

Database System

05 | Query Processing and Optimization

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Goals of the Meeting

01

Students knows the basic process of query processing and understand how to translate SQL Queries into Relational Algebra Expression (RAE)

02

Students know various algorithms for selection and join operations and how to measures query costs

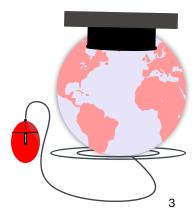
03

Students know various ways to optimize query processing, generate equivalent expressions, and execute an SQL statement to view query evaluation plans in DBMS



OUTLINES

- Step of Query Processing
- Relational Algebra Expression (RAE)
- Query Cost
- Equivalen Rules Query Evaluation Plans on DBMS



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STEP OF QUERY PROCESSING

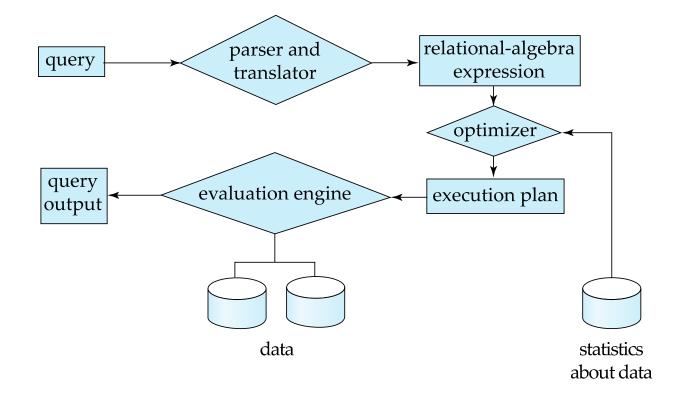


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BASIC STEPS IN QUERY PROCESSING

- 1. Parsing and translation
- 2. Optimization
- 3. Evaluation







BASIC STEPS IN QUERY PROCESSING (CONT.)

- Parsing and translation
 - translate the query into its internal form. This is then translated into relational algebra.
 - Parser checks syntax, verifies relations
- Optimization
 - Each relational algebra operation can be evaluated using one of several different algorithms
 - Annotated expression specifying detailed evaluation strategy is called an **evaluation-plan**
 - Amongst all equivalent evaluation plans choose the one with lowest cost.
- Evaluation
 - The query-execution engine takes a query-evaluation plan, executes that plan, and returns the answers to the query.



RELATIONAL ALGEBRA EXPRESSION

PARSING & TRANSLATION
 QUERY TO RAE



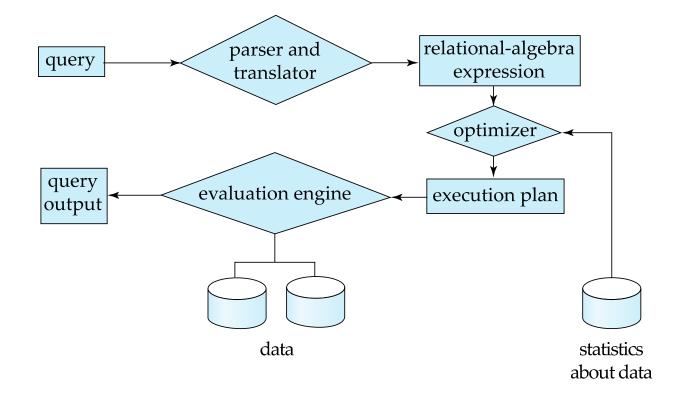
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BASIC STEPS IN QUERY PROCESSING

1. Parsing and translation

- 2. Optimization
- 3. Evaluation







RELATIONAL ALGEBRA

- A procedural language consisting of a set of operations that take one or two relations as input and produce a new relation as their result.
- Operators
 - select: σ
 - project: ∏
 - cartesian product: x
 - join: ⋈
 - union: ∪
 - set-intersection: ∩
 - set-difference: –
 - assignment: ←
 - rename: ρ



SELECT OPERATION

- The **selec**t operation selects tuples that satisfy a given predicate.
- Notation: $\sigma_p(r)$
- p is called the **selection predicate**
- Example: select those tuples of the *instructor* relation where the instructor is in the "Physics" department.
 - Query

SELECT * FROM instructor WHERE dept_name = 'Physics'

Relational Algebra (RA)

$$\sigma_{dept_name= "Physics"}$$
 (instructor)

- Result

| ID | name | dept_name | salary |
|-------|----------|-----------|--------|
| 22222 | Einstein | Physics | 95000 |
| 33456 | Gold | Physics | 87000 |



SELECT OPERATION (CONT.)

· We allow comparisons using

in the selection predicate.

