

# main

December 10, 2019

## 0.1 Please set below variable running to 1 if you run this notebook.

Its purpose is to ensure that interactive functions will display their outputs if you open the notebook on github (without downloading). If you run the notebook without setting running to 1 all interactive functions will display twice.

```
In [129]: running = 0
```

field is a slice of response table you want to analyse  
feature is a single column name of responders table  
group is a slice of people, i.e. men/female/left-handed/right-handed

## 1 Table of content

1. Data preparation
  2. Searching for correlations
    - Principal component analysis for fields **(interactive)**
    - Correlations with a chosen feature **(interactive)**
    - Searching for interesting correlations
  3. Clustering
    - Hierarchical clustering for a chosen field **(interactive)**
    - K-means clustering for a chosen field **(interactive)**
    - T-SNE **(interactive)**
    - Finding outliers **(interactive)**
  4. Other
    - BMI distribution within genders
    - Feature's distribution between groups **(interactive)**
- 

```
In [130]: %matplotlib inline
import matplotlib.pyplot as plt
import matplotlib
import pandas as pd
import numpy as np
import scipy.cluster.hierarchy as sch
```

```

import ipywidgets as widgets
from sklearn.cluster import KMeans
from sklearn.preprocessing import scale, StandardScaler
from pylab import rcParams
from numpy.random import RandomState
from IPython.display import display
from ipywidgets import interact, interactive, fixed, interact_manual, Dropdown, IntSlider
from sklearn.manifold import TSNE

```

Define two functions for cluster analysis visualisation

```

In [131]: from itertools import cycle, islice
          from pandas.plotting import parallel_coordinates

```

```

def pd_centers(featuresUsed, centers):

    colNames = list(featuresUsed)
    colNames.append('prediction')

    # Zip with a column called 'prediction' (index)
    Z = [np.append(A, index) for index, A in enumerate(centers)]

    # Convert to pandas for plotting
    P = pd.DataFrame(Z, columns=colNames)
    P['prediction'] = P['prediction'].astype(int)
    return P

def parallel_plot(data, size):

    my_colors = list(islice(cycle(['b', 'r', 'g', 'y', 'k']), None, len(data)))
    plt.figure(figsize=size).gca().axes.set_ylim([1,5])
    parallel_coordinates(data, 'prediction', color = my_colors, marker='o')
    plt.xticks(rotation=75)
    plt.ylabel('centers of clusters')

```

## 1.1 1. Data preparation

```

In [132]: responses = pd.read_csv("responses.csv")

```

```

responses.at[676, 'Height'] += 100 # repair a value

```

Divide dataset onto several parts

```

In [133]: music = responses.loc[:, 'Dance': 'Opera']
          movies = responses.loc[:, 'Horror': 'Action']
          hobbies = responses.loc[:, 'History': 'Pets']
          phobias = responses.loc[:, 'Flying': 'Fear of public speaking']
          personality = responses.loc[:, 'Daily events': 'Spending on healthy eating'].select_dtypes(include=[object])

```

Create a path to relate to variables using their names

```
In [134]: field_name = {'music':music, 'movies':movies, 'hobbies':hobbies, 'phobias':phobias,
```

### 1.1.1 Define two new features: braveness and BMI

Negation of 'breaveness' is a scaled sum of individual's ratings of all phobias.

*Note: higher value = more brave.*

'BMI' stands for 'Body Mass Index'

```
In [135]: braveness = (50-phobias.sum(axis=1)) / 10 + 1
bmi = round(responses['Weight'] / (responses['Height'] / 100)**2, 2)
```

```
responses_ = responses.copy()
responses_.insert(0, "Braveness", braveness.to_list(), True)
responses_.insert(0, "BMI", bmi.to_list(), True)
```

```
# braveness.plot.hist(bins=40, alpha=0.5, density = True)
```

Filter responses leaving only numerical values

```
In [136]: responses_int = responses_.select_dtypes(include=['int','float'])
print(responses_.shape, responses_int.shape)
```

```
(1010, 152) (1010, 141)
```

## 1.2 2. Search for correlations

### 1.2.1 2.1. Principal Component analysis (PCA) for fields

For a chosen field analyse impact of number of most relevant components took into consideration for quality of representing data.

```
In [137]: @interact(field = ['personality','phobias','music','movies','hobbies'], noOfComponents:
def PCA(field, noOfComponents):
    field = field_name[field]

    df = field.dropna()
    df_np = np.array(df)

    # Calculate covarriance matrix for all features (columns) in TYPE

    Sigma = np.cov(df_np, rowvar=0, bias=1)

    # Calculate eigenvectors of covarriance matrix

    eigenvalues, eigenvectors = np.linalg.eigh(Sigma)
```

