

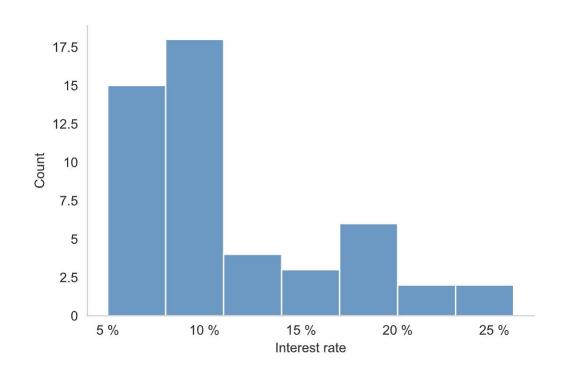
Exploratory data analysis

Exploring numerical data

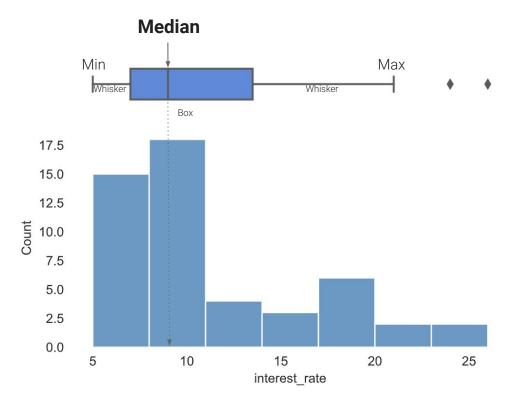
Prof. Dr. Jan Kirenz HdM Stuttgart

Box plots, quartiles, and the median

Histogram for variable interest rate



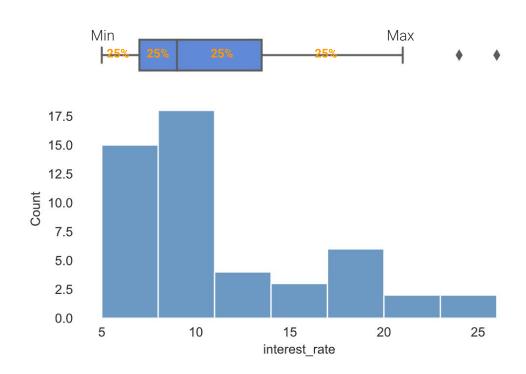
Boxplot and histogram for interest rate



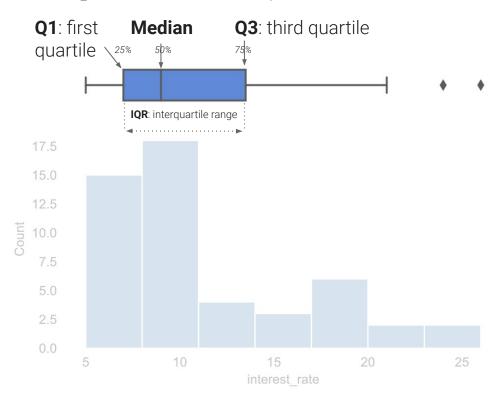
A box plot summarizes a dataset using five statistics while also identifying unusual observations

It includes the median as a bar inside a box with the shape of a rectangle.

Boxplot and quartiles



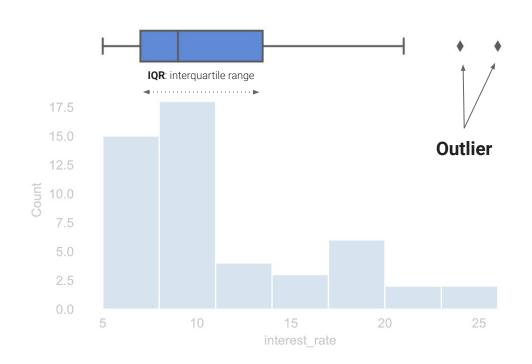
Boxplot, first quartile, third quartile and IQR



The length of the box is called the interguartile range, or IOR.

The two boundaries of the box are called the first quartile (the 25th percentile, i.e., 25% of the data fall below this value) and the third quartile (the 75th percentile, i.e., 75% of the data fall below this value), and these are often labeled Q1 and Q3, respectively.

Boxplot and outlier



An outlier is an observation that appears extreme relative to the rest of the data.

A commonly used formula is that any observation beyond **1.5 × IQR** away from the first or the third quartile is considered an outlier.

