

# UEC747: ANTENNA AND WAVE PROPAGATION

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Lecture 11: Antenna Parameters

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## 2.2 Radiation Pattern

### Antenna (radiation) pattern

- A **mathematical function** or a **graphical representation** of the **radiation properties** of the antenna as a function of space coordinates.
- Determined in the **far-field region**
- Represented as a function of the **directional coordinates**.

### Radiation properties

- power flux density
- Radiation intensity
- Field strength
- Directivity
- Phase
- Polarization
- The radiation property of most concern is the two- or three dimensional **spatial distribution of radiated energy** as a function of the **observer's position** along a path or surface of constant radius.

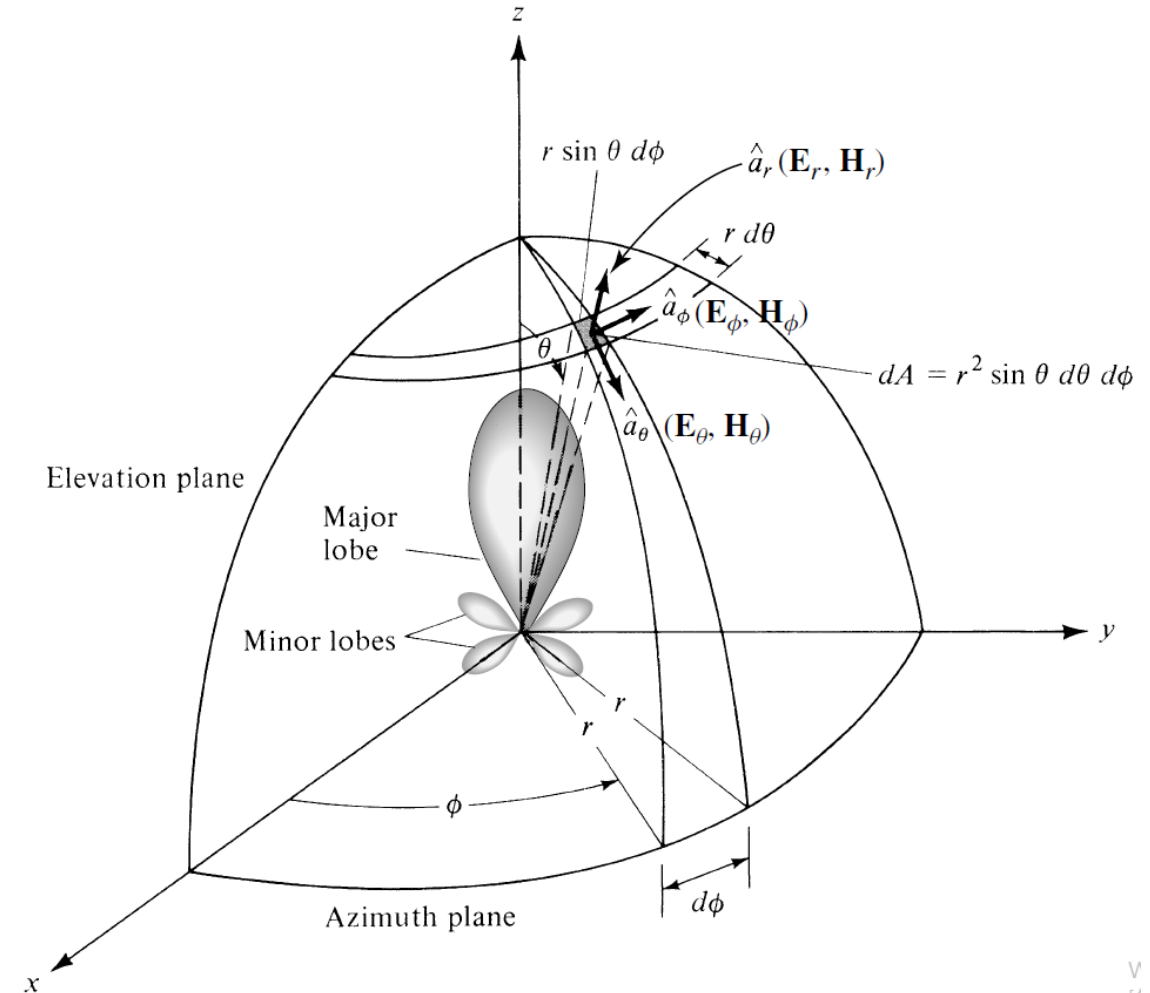
## 2.2 Radiation Pattern

An antenna radiation pattern is defined as "a mathematical function or a graphical representation of the radiation properties of the antenna as a function of space coordinates. ( $\theta$  and  $\phi$ ).

In most cases, the radiation pattern is determined **in the far field region**.

Radiation properties include power flux density, radiation intensity, field strength, directivity, phase or polarization."

- **Field pattern** : E & H fields' magnitude (**Linear scale**. Angular Space)
- **Power pattern** : Square of magnitude's of E&H fields (**Linear scale**. Angular Space)
- **Power pattern** : Magnitude of E & H fields (**dB scale**)



# Amplitude Radiation Pattern

- **Field Pattern:**

A plot of the field (either electric  $|\underline{E}|$  or magnetic  $|\underline{H}|$ ) on a *linear* scale

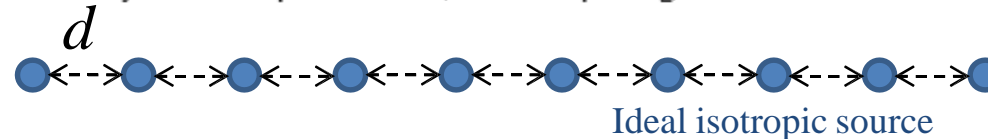
- **Power Pattern:**

A plot of the power (proportional to either the electric  $|\underline{E}|^2$  or magnetic  $|\underline{H}|^2$  fields) on a *linear* or *decibel (dB)* scale.

## 1.2 RADIATION PATTERN

- **Amplitude Field pattern**  
: A trace of the **received electric (magnetic) field** at a constant radius
  - **Amplitude Power pattern**  
: A graph of the spatial variation of the **power density** along a constant radius
  - Often these patterns are normalized with respect to their maximum value.
  - Power pattern is usually plotted on a logarithmic scale or more commonly in decibels (dB).
- To demonstrate these three radiation patterns, the two-dimensional normalized field pattern (*plotted in linear scale*), power pattern (*plotted in linear scale*), and power pattern (*plotted on a logarithmic dB scale*) of a **10-element linear antenna array of isotropic sources, with a spacing of  $d = 0.25\lambda$  between the elements**, are shown in Figure 1.2. 1
- free-space

Figure 1.2.1 10-element linear antenna array of isotropic sources, with a spacing of  $d = 0.25\lambda$  between the elements



To find the points where the pattern achieves its half-power ( $-3$  dB points), relative to the maximum value of the pattern, you set the value of

## 2-D Normalized *Field* $|\underline{E}_n|$ Pattern of a Linear Array

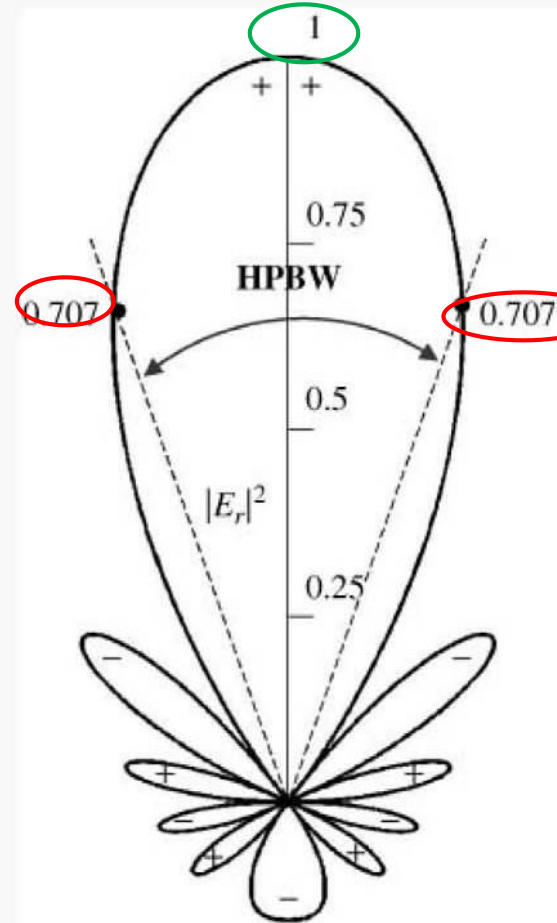
### Linear Scale

$N = 10$  elements

$d = \lambda/4$  spacing

HPBW =  $38.64^\circ$

**Fig. 2.2(a)**



(a) the field pattern at 0.707 value of its maximum.

