ATTENDANCE RECORD



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Start: 9:10am

DATA STRUCTURE AND PROGRAMMING II

Chapter 12: Tree data structure



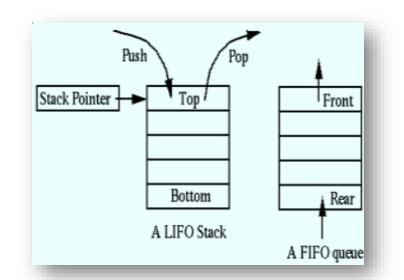
Outline

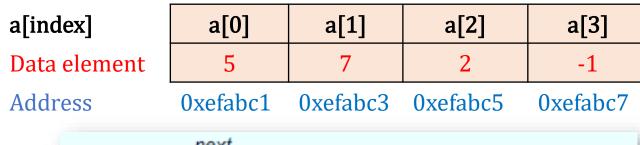
- Data structure
 - Linear Vs. Non linear
- What is Tree? Binary tree? Binary search tree (BST)?
- What are Tree operations?
- Traversal of Tree
- How to implement Tree in C++
- Examples

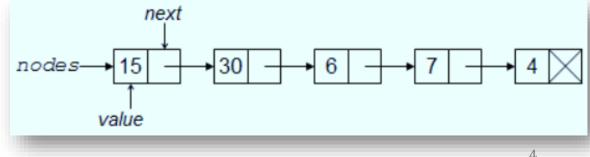
Data structure

☐ Linear Data Structure

- Data structure helps to store and organize data in computer
- Linear data structure stores data in such a way that the data can be accessed sequentially (continuous)
 - Array, linked list, stack queue







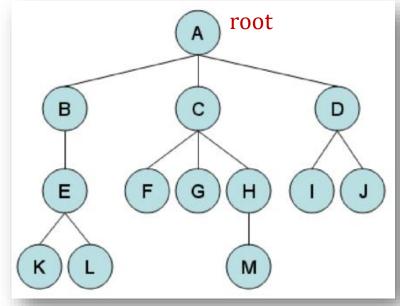
Linear Vs. Non-linear data structure

Comparison

| Factor | Linear data structure | Non-linear data structure |
|--------------------|--|--|
| How data is stored | Data elements construct a sequence of a linear list. | Does not arrange data consecutively but arrange in sorted order. |
| Traversal of data | Data elements are visited sequentially Traversal of element is easy | Traversal of data elements and insertion/deletion are not done sequentially Traversal of element is difficult |
| Implementation | Simple | Complex |
| Levels | Single level of elements | Multiple levels of elements (hierarchical) |
| Memory utilization | Ineffective | Effective |
| Example | Array, linked list, stack, queue | Tree, graph |

Tree

- A tree is a hierarchical (non-linear) data structure defined on a set of elements called nodes
- A tree can be empty or composed of nodes
 - The top-level node is called *root*,
 while other nodes are sub-tree



An example of a tree

Tree

☐ Relation of Tree

■ **Root** : top element

■ Children : have same parents,

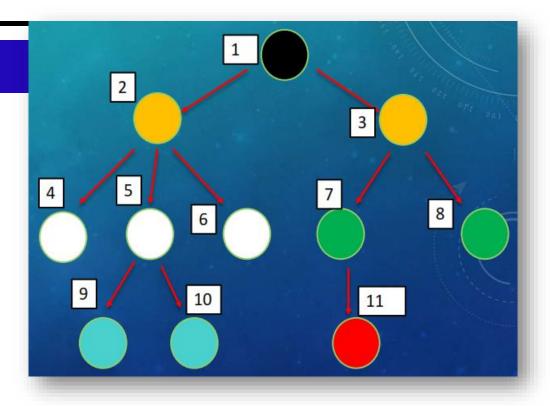
grant parents, great grant parents, ...

Parents: have children

• **Siblings** : have same parent

• **Leaf** : is element that has no children

• Remark: In particular, leaf element has pointer points to NULL



How many leaves are there?

