

第二次离散数学作业

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Let $C(x)$ be the propositional function "x" is in your class.

1.1 a

Let $M(x)$ be the propositional function "x" has a mobile phone.

(1) $\forall x M(x)$

(2) $\forall x (C(x) \wedge M(x))$

1.2 c

Let $S(x)$ be the propositional function "x" can swim.

(1) $\exists x \neg S(x)$

(2) $\exists x (C(x) \wedge \neg S(x))$

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2.1 a

Let $V(x)$ be the propositional function "x" qualifies as a vip. Let $F(x,y)$ be the propositional function "x" flies more than "y" miles a year. Let $N(x,y)$ be the propositional function "x" flies more than "y" times a year.

$$\forall x ((F(x, 25000) \vee N(x, 25)) \rightarrow V(x))$$

2.2 b

Let $M(x)$ be the propositional function "x" is male. Let $T(x,y)$ be the propositional function "x" is able to finish a marathon in less than y hours. Let $Q(x)$ be the propositional function "x" is qualified for the marathon.

$$\forall x(((M(x) \wedge T(x, 3)) \vee (\neg M(x) \wedge T(x, 3.5))) \rightarrow Q(x))$$

2.3 c

Let $Q(x)$ be the propositional function "x" is qualified for a master's degree. Let $B(x)$ be the propositional function "x" gets higher than B in every subject. Let $S(x,y)$ be the propositional function "x" gets more than "y" credits. Let $P(x)$ be the propositional function "x" passed the master thesis defense.

$$\forall x((B(x) \wedge (S(x, 60) \vee (S(x, 45) \wedge P(x)))) \rightarrow Q(x))$$

2.4 d

Let $V(x)$ be the propositional function "x" has learned 21 credit course in a term. Let $A(x)$ be the propositional function "x" got A for all course. Let $S(x)$ be the propositional function "x" is a student.

$$\exists x(S(x) \wedge (V(x) \wedge A(x)))$$

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They are not equivalent. For example, if $P(x)$ is sometimes true and sometimes false, then $\forall x(P(x) \rightarrow Q(x))$ is false but $\forall xP(x) \rightarrow \forall xQ(x)$ is true.

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4.1 a

$$\forall x(P(x) \rightarrow \neg S(x))$$

4.2 b

$$\forall x(R(x) \rightarrow S(x))$$

4.3 c

$$\forall x(Q(x) \rightarrow P(x))$$

4.4 d

$$\forall x(Q(x) \rightarrow \neg R(x))$$

4.5 e

Yes, we can. From (a) and (c), we know that $\forall x(Q(x) \rightarrow \neg S(x))$. But according to (b), $\forall x(R(x) \rightarrow S(x))$. So $\forall x(Q(x) \rightarrow \neg R(x))$.