

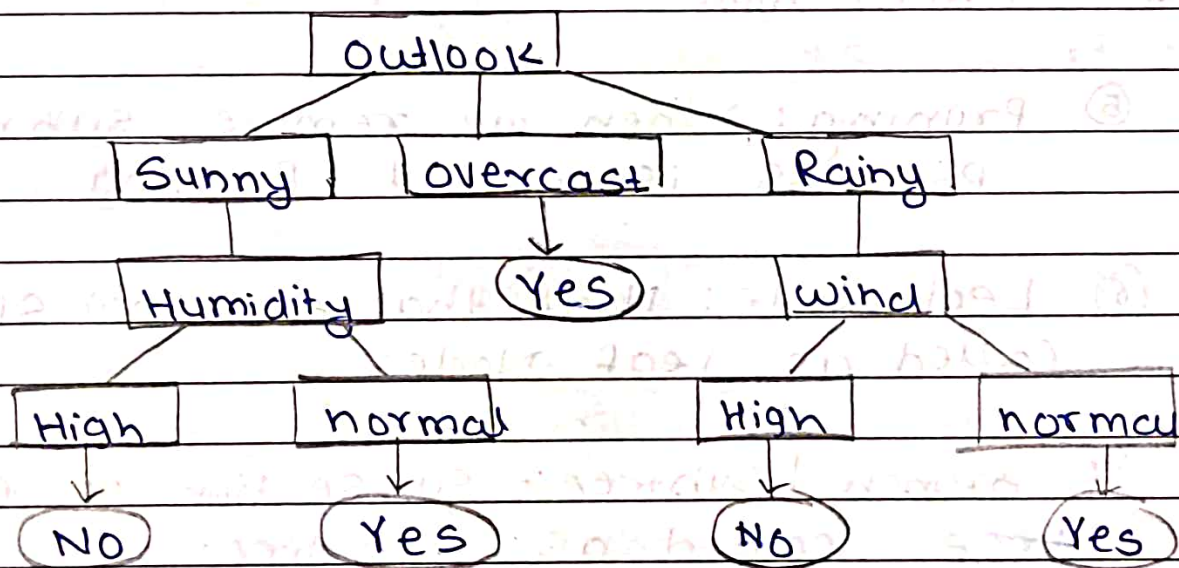
V-4- Decision tree & Probabilistic models.

Q-1. What is Binary Decision tree? — [8M]

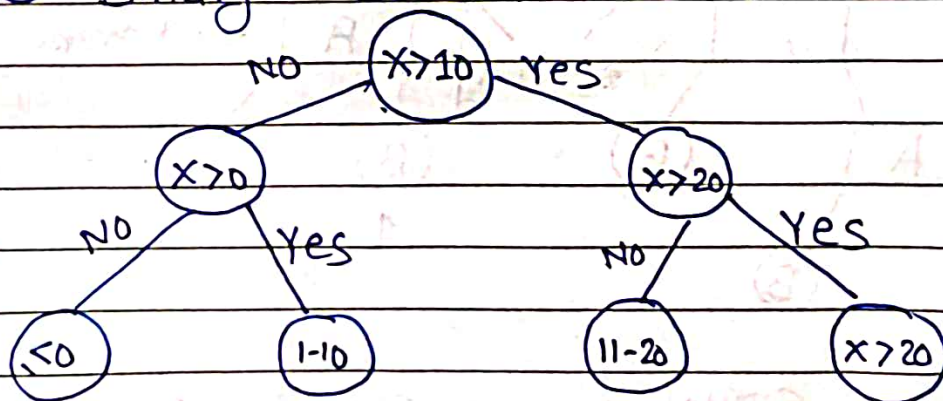
→ Decision tree is a supervised machine learning approach usually used for classification but can also be used as regression

Binary decision tree is a decision tree which operates by every attribute series by binary decision i.e. Yes or No.

