

# 半导体物理

主讲人：蒋玉龙

微电子学楼312室， 65643768

Email: [yljiang@fudan.edu.cn](mailto:yljiang@fudan.edu.cn)

<http://10.14.3.121>

# 第九章 金半接触

9.1 金半接触的能带图

9.2 金半接触的整流输运理论

9.3 少子注入和欧姆接触

# 9.1 金半接触的能带图<sub>1</sub>

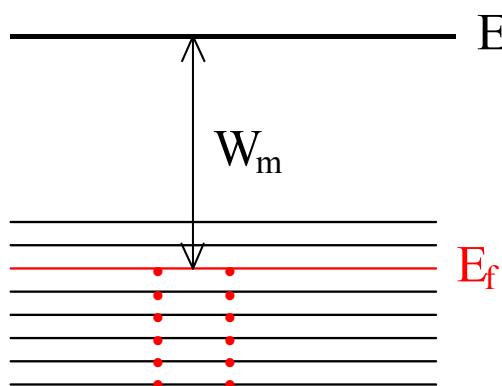
## 9.1.1 功函数和电子亲合能

功函数:  $W = E_0 - E_f$

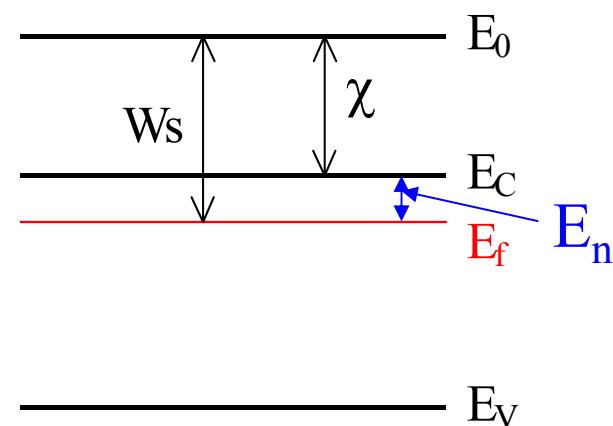
— 真空能级与费米能级之差

电子亲和能 $\chi$ : 真空能级与导带底之差

真空能级 $E_0$ :  
真空中静止电子的能量



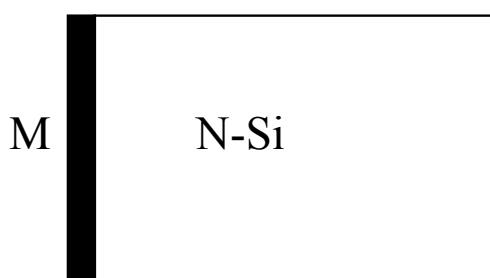
$$W_m = E_0 - E_F$$



