

# Statistical learning & machine learning

## Introduction

Prof. Dr. Jan Kirenz  
HdM Stuttgart

What is statistical  
learning?

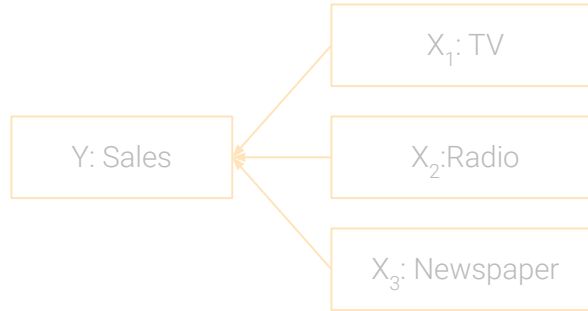
# Suppose we want to **predict sales** of a product

This is our **data**

- Variables:
  - Sales
  - TV advertising spendings
  - Radio advertising spendings
  - Newspaper advertising spendings

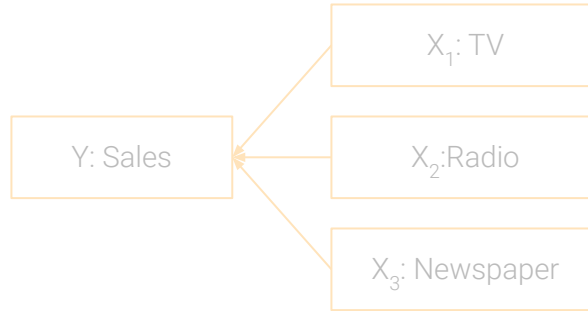
# We first need to define the outcome and predictor variables

- **Outcome** variable (response, dependent variable):
  - Sales (Y)
- **Input** variable (predictors, independent variables, features)
  - TV ( $X_1$ )
  - Radio ( $X_2$ )
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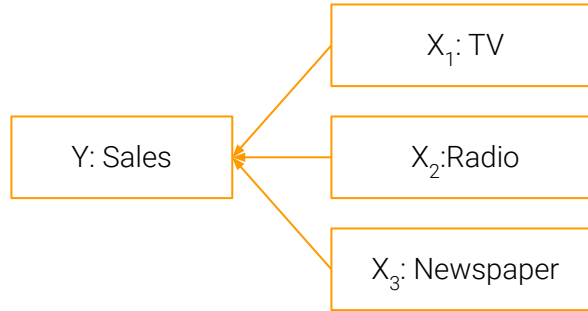
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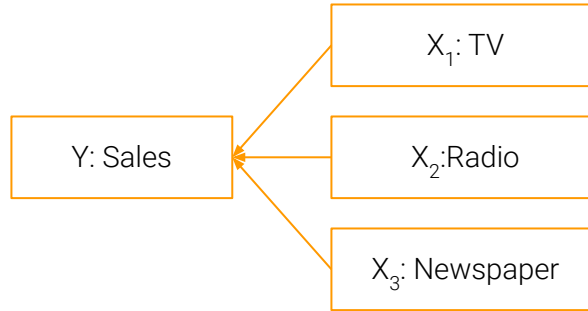
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Statistical learning refers to a set of approaches for **estimating** a **function** (f) between Y and X.