(a)  $\text{dB} = 20\log(x) = -3$   
 $x = \frac{1}{\sqrt{2}} = 0.707$

## 2-D Normalized *Power* $|\underline{E}_n|^2$ Pattern of a Linear Arra

### Linear Scale

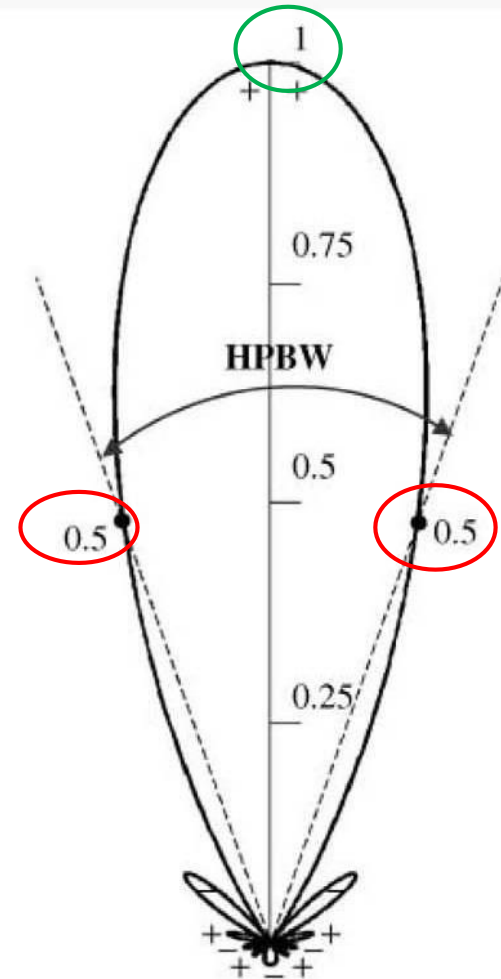
$N = 10$  elements

$d = \lambda/4$  spacing

HPBW =  $38.64^\circ$

Fig. 2.2(b)

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(b) the power pattern (in a linear scale) at its 0.5 value of its maximum, as shown in Figure 1.2b;

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(b)  $\text{dB} - 10\log(x) = -3$   
 $x = \frac{1}{2} = 0.5$



## 2-D Normalized *Power* $|\underline{E}_n|^2$ Pattern of a Linear Array

HPBW =  $38.64^\circ$   
at all the three  
patterns

*dB Scale*

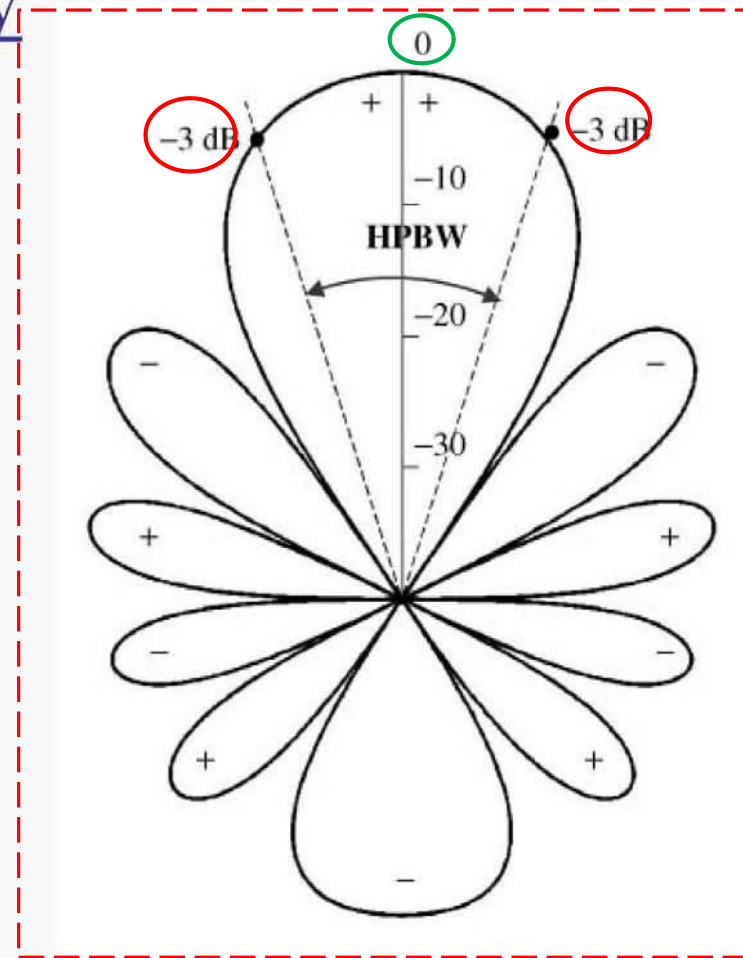
$N = 10$  element

$d = \lambda/4$  spacing

HPBW =  $38.64^\circ$

$$\begin{aligned} \text{(b) dB} - 10\log(x) &= -3 \\ x &= \frac{1}{2} = 0.5 \end{aligned}$$

**Fig. 2.2(c)**



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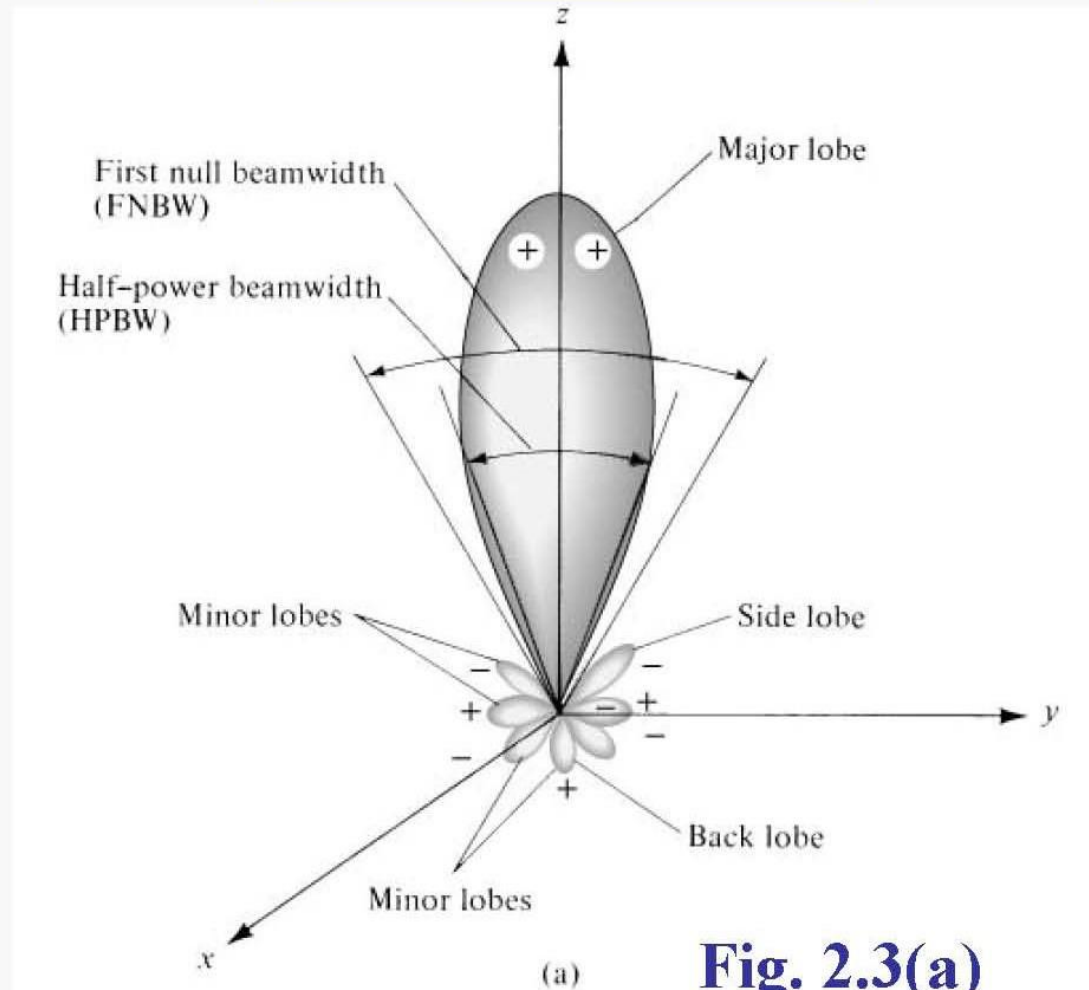
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and (c) the power pattern (in dB) at  $-3$  dB value of its maximum.