=> 6

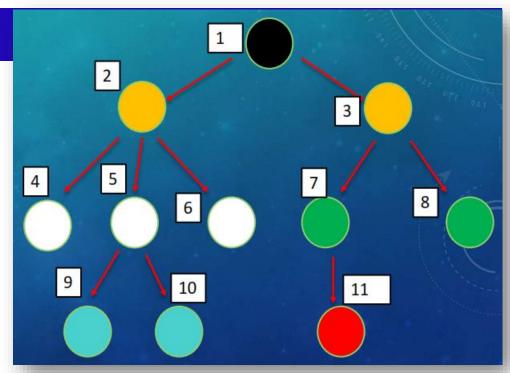
What are they?

=> 4, 9, 10, 6, 11, 8

Relation of Tree

☐ Edge Vs. Depth Vs. Height

- Edge (path)
 - An edge is a line connected two nodes together
 - If a tree have N nodes, then it has (N-1) edges
- Depth of node x
 - Depth of node x is number of edges from x to root
 - <u>Note</u>: Depth of root is 0
- Height of node x
 - Height of node x is number of edges on longest path from x to a leaf
- Remark:
 - Height of a tree = depth of a tree = longest path of the tree
 - Size of a tree is the number of elements (nodes)
 - Branch is any path from the root to a leaf



How many edges? \Rightarrow 10 edges What is the depth of node 7? \Rightarrow 2 What is the height of node 1? \Rightarrow 3

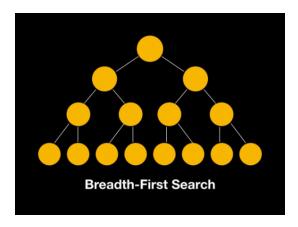
Tree applications

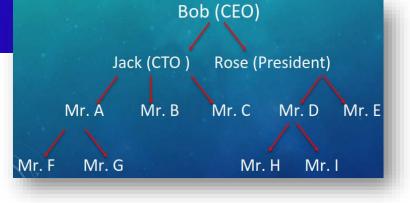
☐ Some examples

1. Store hierarchical data

(file system)

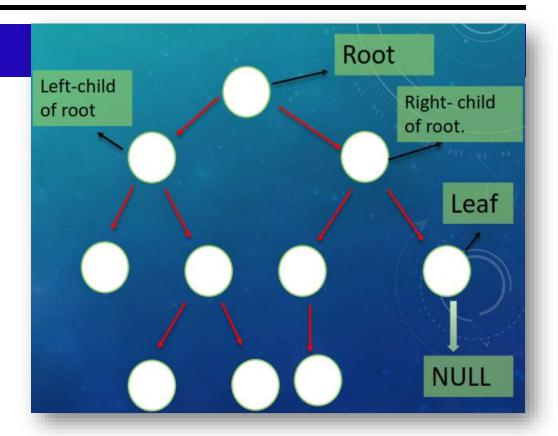
- 2. Organize data for quick search, insertion, deletion
 - Binary search tree (BST)
- 3. Dictionary
- 4. Network routing algorithm





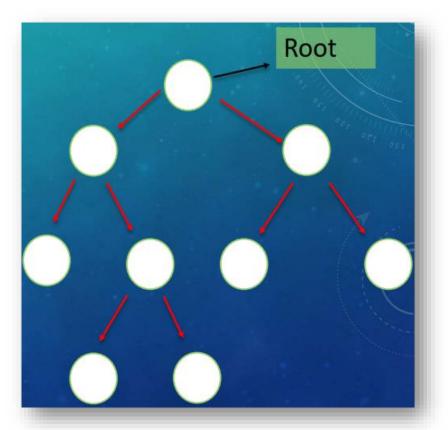
Binary Tree

- Each node can have at most 2 children
- A node has left and/or right child
- A leaf node has no left or right child.
 - It has only NULL
- Types of Binary Tree
 - 1. Strict/proper/full binary tree
 - 2. Complete binary tree
 - 3. Perfect binary tree