$$W_s = E_0 - E_F$$

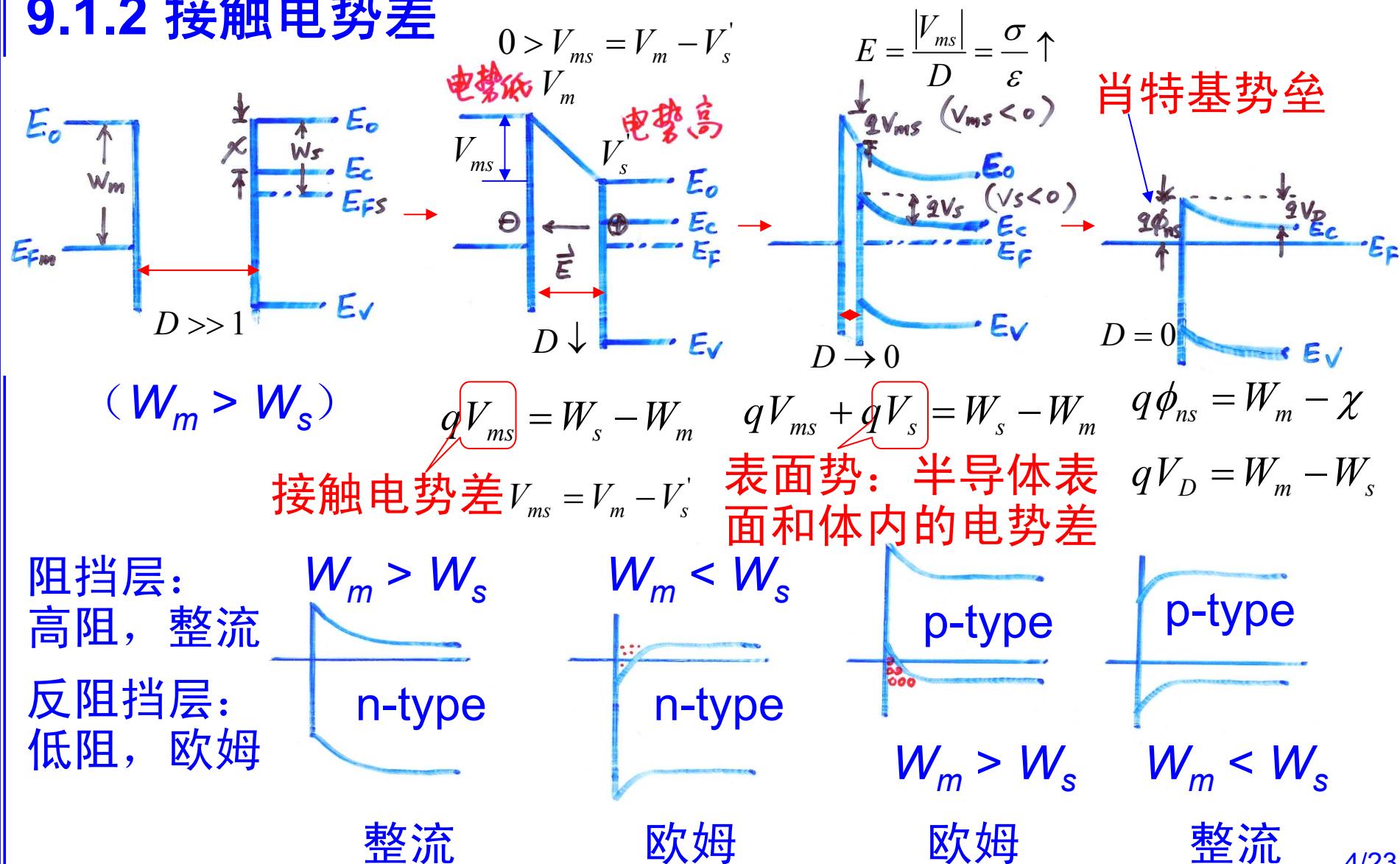
$$\chi = E_0 - E_C$$

$$E_n = E_c - E_f$$



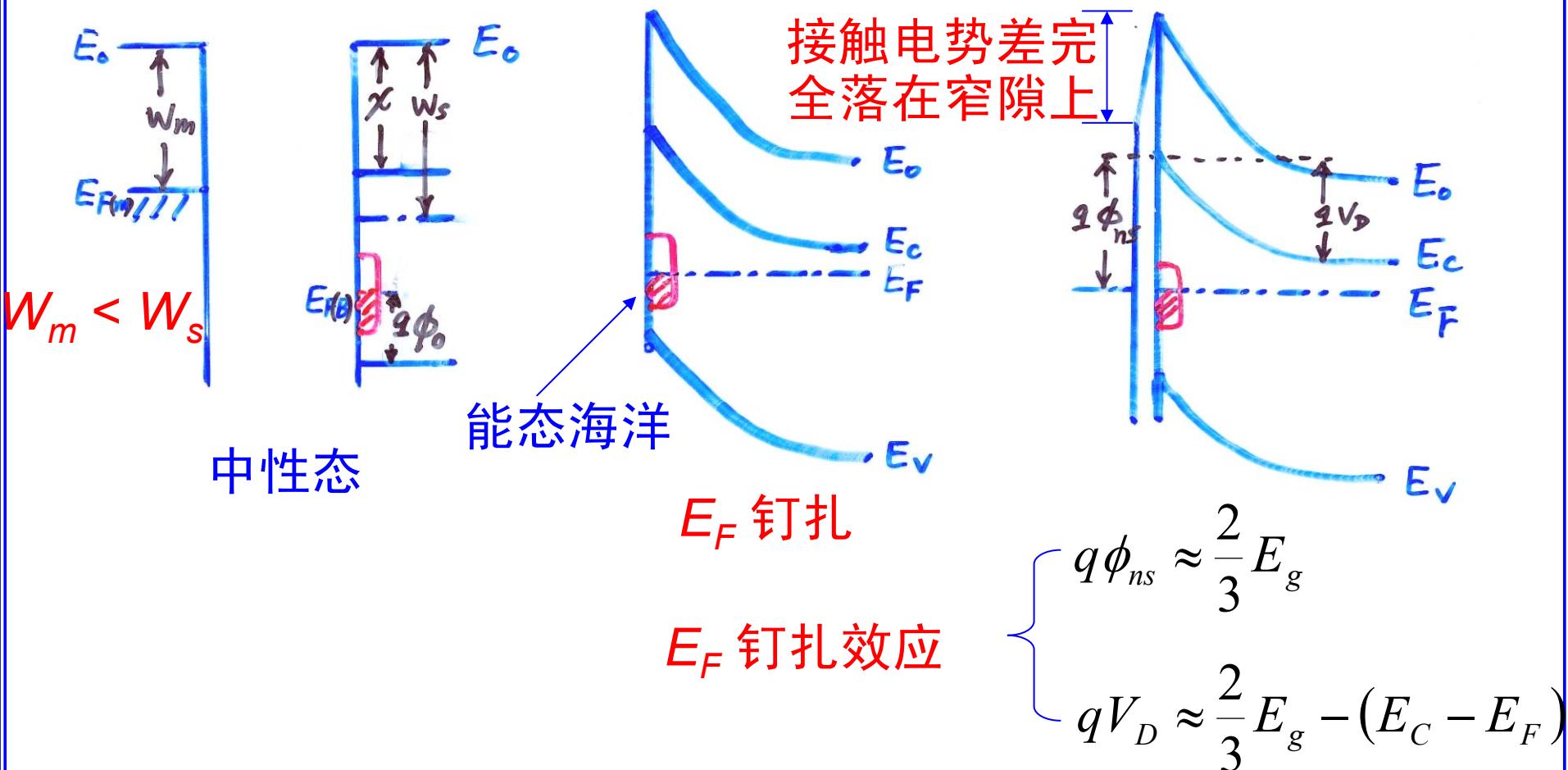
# 9.1 金半接触的能带图<sub>2</sub>

## 9.1.2 接触电势差



# 9.1 金半接触的能带图<sub>3</sub>

## 9.1.3 表面态对接触势垒的影响

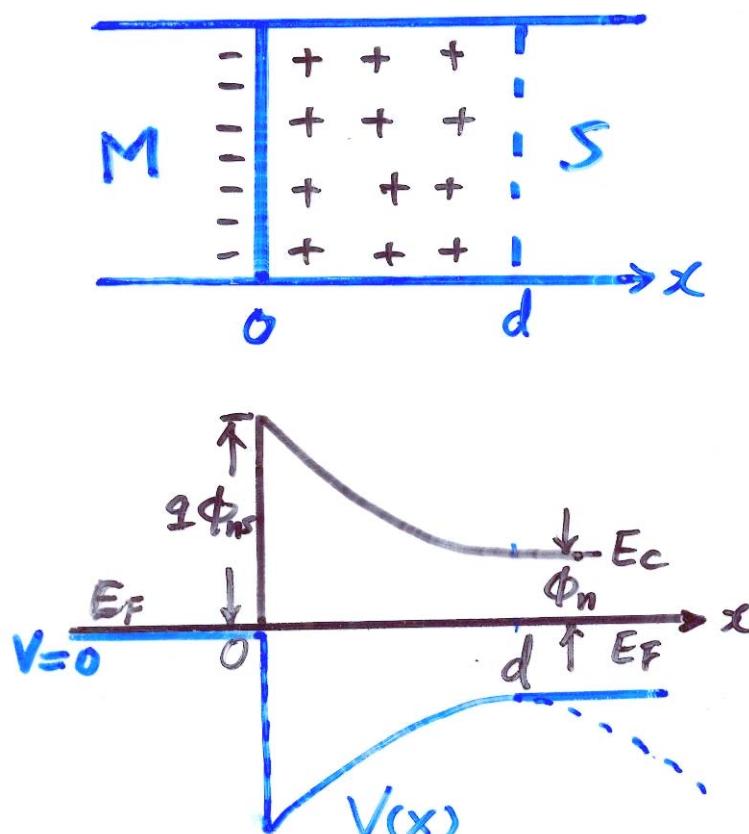


- 1° 势垒高度与金属功函数基本无关
- 2° 即使  $W_m < W_s$ , 阻挡层依然存在

# 9.1 金半接触的能带图<sub>4</sub>

## 9.1.4 势垒区的电势分布

-n型半导体



泊松方程

