cur){
        lef = rig = NULL;
        return;
    int id = get(cur->left) + 1;
    if(id <= key){</pre>
       split(cur->right, cur->right, rig, key - id);
        lef = cur;
   }
    else{
        split(cur->left, lef, cur->left, key);
        rig = cur;
   }
    update_cnt(cur);
Sparse table
const int N;
const int M; //log2(N)
int sparse[N][M];
void build() {
  for(int i = 0; i < n; i++)
    sparse[i][0] = v[i];
  for(int j = 1; j < M; j++)
    for(int i = 0; i < n; i++)
      sparse[i][j] =
       i + (1 << j - 1) < n
       ? min(sparse[i][j-1], sparse[i+(1 << j-1)][j-1])
       : sparse[i][i - 1]:
}
int query(int a, int b){
 int pot = 32 - builtin clz(b - a) - 1;
 return min(sparse[a][pot], sparse[b - (1 << pot) + 1][pot]);</pre>
Trie
 c-='a':
 if (trie[u][c]) return trie[u][c];
  return trie[u][c] = ++trien:
```

```
// Trie <0(|S|), 0(|S|)>
int trie[N][26], trien = 1;
int add(int u, char c){
//to add a string s in the trie
int u = 1:
for(char c : s) u = add(u, c);
```

Aho-Corasick

```
const int K = 26; string target; int curr = 0;
int ans = 0; int taking = 0;
struct Vertex {
    int next[K]:
    bool output = false;
    int p = -1; // parent node
    char pch; // "transition" character from parent to this node
    int link = -1; // fail link
   int qo[K]; // if need more memory can delete this and use "next"
    // additional potentially useful things
    int depth = -1;
    // longest string that has an output from this vertex
    int exitlen = -1;
   Vertex(int p=-1, char ch='$') : p(p), pch(ch) {
        fill(begin(next), end(next), -1);
        fill(begin(go), end(go), -1);
   }
};
vector<Vertex> t(1):
void add string(string const& s) {
   int v = 0:
    for (char ch : s) {
        int c = ch - 'a';
        if (t[v].next[c] == -1) {
            t[v].next[c] = t.size();
           t.emplace back(v, ch); // !!!!! ch not c
        v = t[v].next[c]:
   }
    t[v].output = true;
int go(int v, char ch);
int get link(int v) {
   if (t[v].link == -1) {
        if (v == 0 || t[v].p == 0)
            t[v].link = 0;
            t[v].link = qo(qet link(t[v].p), t[v].pch);
    return t[v].link;
}
int go(int v, char ch) {
   int c = ch - 'a';
    if (t[v].go[c] == -1) {
        if (t[v].next[c] != -1)
            t[v].go[c] = t[v].next[c];
        else
            // !!!!! ch not c
            t[v].go[c] = v == 0 ? 0 : go(get link(v), ch);
    return t[v].go[c];
```