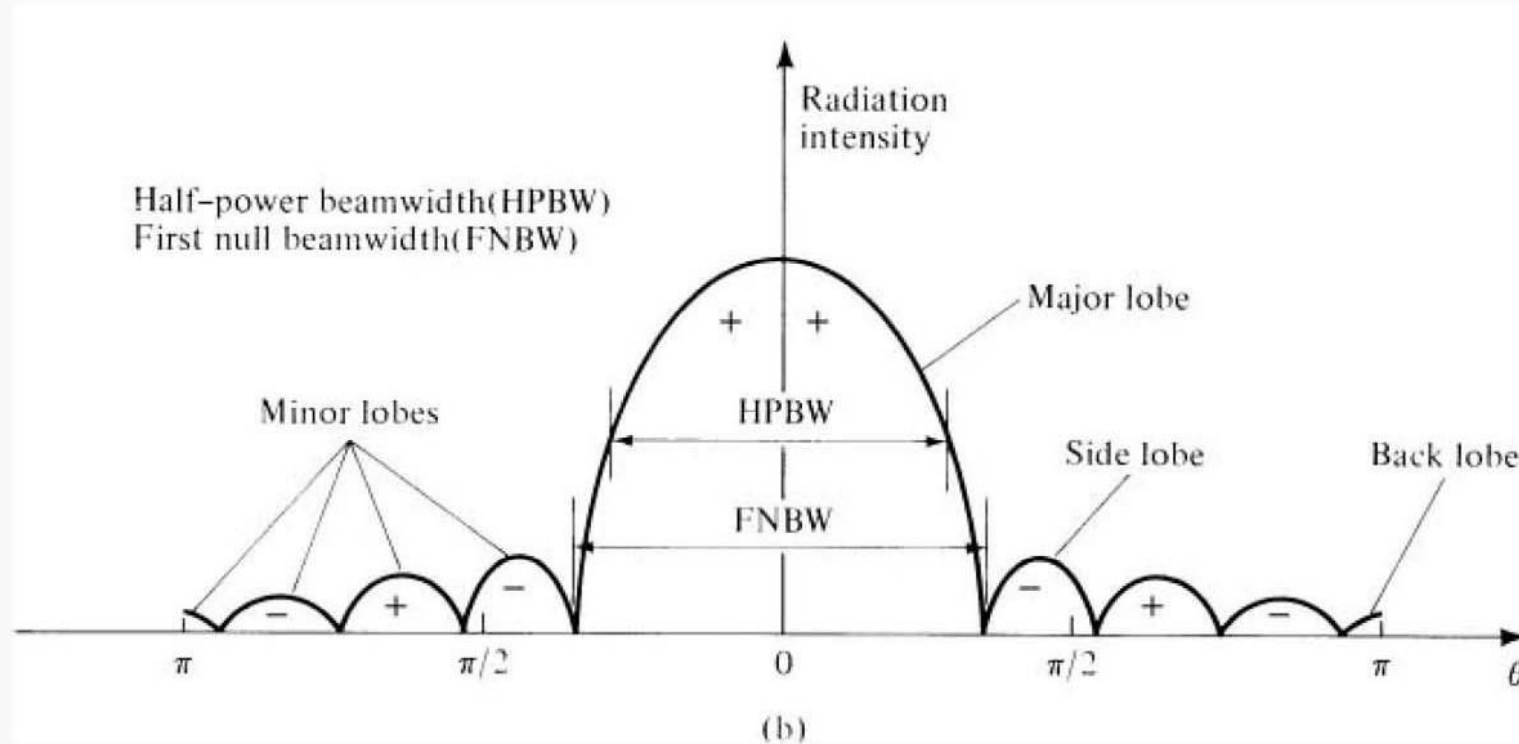


# Polar Pattern

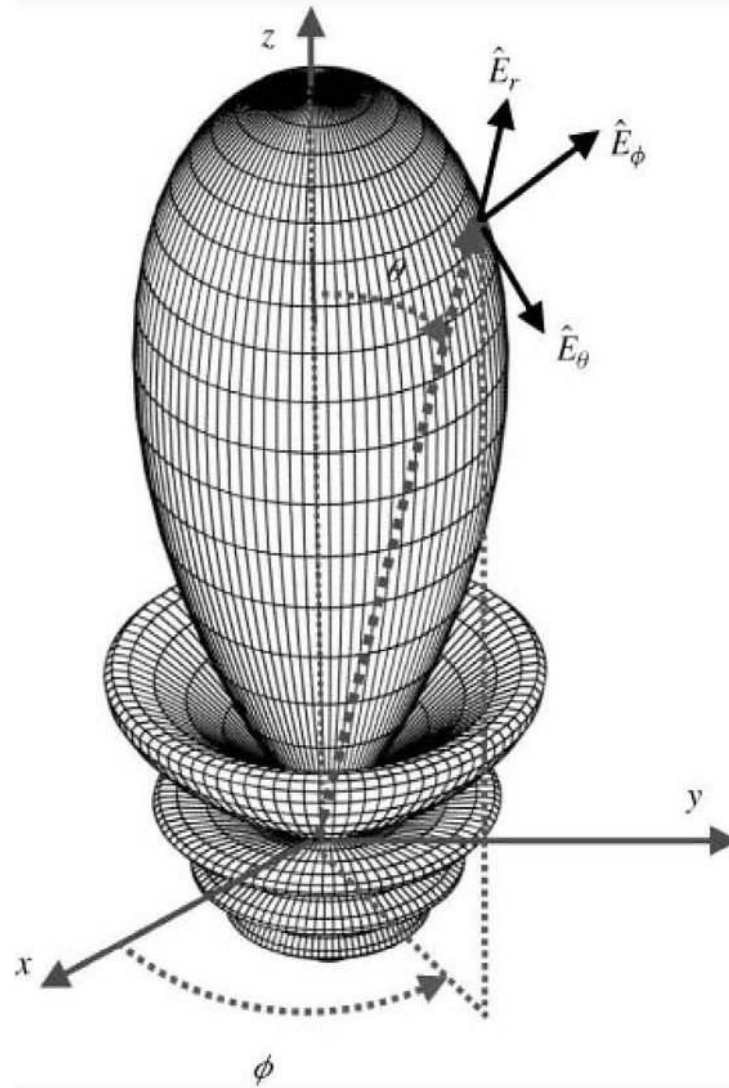


**Fig. 2.3(a)**

# Linear Pattern



**Fig. 2.3(b)**



## Normalized 3-D Amplitude *Field* Pattern of Linear Array

### Linear Scale

$$N = 10, d = \lambda/4$$

$$\begin{aligned} \underline{E}(r, \theta, \phi) |_{r=r_c} = & \hat{a}_r E_r(r_c, \theta, \phi) \\ & + \hat{a}_\theta E_\theta(r_c, \theta, \phi) \\ & + \hat{a}_\phi E_\phi(r_c, \theta, \phi) \end{aligned}$$