Strict/proper/full Binary Tree

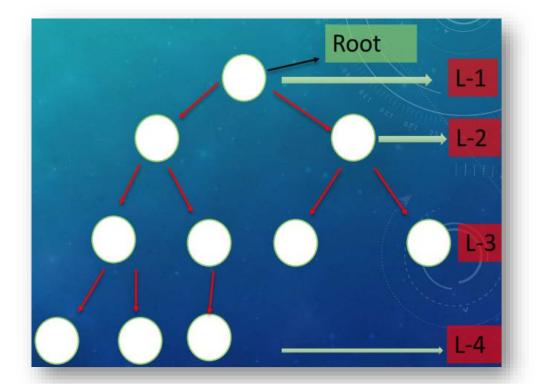
- Each node can have either 2 or 0 child
- It can not have only one left or right child

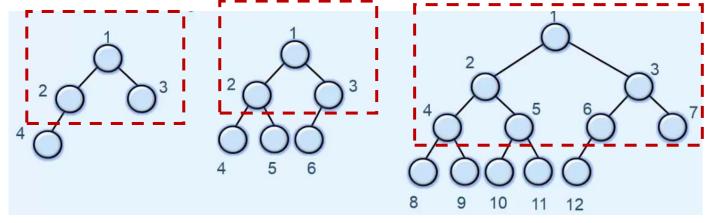


Complete Binary Tree

Definition

 A complete binary tree is a binary tree in which every level, except possibly the last level, is completely filled and all nodes are as far left as possible.

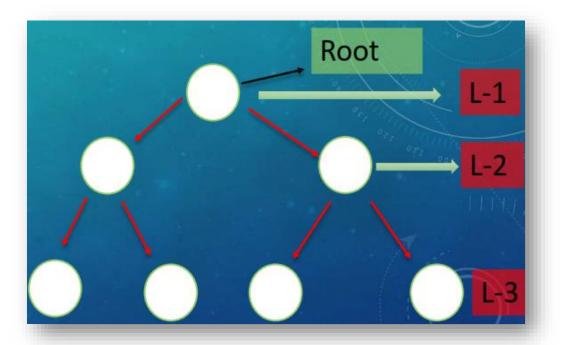




Perfect Binary Tree

Definition

All levels are completed filled and balanced

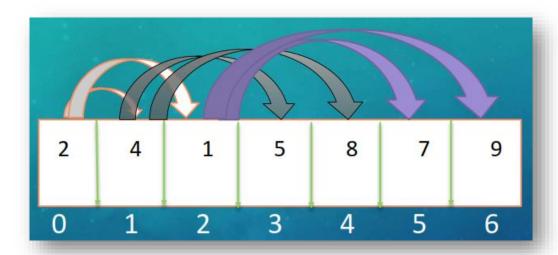


Tree Implementation

Tree implementation

- ☐ There are 2 types of implementation
- Dynamically created nodes
- 2. Array

- int data; struct Node *left; struct node *right;
- struct Node{
- It work only for Perfect Binary Tree
 - For node at index i
 - Left child's index = 2i + 1
 - Right child's index = 2i + 2

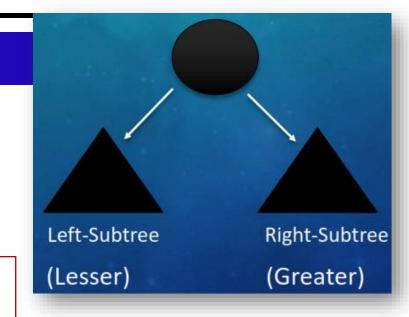


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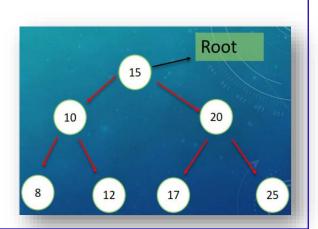
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Binary Search Tree (BST)

- A BST is a binary tree that is constructed in such a way that it is easy to search for the values it contains
- Rules in BST
 - ❖ All values less than (or equal) to root value are stored in the left subtree
 - ❖ All values greater than the root are stored in the right subtree



- **Example**: Suppose we have number 15 as root. We want to add **10, 20, 8, 12, 17, 25** to the tree.
 - 10 < 15 => 10 is inserted to left of the root
 - 20>15 => 20 is inserted to right of the root
 - 8<15 => 8 goes left
 - 8<10 => 8 goes left
 - ... etc.