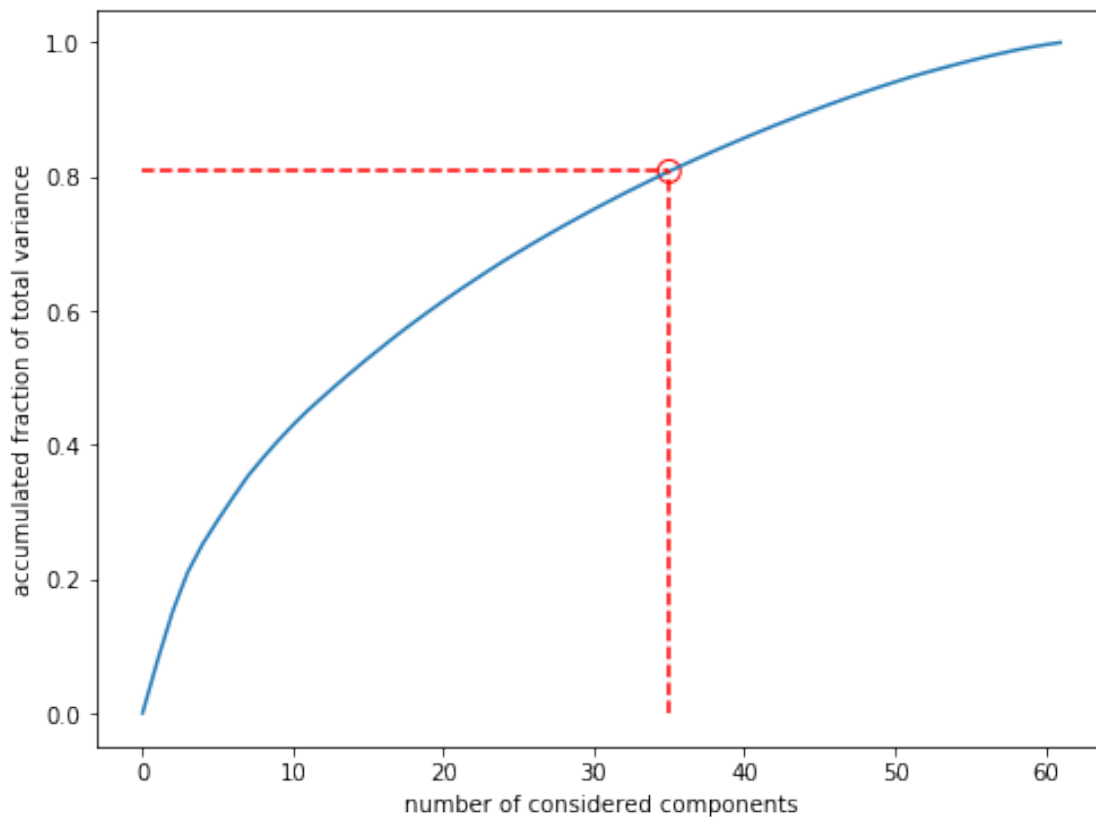
```

plt.figure(figsize=(8,6))
plt.plot([0]+[sum(eigenvalues[-i:]) / sum(eigenvalues) for i in range(1, field.s
plt.xlabel('number of considered components')
plt.ylabel('accumulated fraction of total variance')

x = noOfComponents
y = (lambda i: sum(eigenvalues[-i:]) / sum(eigenvalues))(noOfComponents)
plt.scatter([x], [y], s=100, edgecolors='r', facecolors = 'none')
plt.plot([x,x], [0,y], c='r', linestyle='dashed')
plt.plot([0,x], [y,y], c='r', linestyle='dashed')
plt.show()
print('Amount of total variance covered by {} most impactful components: {}'.form

if running == 0:
    PCA('personality', 35)

```



Amount of total variance covered by 35 most impactful components: 0.8079

**Comment 1:**

For field = personality 5 most impactful personality features (components) occupy only 29% of total variance, what means that features are **not very correlated (rather independent)**. To cover up 80% of total variance it's necessarily to take 35 most impactful features out of total 61.

### 1.2.2 2.2. Correlations with a chosen feature, restricted to a specified group

```
In [138]: @interact(feature = IntSlider(106,0,139,1), group = ['all', 'male', 'female', 'right
def Correlate_with(feature, group):

    cols = responses_int.columns.to_list()
    feature = cols[feature]

    # Filter responses according to `group`

    if group == 'all':
        responses_int_filtered = responses_int
    if group in {'male', 'female'}:
        responses_int_filtered = responses_int[responses['Gender'] == group]
    if group in {'left handed', 'right handed'}:
        responses_int_filtered = responses_int[responses['Left - right handed'] == g

    # Select 1 columns from correlation's table for specified `group`

    correlations = [responses_int_filtered[feature].corr(responses_int_filtered[f]) :

    # Filter, leaving only interesting correlations

    df = pd.DataFrame(correlations, columns = ['Correlations'])
    df = df[abs(df['Correlations']) > 0.25]

    # Make pretty visialisation for selected column

    corr_features = [cols[f] for f in df.index]
    corr = responses_int_filtered[corr_features].corr().loc[:,feature]

    print("Features correlated with '{}':".format(feature))
    corr_ = {'Feature\'s name':corr.index, 'Coefficient':round(corr,3).to_list()}
    corr_ = pd.DataFrame(corr_, index = df.index)
    corr_ = corr_[corr_['Feature\'s name'] != feature]
    display(corr_)

    # Visualise the plot

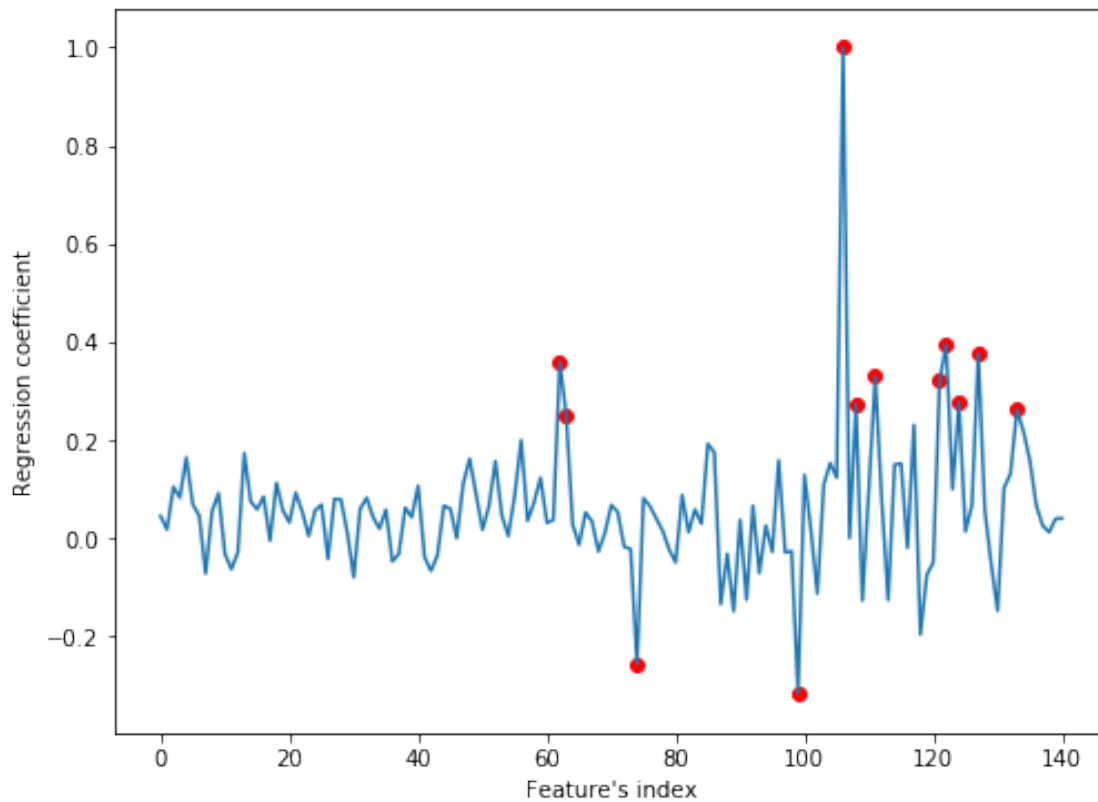
    plt.figure(figsize=(8,6))
    plt.plot(correlations)
    plt.xlabel('Feature\'s index')
    plt.ylabel('Regression coefficient')
    plt.scatter(df.index, np.array(corr), c='r')
```

```
plt.show()
print("Red dots correspond to features correlated with '{}'.format(feature))

if running == 0:
    Correlate_with(106, 'all')
```

