

Sequential ATPG

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Course Roadmap (EDA Topics)

Logic Sim.

Fault Collapsing

Fault Simulation

Testability

Comb. ATPG

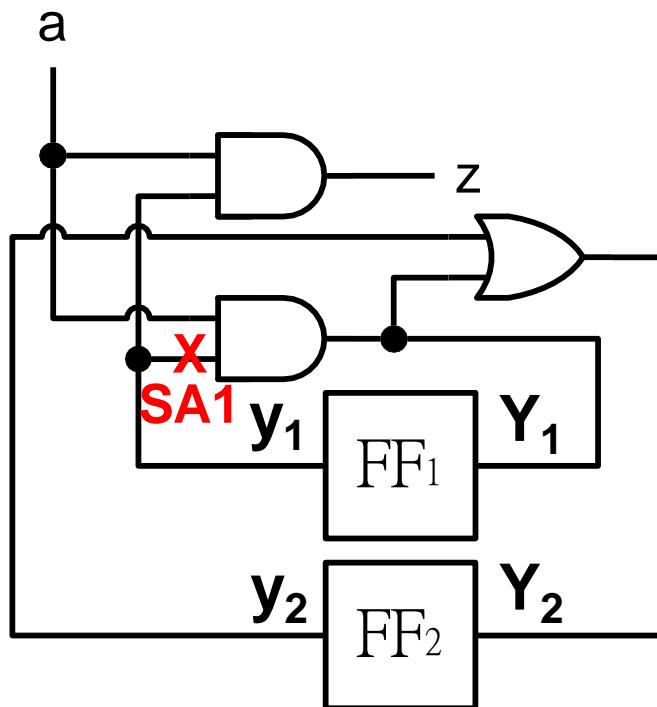
Diagnosis

Seq. ATPG

Delay Test

Motivating Problem

- You already know ATPG for combinational circuits
- But if is required to generate a test for sequential circuits
 - ◆ No scan allowed in flip-flops (FF)



Why Am I Learning This?

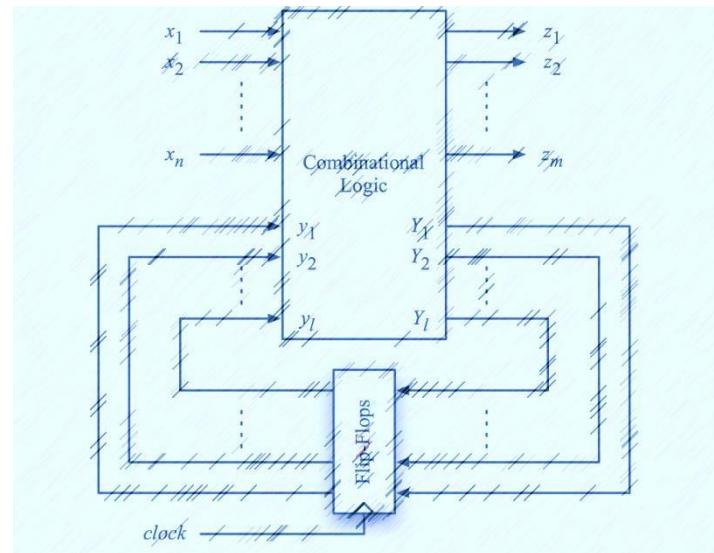
- **Sequential ATPG**
 - ◆ Generate test patterns for sequential circuits
 - ◆ Without DFT or scan

Test Generation

Fault Models	Combinational Circuits (or Sequential ckt. with scan)	Sequential Circuits
No fault model	PET	Checking experiment
Single Stuck-at Fault Model	D PODEM FAN	Extended D 9-valued
Delay Fault Model	Path Delay Transition Delay Fault	Launch on Capture Launch on Shift

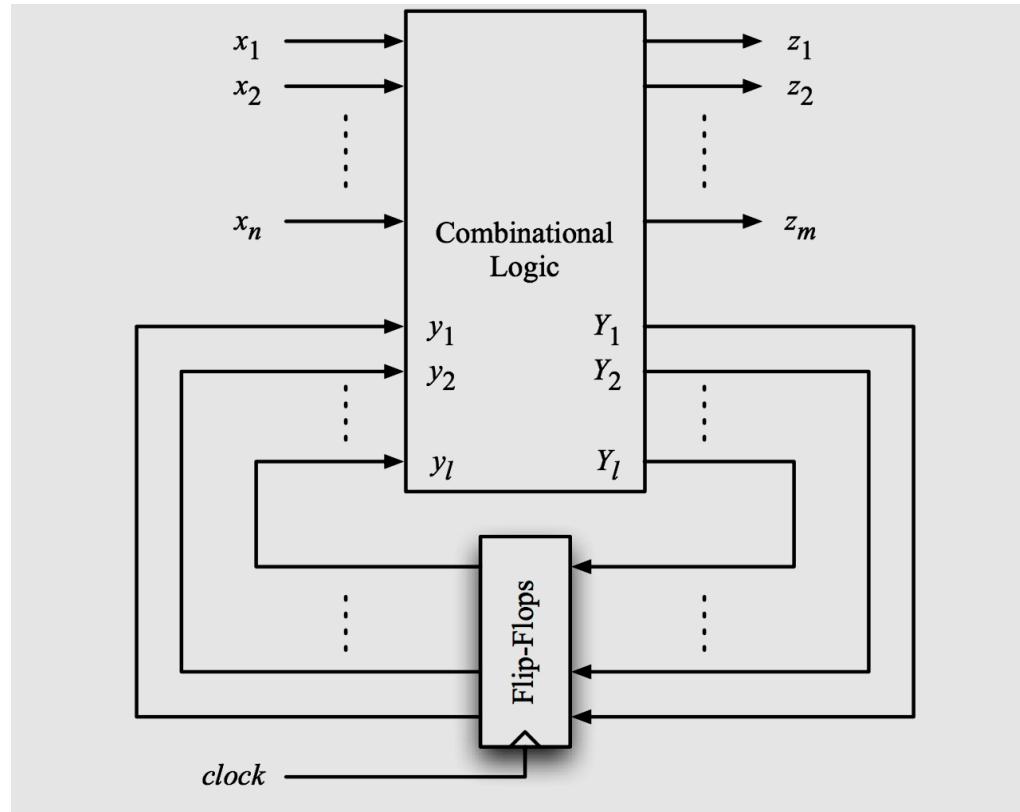
Sequential ATPG

- **Introduction**
- **Time-frame expansion methods**
- **Simulation-based methods**
- **Issues of Sequential ATPG**
- **Conclusions**



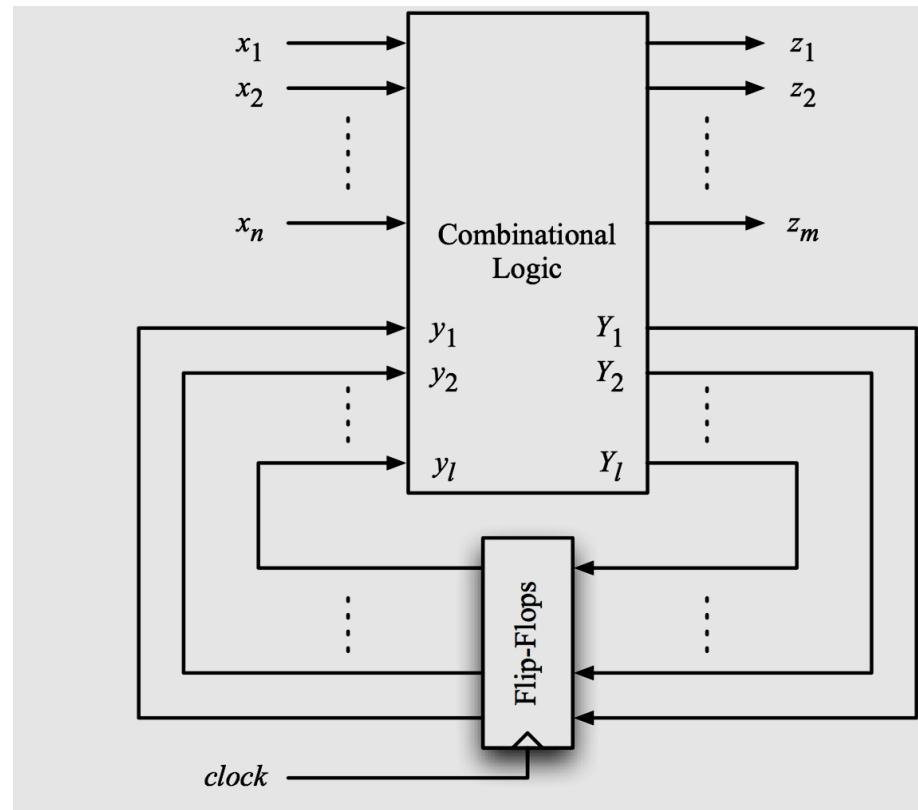
Huffman Model for Sequential Ckt. [Huffman 53]

- x_i = primary inputs (PI)
- z_i = primary outputs (PO)
- y_i = FF (or latch) current states
- Y_i = FF (or latch) next states



Sequential ATPG Assumptions

- **NO SCAN ALLOWED!**
 - ◆ Control only PI
 - FF not controllable
 - ◆ Observe only PO
 - FF not observable
- **Faults in CL only**
 - ◆ NO fault in FF/latches



Challenges of Sequential ATPG

- 1. FF/latches states uncontrollable and unobservable
 - ◆ FF/latch unknown initial states
- 2. Long run time
 - ◆ Comb. ATPG complexity (for a given fault)
 - $O(2^{\text{number_of_PI}})$
 - ◆ Seq. ATPG complexity (for a given fault)
 - $O(2^{\text{number_of_PI}} \times 9^{\text{number_of_FF}})$
- 3. Large memory space required
 - ◆ Time frame expansion
- 4. Low fault coverage
 - ◆ Much worse than Comb. ATPG

*9-valued logic will be covered soon

Seq. ATPG is More Difficult Than Comb. ATPG

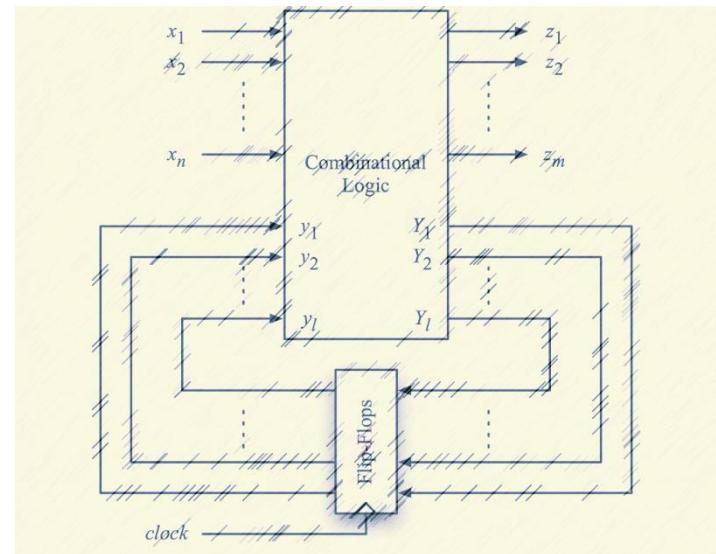
Quiz

Q: For a sequential circuit with 100 flip-flops, what is worst case sequential ATPG complexity?

- A: 9^{100}
- B: 2^{100}
- C: 100^2

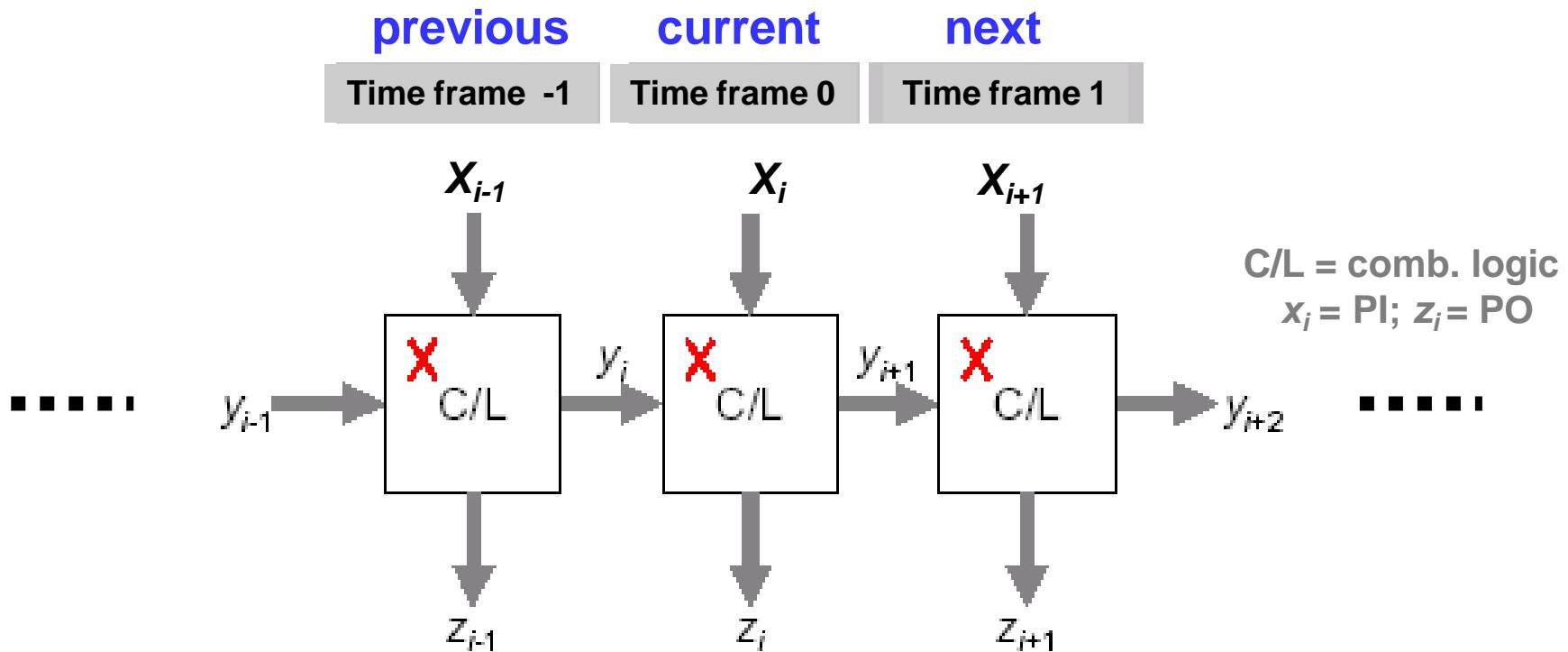
Sequential ATPG

- Introduction
- Time-frame expansion methods
 - ◆ The extended D-algorithm [Kubo 68]
 - ◆ 9-valued D algorithm [Muth 76]
 - ◆ EBT [Marlett 78], BACK [Cheng 88] *
 - ◆ Summary
- Simulation-based methods*
- Issues of Sequential ATPG*
- Conclusions



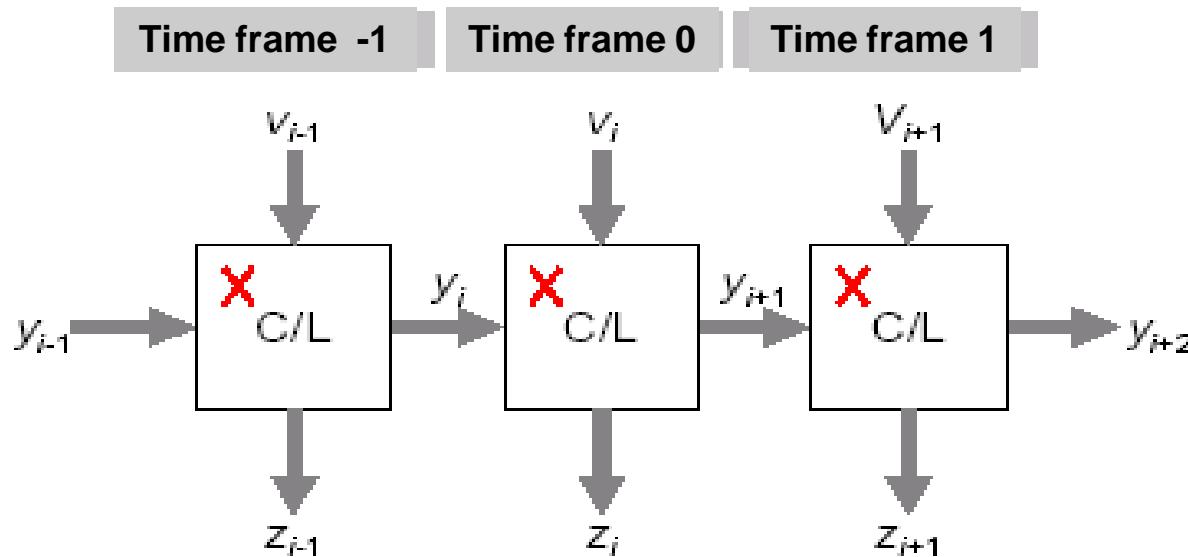
Time Frame Expansion

- IDEA: Replicate circuits and connect time frames **by wires**
 - ◆ y_i = “states”; **No FF!**
 - ◆ Replace **clock cycles** by **space**
- Becomes **combinational ATPG** problem
 - ◆ NOTE: Target fault appears in every time frame



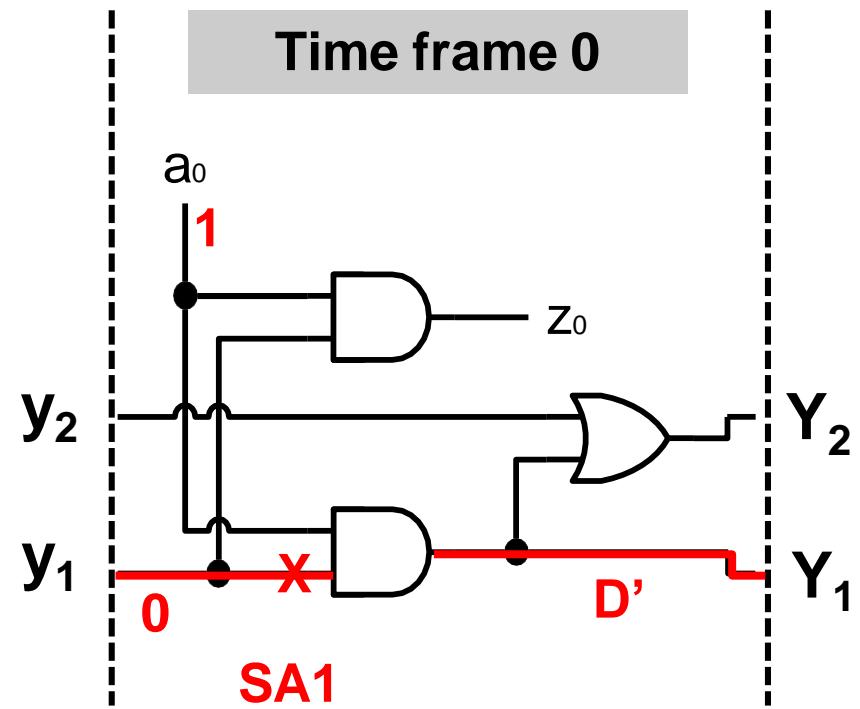
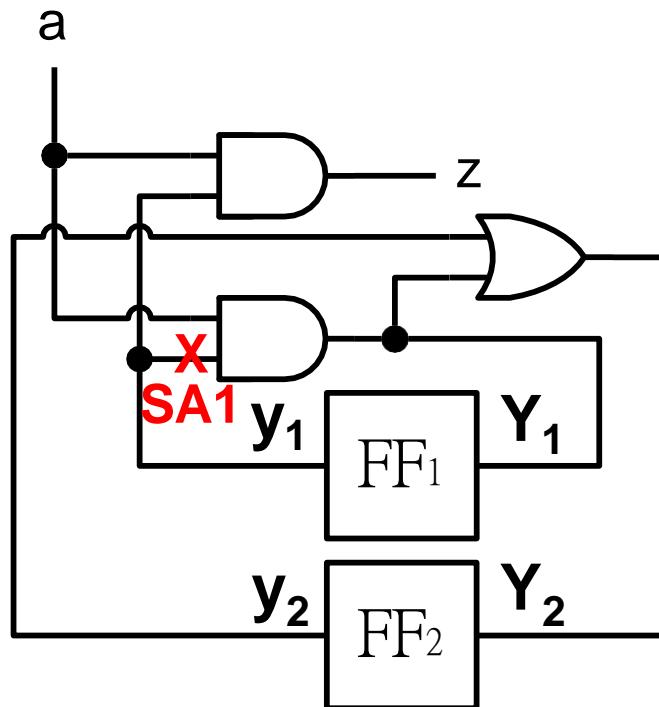
Extended D-Algorithm [Kubo 68]

1. Select a target fault f
2. Create a copy of the combinational logic, set it to time frame 0
3. Generate a test for f for time frame 0 using D-algorithm
4. If the fault effect is propagated to the FF's, continue fault effect *propagation* in the *next time frame*
5. If there are values required in the FF outputs, continue the *justification* in the *previous time frame*