$$|\underline{E}| = \sqrt{|E_r|^2 + |E_\theta|^2 + |E_\phi|^2}$$

**Fig. 2.4**

# Amplitude Radiation Pattern

1. Isotropic,  
Directional,  
Omnidirectional
2. Principal patterns
3. Pattern lobes

## 1.2.2 Isotropic, Directional, and Omnidirectional Patterns

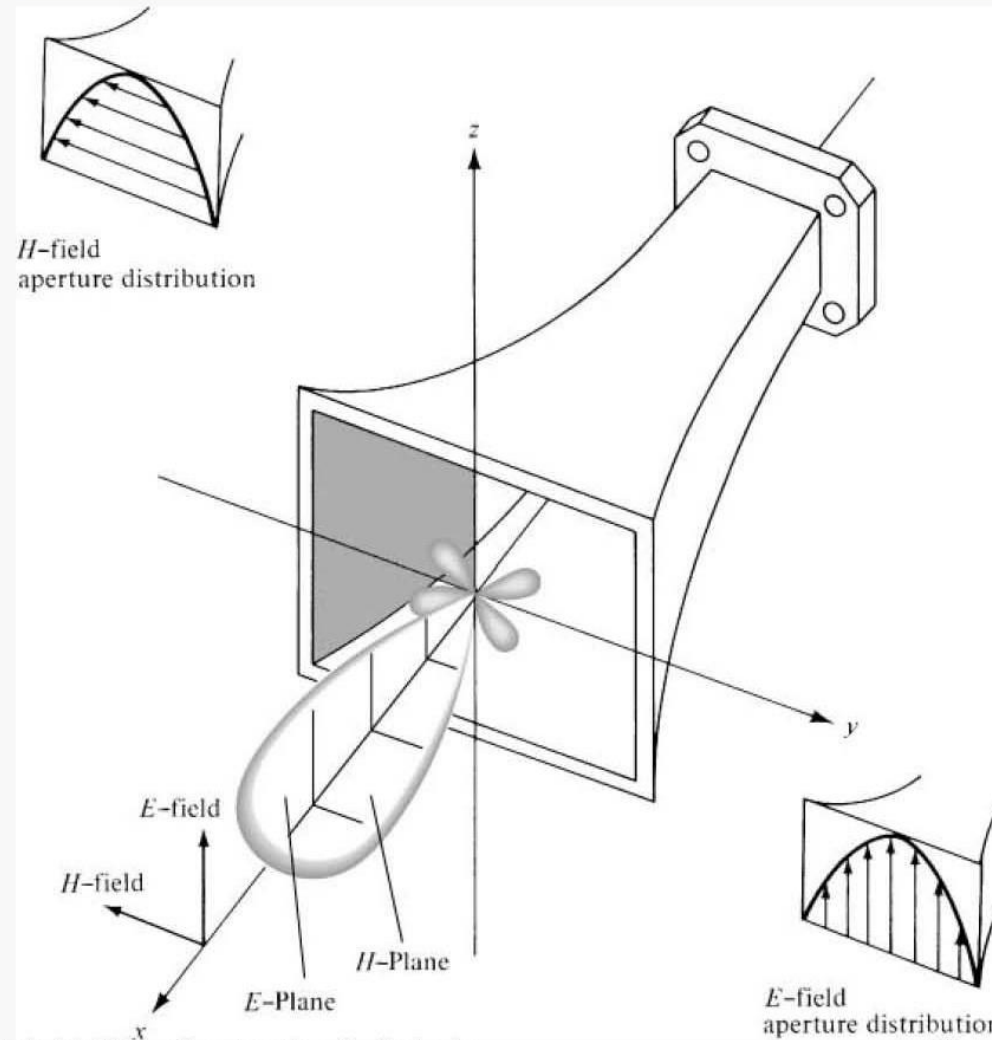
### 1) Isotropic pattern

- A hypothetical lossless antenna having equal radiation in all directions.
- Although it is ideal and not physically realizable, it is often taken as a reference for expressing the directive properties of actual antennas. Ex) dBi

# Directional Pattern of a Horn

## 2) Directional Pattern

- A directional antenna is one having the property of radiating or receiving electro-magnetic waves **more effectively in some directions** than in others.



**Fig. 2.5**

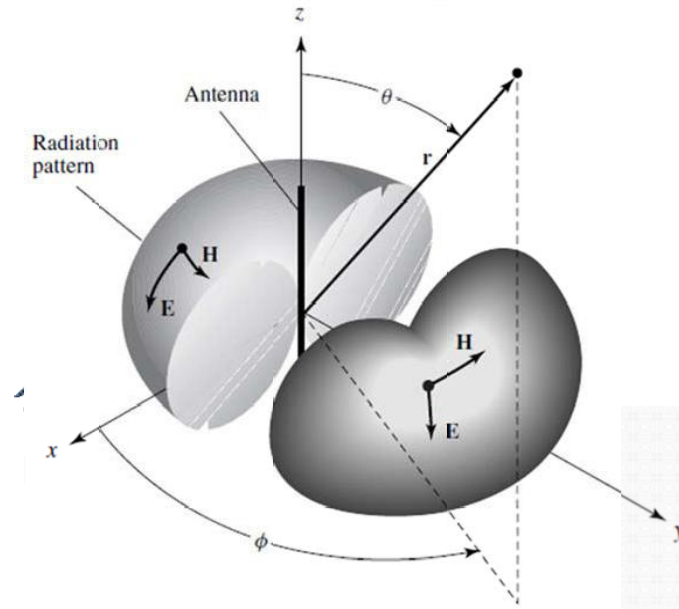
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## ) Omnidirectional Pattern

- having an **essentially non-directional pattern** in a given plane (in this case in azimuth) and a **directional pattern in any orthogonal plane**.



principal E-planes (elevation planes;  $\phi = \phi_c$ ) and one principal H-plane (azimuthal plane;  $\theta = 90^\circ$ ).

An illustration is shown in Figure 2.5. For this example, the x-z plane (elevation plane;  $\phi = 0$ ) is the principal E-plane and the x-y plane (azimuthal plane;  $\theta = \pi/2$ ) is the principal H-plane. Other coordinate orientations can be selected. The omnidirectional pattern of Figure 2.6 has an infinite number of

### 1.2.3 Principal Patterns

- The Three-dimensional pattern is measured and recorded in a series of two-dimensional patterns.
- For most practical applications, a few plots of the pattern as a function of  $\theta$  for some particular values of  $\phi$ , plus a few plots as a function of  $\phi$  for some particular values of  $\theta$ , give most of the useful and needed information.
- For a **linearly** polarized antenna, performance is often described in terms of its **principal E- and H-plane patterns**.
  - E-plane : The plane **containing the electric-field vector** and the direction of maximum radiation.
  - H-plane : The plane containing **the magnetic-field vector** and the direction of maximum radiation

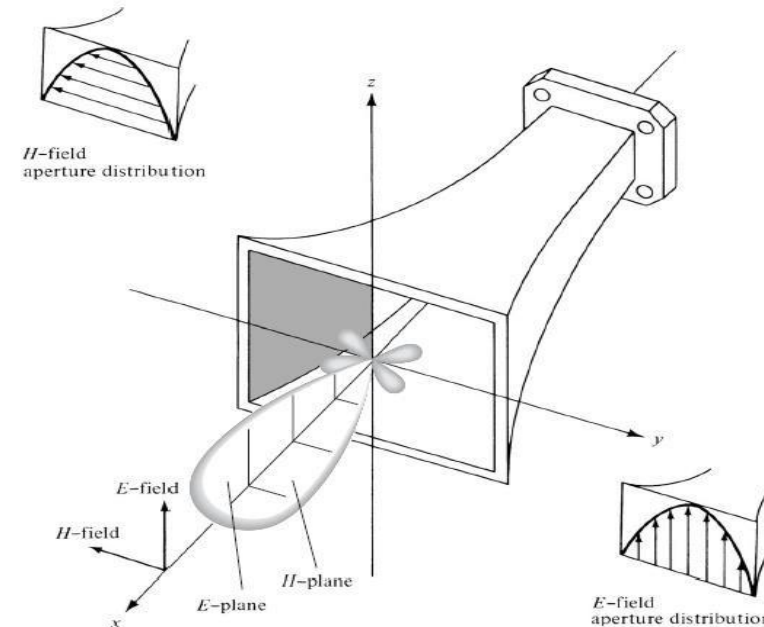
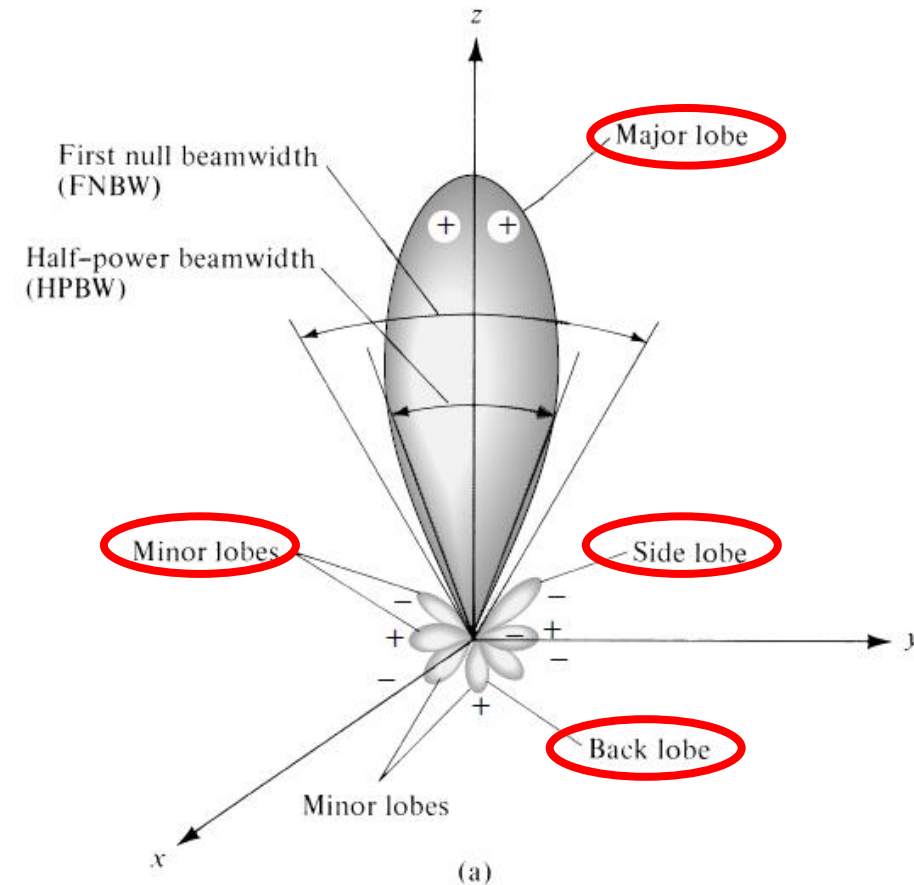