• We can combine several predicates into a larger predicate by using the connectives:

$$\wedge$$
 (and), \vee (or), \neg (not)

- Example: Find the instructors in Physics with a salary greater than \$90,000, we write:
 - Query: SELECT * FROM instructor WHERE dept_name = 'Physics' AND salary > 90000
 - RA:

- The select predicate may include comparisons between two attributes.
 - Example, find all departments whose name is the same as their building name:
 - Query: SELECT * FROM department WHERE dept_name = building
 - RA:

```
\sigma_{dept\_name=building} (department)
```



PROJECT OPERATION

- A unary operation that returns its argument relation, with certain attributes left out.
- Notation:

$$\prod_{A_1, A_2, A_3 \dots A_k} (r)$$

where $A_1, A_2, ..., A_k$ are attribute names and r is a relation name.

- The result is defined as the relation of *k* columns obtained by erasing the columns that are not listed
- Duplicate rows removed from result, since relations are sets



PROJECT OPERATION EXAMPLE

- Example: eliminate the *dept_name* attribute of *instructor*
- Query: SELECT id, name, salary FROM instructor
- RA:

 $\prod_{ID, name, salary}$ (instructor)

• Result:

| ID | name | salary |
|-------|------------|--------|
| 10101 | Srinivasan | 65000 |
| 12121 | Wu | 90000 |
| 15151 | Mozart | 40000 |
| 22222 | Einstein | 95000 |
| 32343 | El Said | 60000 |
| 33456 | Gold | 87000 |
| 45565 | Katz | 75000 |
| 58583 | Califieri | 62000 |
| 76543 | Singh | 80000 |
| 76766 | Crick | 72000 |
| 83821 | Brandt | 92000 |
| 98345 | Kim | 80000 |



COMPOSITION OF RELATIONAL OPERATIONS

- The result of a relational-algebra operation is relation and therefore of relational-algebra operations can be composed together into a **relational-algebra expression**.
- Consider the query -- Find the names of all instructors in the Physics department.
 - Query: SELECT name FROM instructor WHERE dept_name = 'Physics'
 - RAE:

$$\prod_{name} (\sigma_{dept_name = "Physics"} (instructor))$$

• Instead of giving the name of a relation as the argument of the projection operation, we give an expression that evaluates to a relation.



CARTESIAN-PRODUCT OPERATION

- The Cartesian-product operation (denoted by X) allows us to combine information from any two relations.
- Example: the Cartesian product of the relations *instructor* and teaches is written as:
 - Query: SELECT * FROM instructor CROSS JOIN teaches
 - or **SELECT * FROM instructor, teaches**
 - RA:

instructor X teaches

- We construct a tuple of the result out of each possible pair of tuples: one from the *instructor* relation and one from the *teaches* relation (see next slide)
- Since the instructor *ID* appears in both relations we distinguish between these attribute by attaching to the attribute the name of the relation from which the attribute originally came.
 - instructor.ID
 - teaches.ID



THE INSTRUCTOR X TEACHES TABLE

| instructor.ID | name | dept_name | salary | teaches.ID | course_id | sec_id | semester | year |
|---------------|------------|------------|--------|------------|-----------|--------|----------|------|
| 10101 | Srinivasan | Comp. Sci. | 65000 | 10101 | CS-101 | 1 | Fall | 2017 |
| 10101 | Srinivasan | Comp. Sci. | 65000 | 10101 | CS-315 | 1 | Spring | 2018 |
| 10101 | Srinivasan | Comp. Sci. | 65000 | 10101 | CS-347 | 1 | Fall | 2017 |
| 10101 | Srinivasan | Comp. Sci. | 65000 | 12121 | FIN-201 | 1 | Spring | 2018 |
| 10101 | Srinivasan | Comp. Sci. | 65000 | 15151 | MU-199 | 1 | Spring | 2018 |
| 10101 | Srinivasan | Comp. Sci. | 65000 | 22222 | PHY-101 | 1 | Fall | 2017 |
| | | | | | | | | |
| | | | | ••• | | | | |
| 12121 | Wu | Finance | 90000 | 10101 | CS-101 | 1 | Fall | 2017 |
| 12121 | Wu | Finance | 90000 | 10101 | CS-315 | 1 | Spring | 2018 |
| 12121 | Wu | Finance | 90000 | 10101 | CS-347 | 1 | Fall | 2017 |
| 12121 | Wu | Finance | 90000 | 12121 | FIN-201 | 1 | Spring | 2018 |
| 12121 | Wu | Finance | 90000 | 15151 | MU-199 | 1 | Spring | 2018 |
| 12121 | Wu | Finance | 90000 | 22222 | PHY-101 | 1 | Fall | 2017 |
| | | | | | | | | |
| ••• | | | | | ••• | | | |
| 15151 | Mozart | Music | 40000 | 10101 | CS-101 | 1 | Fall | 2017 |
| 15151 | Mozart | Music | 40000 | 10101 | CS-315 | 1 | Spring | 2018 |
| 15151 | Mozart | Music | 40000 | 10101 | CS-347 | 1 | Fall | 2017 |
| 15151 | Mozart | Music | 40000 | 12121 | FIN-201 | 1 | Spring | 2018 |
| 15151 | Mozart | Music | 40000 | 15151 | MU-199 | 1 | Spring | 2018 |
| 15151 | Mozart | Music | 40000 | 22222 | PHY-101 | 1 | Fall | 2017 |
| ••• | ••• | | | | ••• | | | |
| ••• | | | | | ••• | | | |
| 22222 | Einstein | Physics | 95000 | 10101 | CS-101 | 1 | Fall | 2017 |
| 22222 | Einstein | Physics | 95000 | 10101 | CS-315 | 1 | Spring | 2018 |
| 22222 | Einstein | Physics | 95000 | 10101 | CS-347 | 1 | Fall | 2017 |
| 22222 | Einstein | Physics | 95000 | 12121 | FIN-201 | 1 | Spring | 2018 |
| 22222 | Einstein | Physics | 95000 | 15151 | MU-199 | 1 | Spring | 2018 |
| 22222 | Einstein | Physics | 95000 | 22222 | PHY-101 | 1 | Fall | 2017 |
| ••• | ••• | ••• | | | ••• | | ••• | |
| ••• | ••• | | | ••• | | | | |

