

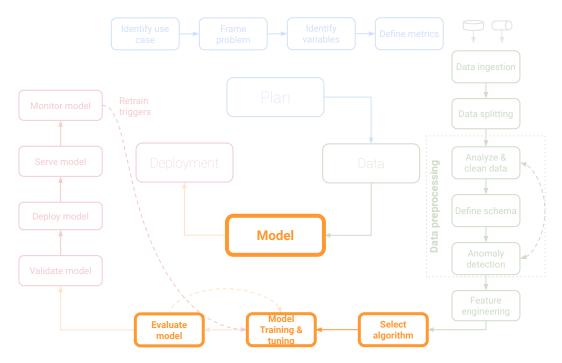
# Models

# Fundamentals

Prof. Dr. Jan Kirenz HdM Stuttgart

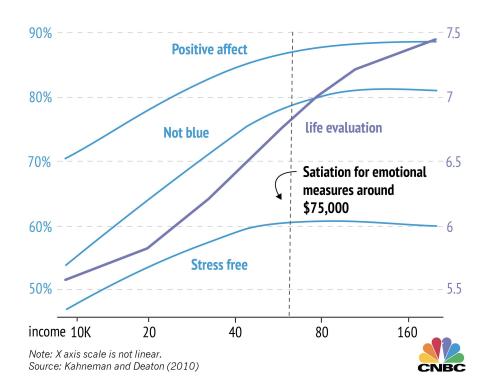
#### **Data Science Lifecycle**

Plan | Data | **Model** | Deployment



How do we select, train, tune (optimize) and evaluate models?

Data:
Money &
Happiness



Widely regarded as one of the world's most influential living psychologist, **Daniel Kahneman** won the Nobel in Economics for his pioneering work in behavioral economics:

"Below an income of … \$60,000 a year, people are unhappy, and they get progressively unhappier the poorer they get. Above that, we get an absolutely flat line. … Money does not buy you experiential happiness, but lack of money certainly buys you misery."

Watch TED-talk:



Money can buy happiness, but only to a point

#### Does money make people happier?

Get the data at GitHub:



Code in Colab.

colab

Raw data:

OECD Better Life Index data: Life satisfaction









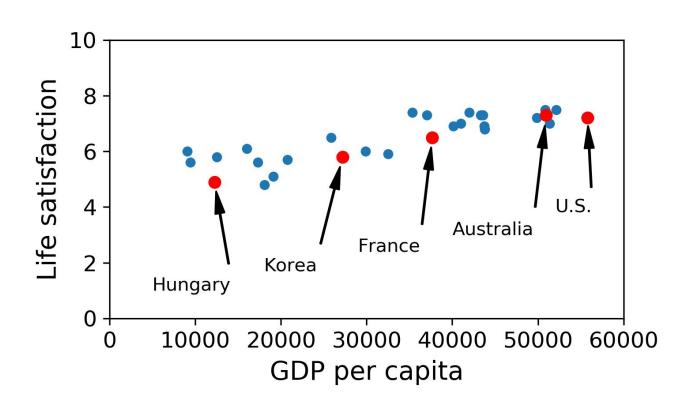
IMF: Gross domestic product per capita







# Exploratory data analysis (EDA)



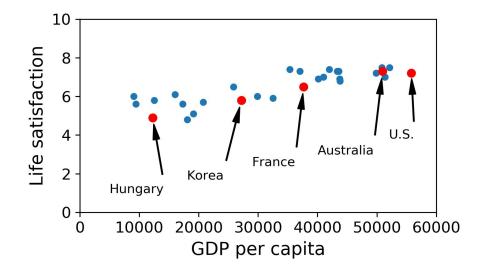
## Do you see a trend?

- Data exploration gives indication for a trend that is:
  - a. Positive or negative?
  - b. Linear or non-linear?

... but be careful, the data is noisy (i.e., partly random)

#### 2. Model (type) selection:

- a. Regression or classification?
- b. Linear or non-linear?



## A simple linear regression model

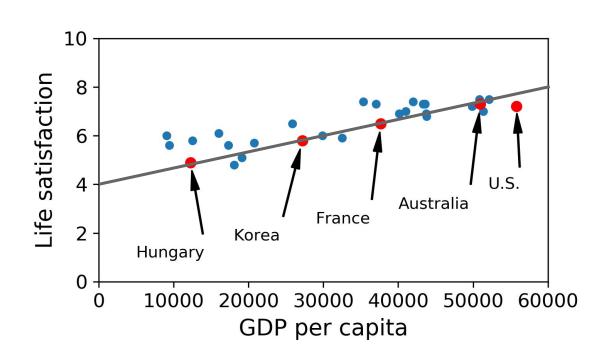
$$\hat{\mathbf{y}}_{i} = \theta_{0} + \theta_{1} \times \mathbf{x}_{1}$$

- $\hat{y}_i$  is the predicted output (life satisfaction).
- $\theta_0$  is the bias (the y-intercept).
- $\theta_1$  is the slope of our feature 1 (in machine learning often called weight of the feature)
- x<sub>1</sub> is our feature GDP (a known input).