Figure 1.5 Principal E- and H-plane patterns for a pyramidal horn antenna.

# Radiation Pattern Lobes

- Radiation lobe : portion of the radiation pattern bounded by regions of relatively weak radiation intensity
- major lobe ( main beam, **front lobe\***) : the radiation lobe containing the direction of **maximum radiation**
- minor lobe : any lobe **except a major lobe**.
  - usually represent radiation in undesirable directions.
  - ★ should be minimized  
(for careful design, side lobe ratio(level) < -30 dB)
  - \*\* Especially, In most radar system, low side lobe ratios are very important
- side lobe : a radiation lobe in any direction **other than the intended lobe**.
- back lobe : a radiation whose axis makes **an angle of 180° with respect to the beam of an antenna**.

## - Radiation Pattern Lobes

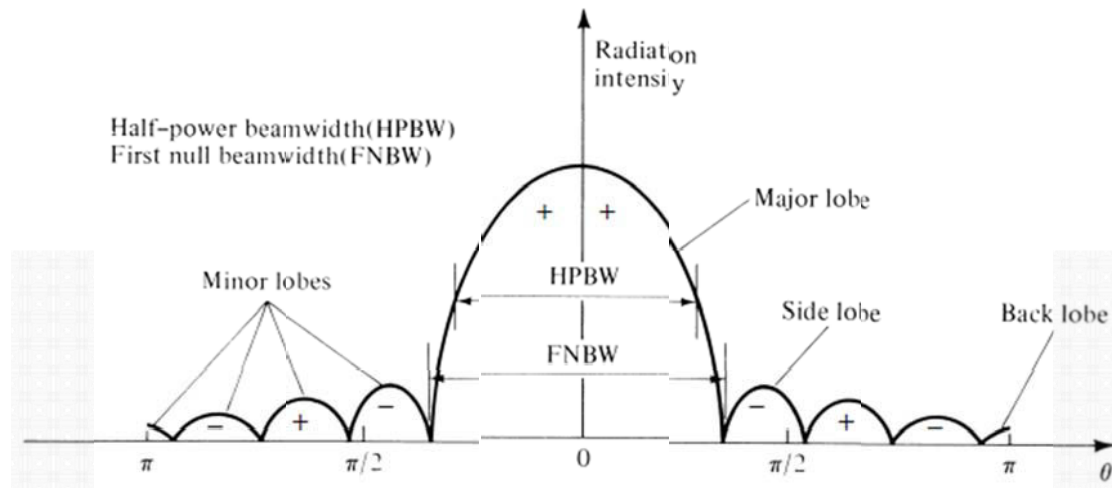


**Figure 1.3** (a) Radiation lobes and beamwidths of an antenna pattern. (b) Linear plot of Power pattern and its associated lobes and beamwidths.

## Radiation Pattern Lobes

: Various parts of a radiation pattern are referred to as lobes, which may be subclassified into **major or main, minor, side, and back lobes**.

Some are of greater radiation intensity than others, but all are classified as lobes. Figure 2.3(b) illustrates a linear two-dimensional pattern where the same pattern characteristics are indicated.



●A **major lobe (main beam)** is defined as “the radiation lobe containing the direction of maximum radiation.” In Figure 2.3 the major lobe is pointing in the  $\theta = 0$  direction. In some antennas, such as **split-beam antennas**, there may exist more than one major lobe.

●A **minor lobe** is any lobe except a major lobe.

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●A **side lobe** is “a radiation lobe in any direction other than the intended lobe.” Usually a side lobe [is adjacent to the main lobe](#)

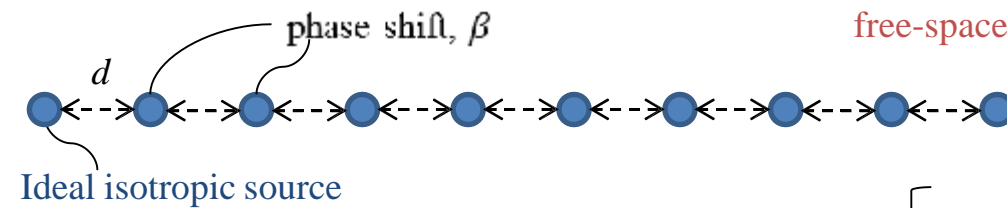
●A **back lobe** is “a radiation lobe whose axis makes an angle of approximately  $180^\circ$  with respect to the beam of an antenna.”

Minor lobes usually represent radiation in undesired directions and should be minimized. Side lobes are the largest minor lobes.

## 1.2.1 Radiation Pattern Lobes

*Examples)*

A normalized three-dimensional far-field amplitude pattern, plotted on a linear scale, of a 10-element linear antenna array of isotropic sources with a spacing of  $d = 0.25\lambda$  and progressive phase shift  $\beta = -0.6\pi$  between the elements is shown Figure 1. 4.



- This pattern has one major lobe, five minor lobes, and one back lobe.
- Three electric-field components ( $E_r$ ,  $E_\theta$ ,  $E_\phi$ ) at each observation point on the surface of constant radius  $r$
- In the far field, the radial  $E_r$  component is zero, or vanishingly small compare to either on, or both, of the other two components.

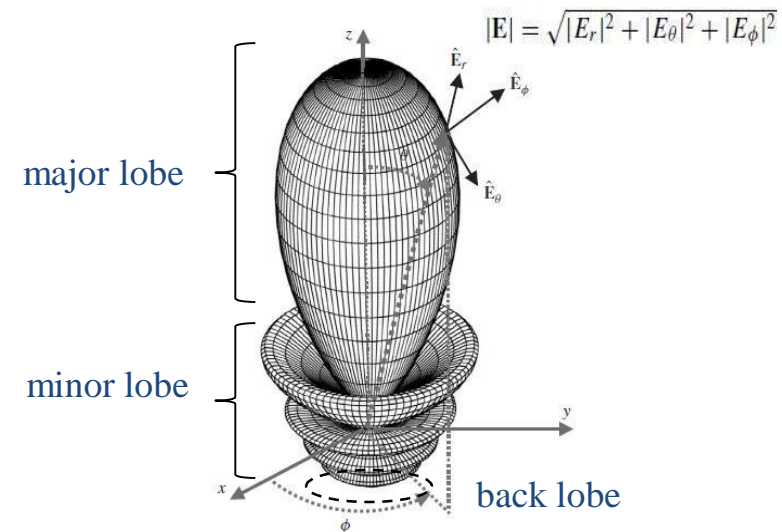


Figure 1.4 Normalized three-dimensional amplitude field pattern (in linear scale) of a 10-element linear array antenna with a uniform spacing of  $d = 0.25\lambda$  and progressive phase shift  $\beta = -0.6\pi$  between the elements.



