

Class CS 147, Sec 01
Homework 1
Due Date Feb 23, 2017 11:59 PM PST

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1. Table 1.1 Result Table

| Code | Binary | Hex | Operation |
|---------------------|---|------------|------------------|
| muli r6, r3, 0x8FA7 | 0011 0100 0110 0110 1000 1111 1010 0111 | 0x34668FA7 | r3 = r6 * 0x8FA7 |
| add r3, r3, r1 | 0000 0000 0110 0001 0001 1000 0010 0000 | 0x611820 | r3 = r3 + r1 |
| nor r2, r3, r5 | 0000 0000 0110 0101 0001 0000 0010 0111 | 0x651027 | r2 = ~(r3 r5) |
| jal 0x34F832 | 0000 1100 0011 0100 1111 1000 0011 0010 | 0xC34F832 | RP = 0x34F832 |

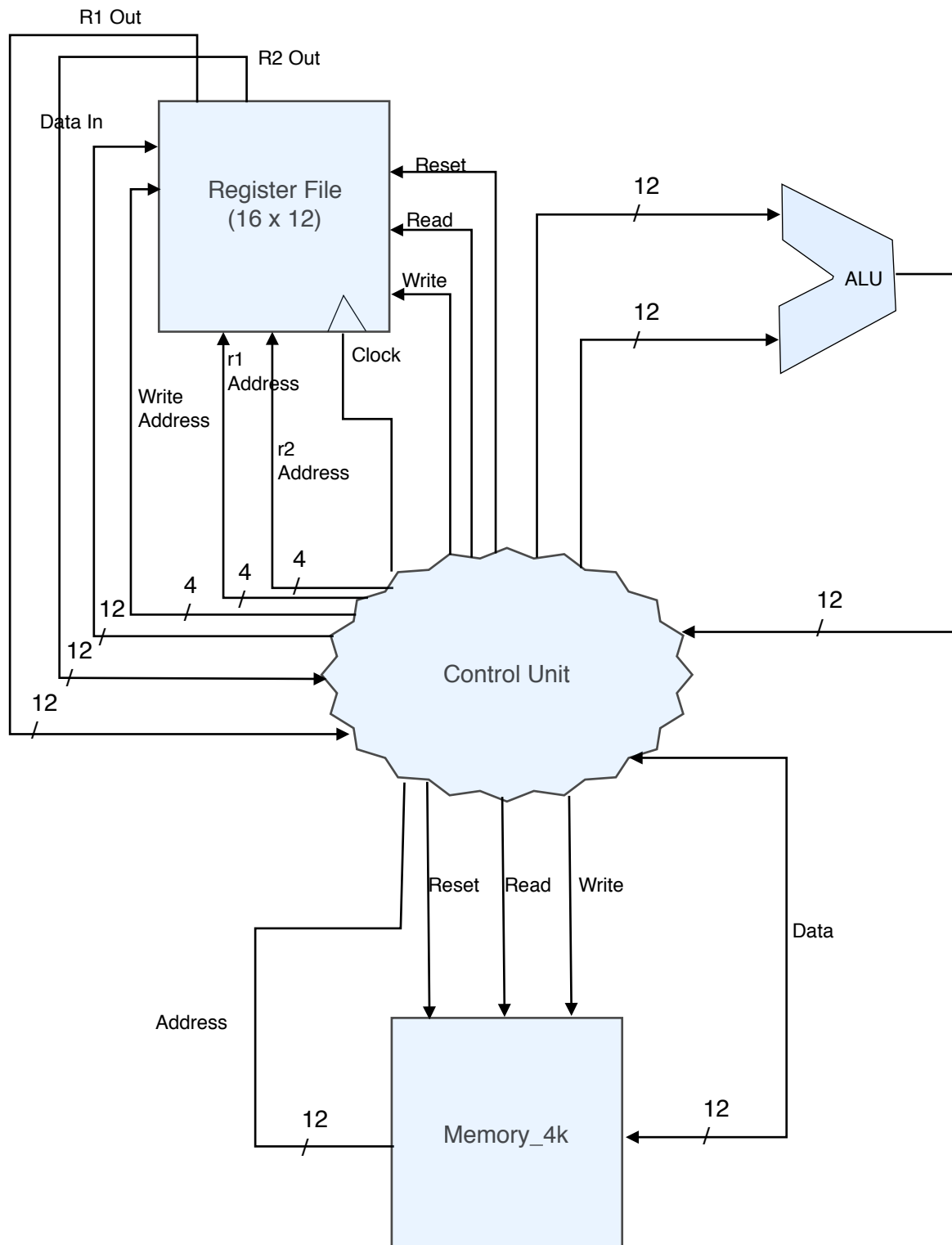
Table 1.2 Calculation Table

| Code | Type | RS | RT | RD | SHAMT | FUNCT | IMM | ADDR |
|---------------------|------|----|----|----|-------|-------|--------|----------|
| muli r6, r3, 0x8FA7 | I | r3 | r6 | | | | 0x8FA7 | |
| add r3, r3, r1 | R | r3 | r1 | r3 | 0000 | 0x20 | | |
| nor r2, r3, r5 | R | r3 | r5 | r2 | 0000 | 0x27 | | |
| jal 0x34F832 | J | | | | | | | 0x34F832 |

2. Table 2.1. Machine Code and execution result table

| Code | Program Address | Content | Data Address | Content |
|---------------------|-----------------|--|--------------|---------|
