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# CHE 1411L Group 6

## Project - Equation of State

### Question

Compute and plot the compressibility factor ( $z$ ) versus pressure ( $x$ ) for the (1) Van der Waal's (2) Redlich-Kwong and (3) Peng-Robinson equations of state.

% Compressibility Factor,  $Z = Pv/RT$ ; where  $v$  is the specific volume ( $V/v$ ).

% Data for n-Butane:

```
T = 500;           % Temperature in K
Tc = 425.2;        % Critical temperature in K
Pc = 37.5;         % Critical pressure in atm
R = 0.08206;       % Gas constant L*atm/mol*K
P = 1.31;          % Pressure in atm
```

% Equations of State:

% Van der Waal:

```
% (P)*(v^3) - (P*b + R*T)*(v^2) + (a)*v - a*b = 0
% a = 0.42188*((R^2)*(Tc^2))/(Pc)
% b = 0.125*((R*Tc)/Pc)
z_vdw = vanderwaal(T,Tc,Pc,R,P);
```

% Redlich-Kwong:

```
% (P)*v^3 - (R*T)*v^2 + (a - P*(b^2) - R*T*b)*v - a*b = 0
% a = 0.42748*((R^2)*(Tc^2))/(Pc)*alpha
% b = 0.08664*((R*Tc)/Pc)
% alpha = (1/(Tr^0.5))
% Tr = T/Tc
z_rk = redlichkwong(T,Tc,Pc,R,P);
```

% Peng-Robinson:

```
% (P)*(v^3) + (b*P - R*T)*(v^2) + (a - 3*P*(b^2) - 2*R*T*b)*v + (P*(b^3) +
% R*T*(b^2) - a*b) = 0
% a = 0.45724*((R^2)*(Tc^2))/(Pc)*alpha
% b = 0.07780*((R*Tc)/Pc)
% alpha = [1 + m*(1 - (Tr^0.5))]^2
% Tr = T/Tc
% m = 0.37464 + 1.54226*w - 0.26992*(w^2)
% w = 0.193
z_pr = pengrobinson(T,Tc,Pc,R,P);
```

% HINTS:

```
% 1. Make P, Pc, T, Tc, and R global variables
% 2. Write three functions. One for each of the equations.
% 3. Write a script file that calls the functions using a root finding
% method to determine
% 4. Use the root to calculate the compressibility factor
```

```
% 5. Plot the compressibility factor verses pressure
```

```
% Note:  
% Show all three graphs in the same plot window. Properly label the axis  
% etc.
```

```
z_vdw =
```

```
    0.9930
```

