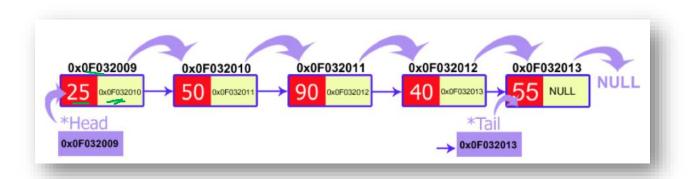
DATA STRUCTURE & PROGRAMMING II

Chapter 9- Linked List



Prepared by:

Lecture overview

☐ Overall lectures

- 1. Introduction to algorithm
- 2. Basic data types and statements
- 3. Control structures and Loop
- 4. Array
- 5. Data structure
- 6. Sub-programs

- 7. Recursive
- 8. Pointers



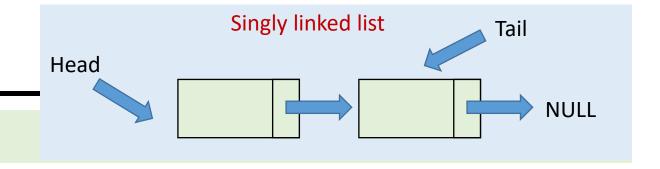
- 9. Linked Lists
- 10. Stacks and Queues
- 11. Sorting algorithms
- 12. Trees



Outline

- ☐ A Brief of Outline
- What is linked list?
 - Single linked list? Double linked list?
- What are the advantages of using linked list and array?
- Linked list implementation in C++
 - Examples

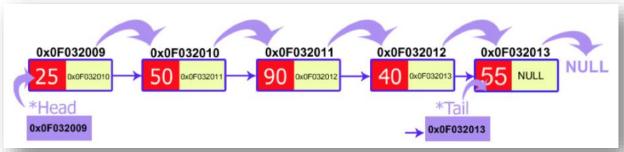
What is Linked list?



- Definition
- A linked list is a data structure that can store an indefinite amount of elements (dynamic size)
- In a linked list, each element is linked with each other. Elements in a linked list are accessed sequentially.
- Each element contains
 - ✓ Data
 - ✓ A link (pointer)
 - ✓ to its next element (successor)
 - ✓ and/or to its previous element (predecessor)
- or)

- struct Element
 - data: integer
 - *next: Element
- End struct

- struct List
 - n: integer
 - *head: Element
 - *tail: Element
- End struct



- Element = called a *node*
- In linked list, the first element is *head* and the last element is *tail*

Array Vs. Linked List

☐ Pros and Con

Array

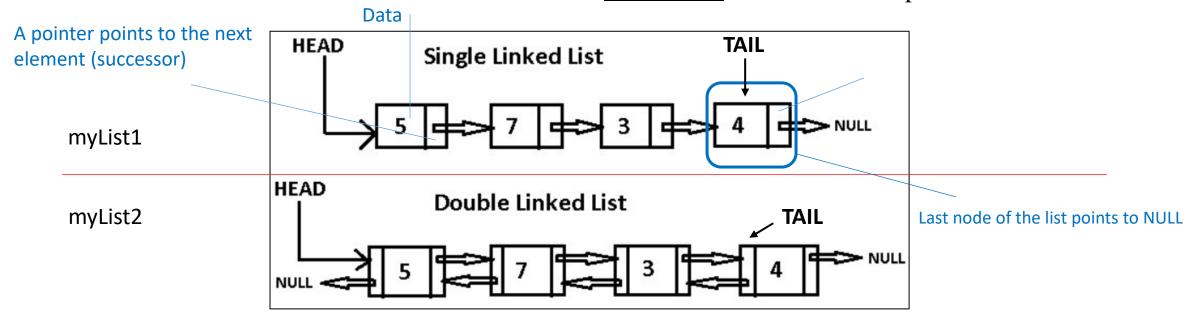
- Fixed size
- Once created, can't add or reduce
 number of elements to be stored
- Can random access
- Faster access
 - Elements in contiguous memory locations

Linked List

- Dynamically shrink and grow
- Dynamic memory management
- No random access is allowed
- Slower access
 - Elements not in contiguous memory locations

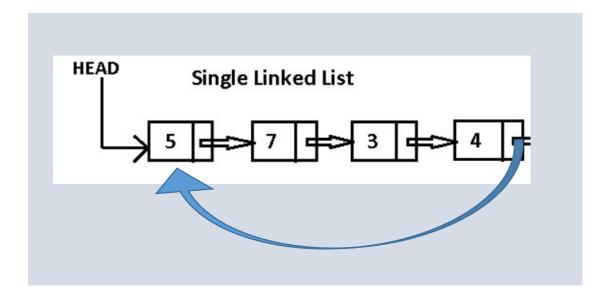
What is Linked list?

- ☐ Type of Linked List
- There are two types of linked lists:
 - A single linked list is a linked list that has a link to either its successor or predecessor.
 - A double linked list is a linked list that has **both links** to successor and predecessor.