$$\frac{d^2V}{dx^2} = \begin{cases} -\frac{qN_D}{\epsilon_0\epsilon_r} & 0 \leq x \leq d \\ 0 & x > d \end{cases}$$

$$E(x) = -\frac{dV}{dx} = \frac{qN_D}{\epsilon_0\epsilon_r}(x-d) \quad \boxed{E(d) = 0}$$

$$V(x) = -\frac{qN_D}{2\epsilon_0\epsilon_r}(x^2 - 2xd) - \phi_{ns} \quad \boxed{V(0) = -\phi_{ns}}$$

$$\boxed{V(d) = -\phi_n \quad \phi_{ns} = \phi_n + V_D}$$

$$d = \left[ \frac{2\epsilon_0\epsilon_r(\phi_{ns} - \phi_n)}{qN_D} \right]^{1/2} = \left( \frac{2\epsilon_0\epsilon_r}{qN_D} V_D \right)^{1/2}$$

# 9.1 金半接触的能带图<sub>5</sub>

## 9.1.5 肖特基接触的势垒电容

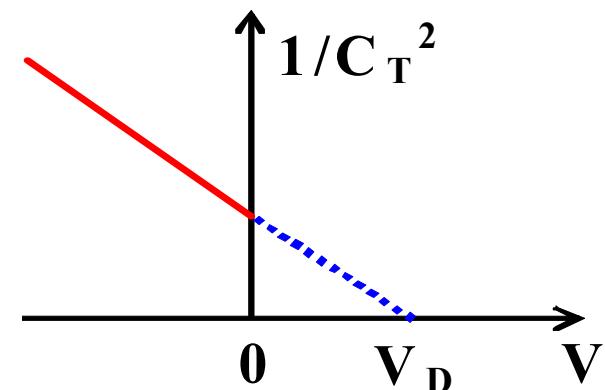
$$d = \left[ \frac{2\epsilon_0 \epsilon_r (\phi_{ns} - \phi_n)}{qN_D} \right]^{1/2} = \left( \frac{2\epsilon_0 \epsilon_r V_D}{qN_D} \right)^{1/2}$$

施加反向偏压V时

$$d = \left[ \frac{2\epsilon_0 \epsilon_r (V_D - V)}{qN_D} \right]^{\frac{1}{2}}$$

平行板电容

$$C_T = A \frac{\epsilon_0 \epsilon_r}{d} = A \left[ \frac{\epsilon_0 \epsilon_r q N_D}{2(V_D - V)} \right]^{1/2}$$