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JOIN OPERATION

The Cartesian-Product

instructor X teaches

associates every tuple of instructor with every tuple of teaches.

- Most of the resulting rows have information about instructors who did NOT teach a particular course.
- To get only those tuples of "instructor X teaches" that pertain to instructors and the courses that they taught, we write:
 - Query: SELECT * FROM instructor, teaches WHERE instructor.id = teaches.id
 - RAE:

```
\sigma_{instructor.id = teaches.id} (instructor x teaches))
```

- We get only those tuples of "instructor X teaches" that pertain to instructors and the courses that they taught.
- The result of this expression, shown in the next slide



JOIN OPERATION (CONT.)

• The table corresponding to:

$\sigma_{instructor.id = teaches.id}$ (instructor x teaches))

| instructor.ID | name | dept_name | salary | teaches.ID | course_id | sec_id | semester | year |
|---------------|------------|------------|--------|------------|-----------|--------|----------|------|
| 10101 | Srinivasan | Comp. Sci. | 65000 | 10101 | CS-101 | 1 | Fall | 2017 |
| 10101 | Srinivasan | Comp. Sci. | 65000 | 10101 | CS-315 | 1 | Spring | 2018 |
| 10101 | Srinivasan | Comp. Sci. | 65000 | 10101 | CS-347 | 1 | Fall | 2017 |
| 12121 | Wu | Finance | 90000 | 12121 | FIN-201 | 1 | Spring | 2018 |
| 15151 | Mozart | Music | 40000 | 15151 | MU-199 | 1 | Spring | 2018 |
| 22222 | Einstein | Physics | 95000 | 22222 | PHY-101 | 1 | Fall | 2017 |
| 32343 | El Said | History | 60000 | 32343 | HIS-351 | 1 | Spring | 2018 |
| 45565 | Katz | Comp. Sci. | 75000 | 45565 | CS-101 | 1 | Spring | 2018 |
| 45565 | Katz | Comp. Sci. | 75000 | 45565 | CS-319 | 1 | Spring | 2018 |
| 76766 | Crick | Biology | 72000 | 76766 | BIO-101 | 1 | Summer | 2017 |
| 76766 | Crick | Biology | 72000 | 76766 | BIO-301 | 1 | Summer | 2018 |
| 83821 | Brandt | Comp. Sci. | 92000 | 83821 | CS-190 | 1 | Spring | 2017 |
| 83821 | Brandt | Comp. Sci. | 92000 | 83821 | CS-190 | 2 | Spring | 2017 |
| 83821 | Brandt | Comp. Sci. | 92000 | 83821 | CS-319 | 2 | Spring | 2018 |
| 98345 | Kim | Elec. Eng. | 80000 | 98345 | EE-181 | 1 | Spring | 2017 |



JOIN OPERATION (CONT.)

- The **join** operation allows us to combine a select operation and a Cartesian-Product operation into a single operation.
- Consider relations r (R) and s (S)
- Let "theta" be a predicate on attributes in the schema R "union" S. The join operation $r \bowtie_{\theta} s$ is defined as follows:

$$r \bowtie_{\theta} s = \sigma_{\theta} (r \times s)$$

Thus

 $\sigma_{instructor.id = teaches.id}$ (instructor x teaches))

Can equivalently be written as

SELECT * FROM instructor JOIN teaches ON instructor.id = teaches.id

instructor ⋈ _{Instructor.id = teaches.id} teaches



JOIN OPERATION (CONT.)