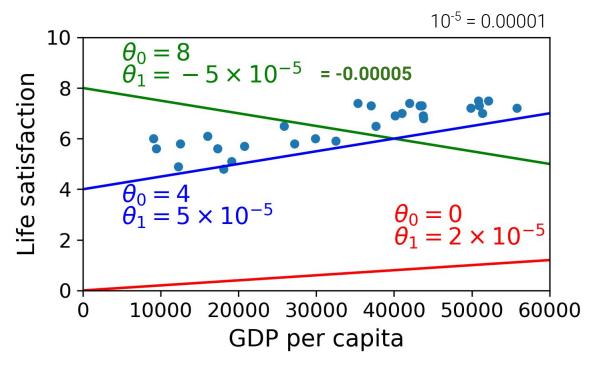
All the same, just different notations:

$$\hat{y}_i = b_0 + b_1 \times X_1$$

$$\hat{y}_i = W_0 + W_1 \times X_1$$



# A few possible linear models with different parameters ( $\theta$ )



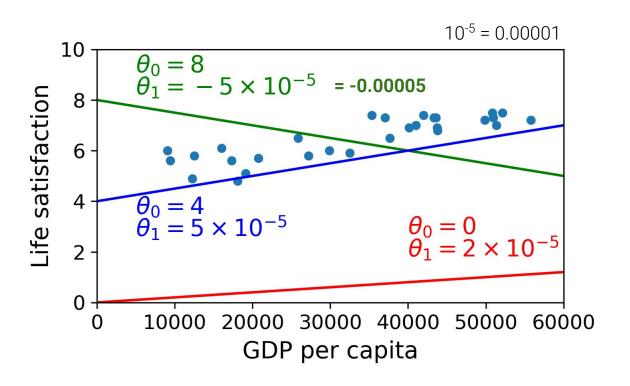
#### Model can refer to a

- Type of model (we usually call this "algorithm")
  - o e.g., Linear Regression
- 2. Fully specified model architecture
  - e.g., Linear Regression with one input and one output.
- 3. Final trained model
  - e.g. Linear Regression with one input and one output, using  $\theta_0$ = 4.85  $\theta_1$ = 4.91 × 10<sup>-5</sup>

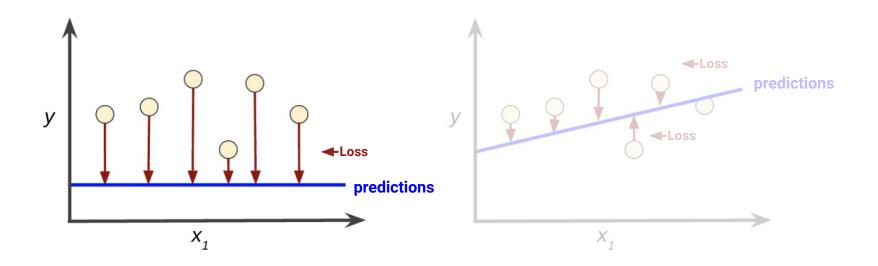
#### Model **selection** includes

- 1. Choosing the type of algorithm
  - o e.g., Linear Regression
- 2. Fully specifying its architecture
  - e.g., Linear Regression with one input and one output.
- 3. Fitting (training) the model to find the model parameters that will make it best fit the training data
  - e.g. Linear Regression with one input and one output, using  $\theta_0 = 4.85 \ \theta_1 = 4.91 \times 10^{-5}$

#### How to select the **best fitting model**?

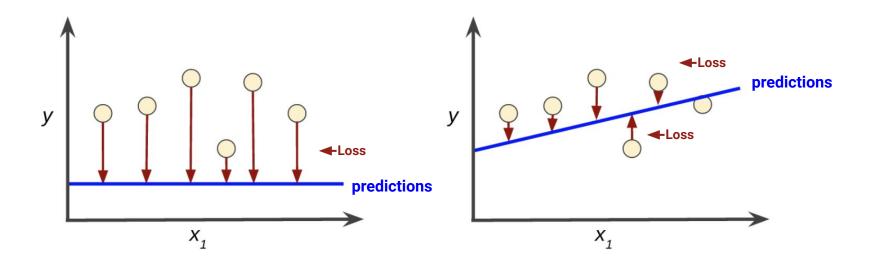


#### How to select the **best fitting model**?



- The arrows represent residuals (loss).
- The **blue lines** represent predictions.

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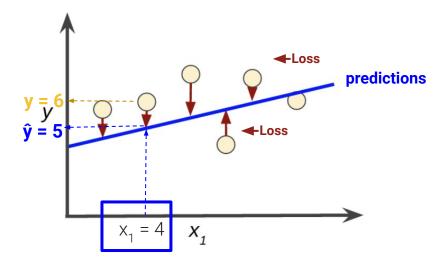
The squared loss for a **single observation** (example) is as follows

= the square of the difference between the true outcome (label) and the prediction