```
// int go(int v, char ch) { // go without the go[K] variable
                                                                 * Usage: dist[node]
                                                                                                                                         if (low[v] >= num[u]) art[u] = 1;
      int c = ch - 'a';
                                                                 * Notation: m:
                                                                                                                                         if (low[v] > num[u]) { /* u-v bridge */ }
                                                                                      number of edges
      if (t[v].next[c] == -1) {
                                                                                (a, b, w): edge between a and b with weight w
                                                                                                                                         low[u] = min(low[u], low[v]);
          // !!!!! ch not c
          t[v].next[c] = v == 0 ? 0 : go(get_link(v), ch);
                                                                                    starting node
                                                                                                                                       else if (v != par[u]) low[u] = min(low[u], num[v]);
                                                                                            parent node of u, used to rebuild the
//
       return t[v].next[c];
int get_depth(int v){
                                                                                                                                   for (int i = 0; i < n; ++i) if (!num[i])
    if (t[v].depth == -1){
                                                                 vector<int> adj[N], adjw[N];
                                                                                                                                     articulation(i), art[i] = ch[i]>1;
       if (v == 0) {
                                                                 int dist[N];
                                                                                                                                   Dinic's max flow / matching
           t[v].depth = 0;
       } else {
                                                                 memset(dist, 63, sizeof(dist));
                                                                                                                                   Time complexity:
           t[v].depth = get_depth(t[v].p)+1;
                                                                 priority queue<pii> pq;
                                                                                                                                   • generally: O(EV^2)
                                                                 pq.push(mp(0,0));
                                                                                                                                   • small flow: O(F(V+E))
                                                                                                                                   • bipartite graph or unit flow: O(E\sqrt{V})
                                                                 while (!pq.empty()) {
    return t[v].depth;
                                                                   int u = pq.top().nd;
                                                                                                                                   Usage:
int get exitlen(int v){
                                                                   int d = -pq.top().st;
                                                                                                                                   • dinic()
    if (t[v].exitlen == -1){
                                                                   pq.pop();
                                                                                                                                   • add_edge(from, to, capacity)
       if (v == 0){
           t[v].exitlen = 0;
                                                                   if (d > dist[u]) continue;
                                                                                                                                   • recover() (optional)
       } else if (t[v].output) {
                                                                   for (int i = 0; i < adj[u].size(); ++i) {</pre>
                                                                                                                                   #include <bits/stdc++.h>
                                                                     int v = adj[u][i];
           t[v].exitlen = get depth(v);
                                                                                                                                   using namespace std;
                                                                     int w = adjw[u][i];
           t[v].exitlen = get exitlen(get link(v));
                                                                     if (dist[u] + w < dist[v])</pre>
                                                                                                                                   const int N = 1e5+1. INF = 1e9:
                                                                       dist[v] = dist[u]+w, pq.push(mp(-dist[v], v));
                                                                                                                                   struct edge {int v, c, f;};
                                                                   }
    return t[v].exitlen;
                                                                 }
                                                                                                                                   int src, snk, h[N], ptr[N];
}
                                                                                                                                   vector<edge> edgs;
                                                                 Floyd-warshall
                                                                  vector<int> g[N];
Graph algorithms
                                                                  * FLOYD-WARSHALL ALGORITHM (SHORTEST PATH TO ANY VERTEX)
                                                                                                                                   void add_edge (int u, int v, int c) {
Bellman-Ford
                                                                                                                                     int k = edgs.size();
                                                                 * Time complexity: 0(V^3)
void solve()
                                                                                                                                     edgs.push_back({v, c, 0});
                                                                 * Usage: dist[from][to]
                                                                                                                                     edgs.push back(\{u, 0, 0\});
                                                                 * Notation: m:
                                                                                     number of edges
    vector<int> d(n, INF);
                                                                                                                                     g[u].push back(k);
                                                                         n:
                                                                                   number of vertices
    d[v] = 0;
                                                                                                                                     g[v].push_back(k+1);
                                                                                (a, b, w): edge between a and b with weight w
    for (;;) {
       bool any = false;
                                                                                                                                   void clear() {
       for (Edge e : edges)
                                                                                                                                       memset(h, 0, sizeof h);
                                                                 int adj[N][N]; // no-edge = INF
           if (d[e.a] < INF)
                                                                                                                                       memset(ptr, 0, sizeof ptr);
               if (d[e.b] > d[e.a] + e.cost) {
                                                                                                                                       edgs.clear();
                                                                 for (int k = 0; k < n; ++k)
                   d[e.b] = d[e.a] + e.cost;
                                                                                                                                       for (int i = 0; i < N; i++) q[i].clear();</pre>
                                                                   for (int i = 0; i < n; ++i)
                   anv = true:
                                                                                                                                       src = 0:
                                                                     for (int j = 0; j < n; ++j)
                                                                                                                                       snk = N-1:
                                                                       adj[i][j] = min(adj[i][j], adj[i][k]+adj[k][j]);
       if (!any)
                                                                 Bridges & articulations
           break;
                                                                                                                                   bool bfs() {
                                                                 // Articulation points and Bridges O(V+E)
                                                                                                                                     memset(h, 0, sizeof h);
                                                                 int par[N], art[N], low[N], num[N], ch[N], cnt;
    // display d. for example, on the screen
                                                                                                                                     aueue<int> a:
                                                                                                                                     h[src] = 1;
                                                                 void articulation(int u) {
                                                                                                                                     q.push(src);
                                                                   low[u] = num[u] = ++cnt;
Diikstra
                                                                                                                                     while(!q.empty()) {
/**********<mark>for.v.:. adj[u]) {</mark>
                                                                                                                                      int u = q.front(); q.pop();
                                                                     if (!num[v]) {
                                                                                                                                       for(int i : g[u]) {
   DIJKSTRA'S ALGORITHM (SHORTEST PATH TO A VERTEX)
                                                                       par[v] = u; ch[u] ++;
                                                                                                                                        int v = edgs[i].v;
```

* Time complexity: O((V+E)logE)

articulation(v);