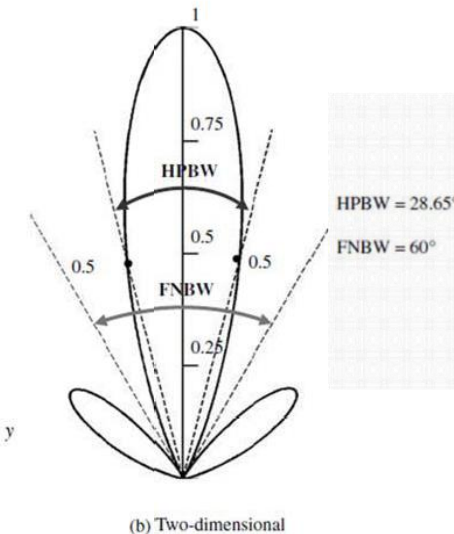
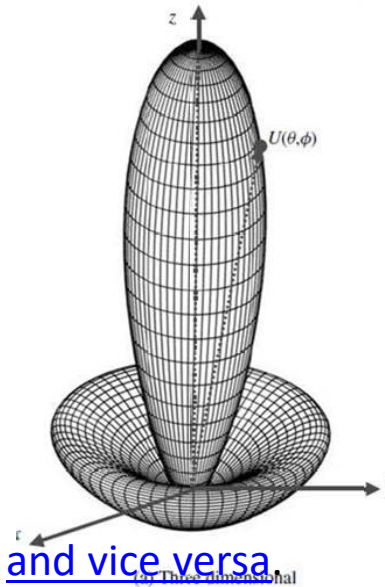
# BEAMWIDTH

The beamwidth of a pattern is defined: the angular separation between two identical points on opposite side of the pattern maximum.

1. Half-Power Beamwidth (HPBW).
2. First-Null Beamwidth (FNBW).

- Often, the term beamwidth usually refers to HPBW.

- The beamwidth is a trade-off between it and the side lobe level. The beamwidth decreases, the side lobe increases and vice versa.



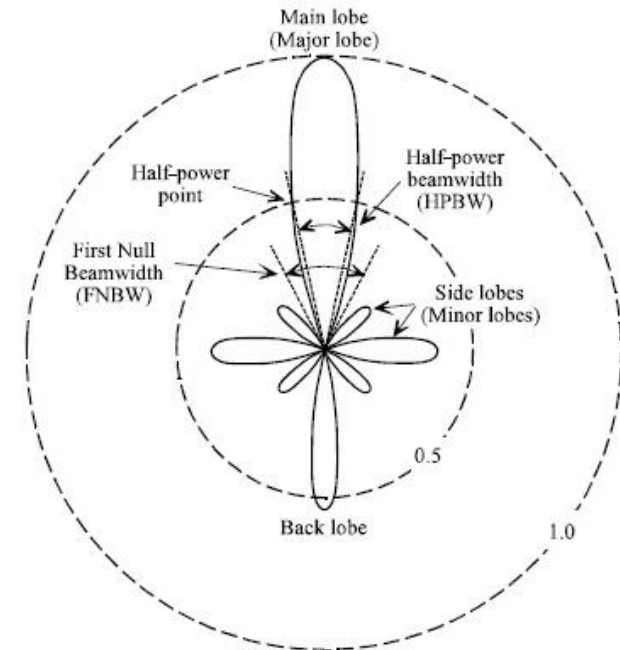
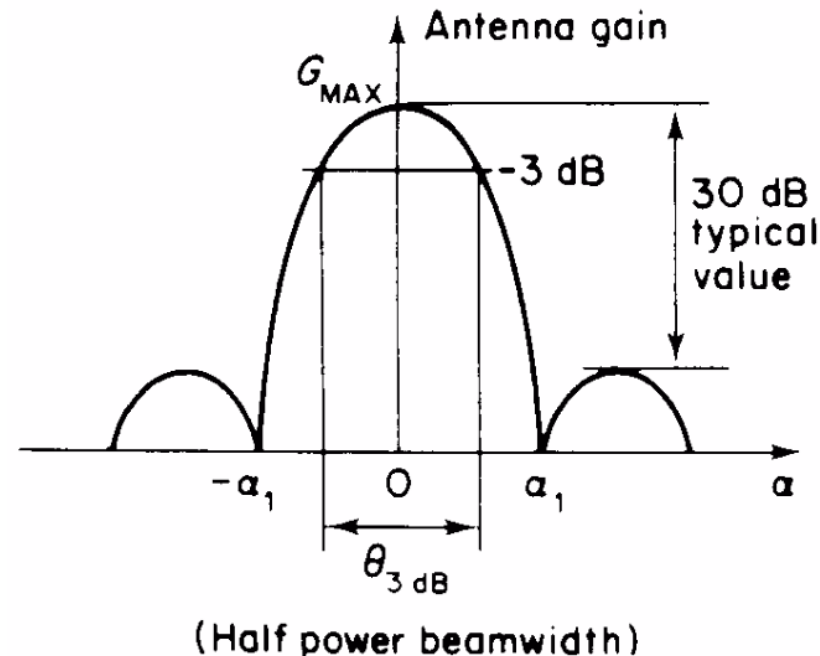
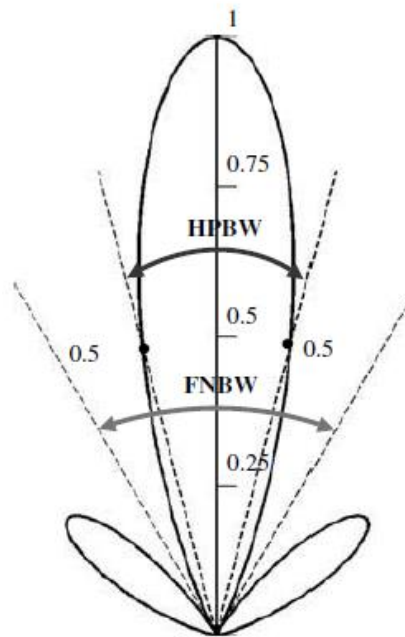
- The beamwidth of the antenna is also used to describe the **resolution capabilities to distinguish two adjacent radiating sources or targets.**

## 2.5 Beamwidth

**Beamwidth** - The **angular separation** between two identical points on opposite side of the pattern maximum.

**Half-Power Beamwidth (HPBW)** - In a plane containing the direction of the maximum of a beam, the angle between the two directions in which the radiation intensity is **one-half value** of the beam.

**First-Null Beamwidth (FNBW)** - The angular separation between the **first nulls** of the pattern.



## 2.5 Beamwidth

Beamwidth of the antenna is used to describe the **resolution capabilities** of the antenna to distinguish between two adjacent radiating sources or radar targets.

$$FNBW / 2 \approx HPBW$$

$$\text{Ex) } U(\theta) = \cos^2(\theta) \cos^2(3\theta), \quad (0^\circ \leq \theta \leq 90^\circ, \quad 0^\circ \leq \phi \leq 360^\circ)$$

a. HPBW

$$U(\theta)|_{\theta=\theta_h} = \cos^2(\theta) \cos^2(3\theta)|_{\theta=\theta_h} = 0.5$$

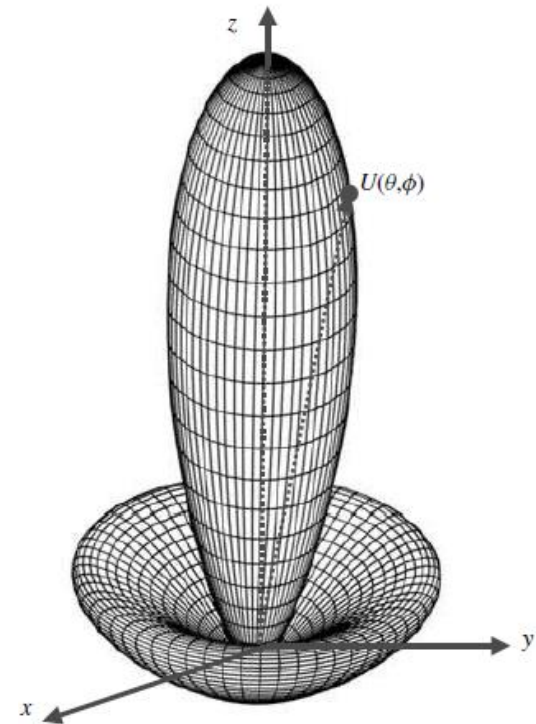
$$\cos(\theta_h) \cos(3\theta_h) = 0.707$$

$$\theta_h = \cos^{-1} \left( \frac{0.707}{\cos 3\theta_h} \right)$$

$$\theta_h \approx 0.25 \text{ radians} = 14.325^\circ$$

$$HPBW = 2\theta_h$$

$$\approx 0.5 \text{ radians} = 28.65^\circ$$



## 2.5 Beamwidth

Ex)  $U(\theta) = \cos^2(\theta) \cos^2(3\theta)$ ,  $(0^\circ \leq \theta \leq 90^\circ, 0^\circ \leq \phi \leq 360^\circ)$