Example (1)

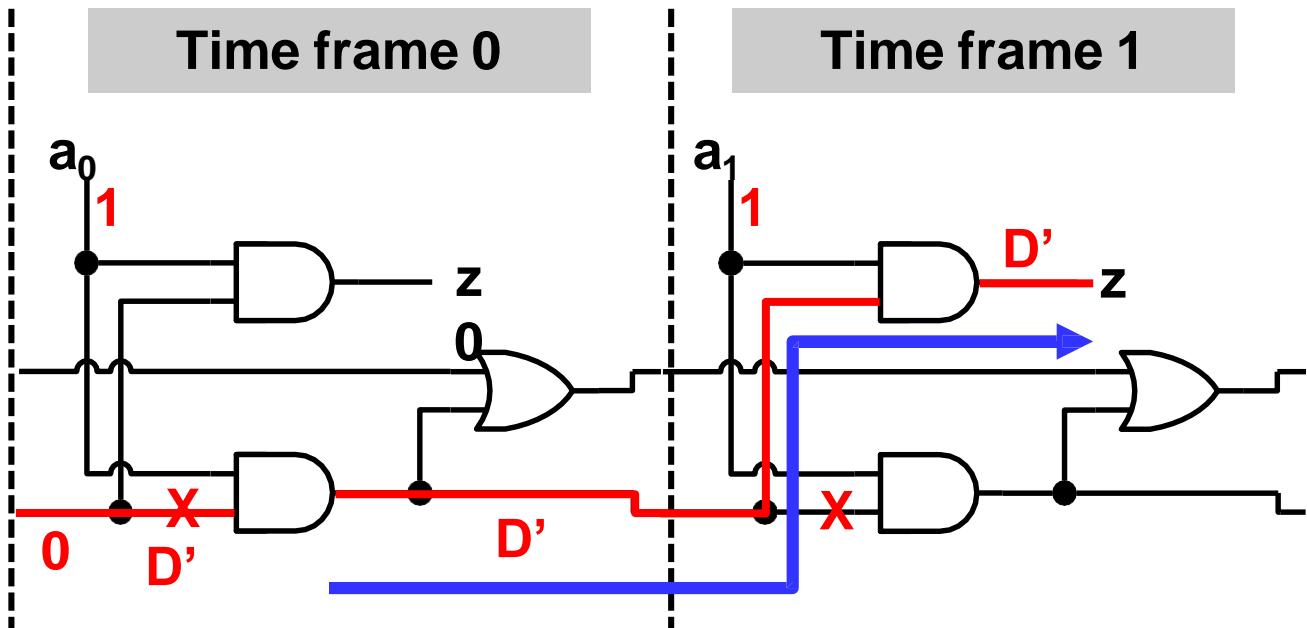
- STEP 2: create Time frame 0
- STEP 3: generate a test
 - ◆ $a_0=1; y_1=0 ; Y_1=D'$



Still Need Propagation

Example (2)

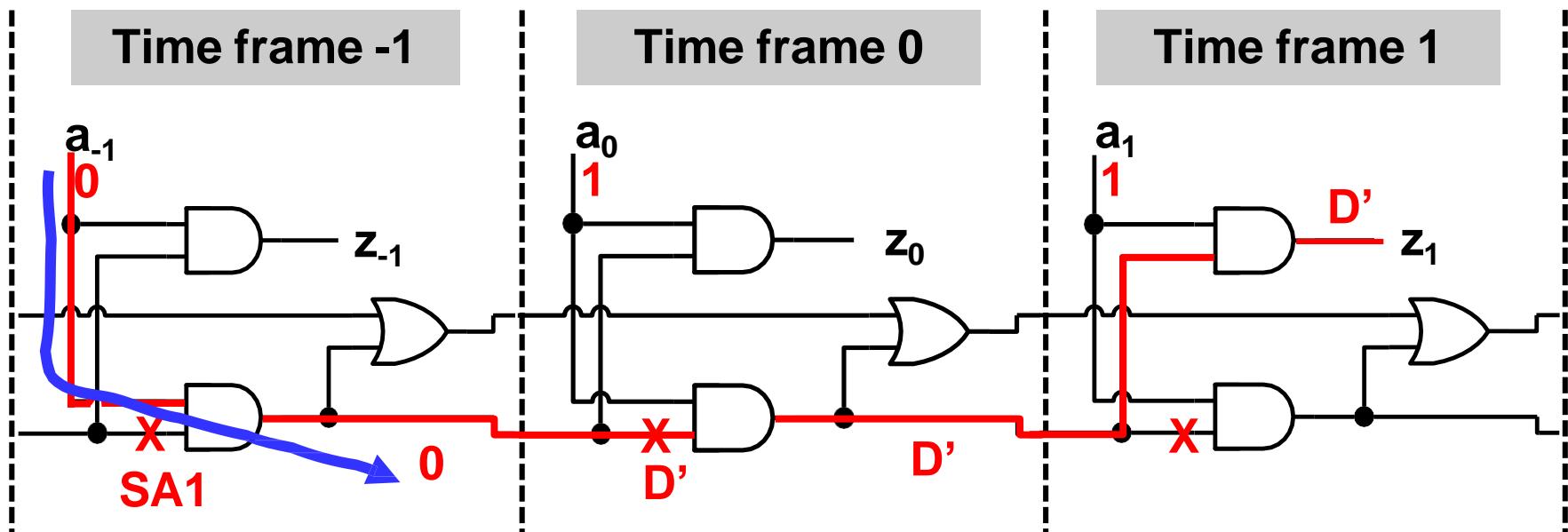
- STEP4: Fault effect propagation to time frame 1
 - ◆ $a_1=1$



Still Need Activation

Example (3)

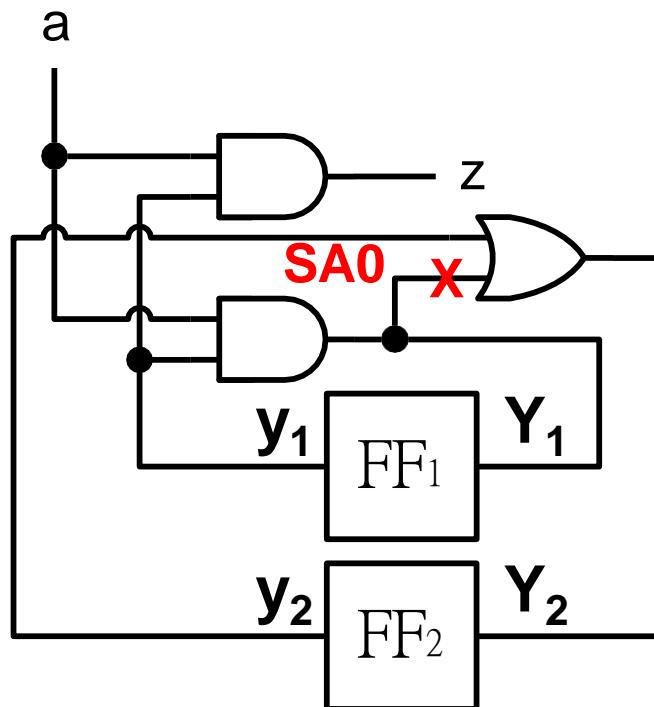
- STEP 5: Fault activation back to time frame -1
 - $a_{-1}=0$



Test Generated = 0, 1, 1

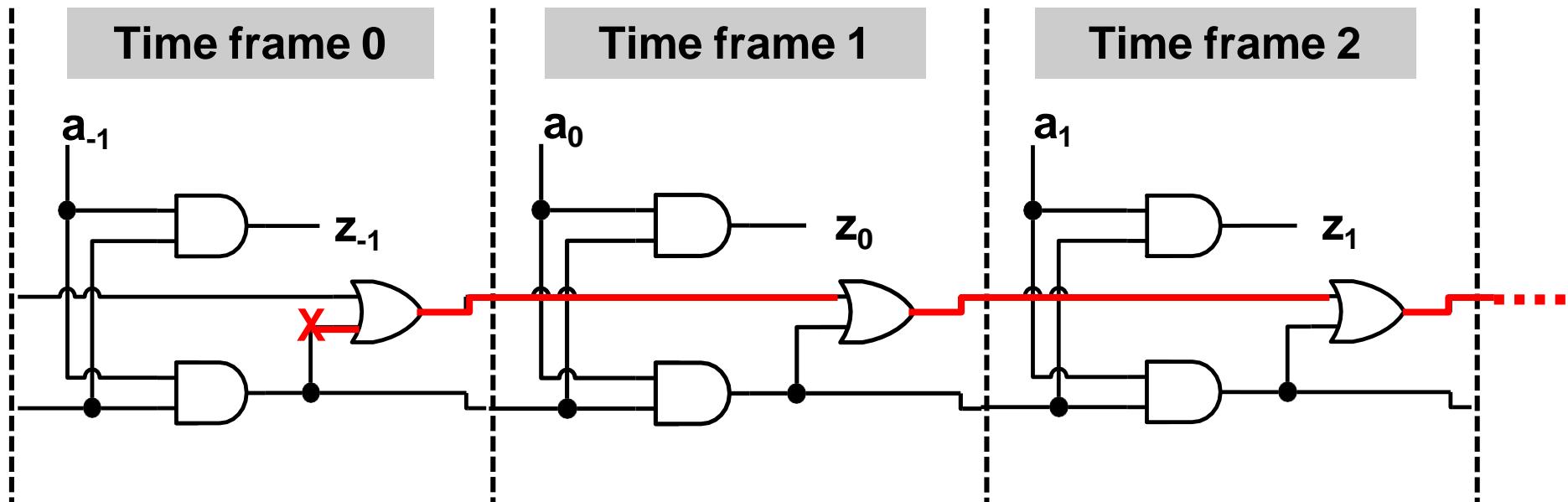
Quiz

Q: Generate a test for stuck-at zero fault in sequential circuit.



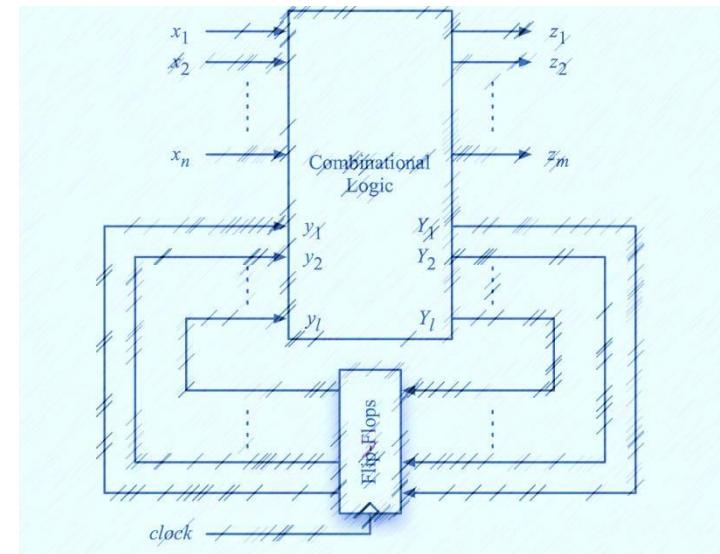
ANS

- No way to propagate
 - ◆ This fault is *untestable* by sequential ATPG
- Endless timeframe expansion ...
 - ◆ Memory explosion!



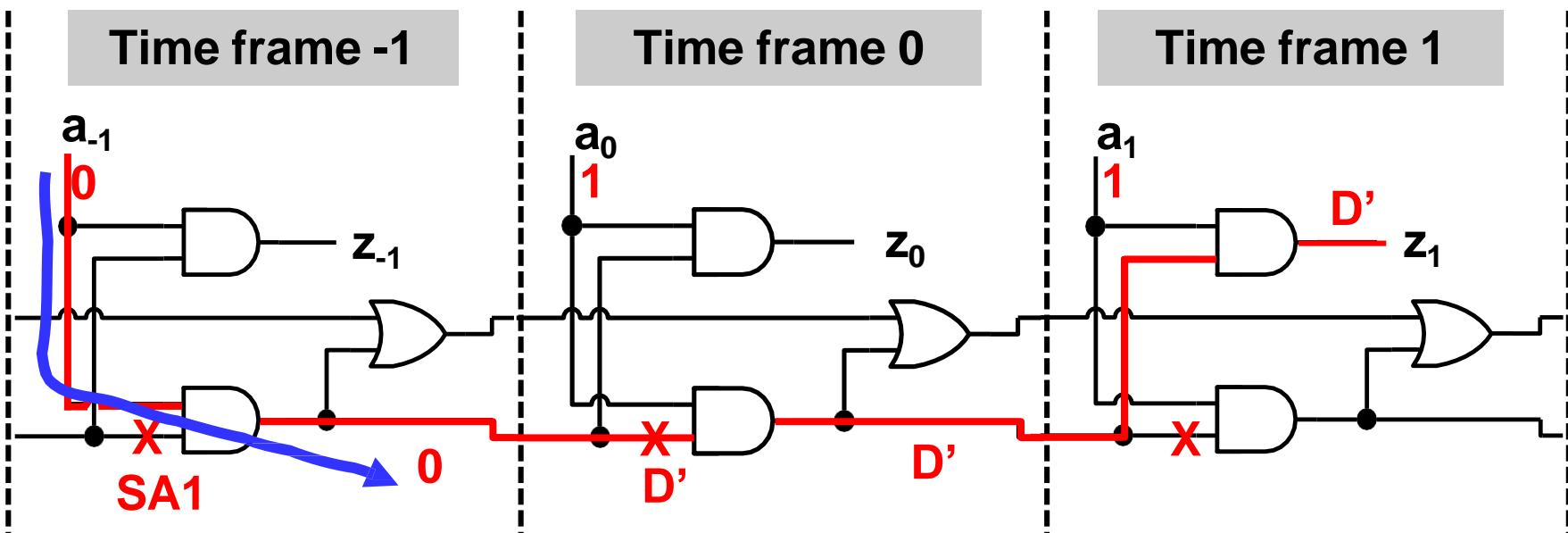
Summary

- Sequential ATPG
 - ◆ Time and space consuming
 - ◆ Low fault coverage
- Time-frame expansion methods - extended D-algorithm
 - ◆ Replicate circuits into many time frames
 - ◆ Propagate forward, then activated backward
 - ◆ create new time frame if needed



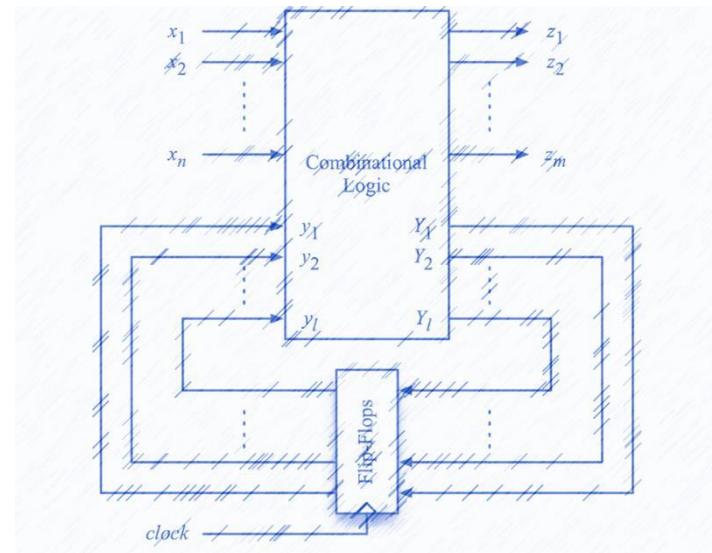
FFT

- In comb. ATPG, first fault activation, then propagation
- In seq. ATPG, first propagation, then activation
 - ◆ why?



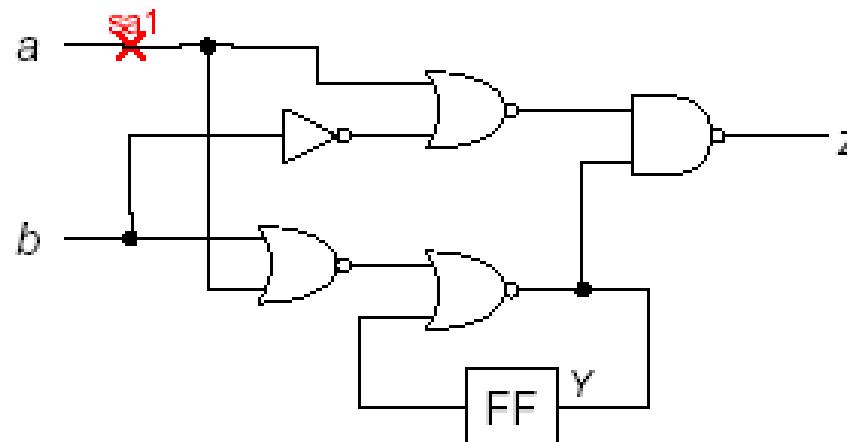
Sequential ATPG

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 - ◆ The Extended D-algorithm [Kubo 68]
 - ◆ 9-valued D algorithm [Muth 76]
 - ◆ EBT [Marlett 78], BACK [Cheng 88] *
 - ◆ Summary
- Simulation-based methods*
- Issues of Sequential ATPG*
- Conclusions



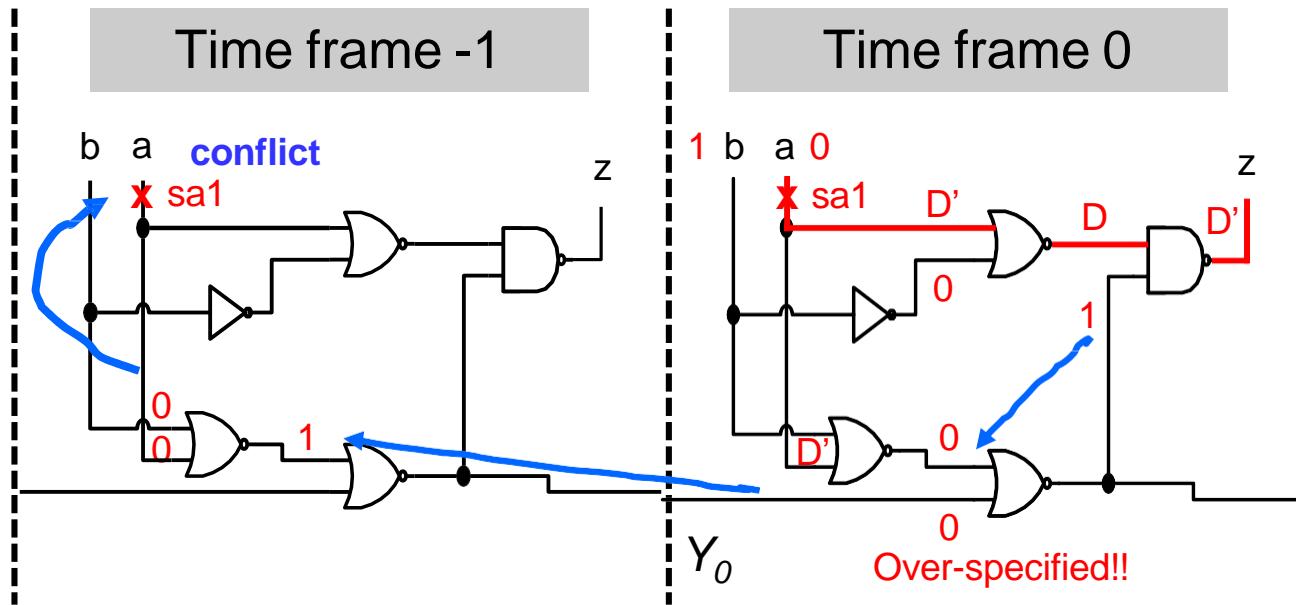
Quiz

Q: Given this test, can we detect the fault?
ANS:



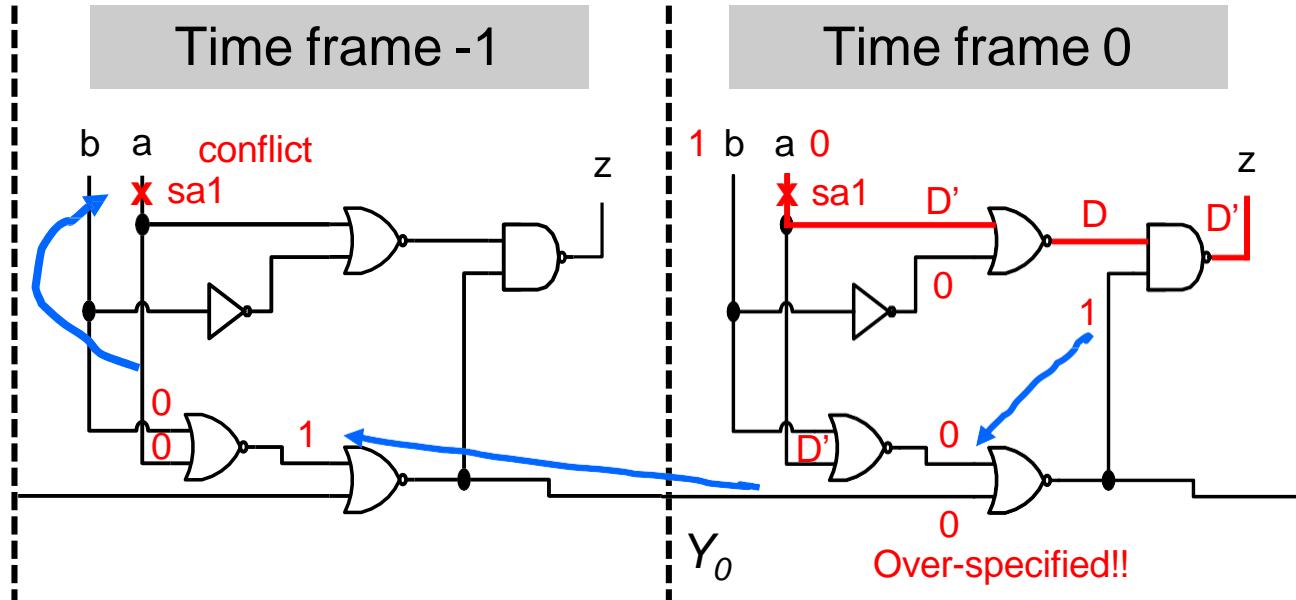
	a	b
v_1	0	0
v_2	0	1

Extended D-algorithm Fails!