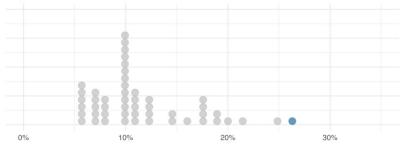
Outliers are extreme

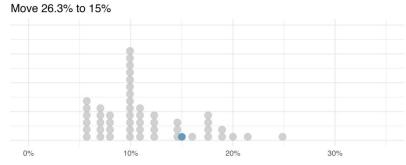
- Examining data for outliers serves many useful purposes, including
 - identifying strong skew in the distribution,
 - identifying possible data collection or data entry **errors**, and
 - providing **insight** into interesting properties of the data.

Keep in mind, however, that some datasets have a naturally long skew and outlying points do not represent any sort of problem in the dataset.

Robust statistics

Original data





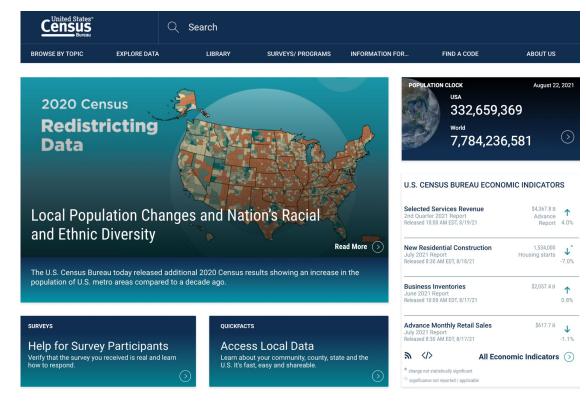
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	Robust		Not robust	
Scenario	Median	IQR	Mean	SD
Original data	9.93	5.75	11.6	5.05
Move 26.3% to 15%	9.93	5.75	11.3	4.61
Move 26.3% to 35%	9.93	5.75	11.7	5.68

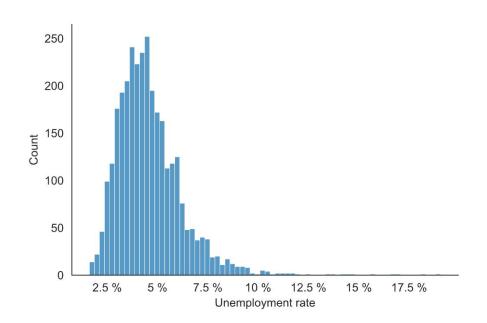
A comparison of how the median, IQR, mean, and standard deviation change as the value of an extreme observation from the original interest data changes.

Transforming data

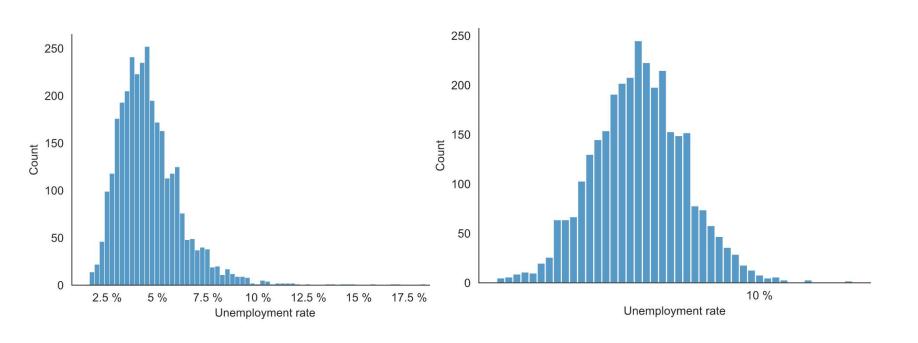
Data for 3142 counties in the United States



Skewed data: histogram of the percentage of unemployed in all US counties.



