### **Problem Statement:**

Given a sorted list of integers (numbers) in non-decreasing order and a target integer (target), find the indices (1-indexed) of two numbers in the list that add up to the target. The solution must use O(1) additional space and ensure that the first index is less than the second.

#### Solution 1

```
def two_sum(numbers: list[int], target: int) -> list[int]:
    if not numbers:
        return []

left, right = 0, len(numbers) - 1
    while left < right:
        two_sum = numbers[left] + numbers[right]

    if two_sum == target:
        return [left + 1, right + 1]

    if two_sum < target:
        left += 1
        else:
        right -= 1</pre>
```

### Step-by-Step Breakdown

### 1. Input:

- numbers: A sorted list of integers, e.g., [2, 7, 11, 15].
- o target: An integer representing the desired sum, e.g., 9.

### 2. Intermittent step 1:

- o Edge Case Check:
  - If numbers is empty, return an empty list [].

### 3. Intermittent step 2:

- Initialize Two Pointers:
  - Set left to the start index (0).
  - Set right to the last index (len(numbers) 1).
- o Iterate with Two-Pointer Technique:
  - While left < right, compute the sum of numbers[left] + numbers[right].</li>

# Compare Sum to Target:

- If the computed sum equals the target, return [left + 1, right + 1] (converting to 1-indexed positions).
- If the sum is less than target, increment left to try a larger value.
- If the sum is greater than target, decrement right to try a smaller value.

# 4. Output:

- If a valid pair is found, the function returns their 1-indexed positions as a list, e.g., [1, 2].
- o If no such pair exists, the function returns an empty list [].

# 5. Efficiency:

- o Time Complexity: O(n) Each element is examined at most once.
- Space Complexity: O(1) Only a few pointers are used regardless of the input size, meeting the O(1) additional space requirement.

# **Visual Flow Diagram**

```
1.
                  Input: numbers = [2, 7, 11, 15], target = 9
 2.
 3.
 4.
                   Check if numbers is empty
                                                  -Yes---> Return []
 5.
 6.
 7.
 8.
              Initialize pointers: left = ∅, right = 3
 9.
10.
11.
12.
13.
                       while left < right:</pre>
14.
15.
16.
17.
                 Compute current_sum = numbers[left] + numbers[right]
18.
19.
20.
21.
              Is current_sum equal to target?
22.
23.
24.
                     Yes
                                           No
25.
26.
27. Return [left+1, right+1]
28.
                                    Is current_sum < target?</pre>
29.
30.
31.
                                         Yes
                                                       No
32.
33.
34.
                                     Increment left Decrement right
35.
36.
                                               -Loop-
                                    (Repeat until left >= right)
37.
38.
39.
40.
                         No valid pair found → Return []
41.
```