Insert a node in BST

Definition

- To insert a new item in a tree, we should check that there is no duplication
 - If a new value is less than the current node's value
 - Go to the left subtree
 - Else,
 - Go to the right subtree

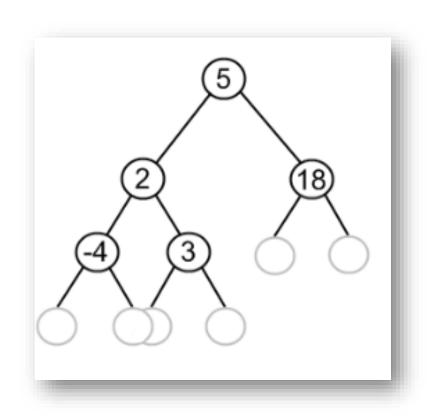
Remark:

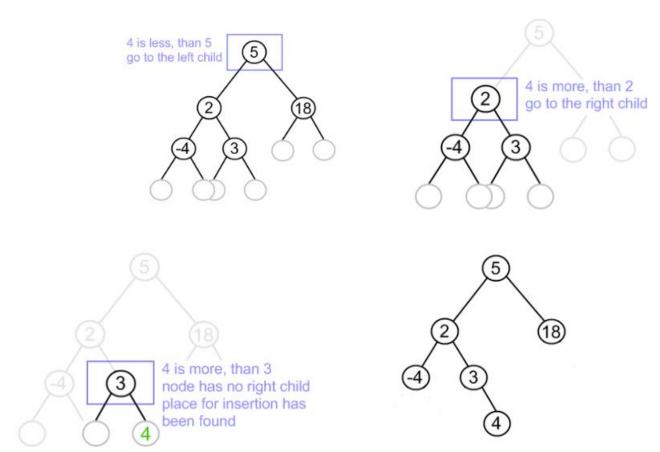
- With this simple rule, the algorithm reaches a node (leaf) which has no left/right subtree
- By the moment a place for insertion is found, we can say that a new value has no duplicate in the tree

Insert a node in BST

☐ Example

• Given a tree below on the left. How to add node of 4 to this tree?



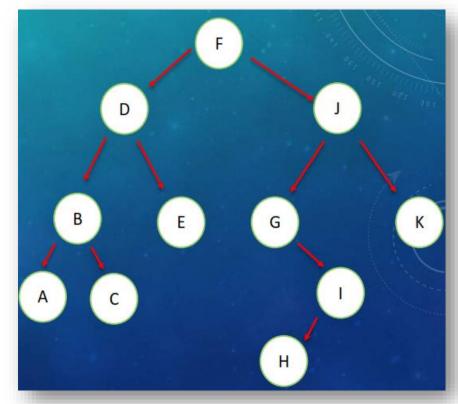


Insert data to a tree by knowing the tree's root

```
Node *insert(Node *root, int data){
           if(root==NULL){
                root=new Node;
3
                                              Insert data
4
                root->left=NULL;
                root->right=NULL;
5
                root->data=data;
6
           }else if(data < root->data){
                                                                    Go left
                root->left = insert(root->left, data);
8
           }else if(data > root->data){
9
                                                                    Go right
               root->right = insert(root->right, data);
10
11
12
           return root;
13
```

Traversal of Binary Tree

- Traversal of a tree is a way that is used to visit each node in the tree
- 2 main types of tree traversal
 - 1. Breadth-first (level-order) traversal
 - FDJBEGKACIH
 - 2. Depth-first traversal
 - Pre-order
 - In-order
 - Post-order



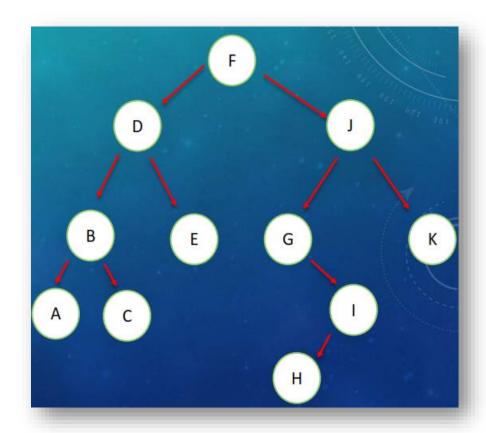
Depth-first Traversal

- 1. Pre-order
- 2. In-order
- 3. Post-order

Pre-order Traversal

- It follows data-left-right order (DLR)
- <root's data><left><right>
 - FDBACEJGIHK