= (observation - prediction(x))<sup>2</sup>

$$= (y - \hat{y})^2$$

$$= (6 - 5)^2$$



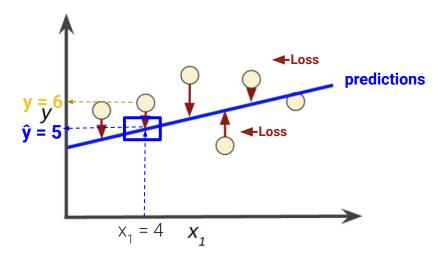
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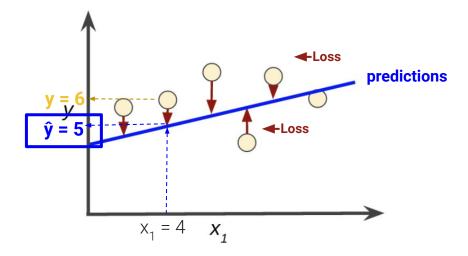
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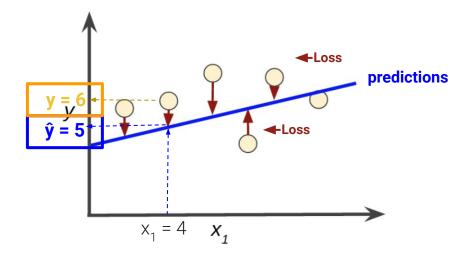
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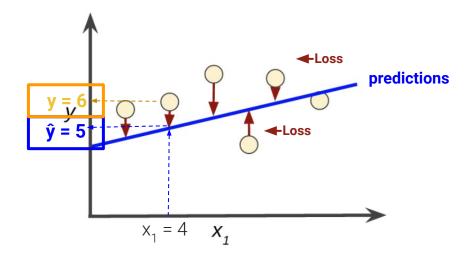
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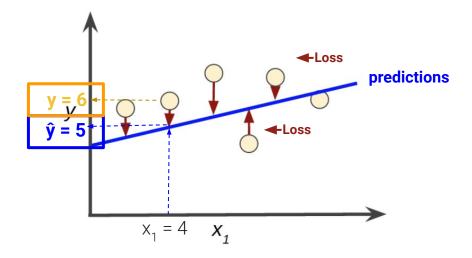
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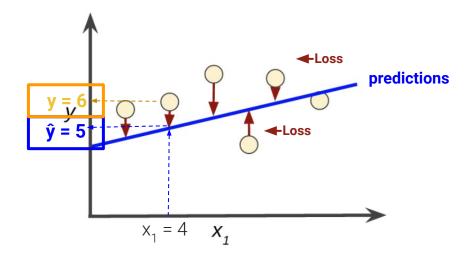
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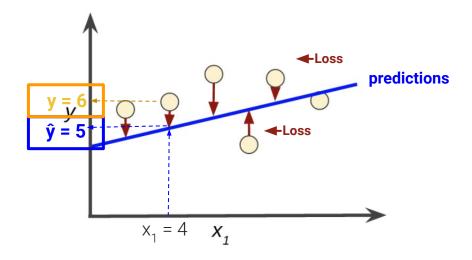
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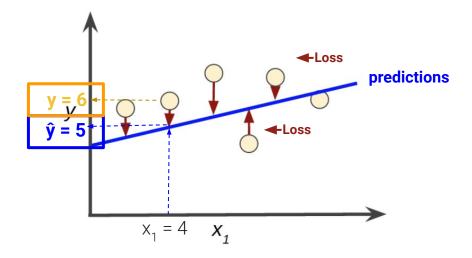
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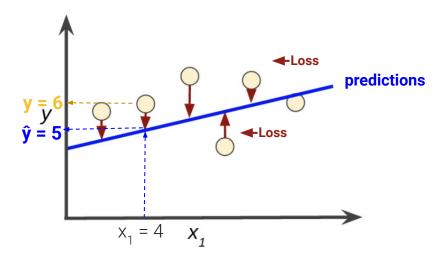
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$$= (\mathbf{y} - \mathbf{\hat{y}})^2$$

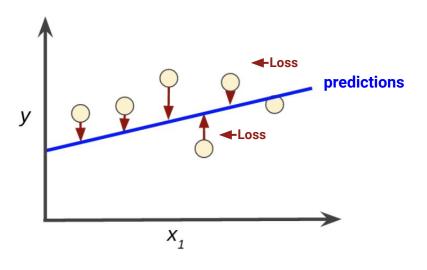
$$= (6 - 5)^2$$

$$(y_i - \hat{y}_i)^2$$



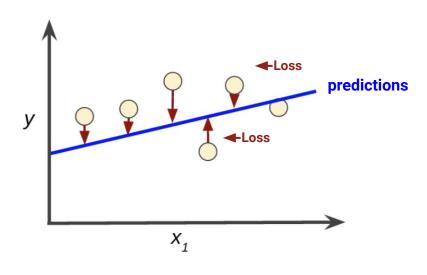
Mean square error (MSE) is the **average squared loss per example** over the whole dataset.

$$MSE = \frac{1}{n} \sum_{i=1}^{n} (y_i - \hat{y}_i)^2$$



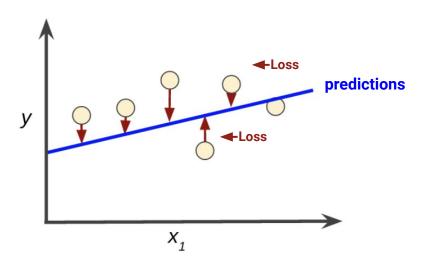
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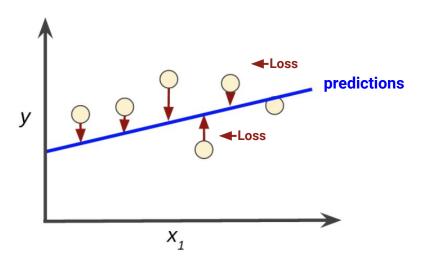
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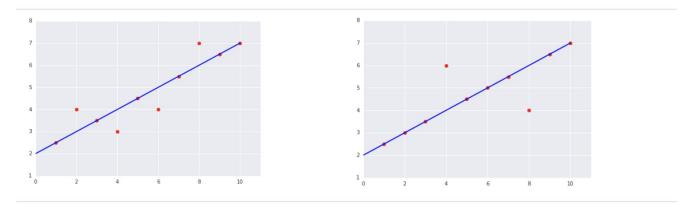
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#### Mean Squared Error

