Introduction to Information Retrieval CS276: Information Retrieval and Web Search Pandu Nayak and Prabhakar Raghavan Scoring, Term Weighting and the Vector Space Model IIR Ch. 6 - Slides modified from Stanford CS276, Spring 2015 (Manning and Nayak) http://nlp.stanford.edu/IR-book/

This lecture; IIR Sections 6.2-6.4.3

- Ranked retrieval
- Scoring documents
- Term frequency
- Collection statistics
- Weighting schemes
- Vector space scoring

Ranked retrieval

- Thus far, our gueries have all been Boolean.
 - Documents either match or don't.
- Good for expert users with precise understanding of their needs and the collection.
 - Also good for applications: Applications can easily consume 1000s of results.
- Not good for the majority of users.
 - Most users incapable of writing Boolean queries (or they are, but they think it's too much work).
 - Most users don't want to wade through 1000s of results.
 - This is particularly true of web search.

Problem with Boolean search: feast or famine

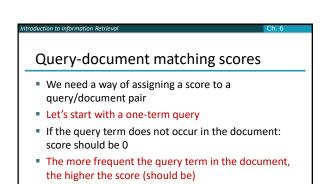
- Boolean queries often result in either too few (=0) or too many (1000s) results.
- Query 1: "standard user dlink 650" → 200,000 hits
- Query 2: "standard user dlink 650 no card found": 0
- It takes a lot of skill to come up with a query that produces a manageable number of hits.
 - AND gives too few; OR gives too many

Feast or famine: not a problem in ranked retrieval

- When a system produces a ranked result set, large result sets are not an issue
 - Indeed, the size of the result set is not an issue
 - We just show the top k (\approx 10) results
 - We don't overwhelm the user
 - Premise: the ranking algorithm works

Scoring as the basis of ranked retrieval

- We wish to return in order the documents most likely to be useful to the searcher
- How can we rank-order the documents in the collection with respect to a query?
- Assign a score say in [0, 1] to each document
- This score measures how well document and query "match".

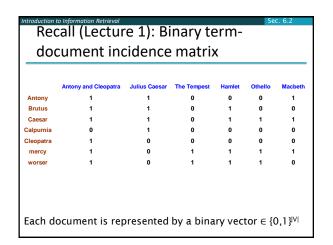


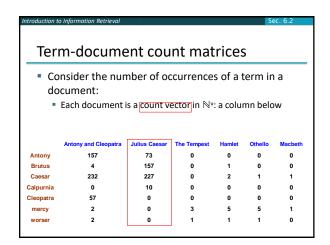
We will look at a number of alternatives for this.

Take 1: Jaccard coefficient jaccard(A,B) = |A ∩ B| / |A ∪ B| jaccard(A,A) = 1 jaccard(A,B) = 0 if A ∩ B = 0 A and B don't have to be the same size. Always assigns a number between 0 and 1.

Document 2: the long march

Issues with Jaccard for scoring
 It doesn't consider term frequency (how many times a term occurs in a document)
 Rare terms in a collection are more informative than frequent terms. Jaccard doesn't consider this information
 We need a more sophisticated way of normalizing for length
 Later in this lecture, we'll use |A∩B|/√|A∪B|
 ... instead of |A ∩ B|/|A ∪ B| (Jaccard) for length normalization.





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Bag of words model

- Vector representation doesn't consider the ordering of words in a document
- John is quicker than Mary and Mary is quicker than John have the same vectors
- This is called the bag of words model.
- In a sense, this is a step back: The positional index was able to distinguish these two documents.
- The IIR book considers "recovering" positional information.
- For now: bag of words model

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Term frequency tf

- The term frequency tf_{t,d} of term t in document d is defined as the number of times that t occurs in d.
- We want to use tf when computing query-document match scores. But how?
- Raw term frequency is not what we want:
 - A document with 10 occurrences of the term is more relevant than a document with 1 occurrence of the term.
 - But not 10 times more relevant.
- Relevance does not increase proportionally with term frequency.

NB: frequency = count in IR

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Log-frequency weighting

The log frequency weight of term t in d is

$$w_{t,d} = \begin{cases} 1 + \log_{10} \mathsf{tf}_{t,d}, & \text{if } \mathsf{tf}_{t,d} > 0 \\ 0, & \text{otherwise} \end{cases}$$

- $0 \to 0, 1 \to 1, 2 \to 1.3, 10 \to 2, 1000 \to 4$, etc.
- Score for a document-query pair: sum over terms t in both q and d:
- score $=\sum_{t \in q \cap d} (1 + \log tf_{t,d})$
- The score is 0 if none of the query terms is present in the document.