Remark

• A single or double linked list can be called a circular linked list when the last element (tail) points to the first element (head).



Circular linked list

List Operations

- ☐ Operations with a list
- ✓ Creating a list
- ✓ Insert a new element to a list
 - ✓ Insert to beginning, end, at a position
- ✓ Delete an element from a list
 - ✓ Delete to beginning, end, at a position
- ✓ Search an element in a list
- ✓ Update an element in a list

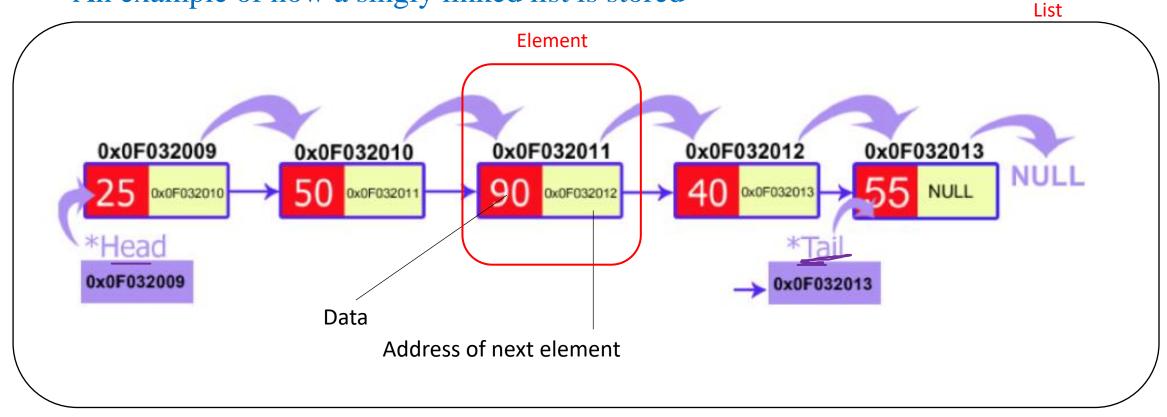
- ✓ Display data in list
- ✓ Reverse a list
- ✓ Combine two lists
- ✓... etc.

Singly Linked List (SLL)

Singly linked list

☐ Overview

An example of how a singly linked list is stored



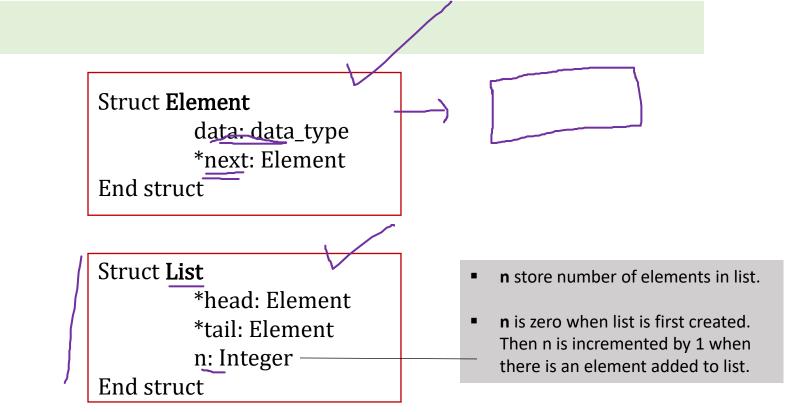
List operation

- ☐ Operation with a list
- All elements of a linked list can be accessed by
 - First setup a pointer pointing to the first element (node) of the list
 - Loop to traverse the list until NULL

- One of the disadvantage of the single linked list is
 - Given a pointer A to a node, we can not reach any of the nodes that precede the node (previous element) to which A is pointing

Operation on linked list

- Operations
- Important operation
 - Create a list
 - Insert element to the list
 - At the beginning
 - At the end
 - · At the specific position
 - Delete the element
 - At the beginning
 - At the end
 - · At the specific position
 - Destroy a list



Examples

☐ Create an element

Var *head, *tmp : Element

• Create an empty list

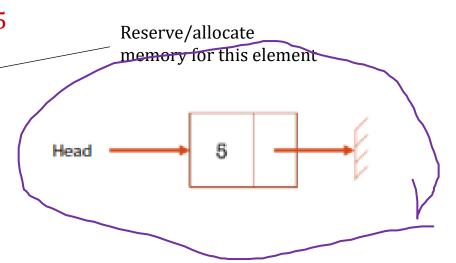
head ← null



Add an element of the list with value 5

Dadress

tmp ← new(size(Element)) tmp→ data ← 5 tmp→ next ← null head ← tmp

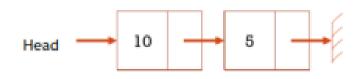


Examples

☐ Add and remove element

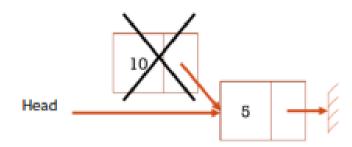
Add a new element containing value 10 to the beginning of the list

```
tmp ← new(size(Element))
tmp→ data ← 10
tmp→ next ← head
head ← tmp
```