b. FNBW

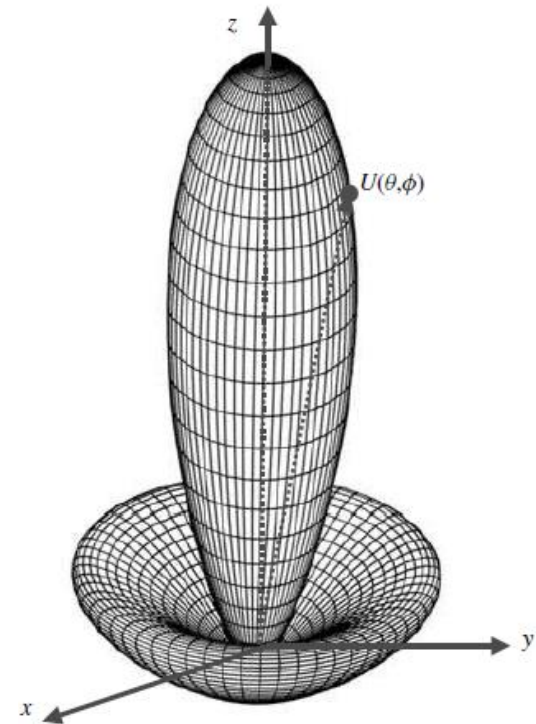
$$U(\theta)|_{\theta=\theta_n} = \cos^2(\theta) \cos^2(3\theta)|_{\theta=\theta_n} = 0$$

i.  $\cos \theta_n = 0 \Rightarrow \theta_n = \cos^{-1}(0) = \frac{\pi}{2} \text{ radians} = 90^\circ$

ii.  $\cos 3\theta_n = 0 \Rightarrow \theta_n = \frac{1}{3} \cos^{-1}(0) = \frac{\pi}{6} \text{ radians} = 30^\circ$

The one with the **smallest value** leads to the FNBW.

$$FNBW = 2\theta_n = \frac{\pi}{3} \text{ radians} = 60^\circ$$



# Field Regions

The space surrounding an antenna is usually subdivided into three regions: reactive near-field, radiating near-field (Fresnel) region and far-field (Fraunhofer) regions

## 1. Reactive near-field region

For most antennas, the outer boundary of this region is  $R < 0.62\sqrt{D^3/\lambda}$ ,  $\lambda$  is the wavelength and  $D$  is the largest dimension of the antenna.

- The reactive field predominates
- For a very short dipole, or equivalent radiator, the outer boundary is commonly taken to  $\lambda/2\pi$ .

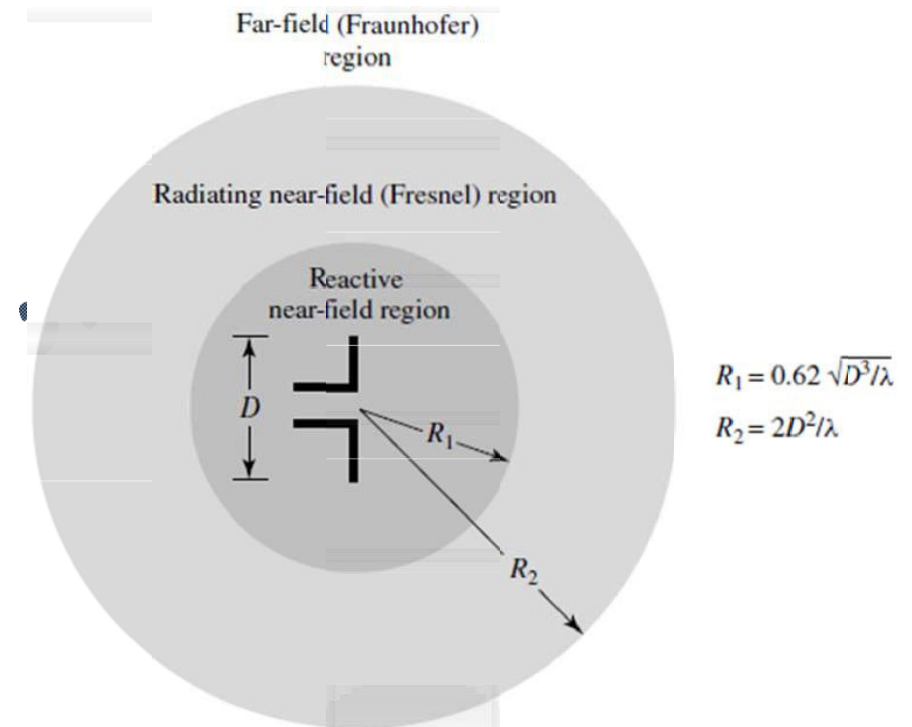


Figure 2.7 Field regions of an antenna.

## 2. Radiating near-field (Fresnel) region

Defined as “that region of the field of an antenna between the reactive near-field region and the far-field region

- a. Radiation fields predominate
- b. The angular field distribution is dependent upon the distance from the antenna.
- c. If the antenna has a maximum overall dimension which is very small compared to the wavelength, this field region may not exist.