Natural join :

• Inner join:

• Outer join:



Full Outer Join

Right Outer Join

Left Outer Join

: :

:

:



RENAME OPERATION

- The results of relational-algebra expressions do not have a name that we can use to refer to them. The rename operator, ρ , is provided for that purpose
- The expression:

$$\rho_{x}$$
 (E)

returns the result of expression *E* under the name *x*

Another form of the rename operation:

$$\rho_{x(A1,A2,\ldots An)}(E)$$

returns the result of expression E under the name x, and with the attributes renamed to $A_1, A_2, ..., A_n$.



RENAME OPERATION EXAMPLE

SELECT * FROM countries nation:

 ρ_{nation} (countries)

SELECT country_id AS id, country_name AS name, region_id FROM countries nation:

 $ho_{
m nation~(id,~name,~region_id)}$ (countries)

SELECT country_id AS id, country_name AS name FROM countries nation:

 $\prod_{id, name} (\rho_{nation (id, name, region_id)} (countries))$



QUERY OPTIMIZATION

- MEASURES OF QUERY COSTS
- · SELECTION ALGORITHM

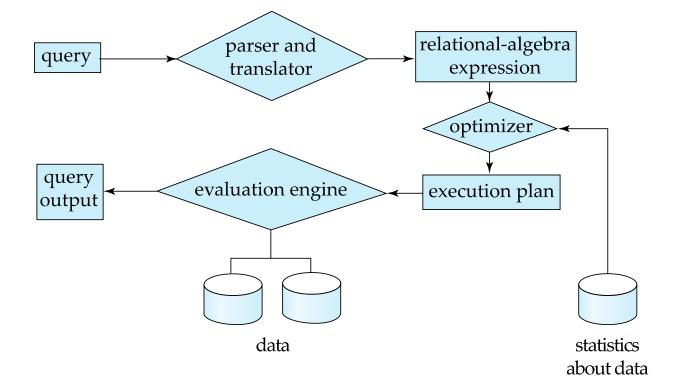


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BASIC STEPS IN QUERY PROCESSING

- 1. Parsing and translation
- 2. Optimization
- 3. Evaluation





BASIC STEPS IN QUERY PROCESSING: OPTIMIZATION

- A relational algebra expression may have many equivalent expressions
 - E.g., $\sigma_{salary < 75000}(\prod_{salary}(instructor))$ is equivalent to $\prod_{salary}(\sigma_{salary < 75000}(instructor))$
- Each relational algebra operation can be evaluated using one of several different algorithms
 - Correspondingly, a relational-algebra expression can be evaluated in many ways.
- Annotated expression specifying detailed evaluation strategy is called an evaluation-plan. E.g.,:
 - Use an index on salary to find instructors with salary < 75000,
 - Or perform complete relation scan and discard instructors with salary ≥ 75000



BASIC STEPS: OPTIMIZATION (CONT.)

- Query Optimization: Amongst all equivalent evaluation plans choose the one with lowest cost.
 - Cost is estimated using statistical information from the database catalog
 - e.g.. number of tuples in each relation, size of tuples, etc.
- In this chapter we study
 - How to measure query costs
 - Algorithms for evaluating relational algebra operations
 - How to combine algorithms for individual operations in order to evaluate a complete expression



MEASURES OF QUERY COST

- Many factors contribute to time cost
 - disk access, CPU, and network communication
- Cost can be measured based on
 - response time, i.e. total elapsed time for answering query, or
 - total resource consumption
- We use total resource consumption as cost metric
 - Response time harder to estimate, and minimizing resource consumption is a good idea in a shared database
- We ignore CPU costs for simplicity
 - Real systems do take CPU cost into account
 - Network costs must be considered for parallel systems
- We describe how estimate the cost of each operation
 - We do not include cost to writing output to disk



MEASURES OF QUERY COST

- Disk cost can be estimated as:
 - Number of seeks * average-seek-cost
 - Number of blocks read * average-block-read-cost
 - Number of blocks written * average-block-write-cost
- For simplicity we just use the **number of block transfers** from disk and the **number of seeks** as the cost measures
 - t_T time to transfer one block
 - Assuming for simplicity that write cost is same as read cost
 - t_s time for one seek
 - Cost for b block transfers plus S seeks $b * t_T + S * t_S$
- t_S and t_T depend on where data is stored; with 4 KB blocks:
 - High end magnetic disk: $t_S = 4$ msec and $t_T = 0.1$ msec
 - SSD: t_S = 20-90 microsec and t_T = 2-10 microsec for 4KB



MEASURES OF QUERY COST (CONT.)