• Delete the first element from the list

```
tmp ← head
head ← head → next
free(tmp)
```



Create a list

☐ A function to create an empty list

```
Function create_list( ) : Pointer of List
          var *ls: List
          ls \leftarrow new(size(List))
          ls \rightarrow n \leftarrow 0
          ls→head ← null
          ls→tail ← null
          return ls
End function
```

Steps to create an empty list:

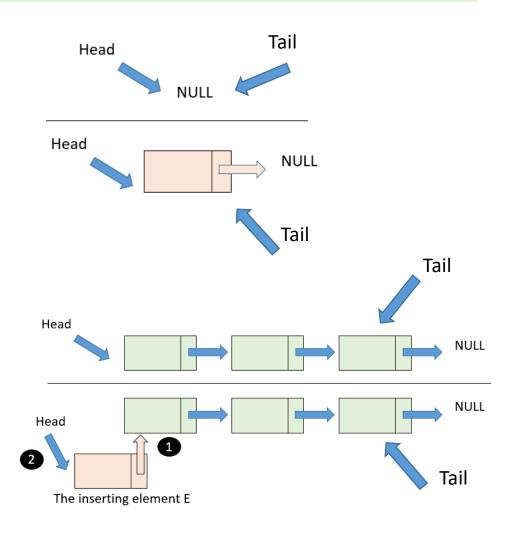
- 1. Create a list variable
- 2. Allocate memory
- 3. Set 0 to n since we are creating an empty list
- 4. Head points to null
- 5. Tail points to **null**

Insertion

☐ Insert an element to the beginning of the list

Steps to add element to beginning of list

- Create a new element E
- 2. Make next pointer of E points to head of list
- 3. Update E to be head of list
- 4. Update tail if needed
- 5. Increase n by 1 (n is number of elements in list)



Display elements in list

```
Procedure void(*ls: List)

var *tmp: Element

tmp ← ls→head

while(tmp!=NULL) do

write(tmp→data)

tmp ← tmp→next

end while

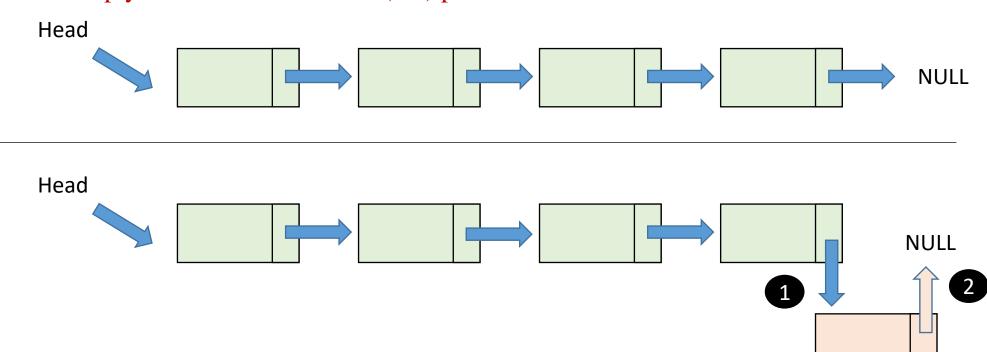
End procedure
```

Steps to display element in list

- 1. Start from head
- 2. Move to each element each time
- 3. ...
- 4. ...

Insertion

- ☐ Insert an element to the end of the list
- Create an element E
- Simply make the last element (tail) points to E



The inserting element E

Insert an element to the list

☐ Insert an element to end of the list

```
Procedure insert_end(*ls: List, d: data_type)
           var *E: Element
            if (ls \rightarrow n == 0) then
                        insert_be(ls, d)
            else
                       E ← new(size(Element))
E→data ← d
                        E \rightarrow next \leftarrow null
                        ls→tail→next ← E
                        ls→tail ← E -
                        ls \rightarrow n \leftarrow ls \rightarrow n + 1
            end if
End procedure
```

```
Steps to add element to end of list
```

```
    ...
    ...
    ...
    ...
```