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Document frequency

- Rare terms are more informative than frequent terms
 - Recall stop words
- Consider a term in the query that is rare in the collection (e.g., arachnocentric)
- A document containing this term is very likely to be relevant to the query arachnocentric
- → We want a high weight for rare terms like arachnocentric.

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Document frequency, continued

- Frequent terms are less informative than rare terms
- Consider a query term that is frequent in the collection (e.g., high, increase, line)
- A document containing such a term is more likely to be relevant than a document that doesn't
- But it's not a sure indicator of relevance.
- → For frequent terms, we want high positive weights for words like high, increase, and line
- But lower weights than for rare terms.
- We will use document frequency (df) to capture this.

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idf weight

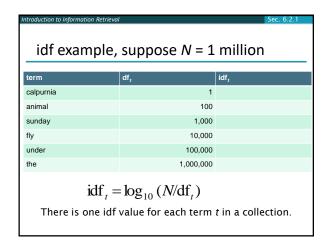
- df_t is the <u>document</u> frequency of t: the number of documents that contain t
 - $lack df_t$ is an inverse measure of the informativeness of t
 - ${\color{red}\bullet} \ \mathsf{df}_t \leq {\color{red} N}$

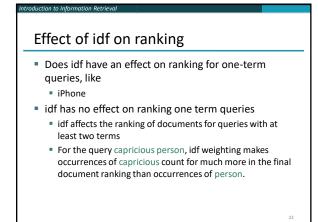
 We define the idf (inverse document frequency) of t by

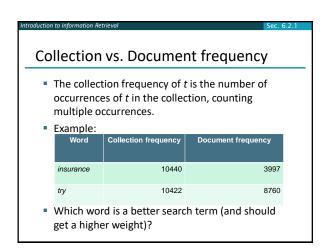
 $idf_t = log_{10} (N/df_t)$

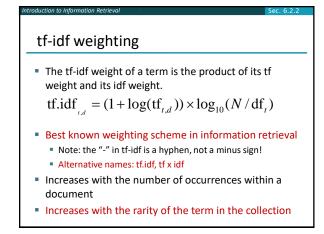
 We use log (N/df_t) instead of N/df_t to "dampen" the effect of idf.

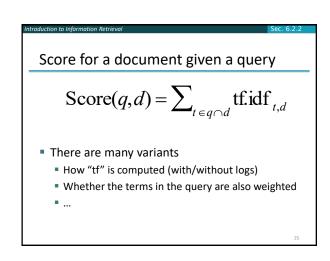
Will turn out the base of the log is immaterial.

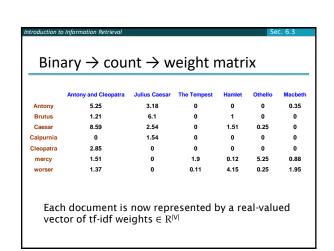












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- So we have a |V|-dimensional vector space
- Terms are axes of the space

Documents as vectors

- Documents are points or vectors in this space
- Very high-dimensional: tens of millions of dimensions when you apply this to a web search engine
- These are very sparse vectors most entries are zero.

Queries as vectors

- Key idea 1: Do the same for queries: represent them as vectors in the space
- Key idea 2: Rank documents according to their proximity to the query in this space
- proximity = similarity of vectors
- proximity ≈ inverse of distance
- Recall: We do this because we want to get away from the you're-either-in-or-out Boolean model.
- Instead: rank more relevant documents higher than less relevant documents

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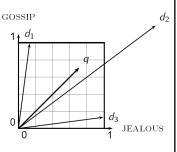
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Formalizing vector space proximity

- First cut: distance between two points
 - (= distance between the end points of the two vectors)
- Euclidean distance?
- Euclidean distance is a bad idea . . .
- ... because Euclidean distance is large for vectors of different lengths.

Why distance is a bad idea The Euclidean GOSSIP

distance between q and $\overrightarrow{d_2}$ is large even though the distribution of terms in the query \overrightarrow{q} and the distribution of terms in the document $\overrightarrow{d_2}$ are very similar.