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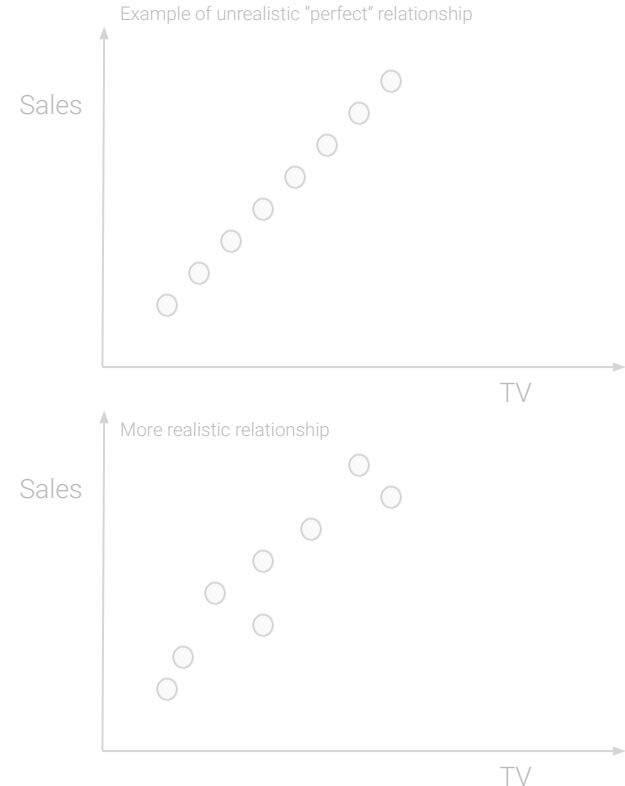
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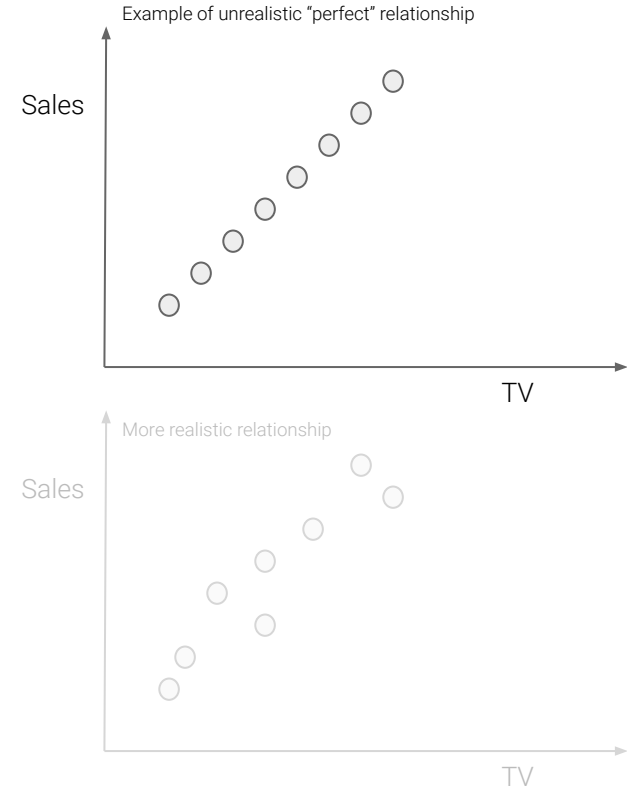
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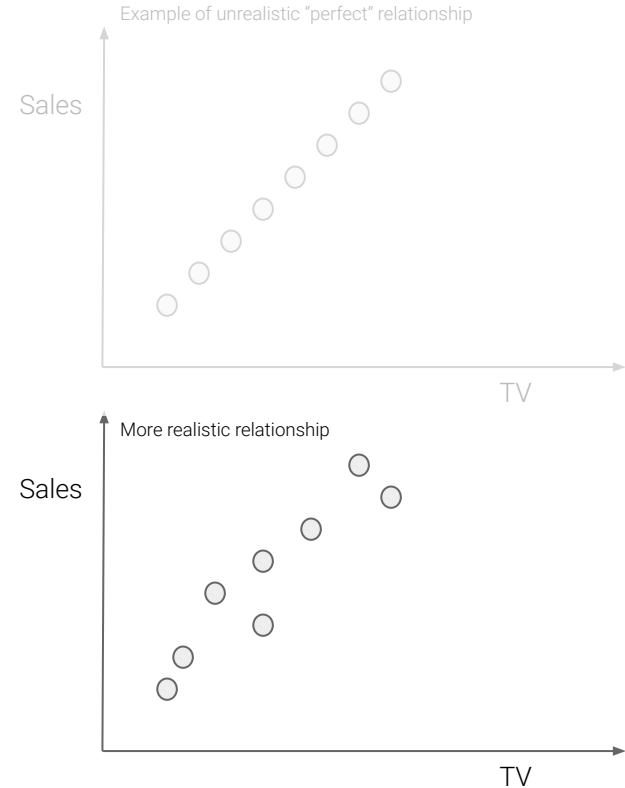
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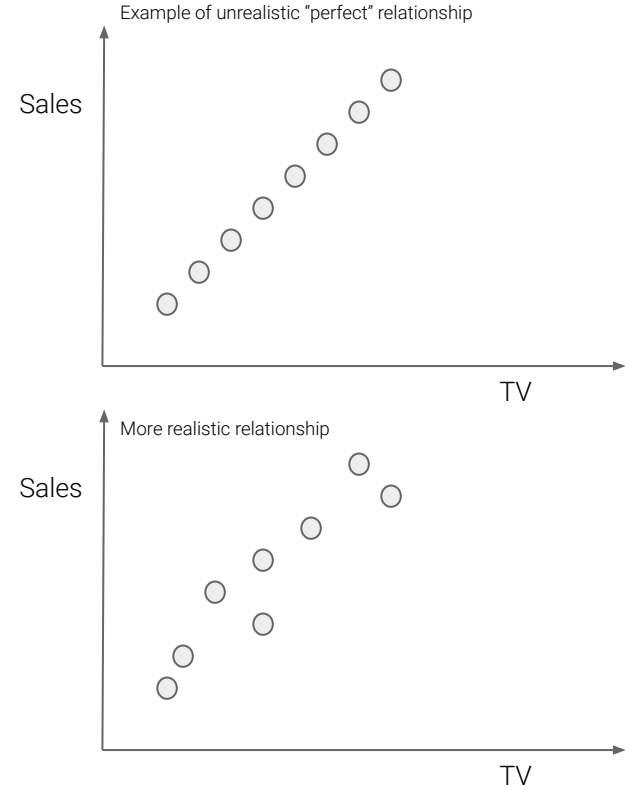
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# We don't know the true association between our outcome and the predictors

