```
/* Check that that neither end-point is a root and if f(a) and f(b) have the same sign, throw an exception.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // Applying a damping factor before re-plugging in the values Fmax = 0; ymax = 0; Udif = 0; U_ave = 0; Fmax = Fmax prev + damp*(Fmax new - Fmax prev); ymax = ymax_prev + damp*(ymax_new - ymax_prev); Udif = Udif new; U_ave = Udif new;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         std::cout<<"rout is "<rroot</pre>
std::cout<<"rout context a * check b > 0 ){
    std::cout<<"f(a) and f(b) do not have opposite signs"<<endl;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                // new values for new n plus update for U+
f_c = evalFunc(ymax_prev, Fmax_prev, Udif_prev, c, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       while ( delt1 > tol){
   std::cout<<"Inner iteration number: "<ccoun<endl;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             std::cout<<"Outer iteration number: "<<iter<<endl; c = 0.5*(a + b)\,;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               f_a = evalFunc(ymax, Fmax, Udif, a, 0);

f_b = evalFunc(ymax, Fmax, Udif, b, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           while ( fabs(Re_D_est - Re_D) > tol ){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // Update from previous timestep
                                                                                                                                                                                                                                                                                                                                                                                          std::cout<<"root is "<=root<endl;
} else if ( check b == 0 ){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    check_c = (2*f_c[3]*c - Re_D);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // Update new variable values
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   check_a = (2*f_a[3]*a - Re_D);
check_b = (2*f_b[3]*b - Re_D);
                                                                                                 check_a = (2*f_a[3]*a - Re_D);
check_b = (2*f_b[3]*b - Re_D);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // Begin the iterations---
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ymax_new = f_c[0];
Fmax_new = f_c[1];
Udif_new = f_c[2];
U_ave_new = f_c[3];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Fmax_prev = Fmax;
ymax_prev = ymax;
Udif_prev = Udif;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                U_ave_prev = U_ave;
                                                                                                                                                                                                                                                                                                          if ( check_a == 0 ) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           delt1 = delt_init;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          double delt1;
                                                                                                                                                                                                                                                                                                                                                               root = a;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              root = b;
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           double Evaluate_dUdy_Plus(double lmix_plus, double y_pl, double R_pl, double ymax, double Fmax, double Udif);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           std::vector <double> getUplus(double ymax, double Fmax, double Udif, double R_pl, int filewrite);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       std::vector <double> evalFunc(double ymax, double Fmax, double Udif, double R_pl, int filewrite);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    U_ave_new =0;
U_ave_prev=0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               double Fmax_new=0, ymax_new=0, Udif_new = 0, double Fmax_prev=0, ymax_prev=0, Udif_prev=0, // From Question Question Question deltinit = 30.6, Fmax = 2.31695, Udif = 23.0412, U_ave = 18.2401; double delt init = 30; int coun = 0 iter=0; double Re_D = 40000, Re_D = sst = 0;
    (Selection of) num3.cpp
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                double damp = 0.3;
double tol = le-5; double toler = le-5;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       std::vector <double> f_a(4);
std::vector <double> f_b(4);
std::vector <double> f_c(4);
std::vector <double> f_fin(4);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                double check_a = 0;
double check_b = 0;
double check_c = 0;
                                                                                                                                                                                                                                                                                                     #include <cmath>
#include <fstream>
#include </stream>
#include <cstdio>
#include <fstream>
#include <fstream>
#include <stdib.h>
#include <stdib.h>
#include 
#includ
                                                     #include <stdio.h>
#include <iostram>
#include <stddef.h>
#include <stding>
#include <stding>
#include <cstdilp>
#include <cstdilp>
#include <cstdilp>
#include <cstdilp>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            double c = 0;
double a= 1;
double b = 10000;
double root = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          using std::cout;
using std::endl;
using std::ios;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                // Main function
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   // variables
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   // Function
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int main(){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               prototypes=
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```

(Selection of) /home/chris/Desktop/TurbHwork/num3/num3.cpp

====== BISECTION METHOD

f_a = evalFunc(ymax, Fmax, Udif, a, 0);
f_b = evalFunc(ymax, Fmax, Udif, b, 0);

double delt1 = fabs(ymax - ymax_prev);
double delt2 = fabs(Fmax - Fmax_prev);

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Fwake = Cwk*ymax*Udif*Udif/Fmax;

inner layer

visc = eddyIN; // inner laye
dU_dy = y_over_R / (1 + visc);