eg:- ① Decision tree for Playing Tennis

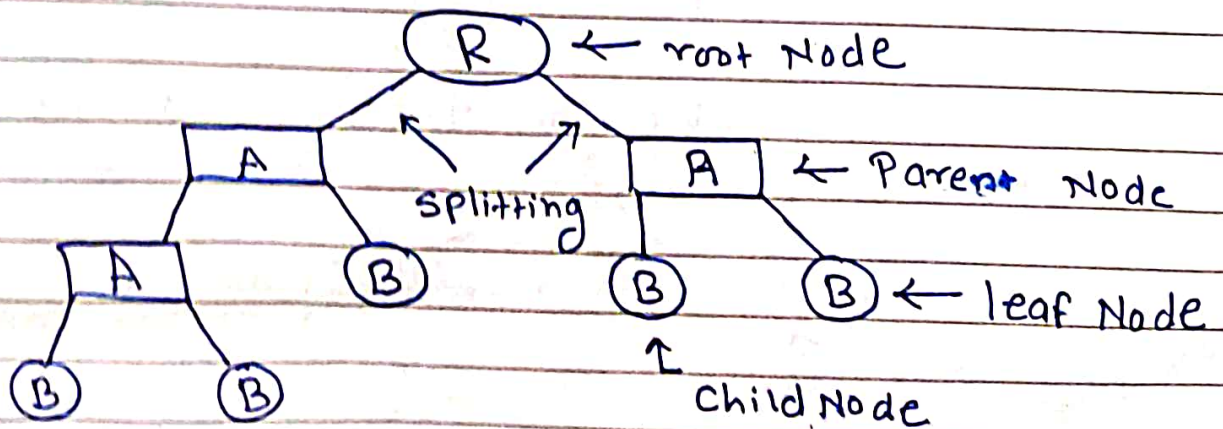


② Binary decision tree for Numbers.

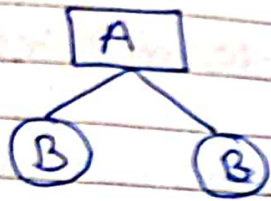


• Key terms

- ① **Root**: The Decision tree begins with root node further divided into subnodes, child
- ② **SPLITTING**: The Process of dividing Parent node into subnode called as splitting
- ③ **Parent Node**: A Node which is divided into sub node called as parent node
- ④ **Child Node**:- All subnodes called as child node
- ⑤ **Pruning**: When we remove subnode the process is called pruning.
- ⑥ **Leaf Node**: Node that does not split further called as leaf Node
- ⑦ **Branch / Subtree**:- Subsection of entire tree called as sub tree.