The "true" but unknown relationship

$$Y = f(X) + \epsilon.$$

$$Y: \text{Sales} = \text{function}(X_1: \text{TV}, X_2: \text{Radio}, X_3: \text{Newspaper}) + \text{noise}$$

- $f$  is some fixed but unknown function of  $X_1, \dots, X_p$
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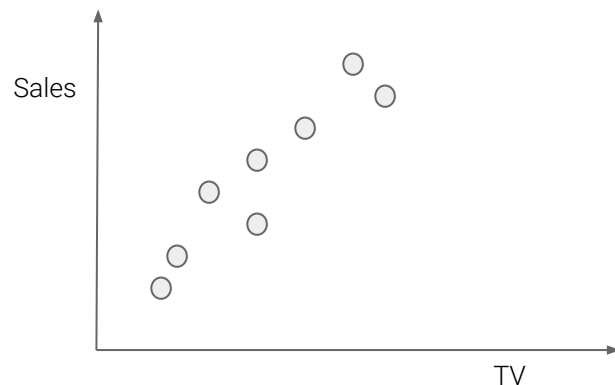
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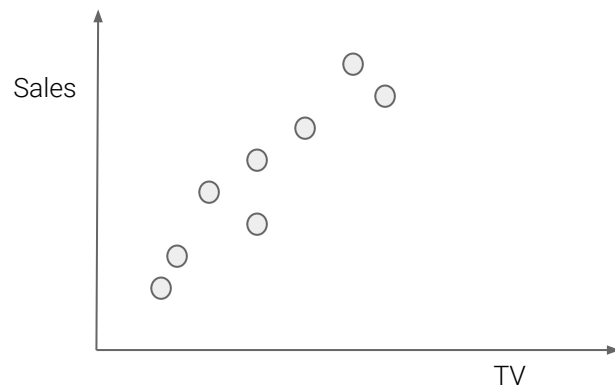