- Extended- D algorithm fails due to a conflict
 - ◆ Requires $a=0$ in time frame -1, but SA1
 - ◆ Actually, Y_0 is **over-specified** in 5-valued logic

Why Fails?



- Traditional 5-valued logic (0/0, 1/1, x/x, 0/1, 1/0) is **NOT sufficient**
 - ◆ cannot express 1/x, 0/x, x/0, x/1

Q: How many total cases do we need?

ANS:

Nine-valued D-algorithm [Muth 76]

- Solution: use **9-valued logic**, instead of 5-valued logic

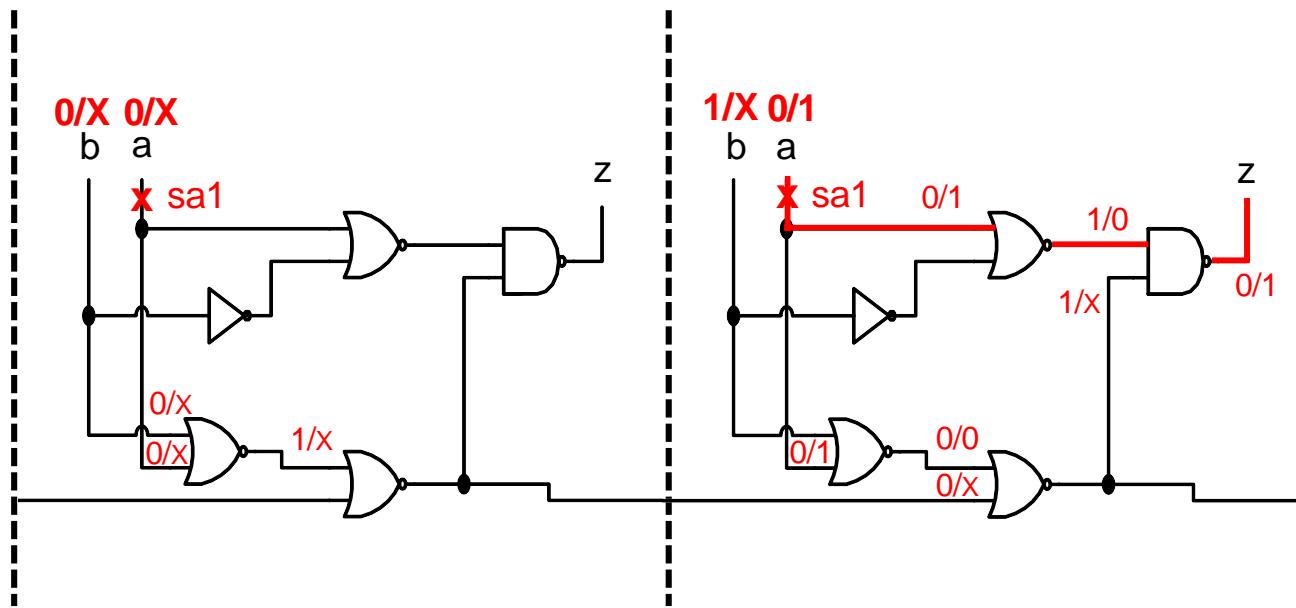
Symbol	Meaning	Roth's 5-valued logic		Muth's 9 valued logic	
		Fault-free	faulty	Fault-free	faulty
D	(1/0)	1	0	1	0
D'	(0/1)	0	1	0	1
0	(0/0)	0	0	0	0
1	(1/1)	1	1	1	1
X	(x/x)	X	X	X	X
G0	(0/x)	-	-	0	X
G1	(1/x)	-	-	1	X
F0	(x/0)	-	-	X	0
F1	(x/1)	-	-	X	1

Nine-valued Truth Table

- Example of AND gate

AND	0	0/x	D'	x/0	x/x	x/1	D	1/x	1
0	0	0	0	0	0	0	0	0	0
0/x	0	0/x	0/x	0	0/x	0/x	0	0/x	0/x
D'	0	0/x	D'	0	0/x	D'	0	0/x	D'
x/0	0	0	0	x/0	x/0	x/0	x/0	x/0	x/0
x/x	0	0/x	0/x	x/0	x/x	x/x	x/0	x/x	x/x
x/1	0	0/x	D'	x/0	x/x	x/1	x/0	x/x	x/1
D	0	0	0	x/0	x/0	x/0	D	D	D
1/x	0	0/x	0/x	x/0	x/x	x/x	D	1/x	1/x
1	0	0/x	D'	x/0	x/x	x/1	D	1/x	1

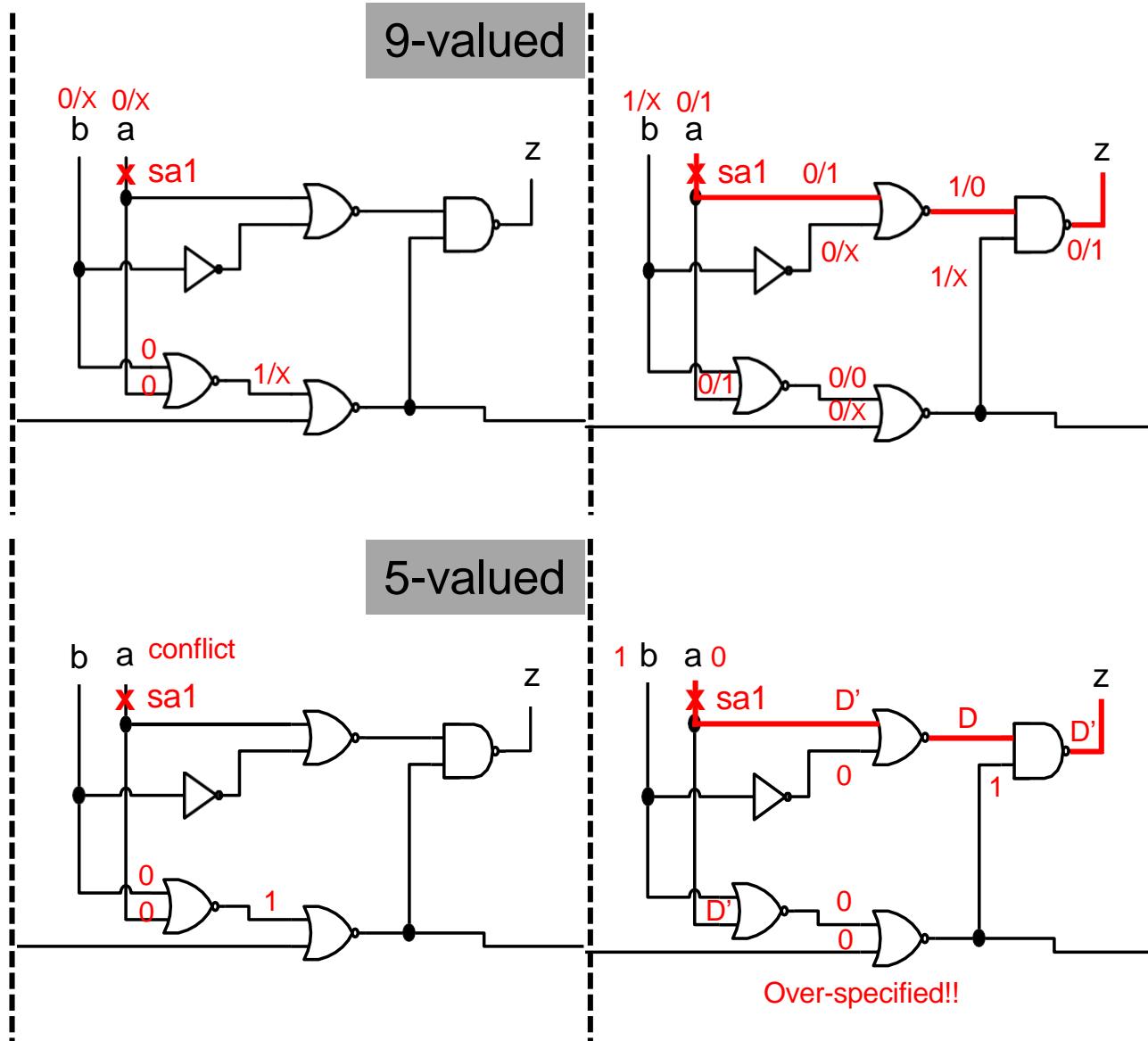
Nine-Valued Test Generation



Test pattern successfully generated

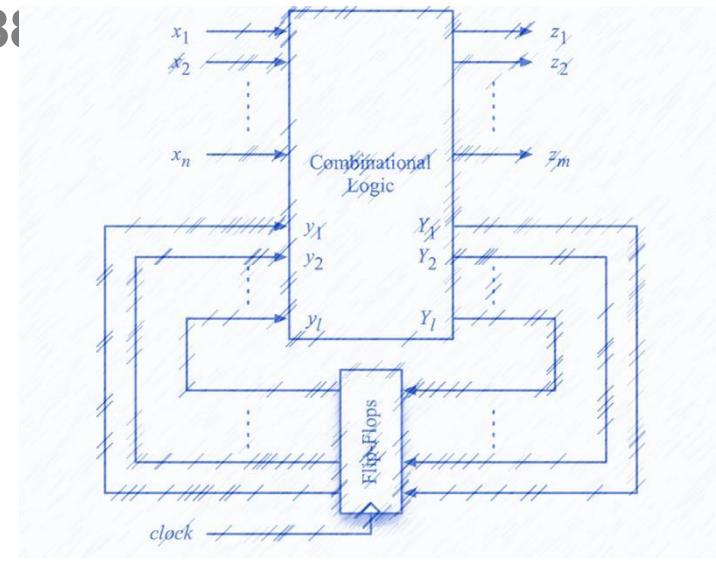
	a	b
v_1	0	0
v_2	0	1

Comparison: 9 v.s. 5 valued



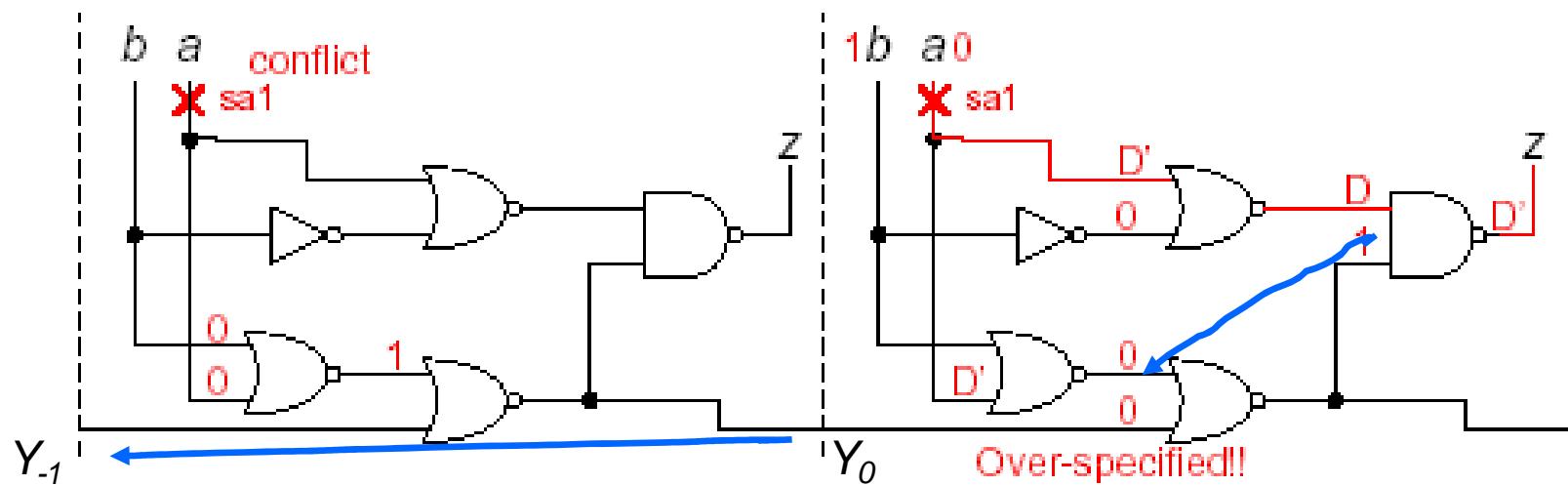
Sequential ATPG

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 - ◆ The Extended D-algorithm [Kubo 68]
 - ◆ 9-valued D algorithm [Muth 76]
 - express **all nine** possible logic states
 - avoid **over-specification**
 - ◆ EBT [Marlett 78], BACK [Cheng 88]
 - ◆ Summary
- Simulation-based methods*
- Issues of Sequential ATPG*
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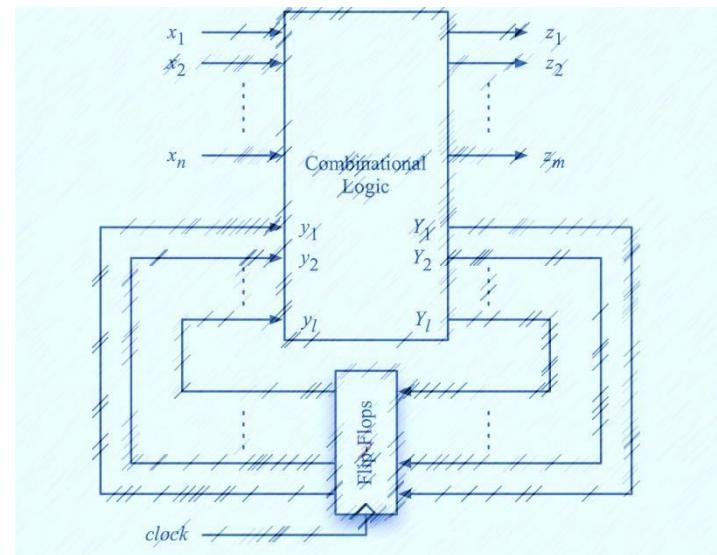
FFT

- Q1: Why NOT consider $1/x$, $0/x$, $x/0$, $x/1$ in combinational ATPG?
- Q2: Why NOT backtrace Y_{-1} one more time frame to the left?



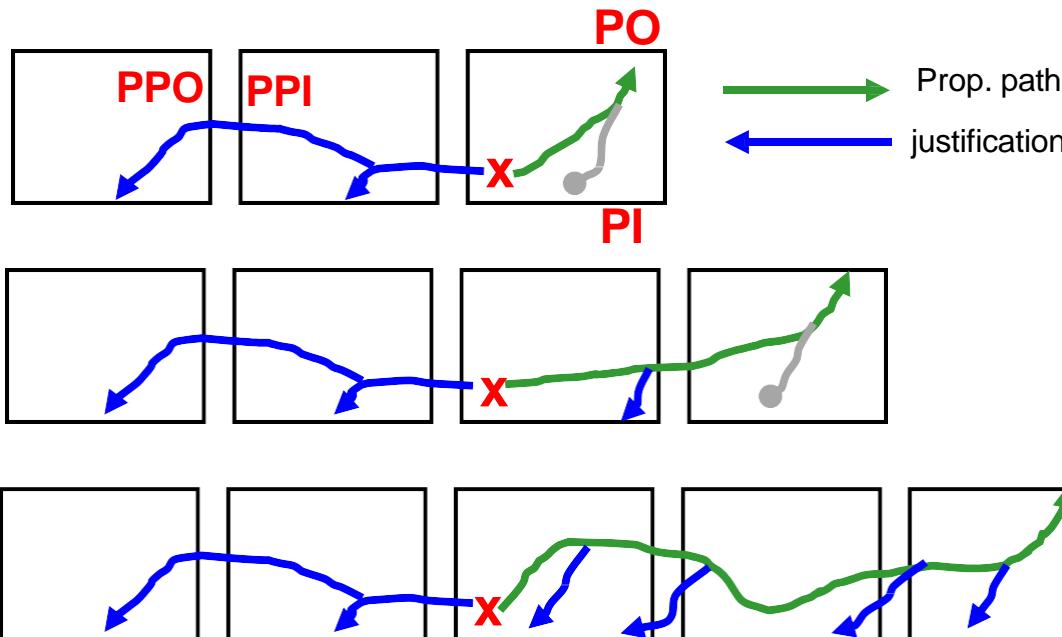
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Problems of Ext. D-Algorithm

- **Mixed Forward and Backward Time Frame Processing**
 - ◆ Reuse existing D-algorithm
 - both **forward** fault propagation and **backward** justification
 - ◆ How many time frames ?
 - Memory requirement **hard to predict**



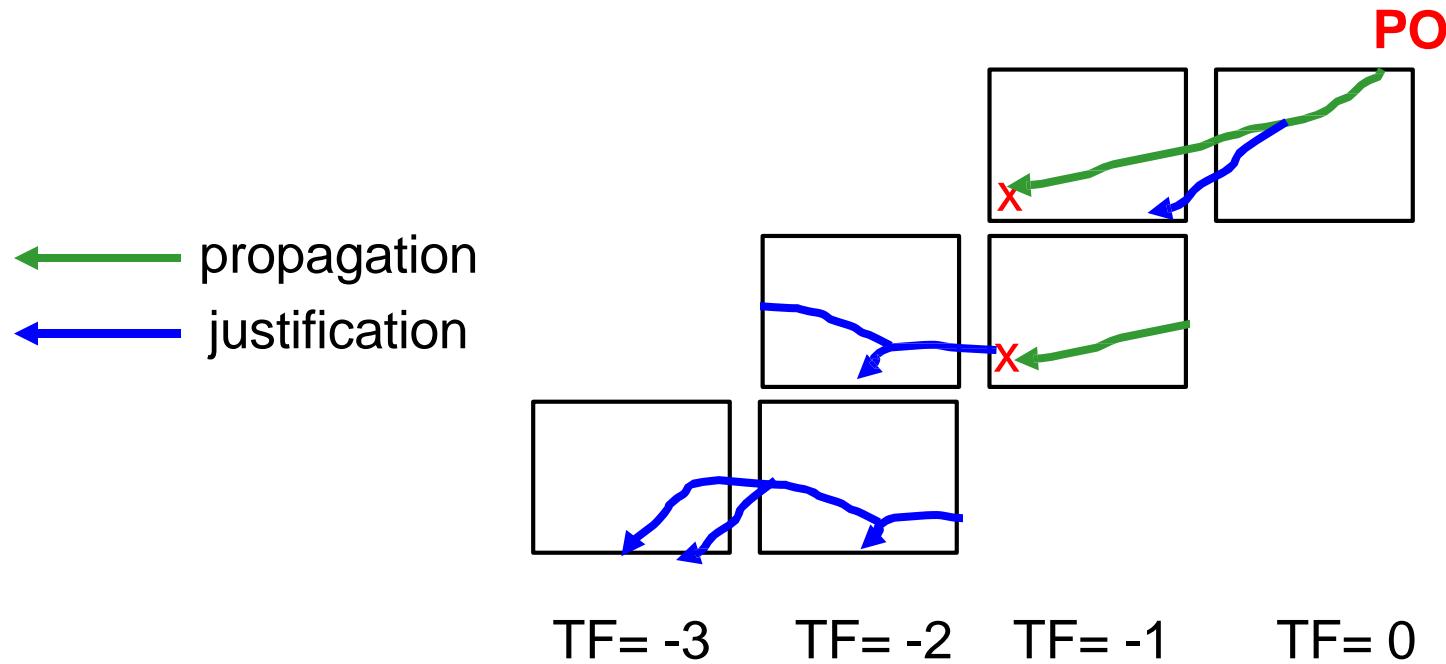
Justification fails,
Backtrack!

Justification fails,
Backtrack!