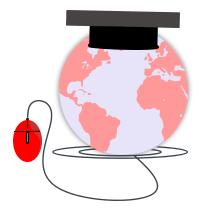
- Required data may be buffer resident already, avoiding disk I/O
 - But hard to take into account for cost estimation
- Several algorithms can reduce disk IO by using extra buffer space
 - Amount of real memory available to buffer depends on other concurrent queries and OS processes, known only during execution
- Worst case estimates assume that no data is initially in buffer and only the minimum amount of memory needed for the operation is available
 - But more optimistic estimates are used in practice



SELECTIONS INVOLVING EQUALITY

COST ESTIMATES FOR SELECTION ALGORITHMS

| | Algorithm | Cost | Reason |
|----|--|--------------------------------------|---|
| A1 | Linear Search | $t_S + b_r * t_T$ | One initial seek plus b_r block transfers, where b_r denotes the number of blocks in the file. |
| A1 | Linear Search, Equality on Key | Average case t_S + $(b_r/2) * t_T$ | Since at most one record satisfies condition, scan can be terminated as soon as the required record is found. In the worst case, b_r blocks transfers are still required. |
| A2 | Primary B ⁺ -tree Index, Equality on Key | $(h_i + 1) * (t_T + t_S)$ | (Where h_i denotes the height of the index.) Index lookup traverses the height of the tree plus one I/O to fetch the record; each of these I/O operations requires a seek and a block transfer. |





SELECTIONS INVOLVING EQUALITY(2)

COST ESTIMATES FOR SELECTION ALGORITHMS

| Primary | $h_i * (t_T +$ | One seek for each level of the tree, one |
|-----------------------------|--|--|
| | , | seek for the first block. Here b is the |
| , | 3, 10.1 | number of blocks containing records |
| | | with the specified search key, all of |
| | | which are read. These blocks are leaf |
| | | blocks assumed to be stored sequen- |
| | | tially (since it is a primary index) and |
| | | don't require additional seeks. |
| Secondary | $(h_i + 1) *$ | This case is similar to primary index. |
| B ⁺ -tree Index, | $(t_T + t_S)$ | |
| Equality on | | |
| Key | | |
| Secondary | $(h_i + n) *$ | (Where n is the number of records |
| B ⁺ -tree Index, | $(t_T + t_S)$ | fetched.) Here, cost of index traversal |
| Equality on | | is the same as for A3, but each record |
| | | may be on a different block, requiring a |
| | | seek per record. Cost is potentially very |
| | | high if n is large. |
| | B ⁺ -tree Index, Equality on Key Secondary | B+-tree Index, Equality on Nonkey Secondary $(h_i + 1) *$ B+-tree Index, Equality on Key Secondary $(h_i + t_S)$ Equality on Key $(h_i + t_S) *$ $(t_T + t_S)$ Equality on Equality on |

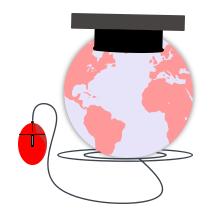




SELECTIONS INVOLVING COMPARISONS

COST ESTIMATES FOR SELECTION ALGORITHMS

| A5 | Primary | $h_i * (t_T +$ | Identical to the case of A3, equality on |
|----|-----------------------------|---------------------|--|
| | B ⁺ -tree Index, | t_S) + $b * t_T$ | nonkey. |
| | Comparison | | |
| A6 | Secondary | $(h_i + n) *$ | Identical to the case of A4, equality on |
| | B ⁺ -tree Index, | $(t_T + t_S)$ | nonkey. |
| | Comparison | | |





JOIN OPERATION

- Several different algorithms to implement joins
 - Nested-loop join
 - Block nested-loop join
- Choice based on cost estimate
- Examples use the following information
 - Number of records of student: 5,000 takes: 10,000
 - Number of blocks of student: 100 takes: 400



NESTED-LOOP JOIN

```
• To compute the theta join r \bowtie_{\theta} s for each tuple t_r in r do begin for each tuple t_s in s do begin test pair (t_r, t_s) to see if they satisfy the join condition \theta if they do, add t_r \bullet t_s to the result. end end
```

- r is called the outer relation and s the inner relation of the join.
- Requires no indices and can be used with any kind of join condition.
- Expensive since it examines every pair of tuples in the two relations.



NESTED-LOOP JOIN (CONT.)

- In the worst case, if there is enough memory only to hold one block of each relation, the estimated cost is $n_r * b_s + b_r$ block transfers, plus $n_r + b_r$ seeks
- If the smaller relation fits entirely in memory, use that as the inner relation.
 - Reduces cost to $b_r + b_s$ block transfers and 2 seeks
- Assuming worst case memory availability cost estimate is
 - with student as outer relation:
 - 5000 * 400 + 100 = 2,000,100 block transfers,
 - 5000 + 100 = 5100 seeks
 - with takes as the outer relation
 - 10000 * 100 + 400 = 1,000,400 block transfers and 10,400 seeks
- If smaller relation (student) fits entirely in memory, the cost estimate will be 500 block transfers.
- Block nested-loops algorithm (next slide) is preferable.