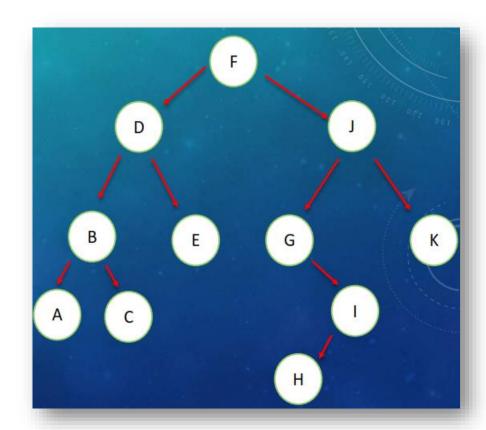
```
void preorder(Node *root){
    if(root!=NULL){
        cout<<root->data;
        preorder(root->left);
        preorder(root->right);
    }
}
```



In-order Traversal

- It follows left-data-right order (LDR)
- <left>< root's data ><right>
 - ABCDEFGHIJK

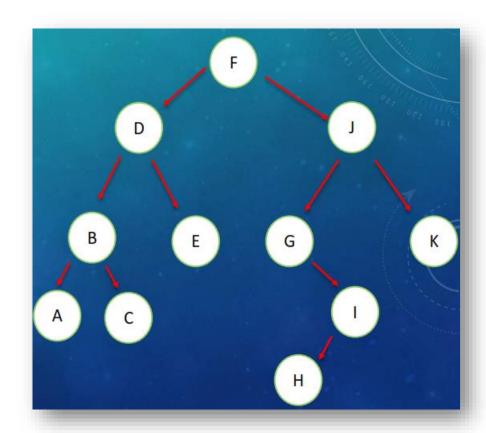
```
void inorder(Node *root){
    if(root!=NULL){
        inorder(root->left);
        cout<<root->data;
        inorder(root->right);
    }
}
```



Post-order Traversal

- It follows left-right-data order (LRD)
- <left><right><root's data>
 - ACBEDHIGKJF

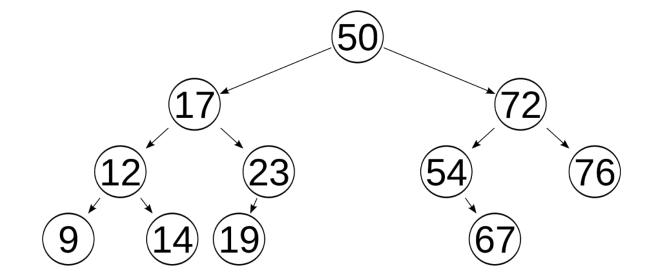
```
void postorder(Node *root){
    if(root!=NULL){
        postorder(root->left);
        postorder(root->right);
        cout<<root->data;
    }
}
```



Practice: Tree traversal

What are the outputs?

- a. Pre-order traversal
- b. In-order traversal
- c. Post-order traversal



Outputs:

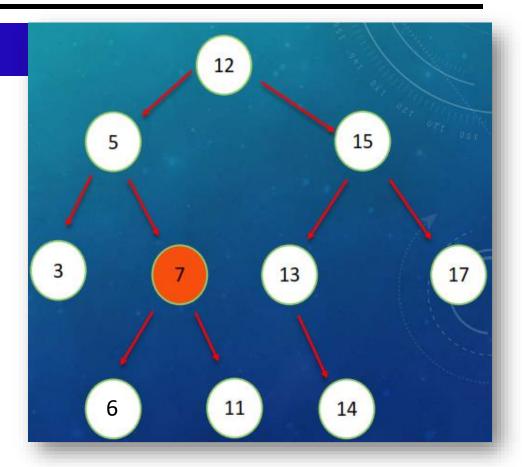
Pre-order traversal: 50 17 12 9 14 23 19 72 54 67 76 In-order traversal: 9 12 14 17 19 23 50 54 67 72 76 Post-order traversal: 9 14 12 19 23 17 67 54 76 72 50

