

TTK4210 Advanced Control of Industrial Systems, Exercise 6

Kristian Løvland

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1 Abstract

In this project, a model of a butane distillation column was used to design a controller for the composition of two product streams consisting of n-butane and iso-butane, respectively. By identifying characteristics of relevant subsystems, PI controllers for the states of these systems were designed with the ultimate goal of keeping the purity of the products at a satisfactory level.

2 Introduction

A good introduction to the control problem we're faced with is given in the assignment text [1]. A short summary follows

The top product is required to contain no more than 4% n-butane, while the bottom product is required to contain less than 2,5% iso-butane.

These compositions, denoted x_D^* and x_B^* are in practice controlled through their temperatures. These are measured on the top and bottom of the distillation column, and are denoted T_D and T_B . The temperature needed to achieve the required compositions are shown in ??, together with the actual temperature setpoint. These are a bit lower/higher than they strictly need to introduce a safety margin.

	Required temperature	Temperature setpoint
Top product (D)	35, 85° C	35, 30° C
Bottom product (B)	47, 69° C	48, 51° C

Table 1: Temperatures giving satisfactory product quality

To satisfy these specifications, the rest of the systems need to work well too. The levels M_D and in the top accumulator and M_B in the distillation column need to be controlled to stable setpoints. The same goes for distillation column pressure p .

To control these five variables, five degrees of freedom is needed. Our five manipulated variables are flow rates in different parts of the system, denoted V_T , L , D , V and B . Each of these is controlled directly by a valve.

Table 2 shows the pairing of manipulated and controlled variables. As mentioned, it is assumed that choosing good setpoints for T_D and T_B gives satisfactory product quality. This control structure is called LV-control, after the manipulated variables used to control product quality.

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Manipulated Variable	V_T	D	B	L	V
Controlled variable	p	M_D	M_B	T_D	T_B

Table 2: Variable pairings

3 Tuning secondary controllers

The secondary controllers were tuned individually using the SIMC method for PI controllers. A step in process input with an amplitude small enough to not cause problems (usually meaning 50% of maximum accepted input magnitude) in other parts of the system was used for all the secondary controllers, controlling the states D , L , B , V and p .

A summary of the method is given in [3]. The method assumes that the system can be approximated by a first order process with time delay

$$G(s) = \frac{ke^{-\theta s}}{1 + T_1 s} \quad (1)$$

and be controlled by a PI controller

$$K(s) = K_p \frac{1 + T_i s}{T_i s} \quad (2)$$

The SIMC method gives rules for choosing K_p and T_i , given a desired closed-loop time constant T_L . Assuming the step response behaves similarly to a first order system, the method is then as follows

1. Fit the step response to a first order model. This means finding time delay θ , slope $k' = \frac{dy/dt}{\Delta u}$ and time constant T_1 from the plot of the step response.
2. To achieve the desired time constant T_L , use the PI controller parameters $K_p = \frac{1}{k'} \frac{1}{\tau + T_L}$, $T_i = \min(T_1, 4(\tau + T_L))$.

The step experiments can be seen in figures 1, 3, 5, 7 and 9. The reference signals should have been omitted from these plots since we are dealing with open loop systems, and can safely be ignored here.

The plots show that for the first three variables, the accuracy of the simulation is clearly not sufficient for fitting a first order model (they behave in a stepwise fashion). Inspecting the order of magnitude of the gains and time constants may however still be useful. To approximate their sizes, a straight line was drawn from initial state to steady-state.

An attempt at making sense of these parameters is shown in table 3, together with the fitted values for V and p . This gives conservative estimates of k' and T_1 .