Test generated

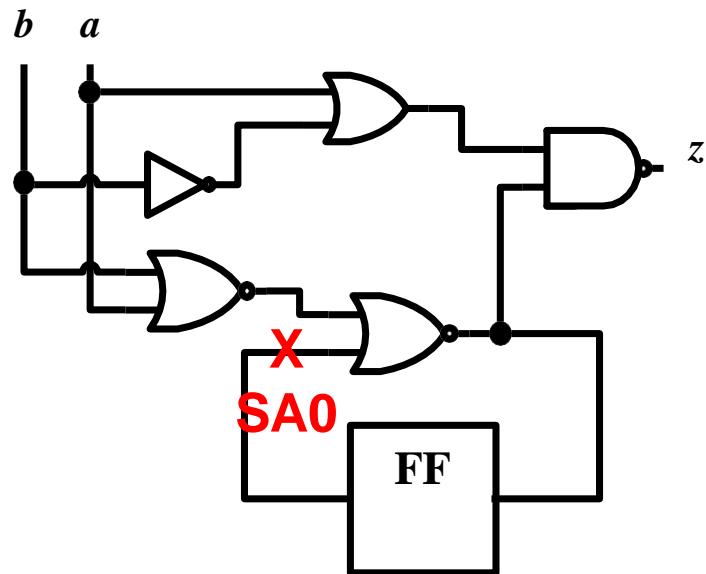
Extended Backtrace (EBT) [Marlett 78]

- **Backward Time Frame Processing Only**
 - ◆ 1. Select a **path** from fault site to PO
 - ◆ 2. **Sensitize path backwards** from the PO
 - ◆ 3. **Justify required values backward**
 - If justification fails, choose another path
- Advantage: only two time frames needed

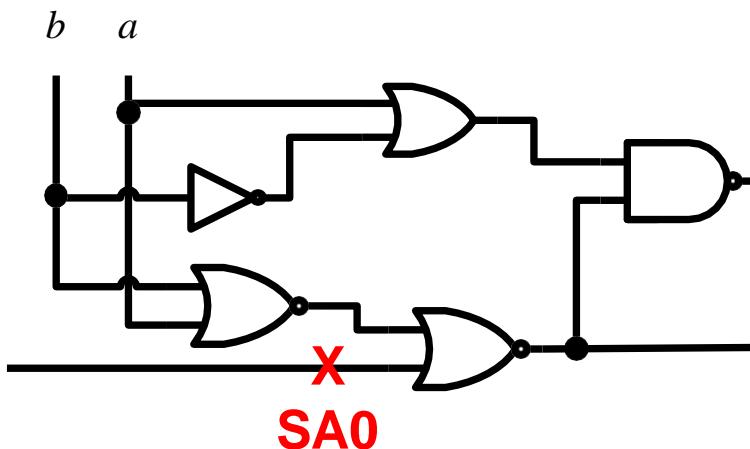


EBT Example

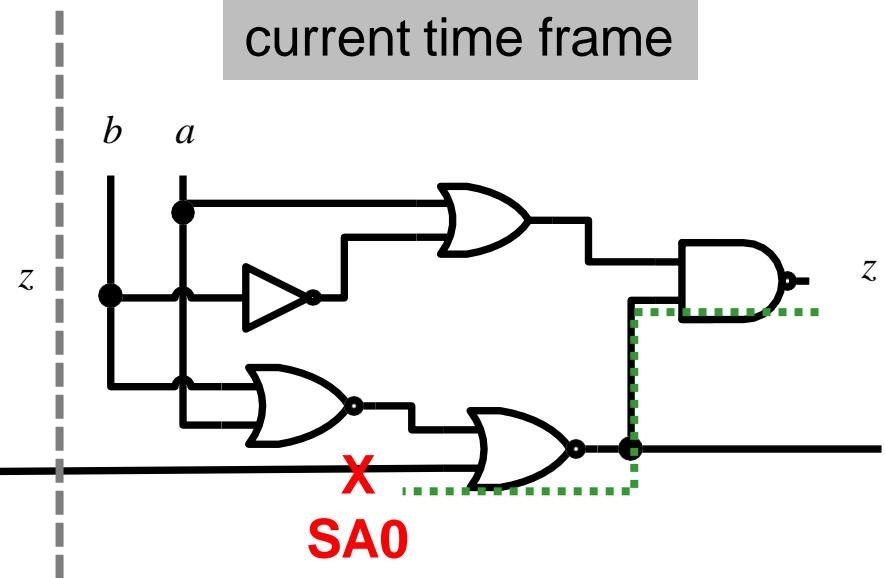
- 1. Create two time frames
- 2. Choose a path

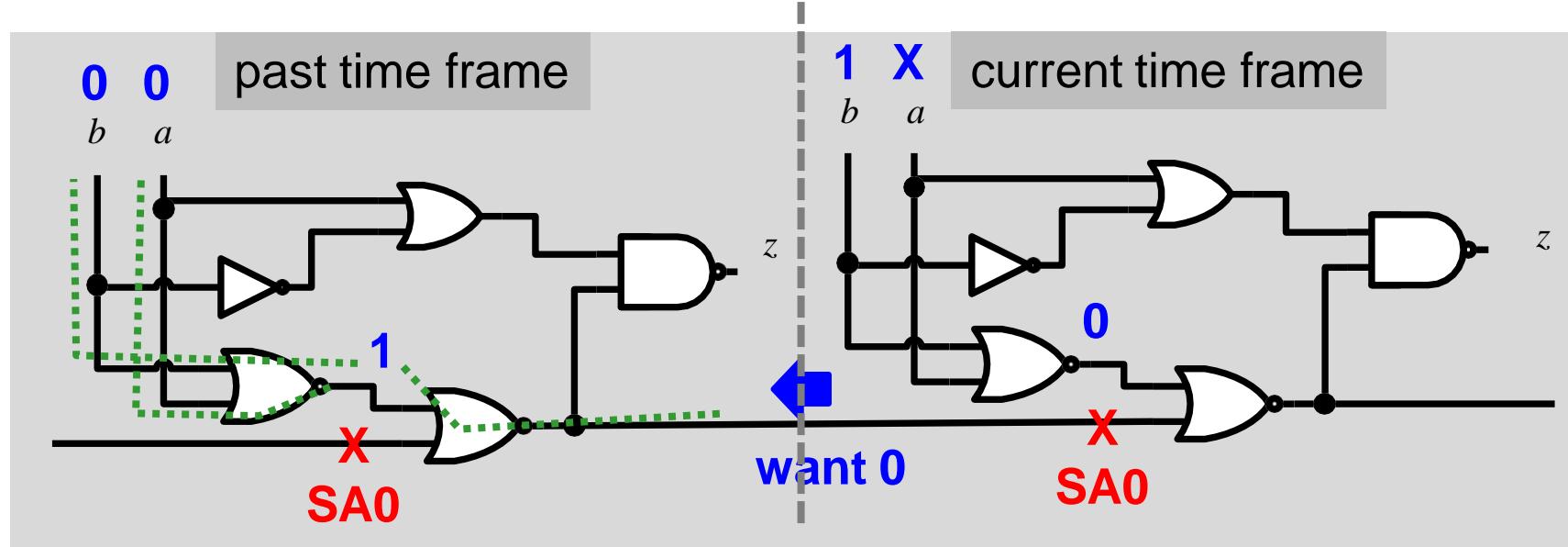
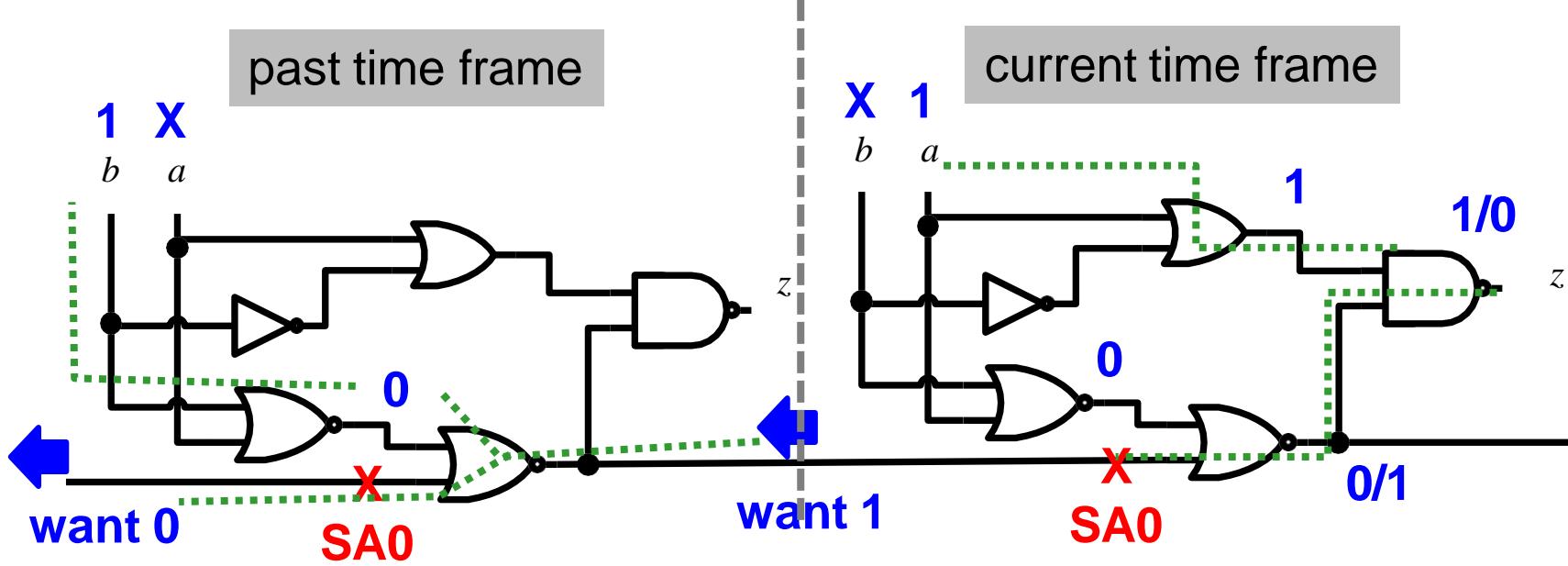


past time frame



current time frame

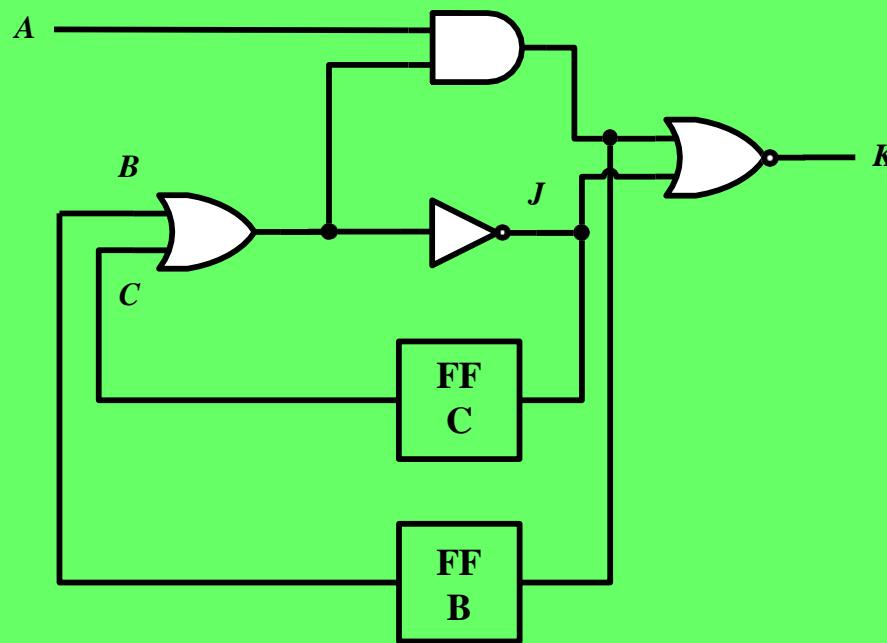




ab = 00, 1x, x1

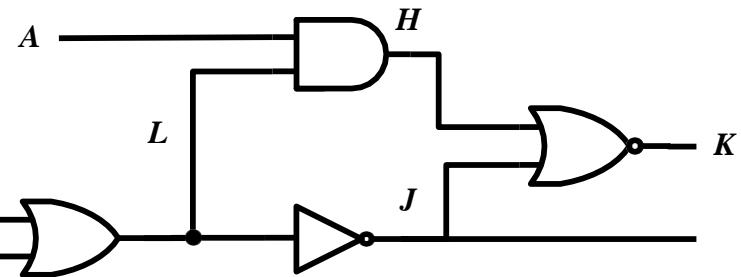
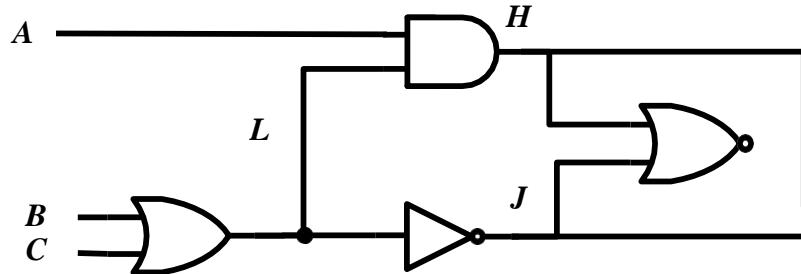
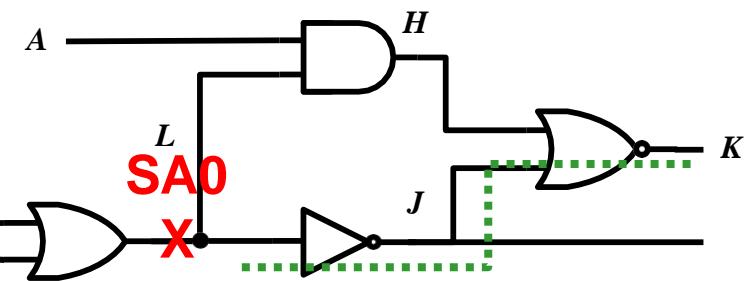
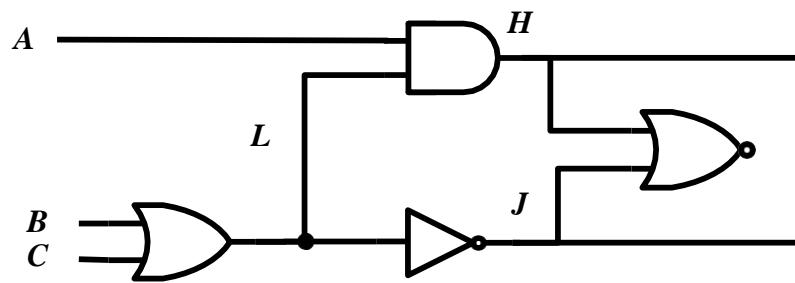
Quiz

Q: Please redraw this into two time frames

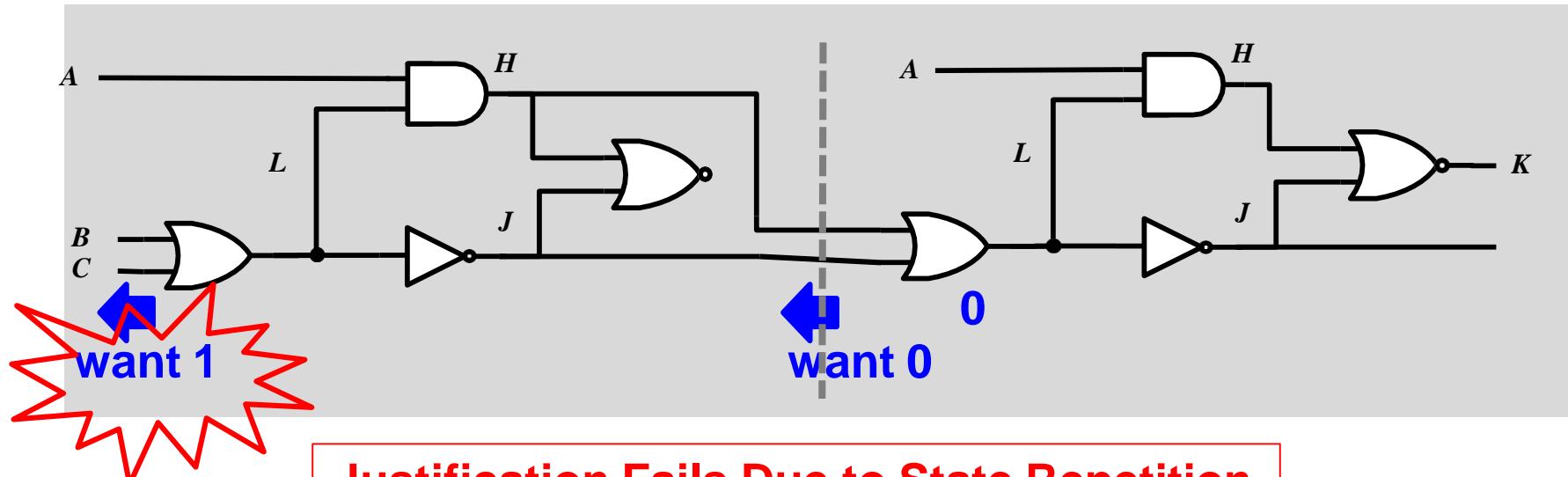
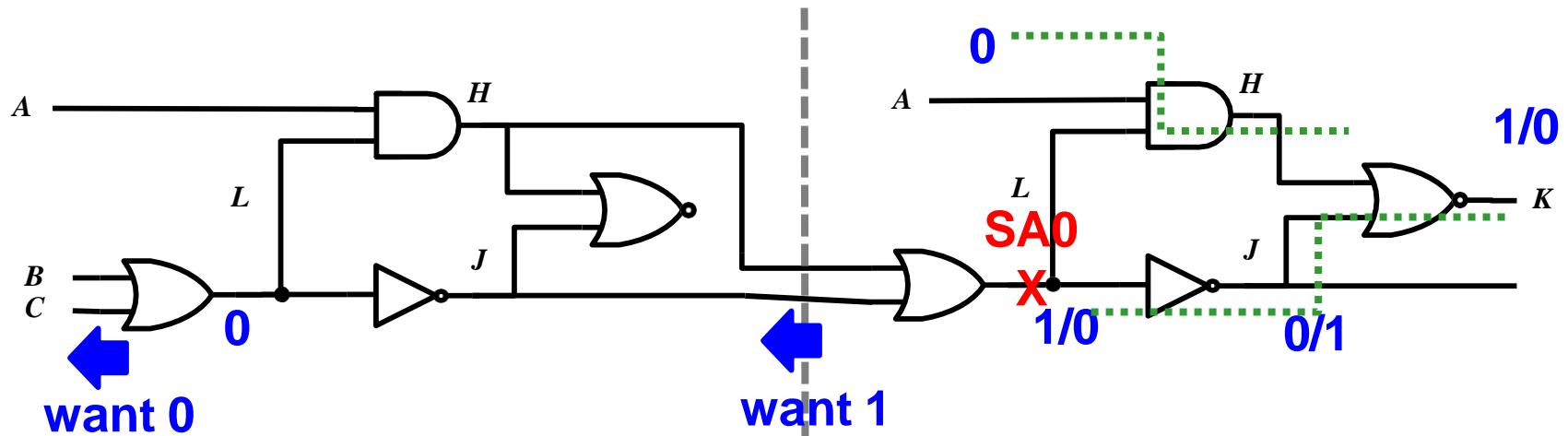


Quiz (cont'd)

Q: Use EBT to generate test patterns for SA0 fault



State Repetition



Justification Fails Due to State Repetition

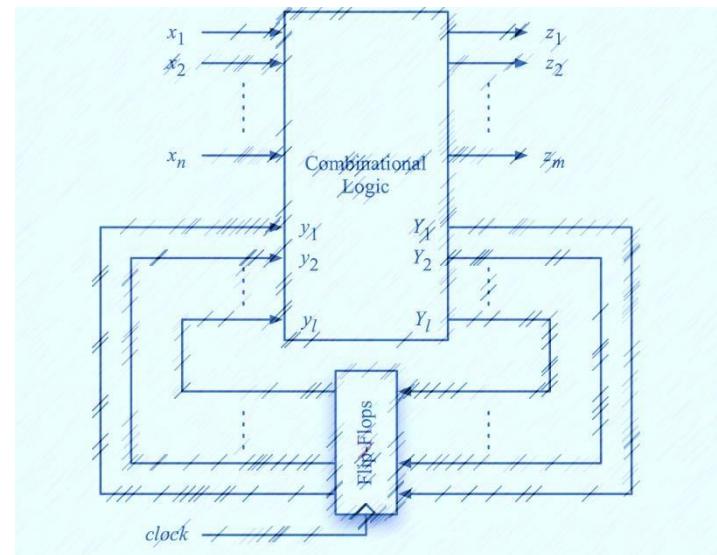
Comparison

	Advantages	Disadvantages	Example
Mixed F/B Time Frame	😊 Reuse existing D algorithm	😢 Too many time frames	Extended D
Backward TF Only	😊 Fixed time frames 😊 State repetition recognized	😢 Too many paths! How to choose path?	EBT