Features correlated with 'Number of friends':

	Feature's name	Coefficient
62	Fun with friends	0.359
63	Adrenaline sports	0.250
74	Fear of public speaking	-0.257
99	Loneliness	-0.317
108	New environment	0.273
111	Socializing	0.329
121	Happiness in life	0.321
122	Energy levels	0.394
124	Personality	0.276
127	Interests or hobbies	0.376
133	Entertainment spending	0.262



Red dots correspond to features correlated with 'Number of friends'

### 1.2.3 2.2. Search for interesting correlations

Consider men and women independently.

Find what features have most correlations with any of 'personality' features. But focus on features which lead to correlations with similar Pearson's value for **both men and women treated separately**. This approach is crucial, because i.e. if men are more likely to be interested in cars than women and at the same time, men are statistically heigher than women, then without considering gender independence we would get a correlation between cars and height, which is a nonsense.

```
In [139]: # Index_1 stands for men, index_2 stands for women
```

```
for feature in personality.columns:

    cols = responses_int.columns.to_list()

    # Select 1 column from correlation's table for specified `group`, per group

    responses_male = responses[responses['Gender'] == 'male']
    responses_female = responses[responses['Gender'] == 'female']
    correlations_1 = [responses_male[feature].corr(responses_male[f]) for f in cols]
    correlations_2 = [responses_female[feature].corr(responses_female[f]) for f in cols]

    # Filter, leaving only interesting correlations

    df_1 = pd.DataFrame(correlations_1, columns = ['Correlations'])
    df_1 = df_1[abs(df_1['Correlations']) > 0.25]
    df_2 = pd.DataFrame(correlations_2, columns = ['Correlations'])
    df_2 = df_2[abs(df_2['Correlations']) > 0.25]

    # Catch feature's index value

    features_index = df_1[df_1['Correlations'] > 0.99].index[0]

    # Preparations for pretty visualisation

    corr_features_1 = [cols[f] for f in df_1.index]
    corr_features_2 = [cols[f] for f in df_2.index]

    corr_1 = responses_male[corr_features_1].corr().loc[:,feature].drop([feature])
    corr_2 = responses_female[corr_features_2].corr().loc[:,feature].drop([feature])

    # Find set of features that lead to correlations in both genders
    set_ = set(corr_1.index) & set(corr_2.index)

    # If at least 5 distinct correlation are found
```

```

if len(corr_1) > 0 and len(set_) > 5:

    corr_ = {'Correlated feature\'s name':list(set_)
             , 'Coefficient for Men':round(corr_1,3).loc[set_].tolist()
             , 'Coefficient for Women':round(corr_2,3).loc[set_].tolist()}

    corr_ = pd.DataFrame(corr_)
    corr_ = corr_.style.set_caption("Feature\'s name: {}".format(feature)).hide_
    print("Feature\'s name ({}): {}".format(features_index, feature))
    display(corr_)

```

Feature's name (106): Number of friends:

<pandas.io.formats.style.Styler at 0x7f52150157b8>

Feature's name (122): Energy levels:

<pandas.io.formats.style.Styler at 0x7f52142983c8>

Feature's name (134): Spending on looks:

<pandas.io.formats.style.Styler at 0x7f5214280940>

## 1.3 3. Clustering

### 1.3.1 3.1. Hierarchical clustering for a chosen field

```

In [140]: @interact(field = ['phobias','music','movies','hobbies','personality'])
def Hierarchical_cluster(field):
    field = field_name[field]

    df_select = field.copy(deep=True).dropna()
    x = df_select.to_numpy().T

    # Adjust figure size to accommodate the full tree

    rcParams['figure.figsize'] = 5, 10

    # Do a hierarchical clustering using Ward's method

    z = sch.linkage(x, method='ward')

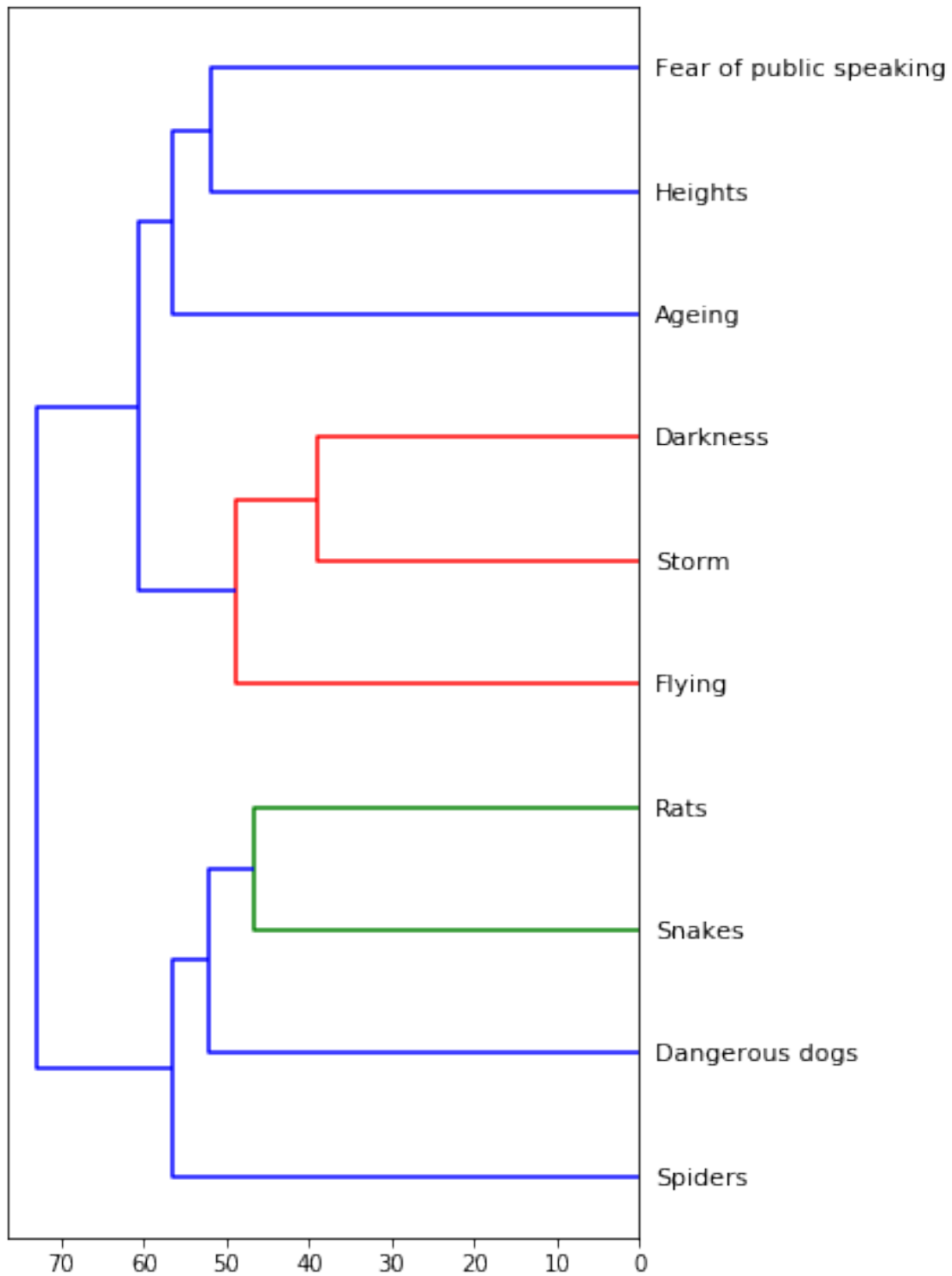
    # Display dendrogram

```



```
names = df_select.columns.tolist()
info = sch.dendrogram(z, orientation='left', labels=names, leaf_font_size=11)
plt.show()

if running == 0:
    Hierarchical_cluster('phobias')
```



**Comment 1:** phobias seem to have 3 distinct types: - animals (Rats, Snakes, Dangerous dogs, Spiders) - nature (Darkness, Storm, Flying) - social (Fear of public speaking, Heights, Ageing)

**Comment 2:** music clusters in 5 distinct types: - **old music:** rock n roll, jazz, alternative - **metal-**

like music: rock<sup>^</sup>, punk, metal - **instrumental music**: opera, classical, country, folk - **popular music**: latino, musical, pop, dance - **rap-like music**: reggae, hiphop, techno  
<sup>^</sup> although rock was assigned to 'yellow label', it's not too far from 'magenta label', which seems more logical

### 1.3.2 3.2. K-means clustering for a chosen field

```
In [141]: @interact(field = ['phobias', 'music', 'movies', 'hobbies', 'personality'], noOfClusters
              randomstate = IntSlider(745, 0, 10000, 10))
def K_means_cluster(field, noOfClusters, randomstate):

    field = field_name[field]
    df_select = field.copy(deep=True).dropna()

    # Perform scaling on the dataframe containing the field's features

    scaler_x = StandardScaler()
    data = scaler_x.fit_transform(df_select)

    # Perform K-Means

    model = KMeans(init='k-means++', n_clusters=noOfClusters, n_init=20, random_state=randomstate)

    print("Total sum of squares of distances:", round(model.inertia_))
    print(90*'_')
    print("\nCount of people in each cluster")
    print(90*'_')
    print(pd.value_counts(model.labels_, sort=False))

    # Display plot showing centers of clusters

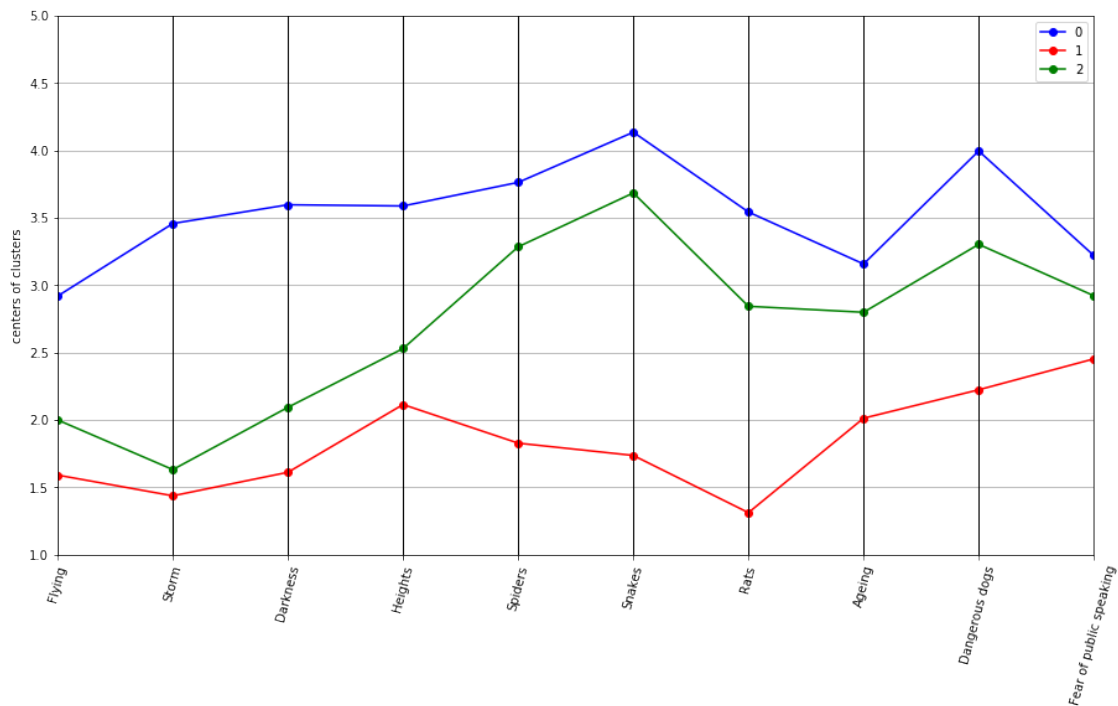
    P = pd_centers(featuresUsed=field.columns.to_list(),
                    centers=scaler_x.inverse_transform(model.cluster_centers_))
    parallel_plot(P, (15, 8))
    plt.show()

    if running == 0:
        K_means_cluster('phobias', 3, 745)
```