与单边突变p-n结相同

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9.2 金半接触的整流输运理论

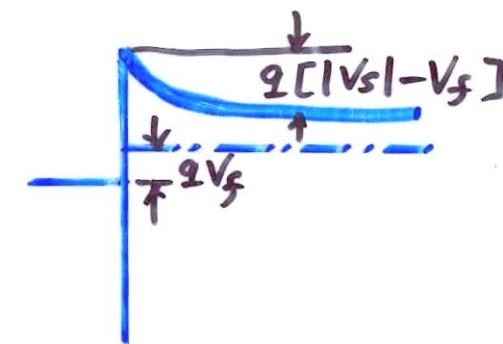
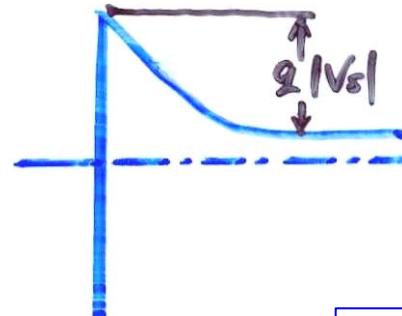
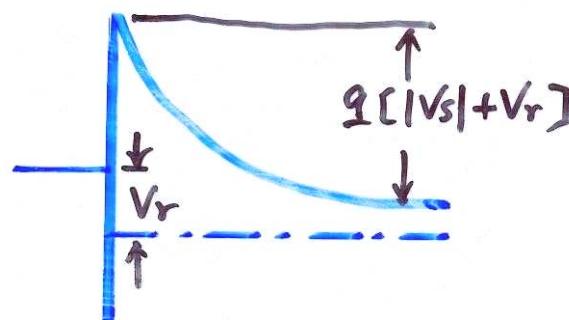
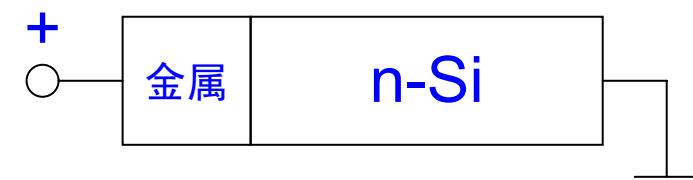
9.3 少子注入和欧姆接触

# 9.2 金半接触的整流输运理论<sub>1</sub>

## 9.2.1 扩散理论

—适用于势垒宽度>>  
电子平均自由程

$$l_n \ll d$$



同时考虑势垒区扩散和漂移电流

$$\mu = \frac{q}{kT} D$$

$$J = qn(x)\mu_n E(x) + qD_n \frac{dn(x)}{dx} = qD_n \left[ -\frac{qn(x)}{kT} \frac{dV(x)}{dx} + \frac{dn(x)}{dx} \right]$$

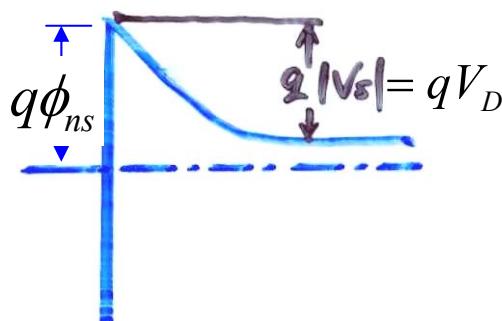
$$E(x) = -\frac{dV}{dx}$$

$$J \exp \left[ -\frac{qV(x)}{kT} \right] = qD_n \frac{d}{dx} \left\{ n(x) \exp \left[ -\frac{qV(x)}{kT} \right] \right\}$$

# 9.2 金半接触的整流输运理论<sub>2</sub>

## 9.2.1 扩散理论

积分  $\int_0^d dx \rightarrow J \exp\left[-\frac{qV(x)}{kT}\right] = qD_n \frac{d}{dx} \left\{ n(x) \exp\left[-\frac{qV(x)}{kT}\right] \right\}$



$$\int_0^d J \exp\left[-\frac{qV(x)}{kT}\right] dx \leftarrow V(x) = -\frac{qN_D}{2\epsilon_0\epsilon_r} (x^2 - 2xd) - \phi_{ns}$$

$$= J \int_0^d \exp\left\{ \frac{q}{kT} \left[ \frac{qN_D}{2\epsilon_0\epsilon_r} (x^2 - 2xd) + \phi_{ns} \right] \right\} dx \leftarrow x^2 \ll 2xd \quad \exp\left[-\frac{qV(x)}{kT}\right]$$

$$\approx J \int_0^d \exp\left( \frac{q\phi_{ns}}{kT} \right) \exp\left( -\frac{q^2 N_D d}{\epsilon_0 \epsilon_r k T} x \right) dx$$