Need Help to Make Smart Decision

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 - BACK [Cheng 88]
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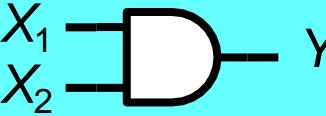
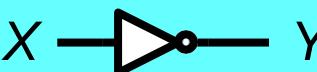
BACK Algorithm [Cheng 88]

- BACK selects a *PO* for fault detection,
 - ◆ Do not explicitly select a *path*
- PO selection based on a testability measures
 - ◆ *Drivability*
- Sensitized path will be created implicitly when drivability calculation

BACK Chooses PO Instead of Path

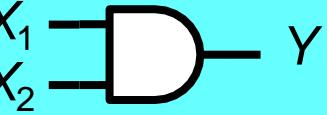
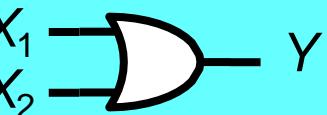
Review: SCOAP (CH 6)

- $CC^0(N)$, $CC^1(N)$
 - ◆ Minimum number of combinational PI assignments and logic levels required to control a 0 or a 1 on node N
 - ◆ Estimates effort to control signal to zero or one
 - Smaller number, easier to control

	$CC^0(Y)$	$CC^1(Y)$
	$\min[CC^0(X_1), CC^0(X_2)] + 1$	$CC^1(X_1) + CC^1(X_2) + 1$
	$CC^0(X_1) + CC^0(X_2) + 1$	$\min[CC^1(X_1), CC^1(X_2)] + 1$
	$CC^1(X) + 1$	$CC^0(X) + 1$
Primary inputs	1	1

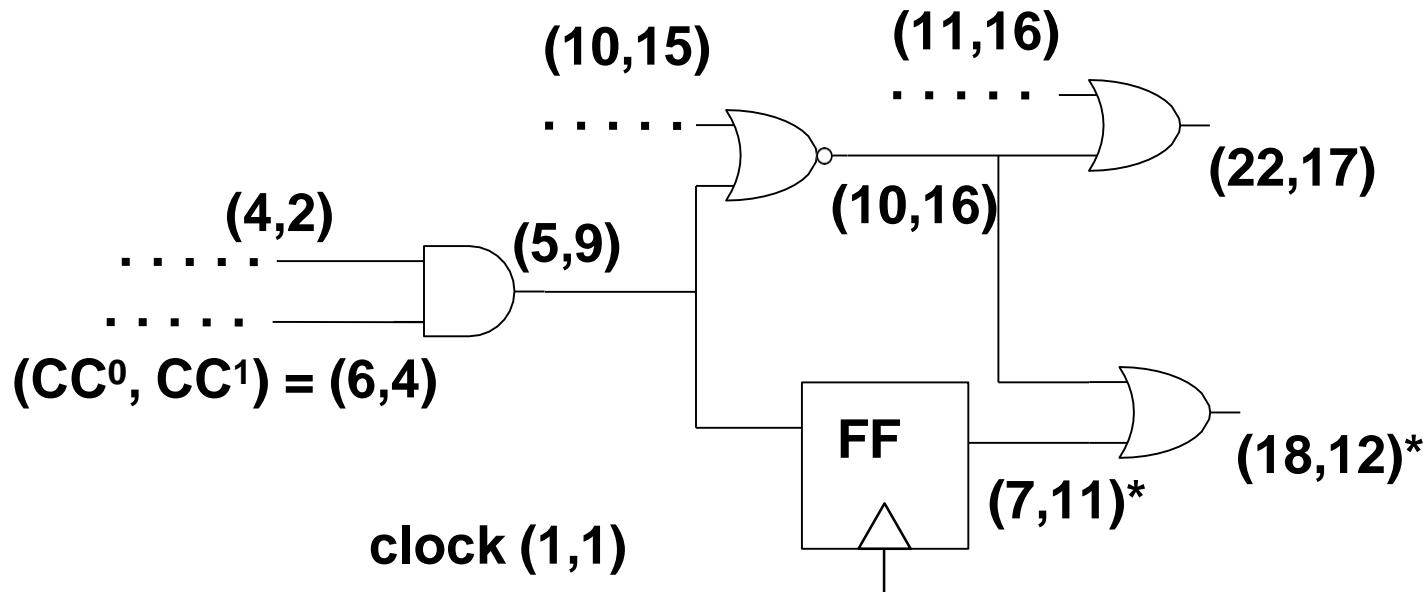
Drivability: $d^{0/1}$, $d^{1/0}$

- Estimates **effort** to propagate a **D or D'** from fault site to Y
 - $d^{0/1}(Y) = \text{drivability of } D' \text{ to node } Y$
 - $d^{1/0}(Y) = \text{drivability of } D \text{ to node } Y$

	$d^{0/1}(Y)$	$d^{1/0}(Y)$
	$\min \{CC^1(X_1) + d^{0/1}(X_2),$ $d^{0/1}(X_1) + CC^1(X_2),$ $d^{0/1}(X_1) + d^{0/1}(X_2)\} + 1$	$\min \{CC^1(X_1) + d^{1/0}(X_2),$ $d^{1/0}(X_1) + CC^1(X_2),$ $d^{1/0}(X_1) + d^{1/0}(X_2)\} + 1$
	$\min \{CC^0(X_1) + d^{0/1}(X_2),$ $d^{0/1}(X_1) + CC^0(X_2),$ $d^{0/1}(X_1) + d^{0/1}(X_2)\} + 1$	$\min \{CC^0(X_1) + d^{1/0}(X_2),$ $d^{1/0}(X_1) + CC^0(X_2),$ $d^{1/0}(X_1) + d^{1/0}(X_2)\} + 1$
	$d^{1/0}(X) + 1$	$d^{0/1}(X) + 1$
$Y = \text{FF out}$ $X = \text{FF in}$	$d^{0/1}(X) + K \text{ (constant)}$	$d^{1/0}(X) + K \text{ (constant)}$

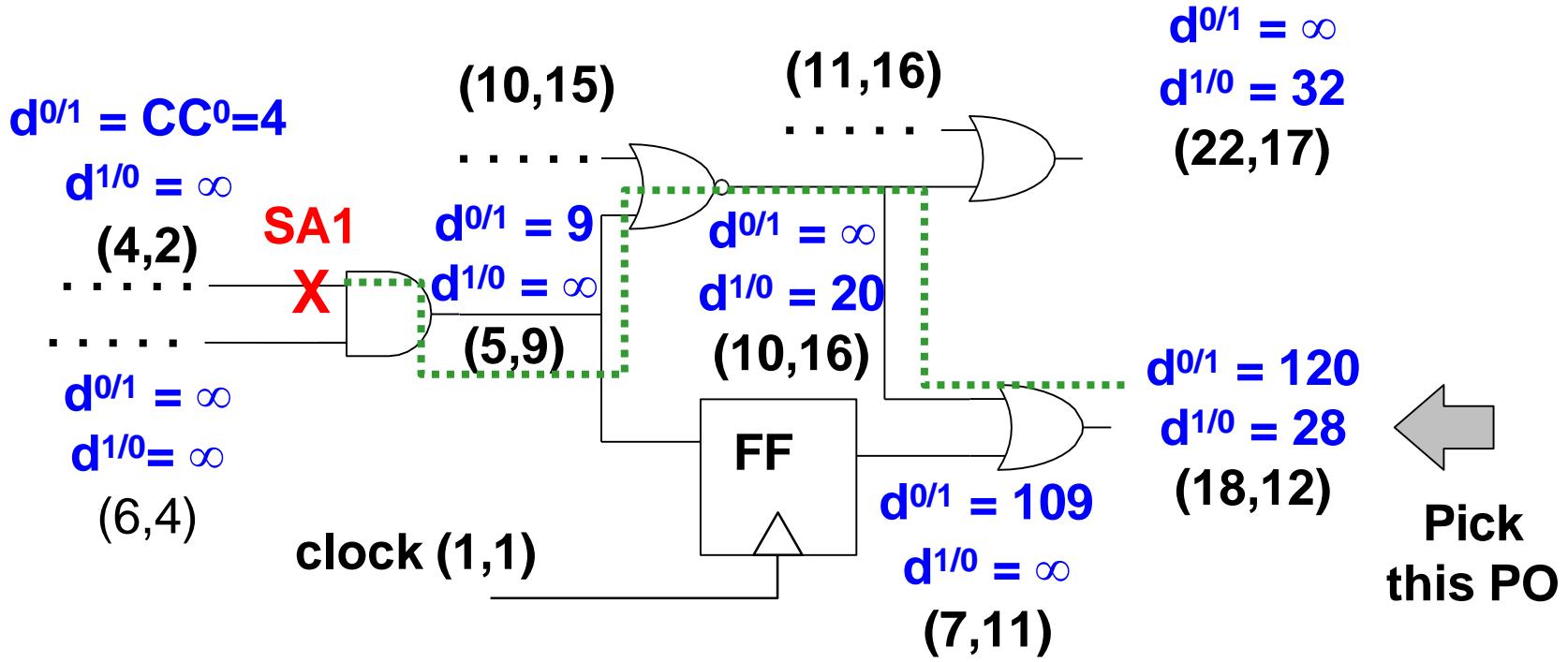
Example 1/2: SCOAP (BA Fig. 8.7)

- Fault-free circuit



* different from textbook

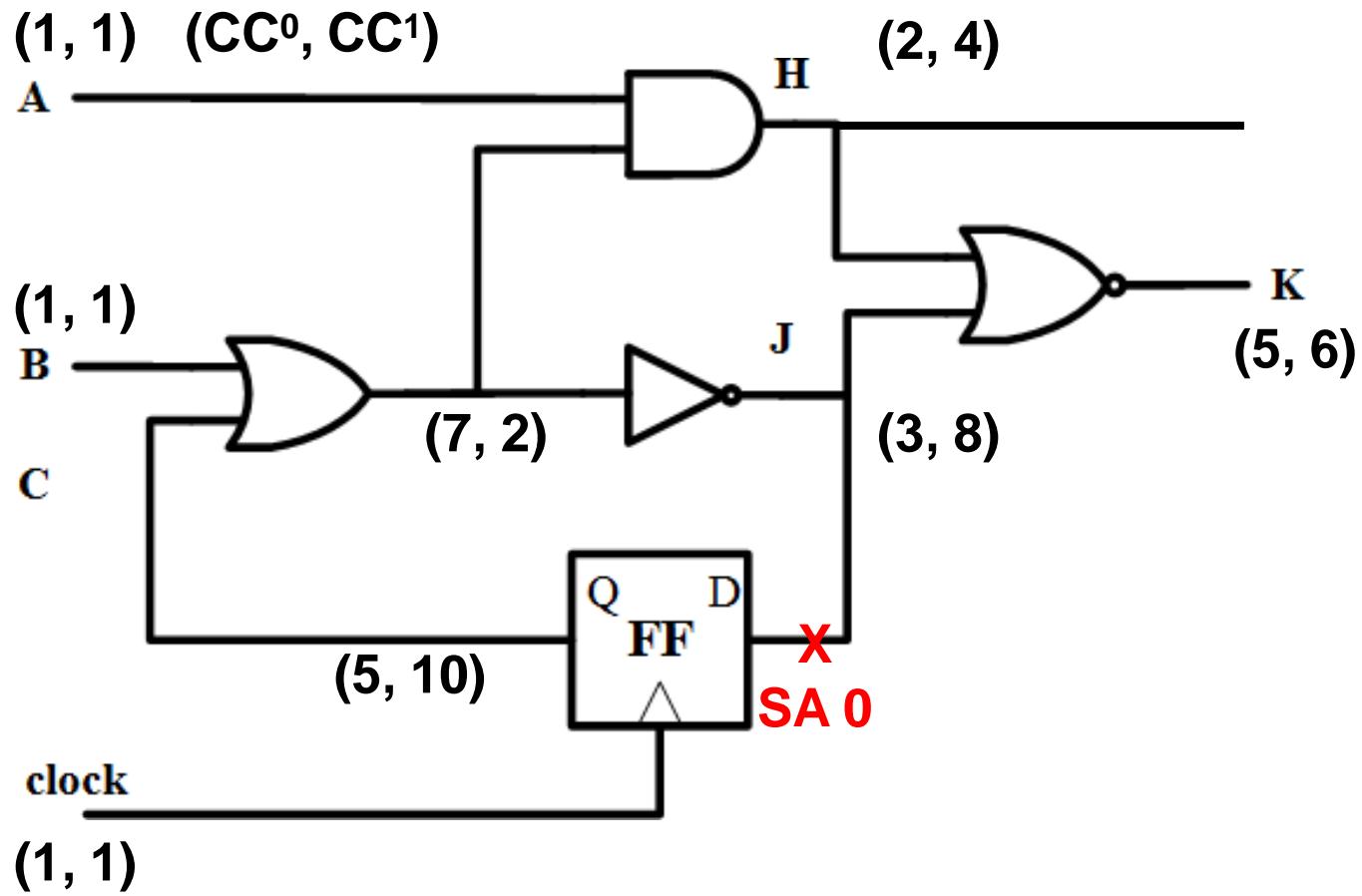
Example 2/2: Drivability (BA Fig. 8.7)



- $K=100$
- When D impossible, $d^{1/0} = \infty$

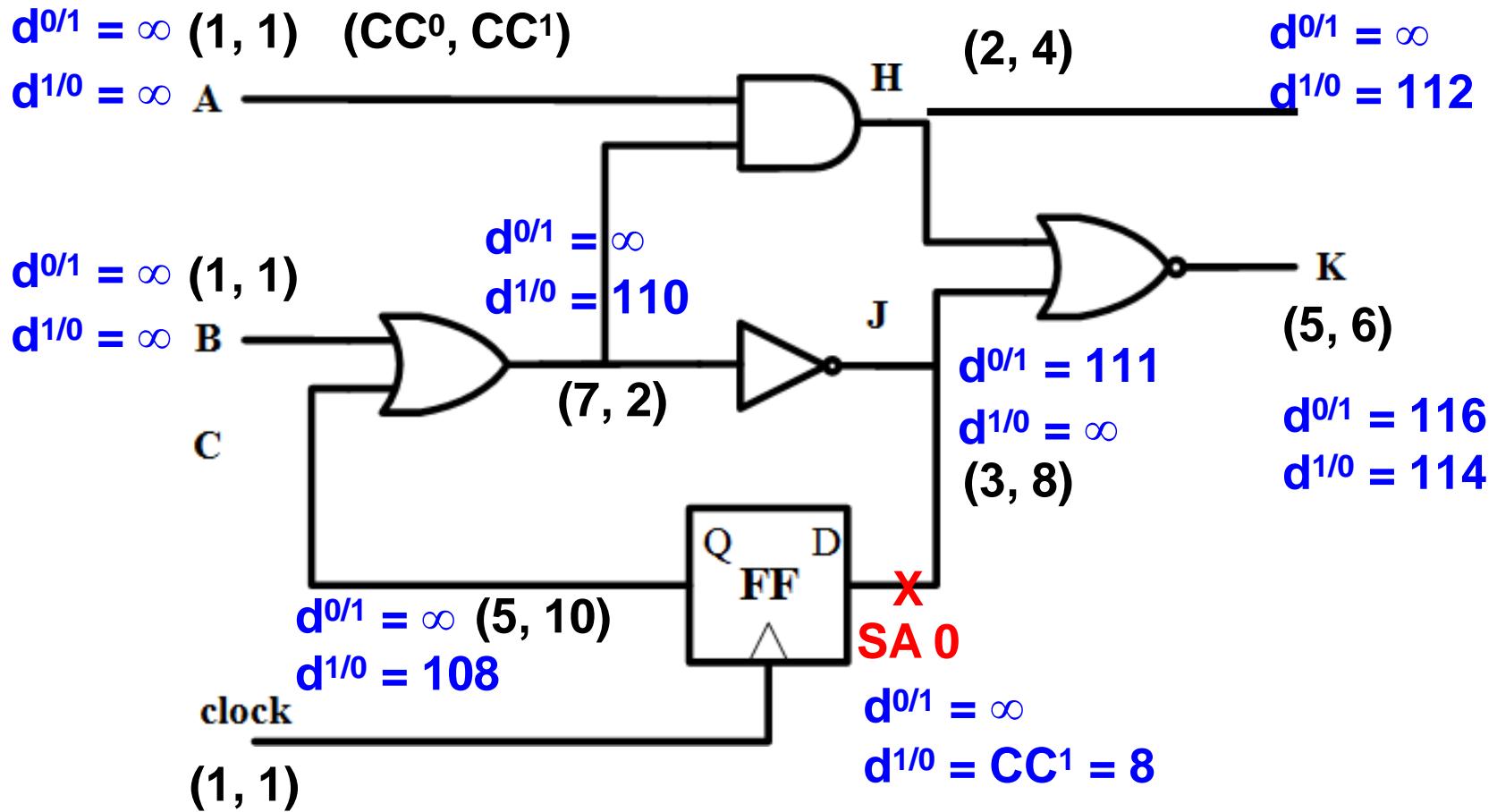
Quiz

Q: Based on SCOAP, please calculate drivability of SA0 fault.
(Assume K=100)



Quiz

Q: Based on SCOAP, please calculate drivability of SA0 fault.
 (Assume K=100)



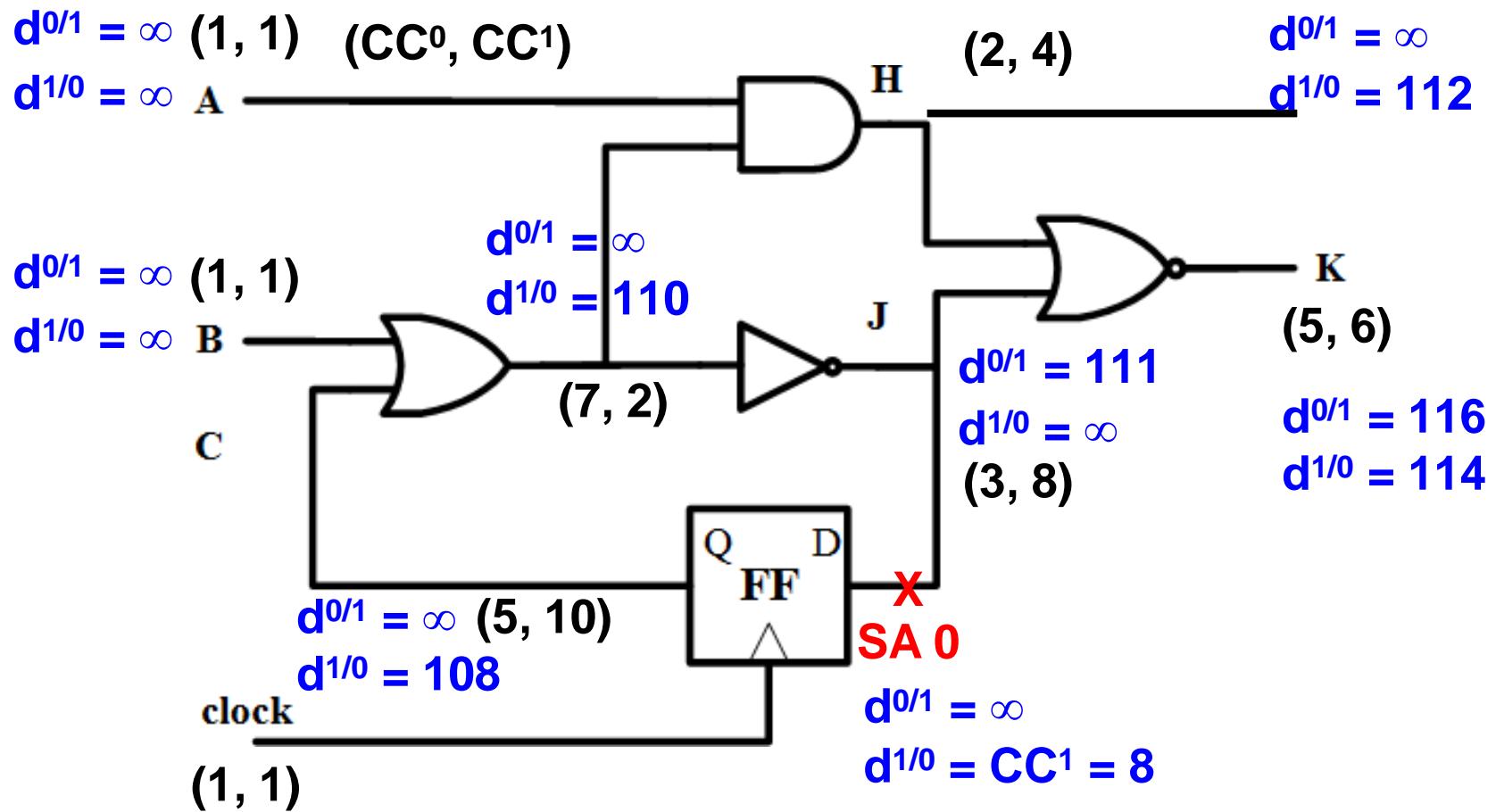
Summary

- **Backward time frame processing** has advantages:
 - ◆ Fixed time frame
 - ◆ State repetition recognized
- EBT selects **one path** at a time
- BACK proposes **drivability** to select best PO

	Advantages	Disadvantages	Example
Mixed F/B Time Frame	😊 Reuse existing alg.	😢 Too many time frames	Extended D
Backward TF Only	😊 Fixed time frames 😊 State repetition recognized	😢 Too many paths!	EBT BACK
Forward TF Only	😊 No need to justify	😢 Hard to decide time frames	FASTEST (PODEM-like)

FFT1

- Do we need feedback to iteratively calculate Drivability?