#### Consider the following two plots:

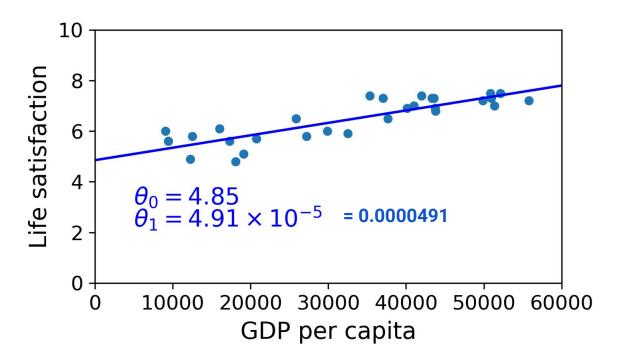


Explore the options below.



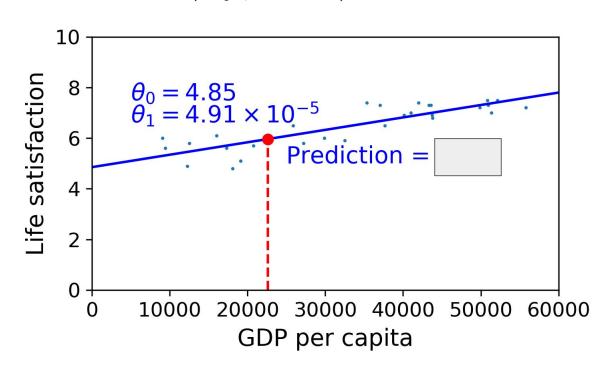
#### Our best fitting model

We used the **mean squared error** to select the best model.

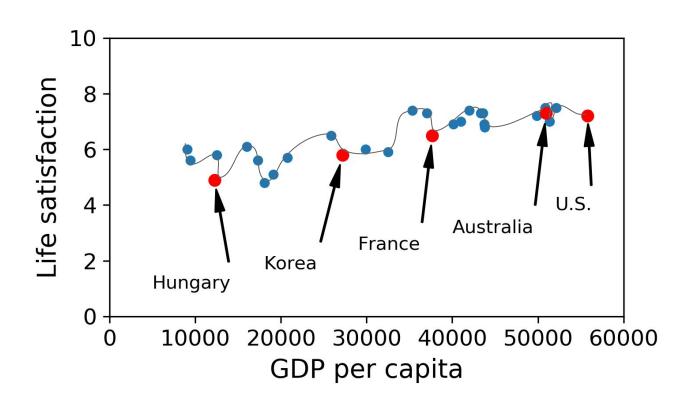


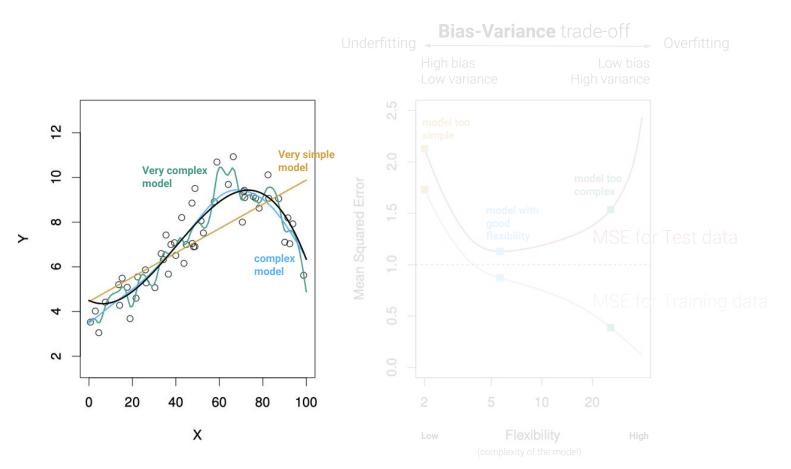
# Use your best fitting model to **predict** the life satisfaction of new data (Cypriots).

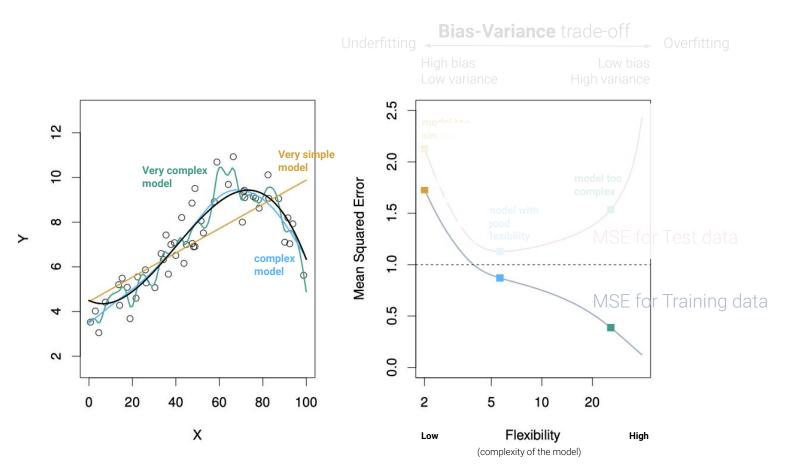
Cyprus's GDP per capita: \$22587.