Search for an Element in BST

Definition

Loop to each node and compare the data

```
bool search(Node *root, int data){
     if(root == NULL){
          return false;
     }else if(data == root->data){
          return true;
     }else if(data > root->data){
          return search(root->right, data);
     }else if(data < root->data){
          return search(root->left, data);
```



Combination of codes for implementing a tree

```
struct Node{
    char data;
    struct Node *left;
    struct Node *right;
};

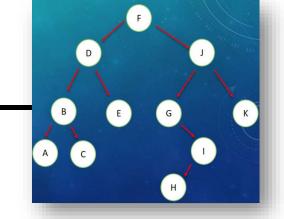
int getSize(No
    if (root ==
        return 0;
    }else{
        return (1 + getSize(root))
    }
}
```

```
int getSize(Node *root){
  if (root == NULL){
    return 0;
  }else{
    return (1 + getSize(root->left)
  + getSize(root->right));
  }
}
```

```
Node *insert(Node *root, char data){
     if(root==NULL){
           root=new Node( );
           root->left = NULL;
           root->right = NULL;
           root->data=data:
     }else if(data < root->data){
           root->left = insert(root->left, data);
      }else if(data > root->data){
           root->right= insert(root->right, data);
     return root;
```

```
bool search(Node *root, char data){
    if(root==NULL){
        return false;
    }else if(data == root->data){
        return true;
    }else if(data >= root->data){
        return search(root->right, data);
    }else if(data <= root->data){
        return search(root->left, data);
    }
}
```

```
void preorder(Node *root){
    if(root!=NULL){
        cout<<root->data<<"";
        preorder(root->left);
        preorder(root->right);
    }
}
```



```
int main(){

Node *root=NULL;
  //root=new Node; //error, no need
  root = insert(root, 'F');
  root = insert(root, 'D');
  root = insert(root, 'B');
  root = insert(root, 'B');
  root = insert(root, 'E');
  root = insert(root, 'G');
  root = insert(root, 'K');
  root = insert(root, 'A');
  root = insert(root, 'I');
  root = insert(root, 'I');
  root = insert(root, 'H');
  preorder(root); cout<<endl;
}</pre>
```

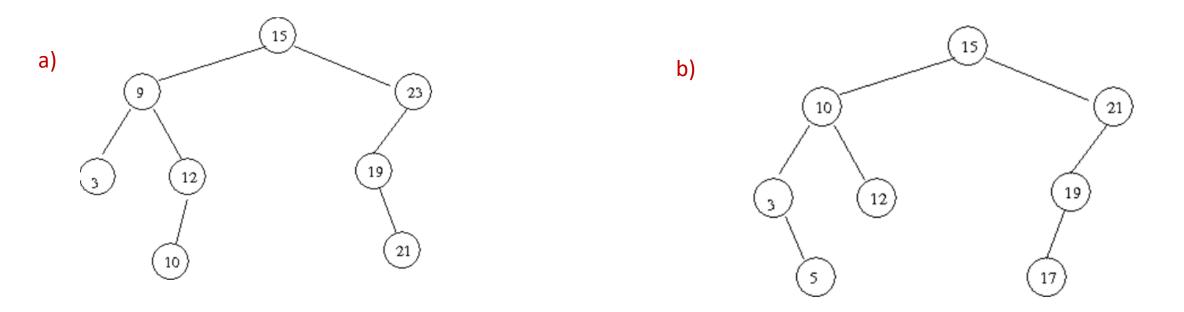
Output: F D B A C E J G I H K

In-class activity:

Now display using in-order and post-order traversal?

Q and A

More practices: What are the outputs of post-order, in-order, and post-order traversal for each tree?



Practice

Exercise

- 1. Write a program to create the tree below.
 - a. Display this tree using an in-order traversal.
 - b. Keep asking a user to input a number and search whether it is in the tree.
 - If exist in the tree, then display a message
 - "This number *n* is in the tree".
 - Otherwise, display a message
 - "*n* does not exist in the tree"