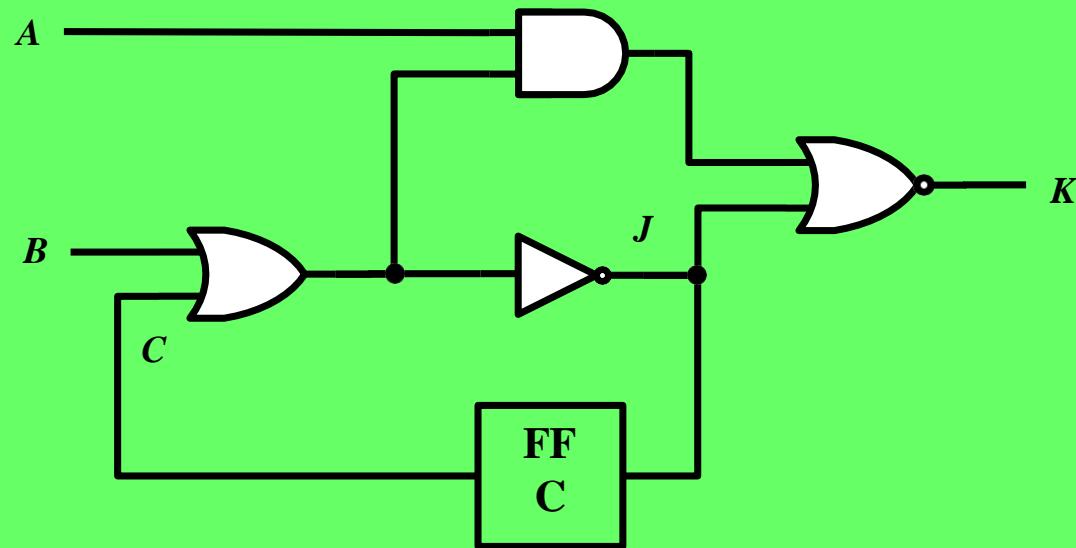
FFT2

- Q: For forward time frame processing, can we fix time frames, like EBT?

	Advantages	Disadvantages	Example
Mixed F/B Time Frame	😊 Reuse existing alg.	😢 Too many time frames	Extended D
Backward TF Only	😊 Fixed time frames 😊 State repetition recognized	😢 Too many paths!	EBT BACK
Forward TF Only	😊 No need to justify	😢 Hard to decide time frames	PODEM-like

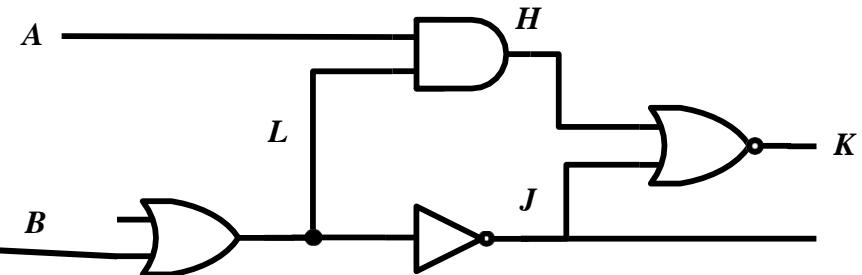
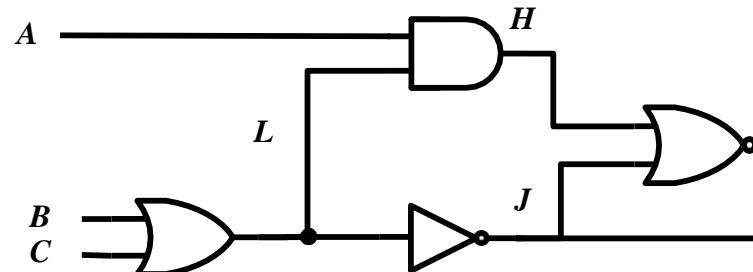
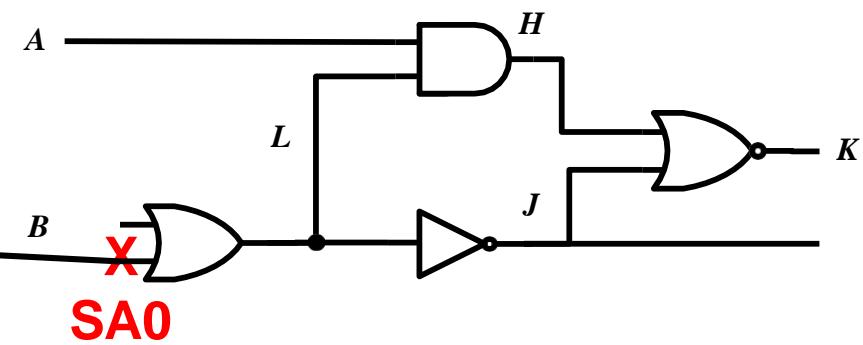
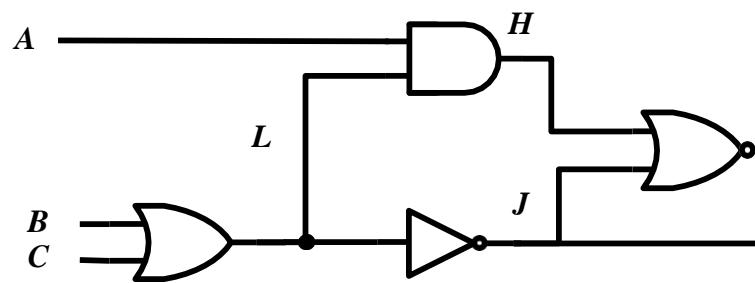
Quiz

Q: Please redraw this into two time frames



Quiz (cont'd)

Q: Use EBT to generate test patterns for SA0 fault



Drivability

- *Drivability* estimates effort of propagating a **D or D'** from fault site to that signal
 - ◆ Similar to **SCOAP**
- Review of SCOAP

	$CC^0(Y)$	$CC^1(Y)$
$Y = X_1 \text{ AND } X_2$	$\min[CC^0(X_1), CC^0(X_2)] + 1$	$CC^1(X_1) + CC^1(X_2) + 1$
$Y = X_1 \text{ OR } X_2$	$CC^0(X_1) + CC^0(X_2) + 1$	$\min[CC^1(X_1), CC^1(X_2)] + 1$
$Y = X'$	$CC^1(X) + 1$	$CC^0(X) + 1$
Primary inputs	1	1

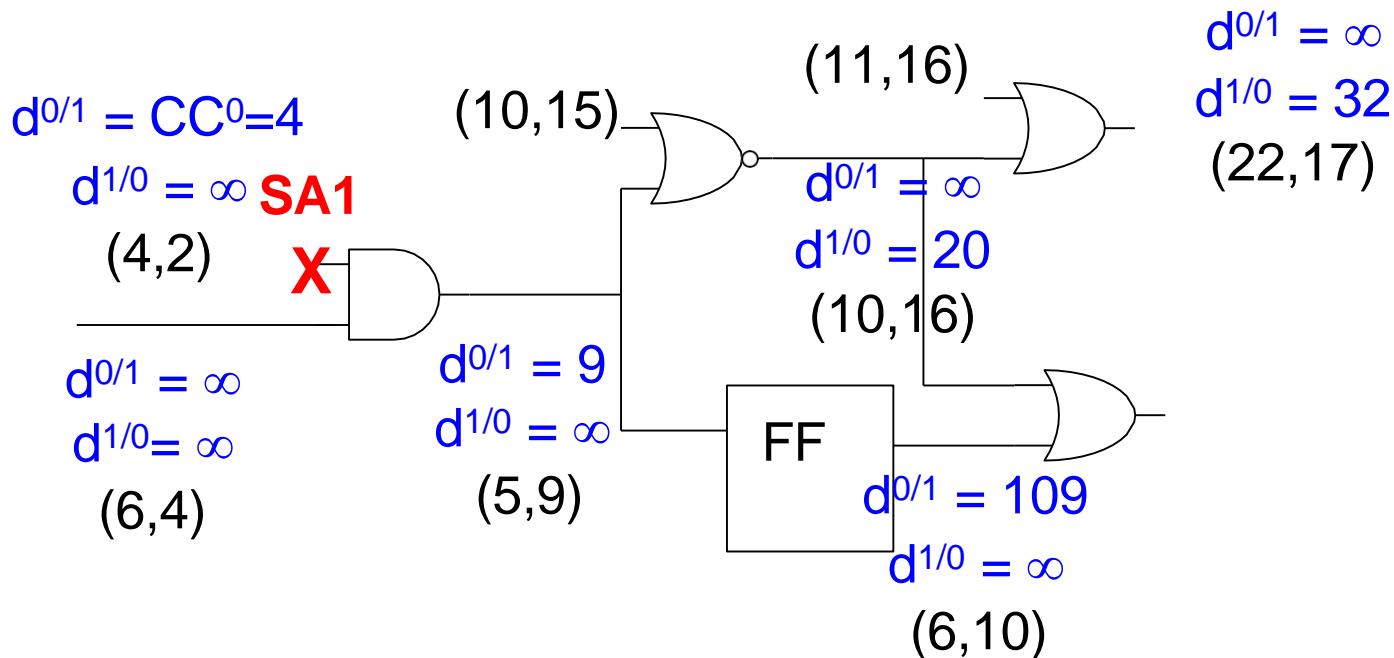
Drivability is like SCOAP for a Specific Fault

Drivability: $d(0/1)$ & $d(1/0)$

- $d^{0/1}(Y) = \text{drivability of } D'$
 - ◆ Effort to bring node Y to D' when the fault presents
- $d^{1/0}(Y) = \text{drivability of } D$

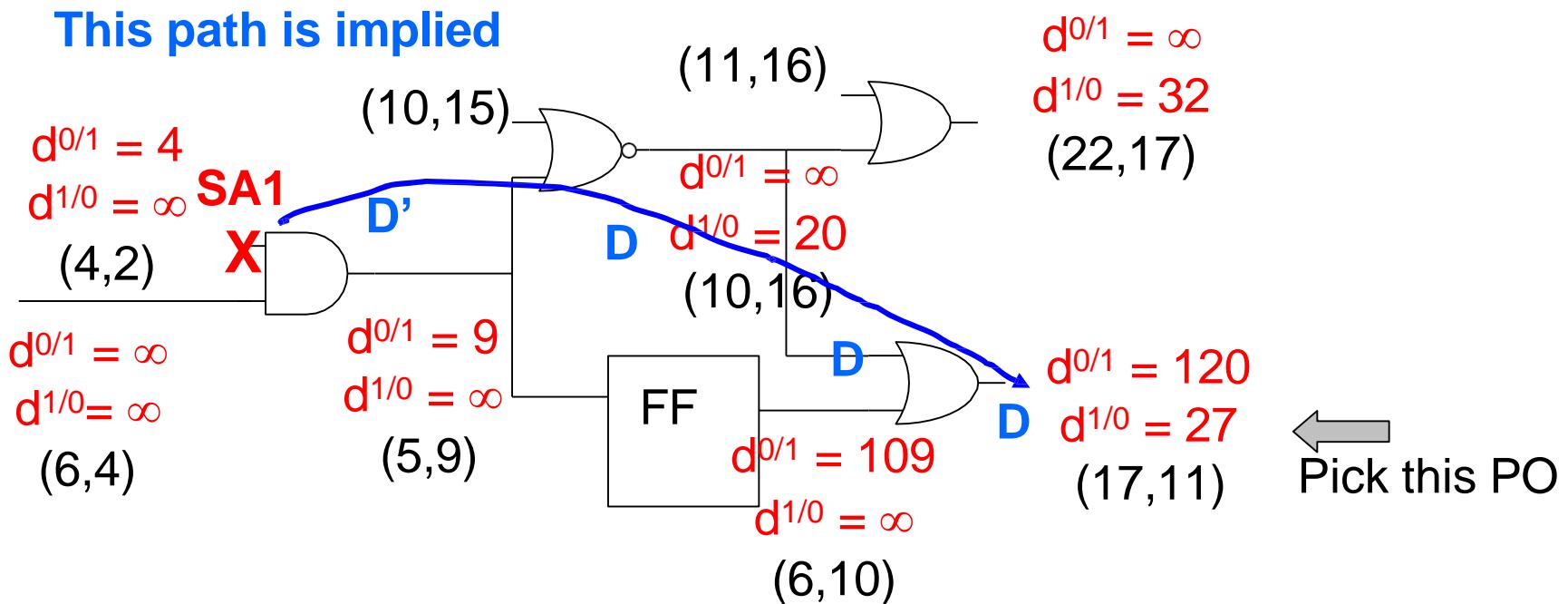
	$d^{0/1}(Y)$	$d^{1/0}(Y)$
$Y = X_1 \text{ AND } X_2$	$\min \{CC^1(X_1) + d^{0/1}(X_2),$ $d^{0/1}(X_1) + CC^1(X_2),$ $d^{0/1}(X_1) + d^{0/1}(X_2)\} + 1$	$\min \{CC^1(X_1) + d^{1/0}(X_2),$ $d^{1/0}(X_1) + CC^1(X_2),$ $d^{1/0}(X_1) + d^{1/0}(X_2)\} + 1$
$Y = X_1 \text{ OR } X_2$	$\min \{CC^0(X_1) + d^{0/1}(X_2),$ $d^{0/1}(X_1) + CC^0(X_2),$ $d^{0/1}(X_1) + d^{0/1}(X_2)\} + 1$	$\min \{CC^0(X_1) + d^{1/0}(X_2),$ $d^{1/0}(X_1) + CC^0(X_2),$ $d^{1/0}(X_1) + d^{1/0}(X_2)\} + 1$
$Y = X'$	$d^{1/0}(X) + 1$	$d^{0/1}(X) + 1$
$Y = \text{FF out}$ $X = \text{FF in}$	$d^{0/1}(X) + K \text{ (constant)}$	$d^{1/0}(X) + K \text{ (constant)}$

Drivability Example 1/2 (BA Fig. 8.7)



- $K=100$
- When D impossible, $d^{1/0} = \infty$

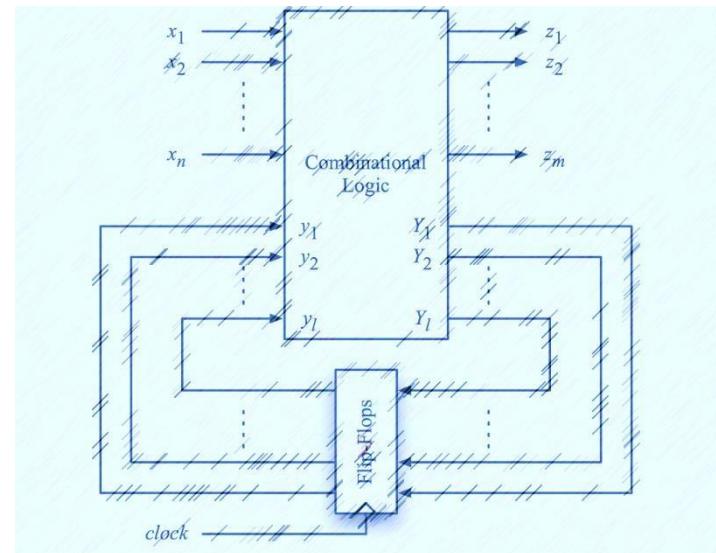
Drivability Example 2/2 (BA Fig. 8.7)



- To justify a D or D' at gate output, select gate input with smallest drivability as D or D' input

Sequential ATPG

- Introduction
- Time-frame expansion methods
- Simulation-based methods (* not in exam)
 - ◆ CONTEST [Agrawal & Cheng 88]
 - ◆ Genetic Algorithm
- Issues of Sequential ATPG
- Conclusions



Simulation-Based Methods

- Idea: use logic/fault simulators to guide ATPG [Seshu 62]
 - ◆ Simulation is faster than ATPG
- Approach
 - ◆ Generate **candidate** test vectors
 - ◆ **Fitness*** of candidates evaluated by logic or fault simulation
 - ◆ Select best candidate based on a certain **cost function**
- Advantage:
 - ◆ No time frame expansion. **Easy memory management**

Simulate Many Vectors and Choose Best

CONTEST– Concurrent Test Generator for Sequential Circuits [Agrawal & Cheng 89]

- Based on **event-driven** concurrent fault simulator
- Search for test vectors guided by cost functions
- Three phases
 - ① Initialization
 - ② Concurrent fault detection
 - ③ Single fault detection

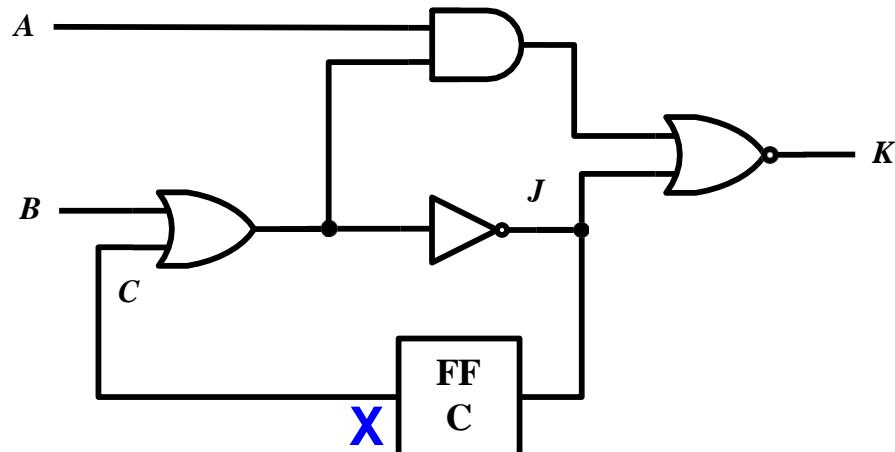
1. Initialization Phase

- Start with arbitrary test vector
 - ◆ Start with FFs in unknown states
- Use logic simulation (not fault simulation)
 - ◆ Cost = number of FFs in unknown state
 - ◆ *Trial vectors* are generated by single-bit change of the current vector. A trial vector is accepted and becomes the current vector if it lowers the cost
- Stop this phase when cost drops below a desired value

QUIZ

Q1: Initially the FF is unknown. Given three trial vectors, please simulate the circuit and decide their costs, where cost = number of unknown FF.

Q2: Which trial vector would you pick?

