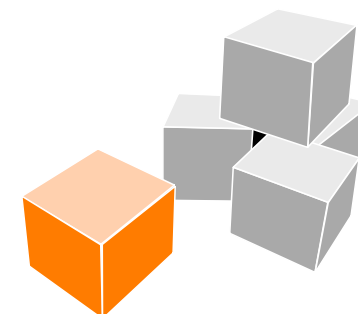


# Concepts of Programming Languages

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## **SIMPLE LANGUAGES**

- A language for arithmetic
- A language with names

# Modeling Syntax

- Different notations for the idealized action of adding the idealized numbers (represented) by “3” and “4”:

– 3 + 4	(infix)	Java
– 3 4 +	(postfix)	FORTH
– (+ 3 4)	(parenthesized prefix)	Scheme

- Ignoring details of concrete syntax, the essence is a tree (AST) ...
- So the first question to answer in modeling languages is how to represent ASTs.

# Syntax

- Concrete syntax
  - What the programmer writes
  - Comments, multiple spaces, newlines, ...
- Abstract syntax
  - Internal representation of the syntax
  - Smaller to make automatic processing (e.g., type checking) and reasoning easier.
  - Example: Arithmetic Expressions

```
<AE> ::= <num>
      | { + <AE> <AE> }
      | { - <AE> <AE> }
```

# Case Classes for ASTs

AST for arithmetic expressions

```
sealed abstract class Expr  
  
case class Num(n: Int) extends Expr  
case class Add(lhs: Expr, rhs: Expr) extends Expr  
case class Sub(lhs: Expr, rhs: Expr) extends Expr
```

Values of this data type:

```
Add(Num(3), Num(4))  
Add(Sub(Num(3), Num(4)), Num(7))
```

# Template for our Interpreters

```
def interp(expr: Expr): Int = expr match {  
  case Num(n) => ???  
  case Add(lhs, rhs) => ???  
  case Sub(lhs, rhs) => ???  
}
```

What goes  
into “???”

# Template for our Interpreters

```
def interp(expr: Expr): Int = expr match {  
  case Num(n) => ???  
  case Add(lhs, rhs) => ???  
  case Sub(lhs, rhs) => ???  
}
```

What goes  
into “???”

```
def interp(expr: Expr): Int = expr match {  
  case Num(n) => n  
  case Add(lhs, rhs) => interp(lhs) + interp(rhs)  
  case Sub(lhs, rhs) => interp(lhs) - interp(rhs)  
}
```

- The AE interpreter



# Next: WAE – a Language with Names

Motivation: reduce repetitions by introducing **identifiers** (not yet variables!)

Example programs:

```
let y = (5 + 10) in y + y
= (5 + 10) + (5 + 10)
```

```
let y = (5 + 10) in
  let x = 20 in (x + y)
= 20 + (5 + 10)
```

# WAE: Abstract syntax

```
<AE> ::= <num>
      | {+ <AE> <AE>}
      | {- <AE> <AE>}
```

Extend  
with “let”

```
<WAE> ::= <num>
      | {+ <WAE> <WAE>}
      | {- <WAE> <WAE>}
      | {let {<id> <WAE>} <WAE>}
      | <id>
```

# WAE: Concrete syntax

**Quiz:** What implementation steps are needed?

```
sealed abstract class Expr
case class Num(n: Int) extends Expr
case class Add(lhs: Expr, rhs: Expr) extends Expr
case class Sub(lhs: Expr, rhs: Expr) extends Expr

???
```

Extend  
with “let”

# WAE: Concrete syntax

**Quiz:** What implementation steps are needed?

```
sealed abstract class Expr
case class Num(n: Int) extends Expr
case class Add(lhs: Expr, rhs: Expr) extends Expr
case class Sub(lhs: Expr, rhs: Expr) extends Expr
```

???