Structure of Decision tree



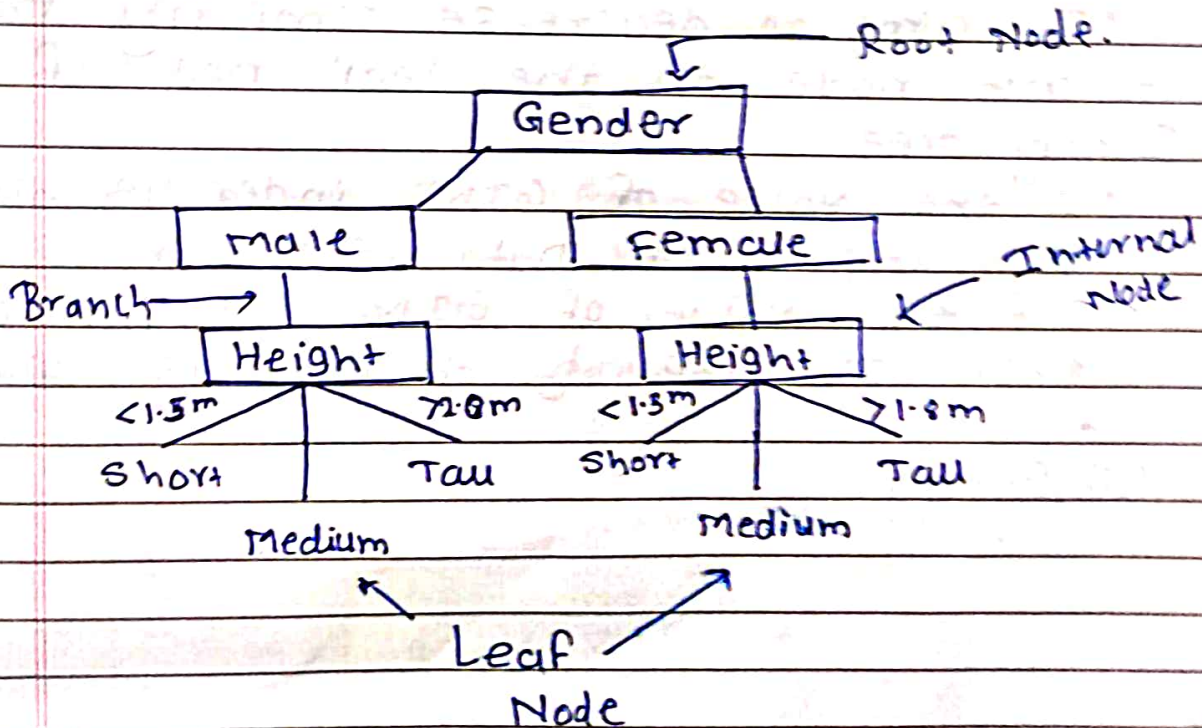
← Subtree / Branch.

R : Root Node of the tree

A : Parent Node / Decision Node

B : Leaf Node of the tree.

Eg:- A Example dataset of 30 students of gender boys & girls of class IX & X and height 5ft to 6ft. 15 out of 30 play cricket in leisure time.



• Algorithms for decision tree

greedy \leftarrow ① ID3 (Iterative Dichotomiser 3)
 \uparrow acc/dynamic \leftarrow ② C4.5
 \downarrow Binary tree \leftarrow ③ CART (Classification & Regression Tree).

Q-2.

Define : (i) GINI Index

(ii) Entropy

2 M
2 M

(i) GINI index

: GINI index is a powerful measure that measure randomness or impurity of the values of dataset

• It aims to decrease Impurity from the root node to the leaf node of the Binary tree

- If the value of GINI index is higher then impurity of Data is higher
- If the value of GINI index is lower then The impurity of Data is lower.

(ii) Entropy

Q-3- Explain Naive Bayes Classifier working — 10m

→ Bayes Thm =
$$\frac{P(B|A)P(A)}{P(B)} = P(A|B)$$

- Using Bayes Thm we can find the Probability of A happening given that B is occurred here B is the evidence & A is the hypothesis

- ✓ Assumption is made that feature is independent
- ✓ Presence of one feature does not affect other features

Naive Bayes Model:

It is a Probabilistic machine learning model that is used for classification tasks.

Let's consider an example of 1000 fruits which could be either 'banana', 'orange' or 'other'. There are three possible classes of variable 'Y' either 'banana', 'orange' or 'other' given that it is: long, sweet & yellow.

Type	Long	Sweet	Yellow	Total
Banana	400	350	450	500
Orange	80	150	300	300
Other	100	150	50	200
Total	500	650	800	1000