Q&A

Implementation

26 27

28

return ls:

```
31
                                                       //Create new element
                                             32
                                                       Element *e;
                                             33
                                                       e = new Element();
     #include<iostream>
                                             34
                                                       e->data = newData;
     using namespace std;
                                             35
     struct Element{
                                             36
                                                       //Update pointer, head, tail
 4
          int data;
                                             37
                                                       e->next = ls->head:
 5
          Element *next;
                                             38
                                                       ls->head = e;
                                                                                            \equivint main(){
 6
                                             39
                                                       if(ls->n == 0){
                                                                                       58
                                             40
                                                           ls->tail = e;
     typedef struct Element Element;
                                                                                       59
                                                                                                 List *L;
                                             41
 8
                                                                                       60
                                                                                                 L = createList();
                                             42
                                                       1s->n = 1s->n + 1;
 9
     struct List{
                                                                                       61
                                             43
                                                                                       62
                                                                                                 insert begin(L, 3);
          int n; //number of elements
10
                                             44
                                                                                       63
                                                                                                 insert begin(L, 2);
11
          Element *head;
                                             45
                                                   void displayList(List *ls) {
                                                                                       64
                                                                                                 insert begin(L, 5);
12
          Element *tail;
                                             46
                                                       Element *tmp; //temporary var.
                                                                                       65
                                                                                                 displayList(L);
13
                                             47
                                                                                       66
                                                                                                 displayList(L);
14
     typedef struct List List;
                                             48
                                                       tmp = ls->head;
                                                                                                 displayList(L);
                                                                                       67
                                             49
                                                       while(tmp!=NULL) {
                                                                                       68
                                                                                                 cout<<L->n<<endl;
17
     //A function to create an empty list
                                             50
                                                           cout<<tmp->data<<" ";</pre>
                                                                                       69
18
    —List* createList() {
                                             51
                                                           tmp = tmp->next;
19
         List *ls;
                                             52
20
                                             53
                                                       cout << endl;
21
         ls = new List(); //allocate memor 54
22
         //ls.n = 0; //error
23
         ls->n = 0;
         ls->head = NULL;
24
25
         ls->tail = NULL;
```

30

void insert begin(List *ls, int newData) {

How to delete data from linked list

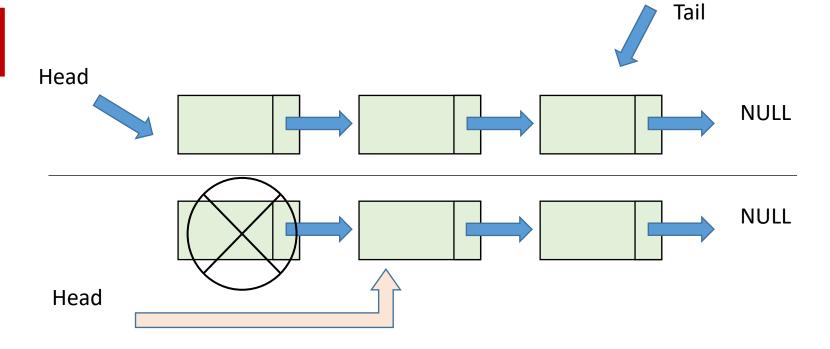
Delete first element (delete from beginning)



Deletion

☐ Delete the first element

Before



After

Delete the first element (delete beginning)

```
Procedure delete_be(*ls: List)
        //1) Get reference to head of list
      var *tmp: Element
      tmp \leftarrow ls \rightarrow head
        //2) Make next element become head
      ls \rightarrow head \leftarrow ls \rightarrow head \rightarrow next
        //3) Delete tmp (old head)
      free(tmp)
         //4) Update tail if necessary
      if (ls \rightarrow n == 1) then
             ls→tail ← NULL
      end if
      ls \rightarrow n \leftarrow ls \rightarrow n - 1
End procedure
```

```
73
     void delete be(List *ls) {
74
          //1) Get reference to head of list
75
         Element *tmp;
76
         tmp = ls->head;
77
          //2) Make next element become head
         ls->head = ls->head->next;
78
79
          //3) Delete tmp (old head)
80
         delete tmp;
81
         //4) Update tail if necessary
82
         if (ls->n == 1) {
83
              ls->tail = NULL;
84
         ls->n = ls->n - 1;
85
86
```

Delete first element (delete beginning)

How it works ...?

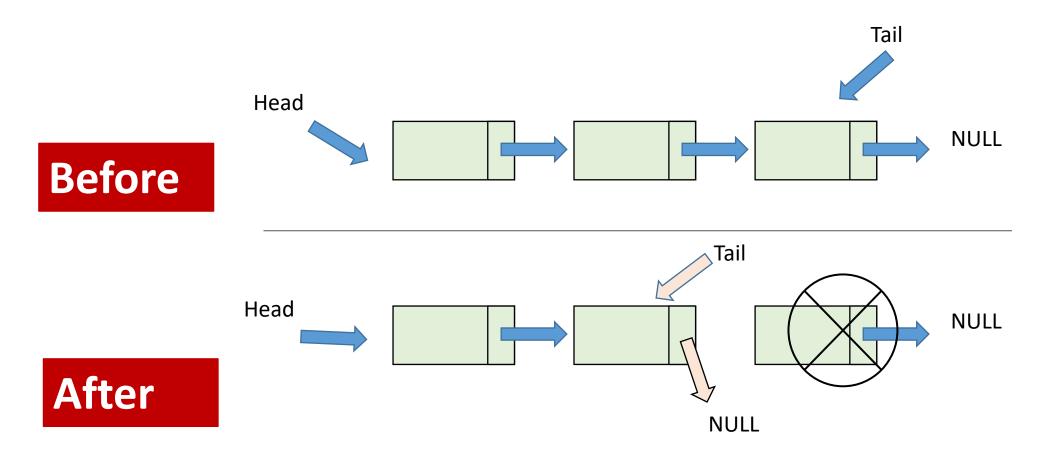
How to delete data from linked list

❖ Delete last element (delete from end)