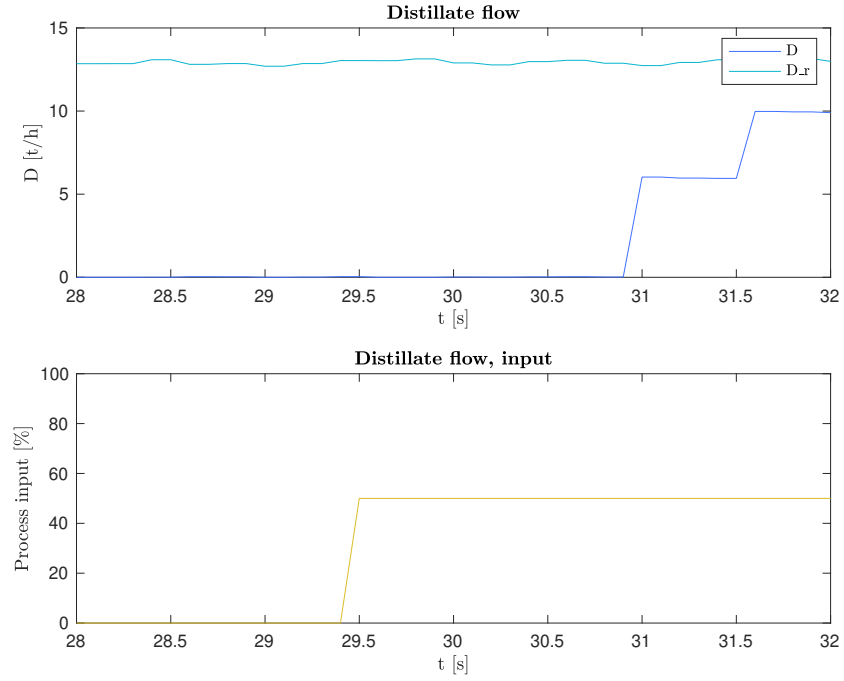


Fig. 1: Open-loop step response of D

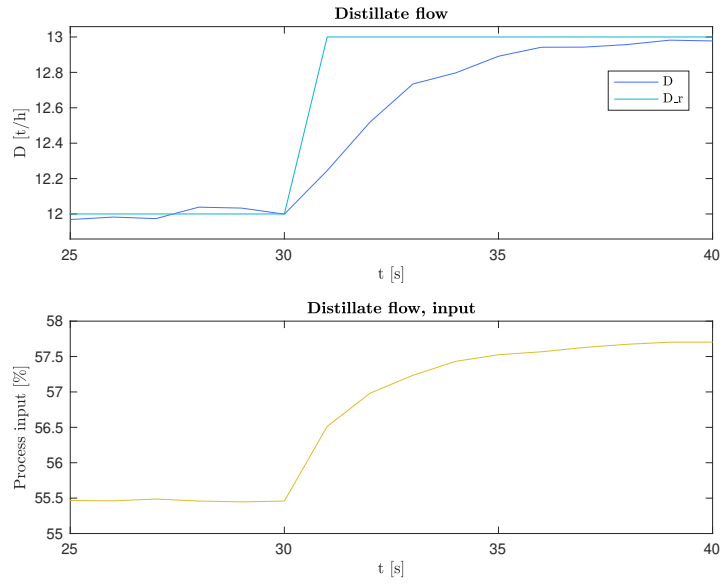


Fig. 2: Closed-loop step response of D

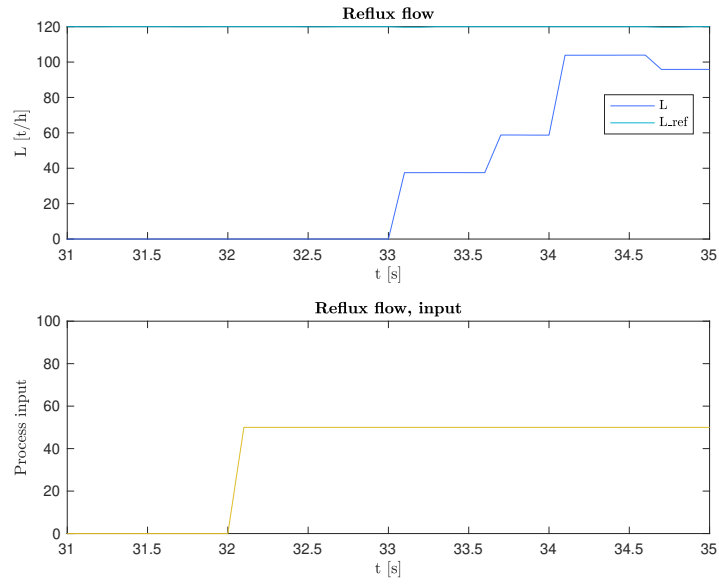


Fig. 3: Open-loop step response of L

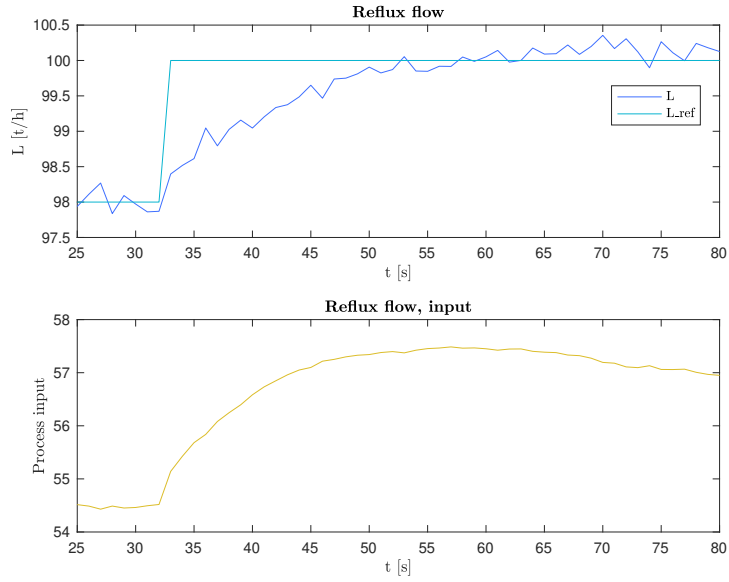


Fig. 4: Closed-loop step response of L

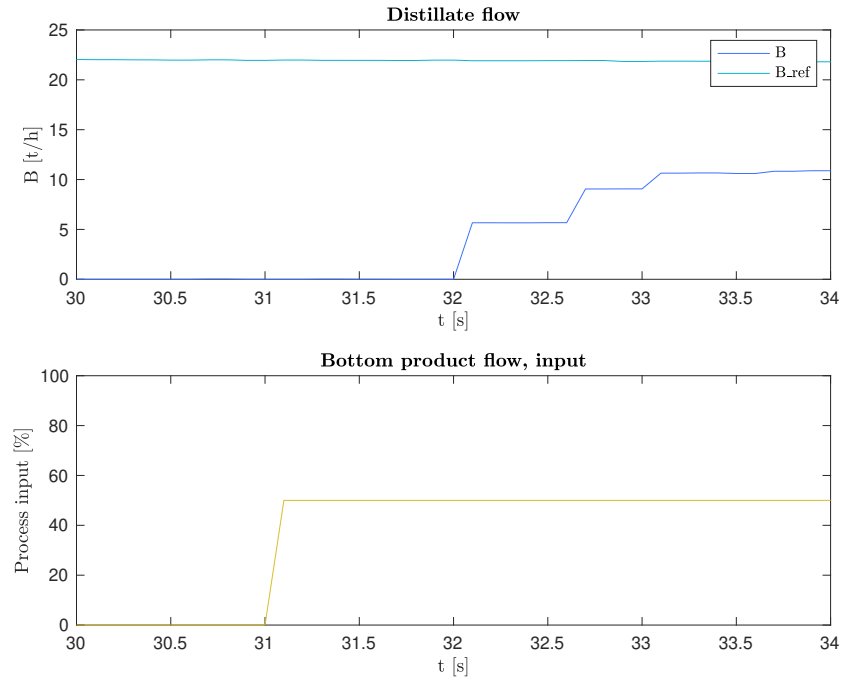


Fig. 5: Open-loop step response of B

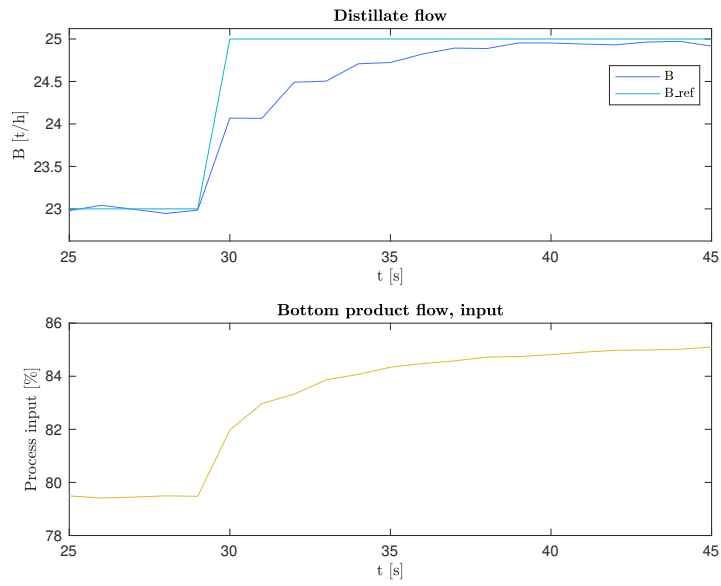


Fig. 6: Closed-loop step response of B

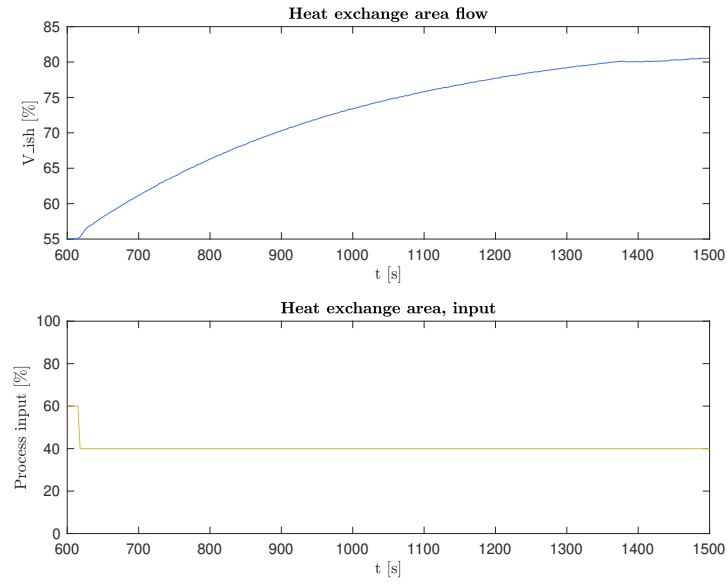


Fig. 7: Open-loop step response of heat exchanger area, related to V

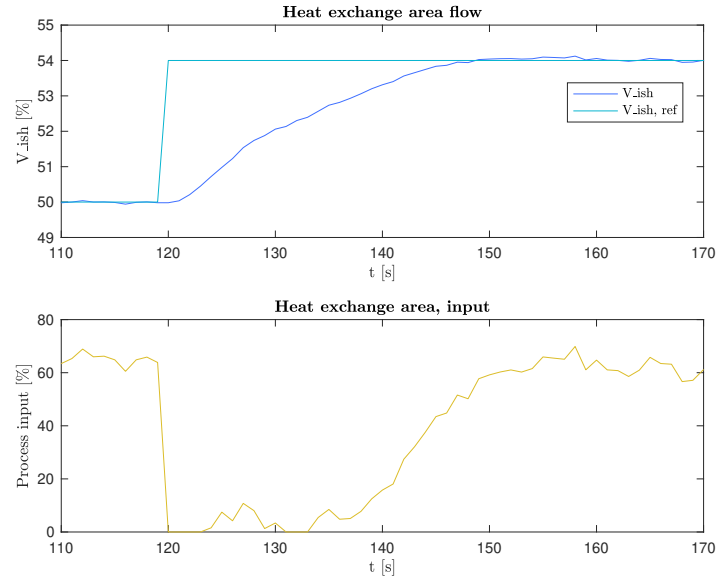


Fig. 8: Closed-loop step response of heat exchanger area, related to V

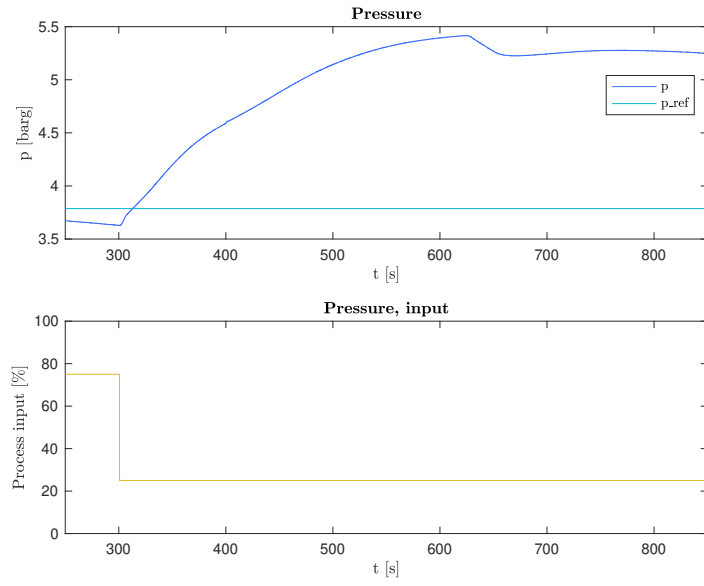


Fig. 9: Open-loop step response of p

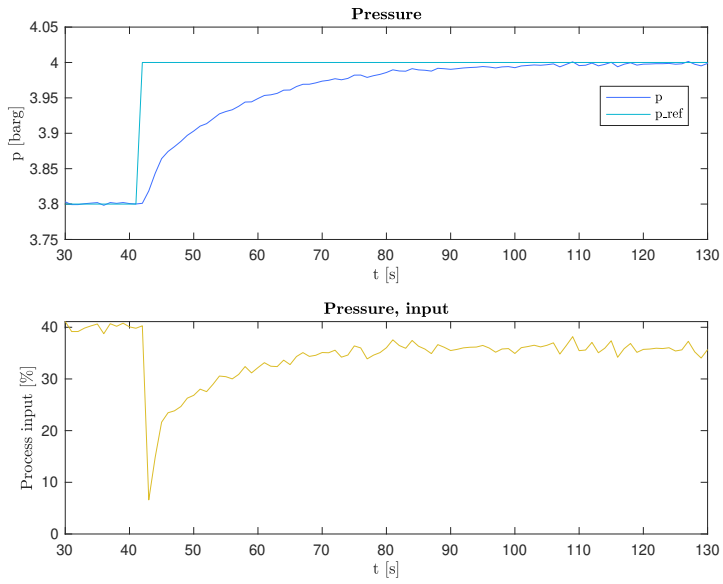


Fig. 10: Closed-loop step response of p

	τ	T_1	$\frac{dy}{dt}$	Δu	k'	T_L
D	1,0s	0,4s	14,3	50%	28,6	2s
L	1,0s	1,0s	47,5	50%	95,0	2s
B	1,0s	0,6s	10,0	50%	20,0	2s
V	≈ 0	400s	0,028	20%	0,14	10s
p	≈ 0	200s	0,088	50%	0,18	10s

Table 3: Identified parameters for inner loop

In the table, a desired time constant for the controlled system T_L is shown in the rightmost column. For a quick response, choosing $T_L = 0,3\tau$ is suggested in [?]. Some simple trial and error in K-spice showed that this lead to oscillation and unfortunate interaction between control loops, especially the controllers for D and L . This is probably partly due to the underestimates of k' and T_1 for these variables, since conservative estimates of these results in more aggressive controllers (to compensate for the slow system) when using the SIMC method.