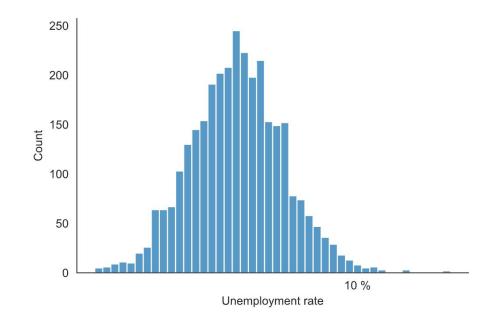
Skewed data and log transformed data



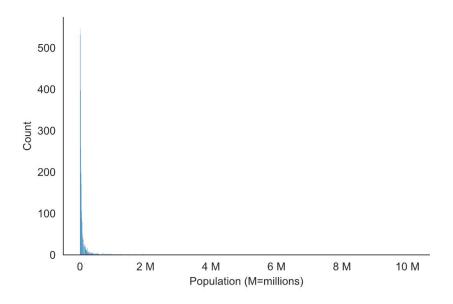
Skewed data and log transformed data

The x-value corresponds to the power of 10, e.g.,

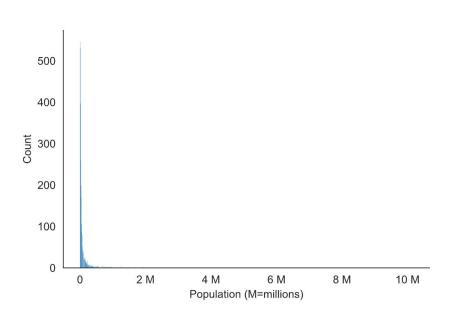
- 1 on the x-axis corresponds to $10^1 = 10$
- 5 on the x-axis corresponds to $10^5 = 100,000$.

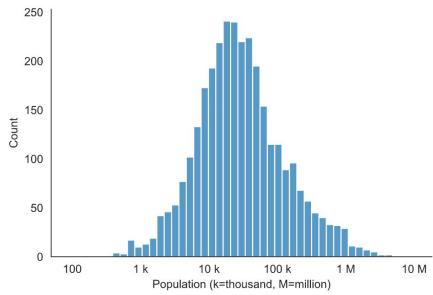


A histogram of population in all US counties

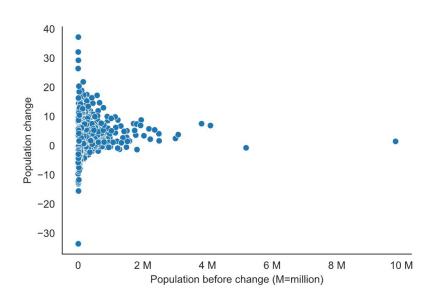


Skewed and log transformed data

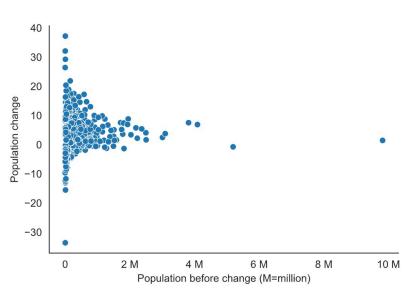


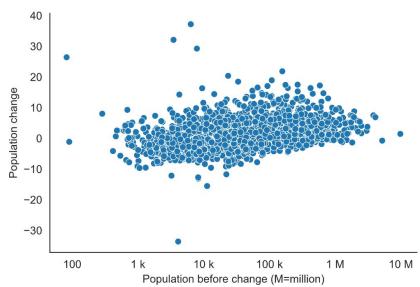


Scatterplot of population change against the population before the change



Result of log transformation



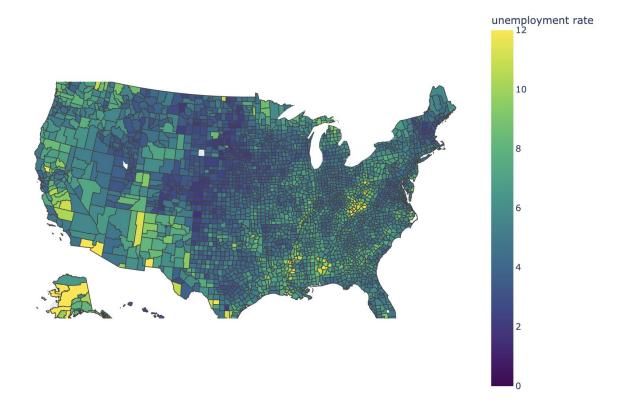


Example for usage of log-scales



Mapping

Intensity map of the unemployment rate (percent)



Terms you should know

average IQR scatterplot

bimodal left skewed standard deviation

box plot mean symmetric

data density median tail

deviation multimodal third quartile

distribution nonlinear transformation

dot plot outlier unimodal

first quartile percentile variability

histogram point estimate variance

intensity map right skewed weighted mean

interquartile range robust statistics whiskers