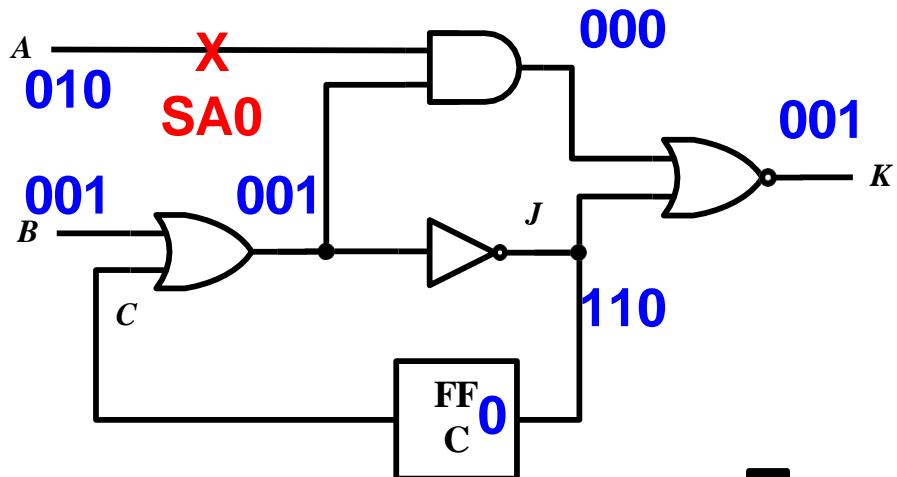


AB	cost = number of unknown FF
00	1
01	
10	

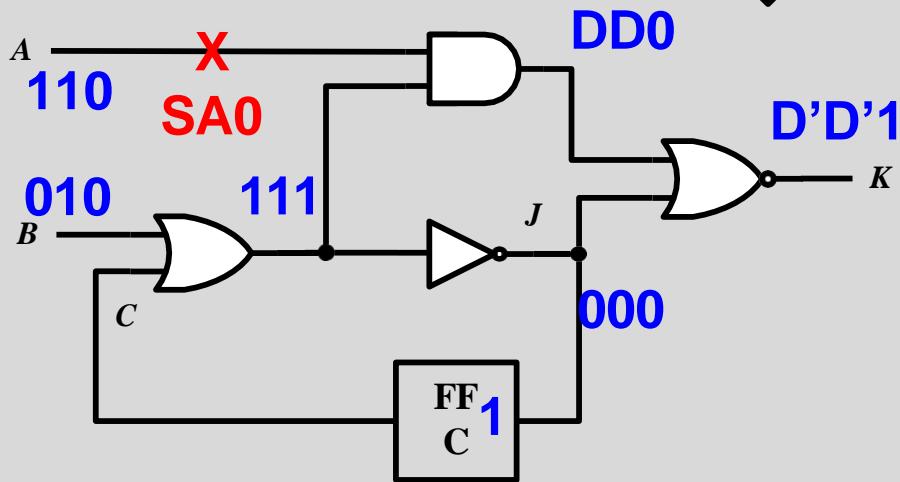
2. Concurrent Fault Detection Phase

- Start with fault simulation of generated initialization sequence
 - ◆ Detected faults are dropped from the fault list
- Compute the cost of the last vector
 - ◆ Cost of an undetected fault f
 - **COST(f)** = minimum distance of its fault effect to a PO
 - distance = level of logic gates
 - ◆ Cost of a vector
 - Sum of costs of all undetected faults
- Trial vectors are generated by **single-bit change**
 - ◆ Only accept the vectors that reduce the cost

Example



AB	cost = distance of D or D' to PO
00	∞
10	2
01	∞

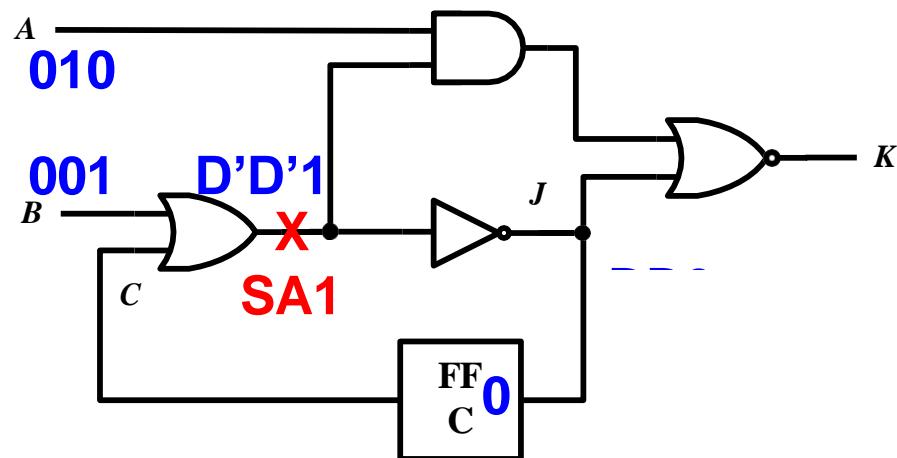


AB	cost = distance of D or D' to PO
10	0
11	0
00	∞

QUIZ

Q1: Given FF initial state is zero, please evaluate the cost of three trial vectors: 00, 10, 01

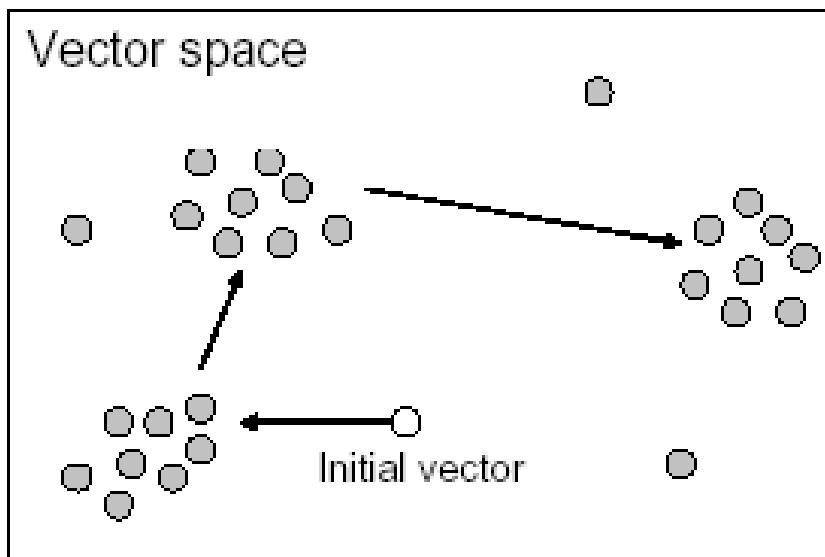
Q2: Which test vector would you pick?



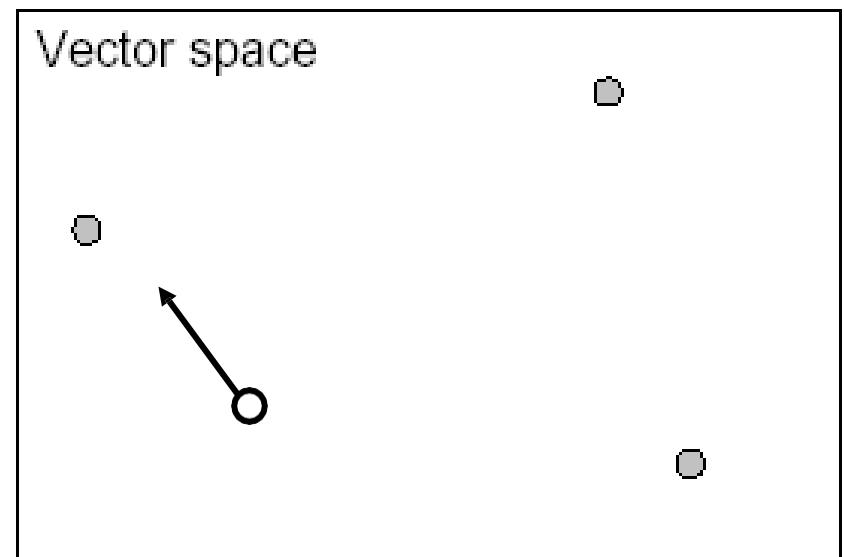
AB	cost = distance of D or D' to PO
00	
10	
01	

Need Phase 3

- Experience shows test patterns for all stuck-at faults are usually **clustered** instead of being evenly distributed
- When only a few faults are left, their tests will be isolated vectors and we need a different test generation strategy



Phase 2: Concurrent Fault Detection



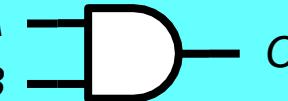
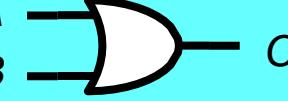
Phase 3: Single Fault Detection

3. Single Fault Detection Phase

- Start with any vector
- Generate new vectors by single-bit change to reduce cost of the selected fault until it is detected
 - ◆ The lowest cost fault is picked first
- Cost of a fault f at signal line g is
 - ◆ If not activated yet:
 $KC_A(f) + C_P(f)$
 $K = \text{constant} ; C_A = \text{activation} ; C_p = \text{propagation cost}$
 - ◆ If activated:
 $\text{Min}(C_P(i))$, $i \in \text{the set of inputs to signal } g$

C_A and DC

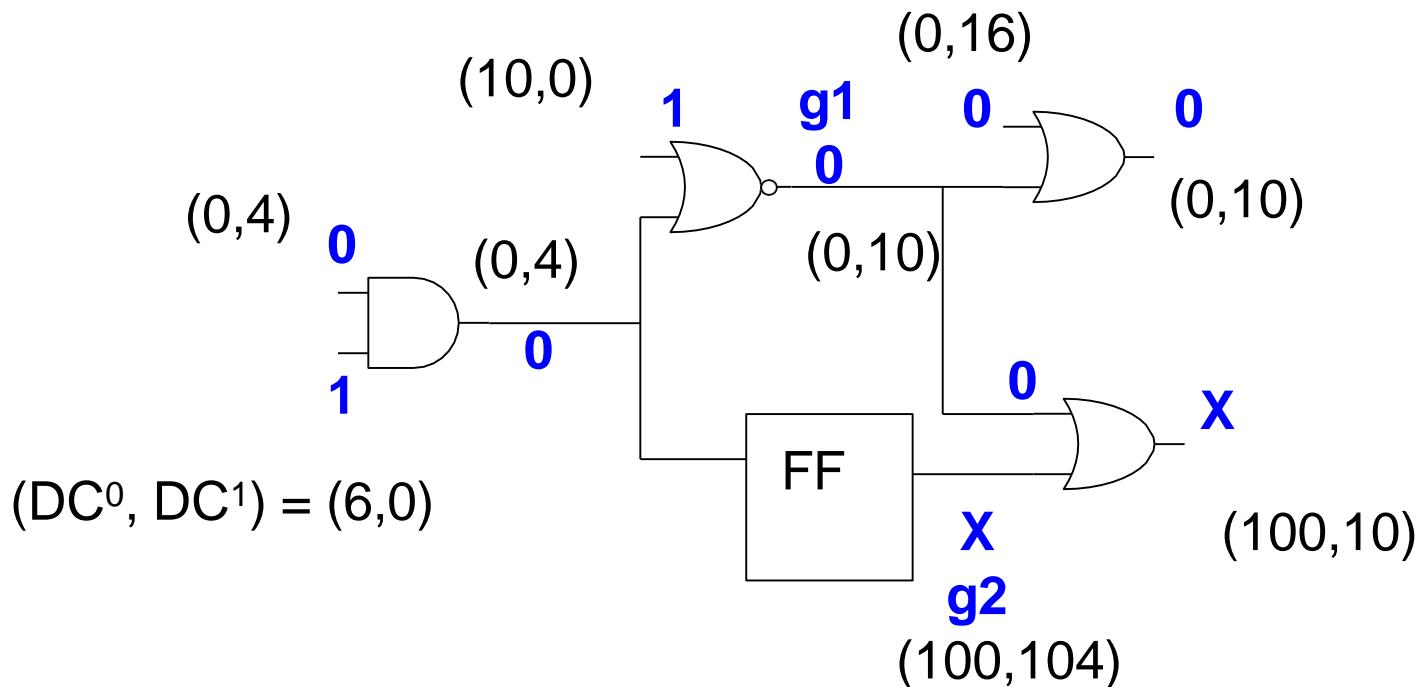
- **Activation Cost, C_A**
 - ◆ $C_A(g \text{ stuck-at-}v) = DC_{v'}(g)$ = dynamic controllability of line g at v'
- **Dynamic Controllability, DC**
 - ◆ Similar to sequential controllability in SCOAP except logic values known

	$DC^0(C)$	$DC^1(C)$
	$\min[DC^0(A), DC^0(B)]$, if $C=1$ or x 0, if $C=0$	$DC^1(A) + DC^1(B)$, if $C=0$ or x 0, if $C=1$
	$DC^0(A) + DC^0(B)$, if $C=1$ or x 0, if $C=0$	$\min[DC^1(A), DC^1(B)]$, if $C=0$ or x 0, if $A=1$
	$DC^1(A)$, if $C=1$ or x 0, if $C=0$	$DC^0(A)$, if $C=0$ or x 0, if $C=1$
Primary inputs	1, if $C=1$ or x 0, if $C=0$	1, if $C=0$ or x 0, if $C=1$
$C = FF(A)$	$DC^0(A)+K$, if $C=1$ or x 0, if $C=0$	$DC^1(A)+K^*$, if $C=0$ or x 0, if $C=1$

* K is a chosen constant

C_A and DC Example

- $C_A(g_1 \text{ stuck-at } 0) = DC_1(g_1) = 10 \leftarrow \text{easier}$
- $C_A(g_2 \text{ stuck-at } 1) = DC_0(g_2) = 100$

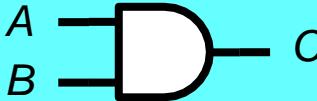
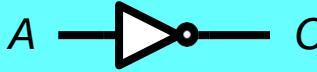
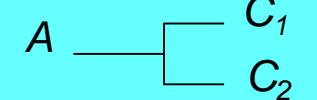


Propagation Cost, C_p

- $C_p(g)$ = Dynamic Observability of node g
- Dynamic observability (DO)
 - ◆ Similar to combinational observability in SCOAP
 - ◆ Measure the effort to observe the fault on a given node
 - the number of gates between N and PO's, and
 - the minimum number of PI assignments required to propagate the logical value on node N to a primary output.

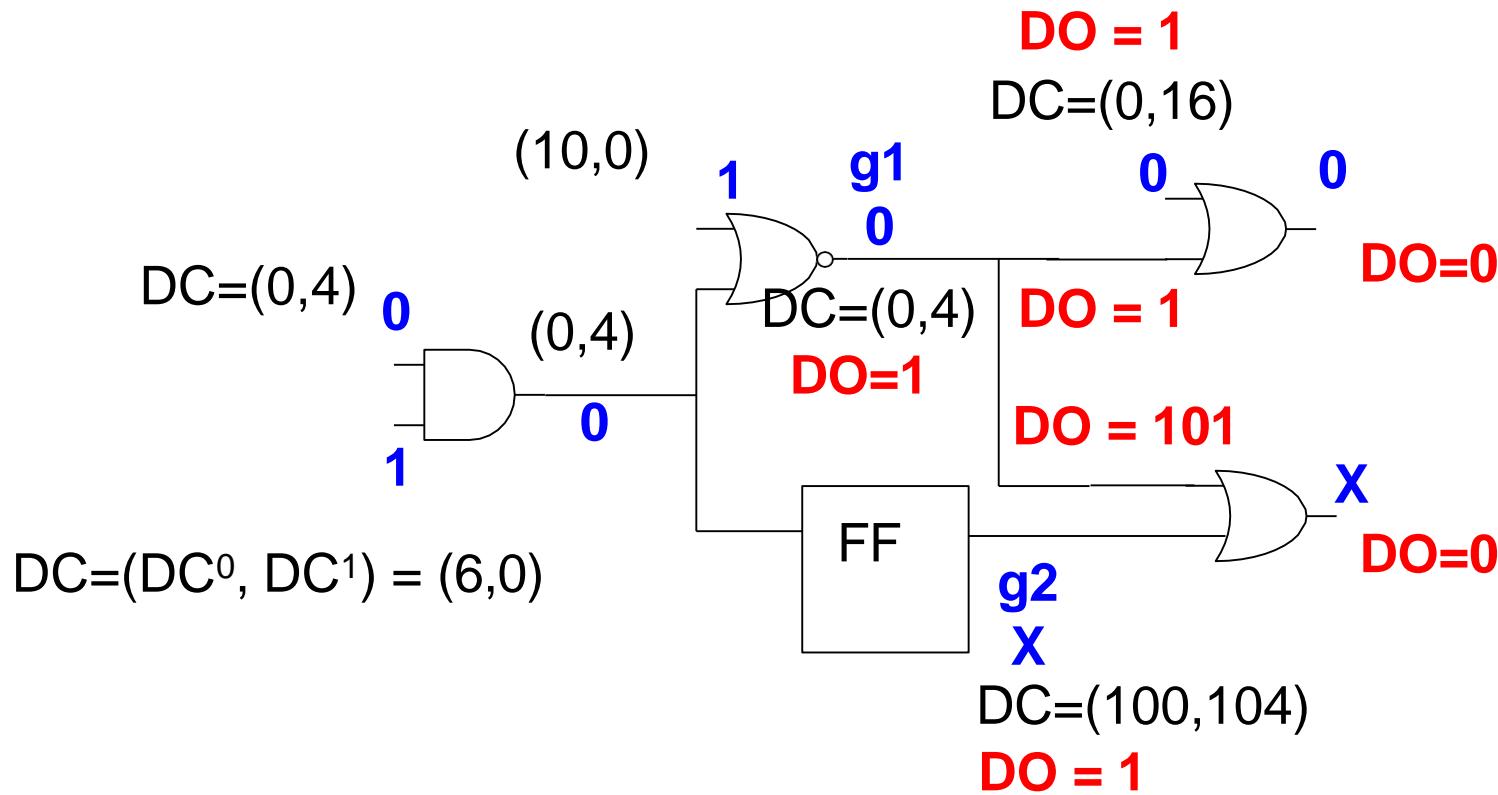
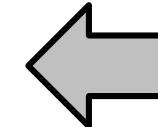
Dynamic Observability (DO)

- Similar to combinational observability in SCOAP

	$DO(A)$
	$DO(C) + DC^1(B) + 1$
	$DO(C) + DC^0(B) + 1$
	$DO(C) + 1$
	$\min[DO(C_1), DO(C_2)]$
Primary outputs	0

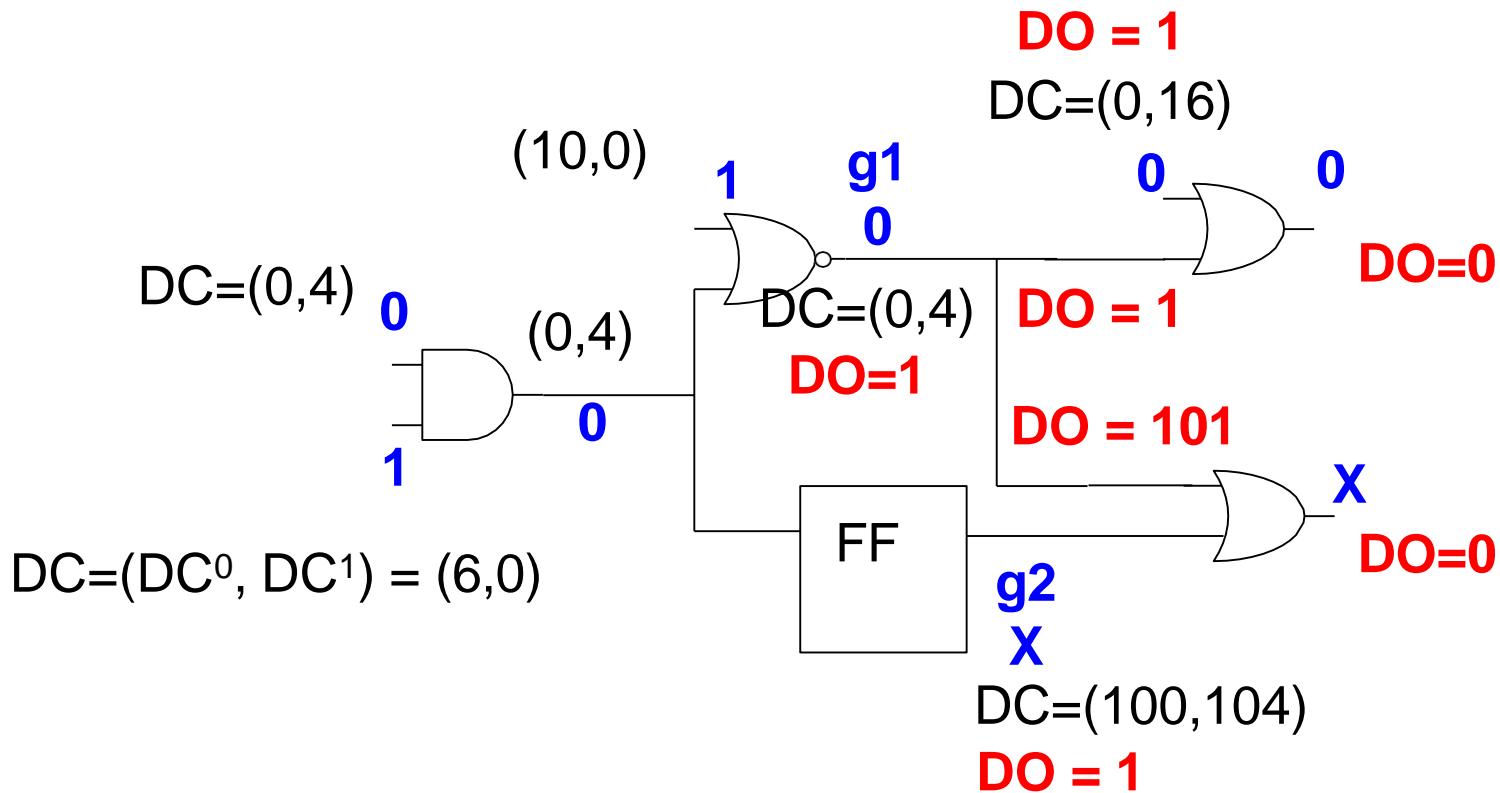
C_p and DO Example

- $C_p(g_1) = DO(g_1) = 1$
- $C_p(g_2) = DO(g_2) = 1$



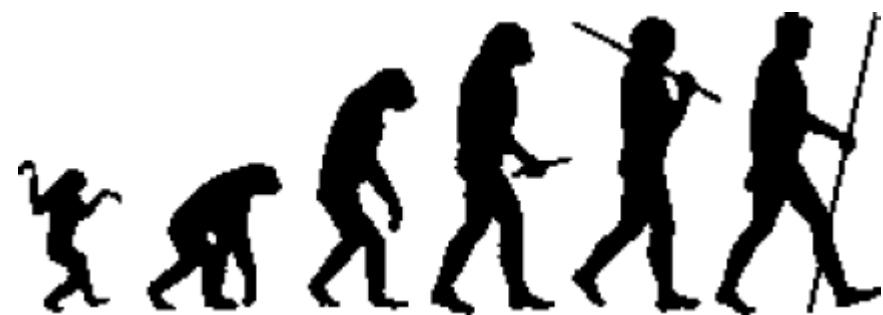
Total Cost

- Fault g_1 : $C_A = 10$, $C_p = 1$
- Fault g_2 : $C_A = 100$, $C_p = 1$
- Choose g_1 SA0 as target fault to generate test vector