The region is limited by

$$0.62\sqrt{D^3/\lambda} < R < 2D^2/\lambda.$$

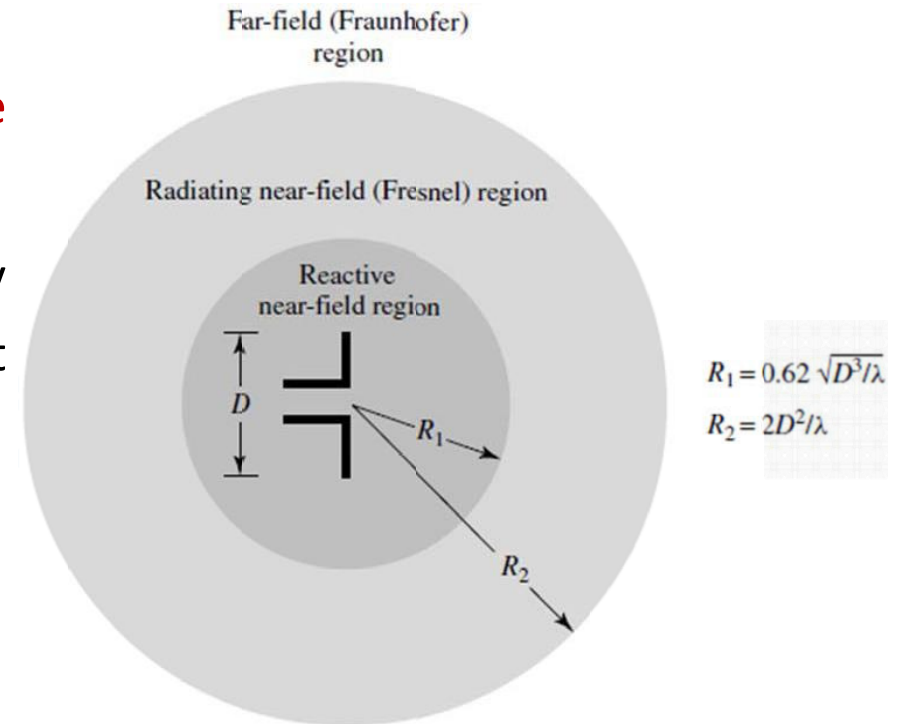


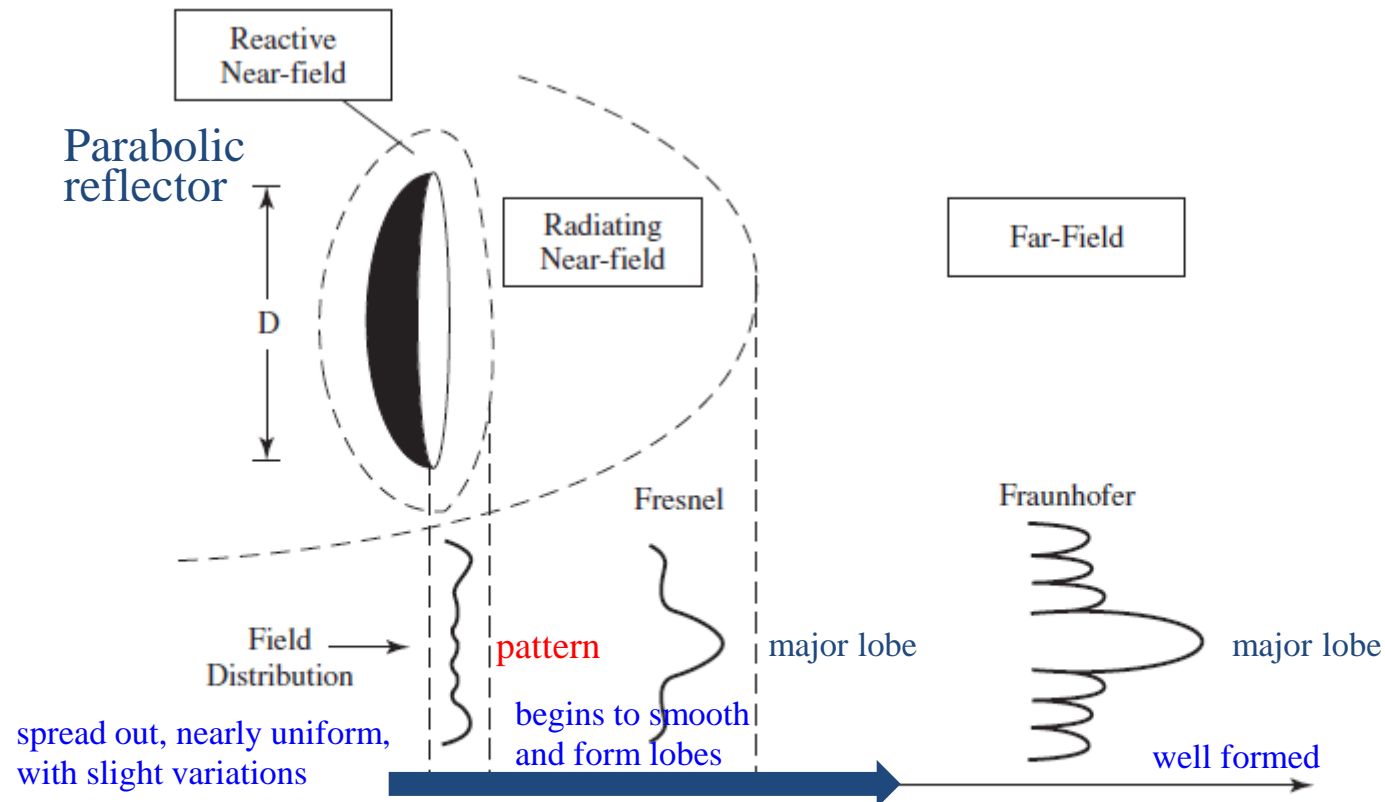
Figure 2.7 Field regions of an antenna.



### 3. Far-field (Fraunhofer) region

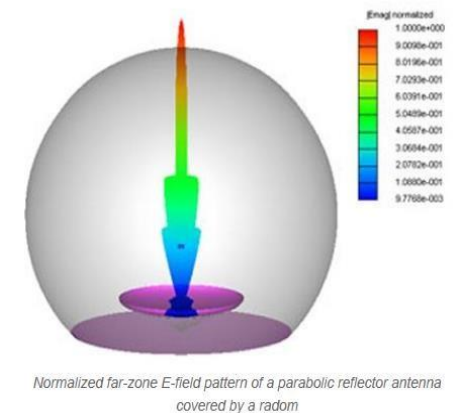
- a. The angular field distribution is essentially independent of the distance from the antenna.
- b. The far-field region is taken to exist at distances greater than  $2D^2/\lambda$  from the antenna.

As the observation is moved to the radiating near-field region, **the pattern begins to smooth and form lobes**. In the far-field region, the **pattern is well formed**, usually consisting of few minor lobes and one, or more, major lobes.



**Figure 1.8** Typical changes of antenna amplitude pattern shape from reactive near field toward the far field. (From: Y. Rahmat-Samii, L. I. Williams, and R. G. Yoccarino, The UCLA bi-polar planar-near-field antenna measurement and diagnostics range, *IEEE Antennas Propag. Mag.*, Vol. 37, No. 6, December 1995. Copyright © 1995 IEEE.)

### E field pattern of Parabolic Reflector Antenna



Reference : Integrated engineering software  
<https://www.integratedsoft.com/applications/rf-microwave-antennas/reflector-antennas>

Figure 2.9 shows three patterns of a parabolic reflector calculated at distances of  $R = 2D^2/\lambda$ ,  $4D^2/\lambda$ , and infinity.

It is observed that the patterns are almost identical, except for some differences in the pattern structure around the first null and at a level below 25 dB. Because infinite distances are not realizable in practice, the most commonly used criterion for minimum distance of far-field observations is  $2D^2/\lambda$ .

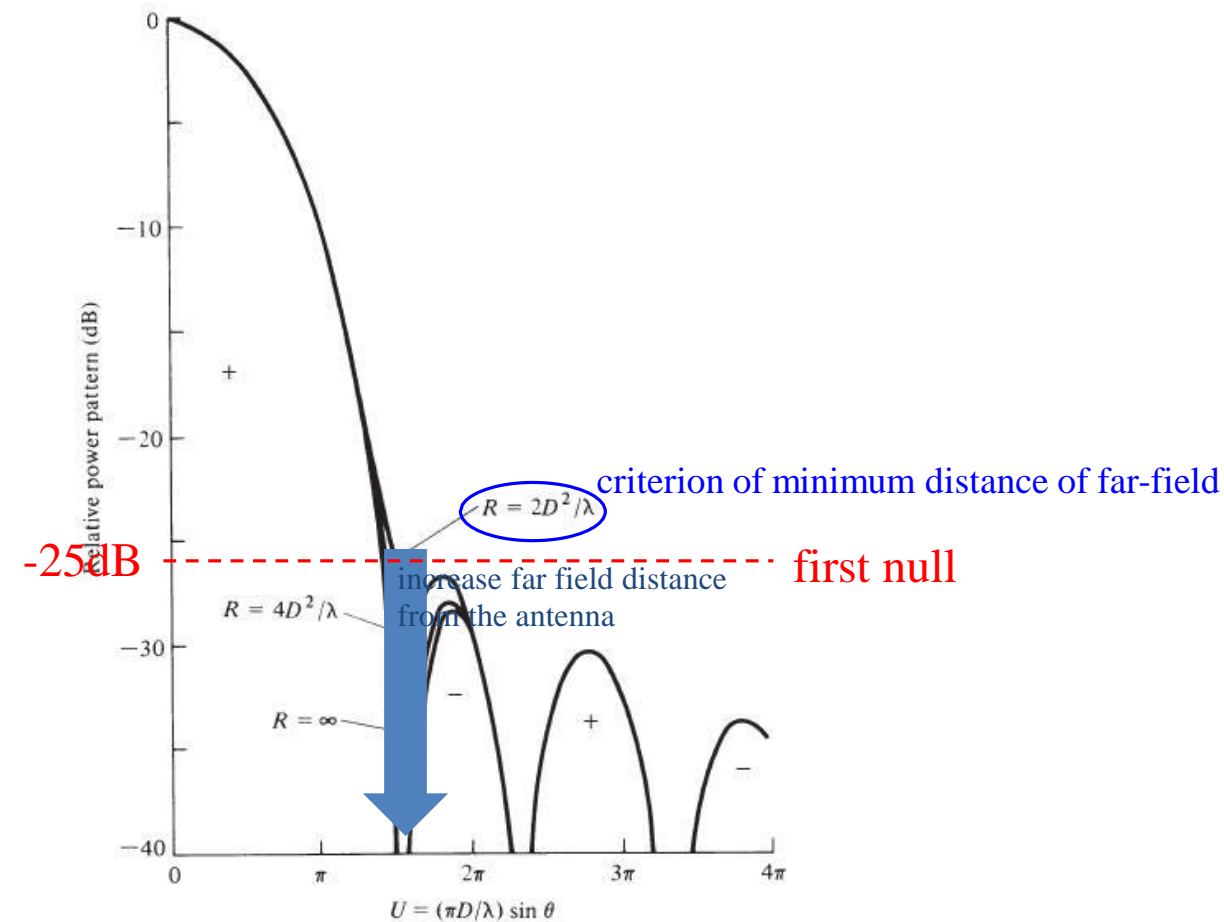


Figure 1.9 Calculated radiation patterns of a paraboloid antenna for different distances from the antenna. (From Ref. 6.)

**Thank you**