
Problem Statement:

Find the top k most frequent elements from a list of integers.

Blind Solution

```
def most_frequent_elements_blind(nums: List[int], element_count: int) -> List[int]:
    freq_counts = defaultdict(int) # A default dict initialises new keys without key errors
    most_frequent_keys = []

    for num in nums:
        freq_counts[num] += 1

    print(freq_counts)

    for _ in range(element_count):
        max_key = max(freq_counts, key=freq_counts.get)
        most_frequent_keys.append(max_key)
        freq_counts.pop(max_key)

    return most_frequent_keys
```

Step-by-Step Breakdown

1. Input:

- `nums = [1, 2, 2, 3, 3, 3, 4, 4, 4, 4, 4]`
- `element_count = 2.`

2. Frequency Count:

Use a defaultdict to count the occurrences of each number. After iterating through `nums`, the frequency map will look like this:

```
freq_counts = { 1: 1,
                2: 2,
                3: 3,
                4: 5 }
```

3. Finding Maximums Repeatedly:

For each of the top k elements (`element_count = 2`):

○ First Iteration:

- `max_key = 4` (highest frequency is 5).
- Append 4 to `most_frequent_keys`.
- Pop 4 from the frequency map:
- `freq_counts = { 1: 1,`
`2: 2,`

3: 3 }

- **Second Iteration:**

- max_key = 3 (highest frequency is now 3).
- Append 3 to most_frequent_keys.
- Pop 3 from the frequency map:
- freq_counts = { 1: 1,
2: 2 }

4. **Output:** most_frequent_keys = [4, 3]

5. **Efficiency:**

- Counting frequencies: $O(n)$, where n is the number of elements in `nums`.
- Finding the max key k times: $O(k \cdot m)$, where m is the size of `freq_counts`.
- Total: **$O(k \cdot m + n)$**

Optimised Heap-Based Solution

```
def most_frequent_elements(nums: List[int], element_count: int) -> List[int]:  
    # Count freq of each element  
    freq_counts = Counter(nums) # O(n)  
  
    # Use a heap to find top k elements  
    most_frequent_keys = heapq.nlargest(element_count, freq_counts.keys(), key=freq_counts.get)  
  
    return most_frequent_keys
```

Step-by-Step Breakdown

1. **Input:**

- `nums` = [1, 2, 2, 3, 3, 3, 4, 4, 4, 4]
- `element_count` = 2.

2. **Frequency Count:**

Use `Counter` to count occurrences of each number. After processing `nums`, the frequency map is:

- `freq_counts` = { 4: 5,
3: 3,
2: 2,
1: 1})

3. **Using `heapq.nlargest`:**

- `heapq.nlargest()` finds the top k elements efficiently by building a max-heap under the hood.
- The heap uses the `freq_counts.get` function to prioritise elements by their frequency.
- Steps:
 - Extract 4 (highest frequency).
 - Extract 3 (second highest frequency).

4. Output:

- `most_frequent_keys = [4, 3]`

5. Efficiency:

- Counting frequencies: $O(n)$, where n is the number of elements in `nums`.
- Building the heap and extracting the top k elements: $O(n+k \cdot \log n)$.
- Total: **$O(n+k \cdot \log n)$**

Comparison

Aspect	Blind Solution	Heap Solution
Efficiency	$O(k \cdot m + n)$	$O(n + k \cdot \log n)$
Memory Usage	Minimal (uses <code>defaultdict</code>)	Moderate (heap + Counter)
Ease of Implementation	Simple and intuitive	Slightly more complex
Scalability	Slower for large inputs	Scales better for large inputs