```
if (!h[v] and edgs[i].f < edgs[i].c)</pre>
        q.push(v), h[v] = h[u] + 1;
  }
  return h[snk];
}
int dfs (int u, int flow) {
  if (!flow or u == snk) return flow;
  for (int &i = ptr[u]; i < g[u].size(); ++i) {</pre>
    edge \&dir = edgs[g[u][i]], \&rev = edgs[g[u][i]^1];
    int v = dir.v;
    if (h[v] != h[u] + 1) continue;
    int inc = min(flow, dir.c - dir.f);
    inc = dfs(v, inc):
    if (inc) {
      dir.f += inc, rev.f -= inc;
      return inc:
  return 0;
int dinic() {
  int flow = 0;
  while (bfs()) {
    memset(ptr, 0, sizeof ptr);
    while (int inc = dfs(src, INF)) flow += inc:
  }
  return flow;
//Recover Dinic
void recover(){
  for(int i = 0; i < edgs.size(); i += 2){
    //edge (u \rightarrow v) is being used with flow f
    if(edgs[i].f > 0) {
      int v = edgs[i].v;
      int u = edgs[i^1].v;
  }
}
int main () {
    // TEST CASE
    d::clear():
    d::add edge(d::src,1,1);
    d::add edge(d::src,2,1);
    d::add edge(d::src,2,1);
    d::add edge(d::src,2,1);
    d::add edge(2.3.d::INF):
    d::add edge(3,4,d::INF);
    d::add edge(1,d::snk,1);
    d::add edge(2,d::snk,1);
    d::add edge(3,d::snk,1);
    d::add_edge(4,d::snk,1);
    cout<<d::dinic()<<endl; // SHOULD OUTPUT 4</pre>
```

```
d::recover();
```

Flow with demands

Finding an arbitrary flow

- Assume a network with [L; R] on edges (some may have L = 0), let's call it old network.
- Create a New Source and New Sink (this will be the src and snk for Dinic).
- Modelling network:
 - 1. Every edge from the old network will have cost R-L
 - 2. Add an edge from New Source to every vertex v with cost:
 - S(L) for every (u, v). (sum all L that LEAVES v)
 - 3. Add an edge from every vertex v to New Sink with cost:
 - S(L) for every (v, w). (sum all L that ARRIVES v)
- 4. Add an edge from Old Source to Old Sink with cost INF (circulation problem)
- The Network will be valid if and only if the flow saturates the network (max flow == S(L))

Finding Min Flow

- To find min flow that satisfies just do a binary search in the (Old Sink
 Old Source) edge
- The cost of this edge represents all the flow from old network
- Min flow = S(L) that arrives in Old Sink + flow that leaves (Old Sink -> Old Source)

Kosaraju's algorithm