| addi r0, r0, 0x1008 | 0x0000 1000 | 0010 0000 0000 0000 0001 0000 0000 1000 | 0x01008000 | 21 |
| sll r0, r0, 0xC | 0x0000 1001 | 0000 0000 0000 0000 0000 0010 0100 0001 | 0x01008001 | 23 |
| addi r2, r2, 0x9 | 0x0000 1002 | 0010 0000 0100 0010 0000 0000 0000 1001 | 0x01008002 | 25 |
| LOOP: | | | | |
| beq r1, r2, END | 0x0000 1003 | 0001 0000 0100 0001 0001 0000 0000 1011 | 0x01008003 | 27 |
| lw r3, r0, 0x0 | 0x0000 1004 | 1000 1100 0000 0011 0000 0000 0000 0000 | 0x01008004 | 29 |
| lw r4, r0, 0x1 | 0x0000 1005 | 1000 1100 0000 0100 0000 0000 0000 0001 | 0x01008005 | 31 |
| add r5, r3, r4 | 0x0000 1006 | 0000 0000 0110 0100 00101 0000 0010 0000 | 0x01008006 | 33 |
| sw r5, r0, 0x0 | 0x0000 1007 | 1010 1100 0000 1001 0000 0000 0000 0000 | 0x01008007 | 35 |
| addi r0, r0, 0x1 | 0x0000 1008 | 0010 0000 0000 0000 0000 0000 0000 0001 | 0x01008008 | 37 |
| addi r1, r1, 0x1 | 0x0000 1009 | 0010 0000 1000 0100 0000 0000 0000 0001 | 0x01008009 | 19 |
| jmp LOOP | 0x0000 100A | 0000 1000 0000 0000 0001 0000 0000 0011 | 0x0100800A | |
| END: | | | | |
| sw r5, r0, 0x0 | 0x0000 100B | 1010 1100 0000 1001 0000 0000 0000 0000 | 0x0100800B | |