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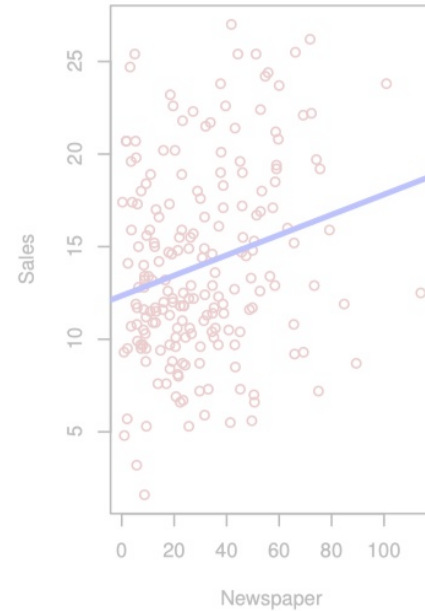
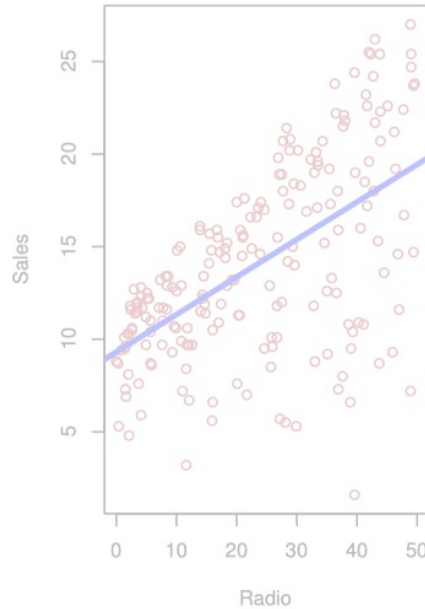
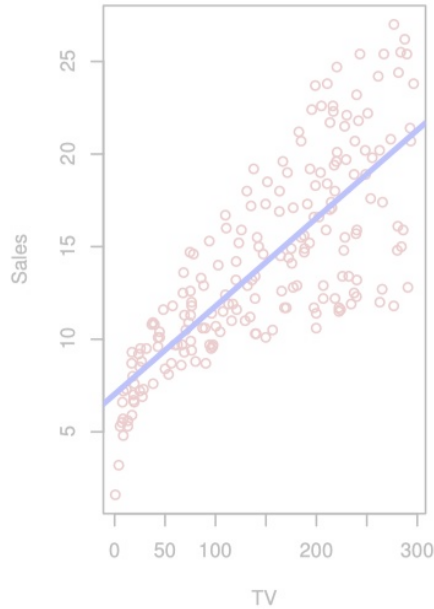
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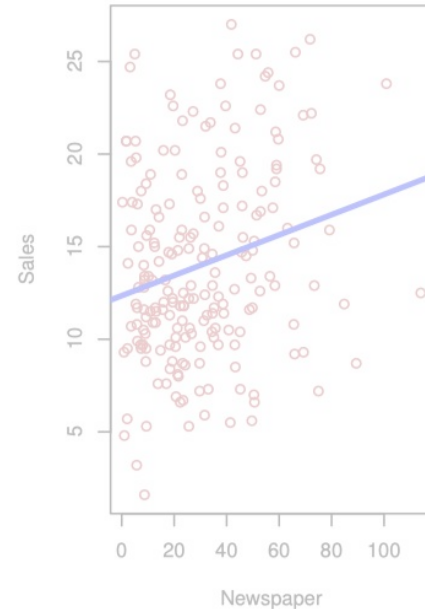
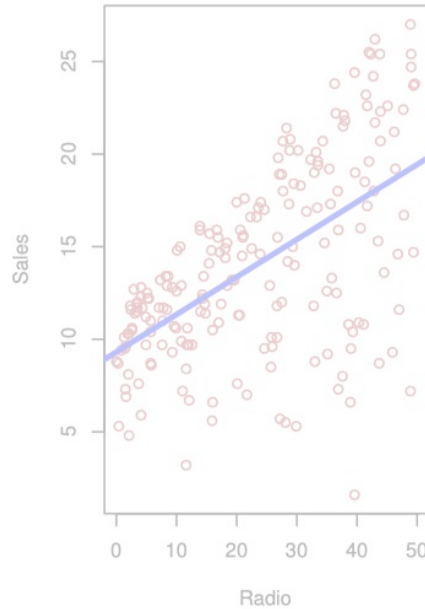
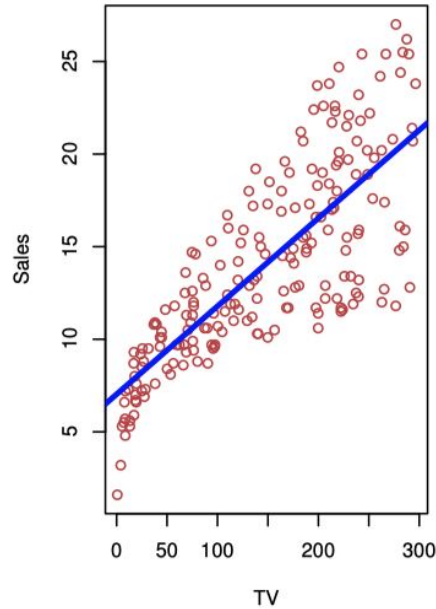