Extend  
with “let”

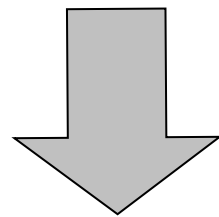
```
sealed abstract class Expr
case class Num(n: Int) extends Expr
case class Add(lhs: Expr, rhs: Expr) extends Expr
case class Sub(lhs: Expr, rhs: Expr) extends Expr

case class Let(name: Symbol, namedExpr: Expr, body: Expr) extends Expr
case class Id(name: Symbol) extends Expr
```

# Substitution or „Name and Conquer“

**Quiz:** What implementation steps are needed?

```
<WAE> ::= <num>
        | {+ <WAE> <WAE>}
        | {- <WAE> <WAE>}
        | {let {<id> <WAE>} <WAE>}
        | <id>
```



```
def parse(prog: String): Expr = ...
```

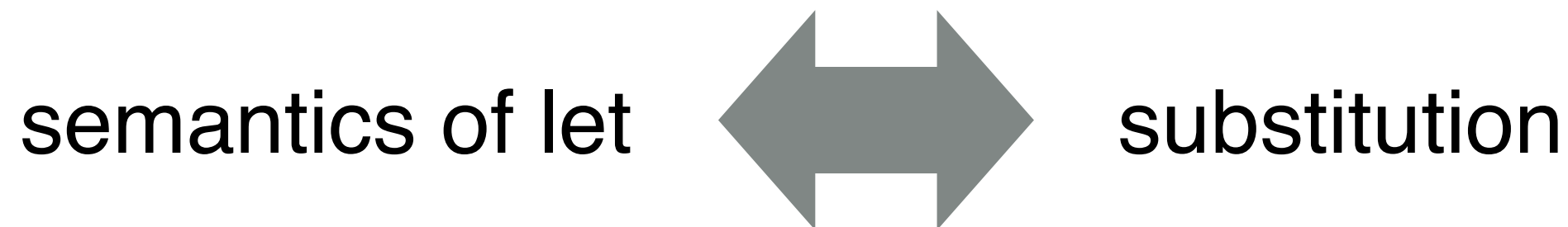
```
sealed abstract class Expr
case class Num(n: Int) extends Expr
case class Add(lhs: Expr, rhs: Expr) extends Expr
case class Sub(lhs: Expr, rhs: Expr) extends Expr
```

```
case class Let(name: Symbol, namedExpr: Expr, body: Expr) extends Expr
case class Id(name: Symbol) extends Expr
```

**The interpreter ...**

# Syntax

- We need to give a semantics to let expressions
- We do so using the concept of substitution



# Defining Substitution

- Wanted: A definition of the process of *substitution*

- Here is one:

*Definition (Substitution):*

*To substitute identifier  $i$  in  $e$  with expression  $v$ , replace all identifier sub-expressions of  $e$  named  $i$  with  $v$ .*

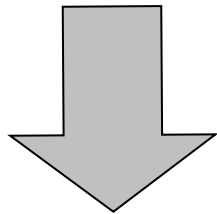
- Try it out with the following WAE expressions:

1. `let x = 5 in x + x`

2. `let x = 5 in x + (let x = 3 in x)`

# Defining Substitution

```
1. let x = 5 in x + x  
2. let x = 5 in x + (let x = 3 in x)
```



```
1. 5 + 5  
2. 5 + (let 5 = 3 in 5)
```

This is not even syntactically legal!  
-> it does not respect the BNF and  
it would be rejected by a parser



# Defining Substitution

*Definition (Binding Instance):*

A binding instance of an identifier is the instance of the identifier that gives it its value. In WAE, the <id> position of a 'let' is the only binding instance.

*Definition (Scope)*

The scope of a binding instance is the region of program in which instances of the identifier refer to the value bound by the binding instance.

*Definition (Bound Instance)*

An identifier is bound if it is contained within the scope of a binding instance of its name.

*Definition (Free Instance)*

An identifier not contained in the scope of any binding instance of its name is said to be free.