Deletion

☐ Delete the last element from single linked list



Delete the last element

```
Procedure delete_last(*ls: List)
       var *tmp: Element
       var i: integer
       if(ls \rightarrow n==1) then
                delete_be(li)
        else
                 //Go to the 2<sup>nd</sup> last element
                tmp ← ls→head
                for(i \leftarrow 1; \leq ls \rightarrow n - 2; i++) do
                       tmp \leftarrow tmp \rightarrow next
                end for
                 //update tail and delete last old element
               ls→tail ← tmp
               tmp \leftarrow tmp \rightarrow next 3
                ls→tail→next ← NULL 4
               free(tmp)
                ls \rightarrow n \leftarrow ls \rightarrow n - 1
        end
End procedures
```

```
88
      void delete last(List *ls) {
 89
           Element *tmp;
 90
 91
           if(ls->n == 1){
 92
               delete be(ls);
 93
           }else{
 94
               tmp = ls->head;
 95
               for(int i=1; i<=ls->n - 2; i++) {
 96
                    tmp = tmp->next;
 97
 98
               ls->tail = tmp;
 99
100
               tmp = tmp->next;
101
               ls->tail->next = NULL;
102
               delete tmp;
103
               ls->n = ls->n - 1;
104
105
```

Delete first element (delete beginning)





How to delete data from linked list

Delete all data(destroy list)



Destroy a list



☐ Delete all data in list

```
void destroy_list(List *ls) {
while(ls->n > 0) {
    delete_be(ls);
}
end while

End procedure
```

```
Procedure delete be(*ls: List)
              //1) Get reference to head of list
             var *tmp: Element
             tmp ← ls→head
               //2) Make next element become head
             1 \rightarrow \text{head} \leftarrow \text{ls} \rightarrow \text{head} \rightarrow \text{next}
              //3) Delete tmp (old head)
             free(tmp)
              //4) Update tail if necessary
             if (ls \rightarrow n == 1) then
                         ls→tail ← NULL
             end if
             ls \rightarrow n \leftarrow ls \rightarrow n + 1
End procedure
                Delete first element
                    (delete beginning)
```





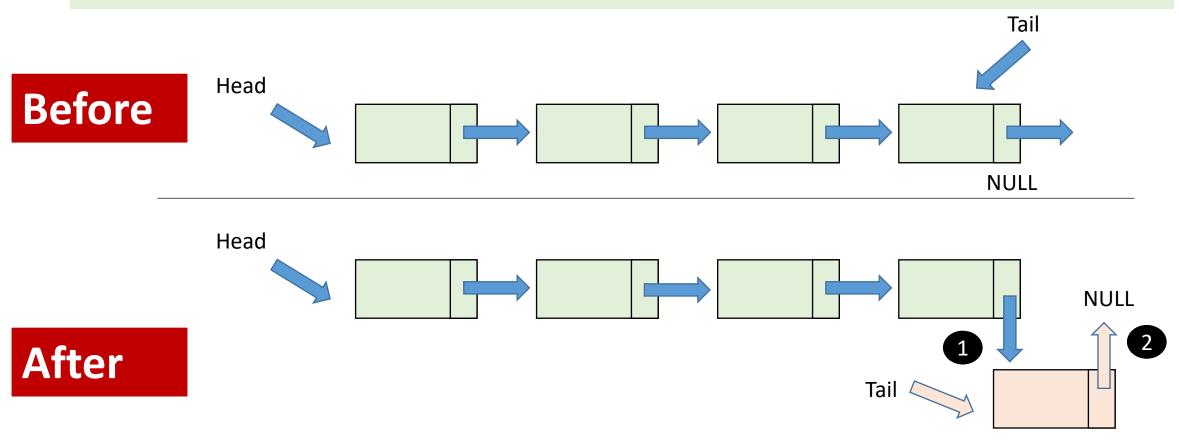
How to add data to linked list

❖ Add to end of list





☐ Insert an element to the end of the list



The inserting element E

Insert an element to the list

☐ Insert an element to end of the list

```
void insert end(List *ls, int newData) {
                                                      56
                                                      57
                                                                   if(ls->n == 0) {
Procedure insert_end(*ls: List, d: data_type)
                                                      58
                                                                         insert begin(ls, newData);
          var *E: Element
                                                      59
                                                                    }else{
          if (ls \rightarrow n == 0) then
                                                                          //Create new element
                                                      60
                    insert_be(ls, d)
                                                                         Element *e;
                                                      61
          else
                                                      62
                                                                         e = new Element();
                    E \leftarrow new(size(Element))
                                                      63
                                                                         e->data = newData;
                    E \rightarrow data \leftarrow d
                                                      64
                                                                         e->next = NULL;
                    E \rightarrow next \leftarrow NULL
                                                      65
                                                      66
                                                                          //Update tail pointer
                                                                         ls->tail->next = e;
                                                      67
                    ls \rightarrow tail \rightarrow next \leftarrow E
                                                      68
                                                                         ls->tail = e;
                    ls→tail ← E
                                                      69
                                                                         ls->n = ls->n + 1;
                    ls \rightarrow n \leftarrow ls \rightarrow n + 1
                                                      70
          end if
                                                      71
End procedure
```

How it works ...?