3. Figure 3.1: Complete processor schematic

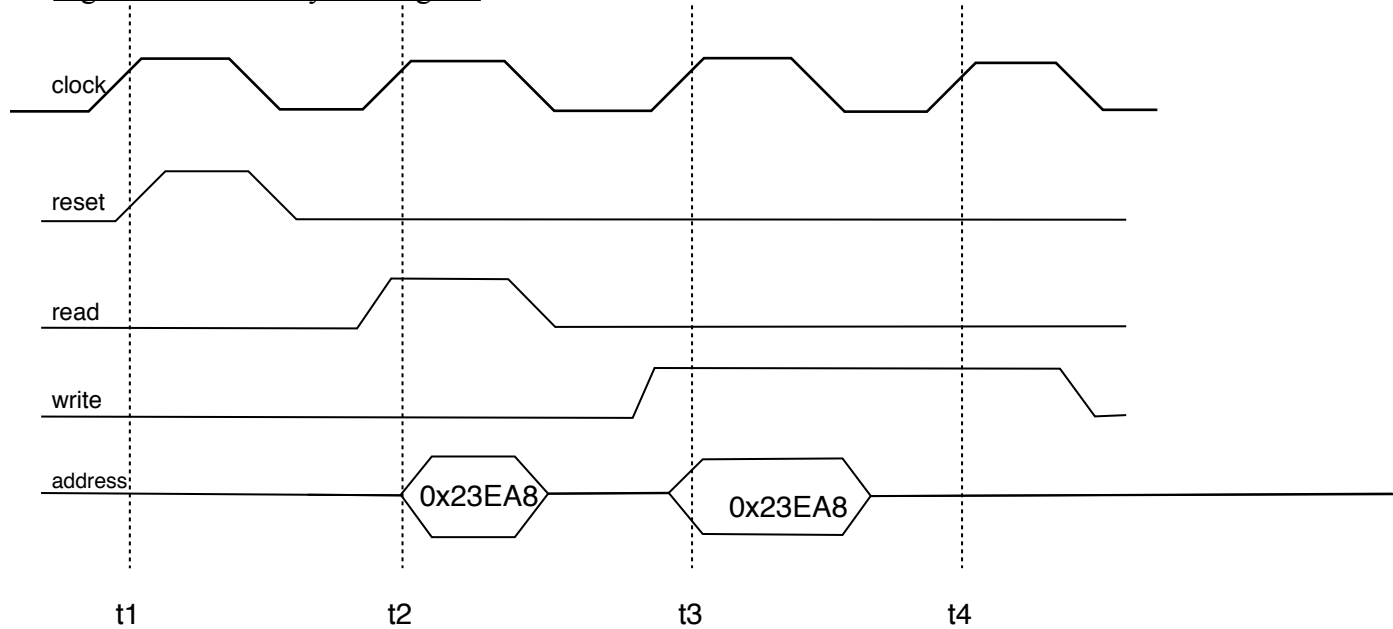


4. Clock Diagram

(a) Time period of the clock is 400ps. $1/(2.5\text{GHz}) * 1000 = \text{ps}$

(b) The clock is at a logic low for 230ps. $400 * .4 = 160 \mid 400 - 160 - 10 = \text{logic low}$

Figure 4.1: Clock Cycle Diagram



5. Table 5.1: Solutions

| Binary | Hex | Octal | Unsigned Decimal | Signed Deciamal |
|-----------|-----|-------|------------------|-----------------|
| 1101 0011 | D3 | 323 | 211 | -45 |
| 1000 1011 | 8B | 213 | 139 | -117 |
| 1010 1111 | AF | 257 | 175 | -81 |
| 1010 1101 | AD | 255 | 173 | -83 |

Table 5.2: Work for Solutions in

| To Hexadecimal | To Binary / Signed Decimal | To Unsigned Decimal | To Octal |
|--|---|--|---|
| $211 \% 16 = 13 \text{ R } 316$ $13 \% 16 = 0 \text{ R } 13 \text{ or D16}$ | $139 \% 2 = 69 \text{ R } 1$ $69 \% 2 = 34 \text{ R } 1$ $34 \% 2 = 17 \text{ R } 0$ $17 \% 2 = 8 \text{ R } 1$ $8 \% 2 = 4 \text{ R } 0$ $4 \% 2 = 2 \text{ R } 0$ $2 \% 2 = 1 \text{ R } 0$ $1 \% 2 = 0 \text{ R } 1$ | $1101\ 00112 = 2^7 * 1 + 2^6 * 1 + 2^5 * 0 + 2^4 * 1 + 2^3 * 0 + 2^2 * 0 + 2^1 * 1 + 2^0 * 1 = 211$ | $175 \% 8 = 21 \text{ R } 7$ $21 \% 8 = 2 \text{ R } 5$ $2 \% 8 = 0 \text{ R } 2$ |
| $139 \% 16 = 8 \text{ R } 11 \text{ or B16}$ $8 \% 16 = 0 \text{ R } 816$ | $175 \% 2 = 87 \text{ R } 1$ $87 \% 2 = 43 \text{ R } 1$ $43 \% 2 = 21 \text{ R } 1$ $21 \% 2 = 10 \text{ R } 1$ $10 \% 2 = 5 \text{ R } 0$ $5 \% 2 = 2 \text{ R } 1$ $2 \% 2 = 1 \text{ R } 0$ $1 \% 2 = 0 \text{ R } 1$ | $2138 = 8^2 * 2 + 8^1 * 1 + 8^0 * 3 = 139$ | $211 \% 8 = 26 \text{ R } 3$ $26 \% 8 = 3 \text{ R } 2$ $3 \% 8 = 0 \text{ R } 3$ |
| Since the unsigned decimal 173 and 175 are two apart using the provided AF from the table and subtracting 216 = AD16 | $-83 \% 2 = -41 \text{ R } 1$ $-41 \% 2 = 20 \text{ R } 1$ $-20 \% 2 = 10 \text{ R } 0$ $-10 \% 2 = 5 \text{ R } 0$ $-5 \% 2 = 2 \text{ R } 1$ $-2 \% 2 = 1 \text{ R } 0$ $-1 \% 2 = 0 \text{ R } 1$ $0101\ 0011 \rightarrow 1010\ 1100 + 1 = 1010\ 11012$ | $AF16 = 16^1 * 10 + 16^0 * 15 = 175$ | $173 \% 8 = 21 \text{ R } 5$ $21 \% 8 = 2 \text{ R } 5$ $2 \% 8 = 0 \text{ R } 2$ |
| | | $-83 = 1010\ 1101_2 = 2^7 * 1 + 2^6 * 0 + 2^5 * 1 + 2^4 * 0 + 2^3 * 1 + 2^2 * 1 + 2^1 * 0 + 2^0 * 1 = 173$ | |