Step 1

$$P(\text{Banana}) = \frac{500}{1000} = 0.50$$

$$P(\text{orange}) = \frac{300}{1000} = 0.30$$

$$P(\text{other}) = \frac{200}{1000} = 0.20$$

Step 2

$$P(\text{long}) = \frac{500}{1000} = 0.50$$

$$P(\text{sweet}) = \frac{650}{1000} = 0.65$$

$$P(\text{Yellow}) = \frac{800}{1000} = 0.80$$

Step 3

① For Banana:

$$P(\text{long} | \text{Banana}) = \frac{400}{500} = 0.80$$

long	yellow	other
0.80	0.20	0.00
0.30	0.30	0.00
0.50	0.50	0.00
0.01	0.08	0.91

$$= \frac{P(\text{Banana} | \text{orange}) P(\text{C})}{P(\text{Banana} | \text{long}) P(\text{long})}$$
$$= \frac{400}{500} \times \frac{500}{1000} = 0.20$$
$$\frac{500}{1000}$$

$$P(\text{Sweet} | \text{Banana}) = \frac{P(\text{Banana} | \text{Sweet}) P(\text{Sweet})}{P(\text{Banana})}$$

$$= \frac{850}{650} \times \frac{650}{1000} = 0.7$$

$$P(\text{Yellow} | \text{Banana}) = \frac{P(\text{Banana} | \text{Yellow}) P(\text{Yellow})}{P(\text{Banana})}$$

$$= \frac{450}{500} \times \frac{800}{1000} = 0.9$$

STEP 4

(P(fruit, S = ch) / 1000) = 0.8 x 0.7 x 0.9

$$P(\text{fruit} | \text{Banana}) = 0.8 \times 0.7 \times 0.9 = 0.504$$

[

Q-4. write Short Note on (16)

(ii) Multinomial Naïve Bayes

→

If feature of Bayes distribution used in text classification for multinomially distributed data.

- Discrete count
- multinomial distribution
- Document classification

B _{G1}	0.44	A	B _{G1}	AB
P	0.44	0.42	0.10	0.04

$$P(x = x_1, \dots, x_k) = \frac{n!}{x_1! \dots x_k!} p_1^{x_1} \dots p_k^{x_k}$$

6 → Person

1 → 0.44 2 → A

2 → B 1 → AB

$$P(x_1 = 1, x_2 = 2, x_3 = 2, x_4 = 1)$$

$$= \frac{6!}{1! 2! 2! 1!} \times (0.44) \times (0.42) \times (0.10) (0.04)^1$$

180x

$$= 0.0065$$

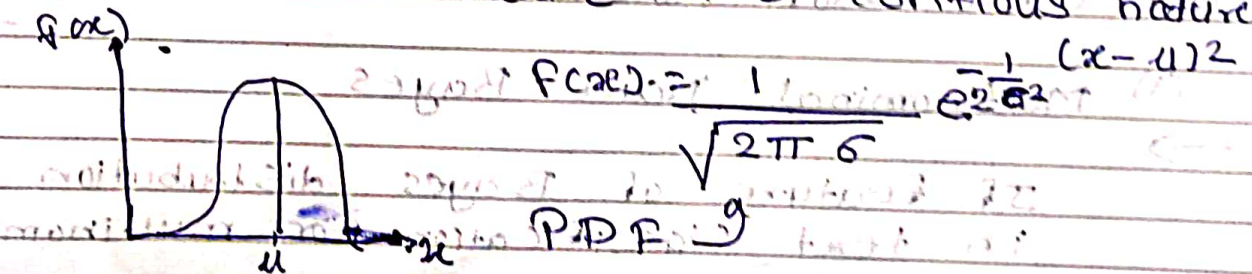
(11)

Gaussian Naive Bayes

- used for classification

- Gaussian Distribution

(*) used for feature having continuous nature



- Normal Distribution

(ii) Bernoulli Naive Bayes

• If features are in Binary nature then we use Bernoulli naive Bayes

$$\begin{aligned} P(\text{Success}) &= P \\ P(\text{Failure}) &= q = 1 - P \end{aligned}$$

If random variable value is 1 \rightarrow Success
If random variable value is 0 \rightarrow Failure

'X has a Bernoulli distribution'

$$P(X=x) = P^x \cdot (1-P)^{1-x}$$

$$P(X=x) = \begin{cases} P & \text{if } x=1 \\ q & \text{if } x=0 \end{cases}$$