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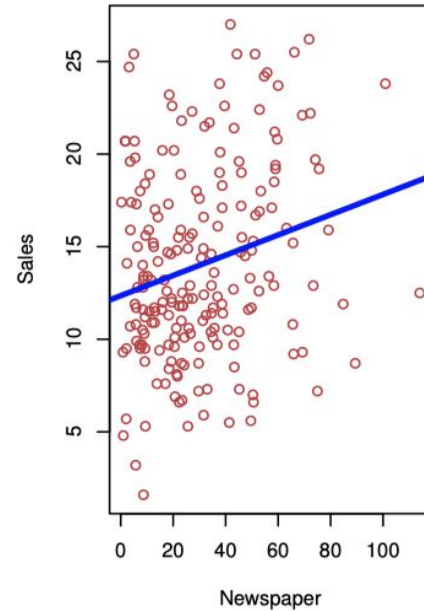
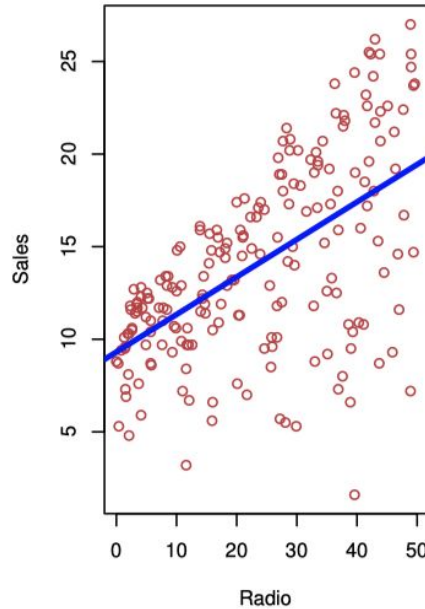
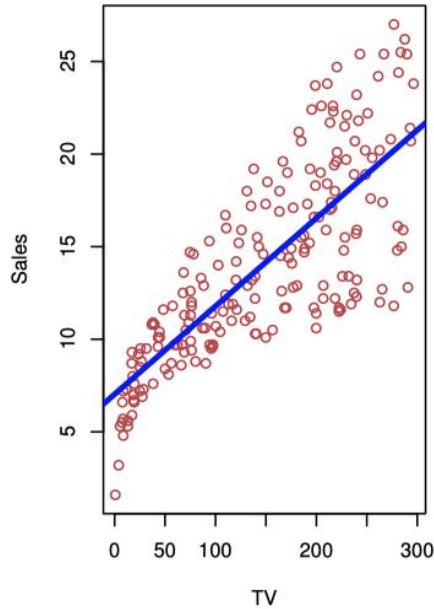


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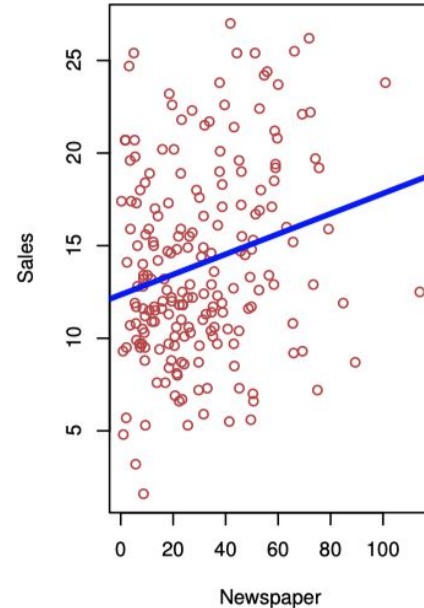
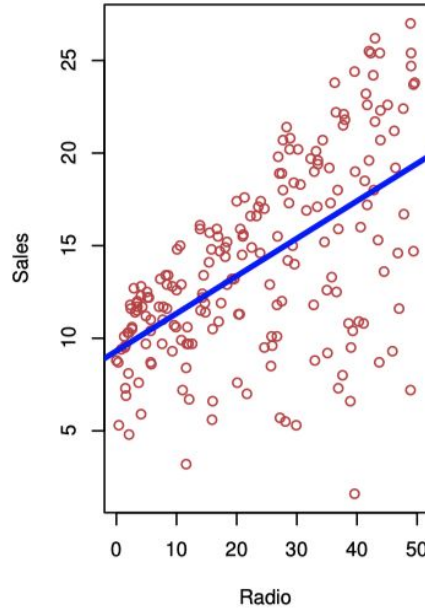
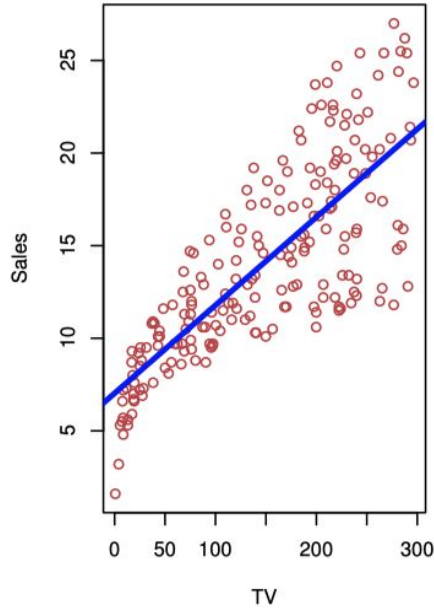