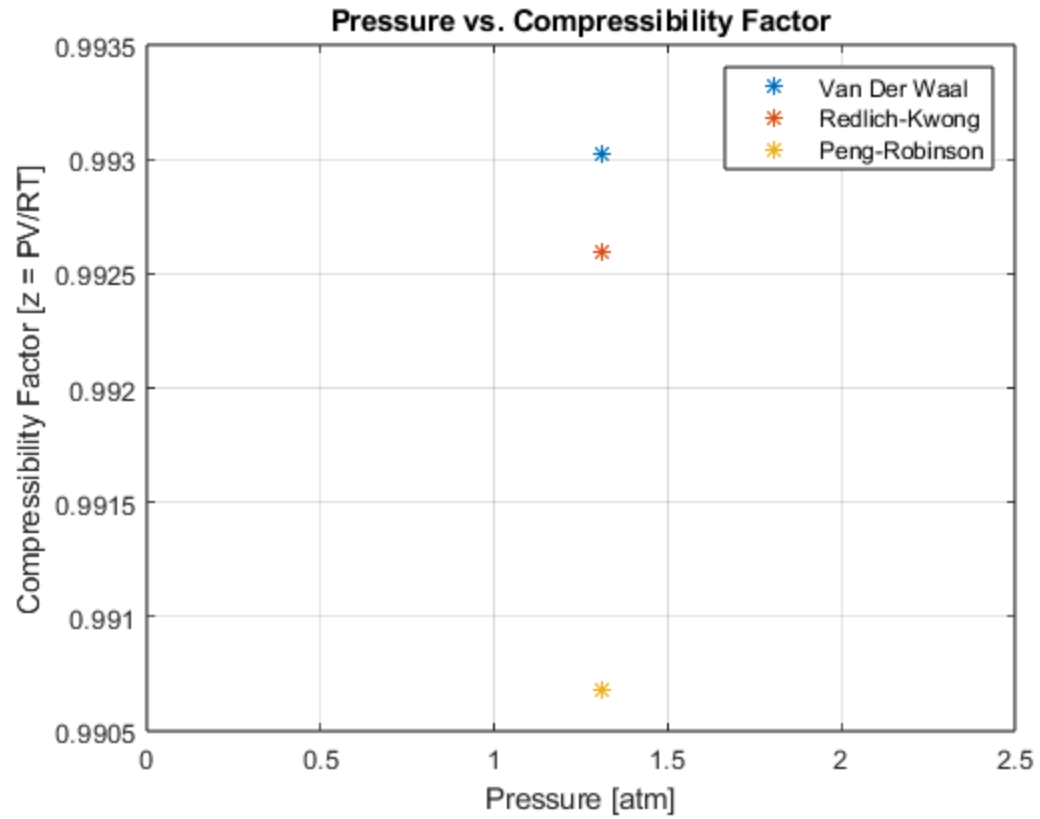
```
z_rk =
```

```
    0.9926
```

```
z_pr =
```

```
    0.9907
```

```
plot(P,z_vdw,'*')  
grid on  
hold on  
plot(P,z_rk,'*')  
hold on  
plot(P,z_pr,'*')  
title('Pressure vs. Compressibility Factor')  
xlabel('Pressure [atm]')  
ylabel('Compressibility Factor [z = PV/RT]')  
legend('Van Der Waal','Redlich-Kwong','Peng-Robinson')  
hold off
```



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```
function z_vdw = vanderwaal(T, Tc, Pc, R, P)

a = 0.42188*((R^2)*(Tc^2))/(Pc);
b = 0.125*((R*Tc)/Pc);

root = @(v) (P)*(v^3) - (P*b + R*T)*(v^2) + (a)*v - a*b;
spec_vol = fzero(root,1);
z_vdw = (P.*spec_vol)./(R*T)
```

Not enough input arguments.

Error in vanderwaal (line 3)  
a = 0.42188\*((R^2)\*(Tc^2))/(Pc);

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---

```
function z_rk = redlichkwong(T, Tc, Pc, R, P)
```

```
Tr = T/Tc;
```

```
alpha = (1/(Tr^0.5));
```

```
a = 0.42748*((R^2)*(Tc^2))/(Pc))*alpha;
```

```
b = 0.08664*((R*Tc)/Pc);
```

```
root = @(v) (P)*v^3 - (R*T)*v^2 + (a - P*(b^2) - R*T*b)*v - a*b;
```

```
spec_vol = fzero(root,1);
```

```
z_rk = (P.*spec_vol)./(R*T)
```

```
Not enough input arguments.
```

```
Error in redlichkwong (line 3)
```

```
Tr = T/Tc;
```

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---

```
function z_pr = pengrobinson(T, Tc, Pc, R, P)
```

```
w = 0.193;
```

```
m = 0.37464 + 1.54226*w - 0.26992*(w^2);
```

```
Tr = T/Tc;
```

```
alpha = [1 + m*(1 - (Tr^0.5))^2];
```

```
a = 0.45724*((R^2)*(Tc^2))/(Pc))*alpha;
```

```
b = 0.07780*((R*Tc)/Pc);
```

```
root = @(v) (P)*(v^3) + (b*P - R*T)*(v^2) + (a - 3*P*(b^2) - 2*R*T*b)*v +  
    (P*(b^3) + R*T*(b^2) - a*b);
```

```
spec_vol = fzero(root,1);
```

```
z_pr = (P.*spec_vol)./(R*T)
```

```
Not enough input arguments.
```

```
Error in pengrobinson (line 5)
```

```
Tr = T/Tc;
```

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