Due to this unsatisfactory behaviour, $T_L = 2\tau$ was chosen for the three fastest control loops instead. The time delay was hard to make a meaningful reading of for the two other systems, so a somewhat arbitrary choice of $T_L = 10s$ was chosen for these systems (instead of using the $T_L = 2\tau$ rule). Like all the other parameters, these were not absolute choices, but a good starting point for further tuning.

After calculating the SIMC controller values some qualitative tuning using K-spice simulations was, not surprisingly, needed. For D and L , the integral times were kept fixed, and the gain was decreased to avoid oscillations. For B , it was necessary to reduce the integral time in addition to reducing the gain to avoid oscillation. The response of V was slow, and to avoid bandwidth limitations in the control of T_B later, both controller parameters were changed to give dramatically more aggressive behaviour. For p , the stationary deviation was initially removed pretty slowly, so the integral time was reduced, while also reducing gain to avoid oscillation.

The results of implementing these controllers in K-spice, using the internally scaled gain $G = K_p \frac{(y_{\max} - y_{\min})}{(u_{\max} - u_{\min})}$ for all controllers, are shown in figures 2, 4, 6, 8 and 10.

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	$K_{p,\text{SIMC}}$	$T_{i,\text{SIMC}}$	$K_{p,\text{final}}$	$T_{i,\text{final}}$
D	0,012	0,4s	0,0035	0,4s
L	0,035	1,0s	0,0018	1,0s
B	0,016	0,6s	0,0025	1,0s
V	0,71	40s	1,65	10s
p	0,57	40s	0,25	20s

Table 4: PI controller parameters for inner loop

4 Level controllers

In this section, the subsystem consisting of the levels in the reflux drum and distillation column is identified, using the inputs D and B . Let $y = [M_D \ M_B]^T$ and $r = [M_{D,\text{ref}} \ M_{B,\text{ref}}]^T$. By exciting the controlled system

$$y(s) = L(s)e(s) = G(s)K(s)(y(s) - r(s)) \quad (3)$$

with changes in the reference r , the loop transfer function $L(s) = \frac{y}{e}(s)$ may be identified. Choosing $K(s)$ to be diagonal makes further analysis and controller tuning easier.

4.1 System identification and analysis

4.1.1 Experiment

The level controllers in the distillation column and reflux drum were expected to be more or less independent, but a MIMO experiment followed by identification using the **d-sr** toolbox was used anyway, due to the convenience of being able to reuse code in the composition control task. The system was excited by step changes in references for M_D and M_B , which were controlled with P controllers, both with $K_p = 1200$. The references were changed after different intervals, to better extract information about all frequencies. The states were attempted held in a reasonable interval, to avoid nonlinear effects such as saturation. The experiments are shown in figures 11 and 12.

4.1.2 Analysis

The identified model was chosen to have order 2, which is natural for a what was expected to be a diagonal system with two variables. The interactions

of the resulting system is shown in figure 13, which show the RGA of the identified $G(s)$. Inspecting this plot shows that the magnitudes of the off-diagonal elements are negligible at frequencies above $10^{-3} \frac{\text{rad}}{\text{s}}$. The diagonal elements have gain close to unity at the bandwidth frequency (which is around $\omega = 0,01$). Since interaction is low, a diagonal controller

$$K(s) = \begin{bmatrix} k_1(s) & 0 \\ 0 & k_2(s) \end{bmatrix} \quad (4)$$

with PI controllers $k_1(s)$ and $k_2(s)$ may be designed independently based on the diagonal elements in the identified $G(s)$. In the following analysis, $L(s)$ is used for simplicity, since it is simply a scaled version of $G(s)$. The controller designed below will then simply be multiplied by the existing $K(s)$ when being implemented.

Figures 14 and 15 show the Bode plots of the transfer functions in the diagonals of the identified model. Ignoring the 360° error in phase, the gain margin of loop transfer function $l_{11}(s) = \frac{M_D}{M_{D,ref}}(s)$ may be found to be to be 6,74dB as $\omega \rightarrow \infty$. Likewise, the gain margin of $l_{22}(s) = \frac{M_B}{M_{B,ref}}(s)$ is read to be 10,7dB as $\omega \rightarrow \infty$. Using the 6dB gain margin rule of thumb (which is often used in [3]), $K_{p,D}$ should not be increased by any significant amount, while $K_{p,B}$ might be increased by a factor of $10^{(10,7-6)/20} \approx 1,7$, yielding the controller gain $K_{p,B} = 2000$.

The phase plot of l_{11} shows that the integral controller should be active in the lower frequency spectrum. To avoid the phase crossing the -180° line, the inequality $\frac{1}{T_{i,D}} < 2 \cdot 10^{-4}$ should be respected. Choosing $T_i = 5000s$ satisfies this. The phase response of l_{22} is pretty similar to the one of l_{11} , so initially choosing the same integral time for control of M_B should be reasonable.

Figures 16 and 17 shows the magnitudes of the sensitivity functions for the two systems using these controllers. The distillation column is, not surprisingly, the hardest system of the two to control quickly. One might wish to push the bandwidth of the M_B loop further to the right, but inspecting the phase plot again suggests not to attempt this. This is because the phase margin would be dangerously low K_p was increased or T_i was decreased, and the system would become more sensitive to time delays and similar phenomena. Disturbances at frequencies above $0,005 \frac{\text{rad}}{\text{s}}$ should hopefully not be common in this system anyway.