6. Using 2's Complement for binary arithmetic

- (a) $6_{10} / 2 = 3 \text{ R } 0$ $-4_{10} / 2 = -2 \text{ R } 0$
 $3_{10} / 2 = 1 \text{ R } 1$ $-2_{10} / 2 = -1 \text{ R } 0$
 $1_{10} / 2 = 0 \text{ R } 1$ $-1_{10} / 2 = 0 \text{ R } 1$
 $0_{10} / 2 = 0 \text{ R } 0$ $0_{10} / 2 = 0 \text{ R } 0$ *Since negative switch 0s and 1s and add 1
 $6_{10} = 0110_2$ $-4_{10} = 0100 \rightarrow 1011 \rightarrow 1011 + 1 = 1100_2$
- (b) i) Zero Extension: $6_{10} = 0110 \rightarrow 0000\ 0110_2$ $-4_{10} = 1100_2 \rightarrow 0000\ 1100_2$
ii) Sign Extension: $6_{10} = 0110 \rightarrow 0000\ 0110_2$ $-4_{10} = 1100_2 \rightarrow 1111\ 11\ 00_2$

7. Truth Tables for Boolean Functions

(a) $F(x,y,z)=x'y+z$

| x | y | z | x'y | x'y + z |
|---|---|---|-----|---------|
| 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 | 1 |
| 0 | 1 | 0 | 1 | 1 |
| 0 | 1 | 1 | 1 | 1 |
| 1 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 0 | 1 |
| 1 | 1 | 0 | 0 | 0 |
| 1 | 1 | 1 | 0 | 1 |

(b) $F(x, y, z) = (xyz') + (x'y'z)$

| x | y | z | xyz' | x'y'z | (xyz') + (x'y'z) |
|---|---|---|------|-------|------------------|
| 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 | 1 | 1 |
| 0 | 1 | 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 0 | 0 | 0 |
| 1 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 0 | 0 | 0 |
| 1 | 1 | 0 | 1 | 0 | 1 |
| 1 | 1 | 1 | 0 | 0 | 0 |

8. Boolean Algebra Manipulation

(a) $\mathbf{a+b + (ab)' = 1}$

$a + b + a' + b'$ by identity 17 (DeMorgan's)

$a + a' + b + b'$ by identity 10 (Commutative)

$1 + 1$ by identity 7

$= 1$ by identity 3

(b) $\mathbf{w'.(wxyz)' = w'}$

$w'(w'+x'+y'+z')$ by Identity 17 (DeMorgan's)

$w'w' + w'x' + w'y' + w'z'$ by Identity 14 (Distributive)

$w' + w'x' + w'y' + w'z'$ by Identity 7

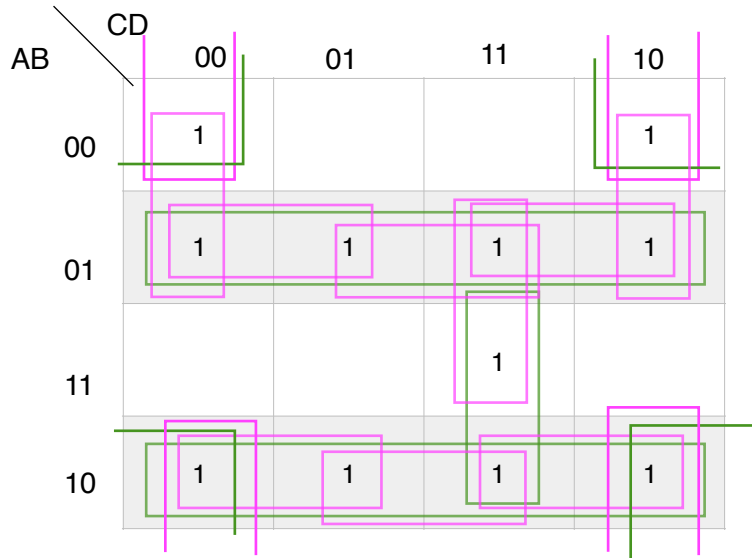
$w'(1 + (x'y'z'))$ by Identity 14 (Distributive)