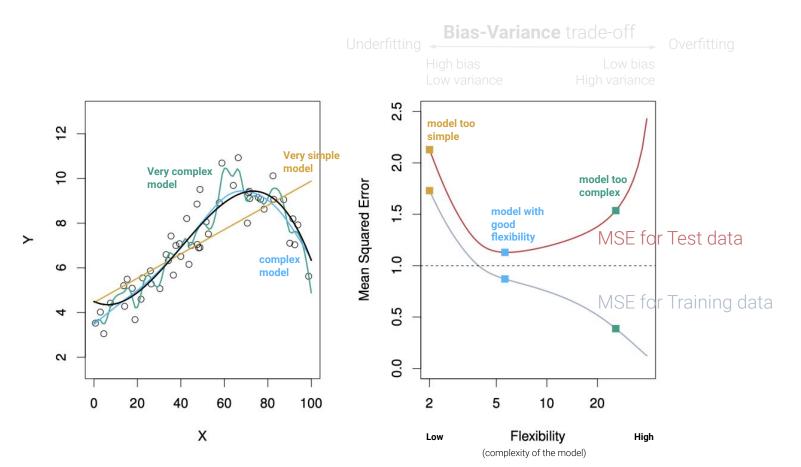


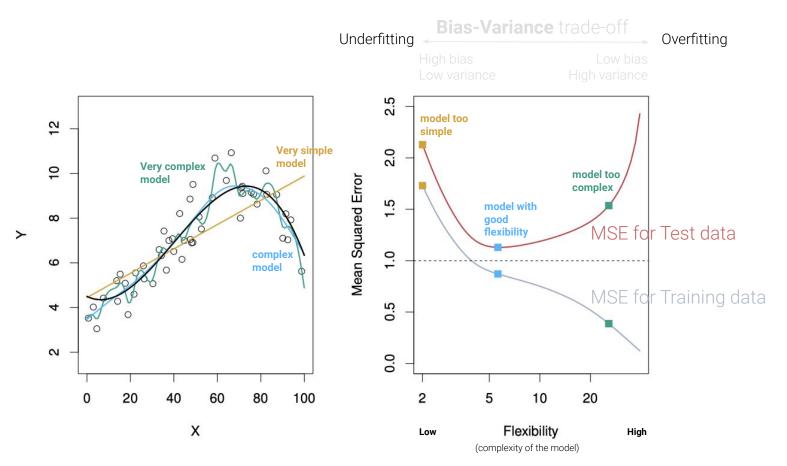
# Can a model be too good? Yes, it can

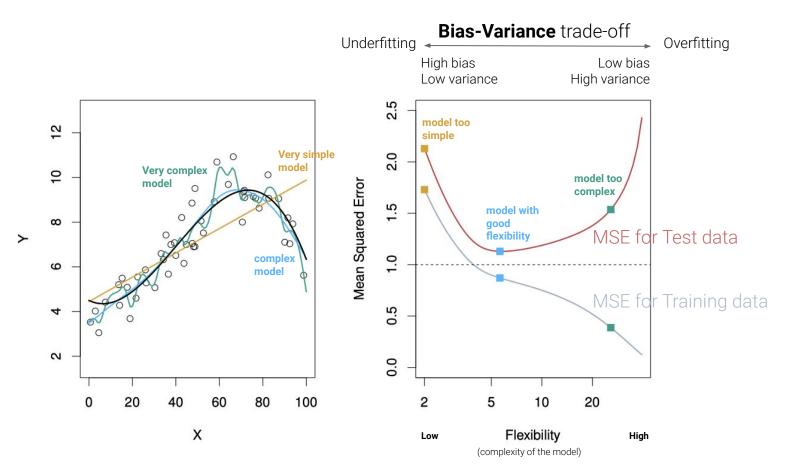








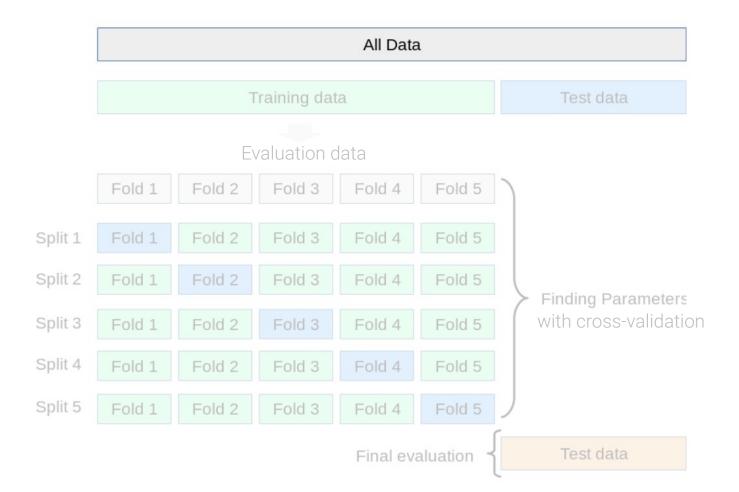


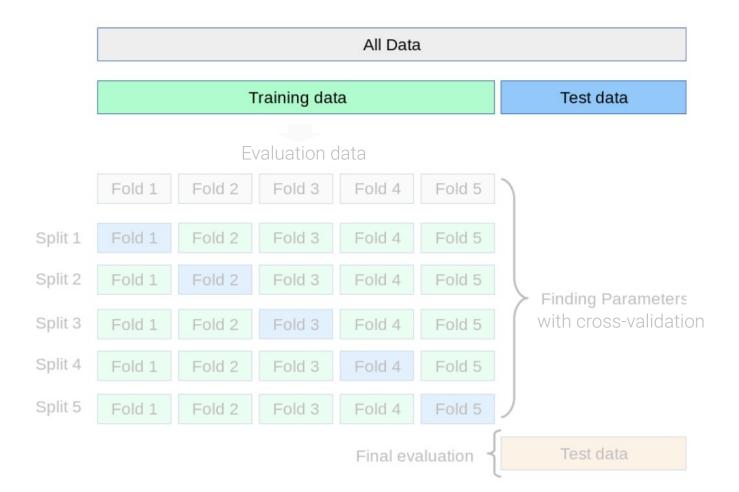


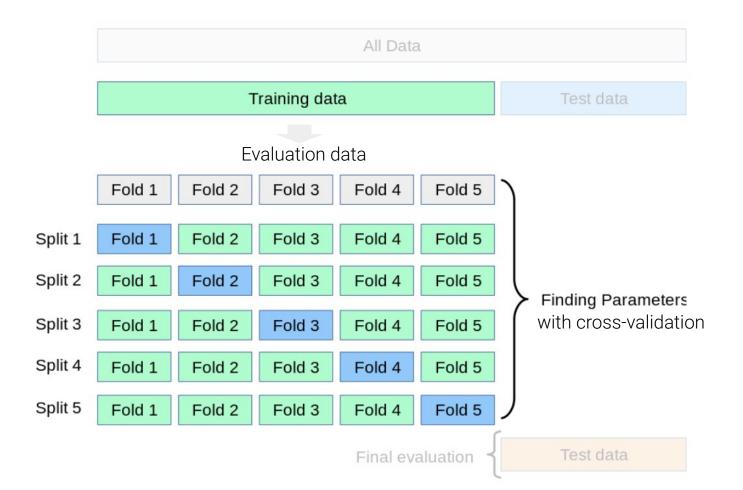
Source: James et. al. (2013)

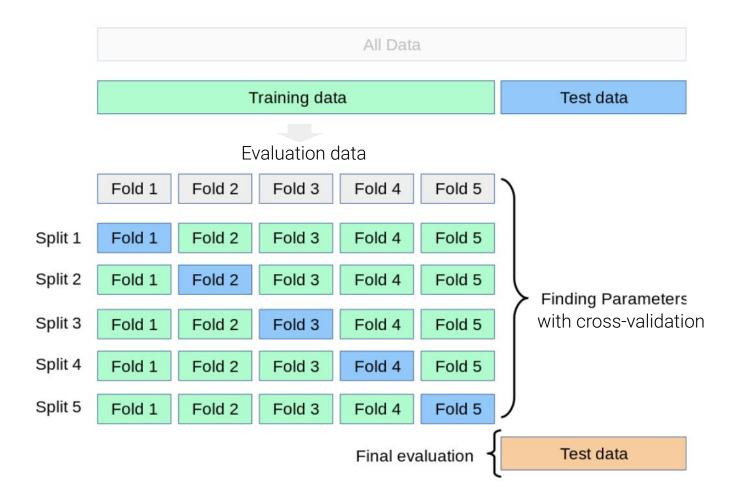
Prof. Dr. Jan Kirenz

Training, evaluation and testing data









## Training set, evaluation set and test set

### **Training set**

- Usually 80% of the data, but depends on sample size
- The error rate on training data is called the training error

### **Evaluation set (holdout set; development set)**

- We split the training set into smaller k sets (usually 5 or 10) to be able to find optimal parameters (hyperparameters)