Total sum of squares of distances: 7088.0

Count of people in each cluster

```
-----
0    223
1    384
2    383
dtype: int64
```



#### Comment 1:

For phobias with 3 clusters people seem to divide in following types:

- people scared of nothing.
- people scared of various animals.
- people scared of everything.

Using 4 clusters reveals an additional group, without changing centers of previous 3 clusters:

- people scared of everything except of animals.

Using 5 clusters modifies some of previous cluster's centers.

### 1.3.3 3.3. t-SNE

Visualise data of specified field by reducing its dimensions to 2D space, using t-distributed stochastic neighbor embedding.

```
In [142]: @interact(field = ['phobias','music','movies','hobbies','personality'], noOfClusters
              randomstate = IntSlider(745,0,10000,10))
def T_SNE_cluster(field, noOfClusters, randomstate):

    field = field_name[field]
```

```

df_select = field.copy(deep=True).dropna()

# Compute K-means to get labels

scaler_x = StandardScaler()
data = scaler_x.fit_transform(df_select)
model = KMeans(init='k-means++', n_clusters=noOfClusters,
               n_init=20, random_state=randomstate).fit(data)

a = [0, 1, 2, 3, 4, 5, 6]
b = ['b', 'r', 'g', 'y', 'k', 'm']
dict_ = dict(zip(a,b))
colors = [dict_[i] for i in model.labels_]

# Show result of T-SNE

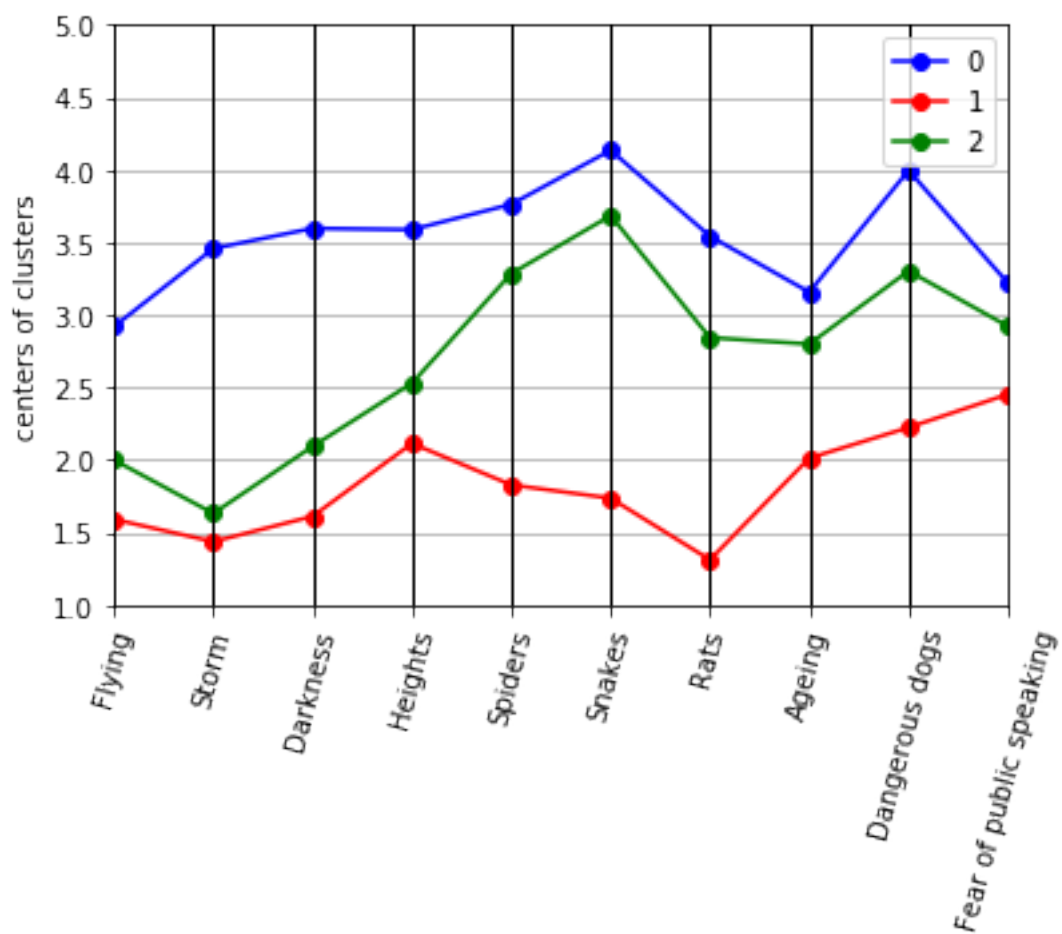
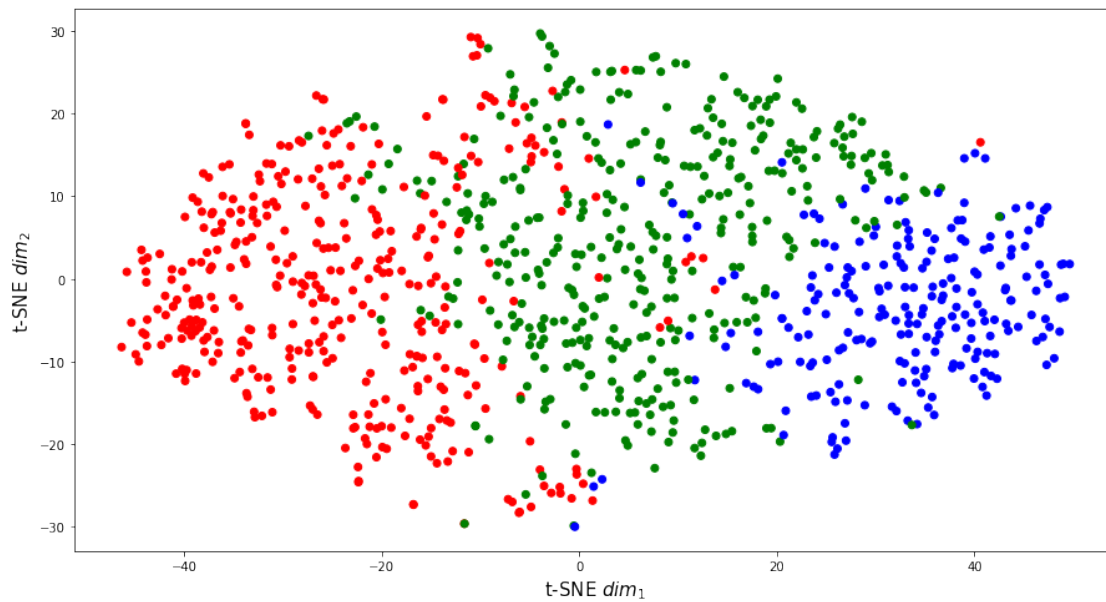
plt.figure(figsize=(15,8))
X_embedded = TSNE(n_components=2, random_state=randomstate).fit_transform(data)
plt.scatter(X_embedded[:,0], X_embedded[:,1], color = colors)
plt.xlabel('t-SNE $dim_1$', size=15)
plt.ylabel('t-SNE $dim_2$', size=15)
plt.show()

# Show result of K-means for labels colors

P = pd_centers(featuresUsed=field.columns.to_list(),
               centers=scaler_x.inverse_transform(model.cluster_centers_))
parallel_plot(P, (6, 4))
plt.show()

if running == 0:
    T_SNE_cluster('phobias', 3, 745)