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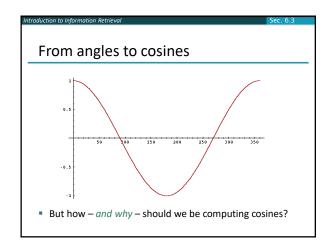
Use angle instead of distance

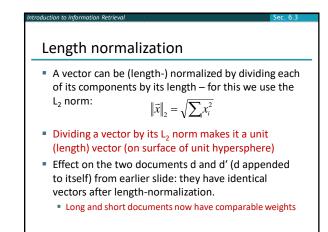
- Thought experiment: take a document d and append it to itself. Call this document d'.
- "Semantically" d and d' have the same content
- The Euclidean distance between the two documents can be quite large
- The angle between the two documents is 0, corresponding to maximal similarity.
- Key idea: Rank documents according to angle with query.

Sec. 6

From angles to cosines

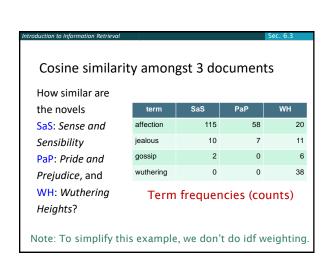
- The following two notions are equivalent.
 - Rank documents in <u>decreasing</u> order of the angle between query and document
 - Rank documents in <u>increasing</u> order of cosine(query,document)
- Cosine is a monotonically decreasing function for the interval [0°, 180°]





cosine(query,document) Dot product $\cos(\vec{q}, \vec{d}) = \frac{\vec{q} \cdot \vec{d}}{|\vec{q}||\vec{d}|} = \frac{\vec{q}}{|\vec{q}|} \cdot \frac{\vec{d}}{|\vec{d}|} = \frac{\sum_{i=1}^{|V|} q_i d_i}{\sqrt{\sum_{i=1}^{|V|} q_i^2} \sqrt{\sum_{i=1}^{|V|} d_i^2}}$ $q_i \text{ is the tf-idf weight of term } i \text{ in the query } d_i \text{ is the tf-idf weight of term } i \text{ in the document}}$ $\cos(\vec{q}, \vec{d}) \text{ is the cosine similarity of } \vec{q} \text{ and } \vec{d} \dots \text{ or, equivalently, the cosine of the angle between } \vec{q} \text{ and } \vec{d}.$

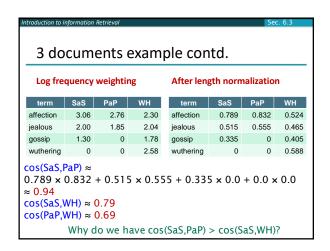
Cosine similarity illustrated POOR $\vec{v}(d_1)$ $\vec{v}(d_2)$ $\vec{v}(d_3)$ RICH

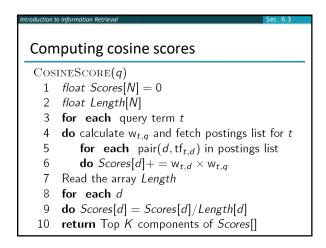


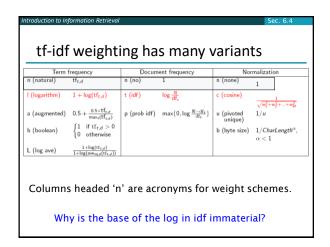
 For length-normalized vectors, cosine similarity is simply the dot product (or scalar product):

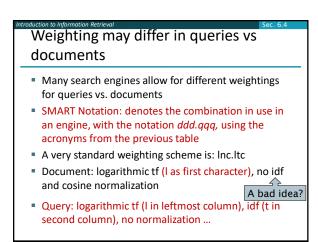
$$\cos(\vec{q}, \vec{d}) = \vec{q} \bullet \vec{d} = \sum_{i=1}^{|V|} q_i d_i$$

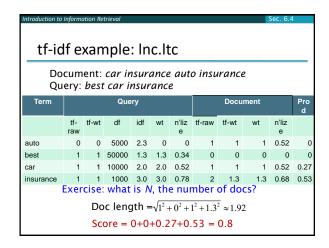
for q, d length-normalized.











Summary — vector space ranking Represent the query as a weighted tf-idf vector Represent each document as a weighted tf-idf vector Compute the cosine similarity score for the query vector and each document vector Rank documents with respect to the query by score Return the top K (e.g., K = 10) to the user

Resources for today's lecture IIR 6.2 – 6.4.3 http://www.miislita.com/information-retrieval-tutorial/cosine-similarity-tutorial.html Term weighting and cosine similarity tutorial for SEO folk!