- This approach is called cross-validation

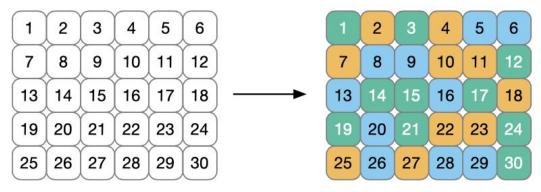
#### **Test set**

- Also called hold out data (usually 20%)
- The error rate on new cases is called the test error or generalization error (out-of-sample error)
- Low training error in combination with a high test error is a sign of overfitting

Source: Géron, A. (2019)
Prof. Dr. Jan Kirenz

- While there are a number of variations, the most common cross-validation method is k-fold cross-validation
- The data are randomly partitioned into k sets of roughly equal size (called the "folds").

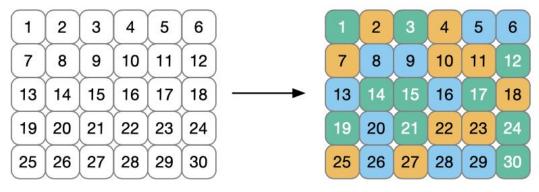
Step 1: assign each observation to one of 3 folds



For illustration, k = 3 is shown for a data set of thirty training set points with random fold allocations.