BLOCK NESTED-LOOP JOIN

 Variant of nested-loop join in which every block of inner relation is paired with every block of outer relation.

```
for each block B_r of r do begin

for each block B_s of s do begin

for each tuple t_r in B_r do begin

for each tuple t_s in B_s do begin

Check if (t_r, t_s) satisfy the join condition

if they do, add t_r \bullet t_s to the result.

end

end

end
```



BLOCK NESTED-LOOP JOIN (CONT.)

- Worst case estimate: $b_r * b_s + b_r$ block transfers + 2 * b_r seeks
 - Each block in the inner relation s is read once for each block in the outer relation
- Best case: $b_r + b_s$ block transfers + 2 seeks.
- Improvements to nested loop and block nested loop algorithms:
 - In block nested-loop, use M 2 disk blocks as blocking unit for outer relations, where M = memory size in blocks; use remaining two blocks to buffer inner relation and output
 - Cost = $\lceil b_r / (M-2) \rceil * b_s + b_r$ block transfers + $2 \lceil b_r / (M-2) \rceil$ seeks
 - If equi-join attribute forms a key or inner relation, stop inner loop on first match
 - Scan inner loop forward and backward alternately, to make use of the blocks remaining in buffer (with LRU replacement)
 - Use index on inner relation if available



QUERY EVALUATION

• EQUIVALENCE RULES

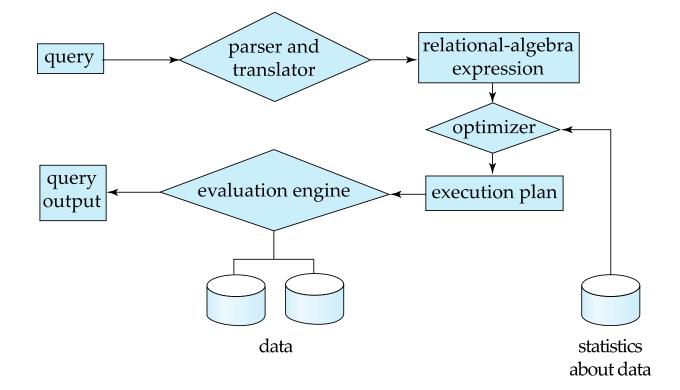


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BASIC STEPS IN QUERY PROCESSING

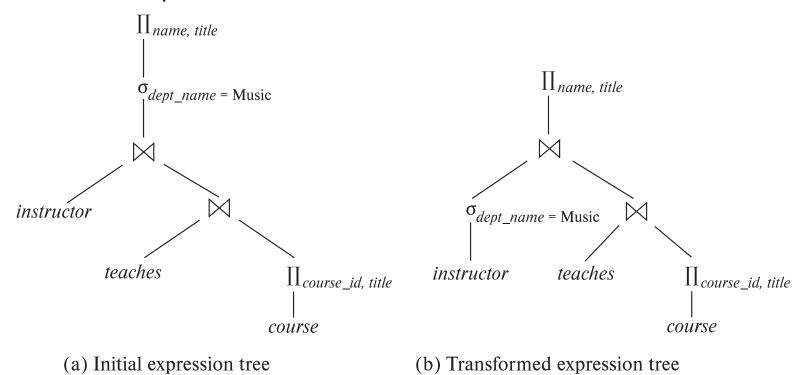
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INTRODUCTION

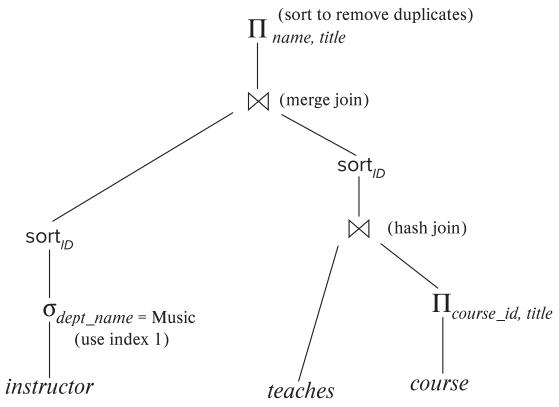
- Alternative ways of evaluating a given query
 - Equivalent expressions
 - Different algorithms for each operation





INTRODUCTION (CONT.)

• An **evaluation plan** defines exactly what algorithm is used for each operation, and how the execution of the operations is coordinated.





INTRODUCTION (CONT.)