Figur av stegrespons til nivåregulering

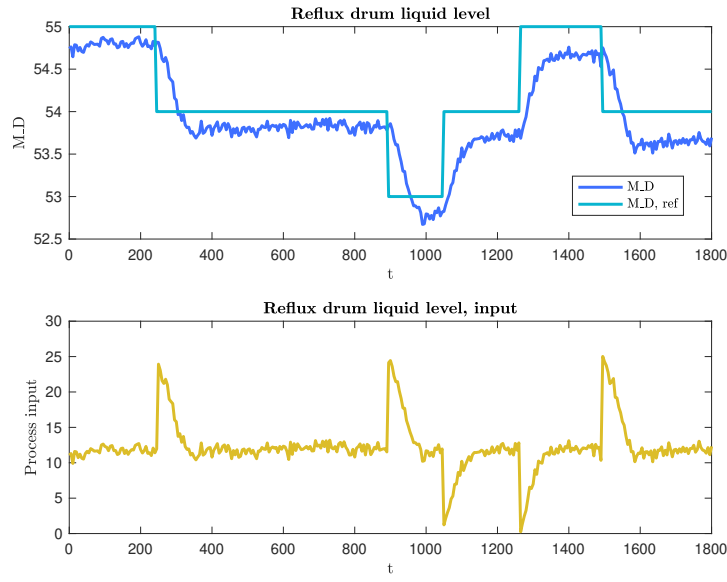


Fig. 11: System identification experiment for M_D controller

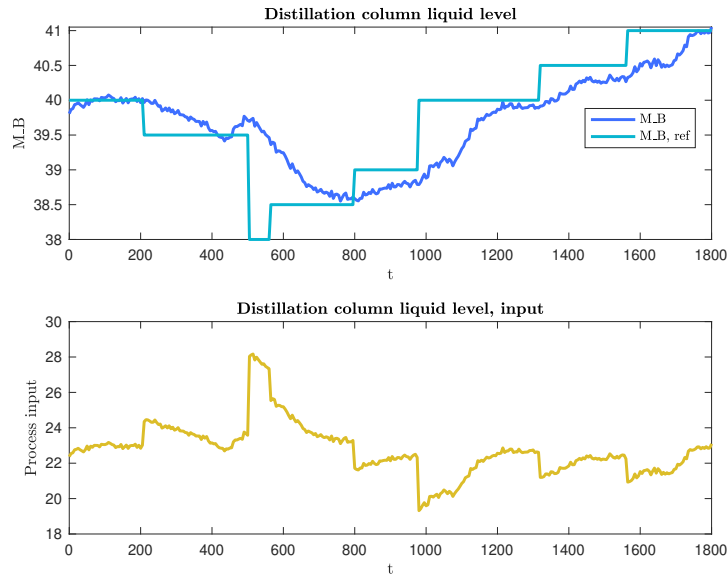


Fig. 12: System identification experiment for M_B controller

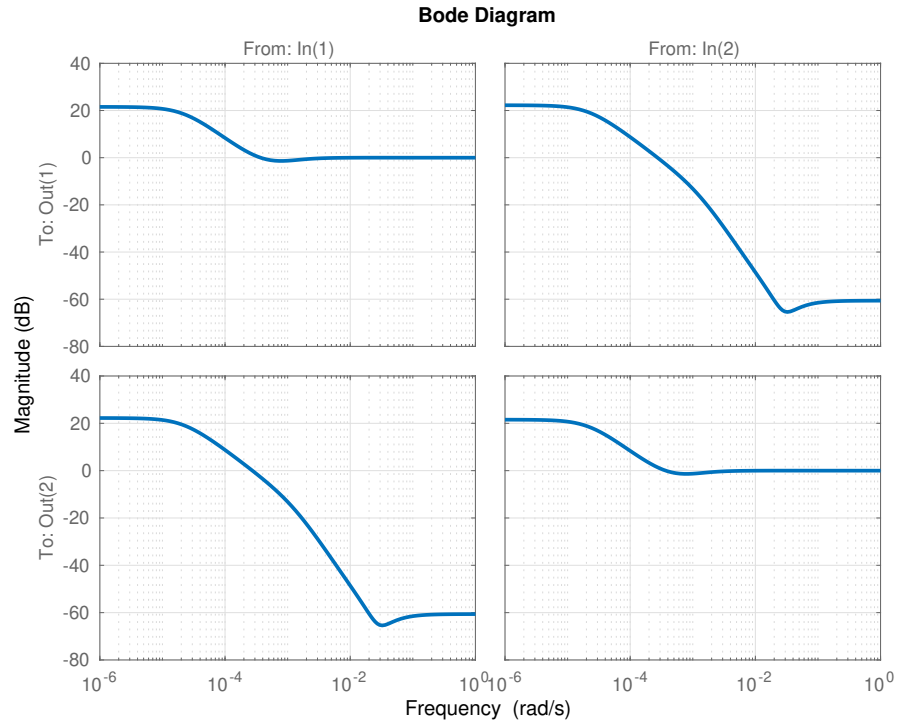


Fig. 13: Magnitude of RGA of identified BD system

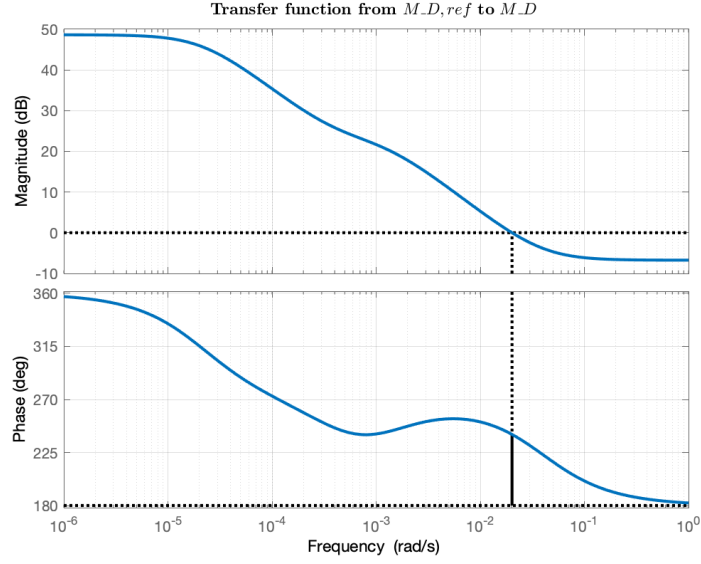


Fig. 14: Magnitude and phase response of reflux drum level from reflux drum level reference

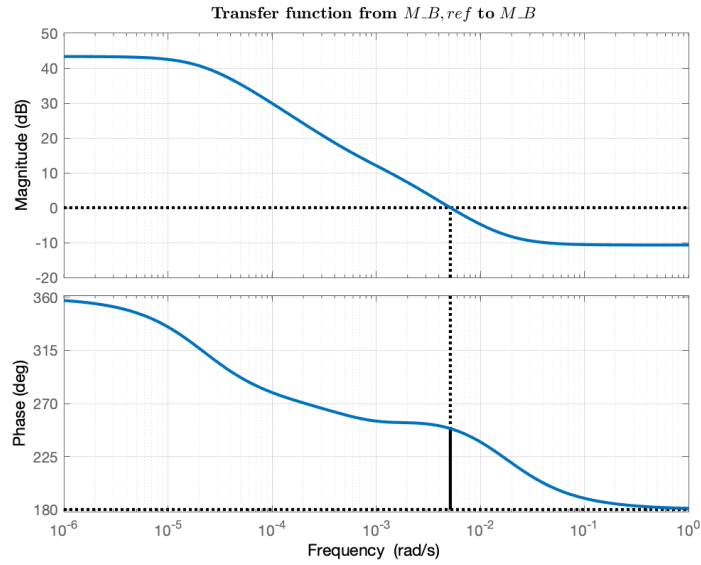


Fig. 15: Magnitude and phase response of distillation column level from distillation column level reference