$w'(1)$ by Identity 3

$= w'$ by Identity 2

9. K-Mapping Technique

(a) $f(A,B,C,D) = \Pi M(1,3,12,13) = \sum m(0, 2, 4, 5, 6, 7, 8, 9, 10, 11, 14, 15)$
 $= B'D' + A'B + AB' + ACD$

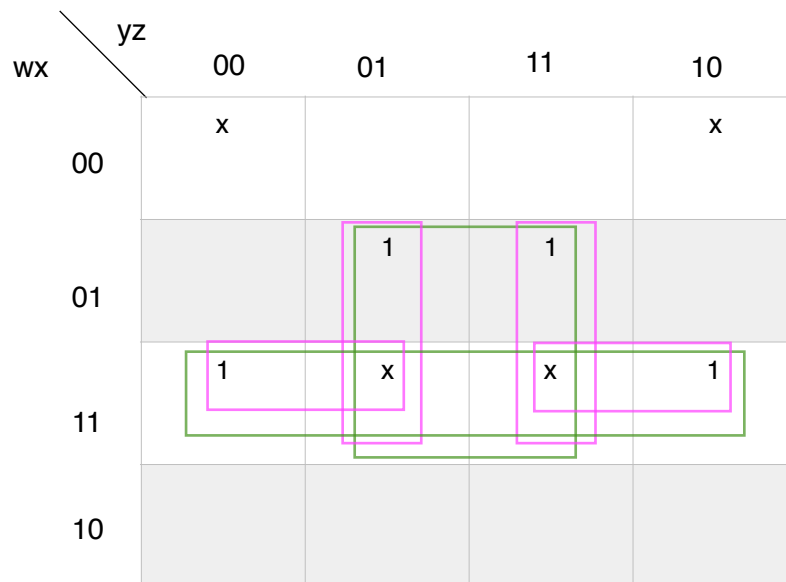


Essential Prime Implicants



Non-Essential Prime Implicants

(b) $f(w, x, y, z) = \sum m(5, 7, 12, 14) + d(0, 2, 13, 15) = xz + wx$



Essential Prime Implicants



Non-Essential Prime Implicants

10. Digital Circuit

| Unsigned Decimal | Signed Decimal | W | X | Y | Z | Output M |
|---------------------|-------------------|---|---|---|---|----------|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 1 | 0 | 0 | 0 | 1 | 1 |
| 2 | 2 | 0 | 0 | 1 | 0 | 1 |
| 3 | 3 | 0 | 0 | 1 | 1 | 1 |
| 4 | 4 | 0 | 1 | 0 | 0 | 1 |
| 5 | 5 | 0 | 1 | 0 | 1 | 1 |
| 6 | 6 | 0 | 1 | 1 | 0 | 1 |
| 7 | 7 | 0 | 1 | 1 | 1 | 1 |
| 8 | | 1 | 0 | 0 | 0 | 0 |
| 9 | -7 | 1 | 0 | 0 | 1 | 1 |
| 10 | -6 | 1 | 0 | 1 | 0 | 1 |
| 11 | -5 | 1 | 0 | 1 | 1 | 1 |
| 12 | -4 | 1 | 1 | 0 | 0 | 1 |
| 13 | -3 | 1 | 1 | 0 | 1 | 1 |
| 14 | -2 | 1 | 1 | 1 | 0 | 1 |
| 15 | -1 | 1 | 1 | 1 | 1 | 1 |

| wx \ yz | 00 | 01 | 11 | 10 |
|---------|----|----|----|----|
| 00 | | 1 | 1 | 1 |
| 01 | 1 | 1 | 1 | 1 |
| 11 | 1 | 1 | 1 | 1 |
| 10 | | 1 | 1 | 1 |

$$F(W,X,Y,Z) = \sum m(1,2,3,4,5,6,7,9,10,11,12,13,14,15)$$

$$\rightarrow X + Y + Y'Z$$

$$\mathbf{M = X + Y + Y'Z}$$

W