- Cost difference between evaluation plans for a query can be enormous
 - E.g., seconds vs. days in some cases
- Steps in cost-based query optimization
 - 1. Generate logically equivalent expressions using equivalence rules
 - 2. Annotate resultant expressions to get alternative query plans
 - 3. Choose the cheapest plan based on estimated cost
- Estimation of plan cost based on:
 - Statistical information about relations. Examples:
 - number of tuples, number of distinct values for an attribute
 - Statistics estimation for intermediate results
 - to compute cost of complex expressions
 - Cost formulae for algorithms, computed using statistics



TRANSFORMATION OF RELATIONAL EXPRESSIONS

- Two relational algebra expressions are said to be equivalent if the two expressions generate the same set of tuples on every legal database instance
 - Note: order of tuples is irrelevant
 - we don't care if they generate different results on databases that violate integrity constraints
- In SQL, inputs and outputs are multisets of tuples
 - Two expressions in the multiset version of the relational algebra are said to be equivalent if the two expressions generate the same multiset of tuples on every legal database instance.
- An equivalence rule says that expressions of two forms are equivalent
 - Can replace expression of first form by second, or vice versa

EQUIVALENCE RULES

1. Conjunctive selection operations can be deconstructed into a sequence of individual selections.

$$\sigma_{\theta_1 \wedge \theta_2}(E) \equiv \sigma_{\theta_1}(\sigma_{\theta_2}(E))$$

2. Selection operations are commutative.

$$\sigma_{\theta_1}(\sigma_{\theta_2}(E)) \equiv \sigma_{\theta_2}(\sigma_{\theta_1}(E))$$

3. Only the last in a sequence of projection operations is needed, the others can be omitted.

$$\prod_{L_1}(\prod_{L_2}(...(\prod_{L_n}(E))...)) \equiv \prod_{L_1}(E)$$

where $L_1 \subseteq L_2 ... \subseteq L_n$

- 4. Selections can be combined with Cartesian products and theta joins.
 - a. $\sigma_{\theta}(E_1 \times E_2) \equiv E_1 \bowtie_{\theta} E_2$
 - b. $\sigma_{\theta_1}(E_1 \bowtie_{\theta_2} E_2) \equiv E_1 \bowtie_{\theta_1 \land \theta_2} E_2$



EQUIVALENCE RULES (CONT.)

5. Theta-join operations (and natural joins) are commutative.

$$E_1 \bowtie E_2 \equiv E_2 \bowtie E_1$$

6. (a) Natural join operations are associative:

$$(E_1 \bowtie E_2) \bowtie E_3 \equiv E_1 \bowtie (E_2 \bowtie E_3)$$

(b) Theta joins are associative in the following manner:

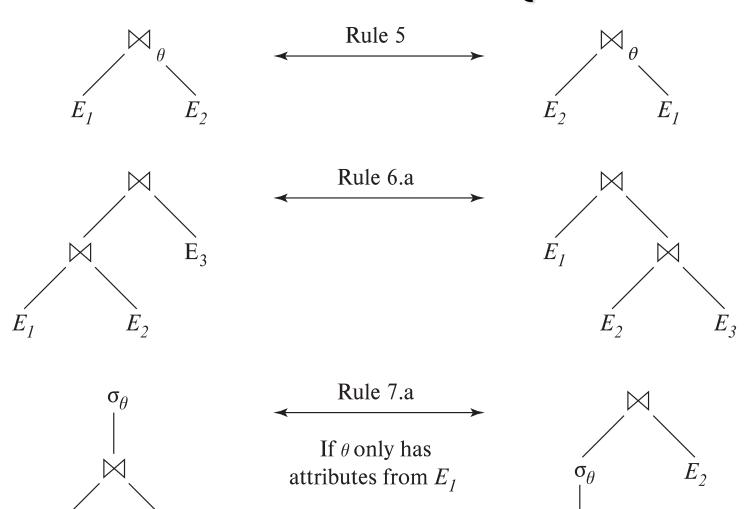
$$(E_1 \bowtie_{\theta_1} E_2) \bowtie_{\theta_2 \wedge \theta_3} E_3 \equiv E_1 \bowtie_{\theta_1 \wedge \theta_3} (E_2 \bowtie_{\theta_2} E_3)$$

where θ_2 involves attributes from only E_2 and E_3 .



PICTORIAL DEPICTION OF EQUIVALENCE

RULES



EQUIVALENCE RULES (CONT.)