```
double alpha = 0.0168;
double CCp = 1.6;
double FKleb, Fwake, CKleb = 0.3, Cwk = 1;
double visc=0, eddyIN, eddyOUT;
                                                                                                                                                                                     "<<endl;
                                                                                                                                                                                     // std::cout<<"Stuck here....
                                                                                                                                                                                                                                                                          while (y_pl <= R_pl){</pre>
                                                                                                                                                                                                                              // Build the Velocity
                                                                                                                   double aa = 2e-1;
double bb= 1e-1;
```

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```
Results[0] = ymax;
Results[1] = Fmax;
Results[2] = Udif;
Results[3] = U_ave;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (filewrite == 1){
                                                                                                                                                                                                                                                                                                                                                                         if (ypl > 2){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  fclose(fout);
                    U_{n1} = U_{n2};
                                                                                                                                                                                                                                                                                                                                                                                                dU_dy3 = Evaluate_dUdy_Plus(lmix_pl + 0.5*delta_y_pl*dU_dy2, y_pl + delta_y_pl, R_pl,ymax, Fmax, Udif);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             /* ======= RK4 Scheme ========*/
dU_dy0 = Evaluate_dUdy_Plus(lmix_pl, y_pl, R_pl,ymax, Fmax, Udif);
dU_dy1 = Evaluate_dUdy_Plus(lmix_pl + 0.5*delta_y_pl*dU_dy0, y_pl + 0.5*delta_y_pl, R_pl,ymax, Fmax, Udif);
                                                                                                                                                                                                                                                                                                                           dU_dy2 = Evaluate_dUdy_Plus(lmix_pl + 0.5*delta_y_pl*dU_dy1, y_pl + 0.5*delta_y_pl, R_pl,ymax, Fmax, Udif);
                                                                                                                                                                                                                                                                                                                                                                                                                      dU_dy = y over R - (y over R*y over R)*(lmix pl*lmix_pl) +
2*(y_over R*y_over R*y_ove_R)*(lmix_plus_fourth);
Reynolds.push_back(lmix_pl*lmix_pl * dU_dy*dU_dy);
                                                                                                                                                                                    \begin{split} & \lim_{X \to D} pl = K^*y\_pl^*(\frac{1}{1} - \exp(-y\_pl/A\theta\_pl) \ ); \\ & \text{double lmix\_plus\_fourth} = \lim_{X \to Dl^*lmix\_pl^*lmix\_pl}; \end{split} 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  summ = summ + U_n^2 * (1 - y_p^1/R_p^1) * delta_y_p^1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if ( ymax*Fmax <= Cwk*ymax*Udif*Udif/Fmax){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      eddy0UT = alpha * Ccp * Fwake * FKleb;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          Fwake = Cwk*ymax*Udif*Udif/Fmax;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          outer layer
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // a build for the Reynold's Stress
if (y_pl <= 1){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            visc = eddyIN; // inner layer
dU_dy = y_over_R / (1 + visc);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Reynolds.push_back(visc * dU_dy);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             double y\_over\_R = (1 - y\_pl/R\_pl);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      counter = counter + 1;
y_pl = y_pl + delta y_pl;
if (fabs(y_pl - R_pl) < 1){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if (eddyIN <= eddyOUT){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Fwake = ymax*Fmax;
                                                                 if (y_pl > 2){
    delta_y_pl = bb;
                         delta_y_pl = aa;
if (y_pl <= 2) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         else{
```

```
fprintf(fout, "%s", var2.c_str() ); fprintf(fout, "\n");
fprintf(fout, "%s, "variables = "U+U-U+U-max' '\y+' '\y+' '\y+' '\y+' '\y+' '\phintf(fout, "\n");
fprintf(fout, "\n"); // Reynolds Shear Stress' fprintf(fout, "\n"); // '\n" '\n"); // '\n" '\n");
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 std::cout<<" "<endl; std::cout<<"U_plus results file successfully written"<endl;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    std::stringstream stream1, stream3, stream4, stream5, stream6, stream7;
stream1 << "U_plus_two-layer_mixing_model.dat";</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   \frac{double \ num\_elem = U\_pl\_profile.size();}{Udif = U\_pl\_profile[counter * ymax/R\_pl];} 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                std::cout<<"U_max is "<<U_pl_profile[counter-1]<<endl;
known and complete
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               ====== now write results to file (Tecplot!):
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     stream3 <='i_="<num_elem;
stream4<="title = "<=".cstream1.str()<=":";
std::string var1 = stream3.str();
std::string var2 = stream4.str();</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    FILE* fout = fopen(fileName1.c_str(), "w");
                                                                             double val_max = 0, Rmax = 0, val_Rmax=0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   std::string fileName1 = stream1.str();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (Reynolds[i] > Rmax){
   Rmax = Reynolds[i];
                                                                                                                                                                                                                                                                                                                                                                                                                       ymax = i * delta_y_pl;
Fmax = (1/K)*val_max;
                       U_ave = (2/R_pl) * summ;
                                                                                                                                                                                                                                                                                                                                                                         delta_y_pl = bb;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     fprintf(fout, "\n");
```

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return Results;

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