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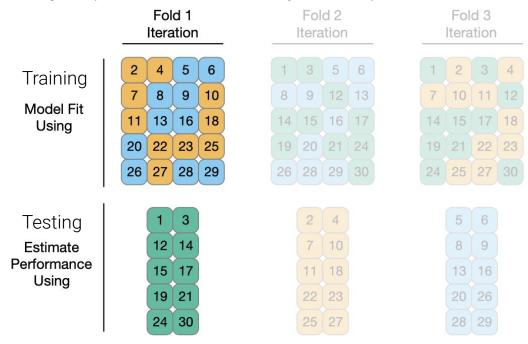
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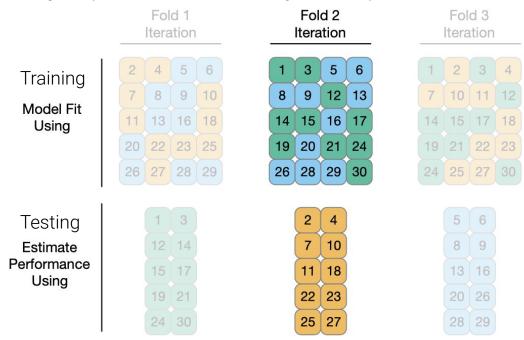
- For each iteration, one fold is held out for assessment statistics and the remaining folds are substrate for the model.
- This process continues for each fold so that three models produce three sets of performance statistics

### Step 2: split the folds into training and test partitions



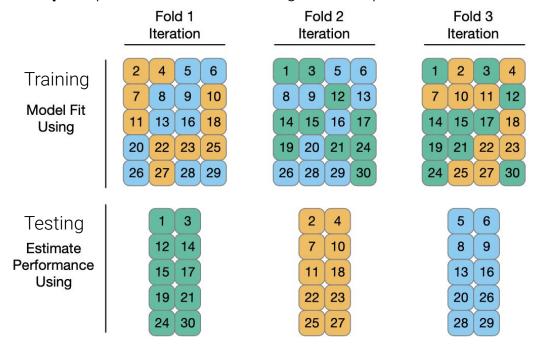
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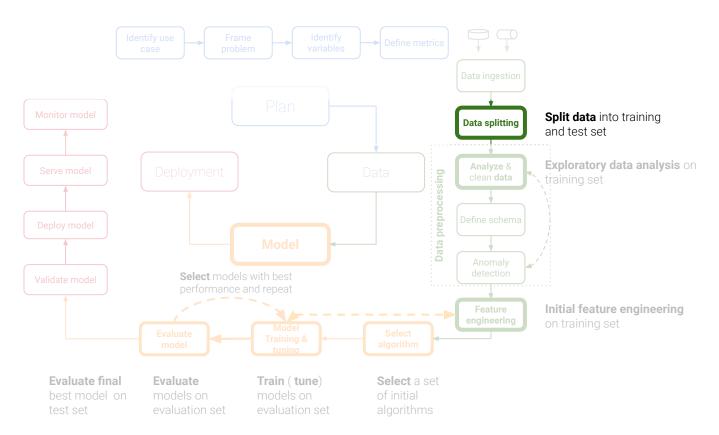
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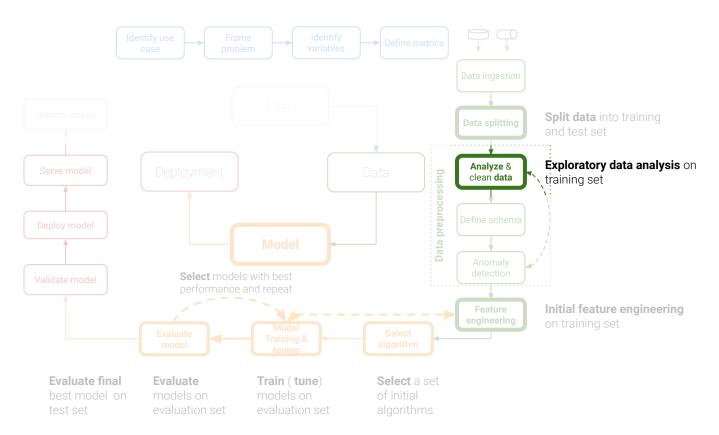


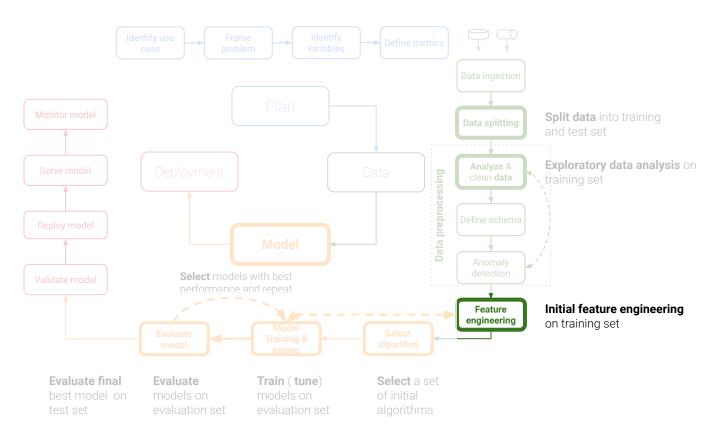
## k-Fold-Cross-Validation

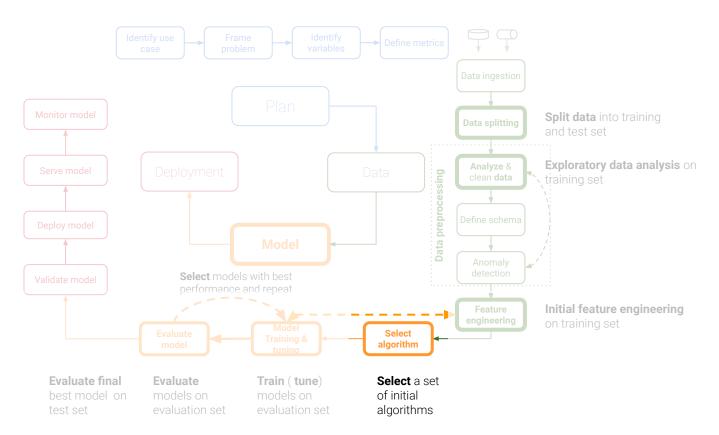
- Using k = 3 is a good choice to illustrate cross-validation but is a poor choice in practice.
- Values of k are most often 5 or 10.
- We generally prefer 10-fold cross-validation as a default.

