
Problem Statement:

Given an integer array, heights, where heights[i] represents the height of the i^{th} bar, determine the maximum amount of water that can be contained between these bars. The water will spill over the shorter of two bars. The solution must efficiently compute this maximum volume.

Solution 1

```
def trapping_rain_water(heights: list[int]) -> int:
    if not heights:
        return 0

    left, right = 0, len(heights) - 1
    left_max, right_max = 0, 0
    volume = 0

    while left < right:
        if heights[left] < heights[right]:
            if heights[left] >= left_max:
                left_max = heights[left]
            else:
                volume += left_max - heights[left]
                left += 1
        else:
            if heights[right] >= right_max:
                right_max = heights[right]
            else:
                volume += right_max - heights[right]
                right -= 1

    return volume
```

Step-by-Step Breakdown

1. Input:

- heights: list of integers representing the heights of the bars [1,8,6,2,5,4,8,3,7].

2. Intermittent step 1:

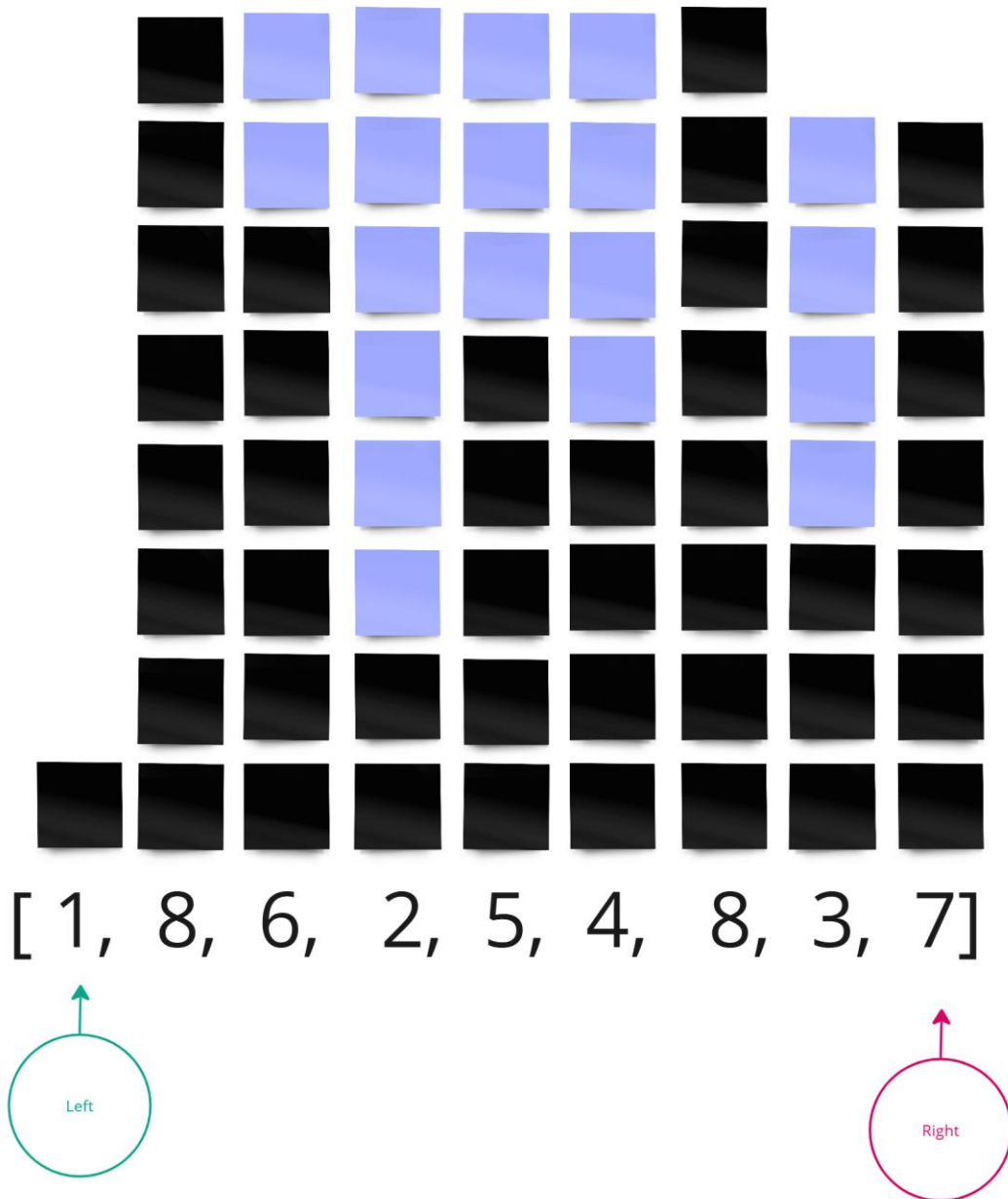
Edge Case Check:

- If heights is empty, return 0 since no container can be formed.
- python

3. Intermittent step 2:

Initialize Pointers and Variables:

- Set left to 0 (the start of the list) and right to len(heights) - 1 (the end of the list).
- Initialize two variables left_max and right_max to track the maximum height seen so far from the left and right, respectively.
- Initialize volume to 0 to accumulate the total trapped water.



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Iterative Two-Pointer Process:

While `left < right`, compare `heights[left]` and `heights[right]`:

- If `heights[left] < heights[right]`:
- If `heights[left]` is greater than or equal to `left_max`, update `left_max` with `heights[left]`.

- Otherwise, the current bar can hold water: add $\text{left_max} - \text{heights}[\text{left}]$ to volume.
- Increment the left pointer to examine the next bar.

Else ($\text{heights}[\text{left}] \geq \text{heights}[\text{right}]$):

- If $\text{heights}[\text{right}]$ is greater than or equal to right_max , update right_max with $\text{heights}[\text{right}]$.
- Otherwise, add $\text{right_max} - \text{heights}[\text{right}]$ to volume.
- Decrement the right pointer to examine the previous bar.

4. Output:

- Return the computed volume which represents the maximum amount of water that can be trapped between the bars.

5. Efficiency:

- Time Complexity: $O(n)$ – The two-pointer approach traverses the array only once.
- Space Complexity: $O(1)$ – Only a fixed number of variables are used, irrespective of the input size.

Visual Flow Diagram