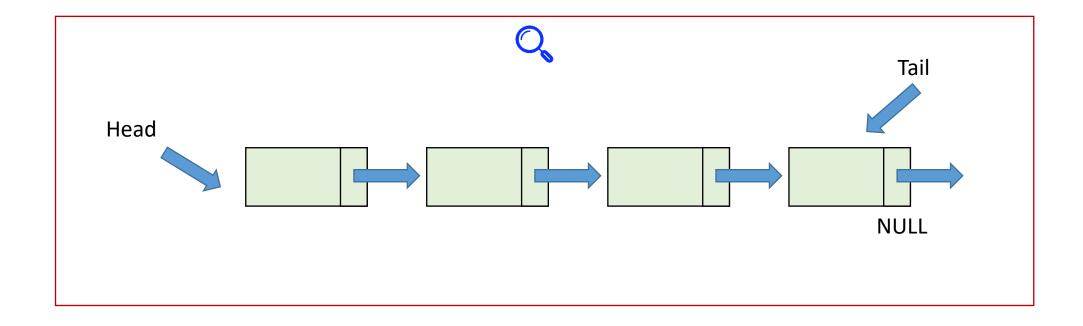
How to search data in linked list

❖ Searching for data





☐ Search for data in list



Search Q

end if

End procedure

☐ Search for data in list

```
113
                                                      void search(List *ls, int x) {
Procedure search(*ls: List, d: data_type)
                                              114
                                                            Element *tmp;
     var *tmp: Element
                                              115
                                                            tmp=ls->head;
     var counter: integer
                                              116
                                                            int counter=0;
     counter \leftarrow 0
                                                            while(tmp!=NULL) {
                                              117
                                              118
                                                                 if(tmp->data == x) {
     tmp \leftarrow ls \rightarrow head
                                              119
                                                                      counter = counter + 1;
     while(tmp != NULL) do
                                              120
          if(tmp\rightarrowdata == d) then
                                              121
                                                                 tmp=tmp->next;
                                              122
               counter \leftarrow counter + 1
                                              123
                                                            if (counter==0) {
          end if
                                                                 cout << "No data found \n";
                                              124
          tmp \leftarrow tmp \rightarrow next
                                              125
                                                            }else{
     end while
                                                                 cout<<"Found data "<<counter<<" times\n";</pre>
                                              126
                                              127
     if(counter==0) do
                                              128
          write("Not found")
     else
          write("Found ", counter, " times")
```

How it works ...?



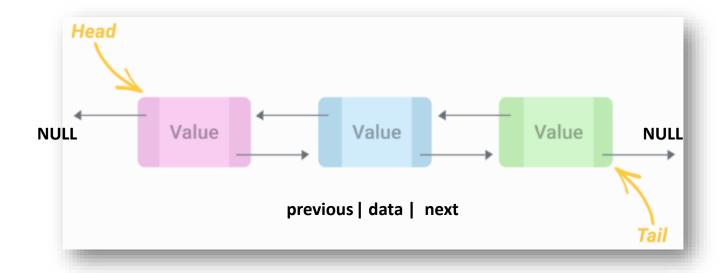
Q&A

Search

- ☐ Search for some data
- Each element is traversed till the data in the element matched with the required value

```
void search(int x){
   Element *tmp;
   tmp=head;
   while(tmp!=NULL){
       if(tmp->data == x){
           cout<<"Found: "<<tmp->data;
           break;
       tmp=tmp->next;
```

Double Linked List (DLL)

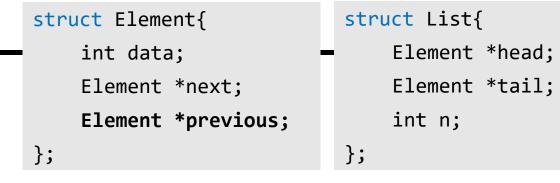


Double linked list

Each element contains

✓ Data

- ✓ A link to its next element (successor)
- ✓ A link to its previous element (predecessor)
 - They are created as a pointer