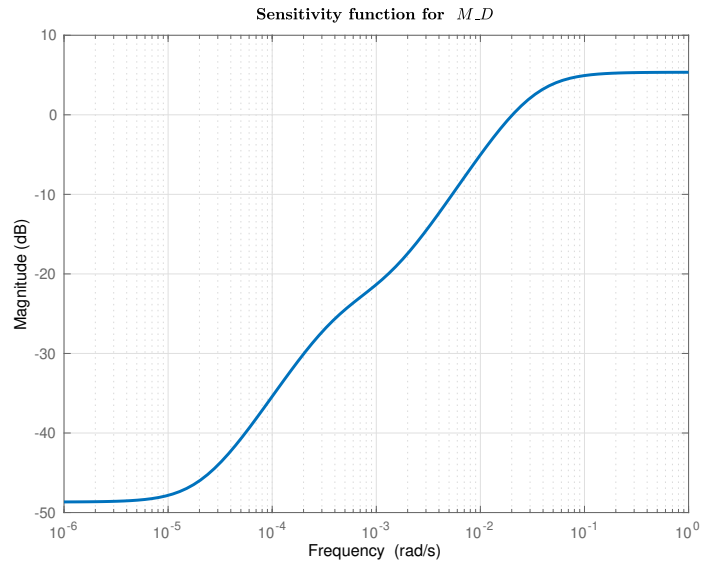


Fig. 16: Sensitivity function for reflux drum level control

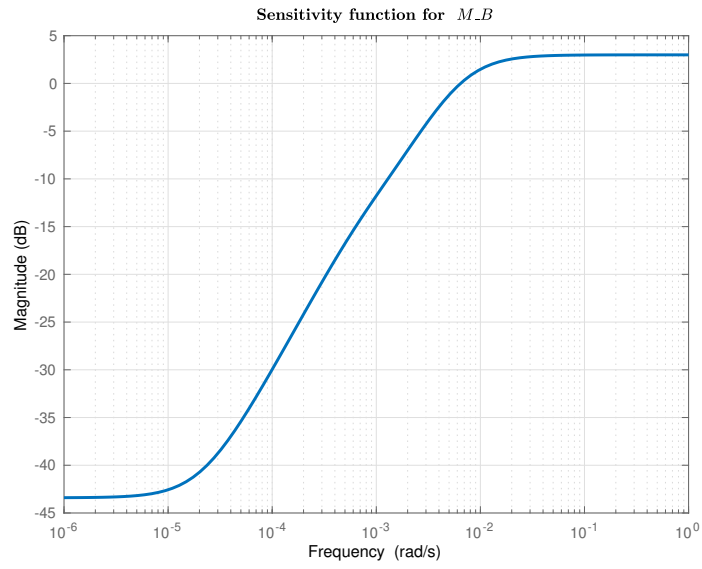


Fig. 17: Sensitivity function for distillation column level control

4.2 Controller tuning

Simulation in K-spice showed stationary deviation in M_D . To counteract this, the integral time was reduced. Control of M_B worked satisfactory using the PI controller derived from the frequency analysis above.

The initial parameters based on loop-shaping, and the final ones are shown in table 5.

	$K_{p,\text{initial}}$	$T_{i,\text{initial}}$	$K_{p,\text{final}}$	$T_{i,\text{final}}$
M_D	1200	5000s	1200	1000s
M_B	2000	5000s	2000	5000s

Table 5: Parameters for level controllers

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5 Composition controllers

Let $y = [T_D \quad T_B]^T$, $r = [T_{D,\text{ref}} \quad T_{B,\text{ref}}]^T$ and $u = [L \quad V]^T$. By changing the setpoints for the manipulated variables L and V , the system transfer function

$$G(s) = \frac{y}{u}(s) \quad (5)$$

may be identified directly.

5.1 System identification and analysis

5.1.1 Experiment

Identification of the LV system was done in a similar manner as in the previous section, using step changes in input (but open-loop this time). Again, **d-sr** was used for identification. The periods of the step changes were chosen more systematically than in the level experiment, with periods of 5 minutes, 15 minutes and ≈ 2 minutes being used for different periods of time. This was done to get an accurate representation of the system at all frequencies. The inputs L and V were changed alternatingly (i.e. 90° out of phase), to avoid ambiguity in which input caused what effect. Figure 18 shows the experiment.

5.1.2 Analysis

Figure 19 shows the RGA of the identified system $G(s) = \frac{y}{u}(s)$. The chosen pairing is clearly the most reasonable. The interactions doesn't seem to be too severe, but the RGA doesn't tell the whole story. It should seem reasonable that temperature in the bottom affects temperature in the top more than the other way around, and the right tool for this analysis is the *Performance Relative Gain Array* (PRGA). To use this however, the system has to be rescaled.

More precisely, given a system

$$e = y - r = G(s)u + G_d(s)d - r \quad (6)$$

the signals should be scaled such that the maximum disturbance and maximum acceptable error both are of magnitude less than one. Table ?? shows the range used in K-spice for the states, and maximum value for signals only

