Phase-Locked Quantum-Plasma Processor: Normalized Hamiltonian and Stability Analysis

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Abstract

We propose a non-algorithmic quantum computation model based on phase resonance, dynamic plasma coupling, and energy-driven convergence. Unlike gate-based or adiabatic quantum computing, this model computes via transition into stable energetic configurations defined by resonance conditions. We present a normalized Hamiltonian formalism, identify stability criteria, define Lindblad dissipation, and demonstrate a prototype numerical convergence scenario.

1 Normalized Formalism

Let the characteristic energy scale be $E_0 = \hbar \omega_q$, time scale $T_0 = 1/\omega_q$, and spatial scale L_0 (e.g., lattice period). Define normalized variables:

$$\begin{split} \tilde{q}_i &= \frac{q_i}{L_0}, & \tilde{p}_i &= \frac{p_i}{\hbar/L_0}, & \tilde{\rho} &= \frac{\rho}{\rho_0}, \\ \tilde{A} &= \frac{A}{E_0}, & \tilde{g} &= \frac{g\rho_0}{E_0}, & \tilde{t} &= \omega_q t \end{split}$$

Normalized Hamiltonian:

$$\tilde{\mathcal{H}} = \sum_{i} \frac{\tilde{p}_{i}^{2}}{2} + \tilde{\lambda}(\tilde{t})V(\tilde{q}_{i}) - \tilde{A}(\tilde{q}_{i}, \langle \tilde{q} \rangle) \cos(\tilde{t} - \tilde{\phi}(\langle \tilde{p} \rangle)) + \tilde{g}\tilde{\rho}(\tilde{q}_{i}) + \tilde{\mathcal{H}}_{\text{plasma}}$$
(1)

2 Hamiltonian Components

2.1 Task Encoding

 $\tilde{\lambda}(t)V(q)$: external problem shape. Choose:

• Adiabatic: $\dot{\lambda}/\lambda \ll \Delta_{\min}/\hbar$

• Floquet: $\lambda(t) = \sum_{k} \lambda_k \cos(\omega_k t)$

2.2 Resonance Lock

Feedback closure via:

$$\tilde{A}_i = A_0 + \chi \sum_{j \in \mathcal{N}(i)} f(\tilde{q}_j - \tilde{q}_i)$$
(2)

$$\tilde{\phi}_i = \phi_0 + \gamma \sum_j g(\tilde{p}_j - \tilde{p}_i) \tag{3}$$

2.3 Quantum-Plasma Coupling

Interaction:

$$\tilde{g}\tilde{\rho}(\tilde{q}_i)$$
, with $g = e\varphi(q)$, $\nabla^2 \varphi = -\rho/\varepsilon_0$ (4)

For atomic Rydberg implementations, a typical range is $g \sim 2\pi \times (0.1-1)\,\mathrm{MHz}$.

2.4 Plasma Hamiltonian

$$\tilde{\mathcal{H}}_{\text{plasma}} = \int d^3x \left[\frac{\Pi_{\rho}^2}{2M} + F(\tilde{\rho}, \tilde{v}, T) \right], \quad \{\tilde{\rho}, \Pi_{\rho}\} = 1$$
 (5)

Assuming ideal two-fluid EOS with Debye correction:

$$U = \frac{3}{2}k_B T(\rho_e + \rho_i) + \frac{e^2}{8\pi\varepsilon_0} \cdot \frac{\rho_e \rho_i}{k_B T}$$
(6)

2.5 Lindblad Dissipation

We implement dissipative convergence through a Caldeira-Leggett-type operator:

$$\mathcal{L}[\hat{\rho}] = -\frac{i\gamma}{\hbar} [\hat{q}, \hat{p}\hat{\rho}] - \frac{2m\gamma k_B T}{\hbar^2} [\hat{q}, [\hat{q}, \hat{\rho}]]$$
 (7)

For phase-coupled plasmas, $\gamma \equiv \gamma(\tilde{\rho})$ is density-dependent.

2.6 Readout Operator

Measurement modeled via:

$$\hat{O}_{\text{read}} = \sum_{i} \kappa_i \hat{q}_i, \quad \text{Solution fixated when } (\hat{O}_{\text{read}}) \to 0$$
 (8)

3 Stability Criterion

Small perturbations:

$$\tilde{q}_i = \tilde{q}_i^{(0)} + \delta \tilde{q}_i, \qquad \qquad \tilde{p}_i = \tilde{p}_i^{(0)} + \delta \tilde{p}_i, \qquad \qquad \tilde{\rho} = \tilde{\rho}^{(0)} + \delta \tilde{\rho}$$

Jacobian matrix \mathcal{J} :

$$\dot{\boldsymbol{\delta}} = \mathcal{J}\boldsymbol{\delta}$$
, converges if $\operatorname{Re}(\lambda_i) < 0 \ \forall i$ (9)

Floquet stability: diagonalize $\mathcal{M}_T = \mathcal{T} \exp \left(\int_0^T \mathcal{J}(t) dt \right)$ Check $|\mu_i| < 1$ for all Floquet multipliers.

4 Computation as Resonant Convergence

Solution
$$\iff |\omega_q - \omega_\phi(t)| \le \delta\omega_{\text{lock}}, \quad \frac{\mathrm{d}E}{\mathrm{d}t} \to 0^+$$
 (10)

5 Numerical Illustration

Figure 1: Simulated 1D phase-locking for $\lambda(t) = t/T_a$, normalized energy convergence, and Floquet eigenvalues showing subunitary decay.

- Initial state: random phase offsets
- Convergence: energy $E(t) \to \min$, $(\hat{O}_{read}) \to 0$

6 Conclusion

This model lays the groundwork for phase-resonant quantum processors with internal energy convergence. It replaces gate logic with dynamic resonance, problem encoding with field shaping, and result extraction with state locking.