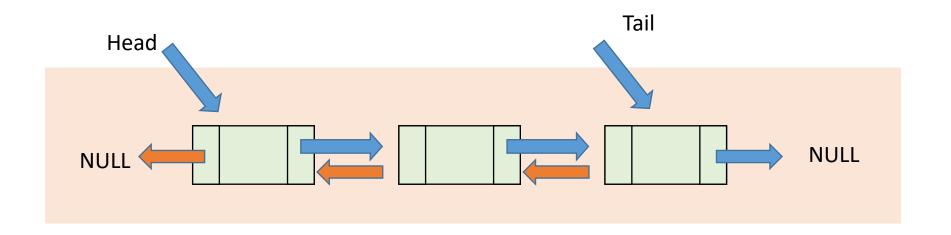


Element

Var data: integer Var *next: Element Var *previous: Element

List

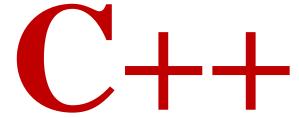
Var *head: Element Var *tail: Element Var n: integer





Implementation:

Double Linked List (DLL)



DLL

```
32
                                                       //Create new element
                                              33
                                                       Element *e;
                                                                                     149
                                                                                           \equivint main(){
                                              34
                                                       e = new Element();
                                                                                     150
      #include<iostream>
                                               35
                                                       e->data = newData;
                                                                                     151
                                                                                                 List *L;
     using namespace std;
                                              36
                                                       e->previous = NULL;
                                                                                     152
                                                                                                 L = createList();
      struct Element {
                                              37
                                                       e->next = ls->head;
                                                                                     153
                                               38
          int data;
                                               39
                                                       //Update tail
                                                                                     154
                                                                                                 insert begin(L, 3);
 5
          Element *next;
                                                       if(ls->n == 0){
                                               40
                                                                                     155
                                                                                                 insert begin(L, 1);
 6
          Element *previous;
                                              41
                                                           ls->tail = e;
                                                                                                 insert begin(L, 0);
                                                                                     156
                                              42
      typedef struct Element Element;
                                                                                     157
                                                                                                 insert begin (L, -4);
                                              43
 8
                                                                                     158
                                              44
                                                       if(ls->n != 0){
 9
      struct List{
                                              45
                                                           ls->head->previous = e;
                                                                                     159
                                                                                                 displayList(L);
10
          int n; //number of elements
                                              46
                                                                                     160
                                                                                                 displayList2(L);
                                              47
                                                       ls->head = e;
11
          Element *head;
                                                                                     161
                                              48
                                                       ls->n = ls->n + 1;
12
          Element *tail;
                                              49
13
14
      typedef struct List List;
                                              51
                                                   void displayList(List *ls) {
                                              52
                                                        Element *tmp;
     //A function to create an empty list
17
                                              53
18
    -List* createList() {
19
                                              54
                                                        tmp = ls->head;
          List *ls;
                                                                                          void displayList2(List *ls) {
                                              55
                                                        while (tmp!=NULL) {
20
                                                                                      63
                                                                                              Element *tmp;
                                                             cout<<tmp->data<<" ";</pre>
21
          ls = new List(); //allocate memor
                                              56
                                                                                      64
22
          //ls.n = 0; //error
                                              57
                                                             tmp = tmp->next;
                                                                                      65
                                                                                              tmp = ls -> tail;
23
                                                                                      66
          ls->n = 0;
                                                                                              while (tmp!=NULL) {
                                              58
                                                                                      67
                                                                                                  cout<<tmp->data<<" ";</pre>
24
          ls->head = NULL;
                                              59
                                                        cout << endl;
                                                                                      68
                                                                                                  tmp = tmp->previous;
25
          ls->tail = NULL;
                                              60
                                                                                      69
26
                                                                                              cout<<endl:
                                                                                      70
27
          return ls;
                                                                                      71
28
```

void insert begin(List *ls, int newData){

Q and A

Doubly Linked List

☐ Creating a list

```
#include<iostream>
using namespace std;
struct Element{
    int data;
    Element *next;
    Element *previous;
};
struct List{
    Element *head;
    Element *tail;
    int n;
```

- 1. Create data structure, 2. Create a list
- 3. Initialize an empty list

```
int main(){
     List *1;
    l = new List;
    1->n = 0;
     Element *e1,*e2,*e3;
     e1=new Element;
     e1->data = 1;
     e1->next = NULL;
     e1->previous = NULL;
    1->head = e1;
    1->tail = e1;
    1->n = 1->n + 1;
     e2=new Element;
     e2 \rightarrow data = 2;
     e2->next = NULL;
    1->tail->next = e2;
     e2->previous = 1->tail;
    1->tail = e2;
    1->n = 1->n + 1;
```

```
4., 5., and 6. Add elements e1, e2, e3 to the end of the list
```

```
e3=new Element;
e3 \rightarrow data = 3;
e3->next = NULL;
1->tail->next = e3;
e3->previous = 1->tail;
1 \rightarrow tail = e3;
1->n = 1->n + 1;
Element *t;
t = 1->head;
while(t != NULL){
   cout<<t->data<<" ";
   t = t->next;
Element *t2;
t2 = 1->tail;
while(t2 != NULL){
   cout<<t2->data<<" ";
   t2 = t2->previous;
```

- 7. Display data in list from head (forward)
- 8. Display data in list from tail (backward)

Exercises

- 1. Create a singly linked list that can store integer numbers. Then perform these operations below
 - a. Create two data structure (Element and List) then create an empty singly linked list
 - b. Add the number 7 to the end of the list
 - c. Add the number 4 to the end of the list
 - d. Add 1 to the beginning of the list
 - e. Remove the first element of the list
 - f. Add 0 the beginning of the list
 - g. Display all numbers in the list
- 2. Create a doubly linked list that stores the English alphabet (A-Z). Then display the list.