# Defining Substitution

```
let x = 5 in  
  x + (let x = 3 in  
        x + x)
```

```
5 + (let x = 3 in  
      5 + 5)
```

```
5 + (5 + 5)
```

15

What can go wrong here?

-> We do not  
respect scoping

# Defining Substitution

## Definition (Binding Instance):

A binding instance of an identifier is the instance of the identifier that gives it its value. In WAE, the <id> position of a 'let' is the only binding instance.

## Definition (Scope)

The scope of a binding instance is the region of program in which instances of the identifier refer to the value bound by the binding instance.

## Definition (Bound Instance)

An identifier is bound if it is contained within the scope of a binding instance of its name.

## Definition (Free Instance)

An identifier not contained in the scope of any binding instance of its name is said to be free.

```
let x = 5 in
  x + (let x = 3 in
        x + y)
```

# Defining Substitution

*Definition (Substitution):*

To substitute identifier  $i$  in  $e$  with expression  $v$ , replace all free instances of  $i$  in  $e$  with  $v$ .

- This definition is implicitly using a notion of scope
- Substitute only in the scope of the identifier
- Respected binding instances, but not their scope.
- An inner binding for the same name introduces a new scope. The scope of the outer binding is shadowed or masked by the inner binding.
- Substituting the inner  $x$  is wrong.

# Calculating WAE Expressions

```
def interp(expr: Expr): Int = expr match {  
  case Num(n) => n  
  case Add(lhs, rhs) => calc(lhs) + calc(rhs)  
  case Sub(lhs, rhs) => calc(lhs) - calc(rhs)  
  case Let(boundId, namedExpr, boundExpr) => ???  
  case Id(name) => ???  
}
```

Use a “subst”  
function

```
def subst(expr: WAE, substId: Symbol, value: WAE)
```

```
def interp(expr: Expr): Int = expr match {  
  case Num(n) => n  
  case Add(lhs, rhs) => interp(lhs) + interp(rhs)  
  case Sub(lhs, rhs) => interp(lhs) - interp(rhs)  
  case Let(boundId, namedExpr, boundExpr) => {  
    interp(subst(boundExpr, boundId, Num(interp(namedExpr))))  
  }  
  case Id(name) => sys.error("found unbound id " + name)  
}
```

# Calculating WAE Expressions

- Any identifier that is in the scope of a let-expr is replaced with a value when the calculator encounters that identifier's binding instance.
- Consequently, the purpose statement of substitution said there would be no free instances of the identifier given as an argument left in the result.
- In other words, subst replaces identifiers with values before the calculator ever “sees” them.
- The calculator can't assign a value to a free identifier, so it halts with an error

# Calculating WAE Expressions

```
def subst(expr: Expr, substId: Symbol, value: Expr): Expr = expr match {  
  case Num(n) => ???  
  case Add(lhs, rhs) => ???  
  case Sub(lhs, rhs) => ???  
  
  case Let(boundId, namedExpr, boundExpr) => ???  
  
  case Id(name) => ...  
}
```

# Calculating WAE Expressions

```
def subst(expr: Expr, substId: Symbol, value: Expr): Expr = expr match {  
  case Num(n) => expr  
  case Add(lhs, rhs) => Add(subst(lhs, substId, value), subst(rhs, substId, value))  
  case Sub(lhs, rhs) => Sub(subst(lhs, substId, value), subst(rhs, substId, value))  
  
  case Let(boundId, namedExpr, boundExpr) => ???  
  
  case Id(name) => ...  
}
```



# Calculating WAE Expressions

```
def subst(expr: Expr, substId: Symbol, value: Expr): Expr = expr match {  
  case Num(n) => expr  
  case Add(lhs, rhs) => Add(subst(lhs, substId, value), subst(rhs, substId, value))  
  case Sub(lhs, rhs) => Sub(subst(lhs, substId, value), subst(rhs, substId, value))  
  
  case Let(boundId, namedExpr, boundExpr) => {  
    val substNamedExpr = subst(namedExpr, substId, value)  
    Let(boundId, substNamedExpr, subst(boundExpr, substId, value))  
  }  
  
  case Id(name) => ...  
}
```

What is wrong with this one?