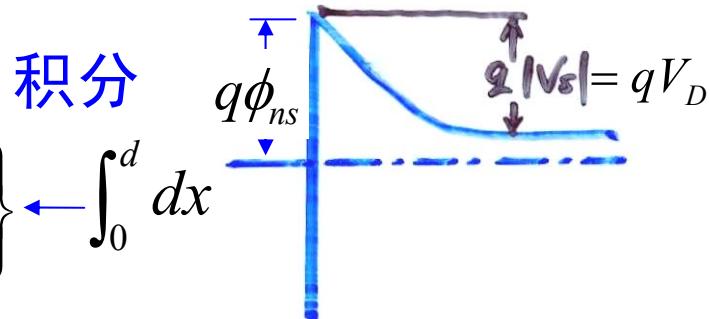
$$= J \exp\left( \frac{q\phi_{ns}}{kT} \right) \frac{\epsilon_0 \epsilon_r k T}{q^2 N_D d} \left[ 1 - \exp\left( -\frac{q^2 N_D d^2}{\epsilon_0 \epsilon_r k T} \right) \right] \approx J \exp\left( \frac{q\phi_{ns}}{kT} \right) \frac{\epsilon_0 \epsilon_r k T}{q^2 N_D d}$$

主要取决于x=0附近的电势值

# 9.2 金半接触的整流输运理论<sub>3</sub>

## 9.2.1 扩散理论

$$J \exp\left[-\frac{qV(x)}{kT}\right] = qD_n \frac{d}{dx} \left\{ n(x) \exp\left[-\frac{qV(x)}{kT}\right] \right\} \int_0^d dx$$



平衡态近似

$$\begin{aligned} n(0) &= n_0 \exp(qV_{s0}/kT) \\ &= n_0 \exp(-qV_D/kT) \\ n(d) &= n_0 \end{aligned}$$

$$qD_n \left\{ n(x) \exp\left[-\frac{qV(x)}{kT}\right] \right\} \Big|_0^d$$

$$\begin{aligned} V(x) &= -\frac{qN_D}{2\epsilon_0\epsilon_r} (x^2 - 2xd) - \phi_{ns} \\ V(0) &= -\phi_{ns} \\ V(d) &= \frac{qN_D}{2\epsilon_r\epsilon_0} d^2 - \phi_{ns} \\ V(d) &= -[\phi_{ns} - (V_D - V)] \end{aligned}$$

$$= qD_n n_0 \exp\left[\frac{q}{kT} (\phi_{ns} - V_D + V)\right] - qD_n n_0 \exp\left(\frac{qV_{s0}}{kT}\right) \exp\left(\frac{q\phi_{ns}}{kT}\right)$$

$-V_D = V_{s0}$

$$= qD_n n_0 \exp\left[q(V_{s0} + \phi_{ns})/kT\right] \left[ \exp(qV/kT) - 1 \right]$$

# 9.2 金半接触的整流输运理论<sub>4</sub>

## 9.2.1 扩散理论

$$\int_0^d J \exp\left[-\frac{qV(x)}{kT}\right] dx = \int_0^d qD_n \frac{d}{dx} \left\{ n(x) \exp\left[-\frac{qV(x)}{kT}\right] \right\} dx$$

$$J \exp\left(\frac{q\phi_{ns}}{kT}\right) \frac{\varepsilon_0 \varepsilon_r kT}{q^2 N_D d} = qD_n n_0 \exp\left[q(V_{s0} + \phi_{ns})/kT\right] [\exp(qV/kT) - 1]$$

$$J = \frac{q^3 D_n n_0 N_D d}{\varepsilon_0 \varepsilon_r kT} \exp(-qV_D/kT) [\exp(qV/kT) - 1]$$

$$d = \left[ \frac{2\varepsilon_0 \varepsilon_r}{qN_D} (V_D - V) \right]^{\frac{1}{2}}$$

$$= \frac{q^2 D_n n_0}{kT} \left[ \frac{2qN_D}{\varepsilon_0 \varepsilon_r} (V_D - V) \right]^{1/2} \exp(-qV_D/kT) [\exp(qV/kT) - 1]$$

$$= J_{SD} [\exp(qV/kT) - 1]$$

—适用于势垒宽度>>电子平均自由程  
12/23