

Q2.

$$Im_new = (-1)^{x+y} \times (\text{Real}(\text{IDFT}(\text{Complex conjugate}(\text{DFT}((-1)^{x+y} \times Im))))))$$

From observation,

$$\begin{aligned} Im_new &= \text{water_image}(\text{mirror_image}(Im)) \\ &= \text{the image obtained by reflecting } Im \text{ both along } x\text{-axis and } y\text{-axis} \\ &= \text{the image obtained by reflecting } Im \text{ w.r.t. the origin} \end{aligned}$$

Now we know that complex conjugate of a complex number $c = a + jb$ is $\bar{c} = a - jb$ — (1)

$$\begin{aligned} Im_new &= \mathcal{F}^{-1}[F^*(u, v)] \\ &= \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} F(u, v) e^{-j2\pi (ux/M + vy/N)} \\ &= \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} F(u, v) e^{j2\pi (u(-x)/M + v(-y)/N)} \\ &= f(-x, -y) \quad (\text{where } Im = f(x, y)) \\ &= \text{mirror of } Im = f(x, y) \text{ about the origin.} \end{aligned}$$