```



### Comment 1:

For phobias, using coloring from K-means algorithm, we notice that for 3 clusters data is well separated, but for 4 clusters two of the clusters are mixed. This suggests that 3 is truly an appropriate number of clusters.

However, cluster regions are tangential with their boundaries, which means that there exist people whose preferences are on the middle, instead belonging purely to one distinct cluster.

### 1.3.4 3.4. Finding outliers

People who likely cheated by answering randomly.

`allowed_dist` is maximum allowed distance from nearest cluster to not be considered as an outlier

```
In [143]: @interact(field = ['phobias', 'music', 'movies', 'hobbies', 'personality'], noOfClusters
              randomstate = IntSlider(745, 0, 10000, 10), allowed_dist = FloatSlider(value=4
def Find_outliners(field, noOfClusters, randomstate, allowed_dist):

    field = field_name[field]
    df_select = field.copy(deep=True).dropna()

    # Compute K-means

    scaler_x = StandardScaler()
    data = scaler_x.fit_transform(df_select)
    model = KMeans(init='k-means++', n_clusters=noOfClusters,
                    n_init=20, random_state=randomstate).fit(data)

    centers = model.cluster_centers_

    # Plot distance from nearest cluster for all points for which cluster analysis w

    plt.figure(figsize=(8,6))
    x = df_select.index.tolist()
    y = [min([np.linalg.norm(a-b) for a in centers]) for b in data[:]]
    plt.scatter(x,y)
    plt.plot([0,1000], [allowed_dist, allowed_dist], 'red') # Above this line are ou
    plt.xlabel("Number of survey responder")
    plt.ylabel("Distance from nearest cluster")
    plt.show()

    # Find which points are far away from any cluster. Print their indexes and meas

    outliers = []
    for i in range(len(y)):
        if y[i] > allowed_dist:
            outliers.append((x[i], y[i], df_select.index[i]))
```

```

print("Number of people above the red line: {}".format(len(outliners)))
print("Number of survey responder and its distance from nearest cluster (max 10)")
for outlier in outliners[:min(10, len(outliners))]:
    print(outliner[0], "\t", round(outliner[1], 3))

# Gather all informations about found ouliners, being carefull on index (notice

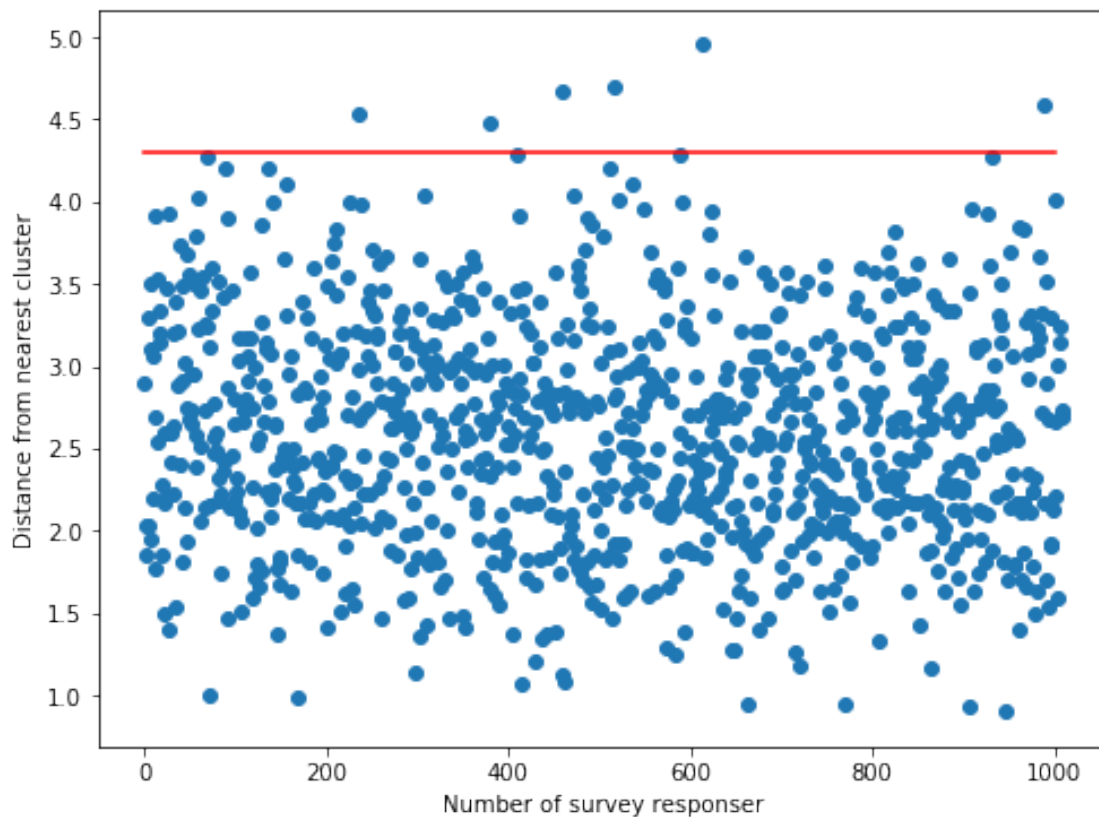
filter_ = np.full(responses.shape[0], False)
for outlier in outliners:
    filter_[outliner[2]] = True
df_ = responses[filter_]

# Select and display only columns including strings

df_cols = set(df_.columns) - set(df_.select_dtypes(include=['int', 'float']).columns)
print( "\nAll non-numeric informations about surveyors detected as outliers (max 10)")
display(df_[df_cols][:min(10, df_.shape[0])])

if running == 0:
    Find_outliners('phobias', 3, 745, 4.3)

```





Number of people above the red line: 6

Number of survey resposner and its distance from nearest cluster (max 10):

236	4.531
378	4.472
458	4.666
516	4.704
614	4.957
989	4.582

All non-numeric informations about surveyors detected as outliers (max 10):

	Alcohol	Only child	House - block of flats	Gender	Village - town \
236	drink a lot	yes	block of flats	female	city
378	drink a lot	no	block of flats	female	city
458	social drinker	no	house/bungalow	female	village
516	never	no	block of flats	male	city
614	social drinker	no	house/bungalow	female	village
989	drink a lot	no	house/bungalow	female	village

	Punctuality	Education	Internet usage \
236	i am often early	secondary school	less than an hour a day
378	i am often running late	secondary school	few hours a day
458	i am often running late	secondary school	few hours a day
516	i am always on time	secondary school	few hours a day
614	i am often early	secondary school	few hours a day
989	i am often early	masters degree	most of the day

	Lying	Smoking	Left - right handed
236	sometimes	tried smoking	right handed
378	sometimes	tried smoking	right handed
458	only to avoid hurting someone	tried smoking	right handed
516	sometimes	tried smoking	right handed
614	sometimes	current smoker	right handed
989	sometimes	former smoker	right handed

#### Comment 1:

Seems like most of the outliers are woman. Possibly, woman tend to be more undecisive than men, not necessary being 'cheaters'.

## 1.4 4. Other

### 1.4.1 4.1. BMI (body mass index) distribution within genders

```
In [144]: plt.figure(figsize=(6,4))
```

```
responses_male = responses_[responses_['Gender'] == 'male']
```

```

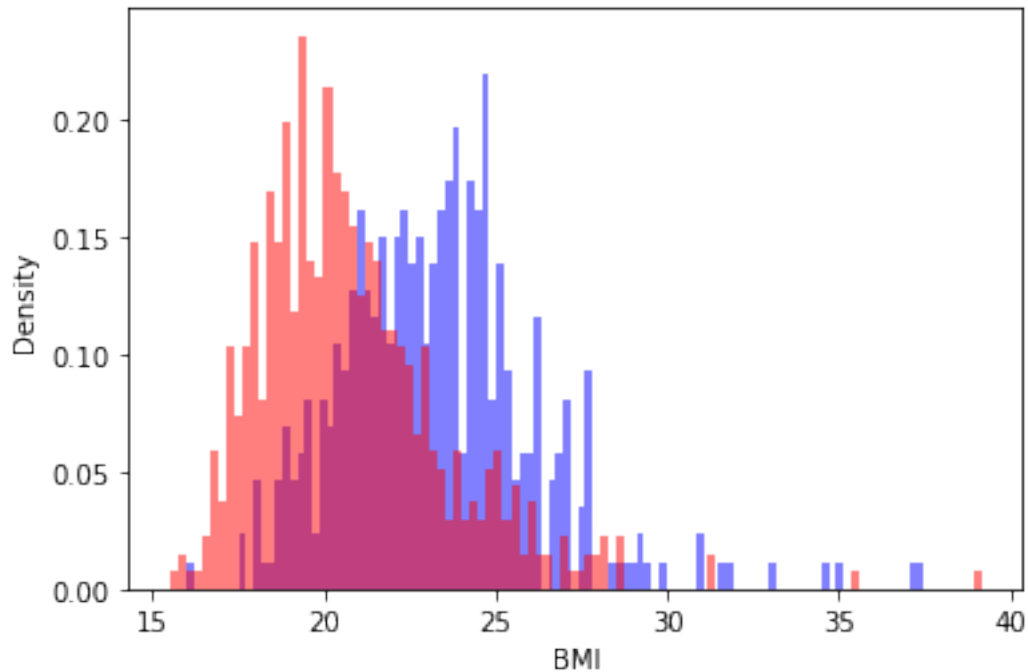
responses_female = responses_[responses_['Gender'] == 'female']

responses_male['BMI'].plot.hist(bins=100, alpha=0.5, color = 'blue', density = True)
responses_female['BMI'].plot.hist(bins=100, alpha=0.5, color = 'red', density = True)

plt.xlabel('BMI')
plt.ylabel('Density')