SLL recall

return ls;

2728

```
31
                                                       //Create new element
                                             32
                                                       Element *e;
                                             33
                                                       e = new Element();
     #include<iostream>
                                             34
                                                       e->data = newData;
     using namespace std;
                                             35
     struct Element{
                                             36
                                                       //Update pointer, head, tail
 4
          int data;
                                             37
                                                       e->next = ls->head:
 5
          Element *next;
                                             38
                                                       ls->head = e;
                                                                                            \equivint main(){
 6
                                             39
                                                       if(ls->n == 0){
                                                                                       58
                                             40
                                                           ls->tail = e;
     typedef struct Element Element;
                                                                                       59
                                                                                                 List *L;
                                             41
 8
                                                                                       60
                                                                                                 L = createList();
                                             42
                                                       1s->n = 1s->n + 1;
 9
     struct List{
                                                                                       61
                                             43
                                                                                       62
                                                                                                 insert begin(L, 3);
10
          int n; //number of elements
                                             44
                                                                                       63
                                                                                                 insert begin(L, 2);
11
          Element *head;
                                             45
                                                   void displayList(List *ls) {
                                                                                                 insert begin(L, 5);
                                                                                       64
12
          Element *tail;
                                             46
                                                       Element *tmp; //temporary var:
                                                                                       65
                                                                                                 displayList(L);
13
                                             47
                                                                                       66
                                                                                                 displayList(L);
14
     typedef struct List List;
                                             48
                                                       tmp = ls->head;
                                                                                                 displayList(L);
                                                                                       67
                                             49
                                                       while(tmp!=NULL) {
                                                                                       68
                                                                                                 cout<<L->n<<endl;
17
     //A function to create an empty list
                                             50
                                                           cout<<tmp->data<<" ";</pre>
                                                                                       69
18
    —List* createList() {
                                             51
                                                           tmp = tmp->next;
19
         List *ls;
                                             52
20
                                             53
                                                       cout << endl;
21
         ls = new List(); //allocate memor 54
22
         //ls.n = 0; //error
23
         ls->n = 0;
         ls->head = NULL;
24
25
         ls->tail = NULL;
26
```

void insert begin(List *ls, int newData) {

30

Q and A

- 1. Create a singly linked list that can store integer numbers. Then
 - a. Add the number 7 to the end of the list
 - b. Add the number 4 to the end of the list
 - c. Add the number 4 to the end of the list
 - d. Display the list
 - e. Delete the first element
 - f. Display the list
- 2. Create a singly linked list that can store names of students. Then
 - a. Add a student named "Jack" to the beginning of the list
 - b. Add a student named "Rose" to the beginning of the list
 - c. Add a student named "Sok" to end of the list
 - d. Display all students' names in the list
 - e. Delete the last element
 - f. Display all students' names in the list
- 3. Create a singly linked list that stores the English alphabet (A-Z). Then display the list.

☐ Write a C++ program to

- 4. Create a singly linked list that can store integer numbers. Then initialize the list with these values [1, 2, 3, 5, 0, -1]. Write a program to
 - a. Create a function to add a number entered by a user to the end of the list
 - b. Create a function to add a number entered by a user to the beginning of the list
 - c. Create a function to delete the number at the beginning of the list
 - d. Create a function to delete the number at the beginning of the list
 - e. Create a function to check whether the list contains a number. The function return *true* when the list contains that number. Return *false* otherwise.

Do ex1 again using above functions.

- 5. Get a positive integer n input by a user. Then read n numbers from the input and build a singly linked list such that the first input number is the 1st element of the list, the second input number is the 2nd element of the list, so on and so forth.
- 6. Create a singly linked list for storing information of students. Each student has id, name, sex and average score. Then write a program to
 - a. Create a function to ask for information (id, name, sex, average score) of a student then add her/him to the end of the list. The program does not add the student to the list when the student with the same id is already exist in the list.
 - b. Create a function to display information of all students in the list

Assignment

- -Teamwork
- -How to score: individual and team score
- -Substitute midterm exam
- -Assigned date: 10th May 2019
- -Deadline: 24th May 2019 (2 weeks)
- -Present your work: 29th May 2019

- 1. Create a singly linked list that can store integer numbers. Then
 - a. Add the number 7 to the end of the list
 - b. Add the number 4 to the end of the list
 - c. Add the number 4 to the end of the list
 - d. Display the list
 - e. Delete the first element
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☐ Write a C++ program to

7. Do ex1-6 with doubly linked list instead.

Q and A