```
//Undirected version:
* KOSARAJU'S ALGORITHM (GET EVERY STRONGLY CONNECTED COMPONENTS
                                                                 int par[N];
* Description: Given a directed graph, the algorithm generates a
                                                                 void dfs(int u) {
list of every
                                                                   vis[u] = 1;
* strongly connected components. A SCC is a set of points in which
                                                                   for (auto v : adj[u]) if(!vis[v]) par[v] = u, dfs(v);
vou can reach *
                                                                   ord[ordn++] = u;
* every point regardless of where you start from. For instance,
cvcles can be
   a SCC themselves or
                                      οf
                                               areater
                                                                 void dfst(int u) {
                                                                   scc[u] = scc\_cnt, vis[u] = 0;
* This algorithm starts with a DFS and generates an array called
                                                                   for (auto v : adj[u]) if(vis[v] and u != par[v]) dfst(v);
"ord" which
* stores vertices according to the finish times (i.e. when it reaches
                                                                 // add edge: u -> v
* Then, it makes a reversed DFS according to "ord" list. The set of
                                                                 void add edge(int u, int v){
                                                                   adj[u].push back(v);
   visited by the reversed DFS defines a new SCC.
                                                                   adj[v].push back(u);
* One of the uses of getting all SCC is that you can generate a new
DAG (Directed *
* Acyclic Graph), easier to work with, in which each SCC being a
"supernode" of *
                                                               // run kosaraju
* the DAG.
                                                               void kosaraju(){
* Time complexity: O(V+E)
                                                                 for (int i = 1; i <= n; ++i) if (!vis[i]) dfs(i);</pre>
   Notation: adj[i]:
                              adjacency
                                        list for
                                                     node
                                                                 for (int i = ordn - 1; i \ge 0; --i) if (vis[ord[i]]) scc cnt++,
                                                               dfst(ord[i]);
                adjt[i]: reversed adjacency list for node i
```

```
ord:
                       array of vertices according to their finish
time
         ordn:
                ord counter
        scc[i]: supernode assigned to i
                   scc cnt: amount of supernodes in the graph
const int N = 2e5 + 5:
vector<int> adj[N], adjt[N];
int n, ordn, scc_cnt, vis[N], ord[N], scc[N];
//Directed Version
void dfs(int u) {
  vis[u] = 1:
  for (auto v : adj[u]) if (!vis[v]) dfs(v);
  ord[ordn++] = u;
void dfst(int u) {
  scc[u] = scc cnt, vis[u] = 0;
  for (auto v : adjt[u]) if (vis[v]) dfst(v);
// add edge: u -> v
void add edge(int u, int v){
  adj[u].push back(v);
  adjt[v].push_back(u);
```

Lowest common ancestor (LCA)

```
// Lowest Common Ancestor <0(nlogn), 0(logn)>
const int N = 1e6. M = 25:
int anc[M][N], h[N], rt;
// TODO: Calculate h[u] and set anc[0][u] = parent of node u for
each u
// build (sparse table)
anc[0][rt] = rt; // set parent of the root to itself
for (int i = 1; i < M; ++i)
 for (int j = 1; j \le n; ++j)
   anc[i][j] = anc[i-1][anc[i-1][j]];
// guery
int lca(int u, int v) {
 if (h[u] < h[v]) swap(u, v);
 for (int i = M-1; i \ge 0; --i) if (h[u]-(1<< i) \ge h[v])
   u = anc[i][u]:
 if (u == v) return u;
 for (int i = M-1; i \ge 0; --i) if (anc[i][u] != anc[i][v])
   u = anc[i][u], v = anc[i][v]:
 return anc[0][u]:
```

String Processing

Knuth-Morris-Pratt (KMP)

```
// Knuth-Morris-Pratt - String Matching O(n+m)
char s[N], p[N]:
int b[N], n, m; // n = strlen(s), m = strlen(p);
void kmppre() {
  b[0] = -1;
  for (int i = 0, j = -1; i < m; b[++i] = ++j)
    while (j \ge 0 \text{ and } p[i] != p[j])
      i = b[i];
}
void kmp() {
  for (int i = 0, j = 0; i < n;) {
    while (j \ge 0 \text{ and } s[i] != p[j]) j=b[j];
    i++, j++;
    if (j == m) {
      // match position i-j
      i = b[i];
    }
  }
```

Suffix Array

```
// Suffix Array O(nlogn)
// s.push('$');
vector<int> suffix_array(string &s){
 int n = s.size(), alph = 256;
 vector<int> cnt(max(n, alph)), p(n), c(n);
```

