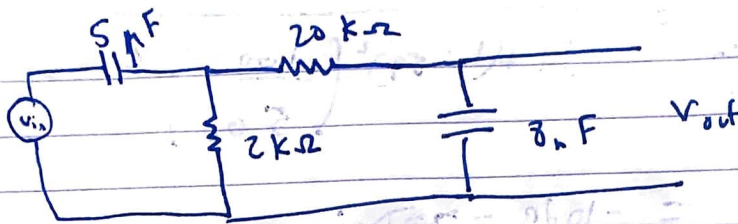


# HW-5 CMPE-460

Answer 1mk



$$\left| \frac{v_{out}}{v_{in}} \right| = \frac{1}{\sqrt{1 + (\omega RC)^2}} = 0.707 \Rightarrow F_H$$

Low Pass

$$\frac{1}{\sqrt{1 + ((2\pi f)(20k)(8n))^2}} = 0.707$$

$$\frac{1}{(0.707)^2} = 1 + ((40k)(8n)(f)(\pi))^2$$

$$f_H = 995.3 \text{ Hz}$$

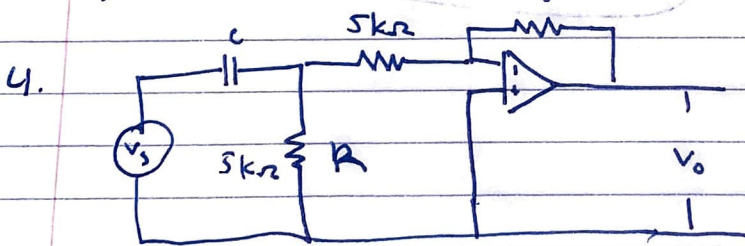
$$f_H = 994.37$$

High Pass

$$f_L = \frac{1}{2\pi RC} = \frac{1}{2\pi (5\mu F)(2k\Omega)} = 15.92 \text{ Hz} = f_L$$

$$f_c = \sqrt{f_H f_L} = 125.824 \text{ Hz} = f_{center}$$

2. , 3. (see other images / matlab script)



$$f_c = \frac{1}{2\pi RC} = \frac{1}{2\pi (5k\Omega)(C)} = 318 \text{ Hz}$$

$$C = 100 \text{ nF} = 0.100 \mu F$$

$$\frac{v_{out}}{v_{in}} = \frac{R_F}{R_{in}} = 4 \text{ dB}$$

$$= 20 \log \left( \frac{v_{out}}{v_{in}} \right)$$

$$1.585 \cdot (5k\Omega) = 7924 \Omega$$

$$\Rightarrow \frac{v_{out}}{v_{in}} = 1.585$$

$$|H(j\omega)| = \frac{1}{\sqrt{1 + \epsilon^2 \left(\frac{\omega}{\omega_p}\right)^{2n}}} = \frac{1}{\sqrt{1 + (1.259)^2 \left(\frac{1000}{500}\right)^{2n}}}$$

6.  $20 \text{ dB} = 20 \log(\epsilon)$

$$\epsilon = 1.259$$

$$= -10 \text{ dB} = 20 \log(\epsilon) = 31.62$$

$$-10 \text{ dB} = 20 \log\left(\frac{V_{\text{out}}}{V_{\text{in}}}\right)$$

$$\frac{V_{\text{out}}}{V_{\text{in}}} = 0.316$$

$$\left(\frac{1000}{500}\right)^{2n} = 5.678$$

$$n = 1.253$$

→ at least 2nd order Butterworth

7.  $0.707 = \frac{1}{\sqrt{1 + (0.25) \left(\frac{\omega}{500}\right)^{2(5)}}}$

$$0.707 = \frac{1}{\sqrt{1 + (0.25) \left(\frac{\omega}{500}\right)^{10}}}$$

$$\frac{1}{2} = \frac{1}{1 + (0.25) \left(\frac{\omega}{500}\right)^{10}}$$

$$1 = (0.25) \left(\frac{\omega}{500}\right)^{10}$$

$$\sqrt[10]{4} = \frac{\omega}{500}$$

$$\omega = 574$$

$$f_c = 91.41 \text{ Hz}$$