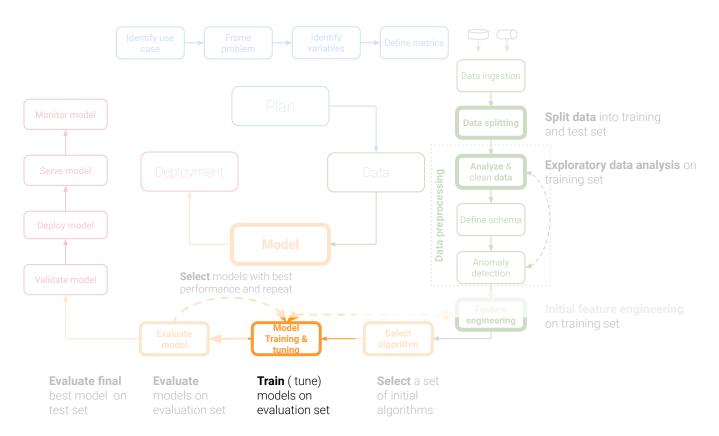
# Procedure

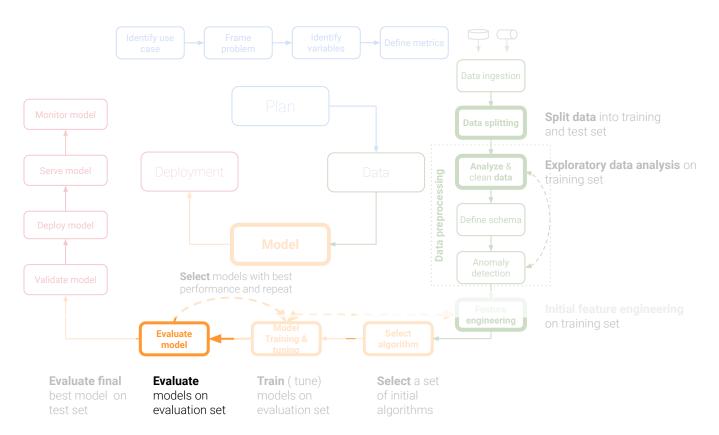


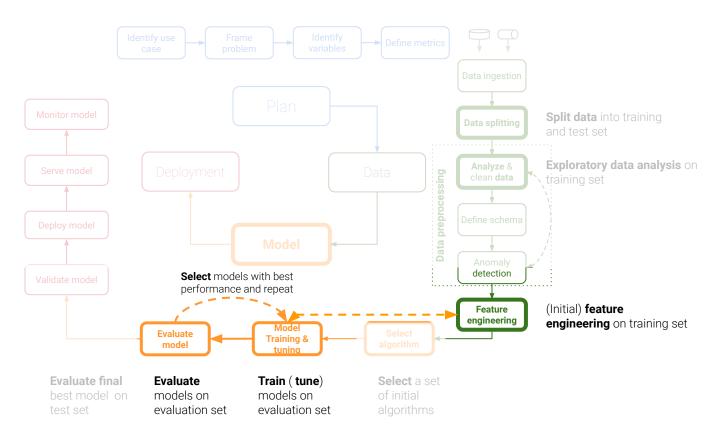


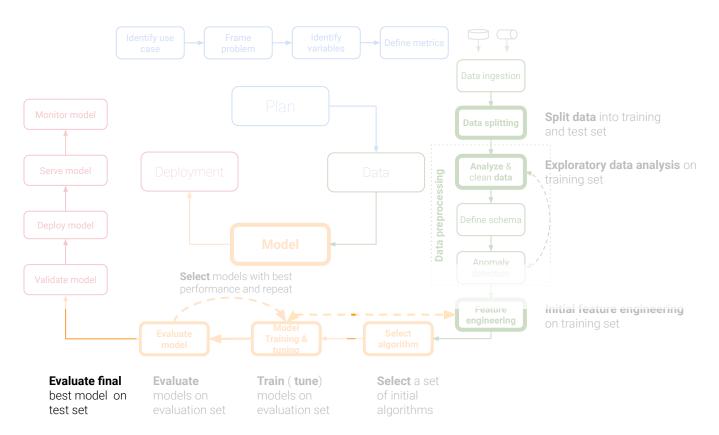












# Modeling procedere in summary

- 1. **Split data** into training and test set
- 2. Create **evaluation set** from training data (cross-validation)
- 3. **Train** a set of initial models using cross-validation (without extensive tuning)
- 4. **Select** the models with the best performance on the validation set
- 5. **Optimize** your models (hyperparameter tuning) on the validation set
- 6. Train the best model one more time on the **full training set**
- 7. Evaluate the final model on the **test set**
- 8. Do not further improve the model (this is your final result!)

Source: Géron (2019) Prof. Dr. Jan Kirenz

### Literature

Géron, A. (2019). Hands-on machine learning with Scikit-Learn, Keras, and TensorFlow: Concepts, tools, and techniques to build intelligent systems. O'Reilly Media.

Kuhn, M., & Silge, J. (2020). Tidy Modeling with R.