```
for(auto c : s) cnt[c]++;
  for(int i = 1; i < alph; i++) cnt[i] += cnt[i - 1];</pre>
  for(int i = 0; i < n; i++) p[--cnt[s[i]]] = i;
  for(int i = 1; i < n; i++)
    c[p[i]] = c[p[i - 1]] + (s[p[i]] != s[p[i - 1]]);
  vector<int> c2(n), p2(n);
  for(int k = 0; (1 << k) < n; k++){
   int classes = c[p[n - 1]] + 1;
    fill(cnt.begin(), cnt.begin() + classes, 0);
    for(int i = 0; i < n; i++) p2[i] = (p[i] - (1 << k) + n)%n;
    for(int i = 0: i < n: i++) cnt[c[i]]++:
    for(int i = 1; i < classes; i++) cnt[i] += cnt[i - 1];</pre>
    for(int i = n - 1; i \ge 0; i--) p[--cnt[c[p2[i]]]] = p2[i];
    c2[p[0]] = 0;
    for(int i = 1: i < n: i++){
      pair<int, int> b1 = {c[p[i]], c[(p[i] + (1 << k))%n]};
     pair<int, int> b2 = {c[p[i - 1]], c[(p[i - 1] + (1 << k))%n]};
      c2[p[i]] = c2[p[i - 1]] + (b1 != b2);
    c.swap(c2);
 }
 return p;
// Longest Common Prefix with SA O(n)
vector<int> lcp(string &s, vector<int> &p){
 int n = s.size();
 vector<int> ans(n - 1), pi(n);
  for(int i = 0; i < n; i++) pi[p[i]] = i;
  int lst = 0;
  for(int i = 0; i < n - 1; i++){
   if(pi[i] == n - 1) continue;
   while(s[i + lst] == s[p[pi[i] + 1] + lst]) lst++;
    ans[pi[i]] = lst;
   lst = \max(0, lst - 1);
 }
  return ans:
// Longest Repeated Substring O(n)
int 1rs = 0:
for (int i = 0; i < n; ++i) lrs = max(lrs, lcp[i]);
// Longest Common Substring O(n)
// m = strlen(s);
// strcat(s, "$"); strcat(s, p); strcat(s, "#");
// n = strlen(s);
int lcs = 0:
for (int i = 1; i < n; ++i) if ((sa[i] < m) != (sa[i-1] < m))
 lcs = max(lcs, lcp[i]);
```

```
// To calc LCS for multiple texts use a slide window with mingueue
// The number of different substrings of a string is n*(n + 1)/2
- sum(lcs[i])
```

Rabin-Karp

```
// Rabin-Karp - String Matching + Hashing O(n+m)
const int B = 31:
char s[N], p[N]:
int n, m; // n = strlen(s), m = strlen(p)
void rabin() {
 if (n<m) return:
  ull hp = 0, hs = 0, E = 1;
  for (int i = 0; i < m; ++i)
   hp = ((hp*B)%MOD + p[i])%MOD,
   hs = ((hs*B)%MOD + s[i])%MOD,
   E = (E*B)%MOD;
  if (hs == hp) { /* matching position 0 */ }
  for (int i = m; i < n; ++i) {</pre>
   hs = ((hs*B)%MOD + s[i])%MOD;
   hhs = (hs - s[i-m]*E%MOD + MOD)%MOD;
   if (hs == hp) { /* matching position i-m+1 */ }
 }
```

Z-function

The Z-function of a string s is an array z where z_i is the length of the longest substring starting from s_i which is also a prefix of s.

Examples:

```
• "aaaaa": [0, 4, 3, 2, 1]
• "aaabaab": [0, 2, 1, 0, 2, 1, 0]
• "abacaba": [0, 0, 1, 0, 3, 0, 1]
vector<int> zfunction(const string& s){
 vector<int> z (s.size());
 for (int i = 1, l = 0, r = 0, n = s.size(); i < n; i++){
   if (i \le r) z[i] = min(z[i-l], r - i + 1);
   while (i + z[i] < n \text{ and } s[z[i]] == s[z[i] + i]) z[i] ++;
   if (i + z[i] - 1 > r) l = i, r = i + z[i] - 1:
 }
  return z:
```

Manacher's