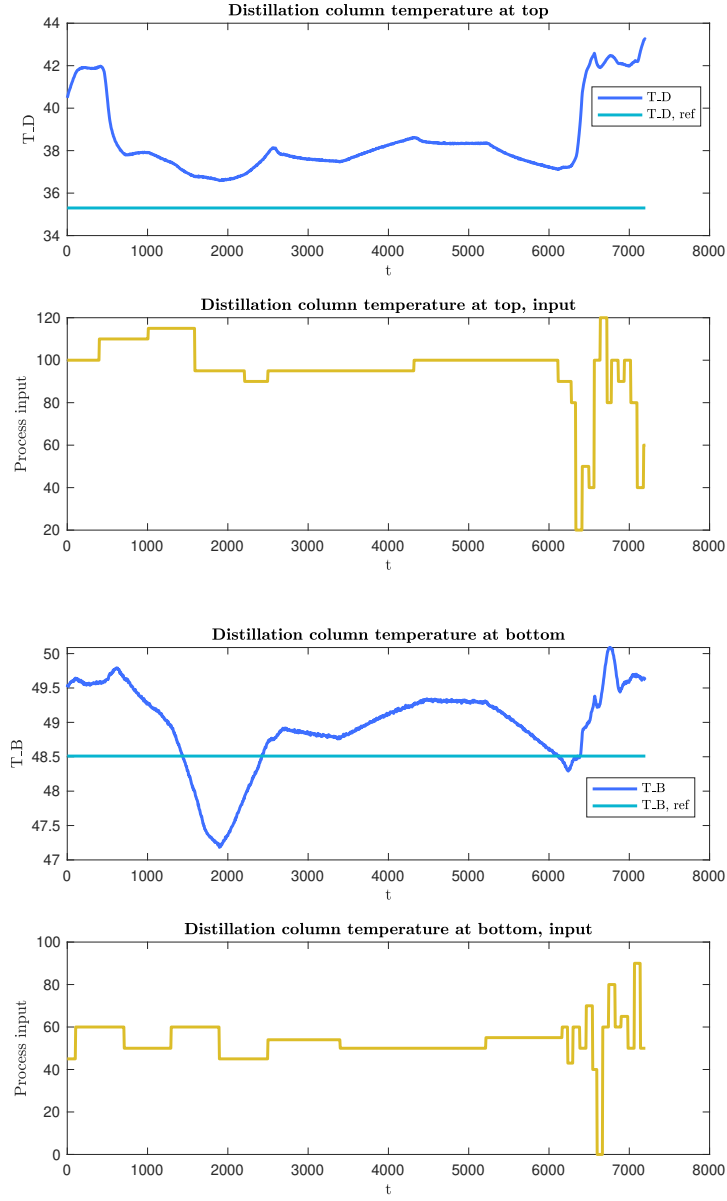


Fig. 18: Response of T_D and T_B to step changes in L and V

Variable	Min	Max	Maximum magnitude
T_D	25°C	50°C	25°C
T_B	25°C	50°C	25°C
$T_{D,\text{ref}}$	25°C	50°C	25°C
$T_{B,\text{ref}}$	25°C	50°C	25°C
L	$0 \frac{\text{t}}{\text{h}}$	$120 \frac{\text{t}}{\text{h}}$	$120 \frac{\text{t}}{\text{h}}$
V	0%	100%	100%
e	-	-	0, 55°C
d	-	-	1, 0°C

Table 6: Scaling used in LV system analysis

used in analysis. To be clear, the following analysis holds for both control loops, with y being temperature, r reference temperature, and u process input. The maximum error allowed is chosen based on the lowest margin proposed in the assignment text. The choice of one degree celsius is somewhat arbitrary, but seemed reasonable and at least not too optimistic given the information that one degree is considered a large step.

The PRGA using this scaling is shown in figure 20. It is now clear that one can't simply choose a bandwidth of $0,01 \frac{\text{rad}}{\text{s}}$ and call it a day, since the interaction from V to T_D has its peak at this frequency.

5.2 Controller tuning

Tune i K-spice

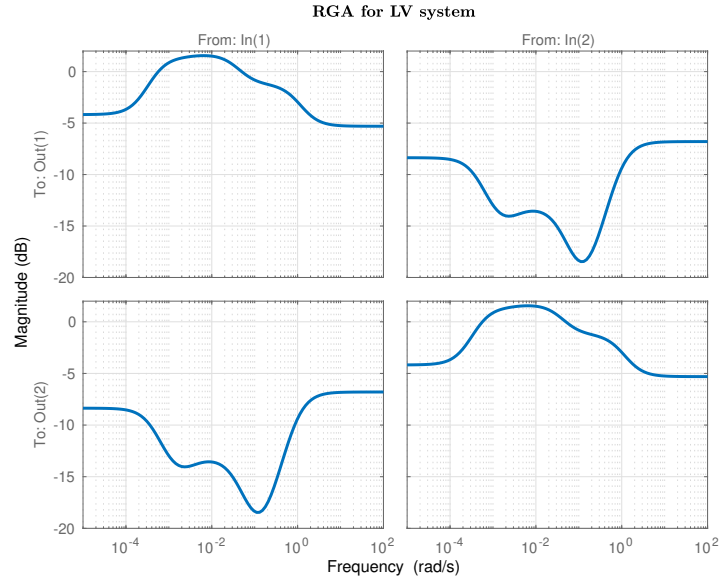


Fig. 19: RGA for LV system

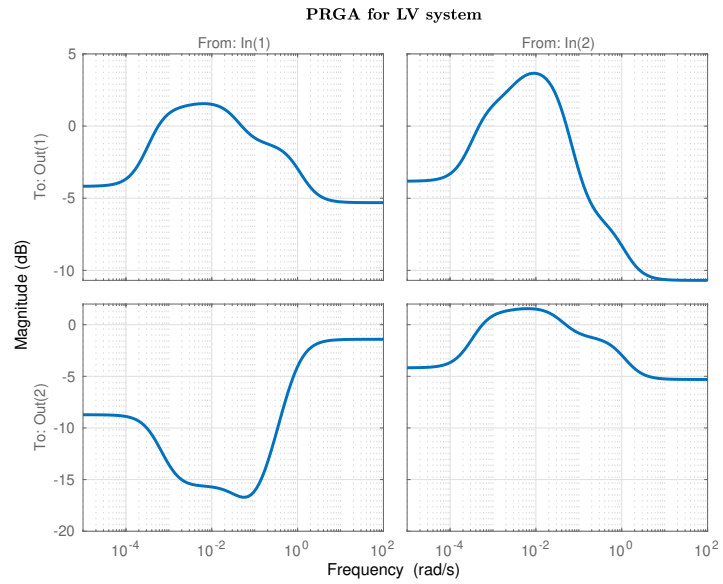


Fig. 20: PRGA for LV system

	K_p	G	T_i
D (FC1005)	0,0035	0,42	0,4s
L (FC1015)	0,0018	0,22	1,0s
B (FC1019)	0,0025	0,3	1,0s
V (LC1028)	200	200	10s
p (PC1024)	5	30	20s
M_D (LC1016)	1200	10	1000s
M_B (LC1015)	2000	16,7	5000s
T_D (TC1015)	12	2,5	100s
T_B (TC1088)	25	6,3	1000s

Table 7: Final controller parameters

6 Results

6.1 PI controller tuning

Table 7 shows the final PI controller parameters for all the control loops tuned in this project, also including the scaled gain G used in the K-spice implementation.