```

Out[144]: Text(0, 0.5, 'Density')



#### Comment 1:

both genders have gaussian-like distribution of BMI values, however their mean values differ:  
 - women's average BMI is around 20 - men's average BMI is around 24

#### 1.4.2 4.2. Feature's distribution between groups.

```

In [145]: @interact(feature = IntSlider(103,0,139,1), group = ['all', 'male', 'female', 'right']
def Compare(feature, group):

    cols = responses_int.columns.to_list()
    feature = cols[feature]

    # Filter responses according to `group`

    if group == 'all':
        responses_int_filtered = responses_int

```

```

if group in {'male', 'female'}:
    responses_int_filtered = responses_int[responses['Gender'] == group]
if group in {'left handed', 'right handed'}:
    responses_int_filtered = responses_int[responses['Left - right handed'] == group]

# Nan values are not plotted, so disclude them in counting

n = sum(responses_int_filtered[feature] == responses_int_filtered[feature])

print("Fraction distribution for '{}' in group '{}':".format(feature, group))
display(responses_int_filtered[feature].value_counts(normalize=True).sort_index())

plt.figure(figsize=(8,6))
responses_int_filtered[feature].plot.hist(bins=5, alpha=0.5, color='b',
                                           weights = [1./n for i in range(0,n)], r
plt.xlabel('Score')
plt.ylabel('Fraction distribution')
plt.ylim(0,0.4)
plt.show()

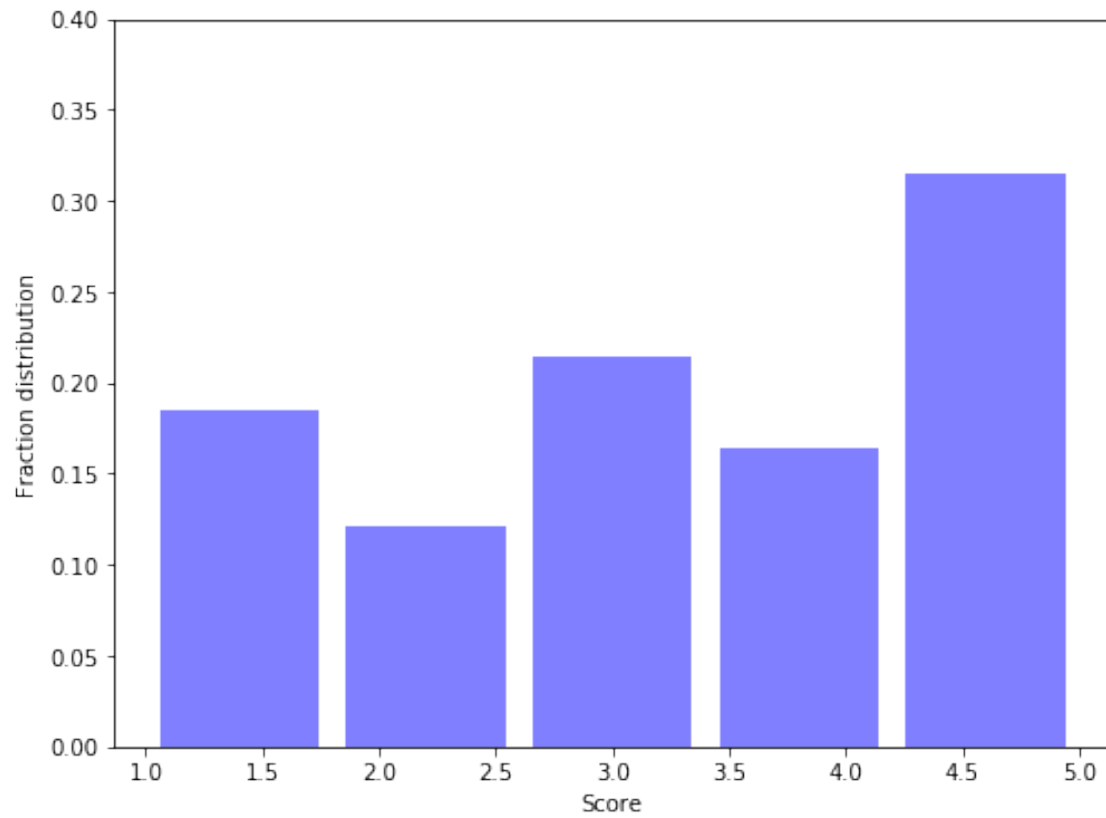
if running == 0:
    Compare(103, 'all')

```

Fraction distribution for 'God' in group 'all':

1.0	0.185516
2.0	0.121032
3.0	0.214286
4.0	0.163690
5.0	0.315476

Name: God, dtype: float64



**Comment 1:**

Woman are more likely to be religious. - 36% of woman and 25% of men are strongly religious (5.0 points in survey). - 15% of woman and 24% of men are atheist-like (1.0 point in survey).