```
// Manacher (Longest Palindromic String) - O(n)
int lps[2*N+5];
char s[N];
int manacher() {
 int n = strlen(s):
 string p (2*n+3, '#');
  p[0] = '^';
  for (int i = 0; i < n; i++) p[2*(i+1)] = s[i];
  p[2*n+2] = '$';
```

```
int k = 0, r = 0, m = 0;
  int l = p.length();
                                                                    type eval(int id, type x) { return hull[id].b + hull[id].m * x; }
  for (int i = 1; i < l; i++) {
                                                                    // Linear search query - O(n) for all queries
    int 0 = 2*k - i;
                                                                    // Only possible if the queries always move to the right
    lps[i] = (r > i) ? min(r-i, lps[o]) : 0;
    while (p[i + 1 + lps[i]] == p[i - 1 - lps[i]]) lps[i]++;
                                                                    type query(type x) {
    if (i + lps[i] > r) k = i, r = i + lps[i];
                                                                     while (pos+1 < nh \text{ and } eval(pos, x) < eval(pos+1, x)) pos++;
    m = max(m, lps[i]);
                                                                      return eval(pos, x);
                                                                      // return -eval(pos, x); ATTENTION: Uncomment for minimum CHT
 return m;
                                                                    // Ternary search query - O(logn) for each query
Dynamic programming
                                                                    type query(type x) {
                                                                     int lo = 0, hi = nh-1:
Convex hull trick
                                                                     while (lo < hi) {
// Convex Hull Trick
                                                                        int mid = (lo+hi)/2:
                                                                        if (eval(mid, x) > eval(mid+1, x)) hi = mid;
// ATTENTION: This is the maximum convex hull. If you need the
                                                                        else lo = mid+1:
// CHT use {-b, -m} and modify the query function.
                                                                      return eval(lo, x);
                                                                      // return -eval(lo, x):
                                                                                                 ATTENTION: Uncomment for minimum CHT
// In case of floating point parameters swap long long with long
double
typedef long long type;
                                                                    // better use geometry line intersect (this assumes s and t are not
struct line { type b, m; };
                                                                    parallel)
                                                                    ld intersect x(line s, line t) { return (t.b - s.b)/(ld)(s.m - t.m); }
line v[N]: // lines from input
                                                                    ld intersect y(line s, line t) { return s.b + s.m * intersect x(s,
int n: // number of lines
                                                                    t); }
// Sort slopes in ascending order (in main):
                                                                    */
sort(v, v+n, [](line s, line t){
     return (s.m == t.m) ? (s.b < t.b) : (s.m < t.m); });
                                                                    Longest Increasing Subsequence
                                                                    // Longest Increasing Subsequence - O(nlogn)
// nh: number of lines on convex hull
// pos: position for linear time search
                                                                    // dp(i) = max j < i \{ dp(j) | a[j] < a[i] \} + 1
// hull: lines in the convex hull
                                                                    //
int nh, pos;
line hull[N];
                                                                    // int dp[N], v[N], n, lis;
bool check(line s, line t, line u) {
                                                                    memset(dp, 63, sizeof dp);
  // verify if it can overflow. If it can just divide using long
                                                                    for (int i = 0; i < n; ++i) {
double
                                                                     // increasing: lower bound
  return (s.b - t.b)*(u.m - s.m) < (s.b - u.b)*(t.m - s.m);
                                                                      // non-decreasing: upper bound
}
                                                                      int j = lower_bound(dp, dp + lis, v[i]) - dp;
                                                                      dp[j] = min(dp[j], v[i]);
// Add new line to convex hull, if possible
                                                                      lis = \max(lis, j + 1);
// Must receive lines in the correct order, otherwise it won't work
void update(line s) {
 // 1. if first lines have the same b, get the one with bigger m
 // 2. if line is parallel to the one at the top, ignore
 // 3. pop lines that are worse
 // 3.1 if you can do a linear time search, use
 // 4. add new line
 if (nh == 1 and hull[nh-1].b == s.b) nh--;
  if (nh > 0 and hull[nh-1].m >= s.m) return;
  while (nh >= 2 and !check(hull[nh-2], hull[nh-1], s)) nh--;
  pos = min(pos, nh):
  hull[nh++] = s;
```