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We want to **predict**  $\hat{Y}$  with the aim to **minimize** the **reducible error**

$$\begin{aligned} E(Y - \hat{Y})^2 &= E[f(X) + \epsilon - \hat{f}(X)]^2 \\ &= \underbrace{[f(X) - \hat{f}(X)]^2}_{\text{Reducible}} + \underbrace{\text{Var}(\epsilon)}_{\text{Irreducible}} \end{aligned}$$

$E(Y - \hat{Y})^2$  = Expected value of the squared difference between the actual and predicted value

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"natural" noise

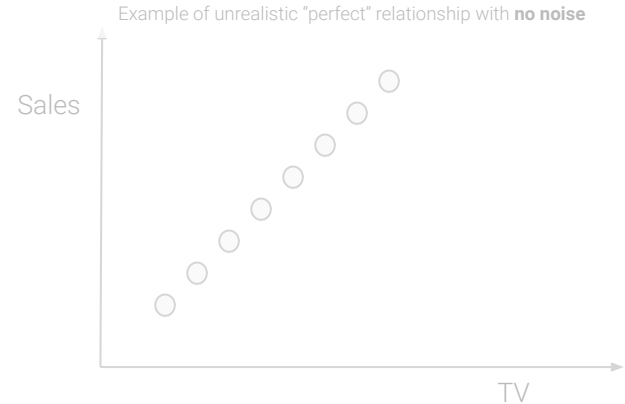


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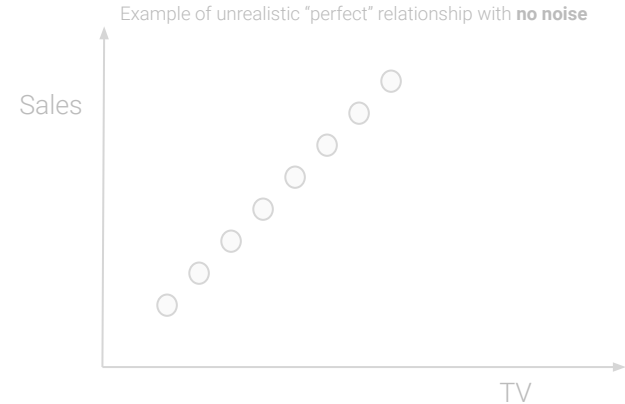


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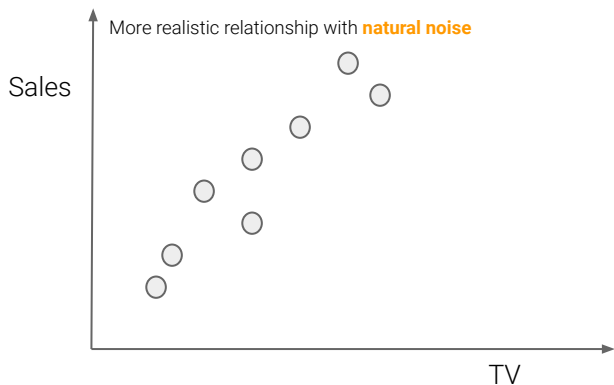
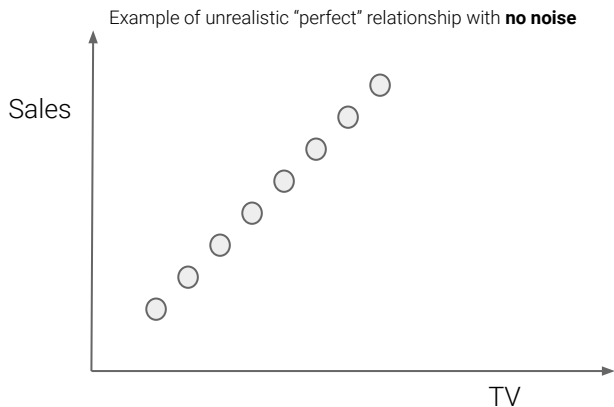