# Calculating WAE Expressions

```
def subst(expr: Expr, substId: Symbol, value: Expr): Expr = expr match {  
  case Num(n) => expr  
  case Add(lhs, rhs) => Add(subst(lhs, substId, value), subst(rhs, substId, value))  
  case Sub(lhs, rhs) => Sub(subst(lhs, substId, value), subst(rhs, substId, value))  
  
  case Let(boundId, namedExpr, boundExpr) => {  
    val substNamedExpr = subst(namedExpr, substId, value)  
    if (boundId == substId)  
      Let(boundId, substNamedExpr, boundExpr)  
    else  
      Let(boundId, substNamedExpr, subst(boundExpr, substId, value))  
  }  
  
  case Id(name) => {  
    if (substId == name) value  
    else expr  
  }  
}
```

# Two Substitution Regimes

**Eager substitution**  
**(static and dynamic reduction)**: avoids re-computing the same value several times.

1

```
{let {x {+ 5 5}} {let {y {- x 3}} {+ y y}}}  
= {let {x 10} {let {y {- x 3}} {+ y y}}}  
= {let {y {- 10 3}} {+ y y}}  
= {let {y 7} {+ y y}}  
= {+ 7 7}  
= 14
```

**Lazy substitution**  
**(Static reduction)**: the expression may be evaluated multiple times.

2

```
{let {x {+ 5 5}} {let {y {- x 3}} {+ y y}}}  
= {let {y {- {+ 5 5} 3}} {+ y y}}  
= {+ {- {+ 5 5} 3} {- {+ 5 5} 3}}  
= {+ {- 10 3} {- {+ 5 5} 3}}  
= {+ {- 10 3} {- 10 3}}  
= {+ 7 {- 10 3}}  
= {+ 7 7}  
= 14
```

# Two Substitution Regimes

- Questions:

1. Which one have we implemented?

```
def interp(expr: Expr): Int = expr match {  
  ...  
  case Let(boundId, namedExpr, boundExpr) => {  
    interp(subst(boundExpr, boundId, Num(interp(namedExpr))))  
  }  
  ...  
}
```

2. Our example suggests that the eager regime generates an answer in fewer steps. Is this always true?

```
{let {x {+ 5 5}}  
  {let {y 4} {+ y y}}}
```

3. Do the two regimes always produce the same result for WAE?

```
{let {x {+ z 4}}  
  {let {y 4} {+ y y}}}
```

- The WAE interpreter

## **FOOD FOR THOUGHTS**

# PL success: Some Ideas

- Large popular software systems use language X.  
(E.g., Unix for C)
- Companies push for it.
- Market pressure. A popular language is requested and becomes even more popular
- A language introduces new concepts
  - Not necessarily applicable from day 1

# More sources

- What makes a programming language
  - Popular
  - Important (?)
  - Inspiring (??)



# The TIOBE index

- The TIOBE Programming Community index is an indicator of the popularity of programming languages.
  - Popular search engines are used to calculate the ratings.
  - It is not about the best programming language or the language in which most lines of code have been written.
  - <http://www.tiobe.com/tiobe-index/>
- Any guess?



- IEEE Spectrum: The Top Programming Languages 2016
  - Popular search engines, twitter, github, stack overflow, ...
    - [http://spectrum.ieee.org/ns/IEEE\\_TPL\\_2016/methods.html](http://spectrum.ieee.org/ns/IEEE_TPL_2016/methods.html)
  - <http://spectrum.ieee.org/static/interactive-the-top-programming-languages-2016>



# More sources

- <http://githut.info>
- <https://github.com/blog/2047-language-trends-on-github>

Disclaimer: Please take all these  
measures with a grain of salt  
(Better, with some skepticism!)