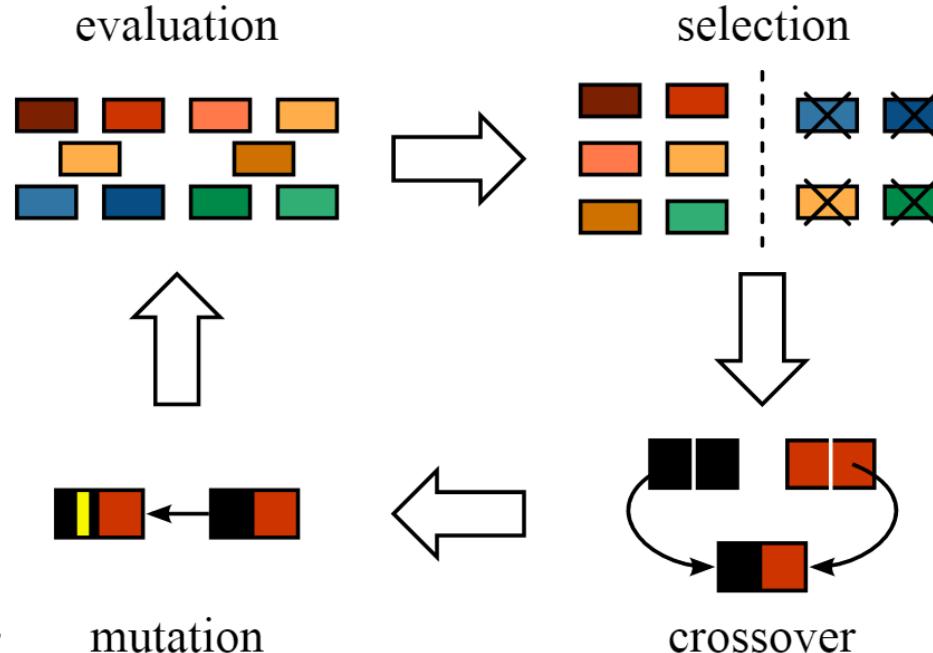
Sequential ATPG

- Introduction
- Time-frame expansion methods
- **Simulation-based methods**
 - ◆ CONTEST
 - ◆ Genetic Algorithm
- Issues of Sequential ATPG*
- Conclusions



Genetic Algorithms (GA) [Holland 1975]

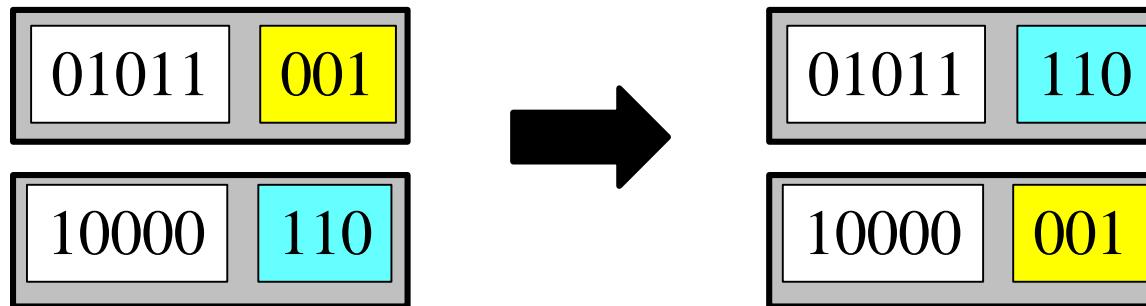
- General Principle: **Survival of fittest(s)**
 - ◆ Keep a *population* of feasible solutions, not just one
 - ◆ Parent population generates child population
 - by gene *crossover, mutation* etc
 - ◆ Select only best children, remove weak children
 - ◆ Repeat the above for many generations



[www.jade-cheng.com]

Crossover and Mutation

- Test vectors are represented by **bit-stream “gene”**
- **Crossover:** Two feasible solutions generate child by switching gene



- **Mutation:** some gene can change by a random probability

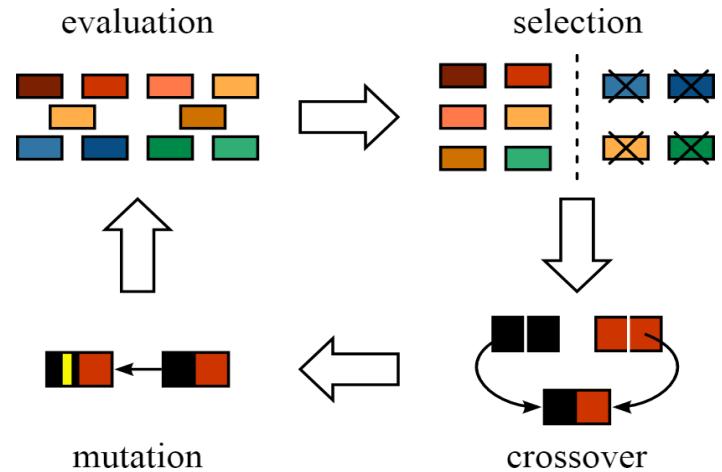


Pseudo Code of GA

GENETICALGORITHM

```
1 pop = set of initial solutions
2 do
3     childpop = ∅
4     for (i = 1 to (n x pop.size)) // n times size
5         crossover = random 0 or 1
6         if (crossover)
7             parent1 = random_choose(pop)
8             parent2 = random_choose(pop)
9             child = crossover(parent1, parent2)
10        else // mutate
11            parent = random_choose(pop)
12            child = mutate(parent)
13            childpop = childpop ∪ {child}
14        pop = evaluate&select(childpop)
15    while (!stop)
16    return (best solution)
```

- Need to decide
- 1. initial solution
- 2. crossover/ mutation
- 3. evaluate & select
- 4. stop criterion

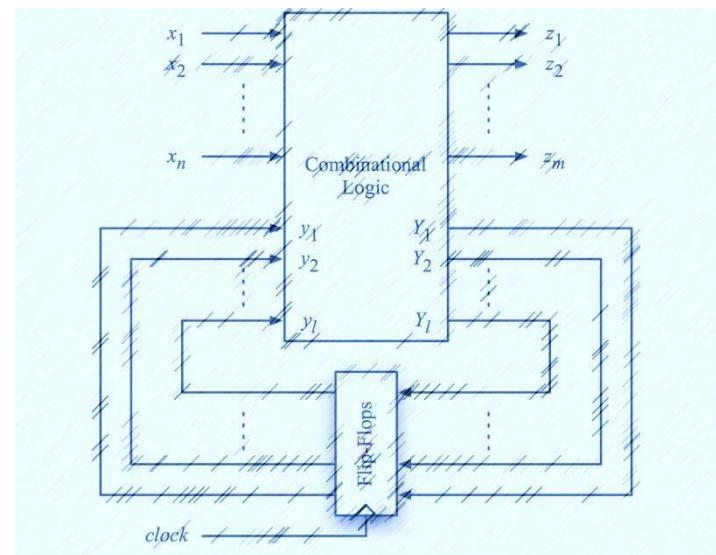


Summary

- **Simulation-based methods**
 - ◆ Randomly generate many trial test vectors
 - ◆ Evaluate test vectors by simulation and pick the best
 - ◆ Need many testability measure to help smart decision
- **Advantages**
 - ◆ Better **memory management** than time frame expansion
 - ◆ **Timing** can be considered
 - ◆ Use **genetic algorithm** to optimize
- **Disadvantages**
 - ◆ Cannot identify **untestable faults**
 - ◆ Test length can be **longer** than time frame expansion

Sequential ATPG

- Introduction
- Time-frame expansion methods
- Simulation-based methods*
- Issues of Sequential ATPG* (not in exam)
- Conclusions

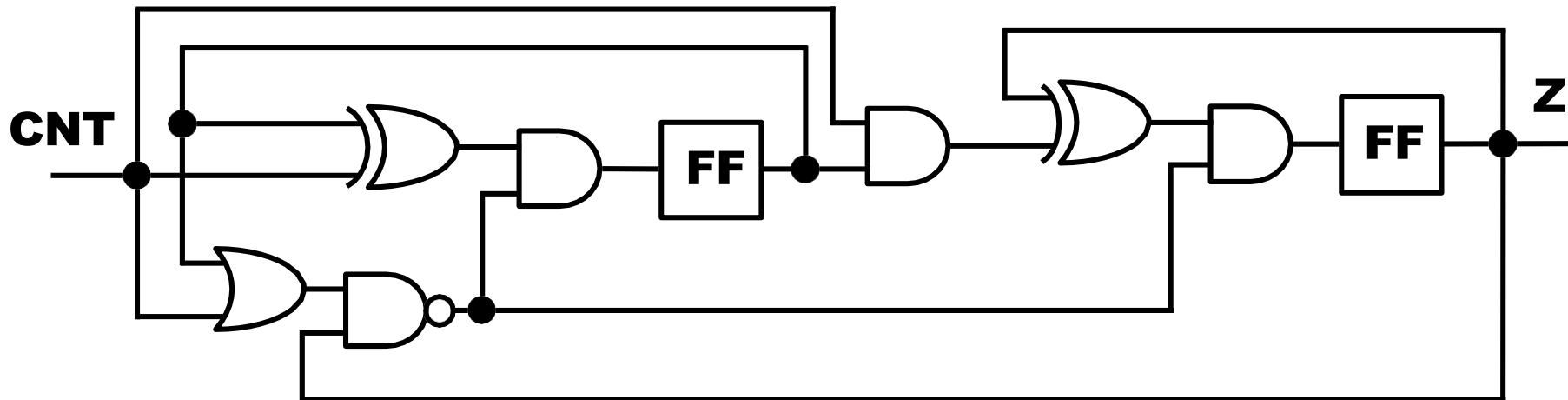


Issues of Sequential ATPG

- ① Ckts. without initialization input
- ② Potentially detected faults can escape test
- ③ Asynchronous ckt. requires special attention

① Circuit w/o Initialization Input

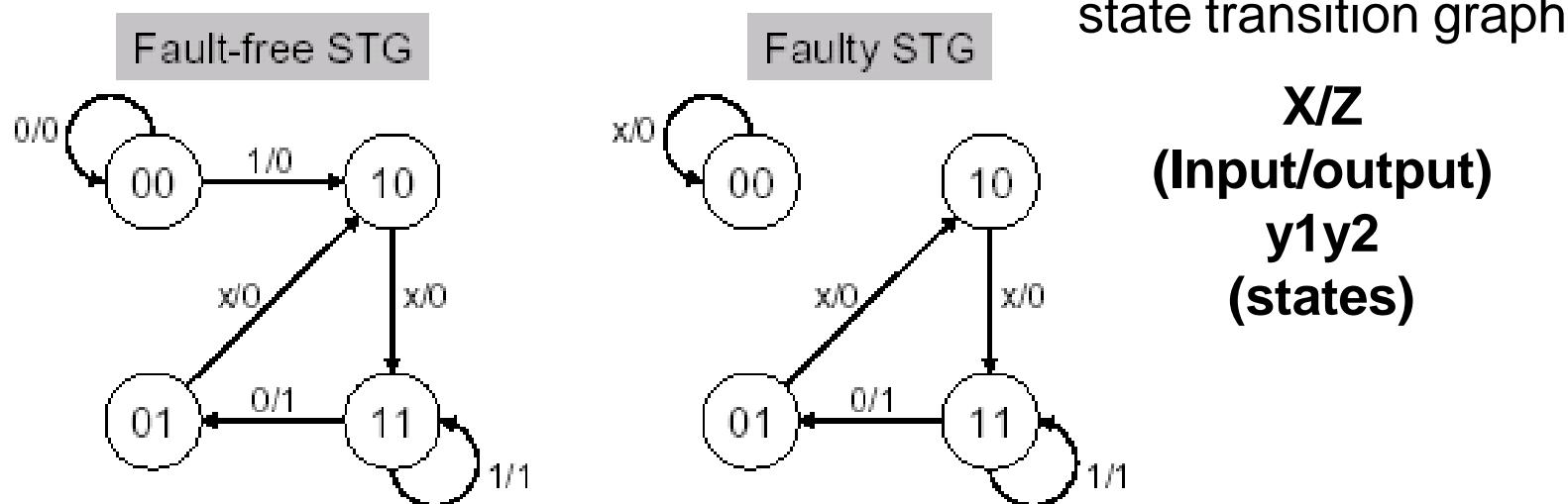
- Example
 - ◆ Mod 3 counter (BA Fig. 8.12)
 - $10 \rightarrow 00 \rightarrow 01 \rightarrow 10 \rightarrow \dots$

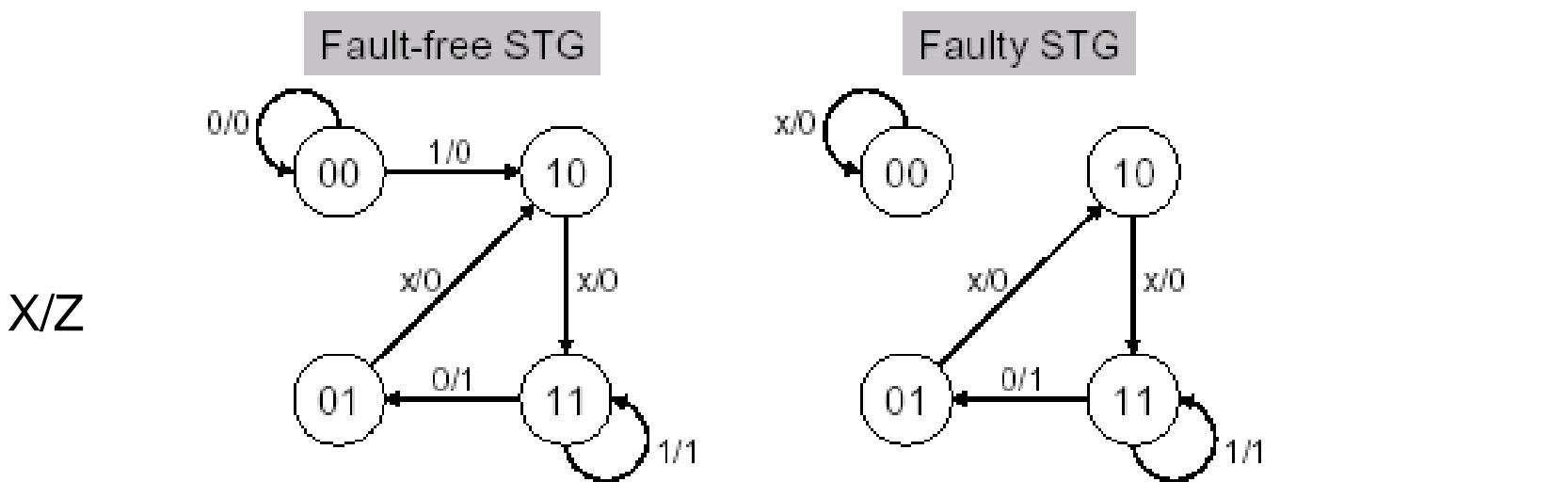


Cannot Find Initialization Sequence

② Potentially Detected Faults

- **DEF:** faults that may or may not be detected
 - ◆ Also see Video 5.7
- Example: detection of fault depends on the power-up states
 - ◆ $Y_1 = xy_1y_2 + y_1'y_2' + y_1'y_2$ (+ $xy_1'y_2'$) faulty STG missing term
 - ◆ $Y_2 = y_1y_2 + y_1y_2'$
 - ◆ $Z = y_1y_2$





- **{0 1 1}** initializes the circuit to state 11
- Good response to input **{0110}** is
 - ◆ $z = 1001$

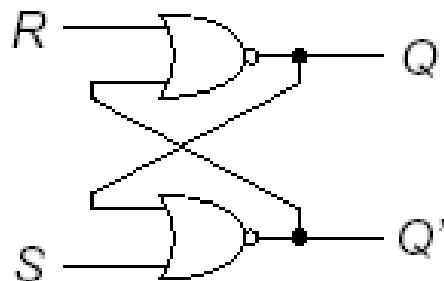
- **{0 1 1}** cannot initialize circuit
- Response at z to **{0110}**:
 - ◆ Power-up state 00,
 - $z = 0000$
 - fault detected
 - ◆ Power-up state 01,10, or 11
 - $z = 1001$
 - fault **NOT** detected

Fault Detection is Uncertain

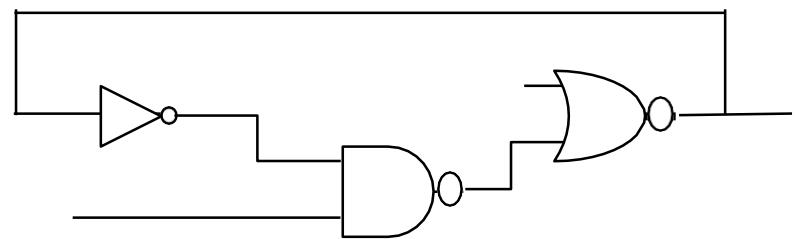
③ Asynchronous Circuits

- No explicit clock. Signals can change asynchronously
- Timing can be difficult to model
 - ◆ Test patterns generated may cause *races* and *hazards*
 - ◆ Need to verify test sequence with a fault simulator
- Example: Circuits with combinational loop

local feedback



global feedback



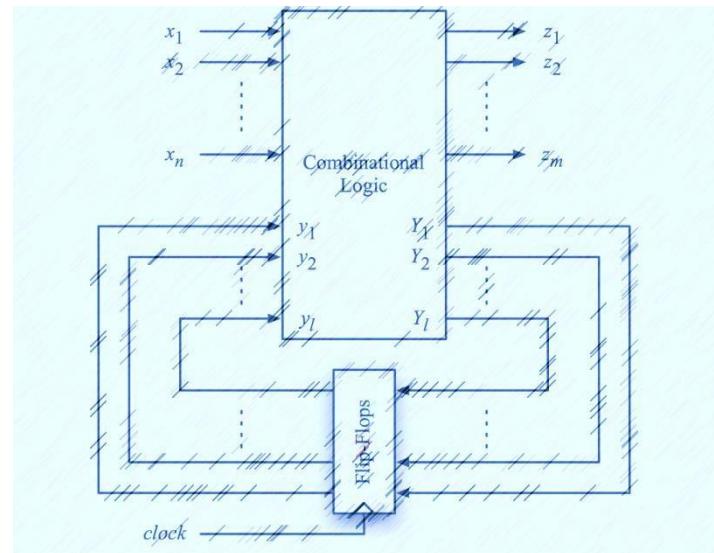
QUIZ

Q: Suppose you are a designer. Which of the following circuits you should avoid in order to avoid sequential ATPG?

- A) Combinational circuits with feedback loops
- B) Non-scan flip-flops without reset pins (video 11.8)
- C) Circuits with many different types of flip-flops
- D) Circuits with SRAM memories

Sequential ATPG

- Introduction
- Time-frame expansion methods
- Simulation-based methods*
- **Issues of Sequential ATPG***
- **Conclusions**



Concluding Remarks

- Sequential ATPG
 - ◆ Generate PI patterns, observe PO. No scan allowed
- Benefits
 - ◆ Enable at-speed testing
 - ◆ Handles partial scan or non-scan circuits
- Problems
 - ◆ Low fault coverage, long run time, large memory
- Techniques
 - ◆ Time frame expansion (EBT, BACK, Extended-D ...)
 - ◆ Simulation (CONTEST)
- Current DFT & ATPG Practice
 - ◆ Use as much combinational ATPG as possible
 - ◆ Use sequential ATPG only when necessary

Sequential ATPG is Difficult. Need DfT! (Ch11)

References

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- [Marlett 78] Marlett, Ralph A. "EBT: A comprehensive test generation technique for highly sequential circuits," Proceedings of the 15th Design Automation Conference. IEEE Press, 1978.
- [Muth 76] P. Muth "A nine-valued circuit model for test generation," IEEE Trans. Comput., 25 (6), pp. 630–636, 1976.
- [Huffman 53] D. A. Huffman, "The Synthesis of Sequential Switching Circuits," MIT Thesis, 1953.

Commercial Tools

- **Mentor Graphics**
 - ◆ Flextest
- **Synopsys**
 - ◆ Tetramax
- **Syntest**
 - ◆ turboscan

Academic Tools

- Time-Frame Expansion
 - ◆ ESSENTIAL [89]
 - ◆ FASTEST[89]
 - ◆ HITEC [Niermanh & Patel 91]
 - ◆ Lee-Reddy [91]
- Genetic Algorithm
 - ◆ CRIS [Saab & Abraham 96]
 - ◆ GATEST [Rudnick 97]
 - ◆ GATTO [96]
 - ◆ STRATEGATE [97]