- 7. The selection operation distributes over the theta join operation under the following two conditions:
 - (a) When all the attributes in θ_0 involve only the attributes of one of the expressions (E_1) being joined.

$$\sigma_{\theta_0}(\mathsf{E}_1 \bowtie_{\theta} \mathsf{E}_2) \equiv (\sigma_{\theta_0}(\mathsf{E}_1)) \bowtie_{\theta} \mathsf{E}_2$$

(b) When θ_1 involves only the attributes of E_1 and θ_2 involves only the attributes of E_2 .

$$\sigma_{\theta_1 \wedge \theta_2}(\mathsf{E}_1 \bowtie_{\theta} \mathsf{E}_2) \equiv (\sigma_{\theta_1}(\mathsf{E}_1)) \bowtie_{\theta} (\sigma_{\theta_2}(\mathsf{E}_2))$$

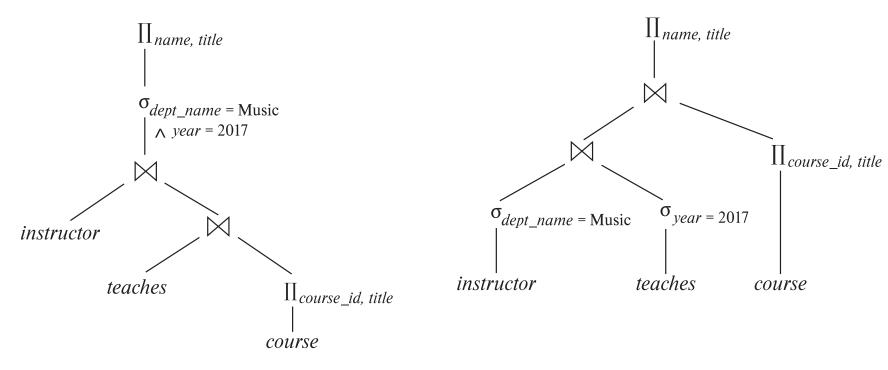


TRANSFORMATION EXAMPLE: PUSHING SELECTIONS

- Query: Find the names of all instructors in the Music department, along with the titles of the courses that they teach
 - $\Pi_{\text{name, title}}(\sigma_{\text{dept_name= 'Music'}})$ (instructor \bowtie (teaches $\bowtie \Pi_{\text{course_id, title}}$ (course))))
- Transformation using rule 7a.
 - $\Pi_{\text{name, title}}((\sigma_{\text{dept_name='Music'}}(\text{instructor})) \bowtie (\text{teaches} \bowtie \Pi_{\text{course id, title}}(\text{course})))$
- Performing the selection as early as possible reduces the size of the relation to be joined.



MULTIPLE TRANSFORMATIONS



(a) Initial expression tree

(b) Tree after multiple transformations



JOIN ORDERING EXAMPLE

• For all relations r_1 , r_2 , and r_3 ,

$$(r_1 \bowtie r_2) \bowtie r_3 = r_1 \bowtie (r_2 \bowtie r_3)$$

(Join Associativity) ⋈

• If $r_2 \bowtie r_3$ is quite large and $r_1 \bowtie r_2$ is small, we choose

$$(r_1 \bowtie r_2) \bowtie r_3$$

so that we compute and store a smaller temporary relation.



JOIN ORDERING EXAMPLE (CONT.)

Consider the expression

```
\Pi_{\text{name, title}}(\sigma_{\text{dept\_name= 'Music''}}(\text{instructor}) \bowtie \text{teaches}) \bowtie \Pi_{\text{course\_id, title}}(\text{course}))))
```

• Could compute $teaches \bowtie \Pi_{course id, title}$ (course) first, and join result with

- but the result of the first join is likely to be a large relation.
- Only a small fraction of the university's instructors are likely to be from the Music department
 - it is better to compute

first.

```
\sigma_{dept\_name= \text{ 'Music''}} (instructor) \bowtie teaches
```



COST ESTIMATION

- Cost of each operator computer
 - Need statistics of input relations
 - E.g., number of tuples, sizes of tuples
- Inputs can be results of sub-expressions
 - Need to estimate statistics of expression results
 - To do so, we require additional statistics
 - E.g., number of distinct values for an attribute



Choice of Evaluation Plans

Must consider the interaction of evaluation techniques when choosing evaluation plans choosing the cheapest algorithm for each operation independently may not yield best overall algorithm.



VIEWING QUERY EVALUATION PLANS

- Most database support explain <query>
 - Displays plan chosen by query optimizer, along with cost estimates
 - Some syntax variations between databases
 - Oracle: explain plan for <query> followed by select * from table (dbms_xplan.display)
 - SQL Server: set showplan_text on
- Some databases (e.g. PostgreSQL) support explain analyse <query>
 - Shows actual runtime statistics found by running the query, in addition to showing the plan
- Some databases (e.g. PostgreSQL) show cost as f..l
 - f is the cost of delivering first tuple and l is cost of delivering all results



REFERENCE

Silberschatz, Korth, and Sudarshan. *Database System Concepts* – 7th Edition. McGraw-Hill. 2019. Slides adapted from Database System Concepts Slide.

Source: https://www.db-book.com/db7/slides-dir/index.html