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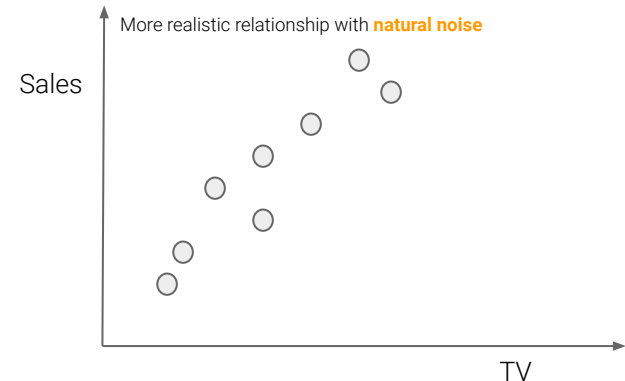
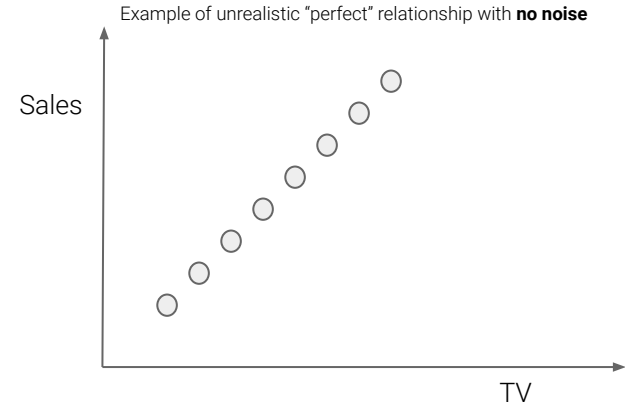


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Statistical learning is not just about **predictions** but also about **inference**

We want to figure out the association between our outcome and input variables.

Typical questions:

- Which predictors are associated with the response?
- What is the relationship between the response and each predictor?
- Can the relationship between  $Y$  and each predictor be adequately summarized using a linear equation, or is the relationship more complicated?



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Goal: identify individuals who are likely to respond positively to a mailing

- **Outcome:** response to the marketing campaign (either positive or negative)
- **Predictors:** demographic variables (age, gender, address,...)
- The company is not interested in obtaining a deep understanding of the relationships between each individual predictor and the response;
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# Difference between statistical learning and machine learning

# Prediction & inference

**Prediction** wants to accurately predict a response using some predictors

## Focus of machine learning

Despite convincing prediction results, the lack of an explicit model can make ML solutions difficult to interpret and directly relate to existing theoretical knowledge.

**Inference** is about understanding the relationship between the response and predictors

## Focus of statistical learning

E.g., compute a quantitative measure of confidence that a discovered relationship describes a 'true' effect that is unlikely to result from noise.

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Points of Significance

# Statistics versus machine learning

Danilo Bzdok, Naomi Altman & Martin Krzywinski

*Nature Methods* **15**, 233–234 (2018) | [Download Citation](#) 

**Statistics draws population inferences from a sample, and machine learning finds generalizable predictive patterns.**

Two major goals in the study of biological systems are inference and prediction. Inference creates a mathematical model of the data-generation process to formalize understanding or test a hypothesis about how the system behaves. Prediction aims at forecasting unobserved outcomes or future behavior, such as whether a mouse with a given gene expression pattern has a disease. Prediction makes it possible to identify best courses of action (e.g., treatment choice) without requiring understanding of the underlying mechanisms. In a typical research project, both inference and prediction can be of value—we want to know how biological processes work and what will happen

# Literature

Bzdok, D., Altman, N., & Krzywinski, M. (2018). Points of Significance: Statistics versus machine learning. *Nature Methods*, 15(4), 233-234. DOI: 10.1038/nmeth.4642

James, G., Witten, D., Hastie, T., & Tibshirani, R. (2021). *Statistical learning*. In *An introduction to statistical learning*. Springer, New York, NY.