6.2 Reference tracking

The results of step changes in reference are shown in figures 21 and 22.

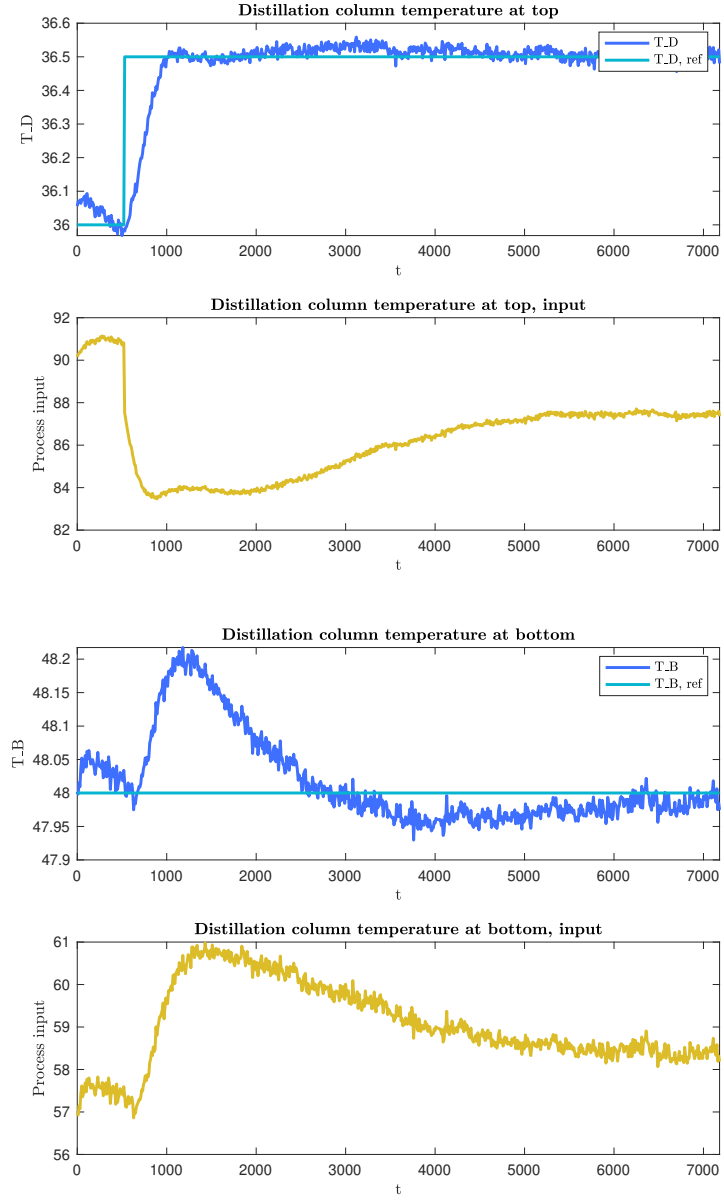


Fig. 21: Response of T_D and T_B to step change in $T_{D,ref}$

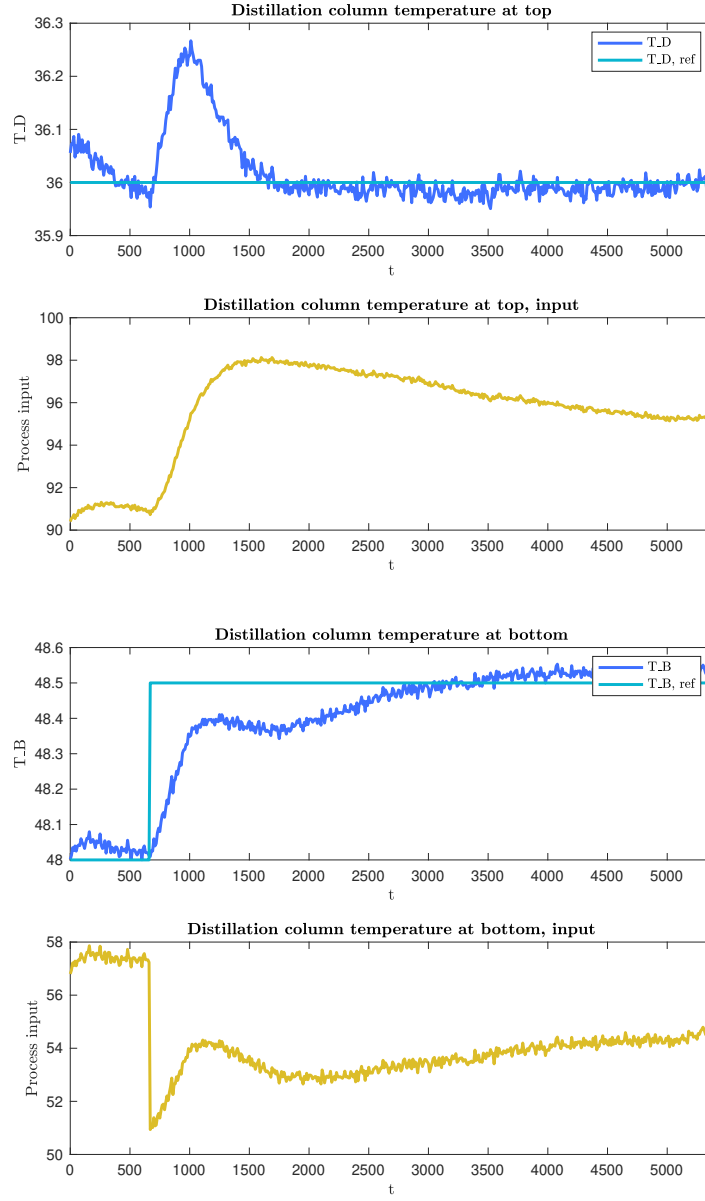


Fig. 22: Response of T_D and T_B to step change in $T_{B,\text{ref}}$

References

- [1] Morten Hovd, *TTK4210 Advanced Control of Industrial Processes, Assignment 6*, 2020.
- [2] Sigurd Skogestad and Ian Postlethwaite, *Multivariable Feedback Control*, John Wiley & Sons Ltd, Chichester, 2nd edition, 2005.
- [3] Jens G. Balchen, Trond Andresen and Bjarne A. Foss, *Reguleringsteknikk*, Institutt for Teknisk Kybernetikk, Trondheim, 6th edition, 2016.